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# **Noise Reduction of Synthetic Aperture Radar (SAR) and Ultrasound Images**

## **Technical Report**

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EE40054 - Digital Image Processing

University of Bath

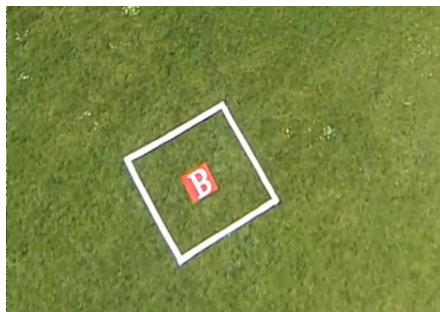
Candidate Number : 10374

## 1 Introduction

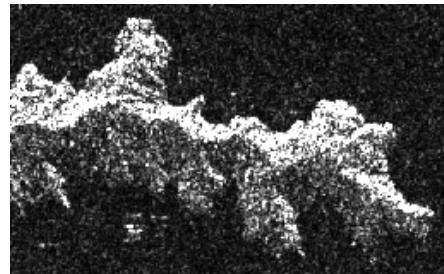
The human vision system is both very sophisticated and highly complicated yet it is not perfect. Noise, the bane of many digital systems but especially image processing, can obfuscate images making them difficult to process by eye when gradients and edges are blurred. Noise, however, typically follows pseudo-random distributions and as such can be counteracted through the use of certain filters. Even in the absence of noise, filters have many uses for enhancing images by artificially exacerbating the gradients and edges that the human vision system has evolved to detect.

## 2 Sample Images

In the initial assignment brief the two images NZjers.png and foetus.png[1]. For further appraisal DropZone.png was selected (taken from footage of an inflight aUAS [3]) and in order to assess the potential reactions to noise 20% gaussian noise was applied to foetus.png. All of these images are displayed in figure 1.



(a) Sample image from Team Bath Drones



(b) Provided image NZjers1.png



(c) Provided image foetus.png



(d) foetus.png with 20% gaussian noise

Figure 1: The images used for comparing filters

## 3 Filters

### 3.1 Comparison of Mean, Median and Gaussian Filters

Comparing the mean filter, the median filter and the gaussian filter for an equivalent window size on the image *foetusNoise2* we are able to see the clear differences in the 3 filters. Comparing the gaussian and the mean filters for windows of the same size the mean filter is producing a much greater amount of blurring and edge reduction than the gaussian whereas the gaussian filter has retained a large amount of the noise in the original image. To achieve the same blurring of the edges as seen in the mean filter we have to vastly increase the size of the gaussian window, when we do this we see a lot of the noise disappear from the image with regards to the edges, however inspecting the image itself we see the contrast is still superior to the mean filter.

Lastly we have the median filter for window size 7. Of all of the images presented this has the most clearly defined edges with the skull, cheekbone and the mass within the skull all well defined, we are also able to see that the line surrounding the image is much thinner, being closer to the gaussian for small window size.

### 3.2 Truncated Mean Filter

By removing outliers within a window before calculating the mean of that window the potential for noise or nearby points of luminescence/darkness adjusting the mean is diminished. Comparing the images in figure 3 we can see how edges are better preserved in the image. Furthermore the shadows on the bottom side of the image and the lighter ridges are much more visible.

### 3.3 Adaptive Weighted Median

By adjusting the weights for median values based upon the characteristics of the window it is possible to improve the noise response for the median filter on a window by weighting the values within it in accordance with the properties of that window using the equation shown in figure4 [2]. Shown in figure 5 the median and adaptive weighted median filters have both been applied to the image *foetus.png* and from visual inspection of both the output images and their Sobel detected edges it is clear to see a notable improvement to the clarity of the image.

When these filters are re-run over the image with 20% gaussian noise added to it we see an even greater improvement in the edges visible, the facial structure is clearly defined as and the spinal section of the foetus is notably separated from the background in comparison to the simple mean filter

## 4 Edge Detection

In order to more easily assess the information retained within the image after filtering edge detection methods were coded into the image class. Comparing the Sobel and Prewitt methods gave very little detectable difference with regards to the outputted image however due to the edges appearing to have greater visibility, figure 7, the Sobel filter was selected. In order to better visualise the

