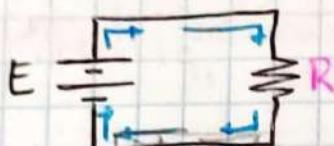


# CONCEPTOS DE CIRCUITOS ELECTRÓNICOS

Ley de Ohm  $V = RI$  La tensión entre los extremos de materiales conductores es directamente proporcional a la corriente que fluye a través del material.

//tensión o voltaje

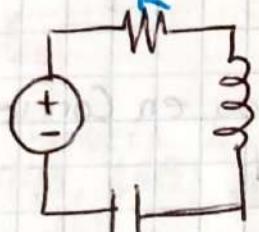
Un resistor es aquél que se opone al paso de la corriente.



$I \rightarrow$  Sale de la terminal positiva.

$10^{-6}$	micro	N	$10^6$	mega	M
$10^{-3}$	milli	m	$10^3$	Kilo	K

Resistor electrolítico y cerámico



R

$\Omega$

V/A

$$R = \frac{V}{I}$$

Carga positiva: (Protón)  $1.602 \times 10^{-19} C$

Carga negativa: (Electrón)  $-1.602 \times 10^{-19} C$

**Ley de Ohm:** Establece que la tensión entre los extremos de materiales conductores es directamente proporcional a la corriente que fluye a través del material:

$$V = RI$$

R: Resistencia eléctrica.

- Voltaje (tensión)

- Corriente: se define corriente en un punto específico, que fluye en una dirección especificada, como la velocidad instantánea a la cual la carga positiva pasa por ese punto en la dirección especificada.

• La unidad de corriente es el amperio

45

ELEMENTOS RESISTIVOS

• Resistencia: Dificultad o oposición que presenta un cuerpo al paso de una corriente eléctrica para circular a través de él  $\Omega$

Resistencia - Potencia Absorbida

Por ley de Ohm  $\downarrow$

La formula de potencia es:

$$P = VI$$

$$P = I^2 R$$

$$P = V^2 / R$$



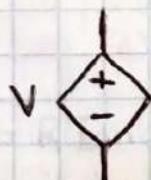
**Capacitor:** (Pasivo) tiene la capacidad de almacenar y devolver energía. El almacenamiento es en el campo eléctrica ( $F$ ) (Farad)



**Inductor:** (Pasivo) tiene la capacidad de almacenar energía durante períodos y la devuelve en otros. Potencia prom = 0 Henry (H)

#### \* TIPOS DE FUENTES.

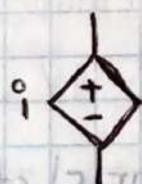
Dependientes



Independientes



Fte. de Voltaje  
de C.D.



Fuente de Corriente  
de C.D.

**Nodo:** Punto en el cual dos o más elementos tienen una conexión común.  
Punto en donde se conectan una o más ramas.

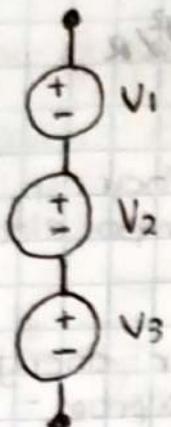
**Traекторia:** Cuando no pasa por un nodo más de una vez.

**Traectoria cerrada o lazo:** Punto en donde dos o más elementos tienen una conexión en común.

**Rama:** Traectoria simple en una red (Número de elementos).

**Malla:** Traectoria cerrada dentro de un circuito de tal forma que si la corriente sale de un nodo, esta regresa al mismo al terminar el recorrido sin pasar dos veces por un mismo nodo.

## Fuentes ind. en serie.

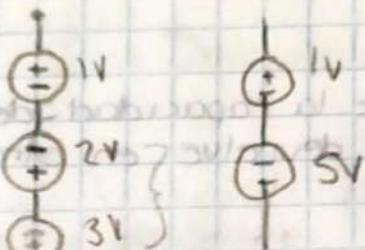


Los fuentes de voltaje  $V_1$ ,  $V_2$  y  $V_3$  están conectados en serie.



$$V_4 = V_1 + V_2 + V_3$$

Ej:



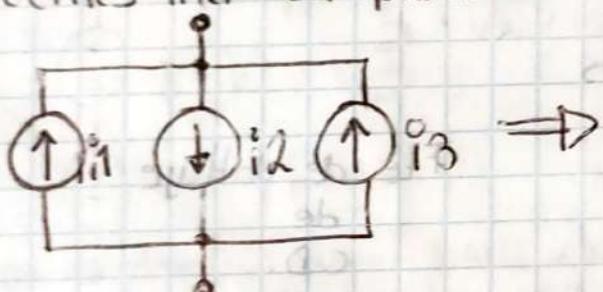
$$+1V - 2V + 3V = 4V$$

$$-4V$$

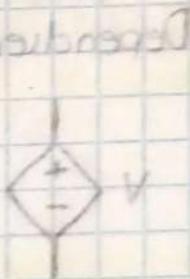
$$4V$$



## Fuentes ind. en paralelo



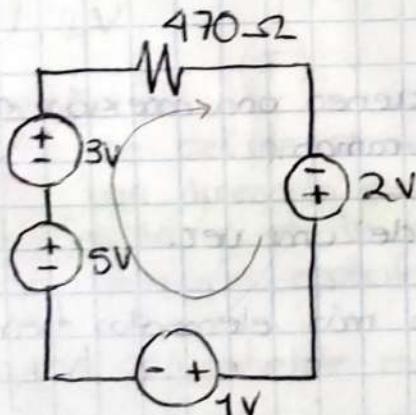
$$\Rightarrow i_4 = i_1 - i_2 + i_3$$



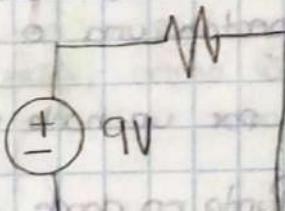
## Fuentes independientes.

En el sig. cto:

- a) Suma las fuentes
- b) Obtener la Corriente
- c) Dibujar el cto simplificado

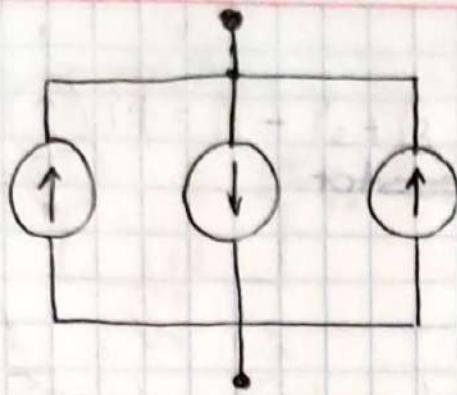


$$\frac{9V}{470\Omega} = 0.019 \text{ Amp}$$



$$-2V + 1V - 5V - 3V = -9V$$

$$\text{ó } 9V$$



$$i_1 = 10A$$

$$i_2 = 3A$$

$$i_3 = 7A$$

$$10A - 3A + 7A = 14A \times$$

El voltaje en paralelo es el mismo  
La corriente en serie es la misma

Círculo en Serie: Configuración de conexión en que los terminales de los dispositivos se conectan secuencialmente.  
 El voltaje se divide.

### LEY DE OHM

$$V = RI$$

Círculo en Paralelo: Conexión del dispositivo tal que las terminales de entrada de todos los dispositivos conectados coinciden entre sí al igual que sus terminales de salida.

### Serie

$$I_T = I_1 = I_2 = I_3 = I_4$$

$$R_T = R_1 + R_2 + R_3 + R_4$$

$$V_T = V_1 + V_2 + V_3 + V_4$$

$$i = \frac{P}{V}$$

$$P = Vi$$

$$i_1 = \frac{27.75 \mu W}{1.5 mV} = 18.5$$

### Paralelo

$$V_T = V_1 = V_2 = V_3 = V_4$$

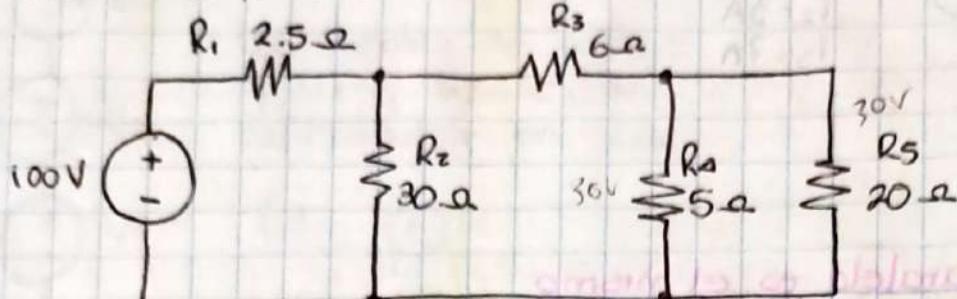
$$R_T = \frac{R_1 R_2}{R_1 + R_2} \text{ (2 Resist.)} \quad \text{ó} \quad R_T = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}$$

$$I_T = I_1 + I_2 + I_3 + I_4$$

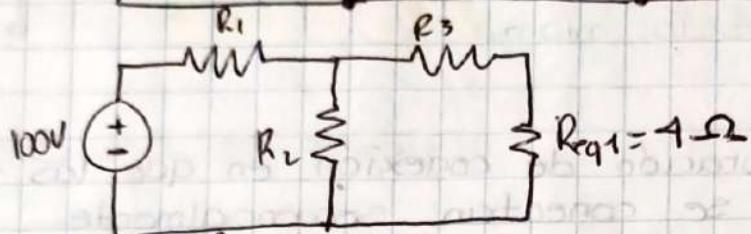
$$I_2 = \frac{-3 \mu W}{1.5 mV} \quad I_3 = \frac{1.20 \mu W}{1.5 mV}$$

# Circuitos en serie y en Paralelo.

Encuentre la potencia absorbida en cada resistor.



$$\frac{5 \cdot 20}{5 + 20} = 4$$



$$100V \quad R_1 \quad R_2 \quad \sum R_{eq1} = 10 \Omega \quad V_{eq1} = 75V$$

$$100V \quad R_2 \quad R_3 \quad \sum R_{eq2} = 7.5 \Omega$$

$$I_T = \frac{V_T}{R_T} = \frac{100V}{10 \Omega}$$

$$I_T = 10A$$

$$V_{eq3} = R_{eq3} I_{eq3} = 75V$$

$$P = i^2 R \quad P = Vi \quad P = \frac{V^2}{R}$$

$$P_{R1} = 10^2 (2.5) = 250W$$

$$P_{R2} = \frac{(75)^2}{30} = 187.5W$$

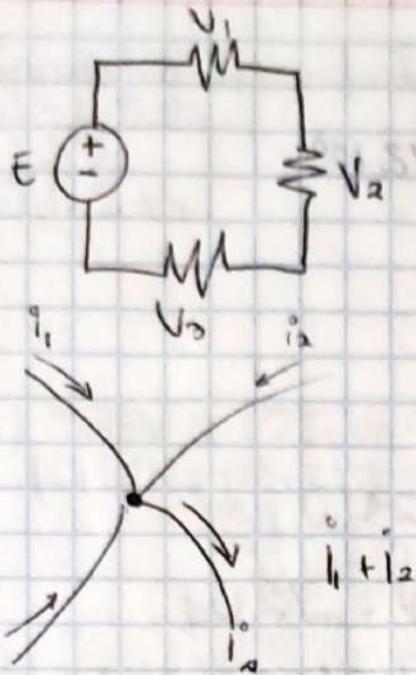
$$P_{R3} = (7.5)^2 (6) = 337.5W$$

$$P_{R4} = \frac{V^2}{R} = \frac{30^2}{5} = 180W$$

$$P_{R5} = \frac{30^2}{20} = 45W$$

$$V = 7.5A (4\Omega)$$

$$30V + 1V + V = V$$



$$E + V_1 + V_2 + V_3 = 0$$

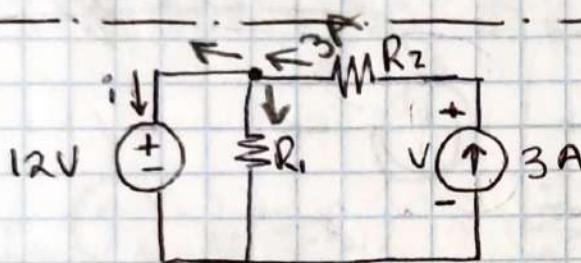
$$P = V^2$$

$$P = i^2 R$$

$$P = \frac{V^2}{R}$$

$$V = iR$$

$$i_1 + i_2 + i_3 = I_A$$



$$\frac{P}{V} = \frac{V}{R} \quad I = \frac{V}{R}$$

$$R_2 = 3\Omega$$

$$12\Omega$$

a) Suponer  $R_1 = 6\Omega$  y  $R_2 = 3\Omega$   
Encontrar la corriente  $i$  y el voltaje  $V$

$$V_3 = 9V \quad \text{En serie } R_2 \text{ y } \uparrow$$

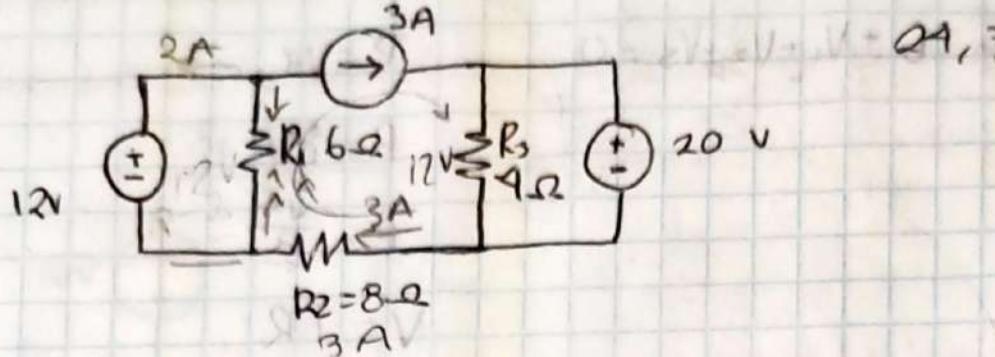
$$\frac{12}{6} = 2A$$

$$i = 1A$$

b) Suponer que  $i = 1.5A$  y  $V = 2V$ . Determine  $R_1$  y  $R_2$   
 $R_1 = 8\Omega$   $R_2 = 6\Omega$

c) Suponer que la fuente de voltaje suministra  $24W$  y la fuente de corriente suministra  $9W$  de potencia, determine corriente  $i$ , voltaje  $V$  y  $R_1, R_2$

Calcular potencia en resistores



$$V_Q = 6V$$

$$V = RI$$

$$P_1 = V \cdot I_1 = (12V)(2A) = 24W$$

$$I = 12/6 = 2A \quad I = \frac{V}{R}$$

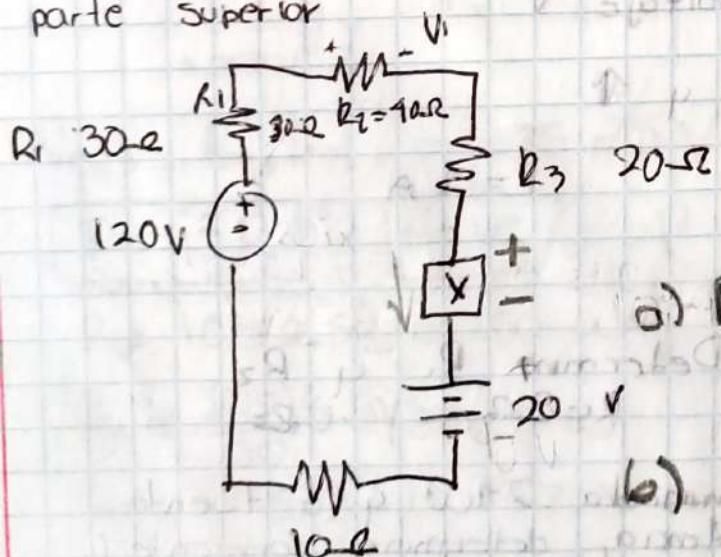
$$P_2 = R \cdot I^2 = (8\Omega)(3A)^2 = 72W$$

$$I_3 = \frac{20}{4} = 5A$$

$$P_3 = U_3 \cdot I_3 = (20V)(5A) = 100W$$



Calcular potencia del elemento X con referencia positiva en la parte superior



$$a) R = 100\Omega$$

$$b) \text{ FVI de } 10V$$

FVD con 20i x

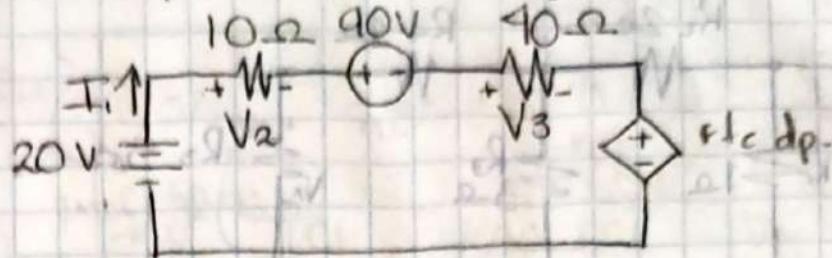
FVD en G-BN

$$c) P = R \cdot I^2 = (100\Omega)(0.5)^2 = 25W$$

b)

Encuentre  $I_1$  si la fuente dependiente de voltaje tiene valor de:

- a)  $-1.5 I_1$
- b)  $2 V_2$
- c)  $1.5 V_3$



$$a) -20V + 10I_1 + 90V + 40I_1 - 15I_1 = 0$$

$$50I_1 + 15I_1 = -90 + 20 \quad (d)$$

$$+ 35I_1 = -70$$

$$I_1 = -70/35$$

(d) ~~fuente de 2 amperes~~

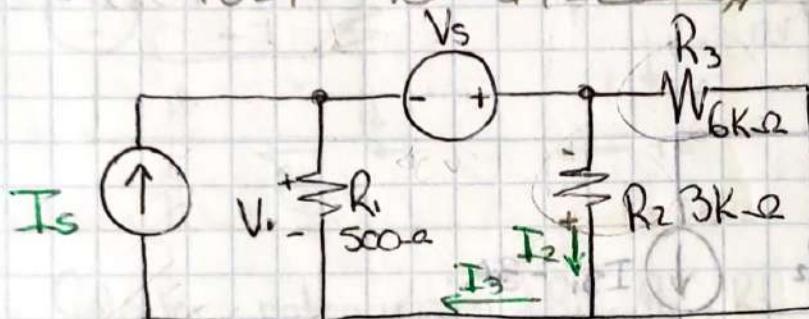
$$c) -20V + 10I_1 + 90 + 40I_1 + 15I_1 = 0$$

$$V_{DC} = 1.5I_1 \quad 100I_1 = -70$$

$$I_1 = -0.63 \text{ am}$$

$$b) -20V + 10I_1 + 90 + 40I_1 + 2(10I_1) = 0$$

$$70I_1 = -70 \quad I_1 = -1 \quad X$$



$$R_{eq} = \frac{6 \times 3}{6 + 3} = \frac{18}{9} = 2 \text{ k}\Omega$$

$$= 2000 \Omega$$

Para el circuito

$$a) \text{ Consider } V_s = 40V \text{ e } I_s = 1A, \text{ determine } V_1$$

$$b) \text{ Consider } V_s = 0V \text{ e } I_s = 3mA, \text{ determine } I_2 \text{ e } I_3$$

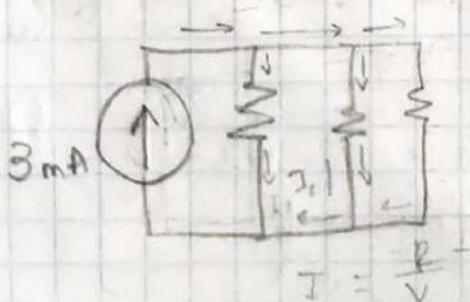
$$a) 40 + 2000i + 500i = 0$$

$$2500i = -40$$

$$i = -0.016 \text{ amp}$$

$$V_1 = R_1 I_1 = (500)(0.016A)$$

$$= 8V \quad X$$



Resistencias en paralelo, se suman

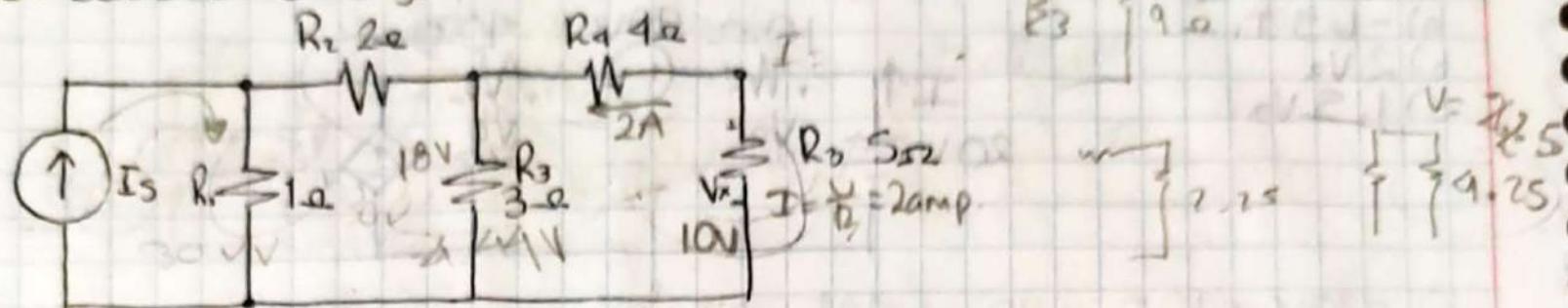
$$R_{eq} = 1000\Omega$$

$$V = R_i I_1 = 1000 \cdot 3mA$$

$$1.2V$$

$$2500$$

Con base en el siguiente circuito:

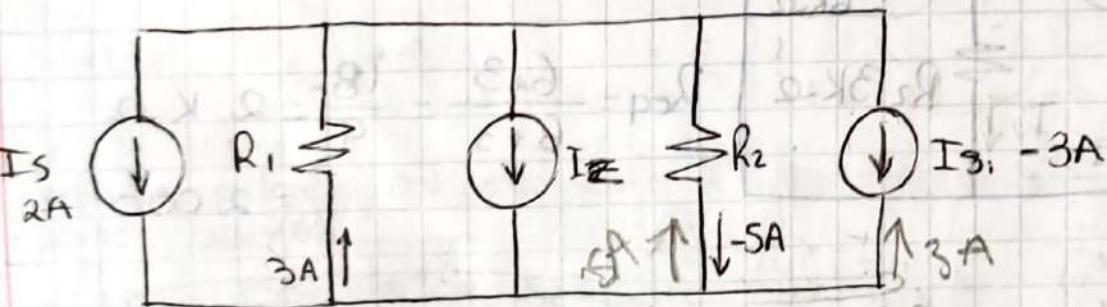


- a) Encuentre  $I_S$  con  $V_x = 10V$   
26 amp. :)

- b) Encuentre  $V_x$  con  $I_S = 50A$

$$U_x = R_x I_x = (23 \text{ amp})(5\Omega)$$

$$\approx 119 \approx 12V$$



- a) Determine  $I_Z$
- $$2A - 3A + I_Z - 5A - 3A = 0$$
- $$I_Z - 9A = 0$$
- $$I_Z = 9A$$

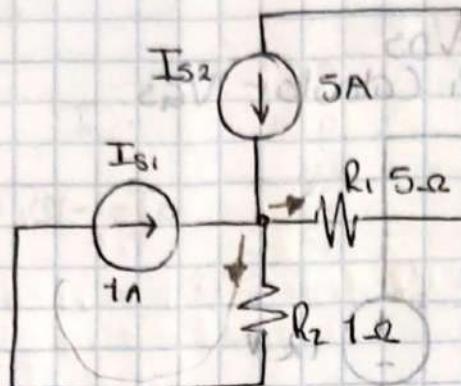
- b) Si  $R_1 = 1\Omega$ , determine  $R_2$

$$U = RI = (1)(-3A) - (-3V)$$

$$R = \frac{U}{I} = \frac{(-3V)}{-5A} = 0.6\Omega$$

11/20

Calcular potencia en  $R_1$  y  $R_2$

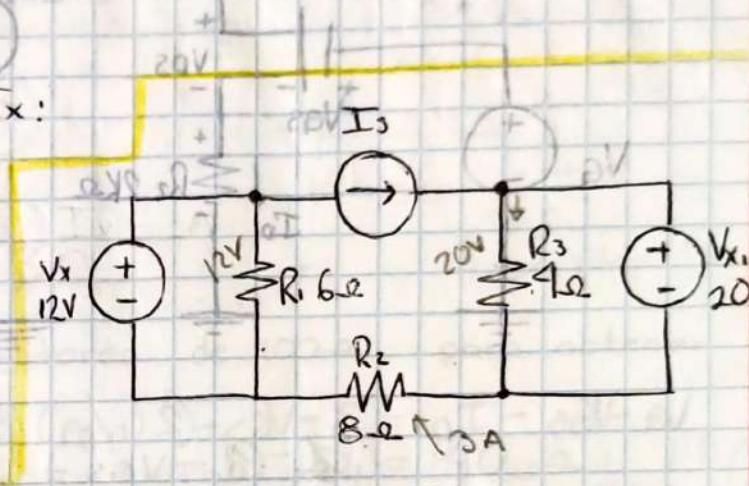
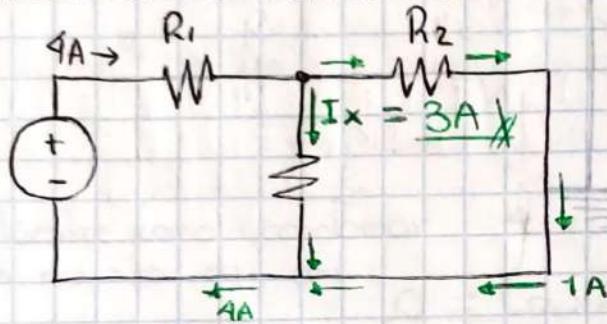


$$P = I^2 R$$

$$P_2 = (1)^2 (1) = 1 \text{ W} \quad \times$$

$$P_1 = (5)^2 (5) = 125 \text{ W} \quad \times$$

Encontrar la corriente en  $I_x$ :

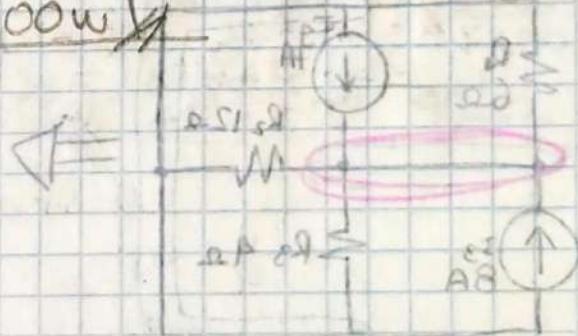
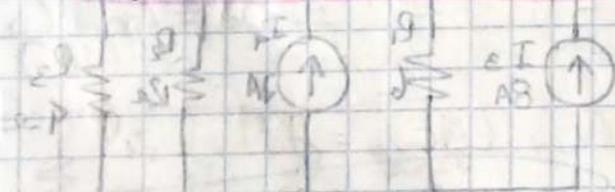


Calcular potencia en  $R_1$ ,  $R_2$ ,  $R_3$

$$P_{R2} = I^2 R = (3A)^2 (8) = 72 \text{ W} \quad \times$$

$$P_{R1} = \frac{V^2}{R} = \frac{(12)^2}{6} = \frac{144}{6} = 24 \text{ W} \quad \checkmark$$

