CSCI 3150 Tutorial 3 - Virtual Memory

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Agenda

- Some sample questions related to virtual memory for the assignment and exams
 - Calculation: given the configuration of virtual memory, calculate some parameters
 - Address translation: given the page mapping and some virtual addresses (VA), find out the corresponding physical addresses (PA)
 - Page table setup: given the relationship between PA and VA, set up the page tables that represents the mapping

Sample Question - Calculation

- Suppose the page size is 8 bytes, the first-level page table has 4 entries and the second-level page table has 8 entries.
 - What is the size of the virtual address space?
 - 2 How many bits does a virtual address have?
 - 4 How many bits should be reserved for the first-level page table index, the second-level page table index and the offset respectively?

First-level index (__ bits) | Second-level index (__ bits) | Offset (__ bits)

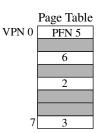
- What is the size of the virtual address space?
 - The 2^{nd} -level page table has 8 entries (pages of 8 bytes) \Rightarrow one 2^{nd} -level page table maps to $8 \times 8 = 64$ bytes
 - The 1^{st} -level page table has 4 entries (referencing 2^{nd} -level page tables) \Rightarrow one 1^{st} -level page table maps to $4 \times 64 = 256$ bytes
 - ullet The 1^{st} -level page table is also the top level, thus the virtual address space has 256 bytes
- How many bits does a virtual address have?
 - ullet The virtual address space has 256 bytes \Rightarrow we have 256 unique VAs
 - $256 = 2^8$
 - Thus we need 8 bits for a VA

- How many bits should be reserved for the first-level page table index, the second-level page table index and the offset respectively?
 - A page has 8 bytes (8 unique offsets)
 - $8 = 2^3$
 - Need 3 bits to locate an offset inside a page
 - A 2nd -level page table has 8 entries
 - $8 = 2^3$
 - Need 3 bits to locate an entry inside a 2nd -level page table
 - For the same reason, we need 2 bits to locate an entry inside a 1st
 -level page table
 - Also notice that 3 + 3 + 2 = 8 is exactly the length of a VA

First-level index (bits)	Second-level index (bits)	Offset (bits)
riist-level ilidex (bits)	Second-level fildex (bits)	Oliset (bits)

Sample Question - Address Translation

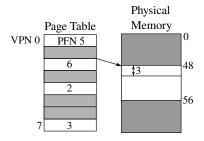
- Suppose page size is 8 bytes. Given the following page table:
 - Which of the virtual addresses are mapped?
 - 19, 45
 - What are the corresponding physical addresses for them if mapped?
- Numbers in entries are phyiscal page frame number (PFN)
- Entries in gray color are not mapped



- For VA=19
 - The virtual page number (VPN) is floor(19/8) = 2
 - You can also use bit-shift to calculate the VPN
 - Page size = $8 \Rightarrow$ offset has $3 (log_2 8)$ bits
 - VPN can be calculated by skipping (right-shift) all offset bits 19 >> 3 = 2
 - PT[2] = 6 so VPN 2 is mapped to PFN 6
- For VA=45
 - VPN is floor(45/8) = 5
 - PT[5] is not mapped

	Page Table
VPN 0	PFN 5
	6
	2
7	3

- We know that only VA=19 is mapped and it is mapped to PFN 6
 - The physical base address of the page is $6 \times 8 = 48$
- The offset of VA=19 within the virtual page is 19%8 = 3
- By adding the offset to the physical base address we can get the PA for VA=19
 - PA = 48 + 3 = 51



Sample Question - Two-Level Address Translation

- Page size is still 8 bytes but we have two levels (a page directory and some page tables)
- Translate the following VAs into PAs:
 - 34, 75, 100

Page Directory	PT@PFN=10	PT@PFN=11
0	0 5	0 3
10		
11		8
3	3 1	3

- A page size is 8 bytes and a PT has 4 entries \Rightarrow a PT maps $4 \times 8 = 32$ bytes
- For VA=34
 - First, we need to find out which PT maps this address
 - VPN1 = floor(34/32) = 1 so it's the second PT (page directory entry 1)
 - Using the page directory, we know that entry 1 is PT@PFN=10
 - The offset within that PT is 34%32 = 2
 - We can continue to PT@PFN=10 and find out the corresponding PA for the byte at offset 2 inside the PT

Page I	Directory		PT@PFN=10		PT@PFN=11
0		0	5	0	3
1	10				
	11				8
3		3	1	3	

- In PT@PFN=10, we want to find the PA for the byte at offset 2
- VPN2=floor(2/8)=0 so it's the first page in the PT (PFN=5)
- The offset inside that page is 2%8 = 2
- So the PA for VA=34 is $5 \times 8 + 2 = 42$

Page Directory	PT@PI	FN=10	PT@PFN=11
0	0 5	0	3
10			
11			8
3	3 1	3	

- Another way is to use the number of bits for each part that we calculate previously
- VPN1: 2 bits (4 entries), VPN2: 2 bits (4 entries), offset: 3 bits (8 bytes page size)
- The binary representation of 34 is 0100010_b
- Thus we can directly obtain VPN1 = $01_b = 1$, VPN2 = $00_b = 0$, Offset = $010_b = 2$
 - Page directory entry 1, page table entry 0 and page offset 2

VPN1 (2 bits) VPN2 (2 bits) Offset (3 bits)

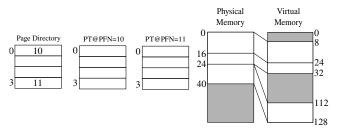
0 1 0 0 0 1 0

- For VA=75
 - VPN1=floor(75/32) = 2, page directory entry 2 is PT@PFN=11
 - Offset within that PT is 75%32 = 11
 - VPN2=floor(11/8)=1, entry 1 in PT@PFN=11 is not mapped
 - Thus VA=75 is not mapped
- For VA=100
 - VPN1=floor(100/32) = 3, page directory entry 3 is not mapped
 - Thus VA=100 is not mapped

Page Directory]	PT@PFN=10		PT@PFN=11
0	0	5	0	3
10				
11				8
3	3	1	3	

Sample Question - Page Mapping Setup

- A program has three pieces of data that should be loaded and mapped
 - Code segment is loaded at physical memory range [0, 16) and should be mapped to virtual memory range [8, 24)
 - 2 Data segment: PA [16, 24) and should be mapped to VA [24, 32)
 - 3 Stack segment: PA [24, 40) and should be mapped to VA [112, 128)
- You should fill in the following page tables to set up the page mapping



- The code segment has 2 pages: PA [0,8) (PFN=0) \rightarrow VA [8,16) and PA [8,16) (PFN=1) \rightarrow VA [16,24)
- For the first page, virtual base address is 8
 - VPN1 = floor(8/32) = 0, PT offset is 8%32 = 8
 - VPN2 = floor(8/8) = 1
- So it is the first page directory entry (PT@PFN=10) and the second page inside that PT
- We can fill the PFN in that entry

	Page Directory		PT@PFN=10		PT@PFN=11
0	10	0		0	
			0		
3	11	3		3	

Repeat this process for every page in every segment

	Page Directory
0	10
3	11

	PT@PFN=10
0	
	0
	1
3	2

PI@PFN=II
3
4