1st Score:	2nd Score:	3rd Score:					
S & G	S & G	S & G					
Grader:	Grader:	Grader:	Final Score				
PLACE LABEL BELOW							
Name:		School:					
SS/ID Number:City:							
Grade: 5 6 7	8 Cla	assification: 1A 2A	3A 4A 5A 6A				

Academic Excellence in Mathematics and Science through Competition TMSCA					
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# TMSCA MIDDLE SCHOOL CALCULATOR

TEST #8 ©

JANUARY 20, 2018

GENERAL DIRECTIONS

#### I. About this test:

- A. You will be given 30 minutes to take this test.
- B. There are 80 problems on this test.
- II. How to write the answers:
  - A. For all problems except stated problem as noted below write three significant digits.
    - 1. Examples (\* means correct, but not recommended)

Correct:  $12.3, 123, 123.*, 1.23x10^*, 1.23x10^0*, 1.23x10^1, 1.23x10^{01}, .0190, 1.90x10^{-2}$ Incorrect:  $12.30, 123.0, 1.23(10)^2, 1.23\cdot10^2, 1.230x10^2, 1.23*10^2, 0.19, 1.9x10^{-2}, 19.0x10^{-3}, 1.90E-02$ 

- 2. Plus or minus one digit error in the third significant digit is permitted.
- B. For stated problems:
  - 1. Except for integer, dollar sign, and significant digit problems, as detailed below, answers to stated problems should be written with three significant digits.
  - 2. Integer problems are indicated by (integer) in the answer blank. Integer problems answers must be exact, no plus or minus one digit, no decimal point or scientific notation.
  - 3. Dollar sign (\$) problems should be answered to the exact cent, but plus or minus one cent error is permitted. The decimal point and cents are required for exact dollar answers.
- III. Some symbols used on the test.
  - A. Angle measure: rad means radians; deg means degrees.
  - B. Inverse trigonometric functions: arcsin for inverse sine, etc.
  - C. Special numbers:  $\pi$  for 3.14159 . . . ; e for 2.71828.
  - D. Logarithms: Log means common (base 10); Ln means natural (base e).

#### IV. Scoring:

A. All problems answered correctly are worth FIVE points. FOUR points will be deducted for all problems answered incorrectly or skipped before the last problem attempted.

# 2017-2018 Middle School Calculator Test 8

1.

8.

9.

697 + 2900 ------ 1=

-2.21 + 0.887 + 0.519 + 1.27 + 2.21 ------- 8=\_\_\_\_\_

712 x 219 x 133 ----- 9=

- 11. A pole casts a 14 meter shadow. Nate is 2 meters tall and casts a shadow 3.21 meters long. Calculate how tall the pole is in meters. 11=\_\_\_\_\_m

16. 
$$\left[ \frac{-286}{430} \right] [(73/142) + 0.382] ----- 16 = \underline{\hspace{1cm}}$$

17. 
$$\left\lceil \frac{44}{89} \right\rceil [(152/182) - 0.616]$$
 ----- 17=\_\_\_\_\_

21. 
$$\frac{501}{(406-160)} - \frac{(303-292)}{217} - \dots 21 = \underline{\hspace{1cm}}$$

- 24. Calculate the cost of a new \$24,989 car with a 7.25% sales tax. 24\$\_\_\_\_\_\_
- 25. Randy works at a feed store for \$11.85 per hour. He works 8 hours Monday Friday and then 4 hours of overtime on Saturday at 1.5 times pay. Calculate his pay for the week.