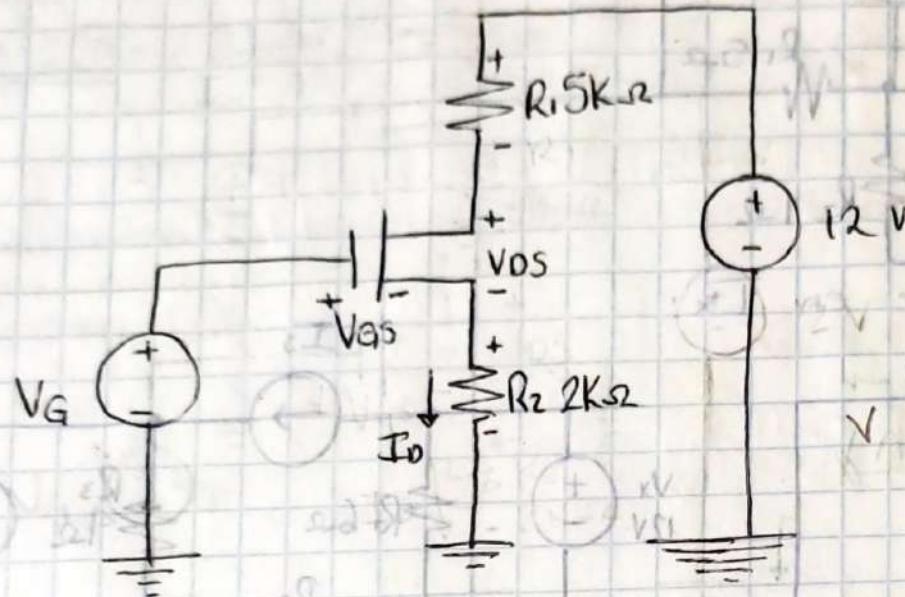
$$P_{R3} = \frac{V^2}{R} = \frac{20^2}{4} = \frac{400}{4} = 100 \text{ W} \quad \times$$



Del cto. transistorizado obtener:

a) Si  $I_D = 1.5 \text{ mA}$ , calcular  $V_{DS}$

b) Si  $I_D = 2 \text{ mA}$  y  $V_G = 3 \text{ V}$ . Calcular  $V_{GS}$ .



a)  $= -12 \text{ V} +$

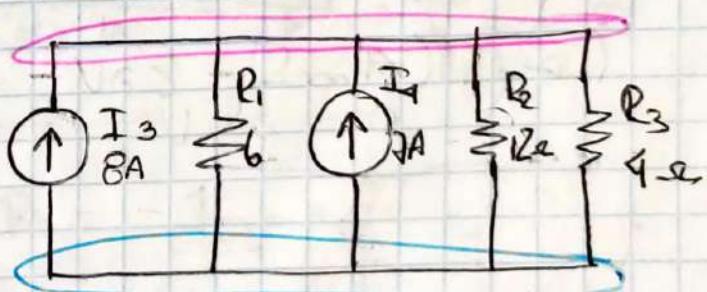
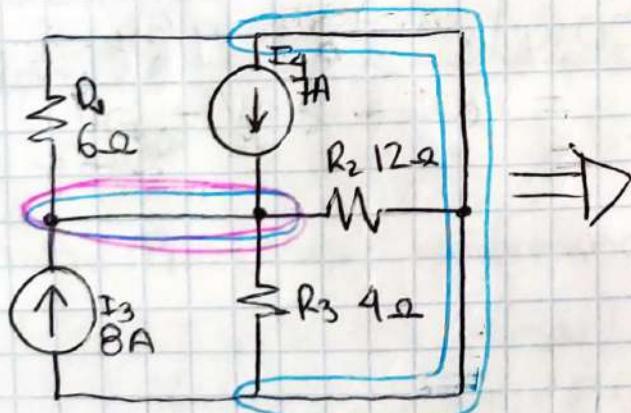
$$V_G - V_{GS} - I_D R_2 = 3 - V_{GS} - (2 \text{ mA})(2 \text{ k}\Omega) = 0$$

$$= 3 - 1 - V_{GS} = 0$$

- 1.5

$V_{GS} = -1$

Calcular la Potencia en todos los elementos.



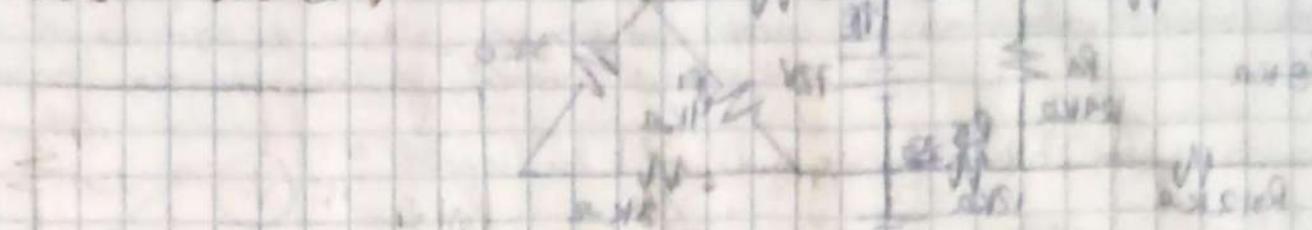
$$8 + \frac{V}{6} + 7 + \frac{V}{12} + \frac{V}{4} = 0$$

$$V \left( \frac{1}{6} + \frac{1}{12} + \frac{1}{4} \right) = -15$$

$$U = (-15)(27)$$

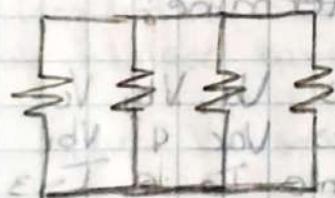
$$U = -330$$

$$P_3 = V_3 I_3 = -330(8A) = -2640 \text{ W}$$



Muestre como combinar 4 resistores de  $100\Omega$  para obtener un resistor eq. de:

a)  $R_{eq} = 25\Omega$

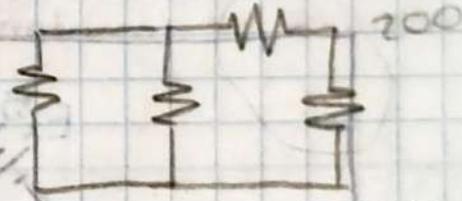


$$\frac{1}{R_{eq}} = \frac{1}{100} + \frac{1}{100} + \frac{1}{100} + \frac{1}{100} = \frac{4}{100} = \frac{1}{25}$$

$$\frac{1}{R_{eq}} = 0.04$$

$$R_{eq} = 25\Omega$$

b)  $R_{eq} = 40\Omega$

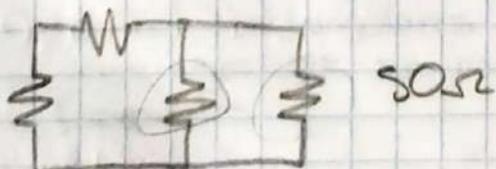


$$2V$$

$$(200)(100) = \frac{(66-66)(100)}{300}$$

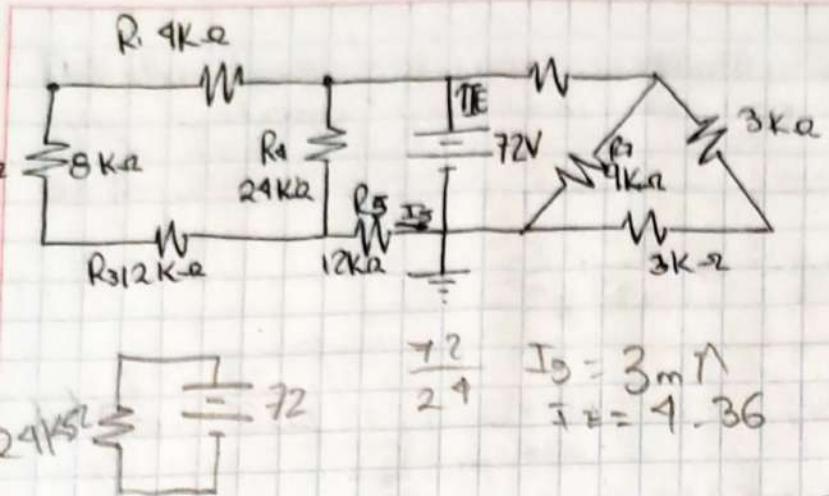
$$100\Omega = 40\Omega$$

c)  $R_{eq} = 60\Omega$



$$50 + 100 = 150$$

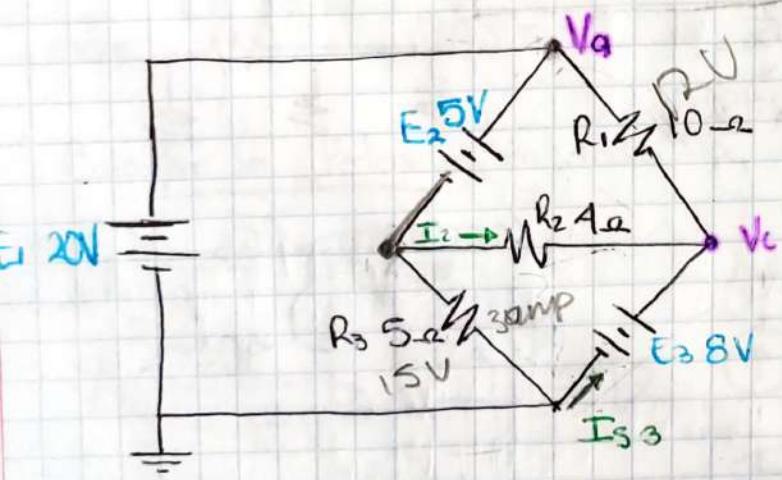
$$\frac{(150)(100)}{250} = 60\Omega$$



7.36 (F1c)

Pt de Winston (Para Condicionar Señales.)

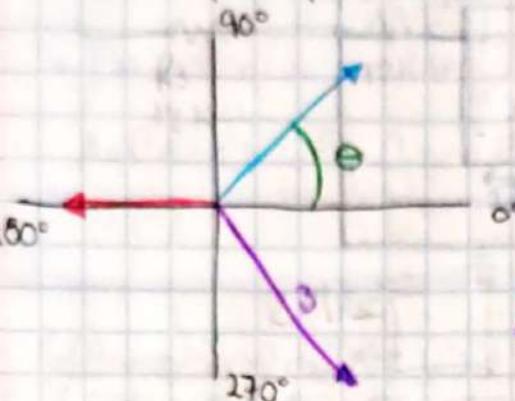
Determine:



- Voltajes  $V_a$ ,  $V_b$ ,  $V_c$
- Voltajes  $V_{ac}$  y  $V_{bc}$
- Corriente  $I_a$  e  $I_{S3}$

## FASORES.

Un fasor es un tipo de vector; se emplea para representar funciones del tiempo que varían en forma senoidal.



Magnitud (longitud de la flecha, medida de una recta).

El ángulo  $\theta$  (con respecto a  $0^\circ$ ), representa la posición angular.

Magnitud = 1, ángulo de fase ( $\theta$ ) =  $180^\circ$

Magnitud = 3, ángulo de fase ( $\theta$ ) =  $-45^\circ$  (o  $315^\circ$ )

Un ciclo completo de una onda seno puede ser representado por la rotación de  $360^\circ$  de un fasor. El valor instantáneo de la onda seno en cualquier punto es igual a la distancia vertical desde la punta del fasor hasta el eje horizontal.

La longitud del fasor es igual al valor pico de la onda seno (puntos de  $90^\circ$  y  $270^\circ$ ). El ángulo del fasor medido a partir de  $0^\circ$  es el punto angular correspondiente de la onda seno.

La longitud de fasor es el valor pico del voltaje sinusoidal,  $V_p$ . Por lo tanto el lado opuesto del triángulo, (valor instantáneo) se expresa:

$$v = V_p \operatorname{sen} \theta$$

## NUMEROS COMPLEJOS

En Cts. se utiliza el prefijo  $\pm j$ .

Complejo: Combinación de un imaginario y un complejo.

Las formas rectangulares y polares son dos formas de números complejos que se utilizan para representar cantidades fotorreales.

$$8 + 3j, 6 - 7j, -3 + 9j, -5 - 10j$$

Rectangular =  $A + Bj$

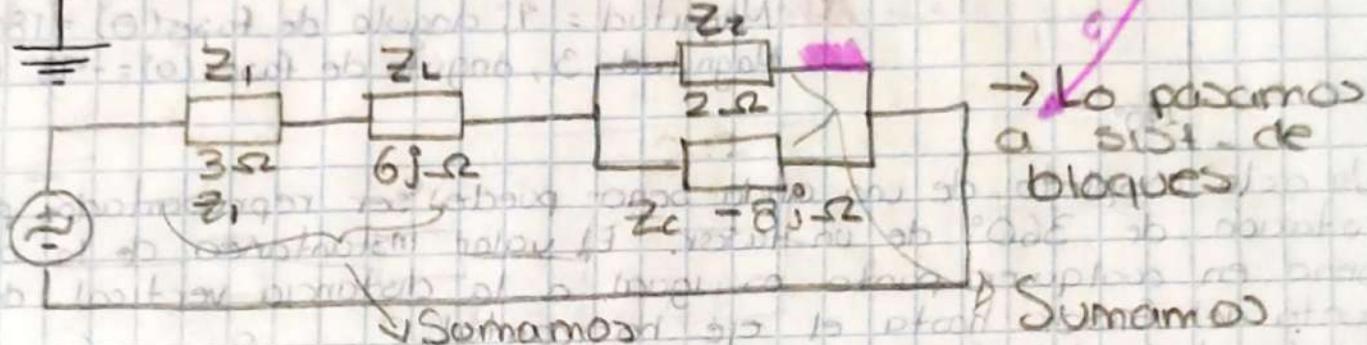
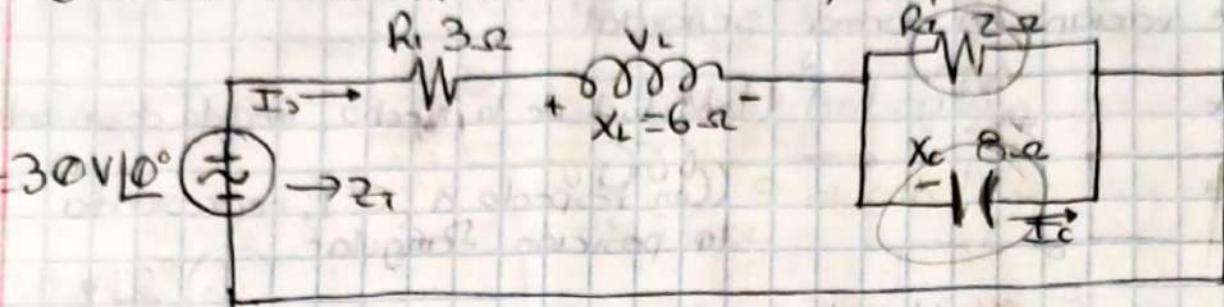
$$8.5 [20.55], 9.21 [199^\circ], 25 [110^\circ], -60 [110^\circ]$$

Polar  $C [ \pm \theta ]$

$$T_i 2. P_8 - 28.18 = 25.18$$

- a) Determine la impedancia total ( $Z_T$ )  
 b) Determine la corriente  $I_o$ ,  $I_{sy}$ ,  $V_L$

23.000TF



↓ Sumamos

↓ Sumamos

$$\frac{-16j}{2-8j}$$

► Hay que multiplicar por su conjugado

$$\frac{-16j}{2-8j} \left( \frac{2+8j}{2+8j} \right)$$

$$\frac{32 + 128j}{4 + 64} = \frac{32}{17} - \frac{8}{17}j \quad Z_T = \frac{32}{17} + \frac{94}{17}j$$

$$I_T = \frac{30V 10^\circ}{7.37 \angle 98.55^\circ} \approx 4.06 \angle -18.55^\circ \approx 2.69 - 3.04j$$

$$V_{Z_T Z_C} = \left( \frac{32}{17} - \frac{8}{17}j \right) (2.69 - 3.04j) = -316.81 - 575.17j$$

$$I_{Z_C} = 71.85 - 39.6j$$

## Forma Rectangular

$$A + Bj$$

- De polar a rectangular

$$A = C \cos \theta \quad B = C \sin \theta$$

## Forma Polar

$$V C L \pm \theta$$

- De rectangular a polar

$$C = \sqrt{A^2 + B^2} \quad \theta = \tan^{-1} \left( \frac{\pm B}{A} \right)$$

## Adición

$$(8+5j) + (2+j) = 10 + 6j$$

$$(20-10j) + (12+6j) = (32-4j)$$

## Sustracción

$$(3+4j) - (1+2j) = 2+2j$$

$$(15+15j) - (10-8j) = (5+23j)$$

## Multiplicación

$$(5+3j)(2-4j) = 10 - 20j + 6j + 12 = 22 - 14j$$

$$(10|95^\circ)(5|120^\circ) = (10 \cdot 5)L(95 + 20) = 50|65^\circ$$

## División

$$\frac{10+5j}{2+4j} = \frac{(10+5j)(2-4j)}{(2+4j)(2-4j)} = \frac{20-40j+10j-20j^2}{21-16j^2}$$

$$\frac{100|50^\circ}{25|20^\circ} = \left(\frac{100}{25}\right)|50^\circ - 20^\circ = 4|30^\circ$$

$$= \frac{20+20-30j}{4+16} = \frac{40-30j}{20} = 2 - 1.5j$$

Ley de Kirchhoff de Voltaje: la suma algebraica de todos los voltajes en una trayectoria cerrada única es cero;

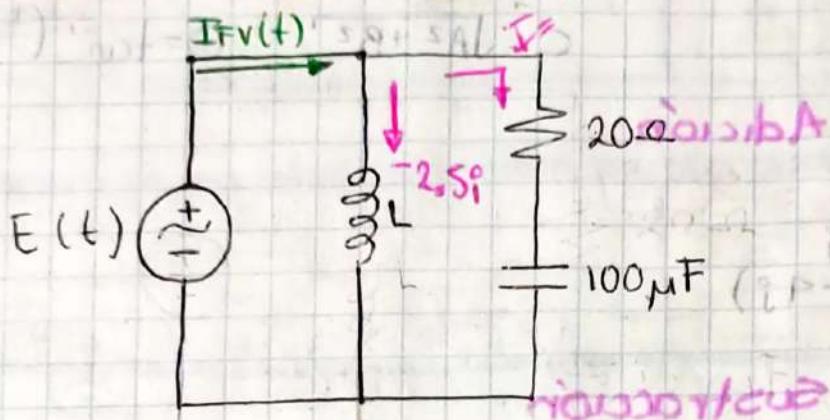
Ley de Kirchhoff de corriente: la suma de las corrientes que entran a un nodo es igual a la suma de las corrientes que salen de dicho nodo.

Encuentre el valor de L donde

$$E(t) = 100 \operatorname{sen}(500t) V$$

$$I_{FV} = 2.5 \operatorname{sen}(500t) A$$

Considerar  $K=1$  notación  $\angle 2.5 + 2.5^\circ$



Amplitud  $\operatorname{sen}(\text{frecuencia} t) + \text{angulo}$   
 $\rightarrow A \operatorname{sen}(wt + \alpha)$

Para pasar a forma polar:

$A K \angle \alpha$

$$\text{Si no hay consideraciones } K = \frac{1}{\sqrt{2}}$$

$$\text{Ahora: } Z_C = \frac{1}{j\omega C} \quad \text{y}$$

$$\& \quad Z_L = j\omega L$$

$$V = RI \quad I_2 = \frac{V_L}{R_2} = \frac{100 \angle 0^\circ}{20 - 20j} = \frac{100 \angle 0^\circ}{28.28 \angle -90^\circ} \quad \text{if } 3.53 \angle 15^\circ = 2.49 + 2.49j$$

$$I_{FV} = 2.5 \operatorname{sen}(500t) A = 2.5(1) \angle 0^\circ$$

$$(2.5 + 0j) - (2.5 + 2.5j) = 0 - 2.5j$$

$\Rightarrow R \operatorname{cost}(\omega t) \Rightarrow A \operatorname{sen}(\omega t + 90^\circ)$

$\Rightarrow$  ~~resistencia en serie~~

$$E(t) = 100 \operatorname{sen}(500t)$$

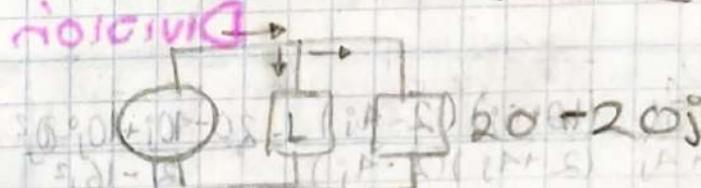
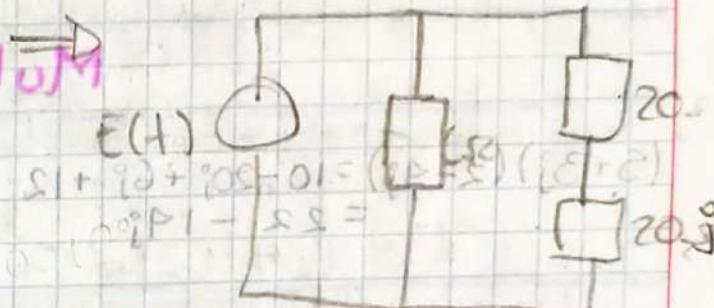
$$E(t) = 100 \operatorname{sen}(500t) \angle 0^\circ = 100 \angle 0^\circ$$

$$\frac{1}{j\omega C} = \frac{1}{j \cdot 500 \cdot 10^{-6}} = 20 \Omega$$

$$\text{Donde } \omega = 500 \quad i_d + 0j - C = 100 \times 10^{-6} \quad (i_P - i_E) = (2.5 + 2.5j) + (100 \times 10^{-6})$$

$$Z_C = \frac{1}{(500)(10 \times 10^{-6})} = \frac{1}{5000} = 0.05 \Omega$$

$$i_S = 0.05 \angle 0^\circ = 20 \angle 0^\circ \quad (i_E + C) = (100 \angle 0^\circ) - (20 \angle 0^\circ)$$

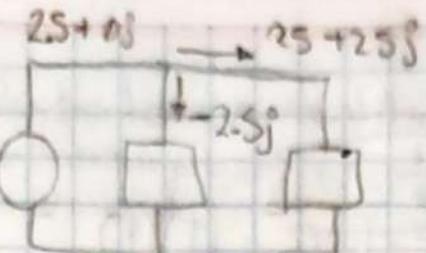


$$R_{eq} = 20 + 20j$$

$$2.5 + 0j \quad \text{if } 2.5 \angle 0^\circ \quad 2.5 + 2.5j$$

$$2.5 + 0j \quad \text{if } 2.5 \angle 0^\circ$$

$$\cos(t) = \operatorname{sen}(t + 90^\circ)$$



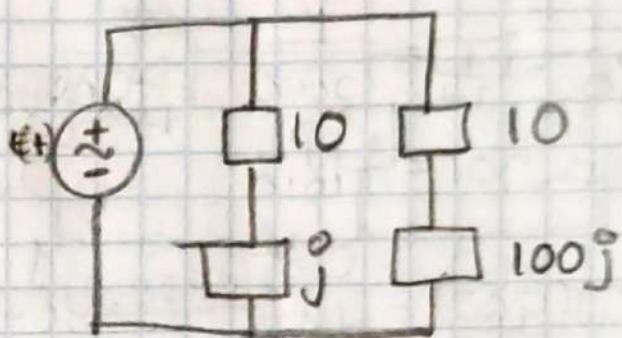
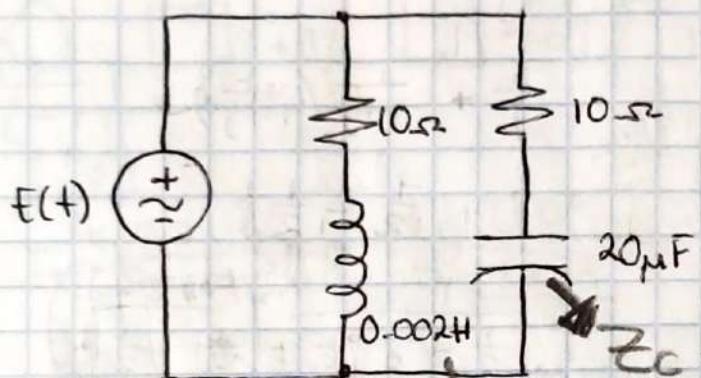
$$V_L = I_L Z_L \quad V_L = I_L (j\omega L)$$

$$\Rightarrow 100 \angle 0^\circ = 10 \angle -2.5^\circ (500jL)$$

$$L = \frac{100 \angle 0^\circ}{500j} = \frac{100}{1250} = 0.08 \text{ H}$$

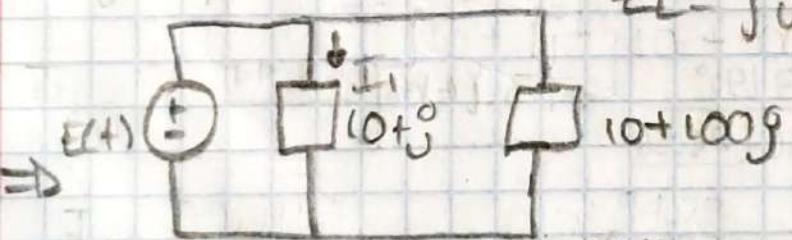
Calcule la corriente en cada rama si  $E(t) = 100 \cos(500t) \text{ V}$

$$E(t) = 100 \left(\frac{1}{\sqrt{2}}\right) \angle 0^\circ = 70.71 \angle 0^\circ$$



$$Z_C = \frac{1}{j\omega C} \Rightarrow \frac{1}{(500)(20 \times 10^{-6})j} = 100 \Omega$$

$$Z_L = j\omega L \Rightarrow (500)(0.002)j = 10 \Omega$$

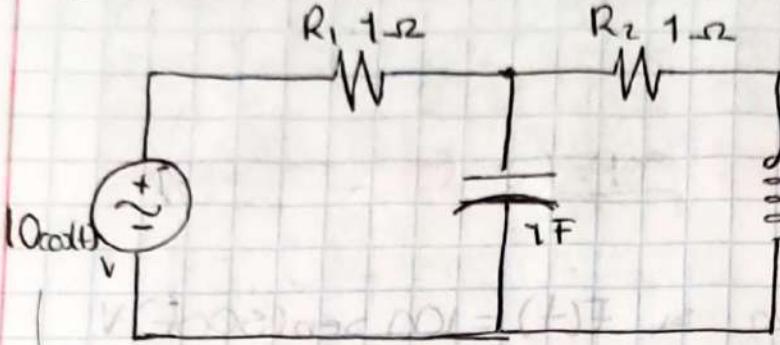


$$\Rightarrow U = RI \quad I_1 = \frac{70.71}{10 + j0} \approx 7 - 0.71 \Omega$$

$$I = \frac{U}{R}$$

$$I_2 = \frac{70.71}{10 + 100j} = 0.07 - 0.71 \Omega$$

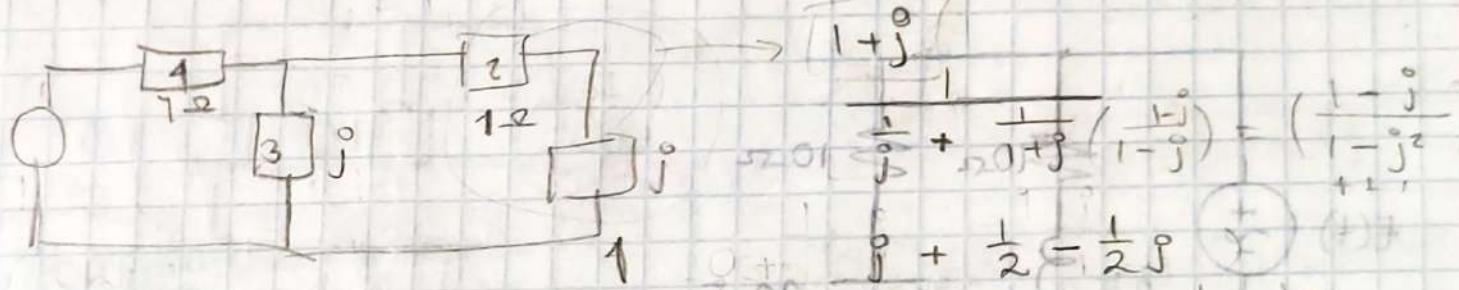
Calcular corriente que circula en la bobina.



$$Z_C = \frac{1}{j\omega C} = \frac{1}{(1)(1)} = 1 - j$$

$$Z_L = j\omega L = (1)(1) = 1^{\circ}$$

$$\rightarrow E(t) = 10 \cos(t) = 10 \sin(t + 90^{\circ}) = 10 \left(\frac{1}{\sqrt{2}}\right) [90^{\circ}] = 7.07 [90^{\circ}]$$



$$\begin{aligned} & \text{Circuit diagram showing a voltage source } 7.07 [90^{\circ}] \text{ V in series with a } 1 \text{ ohm resistor. This is followed by a parallel branch with a } 1 \text{ ohm resistor and a } 1 \text{ F capacitor in series.} \\ & \text{The total impedance is } 1 + j^{\circ}. \\ & \text{Using } V = RI, \quad I = \frac{7.07 [90^{\circ}]}{2.2360 [26.56]} = 3.1618 [63.44] \end{aligned}$$

$$\begin{aligned} V &= (1 + j)(3.1618 [63.44]) = (1.4142 [45^{\circ}])(3.1618 [63.44]) \\ &= 4.47 [108.44] \end{aligned}$$

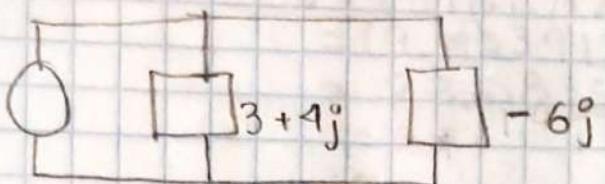
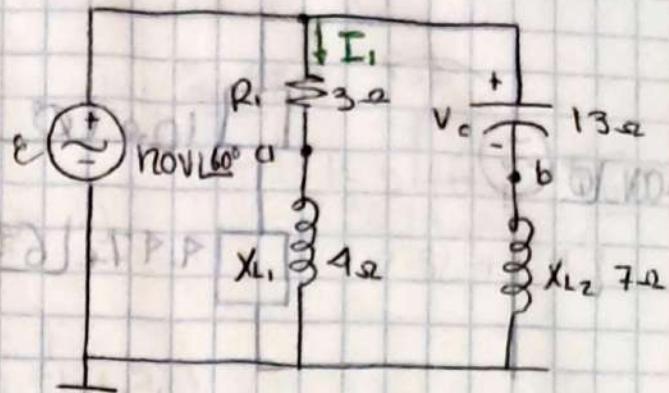
$$I_{1,2} = \frac{V}{R} = \frac{4.47 [108.44]}{1 + j} = \frac{4.47 [108.44]}{1.4142 [45]} = 3.16 [63.44]$$

La admittance ( $Y$ ) está dada en Siemens ( $S$ ) y es la inversa de la impedancia.

$$Y = \frac{1}{Z}$$

⇒ Del siguiente circuito

- Determine corriente  $I_1$ .
- Calcule el valor  $V_c$  y  $V_{ab}$ .



