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In [1]: %%capture
import pandas as pd
import matplotlib.pyplot as plt
import matplotlib.gridspec as gridspec
%matplotlib inline
plt.style.use('seaborn-v0_8-whitegrid')
from matplotlib.legend_handler import HandlerTuple
import matplotlib.ticker as ticker
!pip freeze > requirements.txt
!pip freeze | grep -v -f requirements.txt - | grep -v '^#' | grep -v '^-e ' | xargs pip uninstall -y
```

Abstract

This carrier quantum-confinement simulation of Silicon (Si) inversion layer, pertains to a 1D MOS Capacitor at 300K, using COMSOL's 'Multiphysics®' and nanoHUB's 'Schred 1.0' tool. Such a simulation requires calculating the carrier concentration (in this case electron) as a function of vertical distance from the oxide-channel interface (referred to as 'Arc length' in the upcoming plots), based on standard MOS device parameters (referred from [1] COMSOL Documentation) and carrier transport formalisms such as -

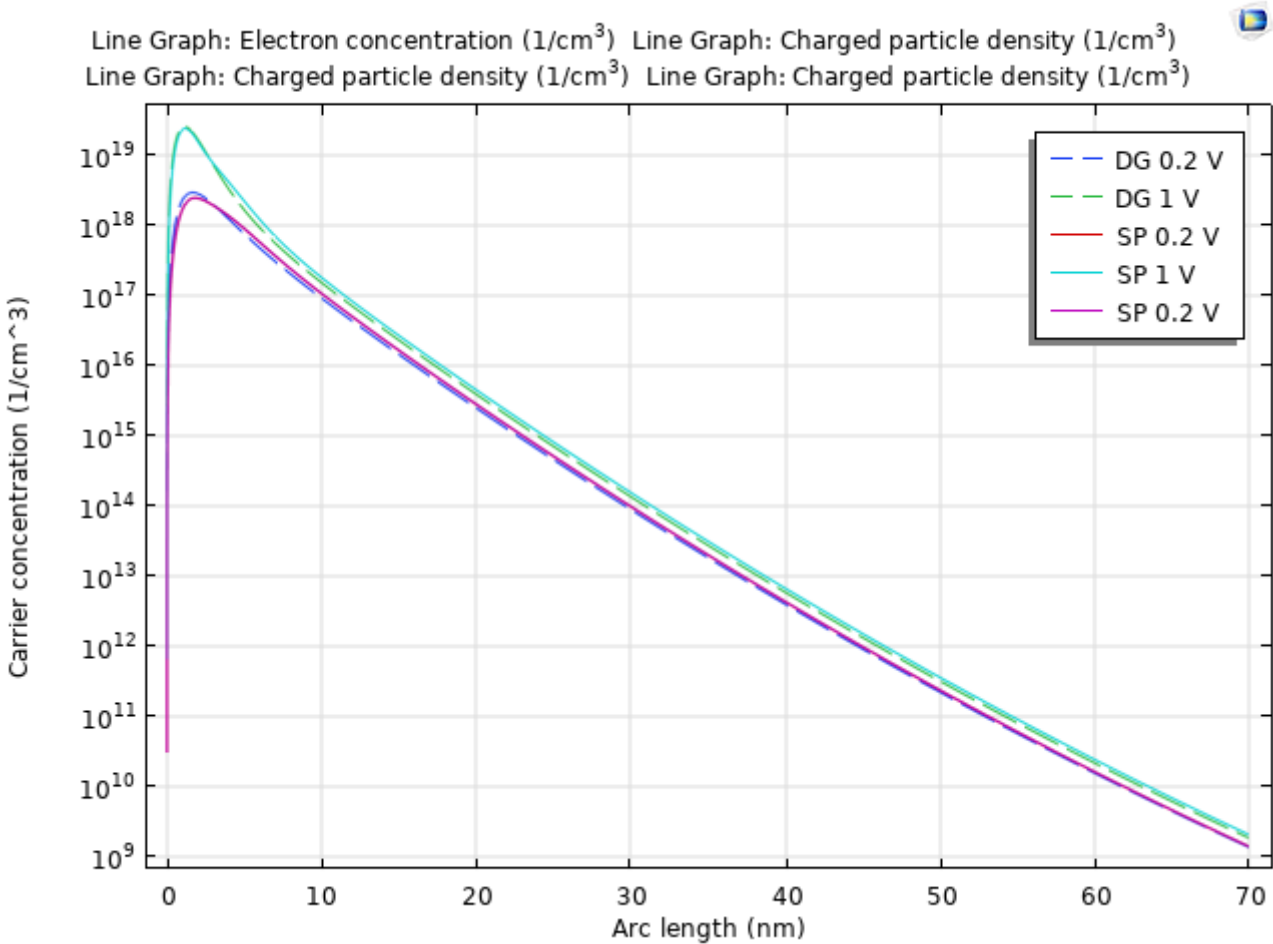
- 1. Density Gradient: based on a quantum potential-corrected continuum transport description of carriers, as originally formulated in [2].
