

# Theory of Activities

May 4, 2018

## 1 The Physical Domain

The domain has four rooms located side by side (*library*, *kitchen*, *office1* and *office2*) and connected. The robot *rob<sub>1</sub>*, can move from one room to the next. A *secure* room can be *locked* or *unlocked*. The robot cannot move to or from a locked room; it can *unlock* a locked room. The domain objects can be located in any of the rooms. The robot can *pickup* an object if it is in the same location as the object, it can *put\_down* an object that it is holding and it can only hold one object at a time. There are two exogenous actions, one that can change the location of any object, and one that can lock a secure room. The agent may not be aware of these exogenous action when they happen. We are also going to define three different defined fluents, two of which we will be using as possible goals.

### 1.1 AL

Sorts:

$$\begin{aligned} \textit{secure\_room} &= \{\textit{library}\}. \\ \textit{room} &= \textit{secure\_room} + \{\textit{kitchen}, \textit{office}_1, \textit{office}_2\}. \\ \textit{robot} &= \{\textit{rob}_1\}. \\ \textit{book} &= \{\textit{book}_1, \textit{book}_2\}. \\ \textit{object} &= \textit{book}. \\ \textit{thing} &= \textit{object} + \textit{robot}. \end{aligned}$$

Static relations:

$$\textit{next\_to}(\textit{office}_1, \textit{office}_2).$$

*next\_to(kitchen, office<sub>1</sub>).*  
*next\_to(library, kitchen).*

Inertial fluents:

*inertial\_fluent = loc(thing, room) + in\_hand(robot, object) + locked(secure\_room).*

Possible goals:

*possible\_goal = tidy\_all(room) + tidy\_book(book, room).*

Defined fluents:

*defined\_fluent = possible\_goal + missing\_book(room).*

Robot actions:

*move(robot, room).*  
*pickup(robot, object).*  
*put\_down(robot, object).*  
*unlock(robot, secure\_room).*

Exogenous actions:

*exo\_move(object, room).*  
*exo\_lock(secure\_room).*

Causal Laws:

*move(R, L)* **causes** *loc(R, L)*  
*pickup(R, O)* **causes** *in\_hand(R, O).*  
*put\_down(R, O)* **causes**  $\neg in\_hand(R, O).$   
*unlock(R, L)* **causes**  $\neg locked(L).$   
*exo\_lock(L)* **causes** *locked(L).*  
*exo\_move(O, L)* **causes** *loc(O, L).*

State Constraints:

*next\_to(L1, L2)* **if** *next\_to(L2, L1).*

$$\begin{aligned}
\neg loc(T, L2) & \text{ if } loc(T, L1), L1 \neq L2. \\
loc(O, L) & \text{ if } loc(R, L), in\_hand(R, O). \\
\neg in\_hand(R, O1) & \text{ if } in\_hand(R, O2), O1 \neq O2.
\end{aligned}$$

Executability Conditions:

$$\begin{aligned}
& \text{impossible } move(R, L) \text{ if } loc(R, L). \\
& \text{impossible } move(R, L2) \text{ if } loc(R, L1), \neg next\_to(L1, L2). \\
& \text{impossible } move(R, L2) \text{ if } loc(R, L1), locked(L1). \\
& \text{impossible } move(R, L) \text{ if } locked(L). \\
& \text{impossible } unlock(R, L) \text{ if } \neg locked(L). \\
& \text{impossible } unlock(R, L1) \text{ if } loc(R, L2), \neg next\_to(L2, L1), L2 \neq L1. \\
& \text{impossible } put\_down(R, O) \text{ if } \neg in\_hand(R, O). \\
& \text{impossible } pickup(R, O1) \text{ if } in\_hand(R, O2). \\
& \text{impossible } pickup(R, O) \text{ if } loc(R, L1), loc(O, L2), L1 \neq L2. \\
& \text{impossible } exo\_move(O, L) \text{ if } loc(O, L). \\
& \text{impossible } exo\_move(O, L) \text{ if } locked(L). \\
& \text{impossible } exo\_move(O, L2) \text{ if } loc(O, L1), locked(L1). \\
& \text{impossible } exo\_move(O, L) \text{ if } in\_hand(R, O). \\
& \text{impossible } exo\_lock(L) \text{ if } locked(L).
\end{aligned}$$

## 1.2 The Theory of Activities

In our *ToA* domain of our agent will also have a list of *possible goals* and one of them will be selected. The agent will need to specify one or more *activities* that would achieve the selected goal. He may have a list of different existing activities. If there are existing activities that achieve the goal, the agent will choose and return one of those activities. If the agent cannot find a successful existing *activity*, he will create and return one. If he cannot use or create a successful *activity*, the goal will be considered futile.

An *activity* will be represented by a triple consisting of *name*, *plan* and *goal*. A *name* is a unique identifier used to refer to the *activity*, and a plan is a sequence of agent actions, which will lead to the realisation of the *goal*.