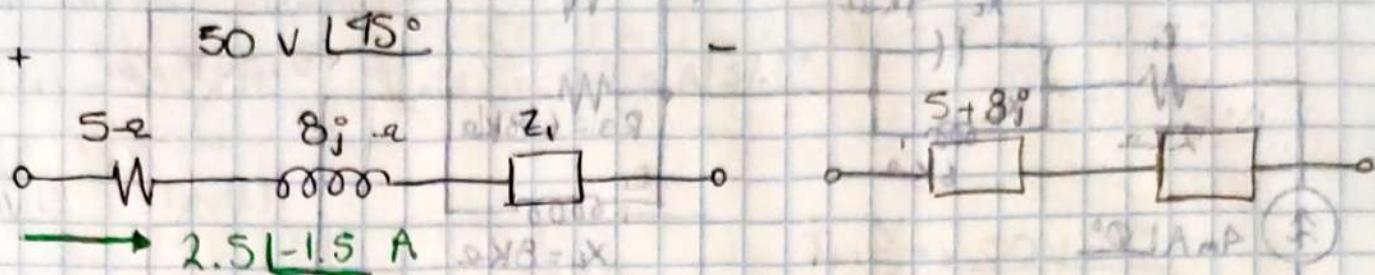
120V  $60^\circ$

$$V = RI$$

$$I_1 = \frac{120 \angle 60^\circ}{3 + j4} = \frac{120 \angle 60^\circ}{5 \angle 53.13^\circ} = 24 \angle 6.8698^\circ$$

0.0238272

Calcular la impedancia  $Z_i$



$$V = RI$$

$$\begin{aligned} V &= (5+8j)(2.5) - 1.5 \\ &= (9.4339 + 15.99j)(2.5) - 1.5 \\ &= 23.58 + 56.99j = 13.0181 + 19.6607j \end{aligned}$$

$$50 \text{ V } [45^\circ] = (35.3553 + 35.3553j) - (13.0181 + 19.6607j)$$

$$V_{Z_i} = 22.3372 + 15.6996j = 27.29 [35^\circ]$$

$$Z_i = \frac{27.29 [35^\circ]}{2.5 - 1.5} = 10.916 [36.5] = 8.77 + 6.49j$$

Calcular  $Z_T$ ,  $V_T$ ,  $I_L$

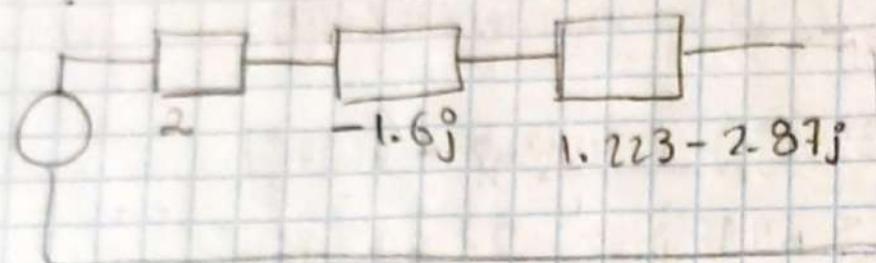
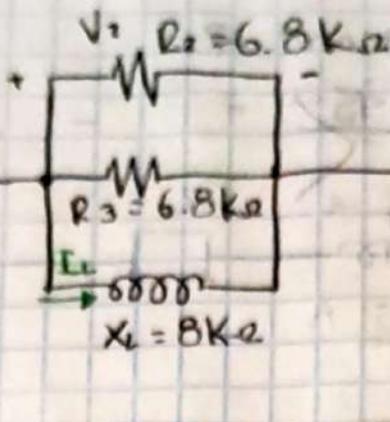
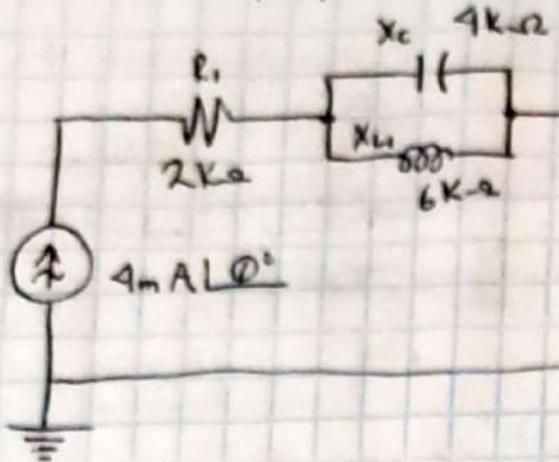


Diagram of the load branch:

$$2.223 - 4.47j \text{ A}$$
$$1.6j \text{ S}$$

$$I = \frac{V}{R} = \frac{4 \text{ mA } 0^\circ}{4.99 \text{ } \underline{-63.55}} = 0.8163.55$$

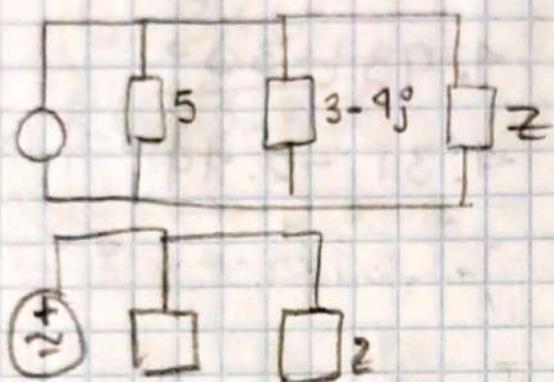
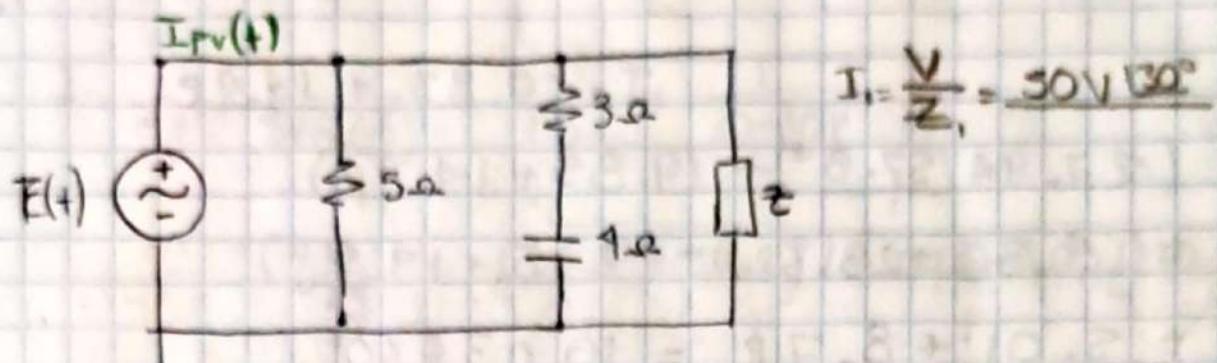
$$V = RI = (1.223 - 2.87j)(0.8163.55) = (3.11 \underline{-66.91})(0.8163.55)$$
$$= 2.48 \underline{-3.36}$$

$$V_T = 2.48 \underline{-3.36} = 2.47 - 0.1^\circ$$

$$I_L = \frac{V}{R} = \frac{2.48 \underline{-3.36}}{8190^\circ} = 0.31 \underline{-93.36} = -0.61 - 0.3^\circ$$

Del siguiente circuito determine el valor de  $\underline{z}$  y la naturaleza de dicho elemento.

$$E(t) = 50V \angle 30^\circ \quad I_{PV}(t) = 2.7.9 A \angle 57.8^\circ$$



$$I_1 = \frac{V}{Z} = \frac{50V \angle 130^\circ}{5} = 10V \angle 130^\circ = 8.66 + 5j$$

$$I_A = \frac{50V \angle 130^\circ}{3 - 1j} = \frac{50V \angle 130^\circ}{5 \angle -53.13^\circ} = 10V \angle 83.13^\circ \\ = 1.19 + 9.9j$$

$$I_A = 4.85 + 14.9j$$

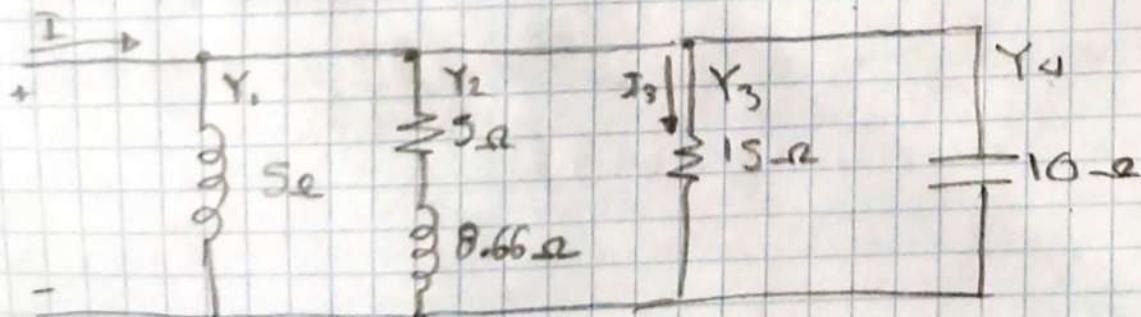
$$(27.9A \angle 57.8^\circ) - (9.85 + 14.9j) \\ = (14.86 + 23.6) - (9.85 + 14.9j)$$

$$I_3 = 5.01 + 8.7j = 10.03 \angle 60^\circ$$

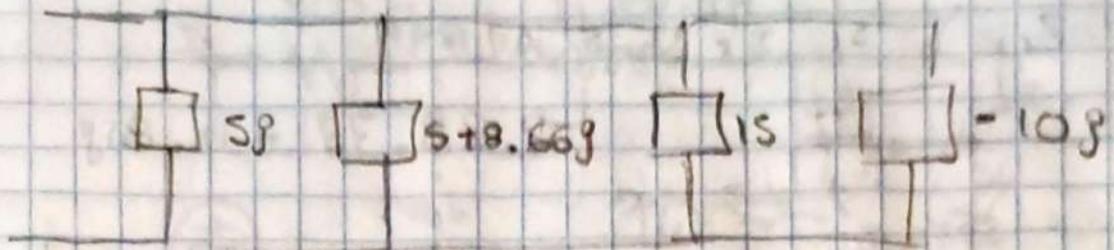
$$Z = \frac{V}{I_3} = \frac{50V \angle 130^\circ}{10.03 \angle 60^\circ} = 4.98 \angle -30^\circ \\ = 4.31 - 2.49j$$

Parte el sig. cto

- Calcular impedancia equivalente  $Z_{eq}$  y la admitancia equivalente  $Y_{eq}$
- Intensidad de corriente total  $I$  que absorbe el cto es  $33A \angle 130^\circ$ . Obtener intensidad de corriente por la rama  $I_3$  y la tensión  $V$ .



a)



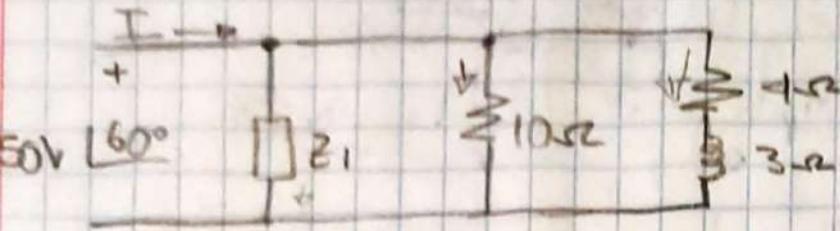
$$\frac{1}{5j} + \frac{1}{5+8.66j} + \frac{1}{15} + \frac{1}{-10j}$$

$$\frac{1}{5j} + \frac{5j}{5+8.66j} = \frac{(0.04 + 0.2j) + (0.05 - 0.08j) + (0.06)}{99.9956} = 0.05 - 0.08j$$

$$\frac{(5 - 8.66j)}{(5 + 8.66j)(5 - 8.66j)} = \frac{25 + 79.9956}{99.9956} = \underline{\underline{100j}}$$

Determinar  $Z_1, Y_1$  si  $I = 31.5 \text{ A} \angle 29^\circ$

$$28.77 + j2.81 \text{ A}$$



$$I_1 = \frac{V}{Z_1} = \frac{50V \angle 60^\circ}{10} = 5V \angle 60^\circ = 2.5 + j4.33 \text{ A}$$

$$I_3 = \frac{V}{Z_3} = \frac{50V \angle 60^\circ}{4 + j3} = \frac{50V \angle 60^\circ}{5 \angle 36.86^\circ} = 10 \angle 23.19^\circ$$

$$I_4 = 11.69 + j8.25 \text{ A}$$

$$I_T = I_4 + I_1 \quad I_T - I_4 = I_1 = (28.77 + j2.81) - (9.19 + j3.92)$$
$$= 19.58 + j8.89 \text{ A} = 21.5 \angle 24.41^\circ$$

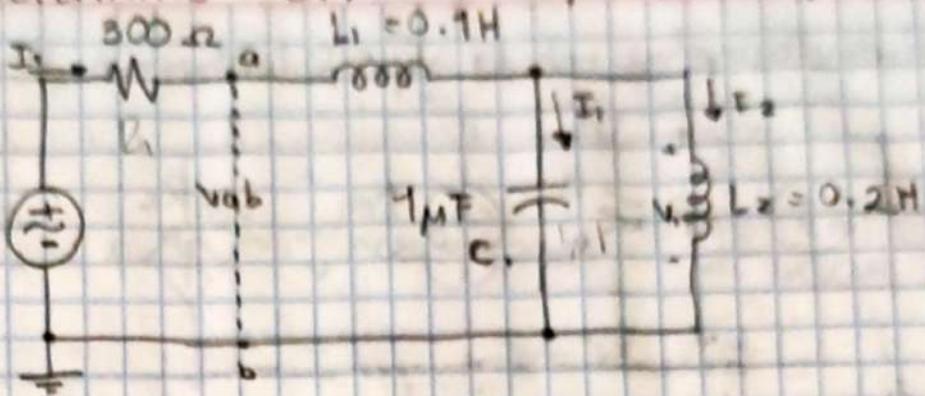
$$Z = \frac{V}{I_1} = \frac{50V \angle 60^\circ}{21.5 \angle 24.41^\circ} = 2.32 \angle 35.6^\circ$$

$$= 1.88 + j1.35 \text{ A} \quad Z = 2 + j2 \text{ ohms}$$

$$Y = \frac{1}{Z}$$

$$Y = \left( \frac{1}{1.88 + j1.35} \right) \left( \frac{1.88 - j1.35}{1.88 + j1.35} \right) = \frac{1.88 - j1.35}{3.5 + j1.82} = 0.35 - j0.25 \text{ S}$$

Determine  $Z_L$ ,  $I_S$ ,  $E_i$ ,  $I_A$ ,  $V_{ab}$  u  $V_{ab}$



$$e = \sqrt{2}(50) \sin \frac{2\pi \cdot 1000t}{w} + 0$$

$$V_{ab} = V_a - V_b$$

AKL

$$\sqrt{2}(50)\left(\frac{1}{\sqrt{2}}\right)$$

$$50 \angle 0^\circ$$

$$V_{dc} R_1 + V \oplus$$

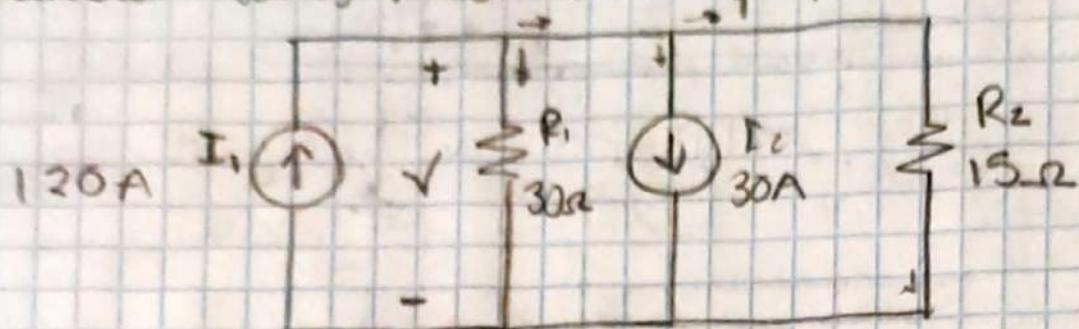
$$Z_L = j 2\pi(1000)(0.2)$$

$$= 1256.63 j$$

$$Z_C = \frac{1}{j(2\pi)(1000)(1 \times 10^{-6})} = 159.15 j$$

1 - 12  
la corriente

Calcular voltaje, corriente y potencia en  $R_1$  y  $R_2$



$$120 = \frac{V}{30} + 30 + \frac{V}{15}$$

$$V \left( \frac{1}{30} + \frac{1}{15} \right) = 90$$

$$V (0.1) = 90$$

$$V_1 = R_1 (I_1)$$

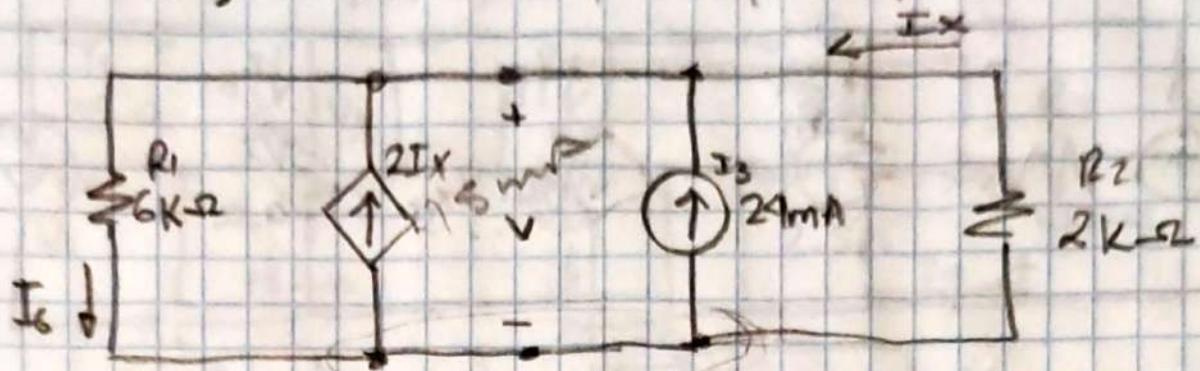
$$I_1 = \frac{V_1}{R_1} = \frac{900}{30} = 30 \text{ A}$$

$$I_2 = \frac{V_1}{R_2} = \frac{900}{15} = 60 \text{ A}$$

$$P = V^2 \quad P_1 = (900)^2 (30) = 270000 \text{ W} = 27 \text{ kW}$$

$$P_2 = (900)^2 (60) = 60000 \text{ W} = 60 \text{ kW}$$

Determina  $V$ , corrientes  $I_V$ ,  $I_x$  y la potencia en la parte dep.



$$I_6 = (2I_x + I_3 - (-I_x))$$

$$\frac{V}{6k\Omega} = -2\left(\frac{V}{2k\Omega}\right) + 24mA + \frac{V}{2k\Omega}$$

$$V\left(\frac{1}{6000} - \frac{2}{2000} + \frac{1}{2000}\right) = 20 \times 10^{-3} A$$

$$V(-1.66 \times 10^{-3}) = 20 \times 10^{-3} A$$

$$V = -12V$$

$$I = \frac{V}{R} \quad I_x = \frac{12V}{2000\Omega} = 6 \times 10^{-3} A \quad 6mA$$