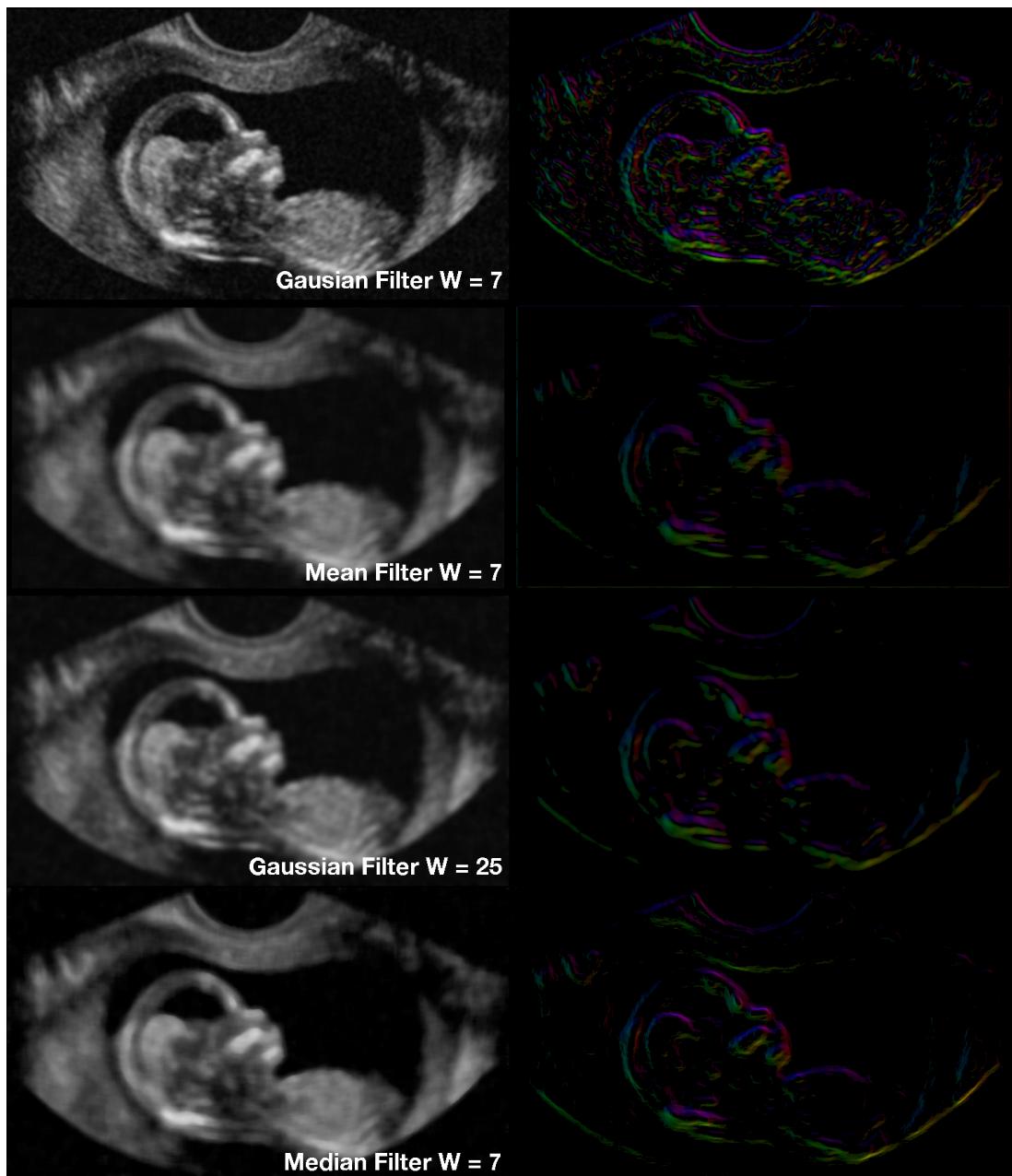


Figure 2: Comparison of a range of filters, minimum gradient = 25

gradients the theta angle generated by the method was encoded as the hue value in an HSV image, with the gradient value itself being assigned as the Value. Saturation was set to 255 across the image to aid in readability. Figure 8 below shows the edge filter applied to the DropZone image after a median filter ( $w=7$ ) was applied, not only are the outlines of the white square in the image clearly visible but the lines themselves clearly show the direction of their gradients. Unfortunately the initial conversion to grayscale makes the red square very difficult to distinguish from the grassy

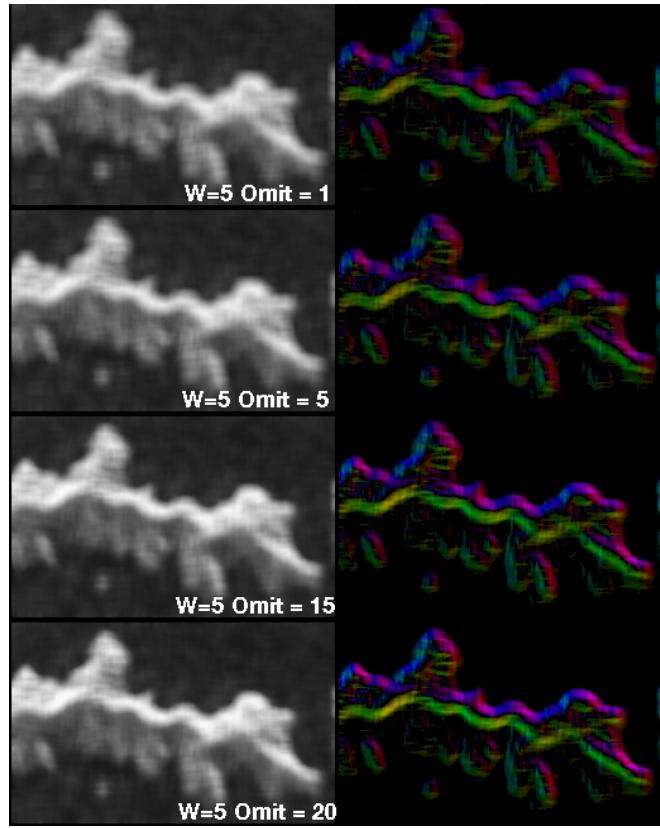


Figure 3: Comparing different amount of values omitted in calculating the mean of a 11x11 image

$$W_{i,j} = W_{mid} - d * c * \frac{\sigma}{\mu}$$

Figure 4: Adaptive Weighting Median, Weighting function

backdrop.

With more noisy images it is important to apply a degree of thresholding to the gradients required to count as an edge. Shown in figure 9 it can be seen that only a low threshold is needed to remove the lower values of noise however

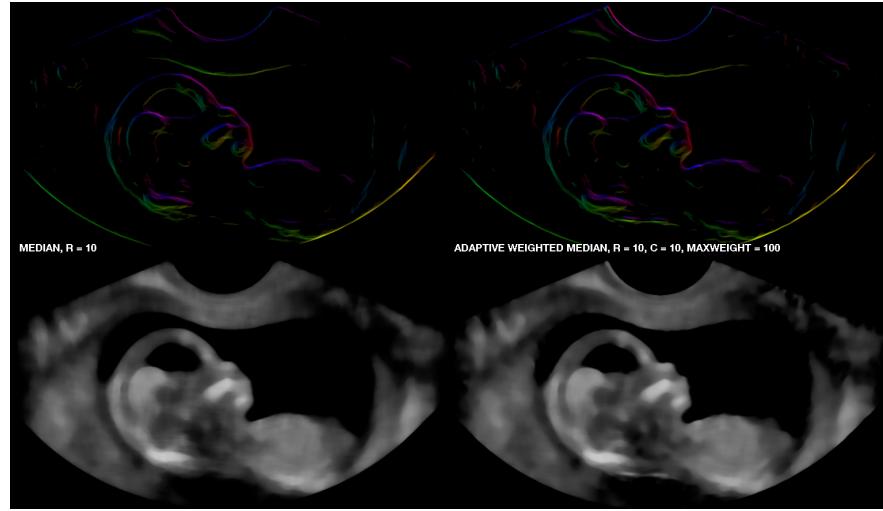


Figure 5: Comparison of the Median and Adaptive weighted Median filters with the same window size on the image: foetus.png