We limit the names of activities to a collection of integers ( $1 \dots max\_name$ ), the length of plans to a maximum length ( $1 \dots max\_len$ ). The fluents of the physical environment that may serve as a *goal* are those of the sort *possible\_goal*.

In order to create the Action Language for the new domain, we will 1-adapt and 2-extend the original Action Language for the physical domain. We will adapt it by

re-defining the sort *inertial\_fluent* as *physical\_inertial\_fluents*, *defined\_fluents* as *physical\_defined\_fluents*, and the sort *agent\_action* as *physical\_agent\_action*. We will define the following new sorts:

- A sort *activity\_name* =  $1, \dots, \text{max\_name}$  to represent the name of an *activity*.
- A sort *index* =  $\{-1, 0, \text{max\_len}\}$  to represent the index of an action as part of an *activity*.
- A sort *mental\_agent\_action* =  $\{\text{select\_activity}(\text{activity\_name})\}$  to represent the action of choosing and activity.
- A sort *mental\_inertial\_fluent* =  $\{\text{current\_action\_index}(\text{activity\_name}, \text{index})\}$  to represent the current (mental) state of an *activity*.
- A sort *mental\_defined\_fluent* =  $\{\text{next\_action}(\text{activity\_name}, \text{action})\}$

We also the following relations that give shape to the concept of *activity*.

*activity\_component(activity\_name, index, physical\_agent\_action).*  
*activity\_length(activity\_name, index).*  
*activity\_goal(activity\_name, possible\_goal).*

We create a hierarchical structure of *fluents* and *actions* as follows:

*inertial\_fluent* = *physical\_inertial\_fluent* + *mental\_inertial\_fluent*,  
*fluent* = *defined\_fluent* + *inertial\_fluent*,  
*agent\_action* = *mental\_agent\_action* + *physical\_agent\_action*,  
*action* = *agent\_action* + *exo\_action*.

As well as the previous statements included in the physical domain, we will include:

Causal Laws:

$$\text{select\_activity}(AN) \quad \mathbf{causes} \quad \text{current\_action\_index}(AN, 0). \quad (1)$$

$$\begin{aligned} PAA \quad \mathbf{causes} \quad \text{current\_action\_index}(AN, K + 1) \quad \mathbf{if} \quad & \text{next\_action}(AN, PAA), \\ & \text{current\_action\_index}(AN, K), \\ & \text{activity\_component}(AN, K + 1, PAA). \end{aligned} \quad (2)$$

State Constraints:

$$\neg \text{current\_action\_index}(AN, K1) \quad \mathbf{if} \quad \text{current\_action\_index}(AN, K2), \quad (3)$$

$$K1 \neq K2.$$

$$\begin{aligned} \text{next\_action}(AN, PAA) \quad \text{if} \quad & \text{current\_action\_index}(AN, K), \\ & \text{activity\_component}(AN, K + 1, PAA). \end{aligned} \quad (4)$$

$$\begin{aligned} \text{tidy\_book}(B, R) \quad \text{if} \quad & \text{loc}(B, R), \neg \text{in\_hand}(B). \\ \text{missing\_book}(R) \quad \text{if} \quad & \neg \text{tidy\_book}(B, R). \\ \text{tidy\_all}(R) \quad \text{if} \quad & \text{not missing\_book}(R). \end{aligned} \quad (5)$$

$$\begin{aligned} \neg \text{selected\_goal}(G1) \quad \text{if} \quad & \text{selected\_goal}(G2), \\ & G1 \neq G2. \end{aligned} \quad (6)$$

Initial State Constraint:

$$\text{current\_action\_index}(AN, -1) \quad (7)$$

## 2 The Architecture: Reasoning Tasks and Behaviour.

### 2.1 Introducing new relations

The axioms that need to be added to the ASP program also involve the following relations:

- *impossible*(A, I) means that action A is impossible at step I.
- *candidate*(AN) means that AN is a candidate for the next activity to be started to achieve the selected goal.
- *existing\_candidate*(AN) means that AN is an existing candidate for the activity to achieve the selected goal.
- *new\_candidate*(AN) means that AN is newly created candidate for the activity to achieve the selected goal.
- *has\_component*(AN, K) means that activity AN has a component at index K.
- *needs\_new\_activity* flag that means that no successful existing activity has been found in the previous run.
- *next\_available\_name* will hold the next number that can be used as a name for a newly created activity.

## 2.2 Translating AL to ASP

The following steps should be followed in order to translate the AL description into an ASP program.