27. 
$$\frac{(101 + 21.8)(1.87 + \pi)}{(1.78 \times 10^{11})}$$
 ------ 27=\_\_\_\_\_

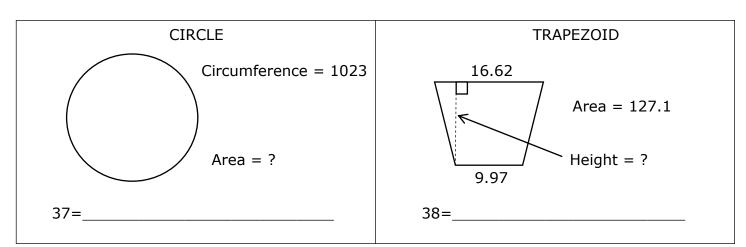
30. 
$$\frac{1}{0.766} + \frac{1}{(\pi)(0.552 - 0.244)} - \dots 30 = \dots$$

31. 
$$(7.4)[(1.12\times10^{-7}) - (1.52\times10^{-7})]$$
 ----- 31=\_\_\_\_

32. 
$$\frac{1}{17} + \frac{1}{(27.1 - 10.9)}$$
 ----- 32=\_\_\_\_

34. 
$$\left[\frac{1/600}{1/160}\right] + [0.157]$$
 ----- 34=\_\_\_\_

- 35. Glenn's Shoe Store has a BOGO sale going on. Buy one pair of shoes and get one of equal or lesser value at half price. Ann wants to purchase two pairs of shoes originally priced at \$89.98 and \$106.99. Calculate the cost of the two pairs of shoes if they are purchased at the BOGO sale, not including tax. ------ 35=\$\_\_\_\_\_\_\_
- 36. Larry can load the pallet in one hour, Mo can load the pallet in 0.8 hour and Curly can load the pallet in 1.2 hours. Calculate the time to load the pallet if they all work together. ------ 36=\_\_\_\_\_hrs.



39. 
$$\frac{(13200 + 2850)^3}{(0.113 - 0.366)^2} - \dots 39 = \dots$$

40. 
$$(1 + 1.58 + 0.672)^2(4.86 + 5.39)^2$$
 -----  $40 =$ 

41. 
$$\left[\frac{363}{39.5}\right](156 + 192)^3$$
 ----- 41=\_\_\_\_\_

42. 
$$\sqrt{(55.8/22.8) + 1.94 - 1.44}$$
 ----- 42=\_\_\_\_\_

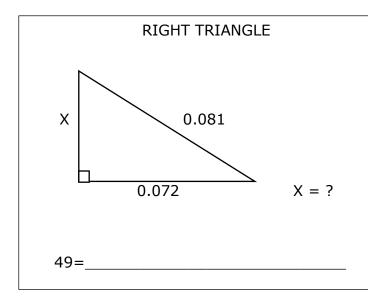
43. 
$$(89.4)\sqrt{113 + 64.8 + 87.3}$$
 ----- 43=\_\_\_\_\_

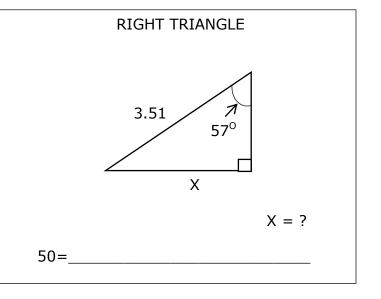
44. 
$$\sqrt{96.7 - 33.9 + 38.8} - \sqrt{50.2}$$
 ----- 44=\_\_\_\_\_

45. 
$$(21400)\sqrt{226 + 246 - 33.6}$$
 ----- 45=\_\_\_\_\_

46. 
$$\sqrt[3]{1.87 - 382/699} + 1/\sqrt{0.256 + 0.111}$$
 ----- 46=\_\_\_\_

48. A group of 40 coins is worth \$4.90 consists of only dimes and quarters. Calculate the number of dimes in the group. ------ 48=\_\_\_\_\_INT.