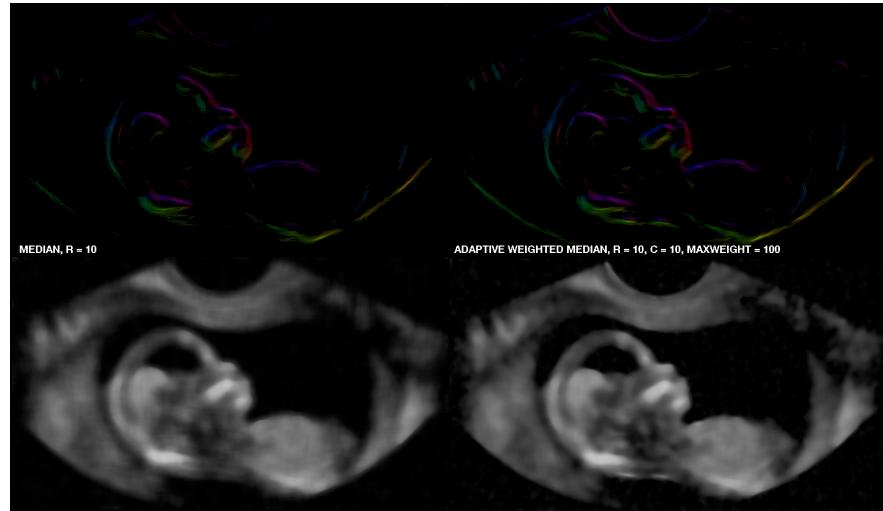
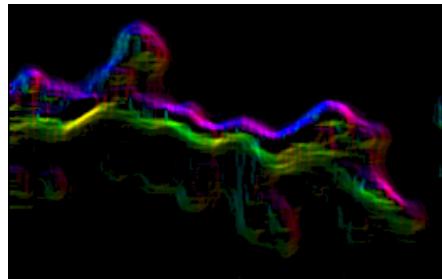


Figure 6: Comparison of the Median and Adaptive weighted Median filters with the same window size on the image: foetus.png with 20% Gaussian Noise

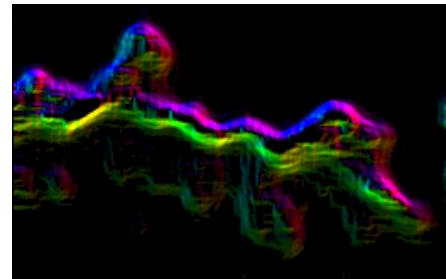
## 5 Evaluation

From the analysis of the different filters it was determined that the adaptive weighted median gave the most consistently good results for improving the images. For both the initially provided images there is a very clear improvement in the edge detection and readability of the images.

However if, in both cases, we determine that we care most about the edges between the objects in the image and the background then the application of a range highlight filter can help aid separating the objects from the backgrounds. The results of these range highlights can be seen in figure 10 and figure 11.



(a) Prewitt Filter



(b) Sobel Filter

Figure 7: Comparison of Sobel and Prewitt edge filters applied to the image *NZjers.png* after a median filter ( $w=7$ )

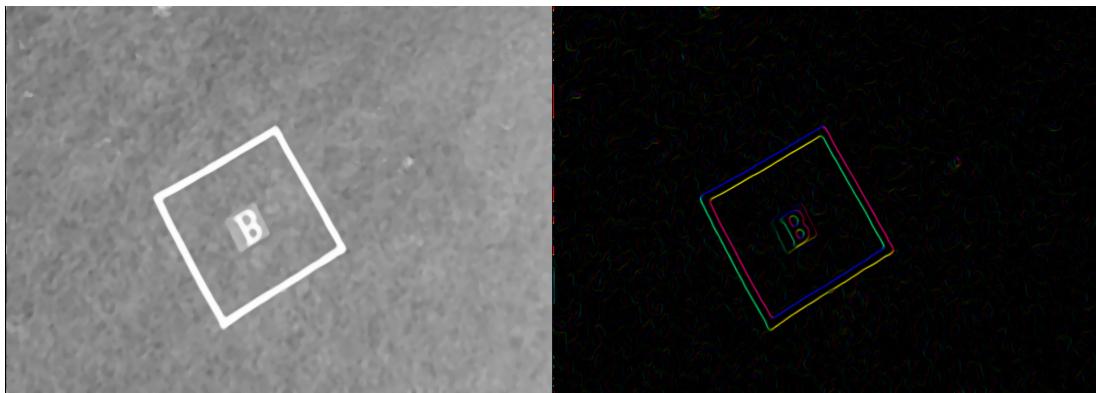


Figure 8: Example of the Sobel edge detector applied after a median filter ( $w = 7$ ) on the image *DropZone.png*

## 6 Image Class

The image class is used to apply filters onto an imported image and to log all of the transforms performed. The methods are detailed in the subsections below.

### 6.1 Universal Functions

These functions were either used for the initialisation of the image class or for common minor adjustments to the image.

1. **\_listFiles(args)** This function lists all png files within the current working directory to aid in loading image files.
2. **\_importPic(args)** Using OpenCV's imread function this imports a grayscale copy of the image specified.
3. **\_printFileList(\_,listOfFiles)** Prints the list of all images found within the current directory.

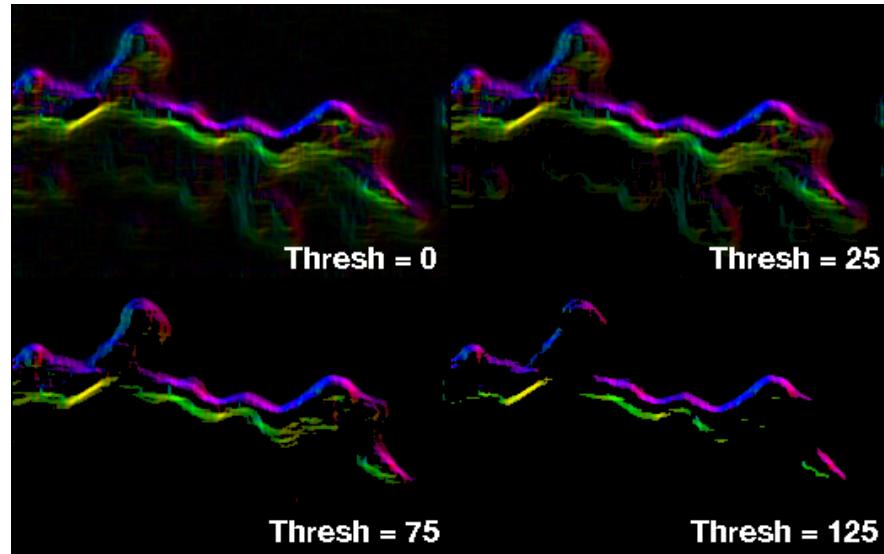


Figure 9: Comparing the effects of minimum gradient thresholds on the Sobel edge detector