For every causal law:  $a$  **causes**  $l$  **if**  $p_0, \dots, p_m$

The ASP contains:  $holds(l, I + 1) :- holds(p_0, I), \dots, holds(p_m, I), occurs(a, I).$

For every state constraint:  $l$  **if**  $p_0, \dots, p_m$

the ASP contains  $holds(l, I) :- holds(p_0, I), \dots, holds(p_m, I).$

The ASP contains the CWA for defined fluents:

$-holds(F, I) :- \#defined\_fluent(F), not holds(F, I).$

For every executability condition: **impossible**  $a$  **if**  $p_0, \dots, p_m$

the ASP contains:  $impossible(a, I) :- holds(p_0, I), \dots, holds(p_m, I).$

It also contains:  $-occurs(A, I) :- impossible(A, I).$

The ASP contains the inertia axioms:

$holds(F, I + 1) :- holds(F, I), not -holds(F, I + 1).$

$-holds(f, I + 1) :- -holds(F, I), not holds(F, I + 1).$

The ASP contains the CWA for actions:

$-occurs(A, I) :- not occurs(A, I).$

Once translation using the above steps has been completed, the axioms in the following section will also need to be added to the ASP program.

## 2.3 Reasoning Axioms

Defining candidates:

The flag *need\_new\_candidate* will trigger the creating of a new candidate:

$$new\_candidate(AN) \leftarrow needs\_new\_activity. \quad (8)$$

$$\begin{aligned} existing\_candidate(AN) \leftarrow & \ activity\_goal(AN, G), \\ & selected\_goal(G), \\ & not \ new\_candidate(AN). \end{aligned} \quad (9)$$

$$\begin{aligned}
\text{candidate}(AN) &\leftarrow \text{new\_candidate}(AN). \\
\text{candidate}(AN) &\leftarrow \text{existing\_candidate}(AN).
\end{aligned} \tag{10}$$

Creating new activities:

$$\begin{aligned}
\text{activity\_goal}(AN, G) &\leftarrow \text{new\_candidate}(AN), \\
&\quad \text{selected\_goal}(G).
\end{aligned} \tag{11}$$

$$\begin{aligned}
\text{activity\_component}(AN, I, PAA) &\leftarrow \text{new\_candidate}(AN), \\
&\quad \text{occurs}(\text{select\_activity}(AN), 0), \\
&\quad \text{occurs}(PAA, I), \\
&\quad 0 < I.
\end{aligned} \tag{12}$$

$$\begin{aligned}
&\leftarrow \text{new\_candidate}(AN), \\
&\quad \text{activity\_component}(AN, K, PAA1), \\
&\quad \text{activity\_component}(AN, K, PAA2), \\
&\quad PAA1 \neq PAA2.
\end{aligned} \tag{13}$$

$$\begin{aligned}
\text{has\_component}(AN, K) &\leftarrow \text{new\_candidate}(AN), \\
&\quad \text{occurs}(\text{select\_activity}(AN), 0), \\
&\quad \text{activity\_component}(AN, K, C).
\end{aligned} \tag{14}$$

$$\begin{aligned}
\text{activity\_length}(AN, K) &\leftarrow \text{new\_candidate}(AN), \\
&\quad \text{occurs}(\text{select\_activity}(AN), 0), \\
&\quad \text{has\_component}(AN, K), \\
&\quad \text{not has\_component}(AN, K + 1).
\end{aligned} \tag{15}$$

Selecting candidates: If it is not impossible to select a candidate, it will be selected.

$$\begin{aligned}
\text{occurs}(\text{select\_activity}(AN), 0) &\leftarrow \text{candidate}(AN), \\
&\quad \text{not impossible}(\text{select\_activity}(AN), 0).
\end{aligned} \tag{16}$$

It is impossible to select an activity at any step other than 0, it is impossible to select an activity if it is not a candidate, and it is impossible to select two different activities .

$$\begin{aligned}
impossible(select\_activity(AN1), 0) &\leftarrow occurs(select\_activity(AN2), 0), \\
&\quad AN1 \neq AN2. \\
impossible(select\_activity(AN), 0) &\leftarrow not\ candidate(AN). \\
impossible(select\_activity(AN), I) &\leftarrow 0 < I. \\
impossible(select\_activity(AN), I) &\leftarrow activity\_goal(AN, G), \\
&\quad holds(G, 0).
\end{aligned} \tag{17}$$

This rule ensures that the selected existing activity is the minimal activity that reaches the goal:

$$\begin{aligned}
occurs(PAA, I) &\stackrel{+}{\leftarrow} existing\_candidate(AN), \\
&\quad occurs(select\_activity(AN), 0), \\
&\quad holds(next\_action(AN, PAA), I), \\
&\quad occurs(A, I - 1), \\
&\quad 0 < I.
\end{aligned} \tag{18}$$

This rule ensures that the newly created activity is the minimal activity that reaches the goal:

$$\begin{aligned}
occurs(PAA, I) &\stackrel{+}{\leftarrow} new\_candidate(AN), \\
&\quad occurs(select\_activity(AN), 0), \\
&\quad occurs(A, I - 1), \\
&\quad 0 < I.
\end{aligned} \tag{19}$$

Planning module:

$$\begin{aligned}
success &\leftarrow holds(G, I),\ selected\_goal(G). \\
&\leftarrow not\ success.
\end{aligned} \tag{20}$$