$$I_6 = \frac{-15V}{6000} = -2.5mA \quad 15mA$$

$$P = V_i = (-15V)(15mA) =$$

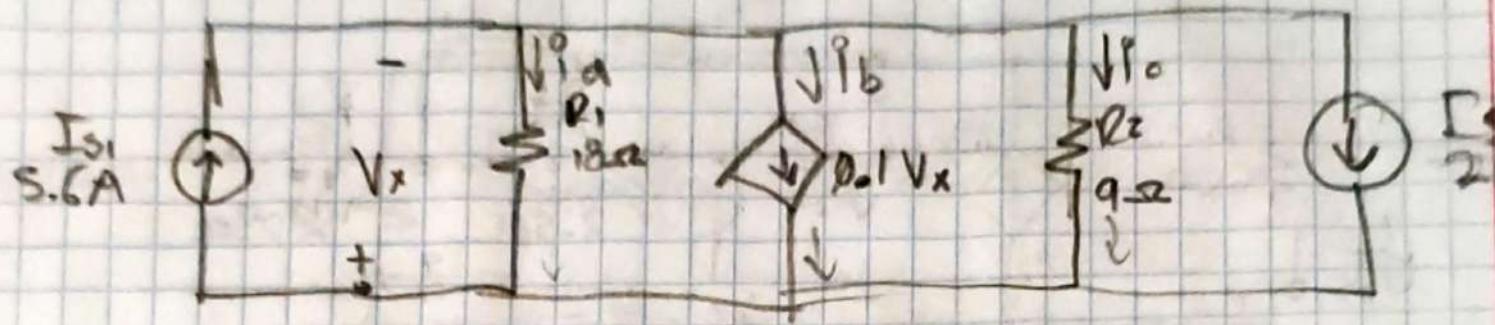
$$V = IR$$

$$I_x = -\frac{V}{R_2}$$

$$I_6 = \frac{V}{R_1}$$

$$14.4V$$

Determine  $V_x$  y los corrientes  $i_a$ ,  $i_b$  e  $i_c$



$$5.6A = \frac{V}{18} + 0.1V_x + \frac{V_x}{9\Omega} + 2A$$

$$3.6A = V \left( \frac{1}{18} + 0.1 + \frac{1}{9} \right)$$

$$V(0.26) = 3.6A$$

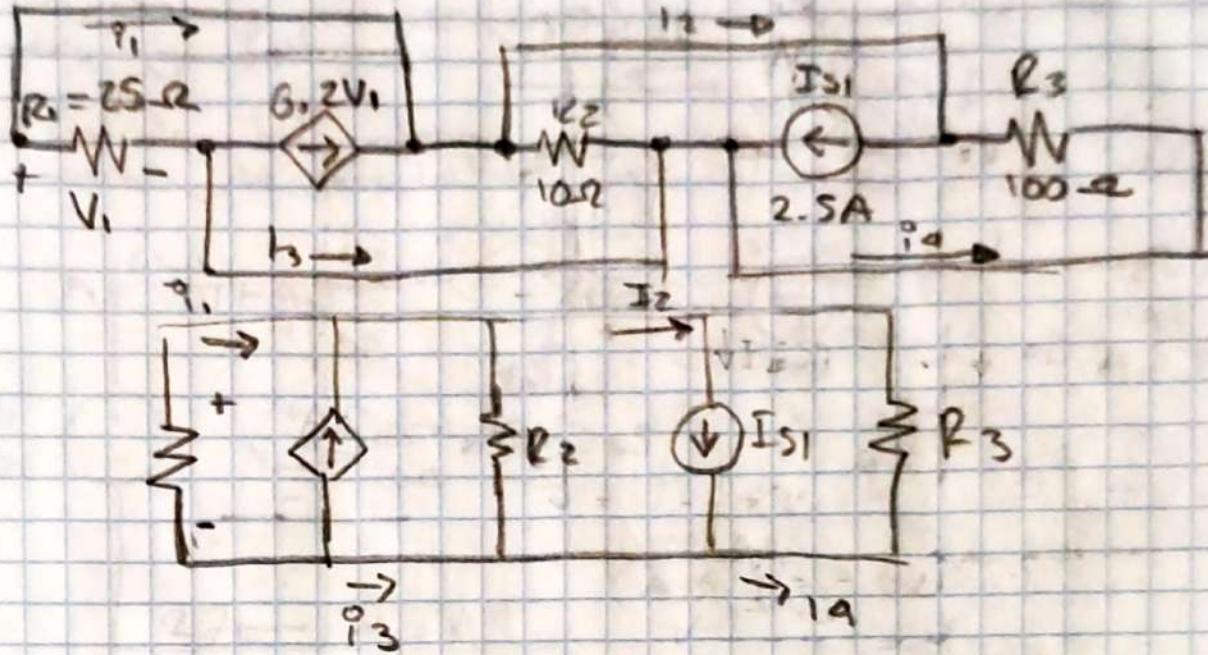
$$V = 13.5V$$

$$I_a = \frac{V}{R} = \frac{13.5}{18} = 0.75$$

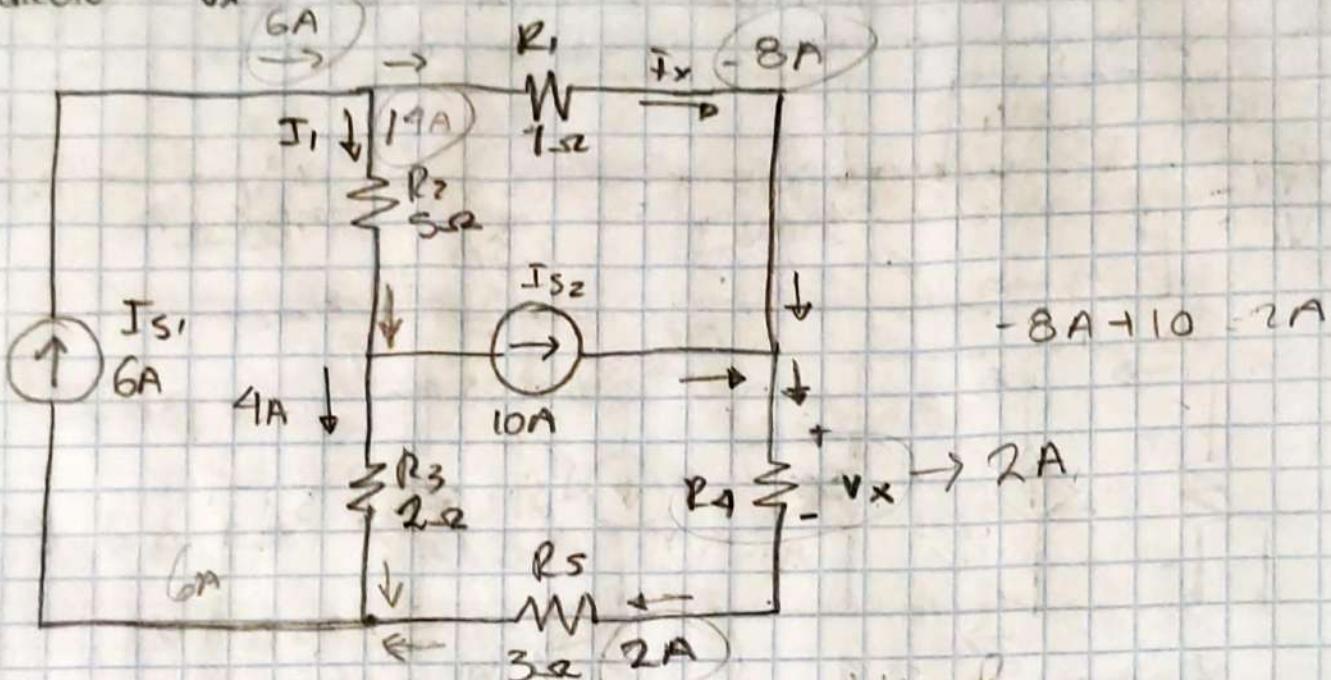
$$I_b = 0.1V_x = (0.1)(13.5) = 1.35$$

$$I_c = \frac{V}{R} = \frac{13.5}{9} = 1.5$$

Calculator și Voltajele  $V_1$ ,  $i_1$ ,  $i_2$ ,  $i_3$  și  $i_4$



Calculate  $V_x$



$$-8A + 10 = 2A$$

$$V_x = 2$$

$$6A = 14 + I_x$$

$$6A - 14 = -8A$$

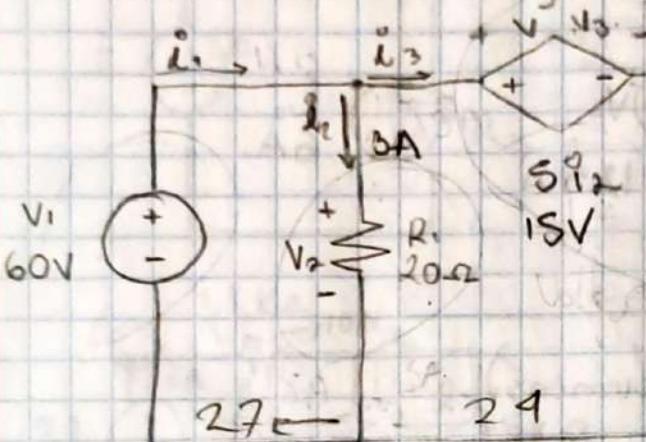
$5i_2 = \text{Voltage}$

$\frac{V_1}{R} = \text{Corriente}$

$$V = IR$$

$$I = \frac{V}{R}$$

- a) Utilizar leyes de Kirchhoff y de Ohm en un procedimiento paso por paso para evaluar todas las corrientes y voltajes.
- b) Calcular la potencia que absorbe  $\%_o$  de los cinco elementos del circuito y mostrar que la suma es cero.



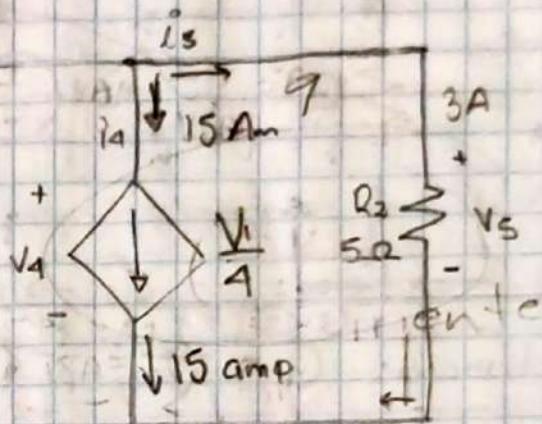
$$i_2 = (60/20) = 3A$$

$$P_{R1} = 60(60/20) = 180 W$$

$$i_3 = 15A$$

$$V_3 = 5i_2 = 5(3A) = 15V //$$

15



$$15/5 = 3A$$

$$P = VI$$

$$P_{R1} = (60V)(18A) = 1080W$$

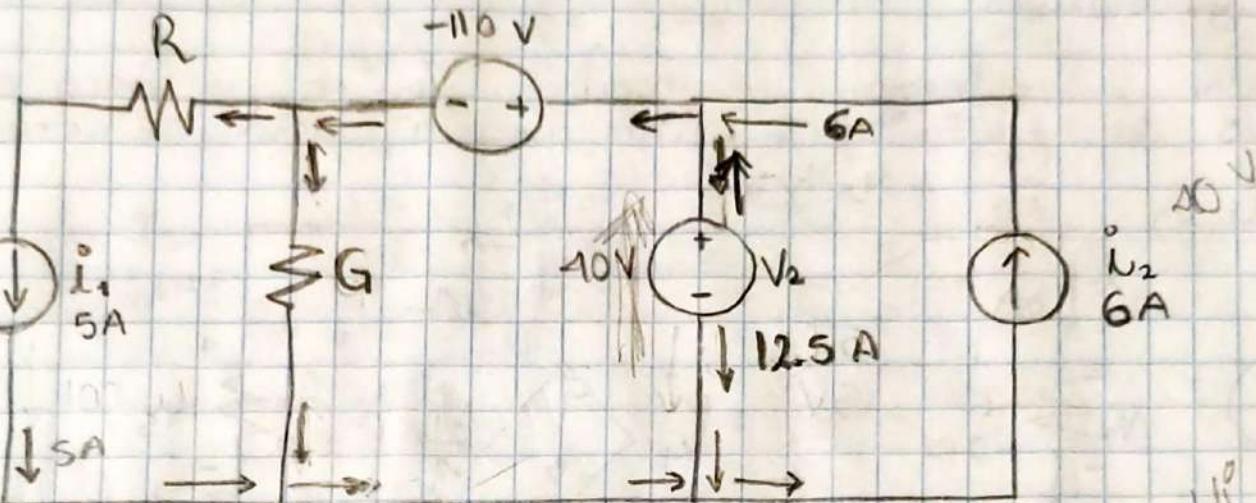
$$\rightarrow P_{R1} = 180 W$$

$$P_{i4} = (15V)(12A) = 180 W$$

$$P_{R2} = (15V)(3A) = 45 W$$

15  
15  
9

Encuentre R y G si la f.c de 5A está suministrando 100 W y la f.c. de 70 V proporciona 500 W.



$$\text{Conductancia: } G = \frac{i}{v} = \frac{1}{R} \text{ (Siemens)}$$

$$P = V_i^2 = V^2 G = \frac{i^2}{G}$$

$$V_1 = \frac{P}{i} = \frac{100W}{5A} = 20V$$

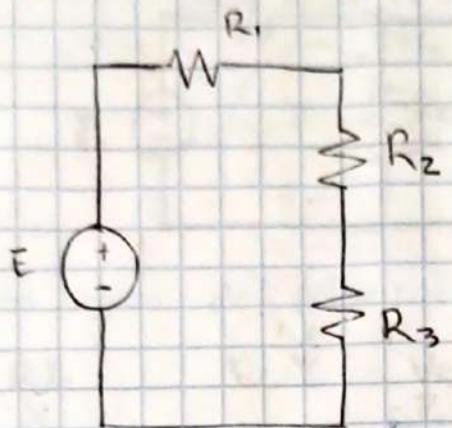
$$i = \frac{P}{V} = \frac{500W}{40V} = 12.5A$$

$$P = V_i^2 = \frac{500}{G}$$

## UNIDAD II

(1) DIVISIÓN DE VOLTAJE, DIVISIÓN DE CORRIENTE, MALLAS, NODOS.)

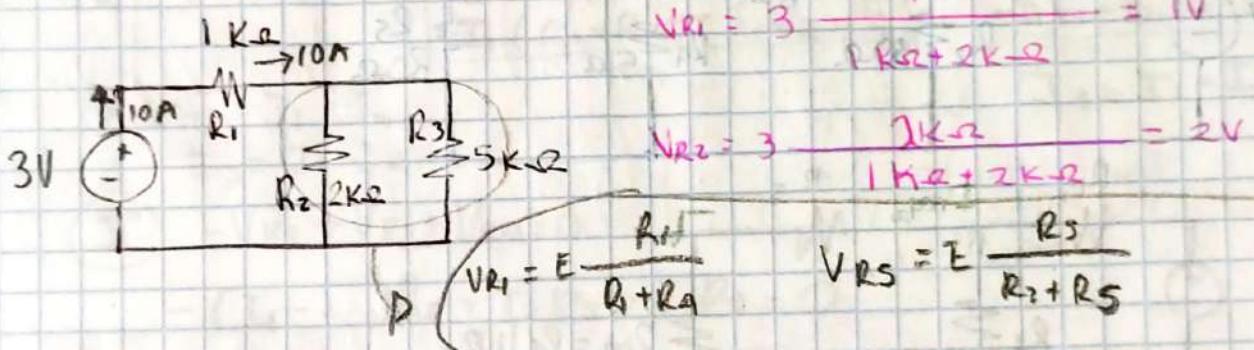
### DIVISOR DE VOLTAJE.



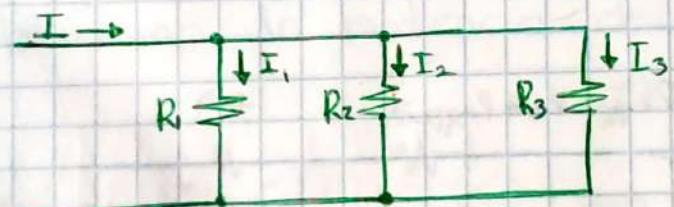
$$VR_1 = E \frac{R_1}{R_1 + R_2 + R_3}$$

$$VR_2 = E \frac{R_2}{R_1 + R_2 + R_3}$$

$$VR_3 = E \frac{R_3}{R_1 + R_2 + R_3}$$

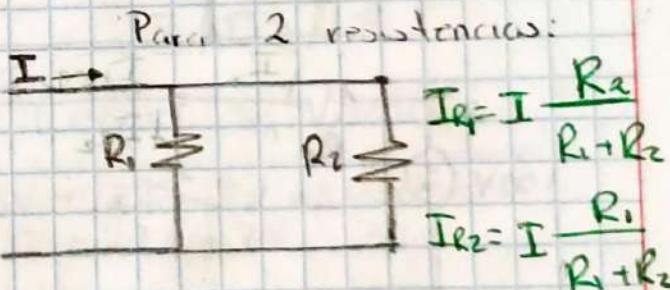


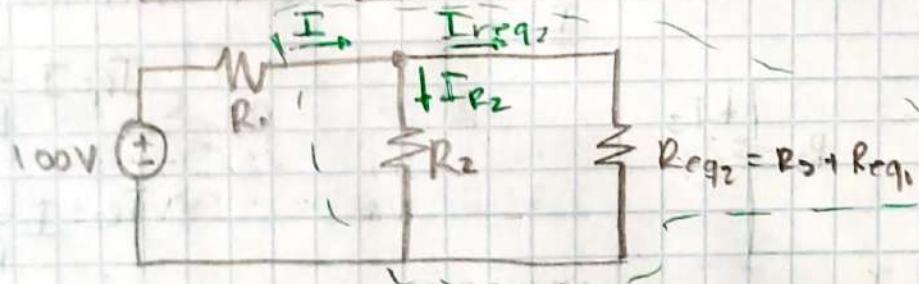
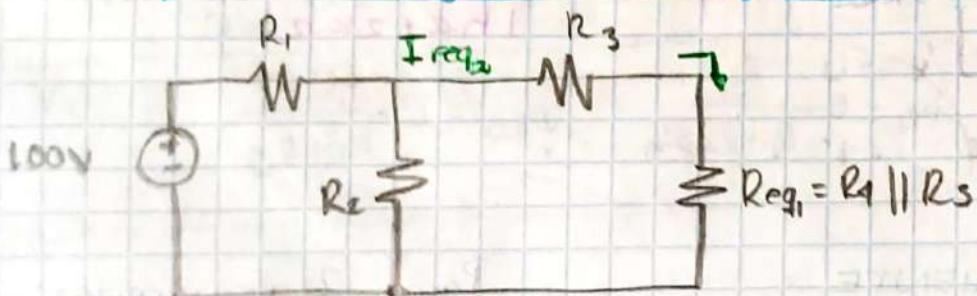
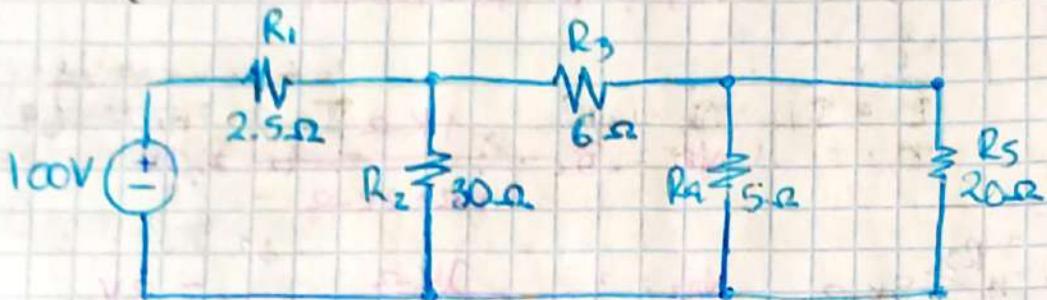
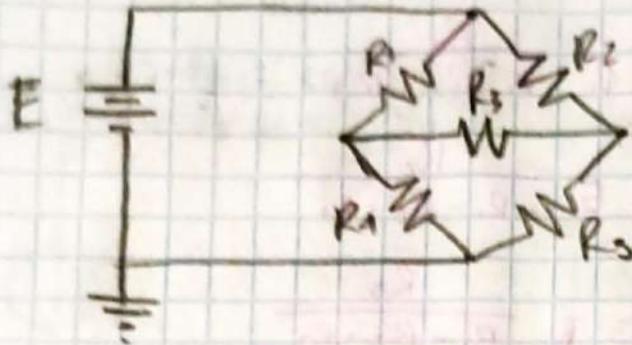
### DIVISOR DE CORRIENTE.



De manera general

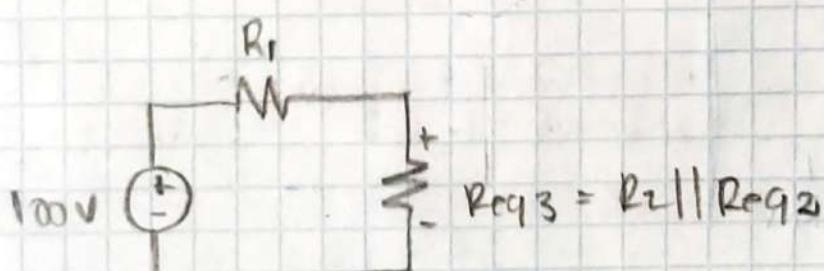
$$I_{Rx} = I \frac{\frac{1}{R_x}}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_N}}$$





$$I_{R2} = I \frac{R_{req2}}{R_2 + R_{req2}}$$

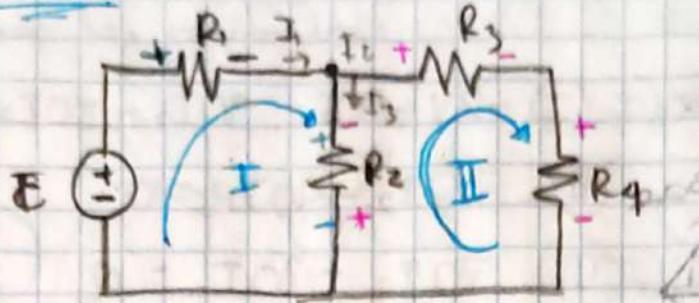
$$I_{req2} = I - \frac{R_2}{R_2 + R_{req2}}$$



$$V_{R1} = 100 \frac{R_1}{R_1 + R_{req3}}$$

$$V_{R_{req3}} = 100 \frac{R_{req2}}{R_1 + R_{req3}}$$

## Mallas



# Mallas = # Ecas

Con signos de polarización.

$$V = RI$$

$$I = \frac{V}{R}$$

$$\text{Ec I. } V_1 + V_2 + V_3 = 0$$

$$-E + VR_1 + VR_2 = 0$$

$$E = I_1 R_1 + (I_1 - I_2) R_2$$

$$I_1 (R_1 + R_2) - I_2 R_2 = E \times$$

$$\text{Ec. II}$$

$$VR_2 + VR_3 + VR_4 = 0$$

$$(I_2 - I_1) R_2 + I_2 R_3 + I_2 R_4 = 0$$

$$-I_1 R_2 + I_2 (R_2 + R_3 + R_4) = 0$$

$$\textcircled{I} \quad I_1 = I_2 + I_3$$

$$I_3 = I_1 - I_2$$

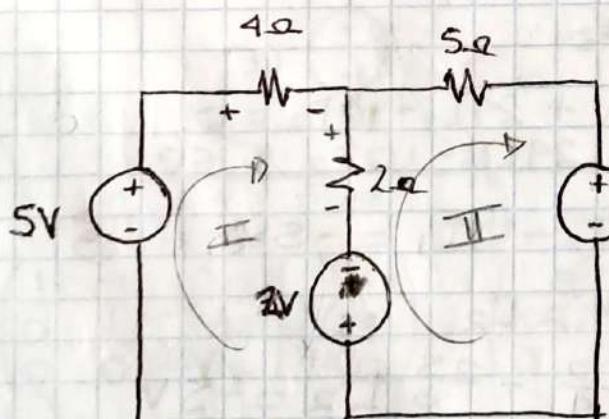
$$\textcircled{II} \quad -VR_2 + VR_3 + VR_4 = 0$$

$$-(I_1 - I_2) R_2 + I_2 R_3 + I_2 R_4 = 0$$

$$I_3 = I_1 - I_2$$

7/03/19

Determine la potencia de la fuente de 2V.



$$\textcircled{I} \quad 5V + 6I_1 - 2I_2 - 2V = 0 \quad | \cdot 1$$

$$6I_1 - 2I_2 = 3V$$

$$2V + 7I_2 - 2I_1 + 1V = 0$$

$$-2I_1 + 7I_2 = -3V$$

$$\begin{pmatrix} 6 & -2 & | & 3 \\ -2 & 7 & | & 0 \end{pmatrix} \sim \begin{pmatrix} 1 & -1/3 & | & 1/2 \\ 0 & 1/3 & | & -2/3 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & | & 1/3 \\ 0 & 1 & | & -2/19 \end{pmatrix} \approx \begin{pmatrix} 1 & 0 & | & 1/3 \\ 0 & 1 & | & -0.10 \end{pmatrix}$$

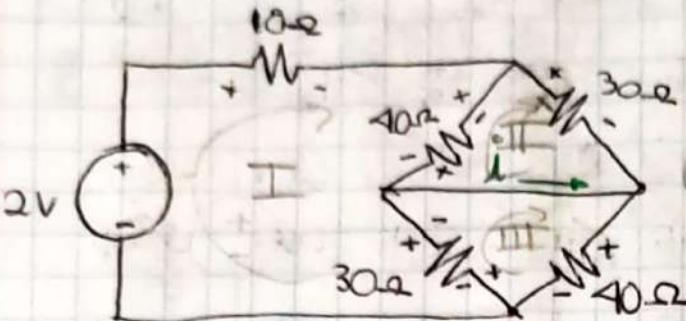
$$P = VI$$

$$I = I_1 - I_2 \\ = 4/3/38 + 2/19 = 47/38 \approx 1.2368$$

2. 27

$$P = VI = (2V)(1.2368A) = \underline{2.47W}$$

Determine la corriente  $i$



$$\begin{array}{l} \textcircled{I} -2V + 80I_1 - 40I_2 - 30I_3 = 0 \\ \textcircled{II} 70I_2 - 40I_1 = 0 \\ \textcircled{III} 70I_3 - 30I_1 = 0 \end{array}$$

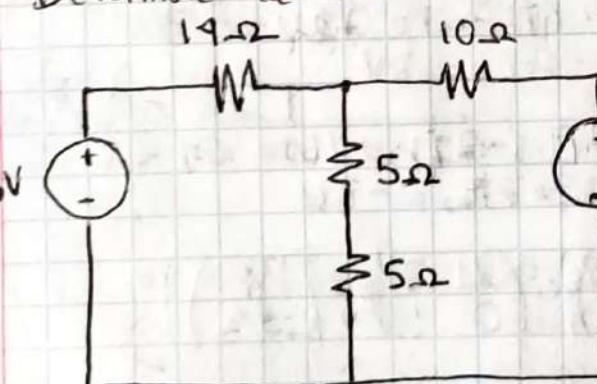
$$\left( \begin{array}{ccc|c} 80 & -40 & -30 & 2 \\ -40 & 70 & 0 & 0 \\ -30 & 0 & 70 & 0 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -1/2 & -3/8 & 1/40 \\ 0 & 50 & -15 & 0 \\ 0 & -15 & 235/4 & 3/4 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -1/2 & -3/8 & 1/40 \\ 0 & 1 & -3/10 & 0 \\ 0 & 0 & 27/4 & 23/20 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & -1/2 & 0 & 1/31 \\ 0 & 1 & 0 & 4/155 \\ 0 & 0 & 1 & 3/155 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & 0 & 7/155 \\ 0 & 1 & 0 & 4/155 \\ 0 & 0 & 1 & 3/155 \end{array} \right) \begin{matrix} I_1 \\ I_2 \\ I_3 \end{matrix}$$

$$i = I_3 - I_2 = \frac{3}{155} - \frac{4}{155} = -\frac{1}{155} \approx 6.45 \times 10^{-3} \text{ A}$$

~~6.45 mA~~

Determine la corriente  $i_1$  e  $i_2$



$$\begin{array}{l} \textcircled{I} -6V + 24I_1 - 10I_2 = 0 \\ 24I_1 - 10I_2 = 6V \end{array}$$

$$\textcircled{II} 20I_2 - 10I_1 = -5V$$

$$I_1 = \frac{1}{4} + \frac{5}{12}I_2$$

$$20I_2 - \frac{10}{4} - \frac{25}{6}I_2 = -5V$$

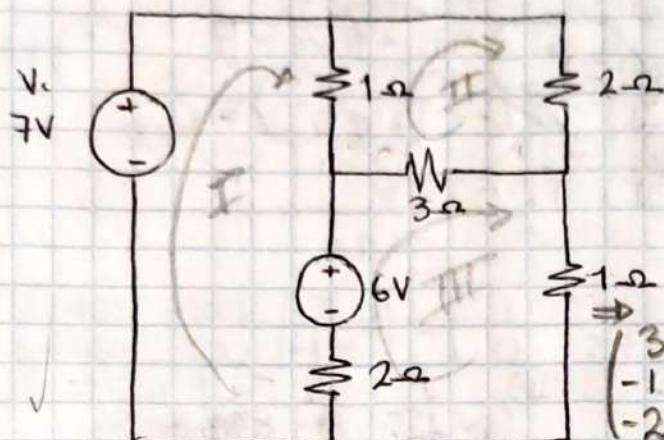
$$\frac{95}{6}I_2 = -\frac{5}{2}$$

$$I_2 = -0.1578 \Rightarrow I_1 = \frac{1}{4} + \frac{5}{12}(-0.1578) = 0.1892$$

~~0.1892~~

~~ANALISIS DE~~

Determine las corrientes



$$I) -7V + 3I_1 - I_2 - 2I_3 + 6V = 0$$

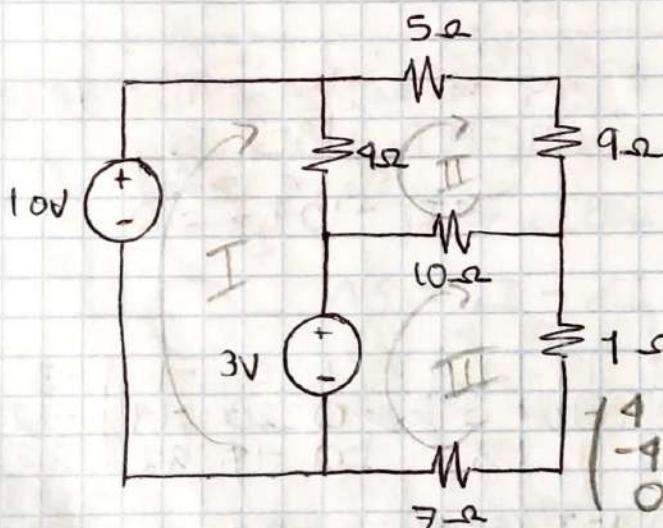
$$3I_1 - I_2 - 2I_3 = 1$$

$$II) 6I_2 - I_1 - 3I_3 = 0$$

$$III) 6I_3 - 2I_1 - 3I_2 = 6$$

$$\left( \begin{array}{ccc|c} 3 & -1 & -2 & 1 \\ -1 & 6 & -3 & 0 \\ -2 & -3 & 6 & 6 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -6 & 3 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 3 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & -6 & 3 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 3 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 3 \end{array} \right) \begin{matrix} I_1 \\ I_2 \\ I_3 \end{matrix}$$



$$I) -10V + 4I_1 - 4I_2 + 3V = 0$$

$$-4I_1 - 4I_2 = -7$$

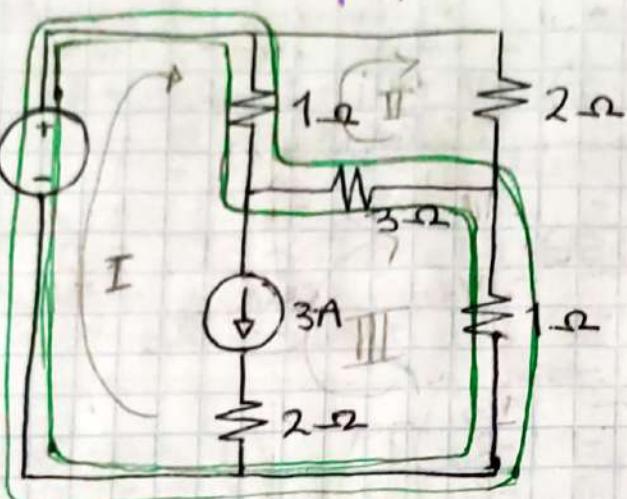
$$II) 28I_2 - 4I_1 - 10I_3 = 0$$

$$III) 18I_3 - 10I_2 = 3$$

$$\left( \begin{array}{ccc|c} 4 & -4 & 0 & 7 \\ -4 & 28 & -10 & 0 \\ 0 & -10 & 18 & 3 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -1 & 0 & 7/4 \\ 0 & 24 & -10 & 0 \\ 0 & -10 & 18 & 3 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & -1 & 0 & 7/4 \\ 0 & 1 & -5/12 & 7/24 \\ 0 & 0 & 83/6 & 71/12 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & 0 & 737/332 \\ 0 & 1 & 0 & 39/83 \\ 0 & 0 & 1 & 71/166 \end{array} \right) \approx \begin{matrix} 2.2198 \\ 0.4698 \\ 0.4277 \end{matrix} \begin{matrix} A \\ A \\ A \end{matrix}$$

