1st Score:	2nd Score:	3rd Score:						
Grader:	Grader:	Grader:	Final Score					
PLACE LABEL BELOW								
Name:		School:						
SS/ID Number:		City:						
Grade: 4 5 6	7 8 Cla	ssification: 1A 2A	3A	4A	5A	6A		

Academic Excellence in Mathematics and Science through Competition T M S C A							
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## TMSCA MIDDLE SCHOOL NUMBER SENSE TEST #13© FEBRUARY 23, 2019

## **GENERAL DIRECTIONS**

- 1. Write only the requested information on this coversheet. Do not make any additional marks on this cover sheet.
- 2. You will be given 10 minutes to take this test.
- 3. There are 80 problems on the test.
- 4. Write in ink only! It would be advantageous to use <u>non-black</u> ink.
- 5. Solve as many problems as you can in the order that they appear.
- 6. Problems that are skipped are considered wrong.
- 7. Problems that appear after the last attempted problem do not count either for or against you.
- 8. ALL PROBLEMS ARE TO BE SOLVED MENTALLY! [No scratch work!]
- 9. Only the answer may be written in the answer blank.
- 10. Starred [\*] problems require approximate INTEGRAL answers that are within 5% of the exact answers. All other problems require exact answers.
- 11. All problems answered correctly are worth <u>FIVE</u> points. <u>FOUR</u> points will be deducted for all problems answered incorrectly or skipped before the last problem attempted.

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## 2018 – 2019 TMSCA Middle School Number Sense Test #13

$$(8) 2 \times 3 \times 4 \times 5 \div 6 = \underline{\hspace{1cm}}$$

(9) 
$$\frac{4}{9} \times 72 =$$
\_\_\_\_\_

(11) 
$$17 \times 41 + 63 \times 41 + 20 \times 41 =$$

$$(12) 81 \times 12 =$$

$$(13) \ 31^2 = \underline{\hspace{1cm}}$$

$$(18) \ \ 24 \times 12 \, \frac{1}{2} = \underline{\hspace{1cm}}$$

$$(21) 16 + 37 - 21 \div 3 - 6^2 = \underline{\hspace{1cm}}$$

$$(23) 1 + 2 + 3 + 4 + \dots + 100 = \underline{\hspace{1cm}}$$

(25) 
$$54 \times 33\frac{1}{3} \times 18 =$$

(28) The square root of 
$$\frac{121}{16}$$
 is \_\_\_\_\_ (mixed number)

$$(31) \ 35^2 = \underline{\hspace{1cm}}$$

(33) 
$$\frac{4}{11} + \frac{11}{4} =$$
 \_\_\_\_\_\_(mixed number)

$$(35) 19^2 + 57^2 = \underline{\hspace{1cm}}$$

(36) 
$$19\frac{2}{7} \times 19\frac{5}{7} =$$
 (mixed number)

\*(40) 33 
$$\frac{1}{3}$$
 % of  $\frac{1}{2}$  of 27599 is\_\_\_\_\_

(41) If 
$$f(x) = 9x^2 - 12x + 4$$
  
and  $f(24) = k^2$ ,  $k > 0$ , then  $k =$ \_\_\_\_\_

(42) If 
$$\frac{3x-4}{7} = 8$$
, then  $x =$ \_\_\_\_\_

$$(43) \ \ 213_7 = \underline{\hspace{1cm}}_{10}$$

$$(44) 15^3 =$$

- $(45) \sqrt{9801} =$
- $(46) 93^2 17^2 = \underline{\hspace{1cm}}$
- $(47) \ \ 39^2 + 31^2 = \underline{\hspace{1cm}}$
- (48) The 15<sup>th</sup> pentagonal number is equal to 15k, k = \_\_\_\_\_
- (49) The measure of the interior angle of a 36-sided polygon is\_\_\_\_\_°
- \*(50) The area of a square with diagonal  $450\sqrt{2}$  is\_\_\_\_\_
- $(51) 67^2 + 64^2 = \underline{\hspace{1cm}}$
- (52) If f(3x + 2) = 4x + 5, then f(23) =
- (53) The sum of the solutions of |3x 4| = 19 is\_\_\_\_\_
- (54)  $11^{17} \div 17$  has a remainder of \_\_\_\_\_\_
- (55) How many terms are in the sequence 19, 27, 35, 43, ..., 139?
- (56) If  $8^x = 125$ , then  $4^x =$
- (57) If x(x+5) < 130, then the largest integer solution is x =
- $(58) \ \ 234_6 52_6 = \underline{\hspace{2cm}}_6$
- (59) The sum of the 8<sup>th</sup> and 9<sup>th</sup> triangular numbers is\_\_\_\_\_
- \*(60) If three consecutive integers have a product of 274560, then the middle integer is\_\_\_\_\_
- (61) If f(x) is a linear function of slope  $-\frac{5}{3}$  and f(4) = 27, then f(10) =\_\_\_\_\_
- $(62) (23_9)^2 =$
- (63) 45 × 85 =\_\_\_\_\_

