



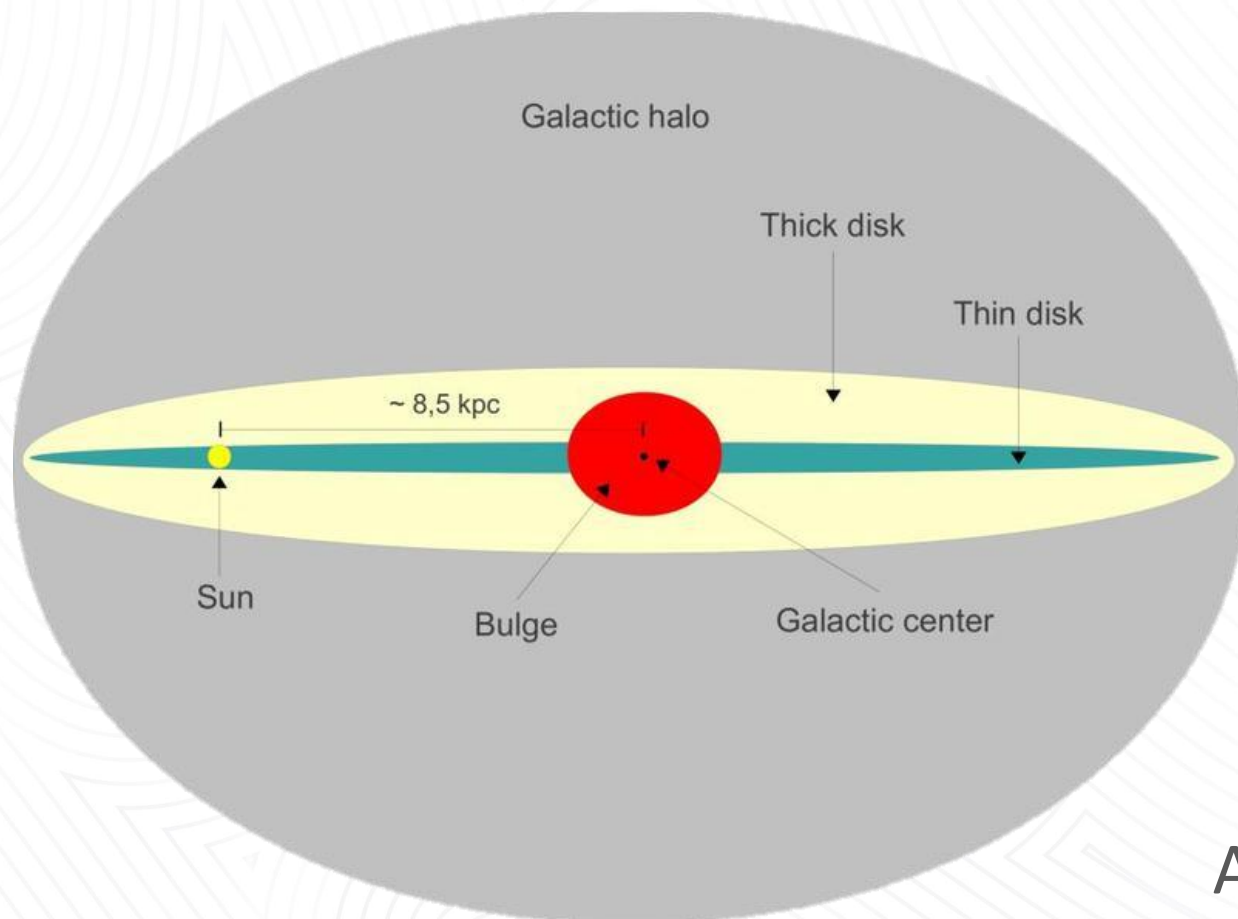
Dinámica de Galaxias

Dylan Castellanos y Juan Felipe Rodríguez

El modelo de galaxia

#LaUISqueQueremos

Universidad
Industrial de
Santander



Bulbo Galáctico

Discos Estelares

Discos de Gas

Aura de Materia Oscura

Los Datos Observacionales



- Eilers, et al., 2018 - *The Circular Velocity Curve of the Milky Way from 5 to 25 kpc.*

(5 – 25 kpc)

- Mroz, et al., 2019 - *Microlensing optical depth and event rate toward the Galactic bulge from 8 yr of OGLE-IV observations.*