# SUPERMALLAS



$$\text{I}) -7V + I_1 - I_2 + 3I_3 - 3I_2 + I_3 = 0$$

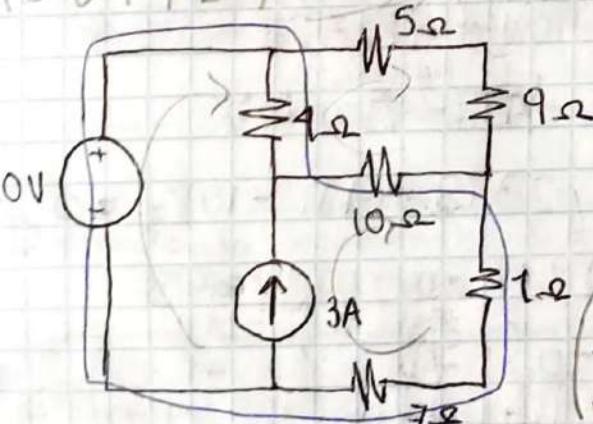
$$I_1 - 4I_2 + 4I_3 = 7$$

$$\text{II}) 6I_2 - I_1 - 3I_3 = 0$$

$$\text{III}) I_1 - I_3 =$$

$$\left( \begin{array}{ccc|c} 1 & -4 & 9 & 7 \\ -1 & 6 & -3 & 0 \\ 1 & 0 & 1 & 7 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -4 & 9 & 7 \\ 0 & 2 & 1 & 7 \\ 0 & 4 & -5 & 0 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -4 & 9 & 7 \\ 0 & 1 & \frac{1}{2} & \frac{7}{2} \\ 0 & 0 & -7 & -14 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -4 & 0 & -1 \\ 0 & 1 & 0 & \frac{5}{2} \\ 0 & 0 & 1 & 2 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & 0 & 0 & 9 \\ 0 & 1 & 0 & \frac{5}{2} \\ 0 & 0 & 1 & 2 \end{array} \right) \xrightarrow{\text{2.5}} \left( \begin{array}{ccc|c} 1 & 0 & 0 & 9 \\ 0 & 1 & 0 & 2.5 \\ 0 & 0 & 1 & 2 \end{array} \right)$$



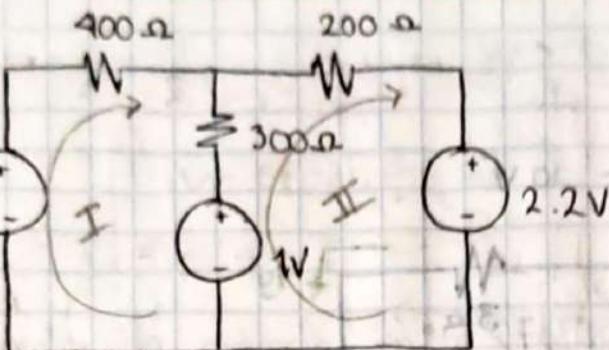
$$\text{I}) -9I_1 - 9I_2 + 18I_3 = 10$$

$$\text{II}) 28I_2 - 9I_1 - 10I_3 = 0$$

$$I_3 - I_1 = 3A$$

$$\left( \begin{array}{ccc|c} 9 & -9 & 18 & 10 \\ -1 & 28 & -10 & 0 \\ -1 & 0 & 1 & 3 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & -1 & -3 \\ 0 & 28 & -19 & -12 \\ 0 & -19 & 22 & 22 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & 0 & -1 & -3 \\ 0 & 1 & -\frac{1}{2} & -\frac{3}{2} \\ 0 & 0 & \frac{1}{5} & \frac{16}{5} \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & 0 & -\frac{29}{10} \\ 0 & 1 & 0 & \frac{11}{10} \\ 0 & 0 & 1 & \frac{16}{5} \end{array} \right) \approx \begin{matrix} -1.93 \\ 0.1097 \\ 1.066 \end{matrix}$$



$$I) -1 + 900I_1 - 300I_2 + 14 = 0$$

$$900I_1 - 300I_2 = 3$$

$$II) -14 + 500I_2 - 300I_1 + 2.2 = 0$$

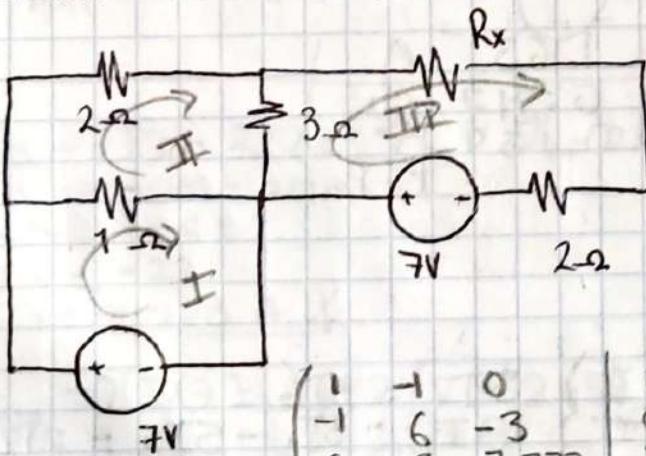
$$-300I_1 + 500I_2 = -1.2$$

$$\left( \begin{array}{cc|c} 400 & -300 & 3 \\ -300 & 500 & -1.2 \end{array} \right) \sim \left( \begin{array}{cc|c} 1 & -\frac{3}{4} & \frac{3}{400} \\ 0 & 275 & \frac{21}{20} \end{array} \right) \sim \left( \begin{array}{cc|c} 1 & 0 & \frac{57}{5500} \\ 0 & 1 & \frac{21}{5500} \end{array} \right)$$

$$0.0103 \text{ A}$$

$$3.8 \text{ mA}$$

Determine  $R_x$  si  $I_2 = 2.273 \text{ A}$



$$I) -7 + I_1 - I_2 = 0$$

$$I_1 - I_2 = 7$$

$$II) 6I_2 - I_1 - 3I_3 = 0$$

$$III) 7.273I_3 - 3I_2 = 7$$

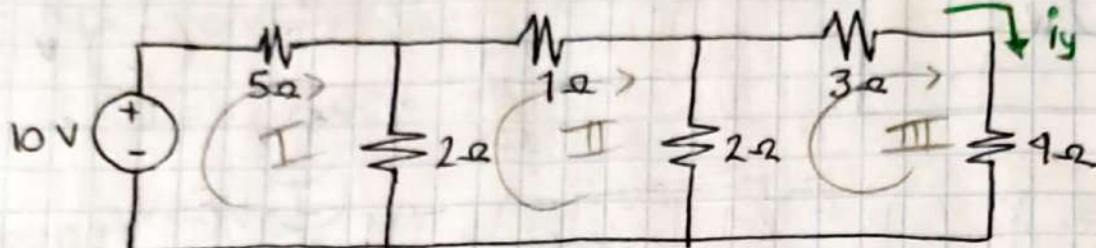
$$\left( \begin{array}{ccc|c} 1 & -1 & 0 & 0 \\ -1 & 6 & -3 & 0 \\ 0 & -3 & 7.273 & 7 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -1 & 0 & 0 \\ 0 & 5 & -3 & 0 \\ 0 & -3 & 7.273 & 7 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & -1 & 0 & 0 \\ 0 & 1 & -3/5 & 0 \\ 0 & 0 & 5.473 & 7 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & 0 & 0.7674 \\ 0 & 1 & 0 & 0.7674 \\ 0 & 0 & 1 & 1.2790 \end{array} \right)$$

## Mallas

- Determine la corriente  $i_y$

- Potencia suministrada por la fte de 10V 16.33 W



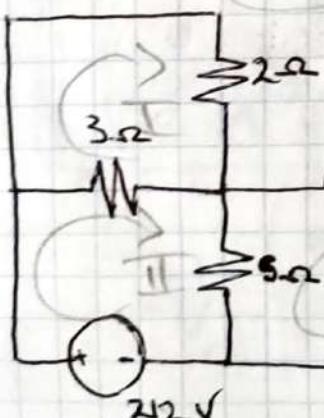
$$I) -10V + 7I_1 - 2I_2 = 0 \\ 7I_1 - 2I_2 = 10$$

$$II) 5I_1 - 2I_1 - 2I_3 = 0 \\ III) 9I_3 - 2I_2 = 0$$

$$\left( \begin{array}{ccc|c} 7 & -2 & 0 & 10 \\ -2 & 5 & -2 & 0 \\ 0 & -2 & 9 & 0 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -2/7 & 0 & 10/7 \\ 0 & 3/7 & -2 & 20/7 \\ 0 & -2 & 9 & 0 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -2/7 & 0 & 10/7 \\ 0 & 1 & -9/2 & 20/7 \\ 0 & 0 & 25/14 & 0 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & 0 & 0 & 410/251 \\ 0 & 1 & 0 & 180/251 \\ 0 & 0 & 1 & 40/251 \end{array} \right) \approx \begin{matrix} 1.63 \\ 0.717 \\ 0.159 \end{matrix} A$$

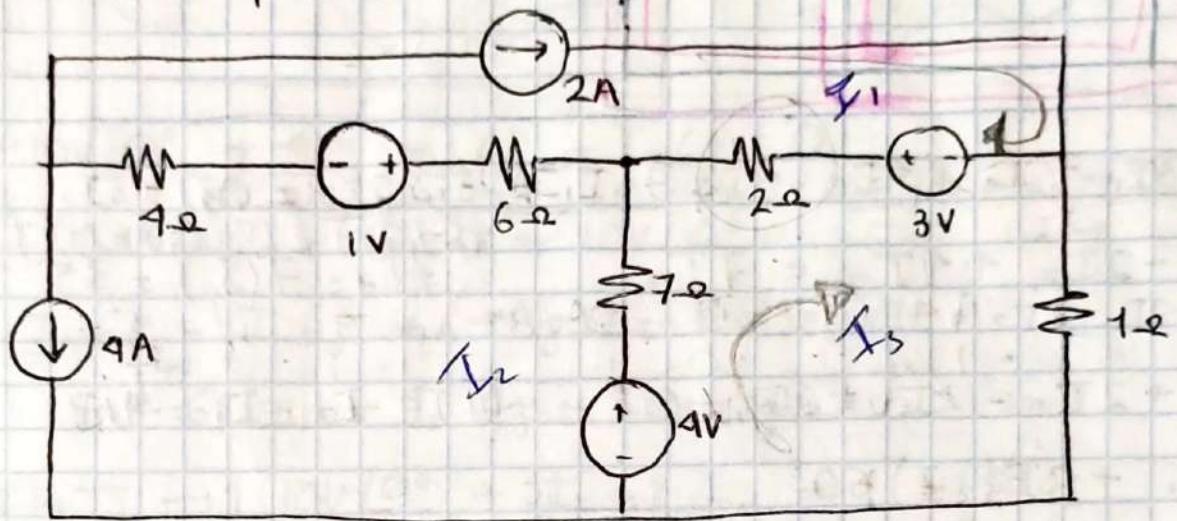
Corriente en  $R=2\Omega$  y  $R=5\Omega$   
26.48.



$$I) 5I_1 - 3I_2 = 0 \\ II) 8I_2 - 3I_1 - 5I_3 = 212 \\ III) 8I_3 - 5I_2 = -122$$

$$\sim \left( \begin{array}{ccc|c} 5 & -3 & 0 & 0 \\ -3 & 8 & -5 & 212 \\ 0 & -5 & 8 & -122 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -3/5 & 0 & 0 \\ 0 & 31/5 & -5 & 212 \\ 0 & -5 & 8 & -122 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -3/5 & 0 & 0 \\ 0 & 1 & -25/31 & 1060/31 \\ 0 & 0 & 123/31 & 938 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & -3/5 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & -25/31 \end{array} \right)$$

Calcular la potencia en la fijo de 2A.



$$10I_3 - 7I_2 - 2I_1 = 1 \quad I_1 = 2A \quad I_2 = -4A$$

$$10I_3 - 7(-4) - 2(2) = 1$$

$$10I_3 + 28 - 4 = 1$$

$$10I_3 = -23$$

$$I_3 = -2.3A \quad \text{X}$$

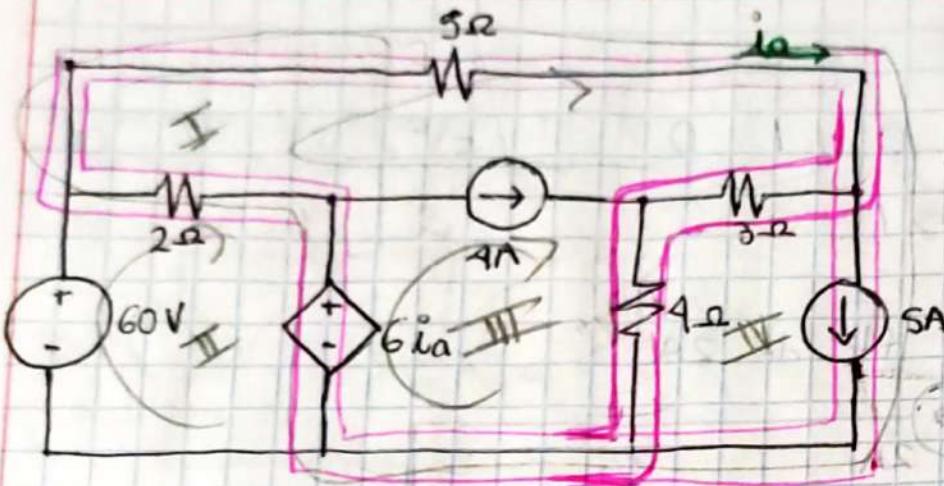
$$\checkmark V_{R_{2\Omega}} = 2(I_1 - I_3) = 2[2 - (-2.3)] = 2(4.3) = 8.6$$

$$\checkmark V_{6\Omega} = 6(I_1 - I_2) = 6[2 - (-4)] = 6(6) = 36$$

$$\checkmark V_{R4} = 4(I_1 - I_2) = 4[2 - (-4)] = 4(6) = 24$$

$$V_T = -3 + 8.6 + 36 + 24 + 1 = 66.6$$

$$P = VI = (66.6)(2) = 133.2 \quad \text{X}$$



Potencia en  $R = 2\Omega$

Sea  $i_a = I_1$

$$I_4 = SA$$

$$\text{I}) \underline{5I_1} + \underline{3I_1} - \underline{3I_1} + \underline{4I_3} - \underline{4I_4} - \underline{6I_1} + \underline{2I_1} - \underline{2I_2} = 0$$

$$4I_1 - 2I_2 + 4I_3 = 7I_4$$

$$4I_1 - 2I_2 + 4I_3 = 35$$

$$7I_1 : 7(5) = 35$$

$$\text{II}) -60 + 2I_2 - 2I_1 + 6I_1 = 0, \quad \text{III}) = I_3 - I_1 = 4A$$

$$4I_1 + 2I_2 = 60$$

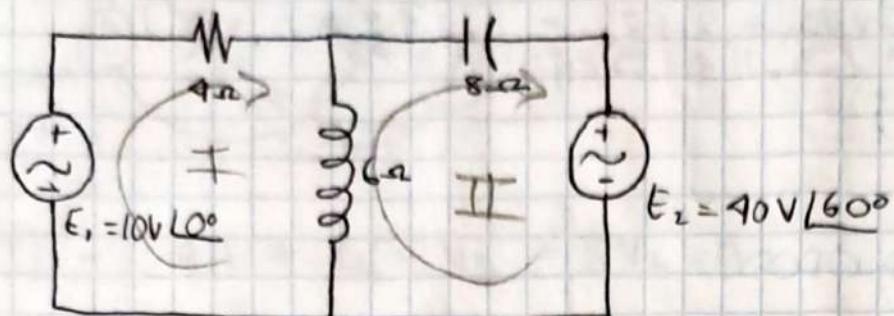
$$\left( \begin{array}{ccc|c} 4 & -2 & 4 & 35 \\ 4 & 2 & 0 & 60 \\ -1 & 0 & 1 & 4 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & -1 & -1 \\ 0 & 2 & 4 & 76 \\ 0 & -2 & 8 & 41 \end{array} \right) \sim \left( \begin{array}{ccc|c} 1 & 0 & -1 & -1 \\ 0 & 1 & 2 & 38 \\ 0 & 0 & 12 & 80 \end{array} \right)$$

$$\left( \begin{array}{ccc|c} 1 & 0 & & 2.66 \\ 0 & 1 & 0 & 24.66 \\ 0 & 0 & 1 & 6.66 \end{array} \right)$$

$$(I_1 - I_2) = 2.66 - 24.66 = -$$

$\downarrow$   $6^\circ$

Calcule la corriente a través de R



$$I) -10V \angle 0^\circ + 4I_1 + 16j - I_2 6j = 0$$

$$(4+6j)I_1 - I_2 6j = 10V \angle 0^\circ$$

$$II) I_2 6j - I_1 6j + (-8j)I_2 + 40V \angle 60^\circ = 0$$

$$-6j I_1 - I_2 2j = -40V \angle 60^\circ$$

$$\text{de } I) \Rightarrow I_1 = \frac{10V \angle 0^\circ}{4+6j} + \frac{I_2 6j}{4+6j}$$

$$= \frac{10V \angle 0^\circ}{7.21 \angle 56.30^\circ} + \frac{I_2 6 \angle 90^\circ}{7.21 \angle 56.30^\circ} = 1.38 \angle -56.30^\circ + 0.832 \angle 33.7^\circ$$

$$= 0.76 - 1.14j + I_2 0.69 + 0.46j$$

$$\text{en } II)$$

$$-6j(0.76 - 1.14j + I_2(0.69 + 0.46j)) - I_2 2j = -40V \angle 60^\circ$$

$$(-4.56j + 6.84) + (-4.14j - 2.76)I_2 - I_2 2j = -40V \angle 60^\circ$$

$$I_2 (-2.76 - 4.14j - 2j) = -40V \angle 60^\circ + (4.56j - 6.84)$$

$$I_2 (-2.76 - 6.14j) = -10V \angle 60^\circ + (-6.84 + 4.56j)$$

$$I_2 = \frac{-10V \angle 60^\circ + (-6.84 + 4.56j)}{-2.76 - 6.14j}$$

$$= \frac{-10V \angle 60^\circ + 8.22 \angle 46.30^\circ}{6.73 \angle -114.20^\circ} = -5.99 \angle 74.2 + 1.22 \angle 260^\circ$$

$$= 5.9 - 0.6j - 0.2 - 1.20j$$

$$I_2 = 5.7 - 1.8j$$

$$I_2 = 5.7 - 1.8j$$

$$\begin{aligned} I_1 &= (0.76 - 1.14j) + I_2 (0.69 + 0.46j) \\ &= (0.76 - 1.14j) + (5.7 - 1.8j)(0.69 + 0.46j) \\ &= (0.76 - 1.14j) + (3.93 + 2.62j - 1.29j - 0.828) \\ &= (0.76 - 1.14j) + (3.1 + 1.38j) \\ &= (3.86 + 0.24j) \end{aligned}$$

## ANÁLISIS DE NODOS.

- Se aplican LCK con 2 o mas nodos para obtener las ecuaciones

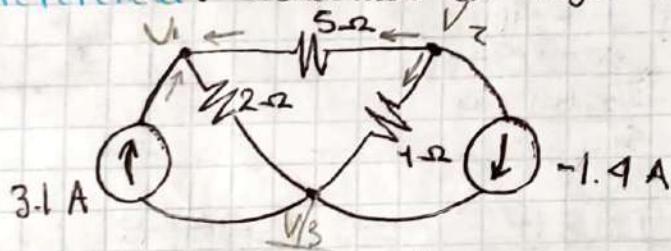
Un circuito de 3 nodos tendrá 2 voltajes desconocidos y 2 ecuaciones

Un circuito de 10 nodos tendrá 9 voltajes desconocidos y 9 ecuaciones

Un circuito de  $N$  nodos tendrá " $N-1$ " voltajes y " $(N-1)$ " ecuaciones

Nodo de referencia: conectado al mayor número de ramas.

Ejemplo.



Para la dirección de la corriente una vez definida, la trabajaremos como: "El nodo del que sale menos el nodo al que llega"

$$I) 3.1 + I_{23} + \frac{V_1}{5}$$

$$3.1 + \frac{V_2 - V_1}{2} + \frac{V_2 - V_1}{5}$$

$$3/5 V_2 - V_1 (\frac{1}{2} + \frac{1}{5}) = -3.1$$

$$II) -1.4 + \frac{V_2 - V_3}{1} + \frac{V_2 - V_1}{5}$$

$$-\frac{6}{5} V_2 + \frac{1}{5} V_1 = 1.4$$

$$\begin{aligned} V_2 &= (1.4 + \frac{1}{5} V_1) \frac{5}{6} \\ &= 1.16 + \frac{1}{6} V_1 \end{aligned}$$

$$-\frac{7}{10} V_1 + \frac{1}{5} (1.16 + \frac{1}{6} V_1) = -3.1$$

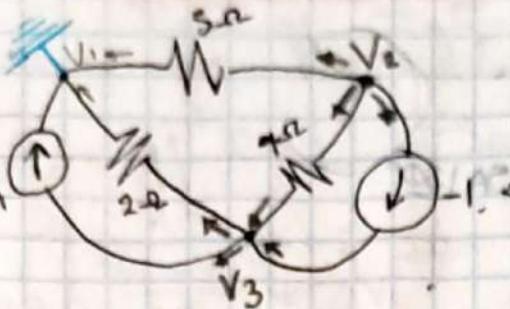
$$-\frac{7}{10} V_1 + 0.232 + \frac{1}{30} V_1 = -3.1$$

$$-\frac{2}{3} V_1 = -3.332$$

$$V_1 = 4.99 \approx 5$$

$$\Rightarrow V_2 = 1.16 + \frac{1}{6} (5)$$

$$= 1.99 \approx 2$$



$$\begin{aligned} V_1 &= 3, 0, 3 \\ V_2 &= 2, 1, -3 \\ V_3 &= 0, -5, -2 \end{aligned}$$

$$I) -1.4A + V_2 - V_3 + \frac{1}{5}V_2 = 0$$

$$\frac{6}{5}V_2 - V_3 = 1.4A$$

$$II) -1.4 + V_2 - V_3 = 3.1 + \frac{1}{2}V_3$$

$$V_2 - \frac{3}{2}V_3 = 4.5$$

$$V_2 = 4.5 + \frac{3}{2}V_3$$

$$\frac{6}{5}(4.5 + \frac{3}{2}V_3) - V_3 = 1.4$$

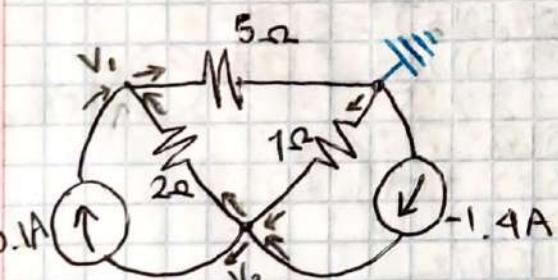
$$5.4 + \frac{9}{5}V_3 - V_3 = 1.4$$

$$\frac{4}{5}V_3 = -4$$

$$V_3 = -5$$

$$V_2 = 4.5 + \frac{3}{2}(-5)$$

$$= -3$$



$$\begin{aligned} ① V_1 &= (4.5 + \frac{3}{2}V_2)2 \\ V_1 &= 9 + 3V_2 \end{aligned} \quad \text{--- } ②$$

$$\frac{7}{5}(9 + 3V_2) - \frac{1}{2}V_2 = 3.1$$

$$\frac{63}{10} + \frac{21}{10}V_2 - \frac{1}{2}V_2 = 3.1$$

$$\frac{8}{5}V_2 = -3.2$$

$$I) -1.4A - V_2 = \frac{V_2 - V_1}{2} + 3.1$$

$$-\frac{3}{2}V_2 + \frac{1}{2}V_1 = 4.5 \quad \text{--- } ①$$

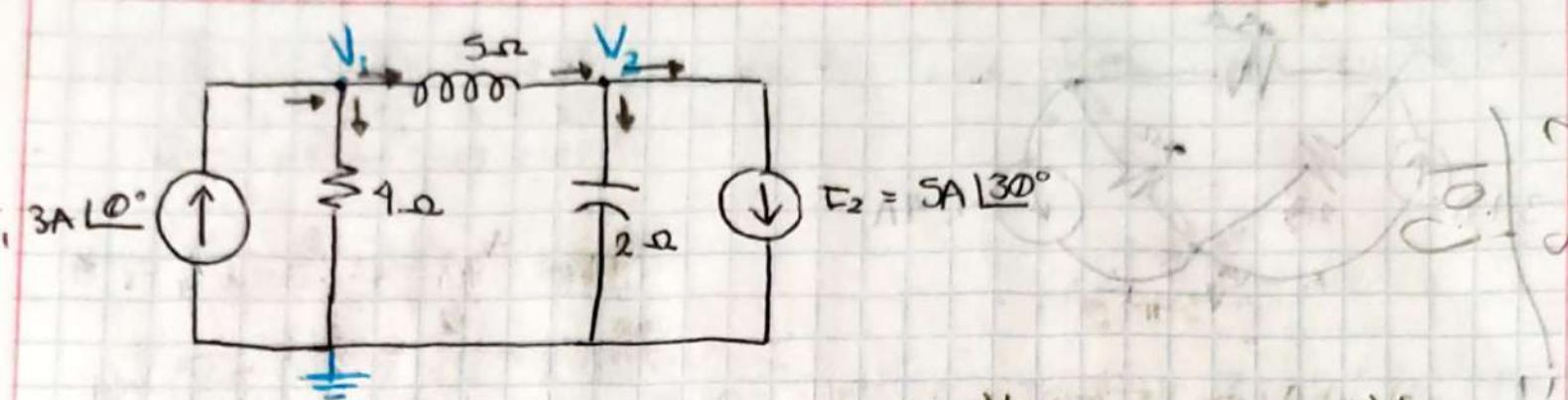
$$II) 3.1 + \frac{1}{2}V_2 - \frac{1}{2}V_1 = \frac{1}{5}V_1$$