51. 
$$\frac{(51100 + 3.98 \times 10^5 - 2.37 \times 10^5)^4}{\sqrt{1.90 \times 10^5 + 1.08 \times 10^5 + 1.30 \times 10^5}} - \dots 51 = \dots 51 = \dots$$

54. 
$$2620 + \sqrt{(1750)(4960)} - (3630 + 2850)$$
 ----- 54=\_\_\_\_

55. 
$$\sqrt{\frac{(42000)(12300)}{(4170)(4.30\times10^5)}} - 0.241 + 0.465 ------ 55 = \underline{\phantom{0}}$$

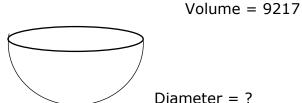
56. 
$$2.92 + \sqrt{(3250)/(325)} - (0.899 + 0.536)^2$$
 ----- 56=\_\_\_\_

57. 
$$\sqrt{\frac{1/(1700-1140)}{(2500)(39.5+109)^5}}$$
 ------ 57=\_\_\_\_

58. 
$$\sqrt{\frac{(68.3)(740)}{(81.4) + (26.2)}} + 1/(0.0462)^{1}$$
 ----- 58=\_\_\_\_\_

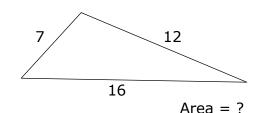
- 59. A canoe travels 15 miles downstream in 4 hours. In the same time it can travel 9 miles upstream. Calculate the rate of the current in miles per hour. -----mph.
- 60. Calculate the odds of rolling a sum of 7 on a pair of dice. ------ 60=\_\_\_\_\_

**HEMISPHERE** 



61=

SCALENE TRIANGLE



62=

<u>27!/22!</u> ----- 63=\_\_\_\_\_ 63.

(deg) (204 - 298)sin(152°) ------ 64=\_\_\_\_\_ 64.

 $(3.59 \times 10^7 - 3.05 \times 10^7)^4 (94100)$  ----- 65=\_\_\_\_\_ 65.

(rad)  $\sin \left[ \frac{(4.51)(\pi)}{(16.9)(1.3)} \right]$  ------ 66=\_\_\_\_\_ 66.

(deg) (526 - 549)tan(0.989°) + 0.196 ----- 67=\_\_\_\_\_ 67.

(deg)  $\frac{\sin(37.9^{\circ})}{\tan(37.9^{\circ})}[20.7]$  ------ 68=\_\_\_\_\_ 68.

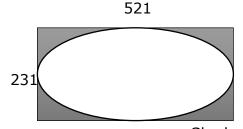
 $\frac{\tan(78.3^{\circ})}{1500 + 1740} - 69 = 69$ 69.

 $(629 - 714)e^{\pi - 0.304}$  ----- 70 =70.

The volume of a right circular cylinder is 27925 ft<sup>3</sup>. Calculate the length of the radius, if the height is 57 feet. ----- 71= ft.

72. Calculate the height of an equilateral triangle if a side measures 1911.91 inches. ----- 72= in.

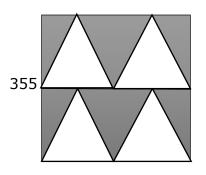
# **RECTANGLE AND ELLIPSE**



Shaded Area =?

73=\_\_\_\_\_

# SQUARE AND EQUIVALENT ISOSCELES TRIANGLES



Shaded Area = ?

74=\_\_\_\_\_

75. 
$$\frac{\text{Log}(448 + 1480)}{6.93 - 10.8} ----- 75 = _____$$

77. 
$$\frac{4350 - 15300}{\log(13800 + 12000)}$$
 ----- 77=\_\_\_\_

78. 
$$(3.73)^{\pi}(0.0351)^{3}(0.0842 - 0.0806)^{4}$$
 ----- 78=\_\_\_\_\_

80. 
$$1 + (0.86) + \frac{(0.86)^2}{2} + \frac{(0.86)^3}{6} + \frac{(0.86)^4}{24} - \dots 80 = \dots$$

