Prim Algorithm: Minimum Spanning Tree

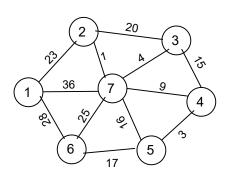
Data structures

- 1. U set and V-U set
- 1.1 U set: vertexes which become MST members
- 1.2 V-S set: vertexes which are not MST members yet
- 2. lowcost[] least weights of each vertex
- 3. closest[] vertexes in V-S which closest to U

Always in V-U set

- 1. update lowcost[] and closest[] using current adjacent edges
- 2. find the index of least in lowcost[]





| 1 | -> | 2(23) 6(28) 7(36) |
|---|----|----------------------------------|
| 2 | -> | 1(23) 3(20) 7(1) |
| 3 | -> | 2(20) 4(15) 7(4) |
| 4 | -> | 3(15) 5(3) 7(9) |
| 5 | -> | 4(3) 6(17) 7(16) |
| 6 | -> | 1(28) 5(17) 7(25) |
| 7 | -> | 1(36) 2(1) 3(4) 4(9) 5(16) 6(25) |

Initialization

S={}, V-S={1,2,3,4,5,6,7}

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|----|----|----|----|----|
| lowcost | 0 | ∞ | ∞ | ∞ | ∞ | ∞ | ∞ |
| closest | -1 | -1 | -1 | -1 | -1 | -1 | -1 |

Step2

S={1,2}, V-S={3,4,5,6,7}

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|----|----|----|----|---|
| lowcost | 0 | 23 | 20 | ∞ | ∞ | 28 | 1 |
| closest | -1 | 1 | 2 | -1 | -1 | 1 | 2 |

Step4

S={1,2,7,3}, V-S={4,5,6}

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|---|---|----|----|---|
| lowcost | 0 | 23 | 4 | 9 | 16 | 25 | 1 |
| closest | -1 | 1 | 7 | 7 | 7 | 7 | 2 |

Step6

S={1,2,7,3,4,5}, V-S={6}

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|---|---|---|----|---|
| lowcost | 0 | 23 | 4 | 9 | 3 | 17 | 1 |
| closest | -1 | 1 | 7 | 7 | 4 | 5 | 2 |

Step1 S={1}, V-S={2,3,4,5,6,7}

| Х | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|----|----|----|----|----|
| lowcost | 0 | 23 | ∞ | ∞ | ∞ | 28 | 36 |
| closest | -1 | 1 | -1 | -1 | -1 | 1 | 1 |

Step3 S={1,2,7}, V-S={3,4,5,6}

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|---|---|----|----|---|
| lowcost | 0 | 23 | 4 | 9 | 16 | 25 | 1 |
| closest | -1 | 1 | 7 | 7 | 7 | 7 | 2 |

Step5 S={1,2,7,3,4}, V-S={5,6}

| Х | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|---|---|---|----|---|
| lowcost | 0 | 23 | 4 | 9 | 3 | 25 | 1 |
| closest | -1 | 1 | 7 | 7 | 4 | 7 | 2 |

Step7 S={1,2,7,3,4,5,6}, V-S={}

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------|----|----|---|---|---|----|---|
| lowcost | 0 | 23 | 4 | 9 | 3 | 17 | 1 |
| closest | -1 | 1 | 7 | 7 | 4 | 5 | 2 |