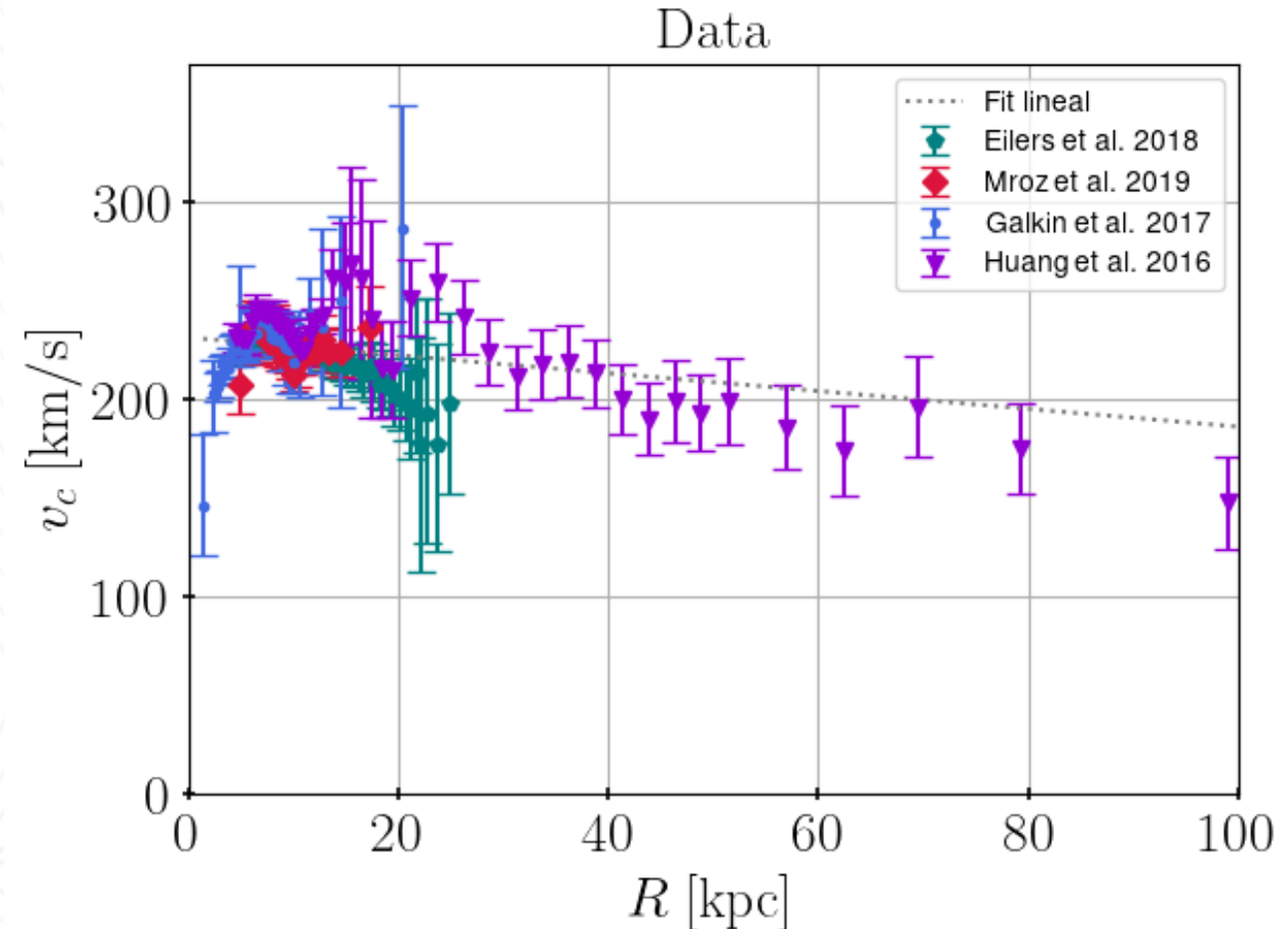
(5 – 20 kpc)

- Galkin, et al., 2017 - *A new compilation of the Milky Way rotation curve data.*

(1 – 20 kpc)

- Huang, et al., 2016 - *The Milky Way's rotation curve out to 100 kpc and its constraint on the Galactic mass distribution.*

(4 – 100 kpc)



Modelo matemático



Teorema del Virial

$$2K + U = 0$$

$$K = \frac{1}{2} m_s v^2 \quad U = \frac{-G M(r) m_s}{r}$$

Se halla v :

$$v = \sqrt{\frac{G M(r)}{r}}$$

Density profile **galactic bulge** (McMillan, 2016)

$$\rho_b = \frac{\rho_{0,b}}{(1 + r'/r_0)^\alpha} \exp \left[- (r'/r_{\text{cut}})^2 \right]$$

Density profile **stellar discs** (McMillan, 2016)

$$\rho_d(R, z) = \frac{\Sigma_0}{2z_d} \exp \left(-\frac{|z|}{z_d} - \frac{R}{R_d} \right)$$

Density profile **gas discs** (McMillan, 2016)