# 2017-2018 TMSCA Middle School Calculator Test 8 Answer Key

Page 1	Page 2	Page 3	Page 4
$1 = 3600$ $= 3.60 \times 10^{3}$	14 = 119 = 1.19x10 <sup>2</sup>	$27 = 3.46 \times 10^{-9}$	$39 = 6.46 \times 10^{13}$
2 = 11.0 = $1.10 \times 10^{1}$	$15 = -6.62 \times 10^{-6}$	28 = -1.51x10 <sup>14</sup>	40 = 1110 = $1.11 \times 10^3$
$3 = 49.0$ $= 4.90 \times 10^{1}$	$16 = -0.596$ $= -5.96 \times 10^{-1}$	29 = -2.05x10 <sup>-12</sup>	$41 = 3.87 \times 10^{8}$ $42 = 1.72$
4 = -16.9 = $-1.69 \times 10^{1}$	$17 = 0.108$ $= 1.08 \times 10^{-1}$	30 = 2.34 = $2.34 \times 10^{0}$	$= 1.72 \times 10^{0}$ $43 = 1460$
5 = -534 = $-5.34 \times 10^2$	$18 = 0.0754$ $= 7.54 \times 10^{-2}$	$31 = -2.96 \times 10^{-7}$	$= 1.46 \times 10^{3}$ $44 = 2.99$ $= 2.99 \times 10^{0}$
$6 = -305$ $= -3.05 \times 10^{2}$	$19 = -31.1$ $= -3.11 \times 10^{1}$	$32 = 0.121$ $= 1.21 \times 10^{-1}$	$45 = 448000$ $= 4.48 \times 10^{5}$
7 = -2.52 = $-2.52 \times 10^{0}$	20 = 2.08 = $2.08 \times 10^{0}$	33 = -38.5 = $-3.85 \times 10^{1}$	$46 = 2.75$ $= 2.75 \times 10^{0}$
8 = 2.68 = $2.68 \times 10^{0}$	21 = 1.99 = $1.99 \times 10^{0}$	$34 = 0.424$ $= 4.24 \times 10^{-1}$	$47 = 2.94 \times 10^{-1400}$
$9 = 2.07 \times 10^7$	$22 = 1.25 \times 10^8$	35 = \$151.98	48 = 34 INT.
$10 = 1.73 \times 10^{11}$	$23 = -5.07$ $= -5.07 \times 10^{0}$	$36 = 0.324$ $= 3.24 \times 10^{-1}$	49 = 0.0371 -2
$11 = 8.72$ $= 8.72 \times 10^{0}$	24 = \$26800.70	37 = 83300	$= 3.71 \times 10^{-2}$
12 = 56 INT.	25 = \$545.10	$= 8.33 \times 10^4$	50 = 2.94 = $2.94 \times 10^{0}$
13 = 48.0 = $4.80 \times 10^{1}$	26 = 9 INT.	$38 = 9.56$ $= 9.56 \times 10^{0}$	

# 2017-2018 TMSCA Middle School Calculator Test 8 Answer Key

Page 5	Page 6	Page 7
$51 = 3.09 \times 10^{18}$	61 = 32.8 = $3.28 \times 10^{1}$	$73 = 25800$ $= 2.58 \times 10^4$
$52 = 6.75 \times 10^8$	$62 = 38.9$ $= 3.89 \times 10^{1}$	74 = 63000
53 = -137 = $-1.37 \times 10^2$	$63 = 236$ $= 2.36 \times 10^{2}$	$= 6.30 \times 10^4$
54 = -914 = $-9.14 \times 10^2$	$64 = -44.1$ $= -4.41 \times 10^{1}$	$75 = -0.849$ $= -8.49 \times 10^{-1}$
	$65 = 8.00 \times 10^{31}$	$76 = 2.03 \times 10^6$
$55 = 0.761$ $= 7.61 \times 10^{-1}$	$66 = 0.601$ $= 6.01 \times 10^{-1}$	77 = -2480
$56 = 4.02$ $= 4.02 \times 10^{0}$	$67 = -0.201$ $= -2.01 \times 10^{-1}$	$= -2.48 \times 10^3$
57 = 3.14×10 <sup>-9</sup>	$68 = 16.3$ $= 1.63 \times 10^{1}$	$78 = 4.54 \times 10^{-13}$
58 = 43.3	$69 = 0.00149$ $= 1.49 \times 10^{-3}$	$79 = 12500$ $= 1.25 \times 10^{4}$
$= 4.33 \times 10^{1}$	$70 = -1450$ $= -1.45 \times 10^{3}$	$80 = 2.36$ $= 2.36 \times 10^{0}$
$59 = 0.750$ $= 7.50 \times 10^{-1}$	71 = 12.5 = $1.25 \times 10^{1}$	
$60 = 0.200$ $= 2.00 \times 10^{-1}$	$72 = 1660$ $= 1.66 \times 10^{3}$	