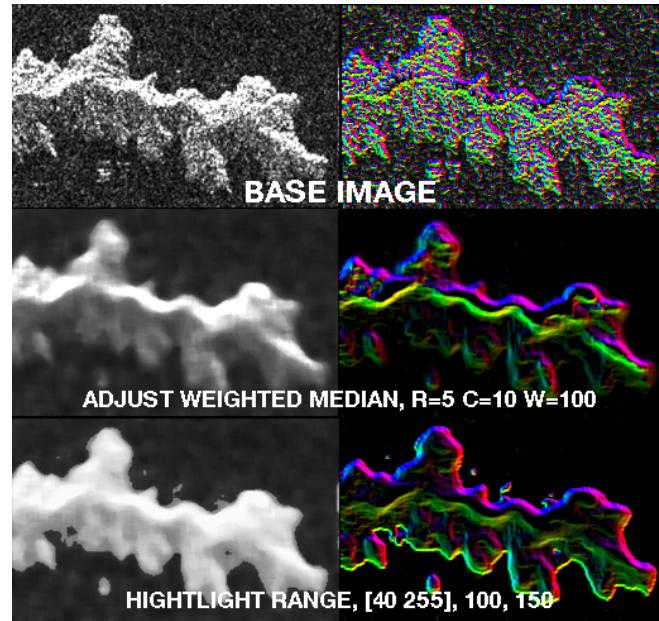


Figure 10: Comparing Stages of image analysis on *Njzers1.png*

4. **`_genborders(self,amount)`** Function to create a border around the image by mirroring the contents out for a distance of *amount* pixels.
5. **`_deborders(self,amount)`** Function to remove a border for a distance of *amount* pixels.
6. **`createWindows(self, windowSize)`** Function that creates an array of all windows within an image of size  $2 * \text{windowSize} + 1$ .

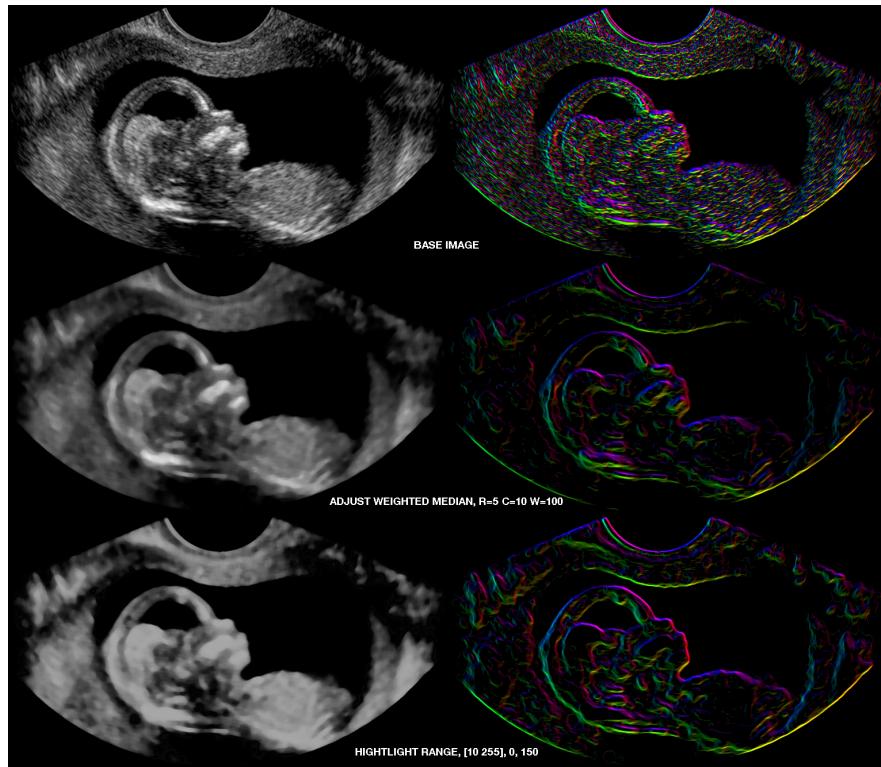


Figure 11: Comparing Stages of image analysis on *foetus.png*

## 6.2 External Functions

These functions were used for large scale manipulations of the images such as applying masks, updating the image or getting the dimensions of the image.

1. **imageSize(self)** Returns the dimensions of the grayscale image.
2. **uodateImage(self, newImage, transform)** Updates the image in the structure with a new image and appends the transform provided to the list of all applied transforms.
3. **duplicate(self)** Returns a new image with the same image as the original image.
4. **mask(self, mask)** Applies a mask provided to the image
5. **overlay(self,imageOver,mask)** Overlays imageOver onttop of the current image in the structure in accordance to the mask provided.
6. **snrRatio(self)** Small function that prints and returns the current signal to noise ratio of the image.

### 6.2.1 Output Functions

These functions were used to display the outputs of the processed images or save to files.

1. **showImage(self)** Function to display the current image of a structure on the screen until a key is pressed.
2. **savelImage(self)** Function to save the current image of a structure in the outputs subdirectory. The image name contains all transforms applied to the image in the order they were applied.
3. **histogram(self)** Displays a histogram of the grayscale levels of the current image.

### 6.3 Point Operator Functions

These functions were all single point operators which worked on a pixel by pixel basis within the image. The code typically looped over each pixel within the image performing operations on each pixel.

1. **POnormalise(self,nMin,nMax)** Function to map the grayscale levels proportionally over the defined range of  $nMax - nMin$
2. **POequalise(self,levels,ignore,offset)** More advanced version of image equalisation from the notes. Includes the functionality to add an array of discrete values to be ignored, the number of levels to be equalised to and an offset value to increase all values in the image by.
3. **PObitSlice(self,lMin,lMax)** Function which produces a mask of all values in the image which are within the range specified by  $lMin -- > lMax$ . The output for each pixel is either 0 or 255.
4. **POnegImage(self)** Function to invert the grayscale values of the image. Also works with coloured pictures not covered in this report.
5. **POfft(self)** Function to generate the fast fourier transform of the image.
6. **POfftMag(self)** Function to generate magnitude spectrum of the fast fourier transform of the image.
7. **POifft(self)** Function to generate the inverse fast fourier transform of the image.

### 6.4 Group Operator Functions

The group operator filters all work through the assessment of the values within a window of the image. This necessitated the creation of the window class, detailed in section 7, and all functions in this section operate in the same way. Firstly creating an array of all the windows in the image, followed by applying a method to each window in that array.