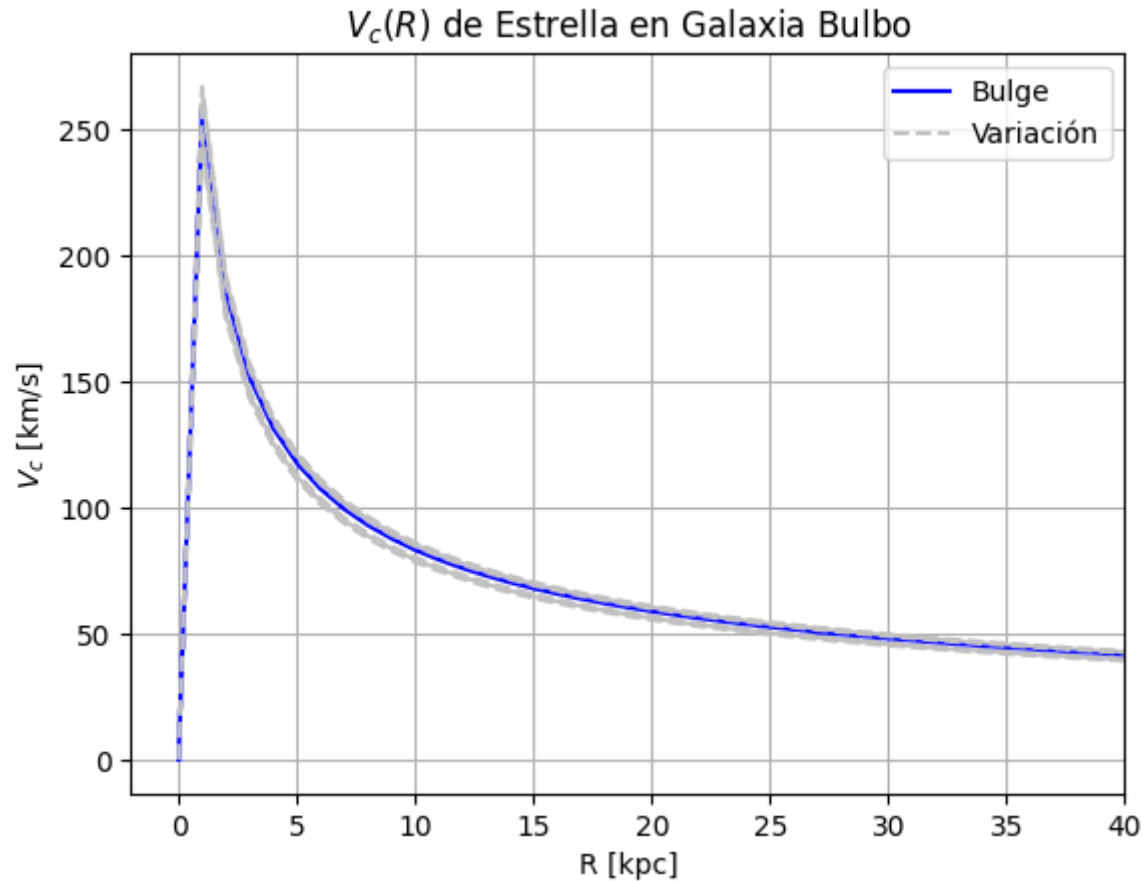
$$\rho_d(R, z) = \frac{\Sigma_0}{4z_d} \exp \left(-\frac{R_m}{R} - \frac{R}{R_d} \right) \text{sech}^2(z/2z_d)$$

Density profile dark matter halo

$$\rho(r) = \frac{\rho_{\text{crit}} \delta_c}{\left(\frac{r}{r_s} \right) \left(1 + \frac{r}{r_s} \right)^2}$$

(Navarro, Frenk, White, 1996)

Bulbo Galáctico



$$\rho_b = \frac{\rho_{0,b}}{(1 + r'/r_0)^\alpha} \exp \left[- (r'/r_{\text{cut}})^2 \right]$$

Best Fitting Model:

$$\rho_{0,b} = 9.84e10 \left[\frac{M_{\text{sun}}}{\text{kpc}^2} \right]$$

$$r_0 = 0.075 \text{ [kpc]} \text{ (fijo)}$$

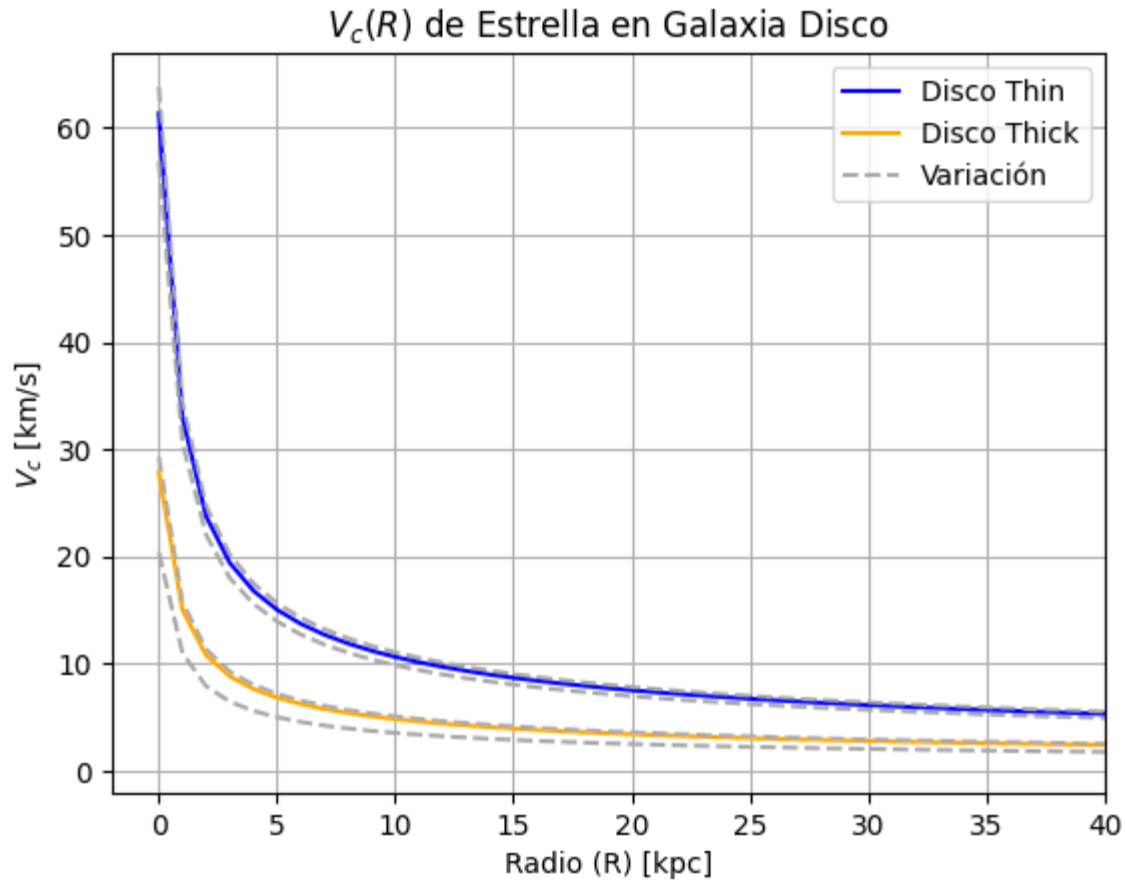
$$r_{\text{cut}} = 2.1 \text{ [kpc]} \text{ (fijo)}$$

