1st Score:	2nd Score:	3rd Score:					
Grader:	Grader:	Grader:	-	Final S	Score		
PLACE LABEL BELOW							
Name:		School:					
SS/ID Number:	(	City:					
Grade: 5 6 7	8 Cla	ssification: 1A 2A	3A	4A	5A	6A	

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# TMSCA MIDDLE SCHOOL NUMBER SENSE TEST #5© NOVEMBER 18, 2017

### **GENERAL DIRECTIONS**

- 1. Write only the requested information on this coversheet. Do not make any additional marks on this cover sheet.
- 2. You will be given 10 minutes to take this test.
- 3. There are 80 problems on the test.
- 4. Write in ink only! It would be advantageous to use <u>non-black</u> ink.
- 5. Solve as many problems as you can in the order that they appear.
- 6. Problems that are skipped are considered wrong.
- 7. Problems that appear after the last attempted problem do not count either for or against you.
- 8. ALL PROBLEMS ARE TO BE SOLVED MENTALLY! [No scratch work!]
- 9. Only the answer may be written in the answer blank.
- 10. Starred [\*] problems require approximate INTEGRAL answers that are within 5% of the exact answers. All other problems require exact answers.
- 11. All problems answered correctly are worth <u>FIVE</u> points. <u>FOUR</u> points will be deducted for all problems answered incorrectly or skipped before the last problem attempted.

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## 2017 – 2018 TMSCA Middle School Number Sense Test 5

(2) 
$$83 \times 50 =$$

$$(7) \quad \frac{4+8+12+16+20}{4} = \underline{\hspace{2cm}}$$

(8) 
$$\frac{8}{25} =$$
\_\_\_\_\_(decimal)

(9) 
$$\frac{9}{11} \times 121 =$$
\_\_\_\_\_

(11) Which of the following is greater 
$$\frac{18}{25}$$
 or  $\frac{7}{10}$ ?

$$(13) \ 66\frac{2}{3} \times 87 = \underline{\hspace{1cm}}$$

(15) 
$$14 \times 92 + 16 \times 92 =$$

$$(16) \ \frac{1+3+5+...+35}{9} = \underline{\hspace{2cm}}$$

$$(21) 32^2 = \underline{\hspace{1cm}}$$

$$(23) 11^3 =$$

(27) 
$$17^2 \div 9$$
 has a remainder of

\*(30) 
$$19^3 + 20^3 + 21^3 =$$

$$(33) 19^2 + 57^2 = \underline{\hspace{1cm}}$$

$$(34) 72^2 + 13^2 = \underline{\hspace{1cm}}$$

(37) 
$$\frac{5}{11} + \frac{11}{5} =$$
 (mixed number)

(38) 
$$9\frac{4}{7} \times 9\frac{3}{7} =$$
\_\_\_\_\_(mixed number)

(39) If 
$$134^2 = 17956$$
, then  $139 \times 129 =$ 

$$(41) \sqrt{4096} =$$

(43) The area of a square with diagonal 
$$7\sqrt{6}$$
 is

- (44)  $f(x) = 4x^2 7x + 4$ . f(3) =
- (45) The sum of the interior angles of an undecagon is \_\_\_\_\_\_°
- (46) How many triangles can be drawn using any three vertices of a hexagon?\_\_\_\_\_
- (48) If  $1+3+5+...+k=28^2$ , then k=\_\_\_\_\_
- (49) The sum of the solutions of |x+4| = 7 is\_\_\_\_\_
- \*(50)  $\sqrt{562 \times 529} =$
- (51) A set with 7 elements has how many subsets with an even number of elements?\_\_\_\_\_
- (52)  $12 \times \frac{13}{16} =$  (mixed number)
- $(53) 77^2 33^2 = \underline{\hspace{1cm}}$
- (54) The area of a regular hexagon with side 16 is  $k\sqrt{3}$ , k =
- (55) 4+11+18+25+...+60=\_\_\_\_\_
- (56) If f(x) = 14x + 4, then  $f(19) f(3) = ______$
- (57) 283<sub>9</sub> 35<sub>9</sub> = \_\_\_\_\_\_\_
- (58)  $(9^4 + 7^4) \div 7$  has a remainder of \_\_\_\_\_
- (59) 1 + 2 + 3 + ... + 49 =\_\_\_\_\_
- \*(60) 98 × 97 × 94 =\_\_\_\_\_
- (61) If x < 0 and  $x^4 = 256$ , then  $x^3 =$
- (62) If  $f(x) = x^2 + 5$ , then f(13) f(7) =
- (63) The sum of the infinite geometric series, 20 + 15 + 11.25 + ... = \_\_\_\_\_