- 2. Schrödinger-Poisson: based on a full quantum transport description of carriers using non-equilibrium Greene's function, as originally formulated in [3].

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Part I: Density-Gradient and Schrödinger-Poisson solution of inversion layer, using COMSOL

Simulations at $V_g = 0.2V, 1V$



	Density-Gradient solution ($V_g = 0.2V$, 1V)	Schrödinger-Poisson solution ($V_g = 0.2V$)	Schrödinger-Poisson solution ($V_g = 1V$)
Time elapsed (s)	9	72	101
Memory usage (GB)	1.01	1.09	1.27

Summary

- As noted in the table above (and as mentioned in [2]), the Density-Gradient formulation is more computationally efficient than Schrödinger-Poisson formulation in solving carrier concentrations (and with similar solutions w.r.t that of Schrödinger-Poisson formulation $\forall V_g$, as observed in the plot above) across the vertical Si channel.
- Both formulations capture the effect of electron quantum-confinement near 3-4 nm range $\forall V_g$ (observed as peaks in the plot above). This effect is due to -
 - Electron quantisation in the Si channel stemming from a degenerate Si bandstructure.
 - Increasing potential barrier height at the oxide-channel interface due to ever decreasing oxide thickness (which has to do with MOS process node scale-down), leading to zero probability of electron tunneling into the oxide.

Part II: Schrödinger-Poisson solution of inversion layer, using NanoHUB and COMSOL

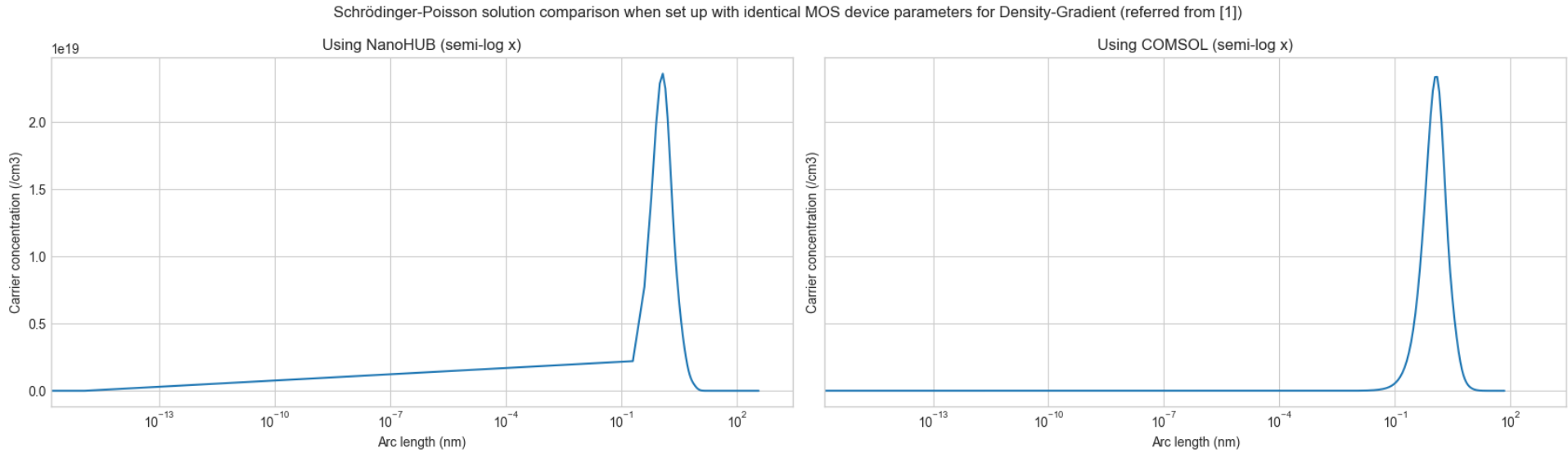
Simulations at $V_g = 1V$

```
In [2]: SPNanoHUB = pd.read_csv('Part II/3.txt', skiprows=4, nrows=999, header=None)