$$\alpha = 1.8 \text{ (fijo)}$$

Variación de parámetros:

$$\rho_{0,b} = 9.73e10 \pm 9.7 \left[\frac{M_{\text{sun}}}{\text{kpc}^2} \right]$$

Disco Galáctico



$$\rho_d(R, z) = \frac{\Sigma_0}{2z_d} \exp\left(-\frac{|z|}{z_d} - \frac{R}{R_d}\right)$$

Best Fitting Model:

$$\Sigma_{0,thin} = 896e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$z_{d,thin} = 0.3 [kpc] \text{ (fijo)}$$

$$R_{d,thin} = 2.5 [kpc]$$

$$\Sigma_{0,thick} = 183e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$z_{d,thick} = 0.9 [kpc] \text{ (fijo)}$$

$$R_{d,thick} = 3.02 [kpc]$$

Variación de parámetros:

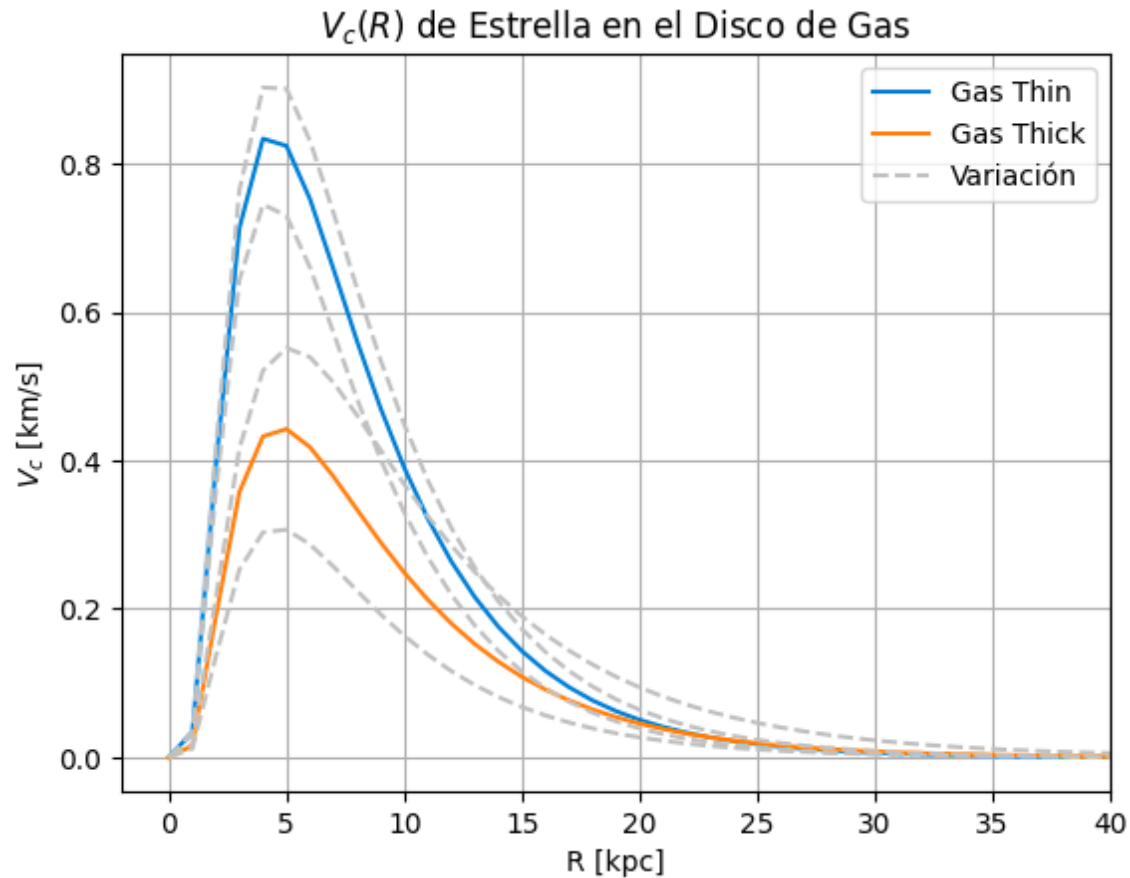
$$\Sigma_{0,thin} = 886.7e6 \pm 116.2e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$R_{d,thin} = 2.53 \pm 0.14 [kpc]$$

$$\Sigma_{0,thick} = 156.7e6 \pm 58.9e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$R_{d,thick} = 3.38 \pm 0.54 [kpc]$$