$$\frac{7}{10}V_1 - \frac{1}{2}V_2 = 3.1$$

$$V_2 = -16/8$$

$$V_2 = -2$$

$$\begin{aligned} ② V_1 &= 9 + 3(-2) \\ &= 3 \end{aligned}$$



$$\text{I) } \frac{V_1 - V_2}{5j} + \frac{1}{4}V_1 = 3A 0^\circ \quad \text{II) } \frac{V_1 - V_2}{5j} = 5A 130^\circ + \frac{V_2}{-2j}$$

$$\left(\frac{1}{4+5j}\right)V_1 - \frac{1}{5j}V_2 = 3A 0^\circ \quad \frac{1}{5j}V_1 + \frac{3}{10j}V_2 = 5A 130^\circ$$

$$\left(\frac{4-5j}{41}\right)V_1 + \frac{5j}{25}V_2 = 3A 0^\circ \quad -0.2V_1 - 3V_2 = 5A 130^\circ$$

$$(0.0975 - 0.1219j)V_1 + 0.2V_2 = 3A 0^\circ$$

$$V_2 = \underline{3 0^\circ} - (0.0975 - 0.1219j)V_1$$

$$V_2 = 15 0^\circ - (0.9875 - 0.6095j)V_1$$

$$\Rightarrow -0.2V_1 - 3(15 0^\circ - (0.9875 - 0.6095j)V_1) = 5 130^\circ$$

$$-0.2V_1 - 45 0^\circ + (1.4625 - 1.8285j)V_1 = 5 130^\circ$$

$$(1.2625 - 1.8285j)V_1 = 5 130^\circ + 45 0^\circ$$

$$= (4.3301 + 2.5j) + (45 + 0j)$$

$$= 49.3301 + 2.5j$$

$$V_1 = \underline{\underline{49.3301 + 2.5j}}$$

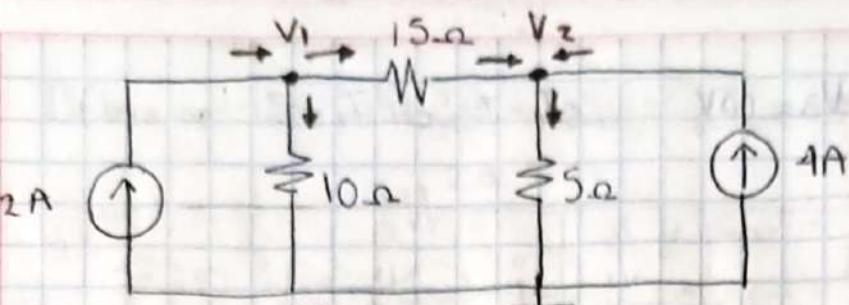
$$2.2270 - 55.3766$$

$$V_1 = 22.2292 \underline{58.2886}$$

$$V_2 = (15 + 0j) - (0.9875 - 0.6095j)(11.6845 + 18.9105j)$$

$$= (15) - (5.69 + 9.21j) - (7.12j + 11.52)$$

$$= -2.21 - 2.09j$$



$$I) \quad 2A = \frac{V_1 - V_2}{15} + \frac{1}{10}V_1$$

$$\frac{1}{6}V_1 - \frac{1}{15}V_2 = 2A$$

$$V_1 = 6(2 + \frac{1}{15}V_2)$$

$$= 12 + \frac{1}{5}V_2$$

$$II) \quad 1A = \frac{1}{15}V_1 - \frac{1}{5}V_2$$

$$\frac{1}{15}V_1 - \frac{1}{5}V_2 = 1A$$

$$\frac{1}{15}V_2 - \frac{1}{5}(12 + \frac{1}{5}V_2) = 1A$$

$$\frac{1}{15}V_2 - \frac{12}{5} - \frac{1}{25}V_2 = 1A$$

$$\frac{6}{25}V_2 = 1A$$

$$V_2 = \frac{120}{6}$$

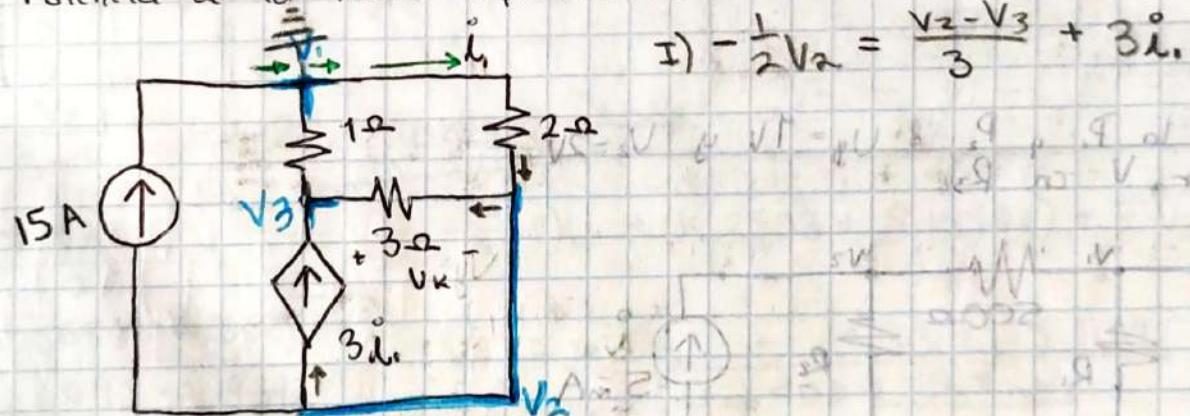
$$= 20A$$

$$V_1 = 12 + \frac{1}{5}(20)$$

$$= 12 + 4$$

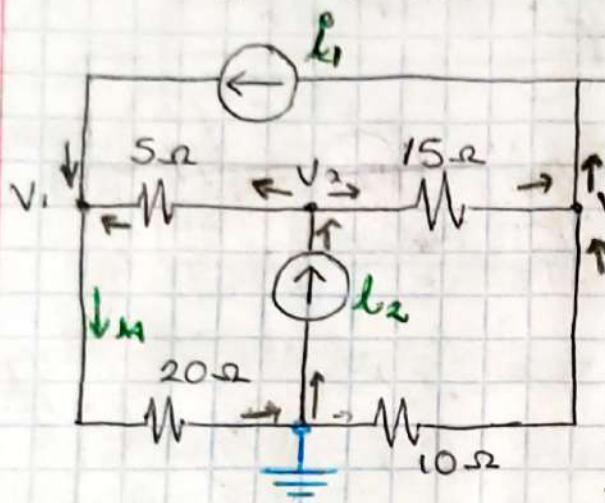
$$= 20A$$

Potencia de la fuente dependiente.



$$I) \quad -\frac{1}{2}V_2 = \frac{V_2 - V_3}{3} + 3I$$

\* Sean  $V_1 = 9V$ ,  $V_2 = 15V$ ,  $V_3 = 18V$        $I_1 = ?$  e  $I_2 = ?$



$$I) \frac{V_2 - V_1}{5} + i_1 = \frac{V_1}{20}$$

$$\frac{15 - 9}{5} + i_1 - \frac{9}{20} = 0$$

$$\underline{i_1 = 2} \quad \checkmark$$

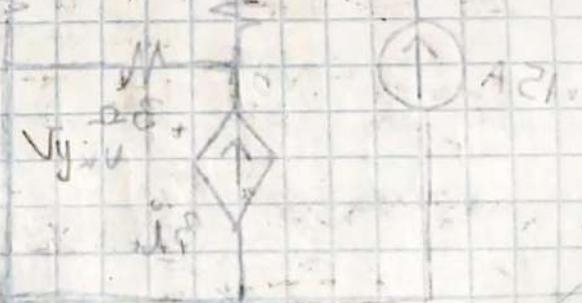
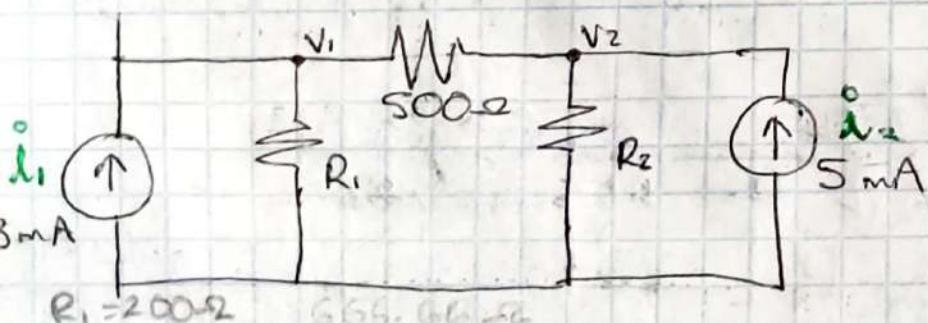
$$II) i_2 = \frac{V_2 - V_3}{15} + \frac{V_2 - V_1}{5}$$

$$= \frac{15 - 18}{15} + \frac{15 - 9}{5}$$

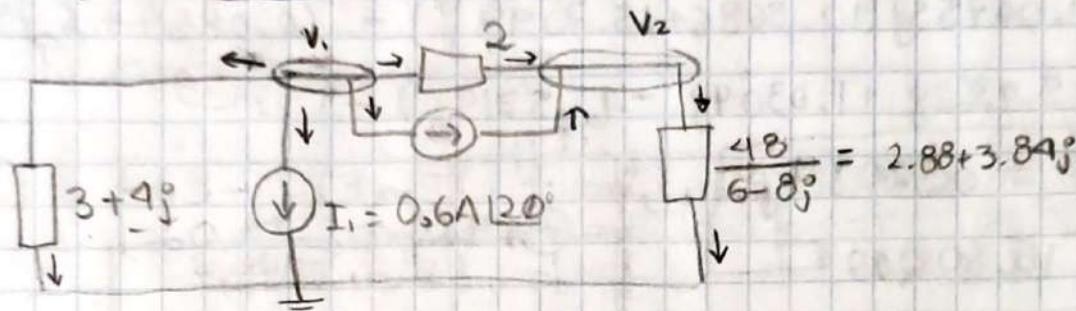
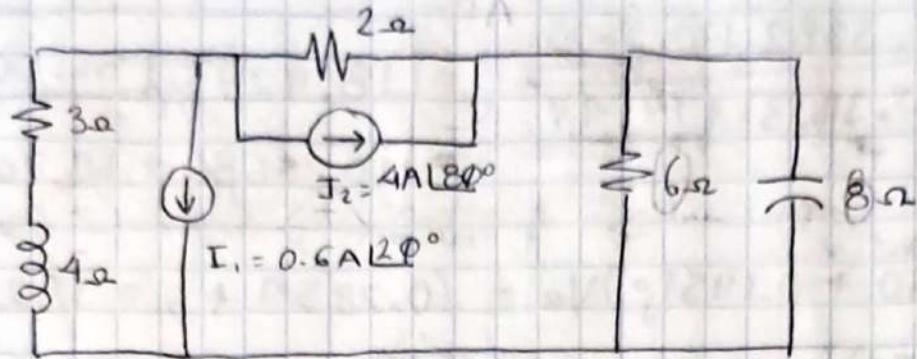
$$= -\frac{3}{15} + \frac{11}{5} = 2 \quad \checkmark$$

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Determine la  $P_1$  y  $P_2$   
Determinar  $V$  en  $R_3$        $V_1 = 1V$  y  $V_2 = 2V$



Determine los Voltajes nodales para la red.



$$\left( \frac{48}{6-8j} \right) \left( \frac{6+8j}{6+8j} \right) = \frac{288 + 384j}{36 + 64} = 2.88 + 3.84j$$

$$\frac{V_1}{3+4j} + 0.6\cancel{120} + 4A\cancel{1800} + \frac{V_1 - V_2}{2j} = 0$$

$$\frac{V_1 (3+4j)}{25} \left[ \left( \frac{31}{50} - \frac{9}{25}j \right) V_1 + (1.2583 + 4.1499j) \right] - \frac{1}{2} V_2 = 0$$

$$0.5638 + 0.2052j \quad || \quad V_1 = \frac{\frac{1}{2} V_2 - 4.3312 \cancel{[73.1109]}}{0.6403 \cancel{[-14.4702]}}$$

$$\frac{\frac{1}{2} V_2}{0.62 - 0.16j} \quad || \quad I) V_1 = (0.7560 + 0.1951)V_2 - (6.7643 \cancel{[87.5811]})$$

$$\frac{\frac{1}{2} (0.62 + 0.16)V_2}{0.41} \quad || \quad II) \frac{V_1 - V_2}{2} + 0.6\cancel{120} = 2.88 + 3.84j$$

$$\frac{1}{2} [(0.756 + 0.1951)V_2 - (0.2859 + 6.7582j)] + (0.5638 + 0.2052j) = 2.88 + 3.84j$$

$$(0.378 + 0.09755)V_2 - (0.1427 + 3.3791j) + (0.5638 + 0.2052j) = 2.88 + 3.84j$$

$$(0.378 + 0.09755j)V_2 = 2.4589 + 6.9671j$$

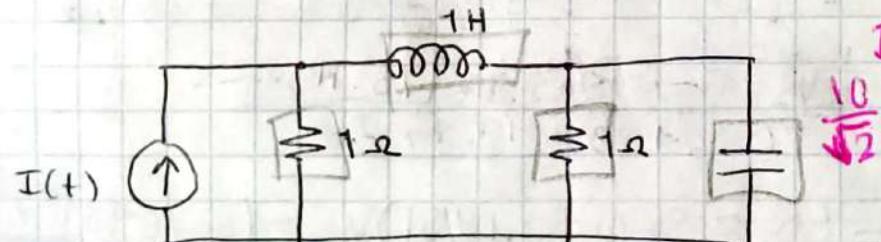
$$V_2 = \frac{7.3882 - 70.5605}{0.3903 - 14.47} = \boxed{18.9295 - 56.0605} \\ = 10.5686 + 15.7099j$$

$$V_1 = \frac{1}{2} (0.7560 + 0.1951j)V_2 - (0.2854 + 6.7582) \\ = (0.378 + 0.09755j)(10.5686 + 15.7099j) - (0.2854 + 6.7582) \\ = (3.9999 + 5.9362j + 1.0309j - 1.5319j) - \rightarrow \\ = 2.1276 + 0.2089j \\ = 2.1378 \angle 5.60$$

$$\frac{0.4455 - 5.0345j}{2.0780 + 1.7935j}$$

$$j\omega L \\ Z_L = j\omega L \\ Z_C = \frac{1}{j\omega C}$$

Calcule el voltaje en el capacitor

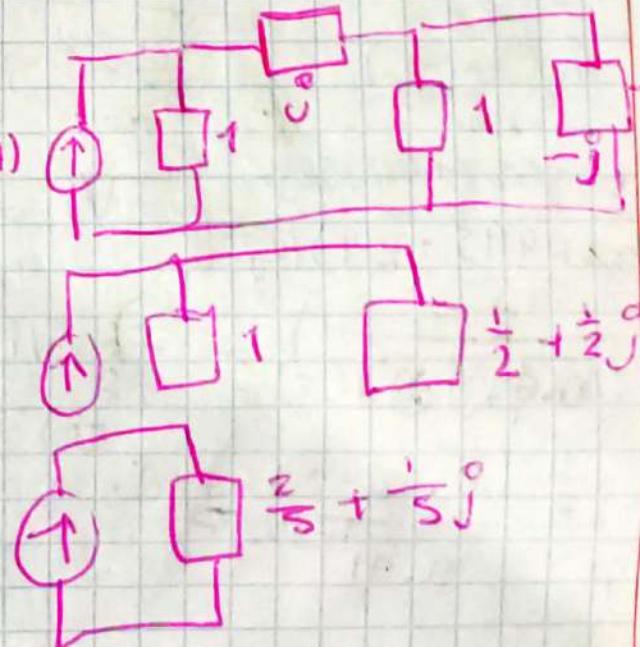


$$I(t) = 10 \text{ sent.} \\ A \text{ sen}(wt + 45^\circ)$$

$$44.71 \text{ A} \\ R = \frac{1}{\sqrt{2}}$$

$$A \text{ RLC} \\ \boxed{\frac{10}{\sqrt{2}} \angle 0^\circ}$$

$$7.07 + 0j$$



I.  $I_1 = 2A \angle 30^\circ$   
 $I_2 = 3A \angle 150^\circ$

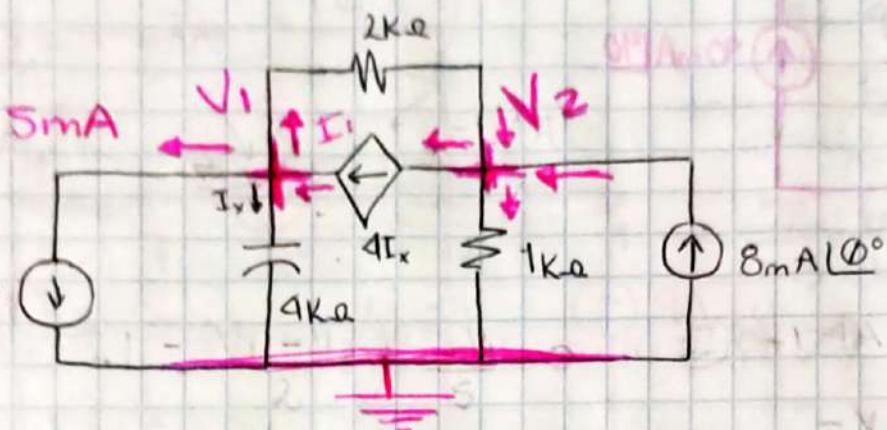
I)  $2A \angle 30^\circ = \frac{V_1}{4} + \frac{V_1 - V_2}{j}$   
 $\Rightarrow 2A \angle 30^\circ = (\frac{1}{4} - j)V_1 + jV_2$

II)  $-jV_1 + jV_2 = \frac{1}{5}V_2 + 3A \angle 150^\circ + \frac{V_2}{1}$   
 $-jV_1 + jV_2 - \frac{1}{5}V_2 - jV_2 + jV_3 = 3A \angle 150^\circ$   
 $= -jV_1 - \frac{1}{5}V_2 + jV_3 = 3A \angle 150^\circ$

III)  $\frac{V_2 - V_3}{-j} + 3A \angle 150^\circ = \frac{\sqrt{3}}{8j}$   
 $\Rightarrow jV_2 - jV_3 - \left(-\frac{8j}{64}V_3\right) = -3A \angle 150^\circ$   
 $= jV_2 - \frac{7}{8}jV_3 = -(3A \angle 150^\circ)$

$V_1$	$V_2$	$V_3$	I
$0.25 - j$ $-j - j$	$-j$ $-0.2$	$j$ $-0.75$	$1.7320 + j$ $-2.598 + 1.5j$ $-(2.59 + 1.5j)$

No 6005: Determine cl voltage on  $R = 1\text{ k}\Omega$



$$N1: 4I_x = 5\text{mA} + I_1 + I_x$$

$$4\left(\frac{1}{-j1000}\right) = 5\text{mA} + \frac{V_1 - V_2}{2000} + \frac{V_1}{-j1000}$$

$$V_1\left(\frac{1}{1000} j\right) + V_1\left(-\frac{1}{2000} + \frac{1}{-j1000}\right) + V_2\left(\frac{1}{2000}\right) = 5\text{mA}$$

$$V_1\left(-\frac{1}{2000} + \frac{3}{4000} j\right) + V_2\left(\frac{1}{2000}\right) = 5\text{mA}$$

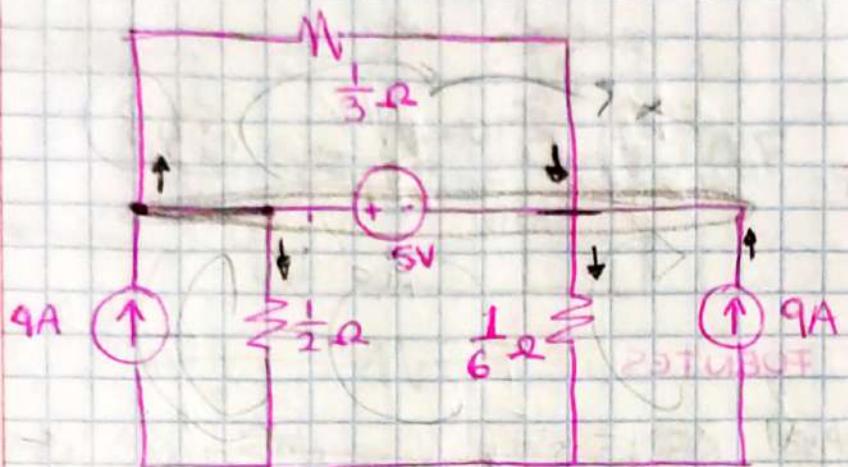
$$N2: \frac{V_1 - V_2}{2000} + 8\text{mA} = \frac{V_2}{1000} + 4I_x$$

$$V_1\left(\frac{1}{2000}\right) - V_2\left(\frac{1}{2000}\right) - V_2\left(\frac{1}{1000}\right) - 4\left(\frac{V_1}{-j1000}\right) = -8\text{mA}$$

$$-V_2\left(\frac{3}{2000}\right)$$

$$V_1\left(\frac{1}{2000} - \frac{1}{1000} j\right) - V_2\left(\frac{3}{2000}\right) = -8\text{mA}$$

Nodos. Calcula el voltaje en cada fte. de corriente



$$I) 9A + 9A + I_3 = I_2 + I_3 + I$$

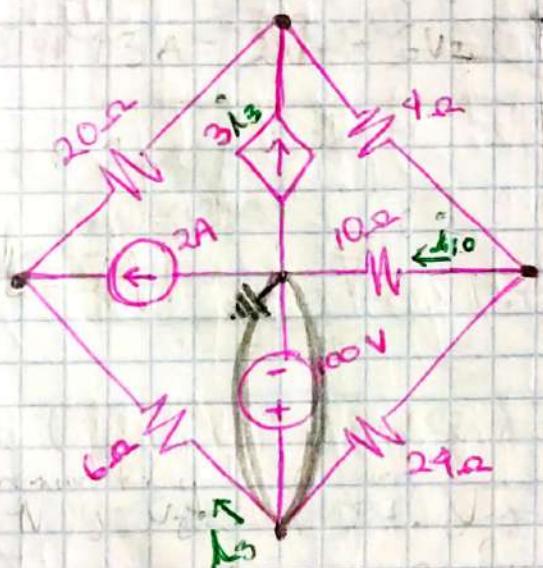
$$I_3 = V_{12} + V_2 / 1/6$$

$$I_3 = 2V_1 + 6V_2$$

$$II) V_1 - V_2 = S \\ \Rightarrow V_1 = S + V_2$$

$$en I) I_3 = 2(S + V_2) + 6V_2$$

$$I_3 = 10 + 2V_2 + 6V_2 \\ 3 = 8V_2$$

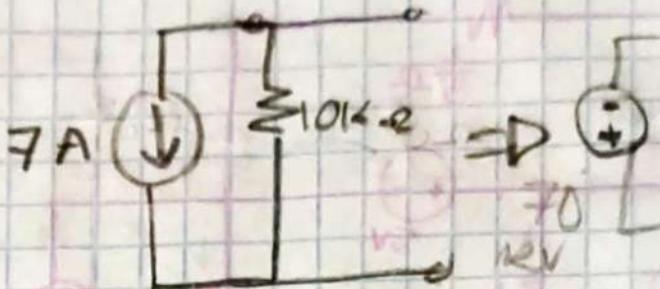
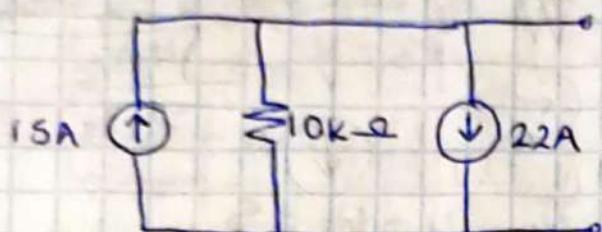


NOTACION

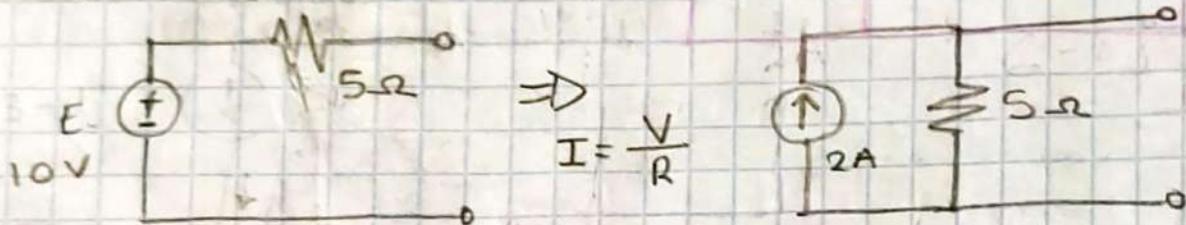
$$= 5.3$$

Tensiones

Convertir una sola fuente de voltaje independiente en serie con resistencia

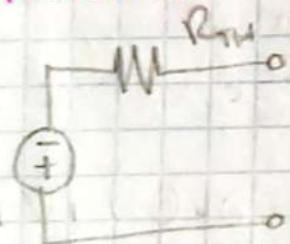


## \* TRANSFORMACIONES DE FUENTES.



$$V = IR$$

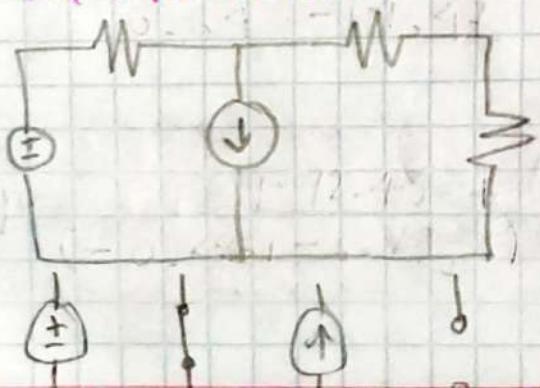
### THEVENIN



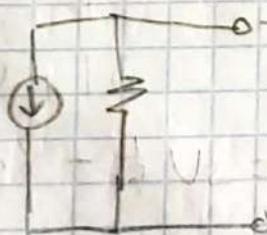
$$V_{TH} = I_{SC} R_{TH}$$

$$V_{TH} = R_{TH}$$

Superposición



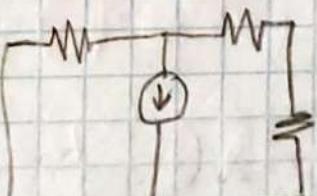
### NORTON



$$I_{SC} = \frac{V_{TH}}{R_{TH}}$$

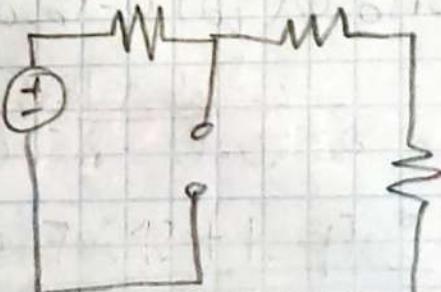
$$V = IR$$

$\Rightarrow$  Caso 1



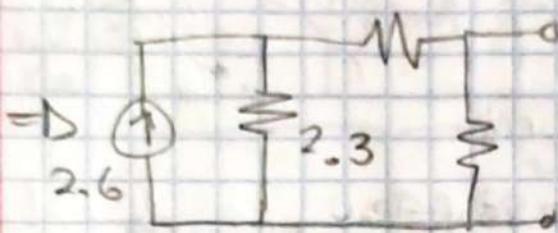
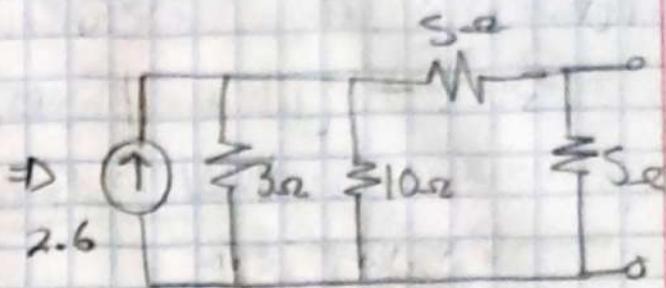
$$V_{R2.1}$$

