

1.

$$\boxed{1} \quad h_1 = W_h h_0 + W_x X_1$$

$$\hat{y}_1 = W_y h_1$$

$$h_2 = W_h h_1 + W_x X_2$$

$$\hat{y}_2 = W_y h_2$$

$$\hat{y}_2 = W_y h_2 = W_y (W_h h_1 + W_x X_2)$$

$$= W_y W_h h_1 + W_y W_x X_2$$

$$= W_y W_h (W_h h_0 + W_x X_1) + W_y W_x X_2$$

$$= W_y W_h^2 h_0 + W_y W_h W_x X_1 + W_y W_x X_2$$

Since  $h_0 = 1$ ,  $X_1 = 10$ ,  $X_2 = 10$ ,  $y_1 = 5$ ,  $y_2 = 5$   
 &  $W_h = 1$ ,  $W_x = 0.1$ ,  $W_y = 2$

$$\begin{aligned} \hat{y}_2 &= (2)(1)^2(1) + (2)(1)(0.1)(10) + (2)(0.1)(10) \\ &= 2 + 2 + 2 = \boxed{6} \neq \end{aligned}$$

$$\hat{y}_2 = 1 \quad h_0 = 1, \quad x_1 = 10, \quad x_2 = 10$$

$$\hat{y}_1 = 5, \quad y_2 = 5$$

$$\begin{aligned} W_h &= 1 \\ W_x &= 0.1 \\ W_y &= 2 \end{aligned}$$

$$\begin{aligned} \hat{y}_2 &= (2)(1)^2(1) + (2)(1)(0.1)(10) + (2)(0.1)(10) \\ &= 2 + 2 + 2 = \boxed{6} \end{aligned}$$

$$\begin{aligned} 2) \quad L_t &= \sum_i (\hat{y}_i - y_i)^2 \\ &= (\hat{y}_1 - y_1)^2 + (\hat{y}_2 - y_2)^2 \\ &= (2((1)(1) + (0.1)(10)) - 5)^2 + (6 - 5)^2 \\ &= (2(1+1) - 5)^2 + (1)^2 \\ &= (-1)^2 + (1)^2 = \boxed{2} \end{aligned}$$

$$③ L_t = (\hat{y}_1 - y_1)^2 + (\hat{y}_2 - y_2)^2$$

~~$$L_t = (w_y h_1 - y_1)^2 + (w_y w_h^2 h_0 + w_y w_h w_x x_1 + w_y w_x x_2)^2$$~~

$$\frac{\partial L_t}{\partial h_1} = 2 (w_y h_1 - y_1) (w_y)$$

~~$$+ 2 (w_y w_h^2 h_0 + w_y w_h w_x x_1 + w_y w_x x_2)$$~~  
~~$$(0)$$~~

$$= 2 (2h_1 - 5) (2)$$

$$= (4h_1 - 10) (2)$$

$$= 8h_1 - 20$$

$$= 8(2) - 20$$

$$= \textcircled{-4} \#$$

$$\boxed{4} \quad L_t = (\hat{y}_1 - y_1)^2 + (\hat{y}_2 - y_2)^2$$

$$= (w_y w_h - y_1)^2 + (w_y w_h^2 h_0 + w_y w_h w_x x_1 + w_y w_x x_2 - y_2)^2$$

$$\begin{aligned} &= (w_y w_h h_0 + w_y w_x x_1 - y_1)^2 + \\ &\quad (w_y w_h^2 h_0 + w_y w_h w_x x_1 + w_y w_x x_2 - y_2)^2 \end{aligned}$$

$$\frac{\partial L_t}{\partial w_h} = 2(w_y w_h h_0 + w_y w_x x_1 - y_1)(w_y h_0)$$

$$+ 2(w_y w_h^2 h_0 + w_y w_h w_x x_1 + w_y w_x x_2 - y_2) \cdot (2 w_y w_h h_0)$$

$$= 2(-1)(2 \cdot 1) + 2(1)(2 \cdot 2 \cdot 1 \cdot 1)$$

$$= -4 + 8 = \boxed{+4} \#$$