Disco de Gas



$$\rho_d(R, z) = \frac{\Sigma_0}{4z_d} \exp\left(-\frac{R_m}{R} - \frac{R}{R_d}\right) \text{sech}^2(z/2z_d).$$

Best Fitting Model:

$$\Sigma_{0,thin} = 896e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$R_{d,thin} = 2.5 [kpc]$$

$$R_m = 12.0 [kpc] \text{ (fijo)}$$

$$z_{d,gas} = 0.045 [kpc] \text{ (fijo)}$$

$$\Sigma_{0,thick} = 183e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$R_{d,thick} = 3.02 [kpc]$$

Variación de parámetros:

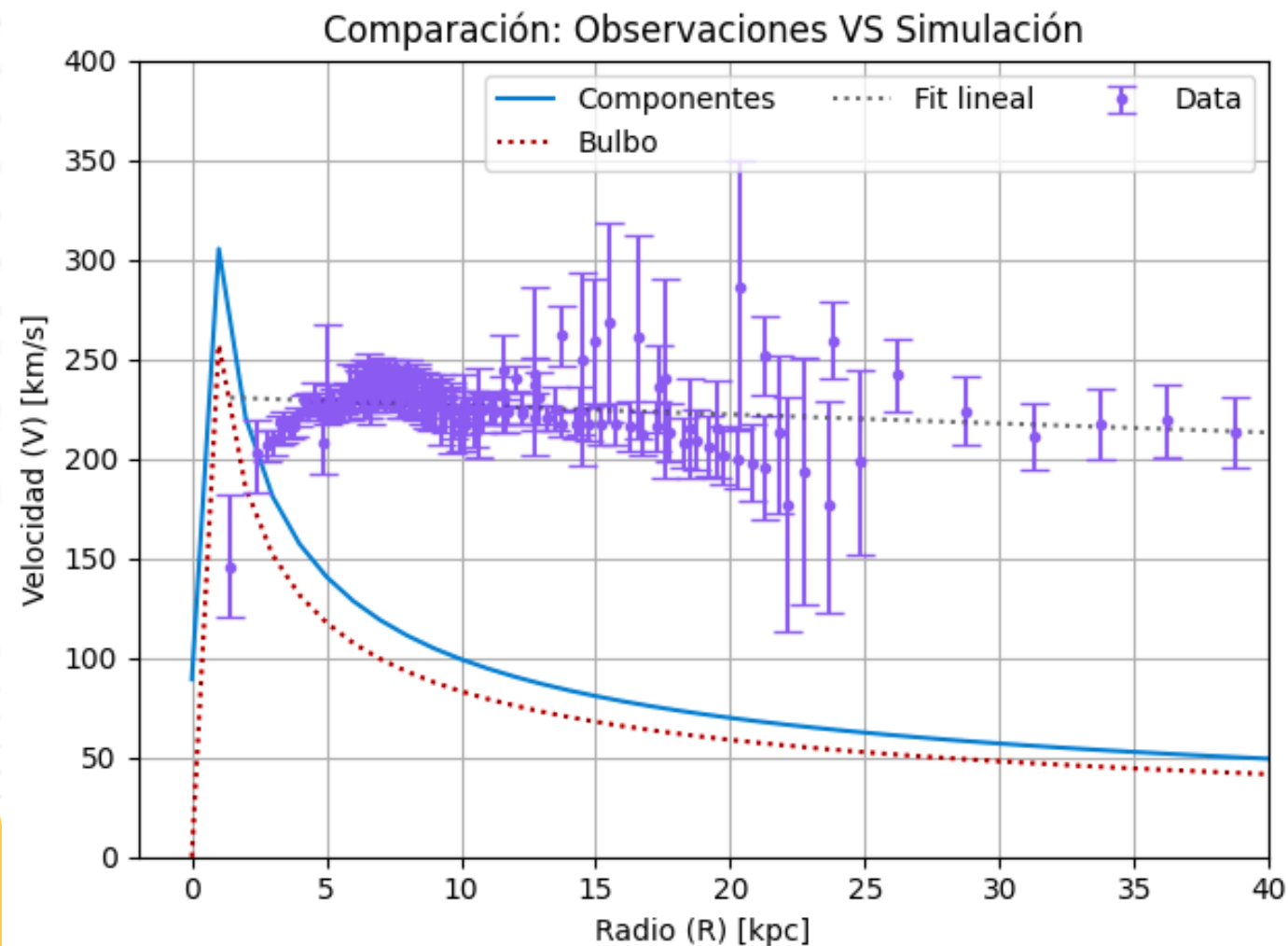
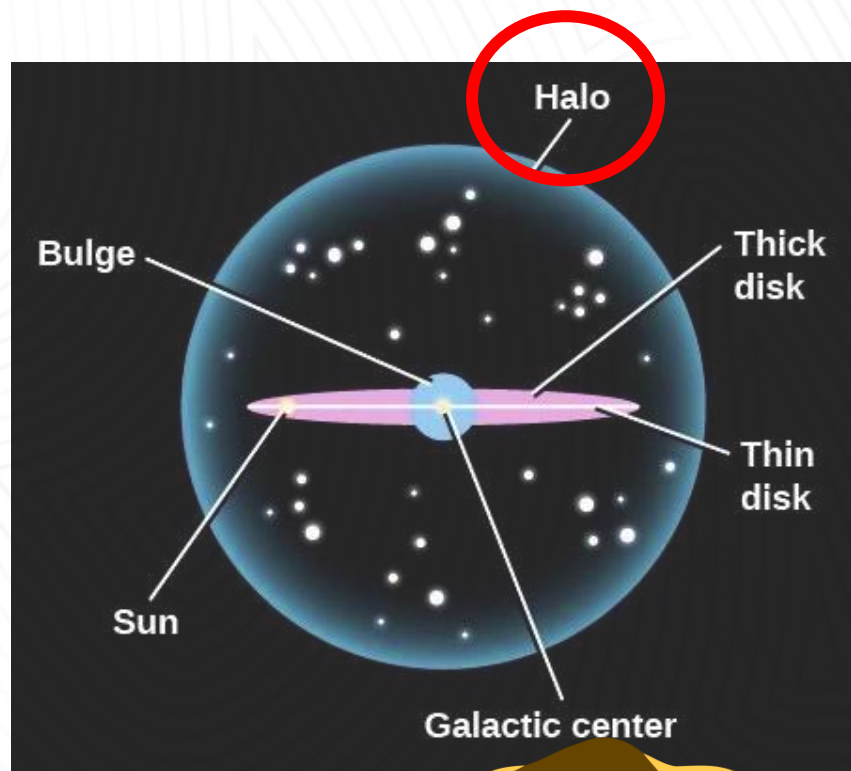
$$\Sigma_{0,thin} = 886.7e6 \pm 116.2e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$R_{d,thin} = 2.53 \pm 0.14 [kpc]$$