1. **GOfmean(self,windowSize)** Function to replace each pixel with the mean value of the surrounding values dictated by the size of the window.
2. **GOfsnr(self,windowSize)** Function to replace each pixel with the signal to noise ratio of the surrounding values dictated by the size of the window.

3. **GOLinearGaussian(self,sigma)** Function to replace each pixel with the mean value of the surrounding values adjusted for distance using a gaussian method, dictated by the size of the sigma used for the gaussian.
4. **GOequalise(self,winSize, levels, ignore, offset)** Function to replace each pixel with the value the pixel equalised with respect to the surrounding values dictated by the size of the window. This filters code has a sys.exit at the start as it takes a long time to run, and as it's not in the notes it validity was uncertain.
5. **GOhysterise(self,windowSize, margin)** Function to remove values from an image if they are not within a specific margin to the greatest value of nearby pixels, dictated by the size of the window.

## 6.5 Non-Linear Functions

Operating similarly to the group operator filters through the use of window methods in loops the Non-Linear functions differ through using non-linear window method. Unfortunately there was insufficient time to successfully complete the adaptive weighted median however the code is left for posterity.

1. **NLmedian(self,winSize)** Function to replace each pixel with the median of the local window.
2. **NLmeanTrimmed(self,winSize, trim)** Function to replace each pixel with the mean of the local window, trimmed by a chosen value.
3. **NLadaptiveMedian(self,winSize, midweight, cVal)** Function to replace each pixel with the median calculated using an adaptive weighted method. Within each window the weighting matrix is constructed and then applied when calculating the median.

## 6.6 Edge Detection Functions

These functions are the implementation of both the Sobel and Prewitt edge detection filters with additional steps to implement to represent the edge gradient as colour. The colour is centre with a theta angle of 0 corresponding to a hue value of 90.

1. **EDGEgradientsPrewitt(self,min)** Function to detect the edges in an image using the Prewitt filters. The value of min dictates the gradient threshold required for an edge to be counted.
2. **EDGEgradientsSobel(self,min)** Function to detect the edges in an image using the Sobel filters. The value of min dictates the gradient threshold required for an edge to be counted.

## 6.7 Other Functions

The functions in this section show example functions that can be created through the application of multiple filters within this document, in addition to one bookkeeping function that exists outside of the class definition.

1. **highlightRange(self,lBound,uBound,dcGain,levels)** Function to highlight a range of values, can also be used to remove all values within the two bounds and set them to a single value equal to dcGain.
2. **VisualiseFFT(self)** Function to replace an image in the class with the magnitude spectrum of that image.
3. **\_\_printSpacer\_\_(\*args)** Function to print a line of asterix', or to print a line of asterix' and the content of args.

## 7 Window Class

The window class is used to apply filters to a window within the image being worked on. For brevity, all functions in the window class work by calculating a new value for the window based on the contents of that image and then filling that window with the new value. This value is then read by functions in the image class and used to set the new values.

## A References

- [1] A. Evans. Noise reduction of synthetic aperture radar (sar) and ultrasound images.
- [2] R. C. Gonzalez and R. E. Woods. *Digital Image Processing*, chapter 5, pages 330–335. Pearson, 2016.
- [3] R. Thomas. Sensors and vision: Phase 3 - technical report.

## B Code

```
1 #! /usr/bin/env python3
2 # Module imageImport.py
3
4 ######
5 #
6 #      Python functions for importing image files      #
7 #
8 #      Author: _____                                #
9 #      Username: _____                             #
10 #
11 #####
12
13 # OpenCV used for loading images
14 from cv2 import *
15 import cv2
16
17
18 # Modules below used for listing available images in the current directory
19 from os import getcwd
20 from os.path import join, split
21 from glob import glob
22
23 # Modules for function termination and writing to file
24 from sys import exit
25 import sys
26
27 # Maths
28 import numpy as np
29 import scipy.signal
30
31 # Allow for plotting histogram graphs and 3d graphs http://matplotlib.org/mpl_toolkits/mplot3d/tutorial
32     .html
32 import matplotlib.pyplot as plt
33 from mpl_toolkits.mplot3d import Axes3D
34
35 # Enable creating the windows breaking list connectivity
36 import copy
37 from math import*
38
39
40 # Multi-threading for faster operating when utilising windows
41 from threading import *
```

```

42
43 class Window:
44     """
45     Attributes:
46     x: x_coordinate_of_image_centre_point
47     y: y_coordinate_of_image_centrepoint
48     width: Width_of_the_window
49     content: NxN_array_containing_the_contents_of_the_window
50     """
51     def __init__(self, wholeImage, centerPoint, width):
52         self.x, self.y = centerPoint
53         self.content = copy.copy(wholeImage.image[ (self.x-width):(self.x+width+1), (self.y-
54             width):(self.y+width+1) ])
55         self.cp = width+1
56         self.width = (2*width)+1
57
58     def cpVal(self):
59         # Returns the value of the pixel at the centre of the window
60         return self.content[self.cp-1, self.cp-1]
61
62     def average(self):
63         ## Averages the values within a window and then fills the window with the new average
64         ## value
65         averageValue = self.content.sum() / (self.width * self.width)
66
67         self.content.fill(averageValue)
68
69     def gfilter(self, filter):
70         # Applies Filter weights provided to the window before calculating mean
71         averageFilterVal = (self.content * filter).sum() / filter.sum()
72         self.content.fill(averageFilterVal)
73
74     def equalise(self, levels, ignore, offset):
75         # Filter returns the centre points value if equalised over the window
76         # VERY SLOW & UNTESTED
77         occurrenceMap = np.zeros([256])
78         greyScaleMap = np.zeros(256, 'uint8')
79         pixelCount=0
80         for nVal in range(0,255):
81             if nVal in ignore:
82                 occurrenceMap[nVal] = 0
83             else:
84                 occurrenceMap[nVal] = (self.content==nVal).sum()
85                 pixelCount += occurrenceMap[nVal]
86         for n in range(256):
87             ## Generating incredibly low values for percentage chance (sigma function
88             ## missing)
89             greyScaleMap[n] = ((np.sum(occurrenceMap[0:n]) / pixelCount ) * (levels-1)) +
90             offset
91             self.content.fill(greyScaleMap[self.content[self.cp, self.cp]])
92
93     def median(self):
94         # Filter to return median value of the window
95         medianValue = np.median(self.content)
96         self.content.fill(medianValue)
97
98     def snr(self):
99         # Filter to return the SNR of the window
100        if not self.content.std() == 0:
101            val = self.content.mean() / self.content.std()
102        else:

```

```

99             val = 0
100            self.content.fill(val)
101
102        def trimmedMean(self, nOmit):
103            # Returns the trimmed mean value of the window
104            numValues = self.width * self.width
105            halfPoint = ceil(numValues/2)
106
107            sortedVal = np.sort(self.content, axis=None, kind='mergesort')
108            trimmed = sortedVal[nOmit:-nOmit]
109            self.content.fill(trimmed.mean())
110
111        def prewittGX(self):
112            # Prewitt GX filter
113            Mx = np.array([[-1,0,1], [-1,0,1], [-1,0,1]])
114            if self.width >=3:
115                tempWindow = self.content
116                gxWin = np.sum(np.sum(np.multiply(Mx,tempWindow)))
117                return gxWin
118            else:
119                return 0
120
121        def prewittGY(self):
122            # Prewitt GY filter
123            My = np.array([[-1,-1,-1], [0,0,0], [1,1,1]])
124            if self.width >=3:
125                tempWindow = self.content
126                gyWin = np.sum(np.sum(np.multiply(My,tempWindow)))
127                return gyWin
128            else:
129                return 0
130
131        def sobelGX(self):
132            # Sobel GX filter
133            Mx = np.array([[-1,0,1], [-2,0,2], [-1,0,1]])
134            if self.width >=3:
135                tempWindow = self.content
136                gxWin = np.sum(np.sum(np.multiply(Mx,tempWindow)))
137                return gxWin
138            else:
139                return 0
140
141        def sobelGY(self):
142            # Sobel GY filter
143            My = np.array([[-1,-2,-1], [0,0,0], [1,2,1]])
144            if self.width >=3:
145                tempWindow = self.content
146                gyWin = np.sum(np.sum(np.multiply(My,tempWindow)))
147                return gyWin
148            else:
149                return 0
150
151        def hysterise(self, margin):
152            # Zeros a window if a value nearby is notably greater than the center value
153            centreVal = self.content[self.cp, self.cp]
154            maxVal = np.amax(self.content)
155
156            if (centreVal + margin) > maxVal:
157                self.content.fill(maxVal)
158            else:
159                self.content.fill(0)

```

```

160
161     def adaptiveMedian(self, c, midweight):
162         # If the mean is 0 the whole window must be 0
163         if not (self.content.mean() == 0):
164             snrlInvert = self.content.std() / self.content.mean()
165             imWidth = int(self.width)
166             # Generate a blank matrix to populate with the weights
167             weightings = np.zeros((imWidth, imWidth))
168
169             # Generate the weights matrix
170             ## IMPROVEMENT: Should put distance outside of Window function as is constance
171             #→ matrix
172             for i in range(imWidth):
173                 for j in range(imWidth):
174                     distance = ((self.cp - i - 1)**2 + (self.cp - j - 1)**2)**0.5
175                     weight = int(midweight - (c * distance * snrlInvert))
176                     weight = int(npamax([0, weight]))
177                     weightings[i, j] = int(weight)
178
179             # Flatten both of the arrays into 1dimensional to allow easier sorting
180             flatIm = self.content.flatten()
181             flatWeight = weightings.flatten()
182
183             # Return the indices of the content that would correspond to it in sorted
184             #→ format
185             sortedIndices = np.argsort(flatIm)
186
187             # Rearrange both matrices in accordance with the sorted indices
188             sortedIm = flatIm[sortedIndices]
189             sortedWeight = flatWeight[sortedIndices]
190
191             # Replace each weight with the cumulative total of weights up to that index
192             cumOcc = np.cumsum(sortedWeight)
193
194             # Calculate the total weights
195             totalOcc = np.sum(flatWeight)
196
197             # Find the first index in the cumulative weights greater than half the value of
198             #→ total weights
199             index = np.argmax(cumOcc > (totalOcc / 2))
200
201             # Return the median value at that index
202             medianVal = sortedIm[index]
203
204     else:
205         medianVal = 0
206         self.content.fill(medianVal)
207
208 class Image:
209     # Define a class that contains an image and its associated name
210     'Common_class_for_an_image'
211     """
212     Attributes:
213         name: A string containing the name of the original image
214         image: An array of the individual pixels of the image
215         transforms: A list of all performed transforms done on the image
216         """
217     def __init__(self, *args):
218         # Constructor for the class
219         # Generate a list of files within the current directory for validation
220         listOfFiles = self._listFiles()

```

```

18
19     # No transforms have been yet done on the image
20     self.transforms = []
21
22     if (0 == len(args)): # Validate that there is an argument to import, if not generate an
23         # empty image
24         [self.image, self.name] = [ [], "" ]
25     else: # If a string is provided check that it exists within the current directory
26         args = args[0]# Select only the first argument provided if it exists
27         if (args) in listOfFiles: # If filename is present within the current directory
28             # import the file and return it
29             imagelImported = self._importPic(args)
30             __printSpacer__( 'Image_file' + args + '_successfully_loaded' )
31             [self.image, self.name] = imagelImported, args
32         elif 'empty' == args:
33             self.image = []
34             self.name = 'emptyImage'
35         else: # If file does not exist within the directory exit the scripts
36             __printSpacer__(args + ':_file_not_found')
37             self._printFileList(listOfFiles)
38             exit()
39
40 #####
41 ## Methods (Internal):
42 #####
43 #####
44
45 def _listFiles(*args):
46     #Function to list available files for processing in the current directory
47     # Define the current working directory
48     cwd = getcwd()
49     # Create a glob-able parser
50     pngFilter = join(cwd, '*.png')
51     # Extract an array of all pngs in the current working directory
52     pngGlob = glob(pngFilter)
53
54     # Initialise an empty array to contain all valid png image files in the directory
55     pngFiles = []
56
57     # For each image detected in the current working directory remove the directory path
58     # and
59     # add file to pngFiles array
60     for image in pngGlob:
61         _, fileName = split(image)
62         pngFiles.append(fileName)
63
64     # return the populated array of file names
65     return pngFiles
66
67
68 def _importPic(*args):
69     # Function to import an image corresponding to a pre-validated string
70
71     # OpenCV's function 'imread' brings in a grayscale image
72     # 1 = color image without alpha channel
73     # 0 = grayscale image
74     # -1 = unchanged image including alpha channel
75     imagelImported = imread(args[1],0)
76
77     # Return imported image
78     return imagelImported