Caso 2

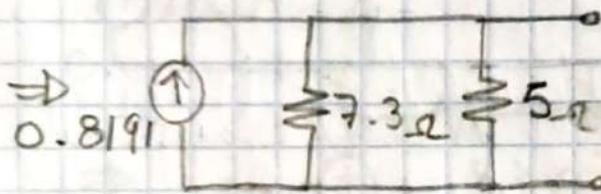
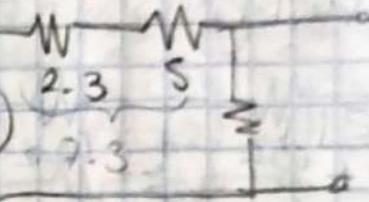


$$\rightarrow V_{R2.2} = V_{R2.1} + V_{R2.2}$$

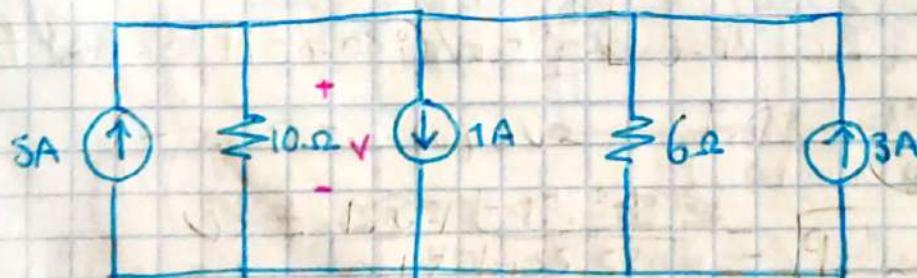
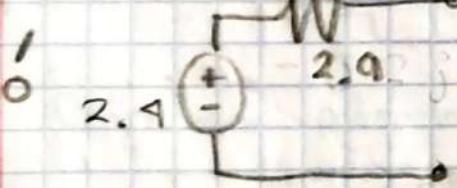
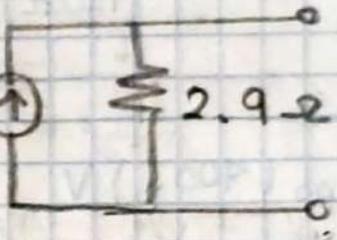
Convertir en una sola fuente de corriente independiente en paralelo con una resistencia



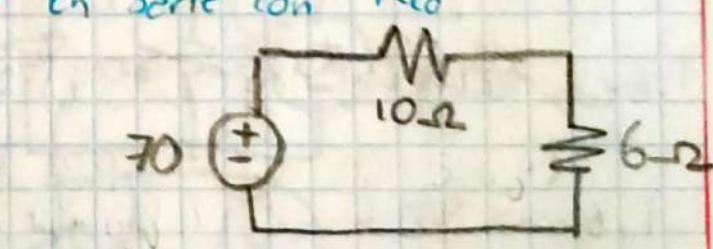
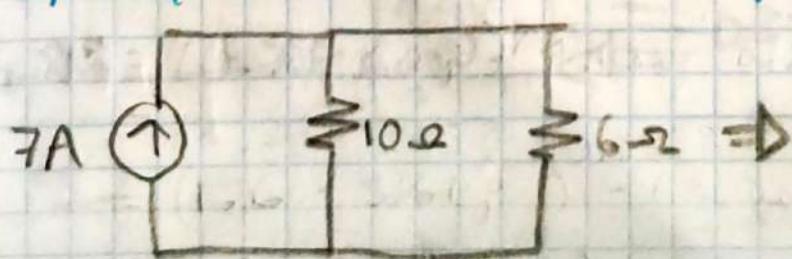
$$\Rightarrow 5.98V$$



$$\Rightarrow 0.8191$$



a) Simplificar a una fuente de voltaje en serie con  $R_{th}$



b) Calcular  $V$   
 c) ¿Por qué  $R_0$  no se debe considerar?

$$2.25V$$

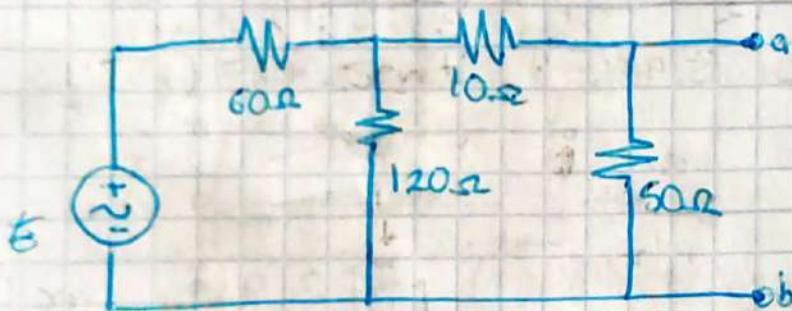
R

$$42V$$

$$6\Omega \text{ Var}$$

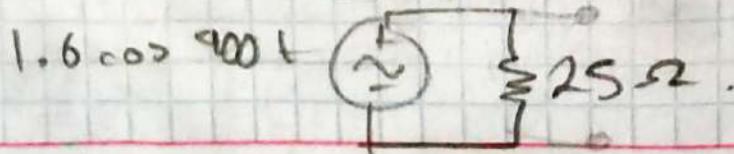
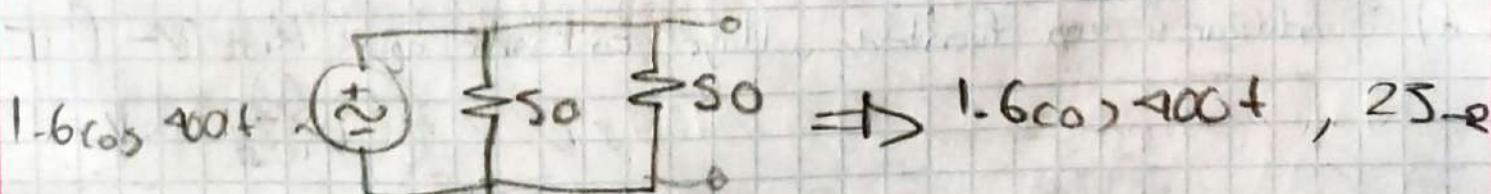
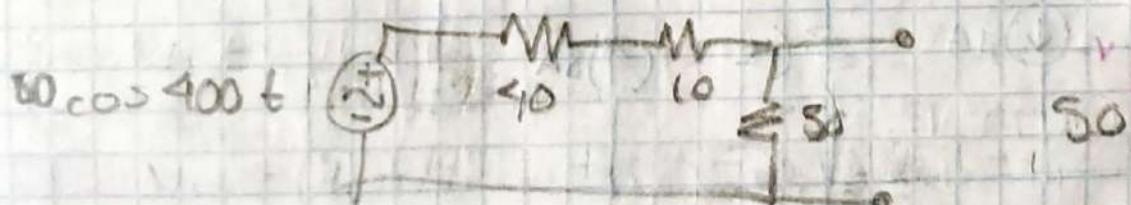
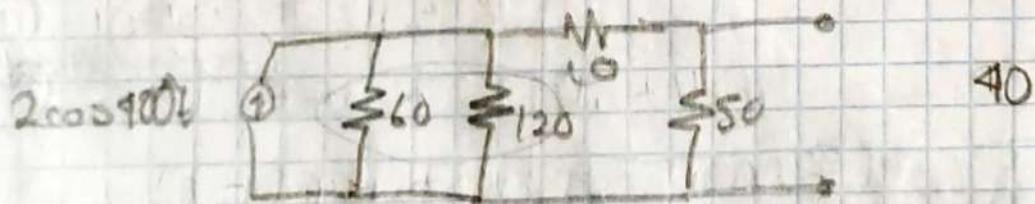
Nor

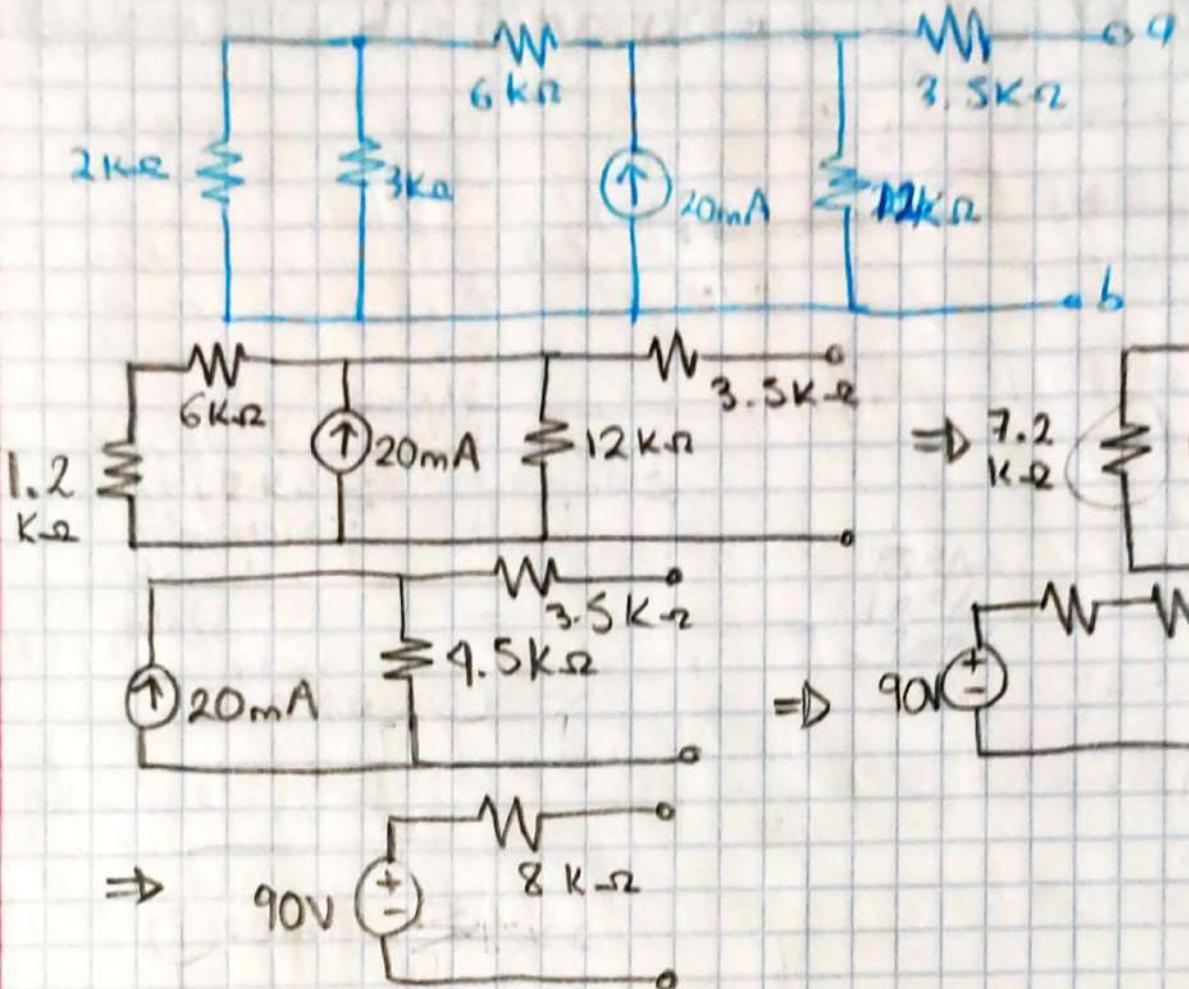
1F



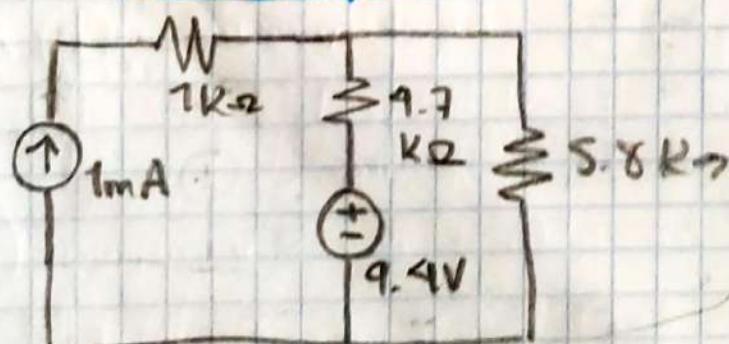
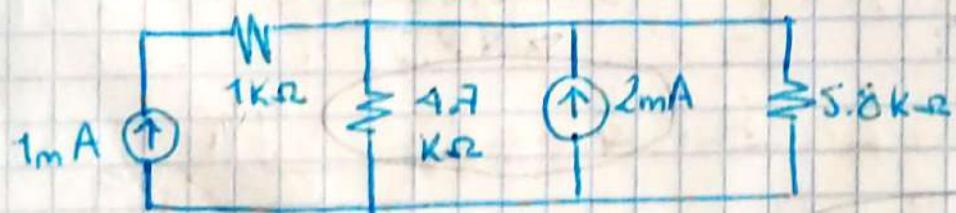
$$E = 120 \cos(900t) V$$

Simplificar ala izquierda de los puntos a y b.



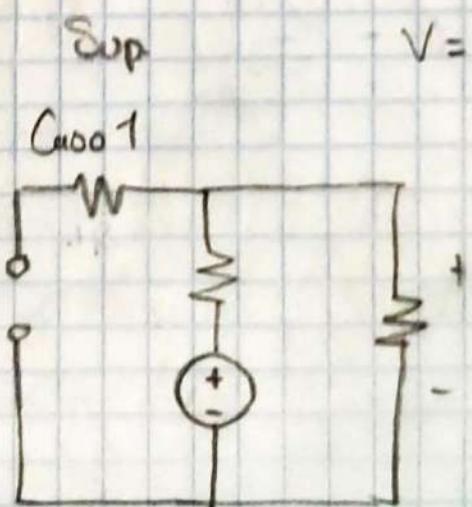


Determinar potencia disipada en  $R_{S,8}$  1kΩ

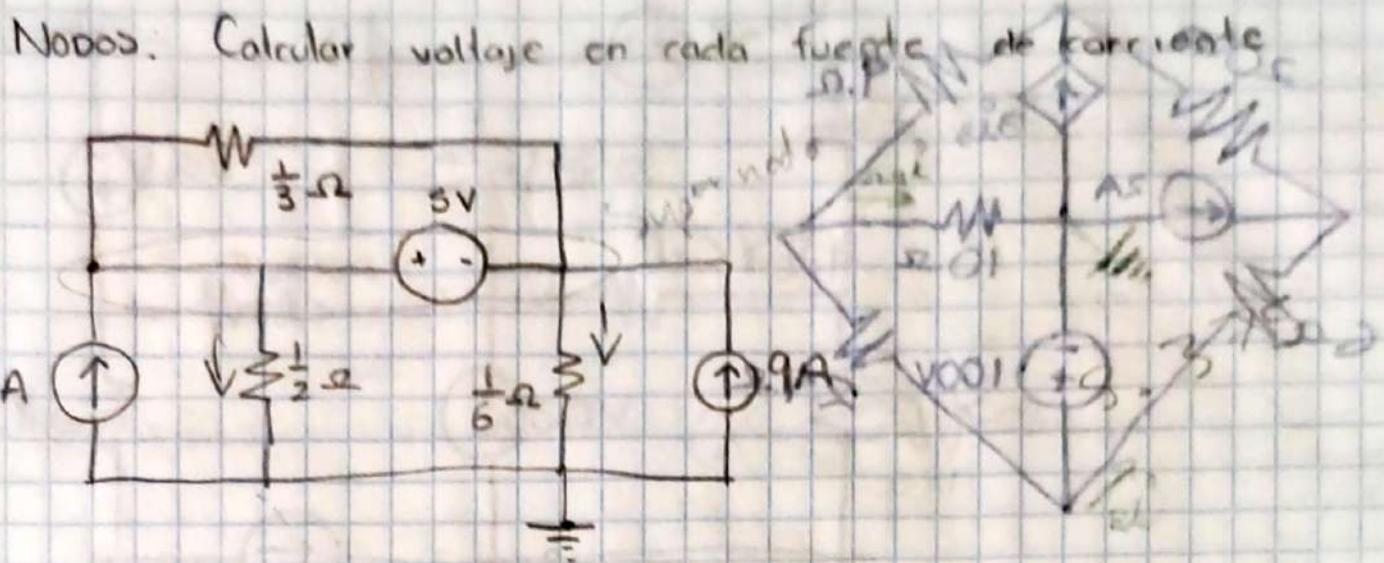


S.7 +

1.6k S.7 s2



95640



Supernodo (todas las corrientes que entran)

$$9A + 9A + I_3^+ = I_2^- + \frac{I_1}{6} + I_3^-$$

$$9A + 9A = 2\cancel{V_1} + 6V_2$$

$$V = 8T$$

$$T = \frac{V}{8}$$

$$V_1 - V_2 = 5 \rightarrow D$$

$$I_3 = 2V_1 + 6V_2$$

$$V_1 = 5 + V_2 \rightarrow V_1 = 5.375$$

$$I_3 = 10 + 2V_1 + 6V_2$$

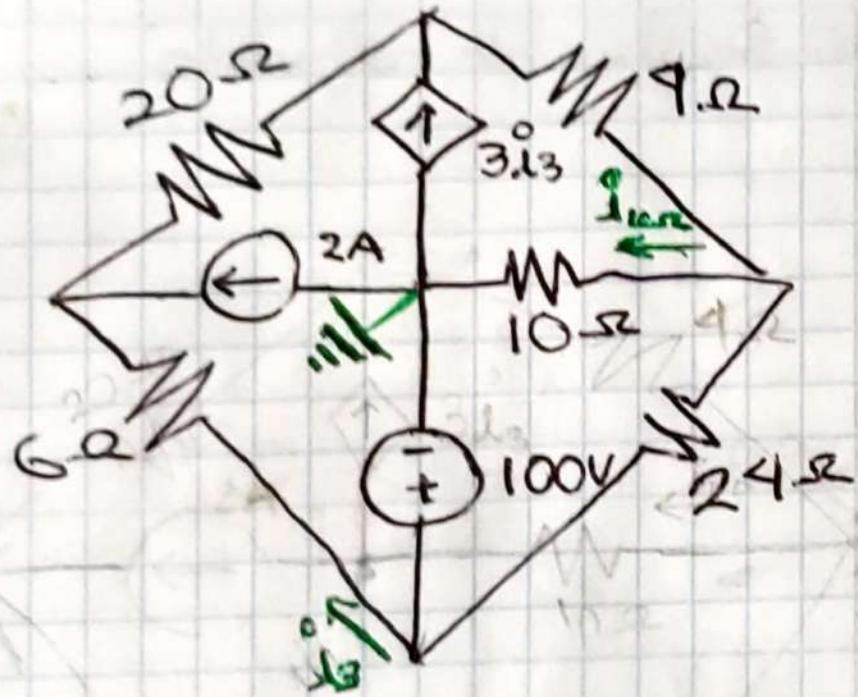
$$I_3 = 8V_2$$

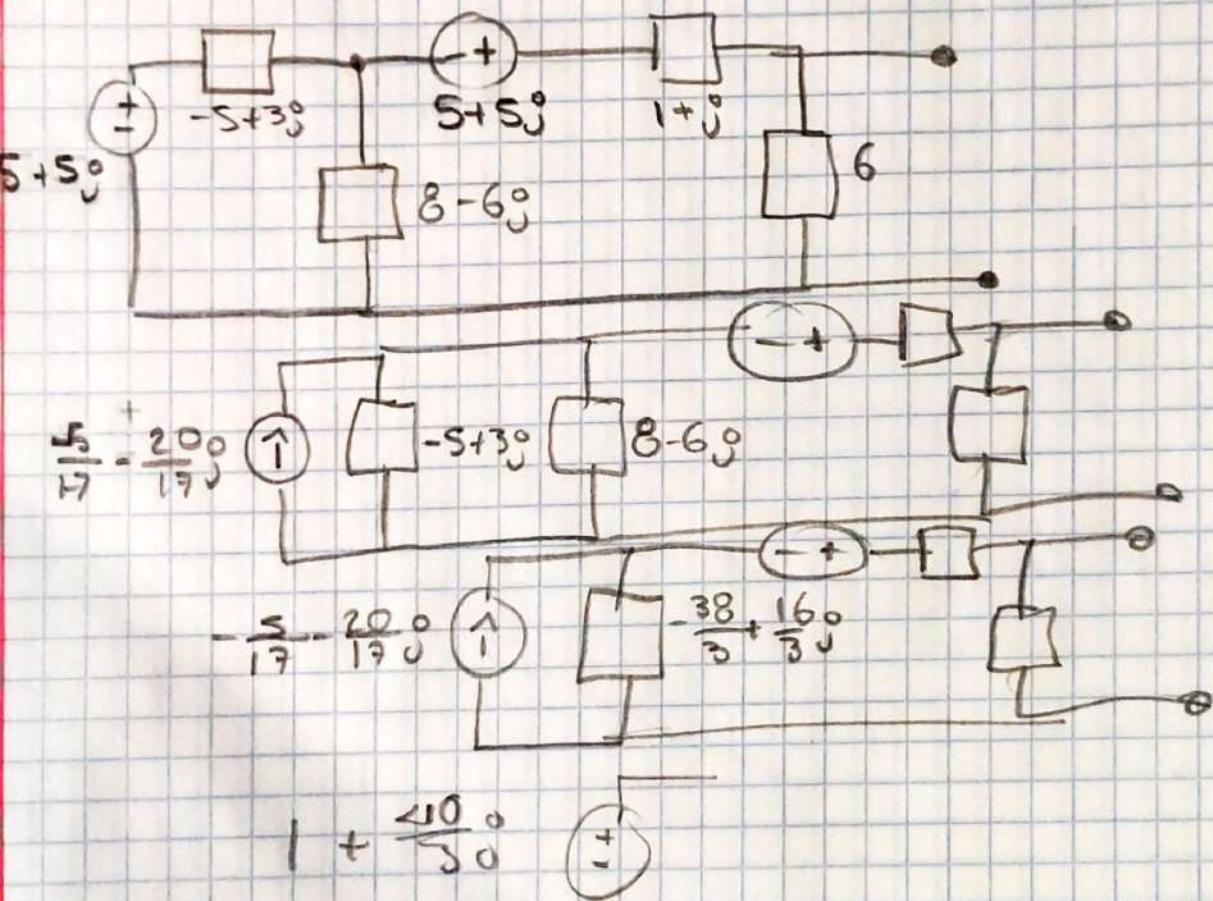
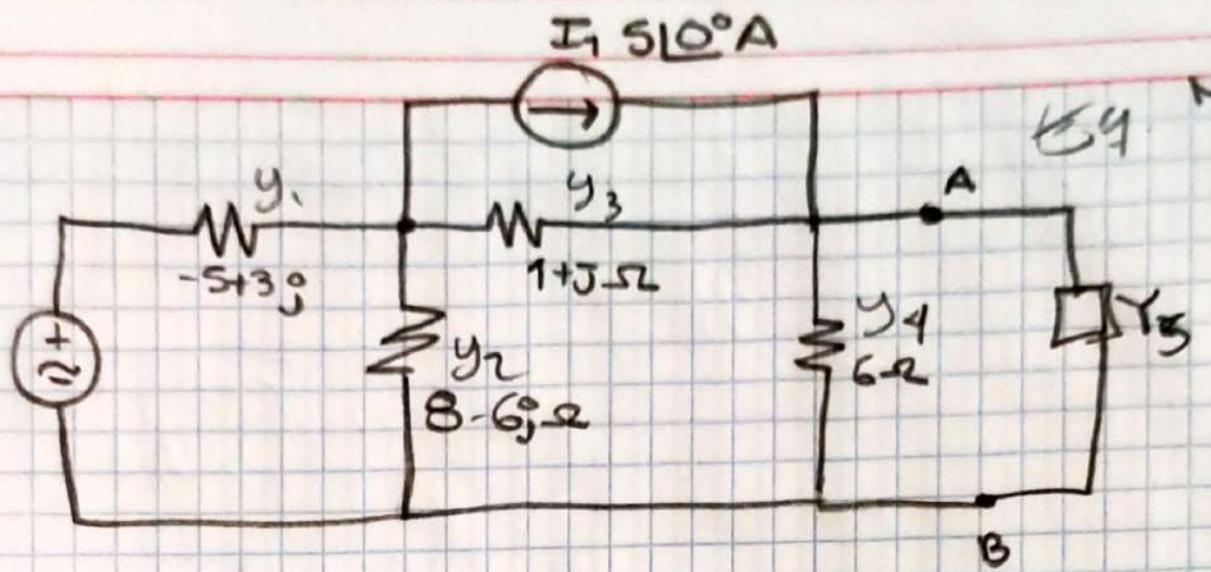
$$V_2 = 0.375$$