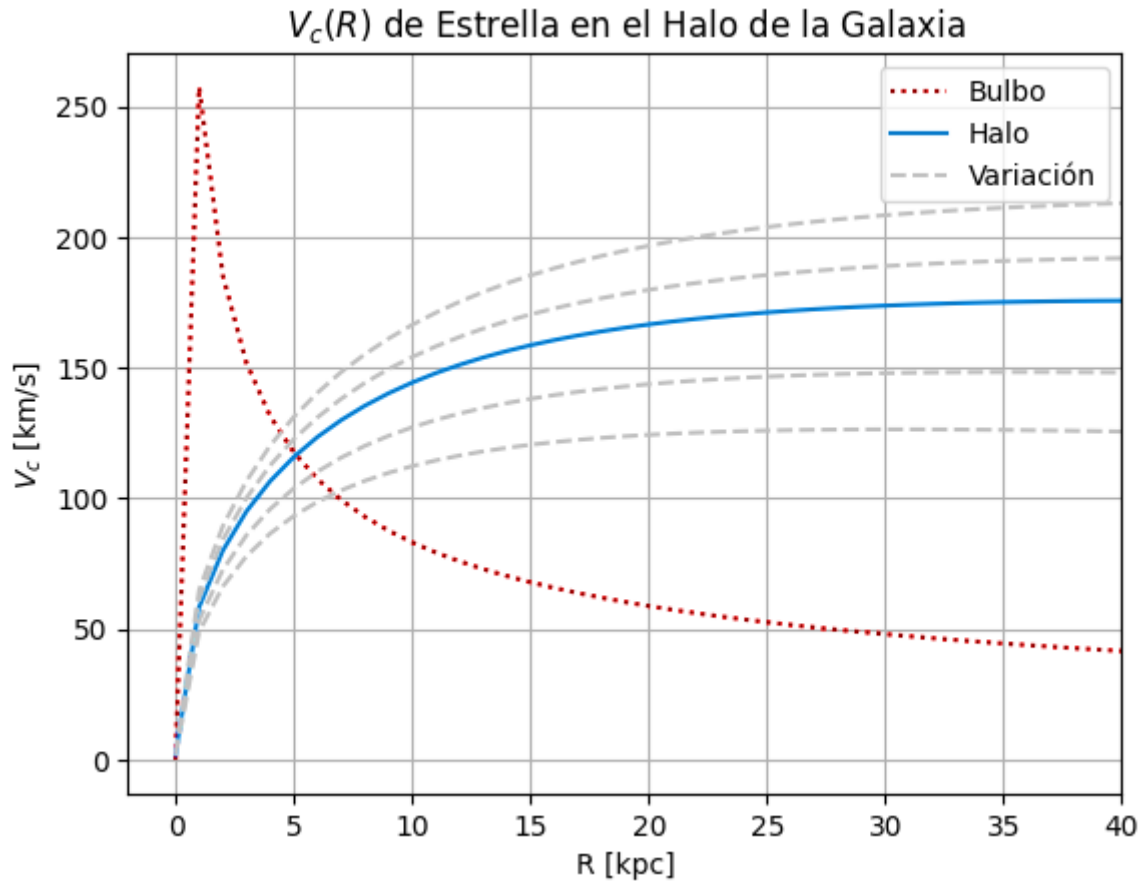
$$\Sigma_{0,thick} = 156.7e6 \pm 58.9e6 \left[\frac{M_{sun}}{kpc^2} \right]$$

$$R_{d,thick} = 3.38 \pm 0.54 [kpc]$$

Aún falta masa...