```



```

334
335     def duplicate(self):
336         # Function to create a duplicate of the current structure
337         newStruct = Image('empty')
338         # Hard assigns to stop altering original
339         imageM, imageN = self.imageSize()
340         newImage = np.zeros([imageM, imageN], 'uint8')
341         for i in range(imageM):
342             for j in range(imageN):
343                 newImage[i, j] = self.image[i, j]
344         newStruct.image = newImage
345
346         newStruct.name = self.name
347         newStruct.transforms = self.transforms
348         return newStruct
349
350
351     def mask(self, mask):
352         # Function to apply a mask provided to the image
353         self.image = np.minimum(self.image, mask.image)
354
355
356     def overlay(self, imageOver, mask):
357         # Function to overlay two images of the same size using a defined mask
358         # Apply mask to the base image
359         self.mask(mask)
360         # Invert the mask
361         mask.POnegImage()
362         # Apply the inverted mask to the image to overlay
363         imageOver.mask(mask)
364         # Combine the two masked images
365         self.image = self.image + imageOver.image
366
367
368     def snrRatio(self):
369         a = self.image.mean() / self.image.std()
370         print(a)
371         return a
372
373 #####
374 ## Methods (Outputs) ##  
##  
##  
#####
375
376     def showImage(self):
377         # Shows the contained image until a key is pressed
378         imshow(self.name, self.image)
379         waitKey(0)
380         destroyAllWindows()
381
382
383     def saveImage(self):
384         # Function to save an image to file after processing
385         imwrite("./outputs/" + self.name + "_" + join(self.transforms) + ".png", self.image)
386
387
388     def histogram(self):
389         # Function to create a histogram of an image's greyscale levels using the formula:
390         # p(r) = n / MN
391
392         # Find the total number of elements in the image
393         imageM, imageN = self.imageSize()
394         imageMN = imageM * imageN * 1.0
395         print(imageMN)
396
397
398         # Initialise an array for counting the occurrences of each grey value
399         nkCount = np.zeros(256)

```

```

395
396     for i in range(imageM):
397         for j in range(imageN):
398             nkCount[ self.image[i,j] ] = nkCount[ self.image[i,j] ] + 1.0
399
400     # Calculate probability of occurrence
401     probRk = nkCount / imageMN
402
403     plt.plot(probRk)
404     plt.xlim(0,255)
405     plt.show()
406
407 #####
408 ## ## Methods (Point Operator Filters) ## ##
409 ## ## #####
410 def POnormalise(self, nMin, nMax):
411     # Function to utilise contrast stretching for a given image using the formula:
412     #  $f(x,y) = [f(x,y) - Omin] \times (Nmax-Nmin)/(Omax-Omin) + Nmin$ 
413
414     # Ensure that the boundaries are floats so that the conversion ratio is a float
415     nMin = float(nMin)
416     nMax = float(nMax)
417
418     # Find Omax and Omin Values
419     oMin = np.amin(self.image)
420     oMax = np.amax(self.image)
421
422     # Generate the conversion ratio to reduce the amount of divisions required
423     conversionRatio = ((nMax - nMin)/(oMax-oMin))
424
425     # Create an empty array to populate with the new image information
426     imageM, imageN = self.imageSize()
427     newImage = np.zeros([imageM, imageN], 'uint8')
428
429     for i in range(imageM):
430         for j in range(imageN):
431             newImage[i,j] = int((self.image[i,j] - oMin) * conversionRatio + nMin)
432             self.updateImage(newImage, 'normalise')
433
434 def POequalise(self, levels, ignore, offset):
435     """
436     Inputs:
437     self = I don't understand object orientated enough to explain why self
438     levels = the number of unique luminence levels in the image
439     ignore = an array containing all luminence values to be ignored for the current array
440     → processing
441     """
442
443     # Create an empty array to populate with the new iamge information
444     imageM, imageN = self.imageSize()
445     imageMN = imageM * imageN * 1.0
446     newImage = np.zeros([imageM, imageN], 'uint8')
447
448     # Initialise an array for counting the occurrences of each grey value
449     occurrenceMap = np.zeros([256])
450     greyScaleMap = np.zeros(256, 'uint8')
451
452     pixelCount = 0
453
454     if ((levels + offset) > 255):

```

```

455     __printSpacer__( 'Warning : _DC_offset_+_desired_level_range_exceeds_255,_high_
456                         ↪ values_may_show_as_black' )
457
458     for nVal in range(0,255):
459         if nVal in ignore:
460             occurenceMap[nVal] = 0
461         else:
462             occurenceMap[nVal] = (self.image==nVal).sum()
463             pixelCount += occurenceMap[nVal]
464
465     for n in range(256):
466         greyScaleMap[n] = ((np.sum(occurenceMap[0:n]) / pixelCount ) * (levels-1)) +
467                         ↪ offset
468
469     for si in range(imageM):
470         for sj in range(imageN):
471             newImage[si ,sj] = greyScaleMap[self.image[si ,sj]]
472     self.updateImage(newImage, 'equaliseHistogram' + '_' + str(levels) + '_' + str(ignore)
473                      ↪ + '_' + str(offset))
474
475     def PObitSlice(self , lMin , lMax):
476         # Function to produce the parts of the image within a certain bit range,
477         # Returns a new image structure so that it can be used for generating masks
478         newImageStruct = self.duplicate()
479         newImage = newImageStruct.image
480
481         lowerSubset = newImage < lMin
482         midSubset = (newImage >= lMin) & (newImage <= lMax) # We want to include the values
483                         ↪ specified
484         upperSubset = newImage > lMax
485
486         newImage[lowerSubset] = 0
487         newImage[midSubset] = 255
488         newImage[upperSubset] = 0
489
490         newImageStruct.updateImage(newImage, 'GreySlice ')
491         return newImageStruct
492
493     def POneglImage(self):
494         # Function to invert the colours (or greyscale) of the image
495         initialImage = self.image
496         newImage = 255 - initialImage
497         self.updateImage(newImage, 'Invert')
498
499     def POfft(self):
500         f = np.fft.fft2(self.image)
501         fFshift = np.fft.fftshift(f)
502         self.updateImage(fFshift , 'fft ')
503
504     def POfftMag(self):
505         # Function to perform a fast fourier transform on an image and subsequently
506         # generate the resulting magnitude spectrum
507         self.POfft()
508         magnitude_spectrum = 20*np.log(np.abs(self.image))
509         self.updateImage(magnitude_spectrum , 'Magfft ')
510
511     def POifft(self):
512         ifShift = np.fft.ifftshift(self.image)
513         ifft = np.abs(np.fft.ifft2(ifShift))
514         self.updateImage(ifft , 'ifft ')
515         # Re normalise results to the range of grayscale values