- (64) 9021 = 93 × \_\_\_\_\_
- (65) If  $12^2 + 24^2 + 12^2 + 36^2 = (12^2)$  k, then k =
- (66) 0.343434... = \_\_\_\_\_(fraction)
- (67) If 11≤5x+1≤106, then x has how many integer solutions?\_\_\_\_\_
- (68) Find the sum of the 13<sup>th</sup> and 14<sup>th</sup> triangular number.
- (69)  $1_8 + 2_8 + 3_8 + \dots + 11_8 =$
- \*(70) The area of a circle with radius 32 is \_\_\_\_\_
- (71) The number of positive integral divisors less than 38 that are relatively prime to 38 is\_\_\_\_\_
- (72) If the sum of the coefficients in the expansion of  $(5x-2)^4$  is
- (73) The sum of the integral solutions of  $|x + 3| \le 13$  is\_\_\_\_\_
- (74)  $\log_6 9 + \log_6 16 \log_6 4 =$
- (75) f(x) is a parabola with a vertex of (3, -2) and g(x) = 4f(x-2) + 5. g(x) has a vertex of (h,k). h =
- (76) Find the probability of choosing a perfect cube from the smallest 30 positive integers. \_\_\_\_\_
- (77)  $\frac{(n+3)!}{(n-2)!}$  is a polynomial of degree\_\_\_\_\_
- (78) If  $f(x) = (x^2 3x 2)(x^2 4x + 4)$ , then f(x) has how many distinct real roots?
- (79) P and Q are roots of  $4x^2 17x + 10 = 0$ . The arithmetic mean of P and Q is \_\_\_\_\_\_
- \*(80) A cone with a height of 25 and radius of 6 has a volume of

# 2017-2018 TMSCA Middle School Number Sense Key #5

			-
(1) 1130	(23) 1331	(44) 19	(64) 97
(2) 4150	(24) 79574		(65) 15
(3) $\frac{2}{5}$	(25) 3108	(45) 1620	$(66) \ \frac{34}{99}$
(4) 594	(26) 12	(46) 20	
(5) 216	(27) 1	(47) 884	(67) 20
(6) 5	(28) 275	(48) 55	(60) 106
(0) 3	(28) 375	(49) -8	(68) 196
(7) 15	(29) 49	*(50) 518 – 572	(69) 55
(8) .32			*(70) 3057 – 3377
(9) 99	*(30) 22914 – 25326	(51) 64	(71) 18
*(10) 2718 – 3004	(31) 216	$(52) 9\frac{3}{4}$	. ,
$(11) \frac{18}{25}$	(32) 13.20	(53) 4840	(72) 81
	(33) 3610	(54) 294	(73) – 81
(12) 13224	(34) 5353	(54) 384	(74) 2
(13) 5800		(55) 288	
(14) 2	(35) 323	(56) 224	
(15) 2760	(36) 12	(57) 247	(75) 5
(16) 36	$(37) \ 2\frac{36}{55}$	(58) 2	
(10) 30	$(37)^{2}\frac{1}{55}$	(59) 1225	$(76) \frac{1}{10}$
(17) 1649	$(38) 90\frac{12}{49}$	*(60) 848886 – 938242	(77) 5
(18) 24216	(39) 17931	(61) -64	(11) 5
(19) 896	*(40) 3868708 – 4275940	(62) 120	(78) 3
*(20) 530730 - 586596	(41) 64	(62) 00	(79) $\frac{17}{2}$ , $2\frac{1}{2}$ , or 2.125

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(63) 80

(41) 64

(42) 16

(43) 147

(21) 1024

(22) 9702

(79)  $\frac{17}{8}$ ,  $2\frac{1}{8}$ , or 2.125

\*(80) 896 - 989