- (64)  $0.878787... = \frac{a}{b}$ , where a and b have no common factors, then  $a + b = \underline{\hspace{1cm}}$
- (65) If 3x 7y = 12 is perpendicular to 35x + by = 100, then b =\_\_\_\_\_
- (66) If  $7 \times 8 \times 9 \times 10 + 1 = k^2$ , k > 0, then  $k = _____$
- (67) If the inner diagonal of a cube is  $7\sqrt{3}$ , the volume is \_\_\_\_\_
- (68) The discriminant of  $4x^2 7x 1 = 0$  is\_\_\_\_\_\_
- $(69) \sqrt{39^2 36^2} = \underline{\hspace{1cm}}$
- \*(70) The area of an equilateral triangle with side 60 is
- (71) If  $y = 3(x-2)^2 + k$  has a y-intercept of 14, then k =\_\_\_\_\_
- (72) How many positive integers less than 99 are relatively prime to 99? \_\_\_\_\_\_
- (73) If the two roots of  $f(x) = x^2 + bx + c$  are - 3 and 17, then the axis of symmetry is x =\_\_\_\_\_
- (74) The sum of the infinite geometric series 10 + 4 + 1.6 + ... = \_\_\_\_\_
- $(75) \quad \frac{3! + 4! + 5!}{3!} = \underline{\hspace{1cm}}$
- (76) The first 4 decimal places of  $\frac{231}{900}$  is 0.\_\_\_\_\_
- (77) The number of triangles which can be drawn from any vertex of a dodecagon is
- (78) How many nonnegative integers ordered pairs are solutions of 3x + 5y = 90?
- (79) If  $4^{2x+3} = 1600$ , then  $4^x =$
- \*(80) 102 × 104 × 107 =

## 2018-2019 TMSCA Middle School Number Sense Key #13

(1) 4037	(25) 32400	(45) 99	
(2) 248	(26) 6	(46) 8360	(64) 62
(3) 441	(27) 198	(47) 2482	(65) 15
(4) 2100			(66) 71
(5) 1400	(28) $2\frac{3}{4}$	(48) 22	(66) 71
(6) 13	(29) 4.25	(49) 170	(67) 343
(7) 2	*(30) 30689 – 33919		(68) 65
(8) 20	(31) 1225	*(50) 192375 – 212625	(69) 15
(9) 32	(32) 463	(51) 8585	
*(10) 4990 – 5514	$(33) \ 3\frac{5}{44}$	(52) 33	*(70) 1481 – 1636
(11) 4100		(53) $\frac{8}{3}$ or $2\frac{2}{3}$	(71) 3
(12) 972	(34) 28583	(54) 11	(71) 2
(13) 961	(35) 3610		(72) 60
(14) 8924	$(36) \ 380 \frac{10}{49}$	(55) 16	(52) 5
		(56) 25	(73) 7
(15) 29	(37) 3		50 2
(16) 2300		(57) 9	(74) $\frac{50}{3}$ or $16\frac{2}{3}$
(17) 11016		(58) 142	(75) 25
(18) 300	(38) 9	()	(75) 25
(10) 300	(39) 9	(59) 81	(76) 2566
(19) 3441	*(40) 4370 – 4829	,	
*(20) 29215 – 32289		*(60) 62 – 68	(77) 220
(21) 10	(41) 70		(79) 7
(22) 2464	(42) 20	(61) 17	(78) 7
	(43) 108	(62) 540	(79) 5
(23) 5050	(-5) 200	(62) 540	*(\$0) 1078304 1101808

(63) 3825

(44) 3375

(24) 302.1

\*(80) 1078304 - 1191808