

Neutrino Scattering

It is possible to create a neutrino beam using a proton beam from a high-energy accelerator. The method is to shoot the proton beam into a target, produce pions, allow the pions to pass through an empty volume in which they can decay ($\pi^\pm \rightarrow \mu^\pm \nu_\mu$, $\pi^\pm \rightarrow e^\pm \nu_e$), and then absorb all of the decay products except for the neutrinos, which interact only through the weak interactions and are thus highly penetrating. For example, at Fermilab the pion beam was shot horizontally underground, so the ground had the role of the absorber (of charged particles and other ones not in study). What we can do with the neutrino beam is to study interactions with other particles. The V-A theory predicts neutrino and antineutrino reactions with quarks and antiquarks:

$$\nu_L d_L \longrightarrow \mu_L^- u_L \quad (1)$$

$$\bar{\nu}_R u_L \longrightarrow \mu_R^+ d_L \quad (2)$$

$$\nu_L \bar{u}_R \longrightarrow \mu_L^- \bar{d}_R \quad (3)$$

$$\bar{\nu}_R \bar{d}_R \longrightarrow \mu_R^+ \bar{u}_R \quad (4)$$

and similar reactions on the s and c quarks and antiquarks in the parton sea. These reactions should be seen as events with hadronic energy deposition and an outgoing muon, called **charged-current events**. The neutrino experiments also observe **neutral-current events**, with a neutrino in the final state. An example is showed in Figure 1.

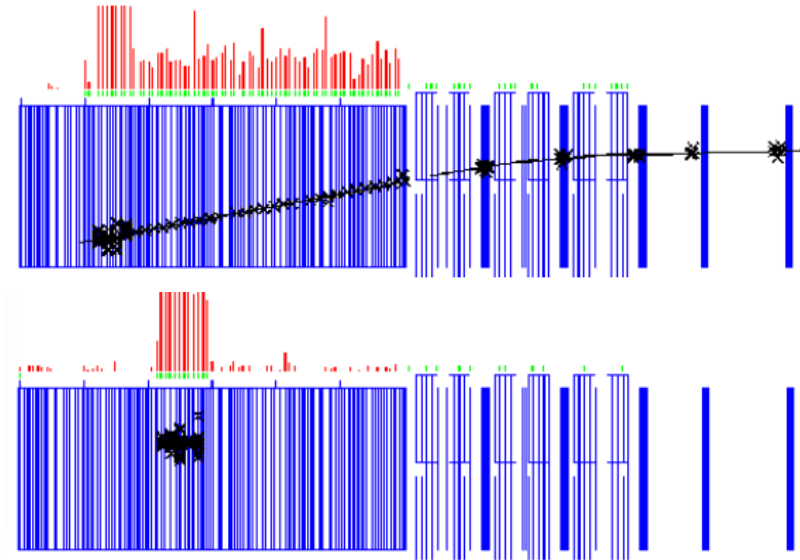


Figure 1: Event displays of charged-current (top) and neutral-current (bottom) neutrino deep inelastic scattering events recorded by the NuTeV experiment at Fermilab.

To predict the cross section for deep-inelastic neutrino scattering, we can look at the calculations done for deep-inelastic electron scattering and do something similar. We got for the electron-quark scattering:

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi Q_f^2 \alpha^2}{s} \frac{s^2 + u^2}{t^2} \quad (5)$$

and we derived the matrix elements:

$$|\mathcal{M}(e_L^- q_L \rightarrow e_L^- q_L)|^2 = 4Q_f^2 e^4 \frac{s^2}{t^2} \quad (6)$$

$$|\mathcal{M}(e_L^- q_R \rightarrow e_L^- q_R)|^2 = 4Q_f^2 e^4 \frac{u^2}{t^2} \quad (7)$$

In neutrino scattering, the V-A interaction fixes the helicity to be left-handed for neutrinos and quarks and right-handed for antineutrinos and antiquarks. Changing the prefactors appropriately, the cross sections for neutrino and antineutrino scattering on u and d quarks are:

$$\frac{d\sigma}{d\cos\theta} = \frac{G_F^2}{2\pi s} \cdot s^2 \quad (8)$$

$$\frac{d\sigma}{d\cos\theta} = \frac{G_F^2}{2\pi s} \cdot u^2 \quad (9)$$

To derive the formulae for deep inelastic scattering, we integrate with the pdfs and average over the initial quark spins. We don't average over the neutrino or antineutrino spin since the neutrinos are produced completely polarized from π decay. So we get for neutrino scattering and antineutrino scattering:

$$\frac{d^2\sigma}{dx dy}(\nu p \rightarrow \mu^- X) = \frac{G_F^2 s}{\pi} [x f_d(x) + x f_{\bar{u}}(x)(1 - y^2)] \quad (10)$$

$$\frac{d^2\sigma}{dx dy}(\bar{\nu} p \rightarrow \mu^+ X) = \frac{G_F^2 s}{\pi} [x f_u(x)(1 - y^2) + x f_{\bar{d}}(x)] \quad (11)$$

plus small contributions from heavier sea quarks and antiquarks.

0.1 Electroweak interaction

We saw that weak interaction is based on V-A theory and that neutrino interaction implies the existence of charged current (CC) and neutral current (NC). Weak interactions are generated by spin 1 bosons, namely W^\pm for CC and Z^0 for NC.

In the diagram, W^- appears as a resonance, with the Breit-Wigner denominator:

$$\frac{1}{q^2 - m_W^2} \quad (12)$$

But there was no sign of the q^2 -dependence in the data. This implies that the W^- boson is heavier than about 30 GeV, in fact its mass is about 80 GeV.

Our need for a massive spin 1 boson forces us to face a problem that we have avoided up to now: What is the wave equation for the associated massive spin 1 field? There is only one way known to solve this problem. That is to mix the two concepts of gauge invariance and spontaneous symmetry breaking.

The starting point is a gauge theory with complex fields and symmetry group $U(1)$:

$$\mathcal{L} = -\frac{1}{4}(F_{\mu\nu})^2 + |D_\mu\varphi|^2 - V(\varphi) \quad (13)$$

with:

$$D_\mu\varphi = (\partial_\mu - ieQA_\mu)\varphi \quad (14)$$

where Q is the charge of the field.

The next step is a gauge theory based on $SO(3)$ adding, with scalar field φ . It gives us massive bosons and one massless boson.