Halo de Materia Oscura



$$\rho(r) = \frac{\rho_{crit} \delta_c}{\left(\frac{r}{r_s}\right) \left(1 + \frac{r}{r_s}\right)^2} \quad (\text{NFW profile})$$

Best Fitting Model:

$$\rho_{crit} = \frac{(3H^2)}{8\pi G} \left[\frac{M_{sun}}{kpc^2} \right] \approx 8.86e6 \left[\frac{M_{sun}}{kpc^2} \right] \text{ (fijo)}$$
$$r_s = 19.6[kpc]$$
$$\delta_c = 5.0 \text{ (fijo)}$$

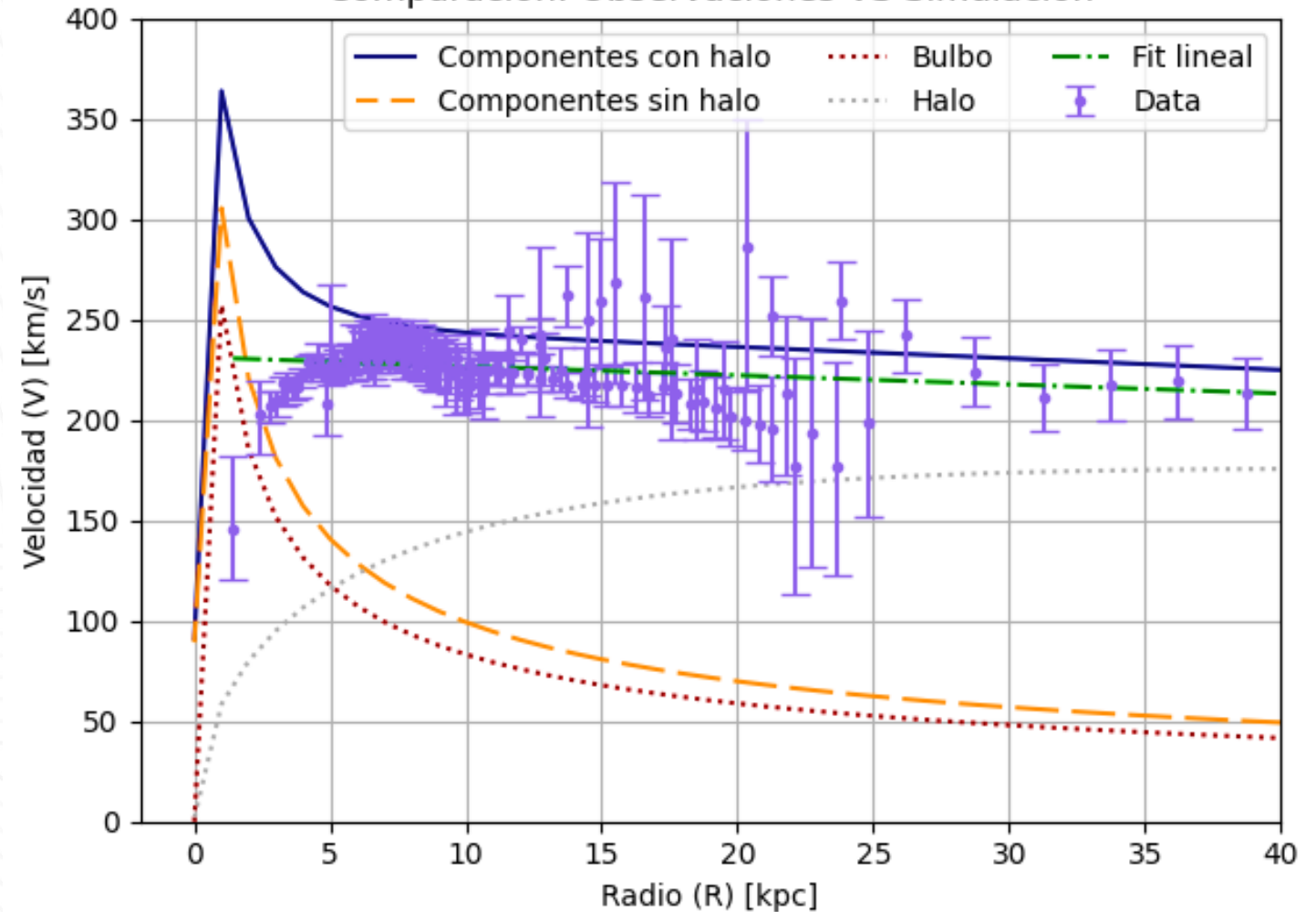
Variación de parámetros:

$$r_s = 19.0 \pm 4.9 [kpc]$$

Modelo Completo



Comparación: Observaciones VS Simulación



Conclusiones



- Se logró modelar las distintos componentes de una galaxia y obtener la velocidad de una estrella en función de su radio.
- Se comprobó que este modelo es consistente con los datos observacionales.
- En futuros estudios se recomienda la variación individual de los parámetros en los modelos de disco, así como el uso de datos de otras galaxias.