**11.** 
$$\frac{x}{14} = \frac{2}{3.21}$$
 so  $x = \frac{2(14)}{3.21}$ 

**12.** 
$$\frac{8}{15}$$
 are boys.  $\frac{8}{15}$  (105)

**13.** Length = 
$$\frac{240}{5}$$

**26.** Mode is the number that appears most frequently. 9

# 36.

	Work	Time	Part of
	Rate		work
			done
Larry	1	Х	1x
Мо	1/.8	Х	(1/.8)x
Curly	1/1.2	Х	(1/1.2)x

The work rate is the fraction of the job that can be done in one hour. The "Part of work done" is the fraction of the complete job each man does in x hours.

A complete job = 1
$$1x + \frac{1}{.8}x + \frac{1}{1.2}x = 1 job$$

$$x = \frac{1}{\left(1 + \frac{1}{.8} + \frac{1}{1.2}\right)}$$

**37.** C = 
$$2\pi r$$
, so  $r = \frac{C}{2\pi}$   
Area =  $\pi r^2$   $A = \left(\frac{1023}{2\pi}\right)^2$ 

**38.** 
$$127.1 = \frac{1}{2}[(16.62 + 9.97)h]$$

$$h = \frac{127.1(2)}{(16.62 + 9.97)}$$

digits to the left of the decimal. This gives
-1399 for the exponent.
Write down -1399.) Then punch\_\_\_\_

(This gives 2.94 E-1. 2.94 is the first part of your answer. Since you have E-1, you have to add negative 1 to negative 1399.

The answer is **2.94 x 10**<sup>-1400</sup>). This is done on the HP RPN calculator.

**49.** 
$$\sqrt{.081^2 - .072^2}$$

**50.** 
$$\frac{\sin 57}{1} = \frac{x}{3.51}$$
 so

$$x = 3.51(\sin 57)$$

**59.** Use 
$$r = \frac{d}{t}$$
 b = canoe rate

c = current rate

$$b + c = \frac{15}{4}$$
;  $b - c = \frac{9}{4}$   
Solve the system.  $2c = 6/4$  so  $c = .750$ 

### 60.

There are 6 ways to roll a 7 and 30 ways to not roll a 7.

$$\frac{6}{30}$$

**61.** 
$$9217 = \frac{2}{3}\pi r^3$$

$$r = \sqrt[3]{\frac{9217(3)}{2\pi}}$$

Double this answer for the diameter.

# **62**.

 $\sqrt{s(s-a)(s-b)(s-c)}$  where s = semiperimeter

$$s = \frac{7 + 12 + 16}{2} = 17.5$$

Substitute 17.5 for s and 7,12,16 for a,b,c.

71. 
$$V = \pi r^2 h$$
;  
 $27925 = \pi r^2 (57)$   
 $r = \sqrt{\frac{27925}{57\pi}}$ 

**72.** h= 
$$\frac{side}{2}\sqrt{3} = \frac{1911.91}{2}\sqrt{3}$$

**73.** Area of rectangle minus area of ellipse

$$521(231) - \left(\frac{521}{2} \cdot \frac{231}{2}\right) \pi$$

**74.** The 4 white triangles = sum of the shaded triangles so the shaded area =  $\frac{1}{2}$  the area of the square.

$$\frac{355^2}{2}$$