```

```

512         self.POnormalise(0,255)
513
514         ##########
515         ##
516         ## Methods (Group Operator Filters)          ##
517         ##
518         #####
519
520     def GOmean(self ,windowSize):
521         # Create an array of windows
522         windowArray = self.createWindows(windowSize)
523
524         # Create a new image to populate
525         imageM, imageN = self.imageSize()
526         newImage = np.zeros([imageM, imageN], 'uint8')
527
528         # Apply the average window function to each window in array
529         for window in windowArray:
530             window.average()
531             newImage[window.x, window.y] = window.cpVal()
532         # Update image
533         self.updateImage(newImage, 'mean')
534
535     def GOsnr(self ,windowSize):
536
537         windowArray = self.createWindows(windowSize)
538
539         imageM, imageN = self.imageSize()
540         newImage = np.zeros([imageM, imageN], 'uint8')
541
542         for window in windowArray:
543             window.snr()
544             newImage[window.x, window.y] = window.cpVal()
545
546         self.updateImage(newImage, 'snrCompare_ ' + str(windowSize))
547
548     def GOlinearGaussian(self , sigma):
549
550         winSize = 2*(3*sigma) + 1
551
552         self._genBorders(winSize+1)
553
554         windowArray = self.createWindows(3*sigma)
555
556         imageM, imageN = self.imageSize()
557         newImage = np.zeros([imageM, imageN], 'uint8')
558
559         # Make an empty array to contain the mask
560         gausMask = np.zeros([winSize,winSize])
561
562         # Populate the mask with calculated weightings
563         for i in range(3*sigma+1):
564             for j in range(3*sigma+1):
565                 gVal = exp( - ( pow(3*sigma - i,2) + pow(3*sigma - j,2) ) / ( 2 * sigma
566                                         * sigma ) )
567
568                 # Gaussian mask is symetrical around centre so can set multiple values
569                 # at the same time
570                 gausMask[i,j] = gVal
571                 gausMask[i,winSize-j-1] = gVal
572                 gausMask[winSize-i-1,j] = gVal

```





```

692     windowArray = self.createWindows(1)
693
694     newlImage = np.zeros([imageM, imageN], 'uint8')
695     thetalImage = np.zeros([imageM, imageN], 'uint8')
696     blanklImage = np.zeros([imageM, imageN], np.uint8)
697
698     # For each window run the two directions of the edge detectors
699     for window in windowArray:
700         Gx = window.prewittGX()
701         Gy = window.prewittGY()
702         G = sqrt(Gx**2 + Gy**2)
703         if G > 255:
704             G = 255
705         elif G < min:
706             G = 0
707
708         newlImage[window.x, window.y] = G
709         thetalImage[window.x, window.y] = 90+(90*atan2(Gy, Gx)/np.pi)
710
711     # Create a RGB version of the image, convert to HSV and replace the H values with that
712     # ↪ of the theta values
713     # Saturation set to max for visibility. Converted back to RGB for display
714     BGR = np.dstack((newlImage, newlImage, newlImage))
715     HSV = cv2.cvtColor(BGR, cv2.COLOR_BGR2HSV)
716     HSV[:, :, 0] = thetalImage
717     HSV[:, :, 1] = 255 - blanklImage
718     final = cv2.cvtColor(HSV, cv2.COLOR_HSV2BGR)
719
720     # Update the image with the edge detected image
721     self.updateImage(final, 'EDGEprewitt')
722
723     def EDGEGradientsSobel(self, min):
724         self._genBorders(2)
725
726         imageM, imageN = self.imageSize()
727
728         windowArray = self.createWindows(1)
729
730         newlImage = np.zeros([imageM, imageN], np.uint8)
731         thetalImage = np.zeros([imageM, imageN], np.uint8)
732         blanklImage = np.zeros([imageM, imageN], np.uint8)
733
734         # For each window run the two directions of the edge detectors
735         for window in windowArray:
736             Gx = window.sobelGX()
737             Gy = window.sobelGY()
738             G = sqrt(Gx**2 + Gy**2)
739             if G > 255:
740                 G = 255
741             elif G < min:
742                 G = 0
743
744             newlImage[window.x, window.y] = G
745             thetalImage[window.x, window.y] = 90+(90*atan2(Gy, Gx)/np.pi)
746
747         # Create a RGB version of the image, convert to HSV and replace the H values with that
748         # ↪ of the theta values
749         # Saturation set to max for visibility. Converted back to RGB for display
750         BGR = np.dstack((newlImage, newlImage, newlImage))
751         HSV = cv2.cvtColor(BGR, cv2.COLOR_BGR2HSV)
752         HSV[:, :, 0] = thetalImage

```

```

751         HSV[:, :, 1] = 255 - blankImage
752         final = cv2.cvtColor(HSV, cv2.COLOR_HSV2BGR)
753
754         # Update the image with the edge detected image
755         self.updateImage(final, 'EDGESobel' +str(min))
756
757
758
759         ##########
760         ##
761         ## Methods (Filter Applications)          ##
762         ##                                     ##
763         ##                                     ##
764         ##########
765
766     def highlightRange(self, lBound, uBound, dcGain, levels):
767         # Function to take all values in the range [lBound uBound] and remap them
768         # to the range [dcGain dcGain+levels]
769         mask = self.PObitSlice(lBound, uBound)
770         rangePixels = self.duplicate()
771         rangePixels.mask(mask)
772         rangePixels.POequalise(levels, [0], dcGain)
773         mask.POnegImage()
774         self.overlay(rangePixels, mask)
775
776     def VisualiseFFT(self):
777         # Example function to visualise the FFT of an image
778         self.POfftMag()
779         self.POnormalise(0, 255)
780
781
782 def __printSpacer__(*args):
783     # Function created to print a line of asterix, made separate to make code neater
784     if (0 == len(args)): # If no arguments are included then print an asterix line spacer
785         print('*****')
786         print('')
787     else:               # If arguments are provided then print the argument surrounded
788         ↪ by asterix'
789         for i in range(len(args)):
790             print('*****')
791             print('')
792             print(args[i])
793             print('')

```