SPCOMSOL = pd.read_fwf('Part I/2.txt', skiprows=8, nrows=199, header=None)
fig, axes = plt.subplots(nrows=1, ncols=2, tight_layout=True, sharex=True, sharey=True, figsize=(17, 5))
fig.suptitle('Schrödinger-Poisson solution comparison when set up with identical MOS device parameters for Density

plt.subplot(121)
plt.plot(SPNanoHUB[0], SPNanoHUB[1])
plt.xscale('log')
axes[0].set_xlabel('Arc length (nm)')
axes[0].set_ylabel('Carrier concentration (/cm3)')
axes[0].set_title('Using NanoHUB (semi-log x)')

plt.subplot(122)
plt.plot(SPCOMSOL[0], SPCOMSOL[1])
plt.xscale('log')
axes[1].set_xlabel('Arc length (nm)')
axes[1].set_ylabel('Carrier concentration (/cm3)')
axes[1].set_title('Using COMSOL (semi-log x)')
```

Out[2]: Text(0.5, 1.0, 'Using COMSOL (semi-log x)')

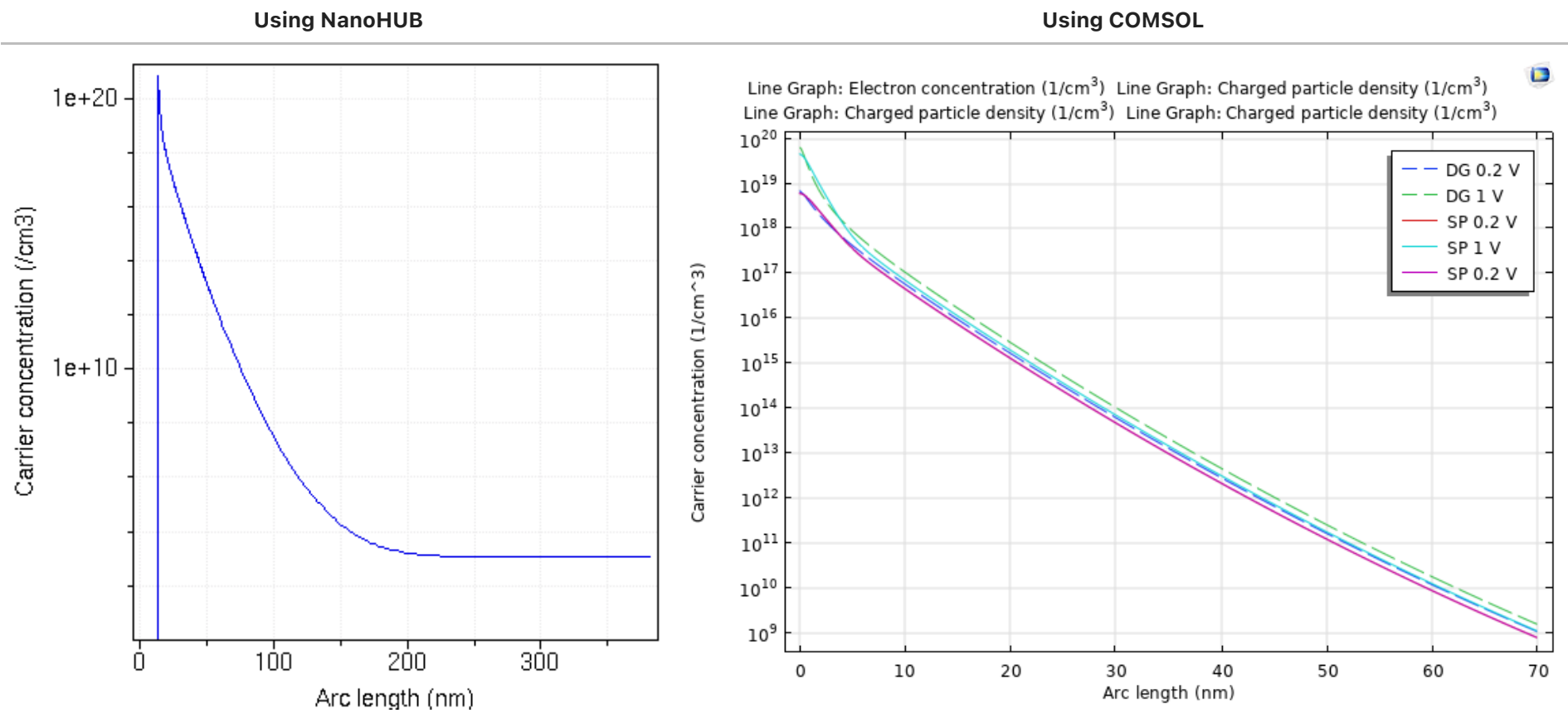


Summary

- 1. Both NanoHUB (Schred tool) and COMSOL capture the electron charge centroid (peaks in the plots above) at the same position in the vertical Si channel, which indicates that the Schrödinger-Poisson formulation in both tools are similarly defined.
- 2. The slight discreteness in the NanoHUB plot above indicates a lack of enough discretisation nodes defined along the vertical Si channel in the Schred tool.

Part III: Classical-Poisson solution of inversion layer, using NanoHUB and COMSOL

Simulations at $V_g = 1V$ (in NanoHUB) and $V_g = 0.2V, 1V$ (in COMSOL)



Summary

- To perform a Classical-Poisson simulation of the inversion layer:
 - Using NanoHUB Schred: As noted in page 11 of [4], Schred 2.0 with the semiclassical charge model is used and the resulting simulation plot is shown in the left above.