¡Gracias!

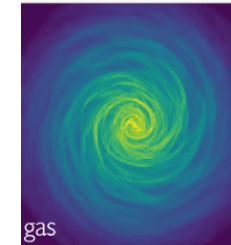
When someone uses
light years
instead of parsecs



Never Ask A Woman
Her Age



A Man,
His Salary



An Astrophysicist

What they use to kludge
together Dark Matter in
their galaxy simulations

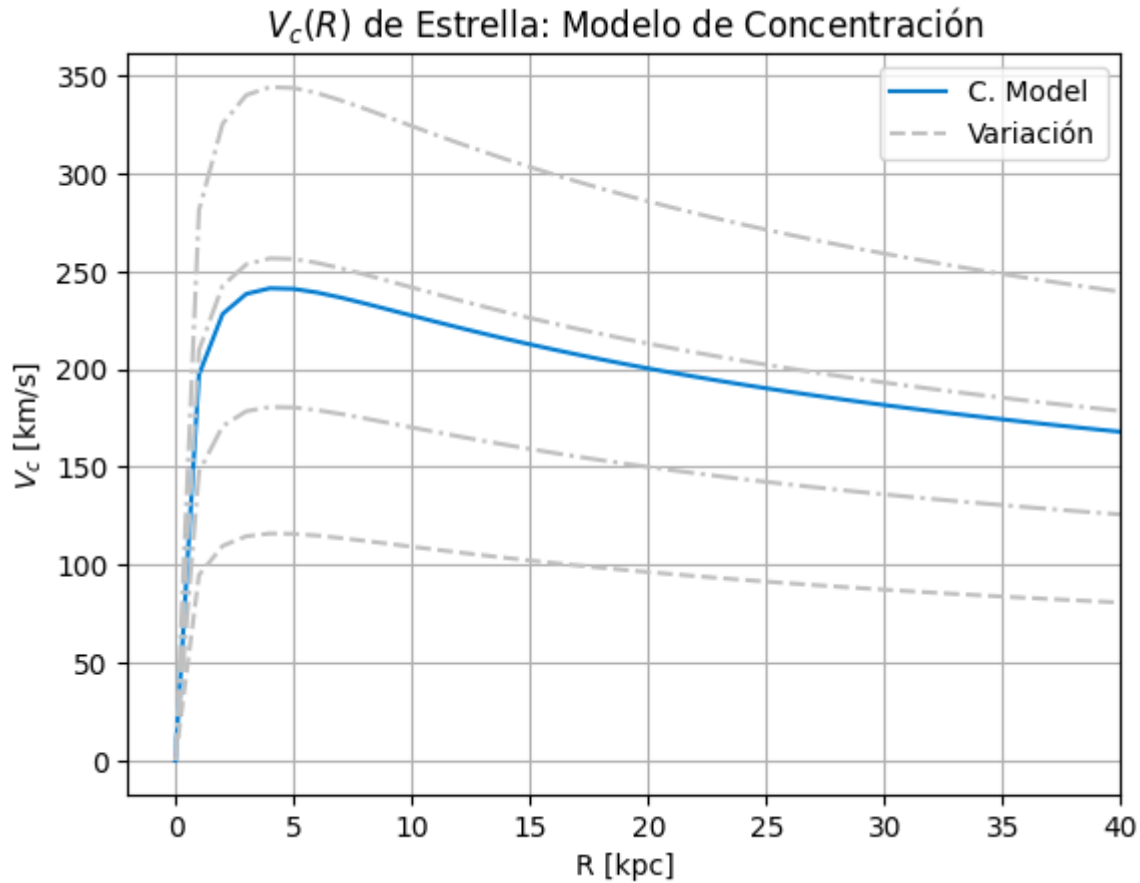


Thank you for
changing my life



**We are literally thousands
of light years away from you**

Modelo de Concentración



$$M = \int_0^{R_{\text{vir}}} 4\pi r^2 \rho(r) dr = 4\pi \rho_0 R_s^3 \left[\ln(1+c) - \frac{c}{1+c} \right]$$

Best Fitting Model:

$$\rho_0 \equiv \rho_{\text{crit}}$$

$$R_s \equiv r$$

$$\rho_{\text{crit}} \approx 8.86e6 \left[\frac{M_{\text{sun}}}{\text{kpc}^2} \right] \text{ (fijo)}$$

$$r_s = 19.6 [\text{kpc}]$$

$$r = cr_s$$

$$\rightarrow c = \frac{r}{r_s}$$

Variación de parámetros:

$$c \in (0, \infty)$$

$$r_s = 19.0 \pm 4.9 [\text{kpc}]$$

Modelo de Concentración Completo



Comparación: Observaciones VS Simulación