 - Using COMSOL: As inferred from [1] and based on the discussion in point 2 of Summary in Part I) -
 - For classical approximation from Density-Gradient formulation: electron mass (meDG) is set to 10xme_const/3 (inferred from page 7 of [1]), and n barrier height at oxide interface (Φ_n^{Ox}) is set to 0 (inferred from page 8 of [1]).
 - For classical approximation from Schrödinger-Poisson formulation: Zero Probability node in the COMSOL model tree is disabled (inferred from page 13 of [1]).
 - The combined resulting simulation plot (classical approximation from Density-Gradient \& Schrödinger-Poisson formulations) is shown in the right above.
- Both plots above (Classical-Poisson simulations using NanoHUB and COMSOL) indicate a monotonically decreasing inversion electron concentration from the oxide-Si channel interface (non-existent electron charge centroids at further depths in the vertical Si channel), which is the case when there is no carrier quantum-confinement effect.

References

- [1] [COMSOL Documentation - Density-Gradient and Schrödinger–Poisson Results for a Silicon Inversion Layer](#)
- [2] [Density-gradient theory: a macroscopic approach to quantum confinement and tunneling in semiconductor devices - M.G. Ancona](#)
- [3] [Nanoscale device modeling: the Green’s function method - Supriyo Datta](#)
- [4] [Schred Documentation - Quantum Size Effects and the Need for Schred - Dragica Vasileska](#)

Additional information

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Data and config file at: [Github](#)