N<sub>1</sub> 9927  
V<sub>2</sub> 46.93

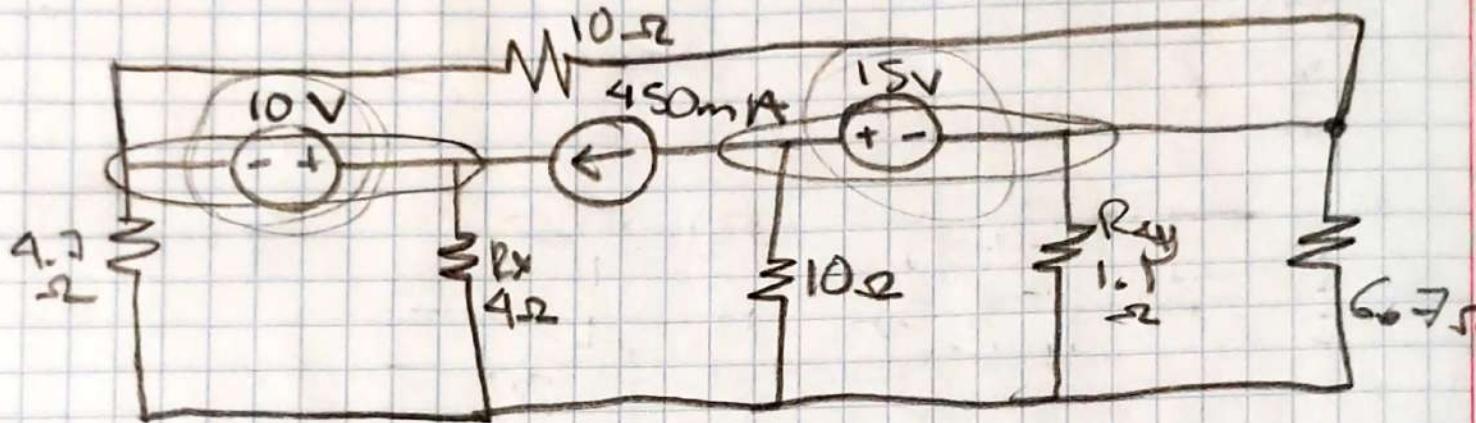
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358004/04/003<99/8 ~



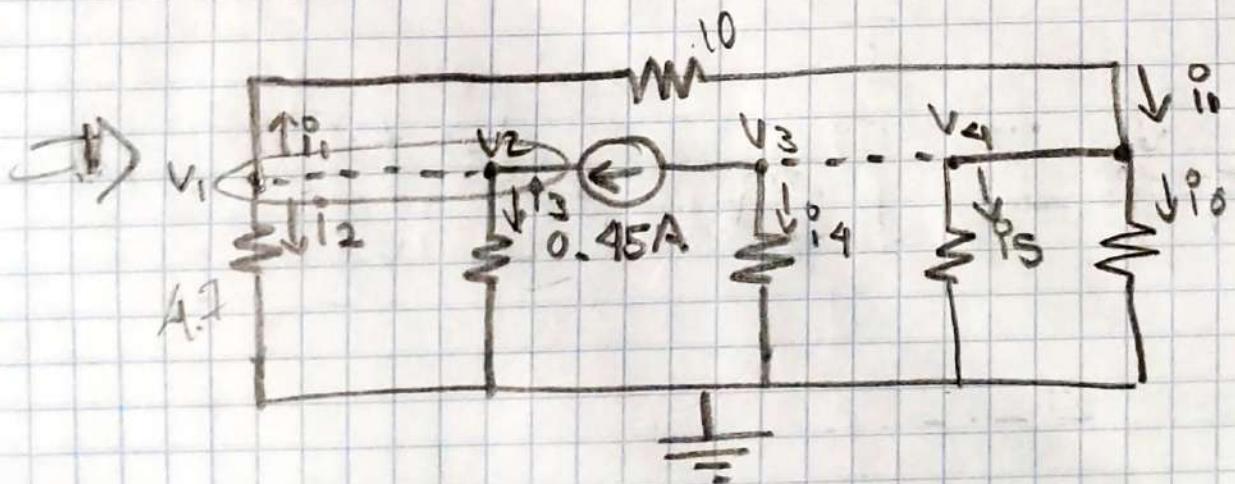


- a)  $I_{en R_y}$   
 b) Pdtt en  $R_x$   
 c)  $V$  en la ff. de  $\square$



ANALISIS DE NODOS

A SUPERNODOS (FTEs DE VOLT. IND O DEP EN MEDIO DE DOS NODOS)



LCK:

$$i_2 + i_1 + i_3 = 0.45A$$

$$\frac{v_1 - v_4}{10} + \frac{v_1}{4.7} + \frac{v_2}{4} = 0.45A \quad \text{--- (1)}$$

$$V_1 = -3.30 \text{ V}$$

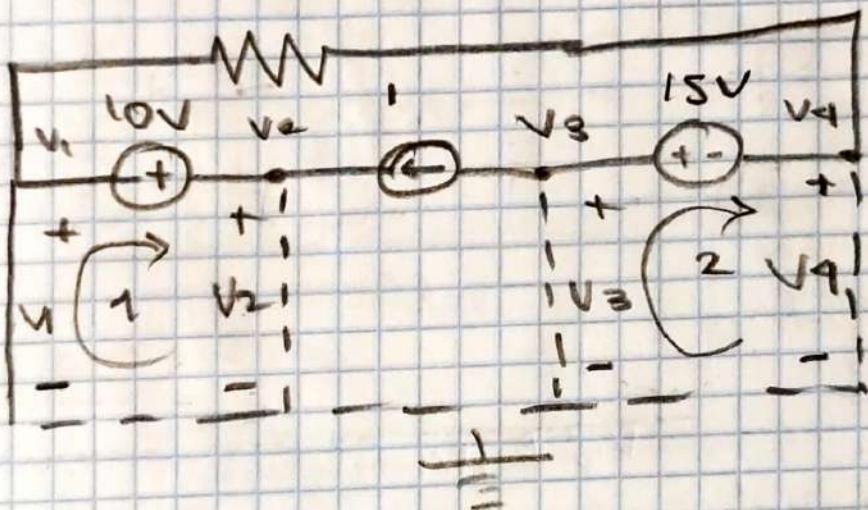
$$V_2 = 6.67 \text{ V} \quad V_3 = 13.53$$

$$V_4 = -1.47 \text{ V}$$

$$i_1 + i_{st} + i_6 + 0.75 \text{ A} = 0,$$

$$\frac{V_2}{10} + \frac{V_4}{1.1} + \frac{V_1}{0.7} + 0.75 = \frac{V_4 - V_1}{10} \quad \rightarrow ②$$

LVRK

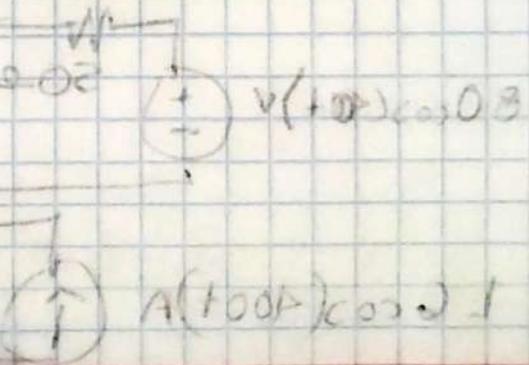
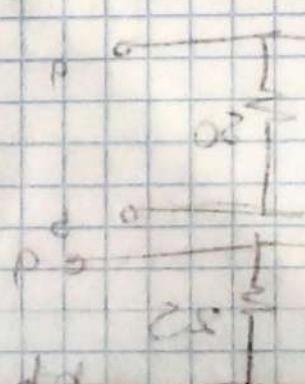
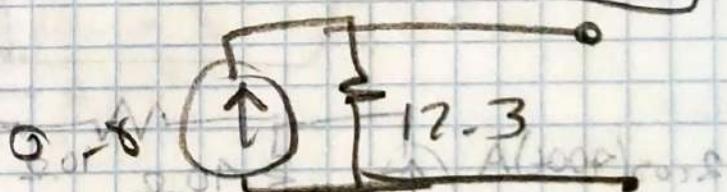
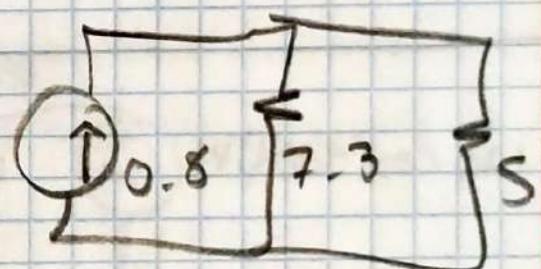
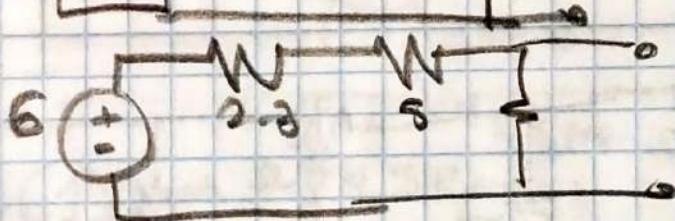
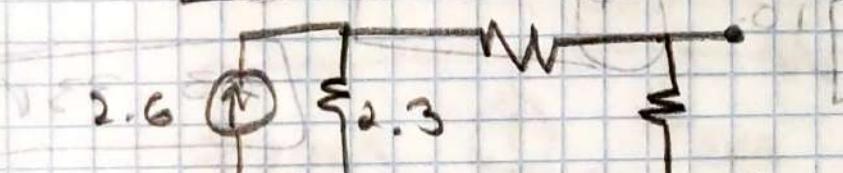
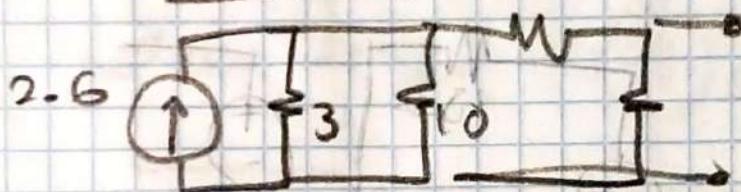
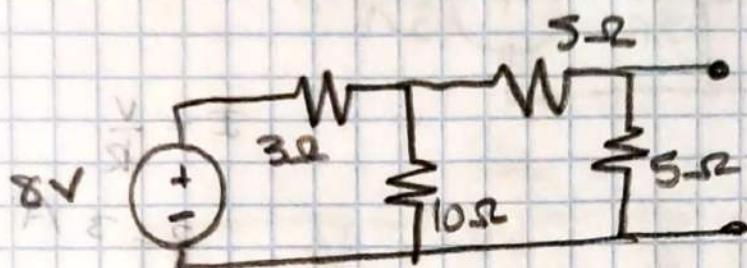
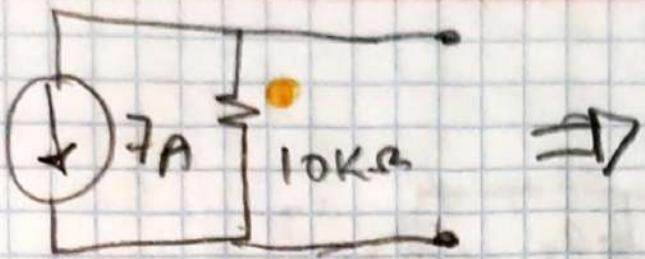


$$-V_1 - 10\text{V} + V_2 = 0$$
$$V_2 - V_1 = 10 \quad \textcircled{3}$$

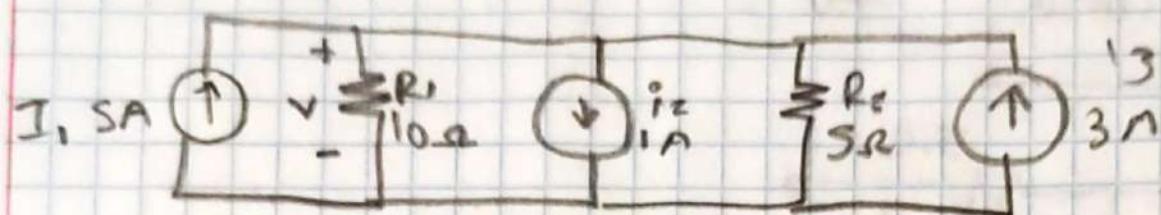
$$-V_3 + 15\text{V} + V_4 = 0$$

$$V_4 - V_3 = -15 \quad \textcircled{4}$$

$$I_{Ry} = -1.34 \text{ A}$$

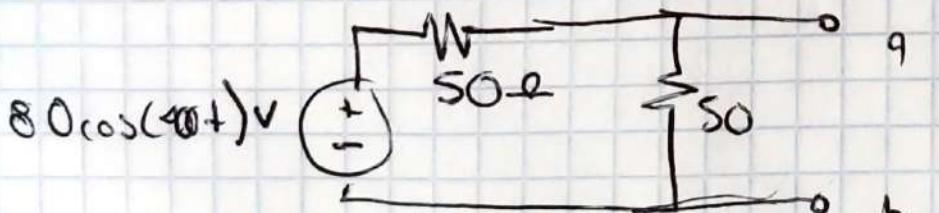
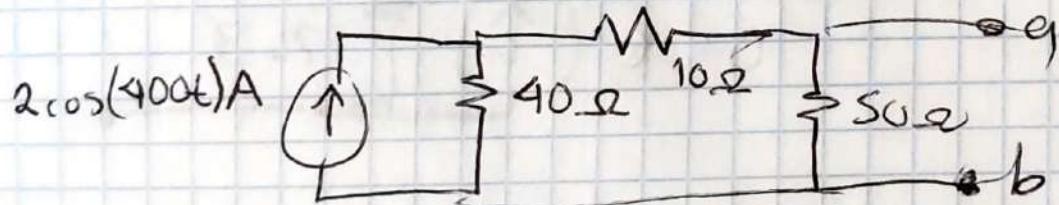
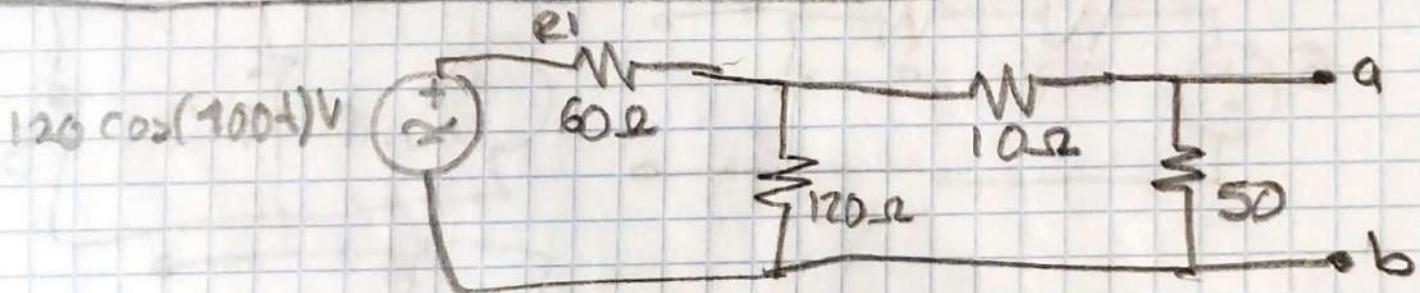
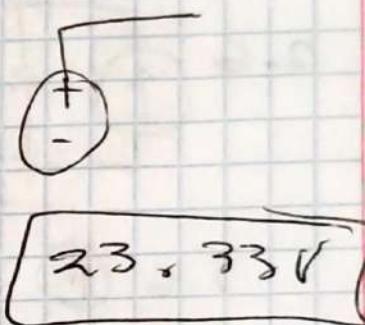
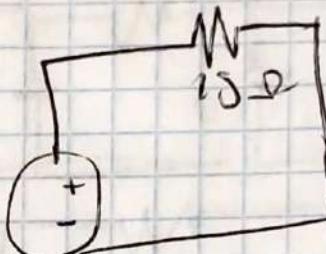
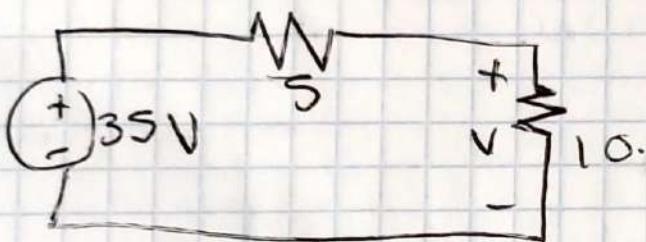
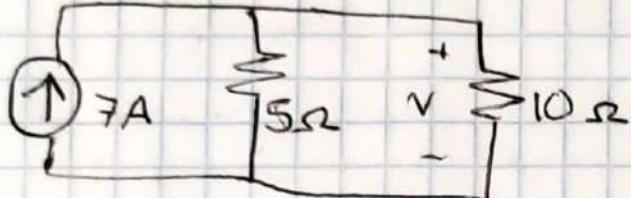


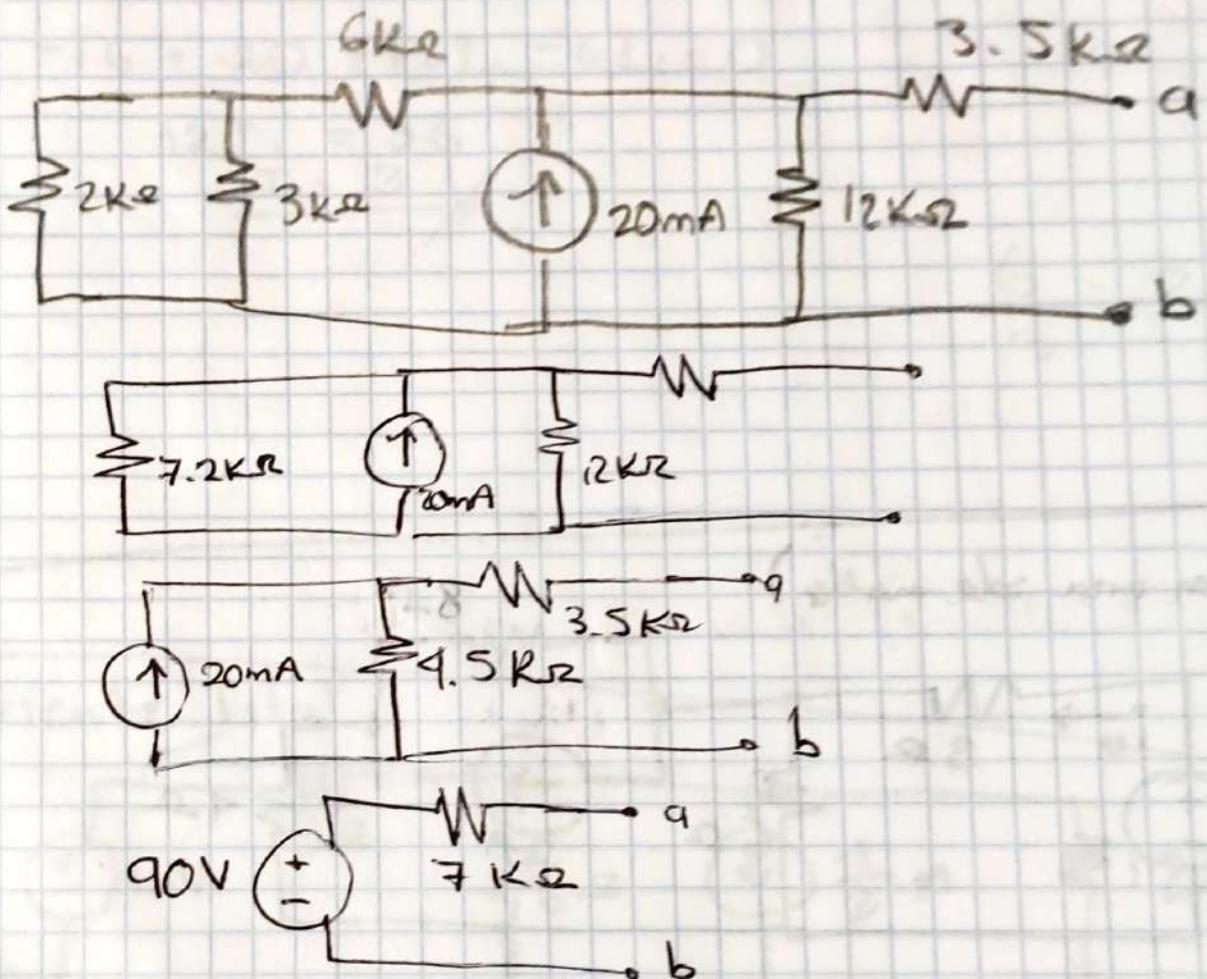
a) V en serie con R1  
b) Calcular V



$$I = \frac{V}{R}$$

$$2 - 3 \text{ A}$$

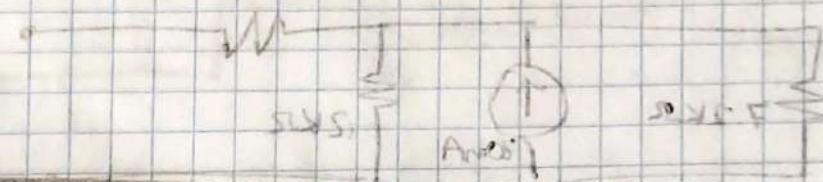
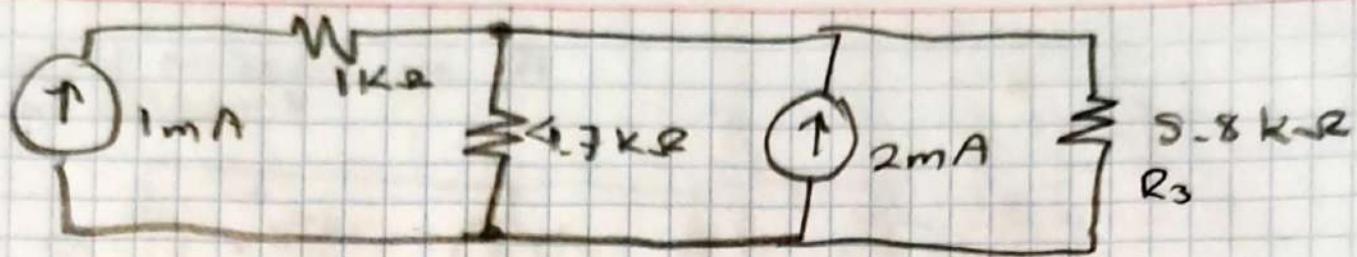




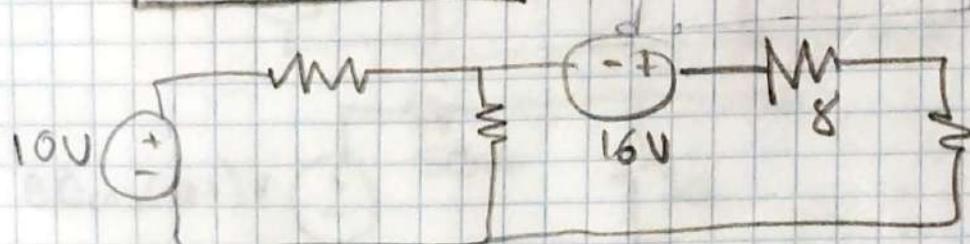
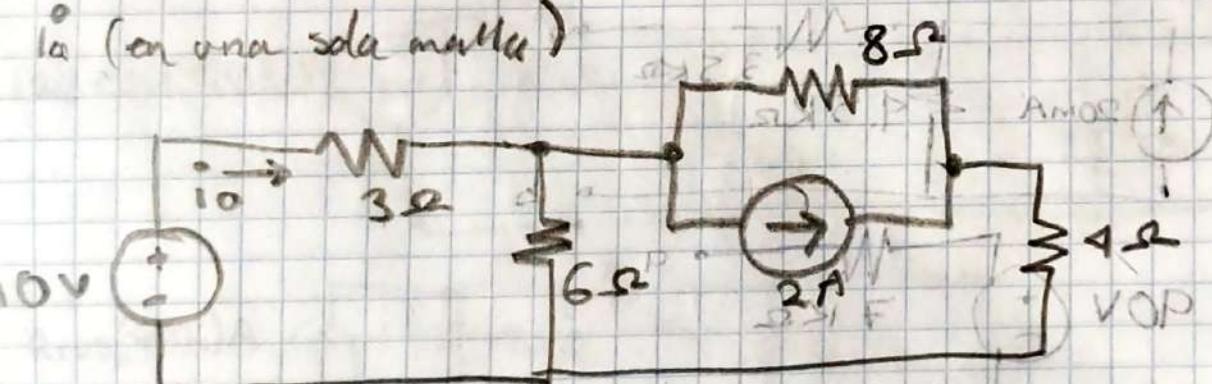
$$V = RI$$

$$V_{TH}$$

Pot. en  $R_3$



$I_a$  (en una sola malla)



$$-10 + 9I_1 - 6I_2 = 0 \rightarrow ①$$

$$-16 + 12I_2 - 8I_1 = 0 \rightarrow ②$$

$$6I_2 = -10 + 9I_1$$

$$6I_2 = \frac{-10 + 9I_1}{6}$$

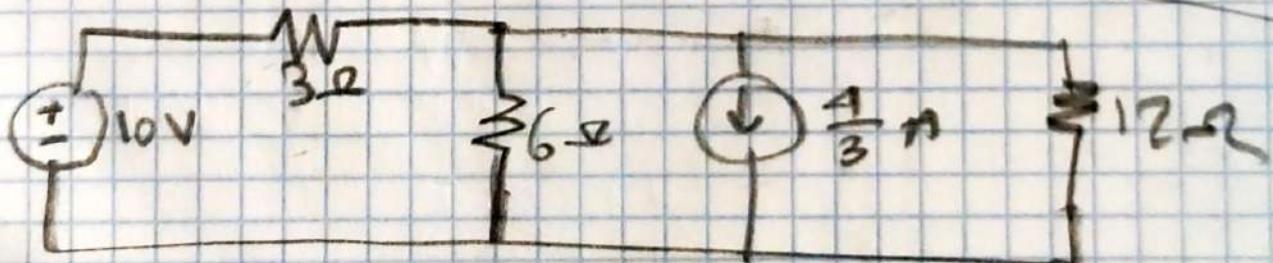
$$-16 + 12\left(\frac{-10 + 9I_1}{6}\right) - 6I_1 = 0$$

$$-16 + -20 + 18I_1 - 6I_1 = 0$$

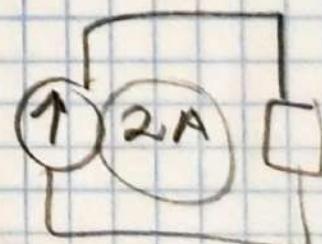
$$\begin{aligned} 12I_1 &= 36 \\ I_1 &= 3 \end{aligned}$$

$$\frac{6}{3} = 2$$

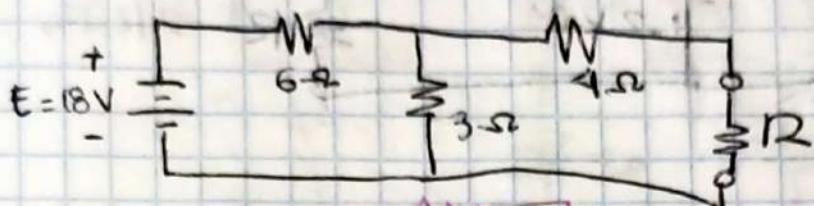
Corriente Total



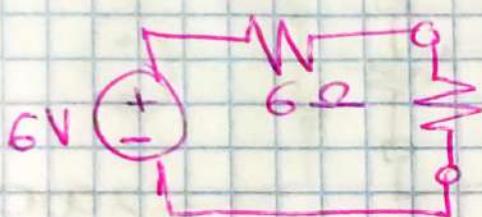
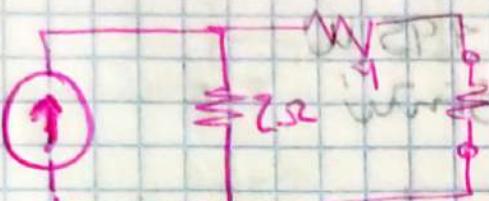
RI



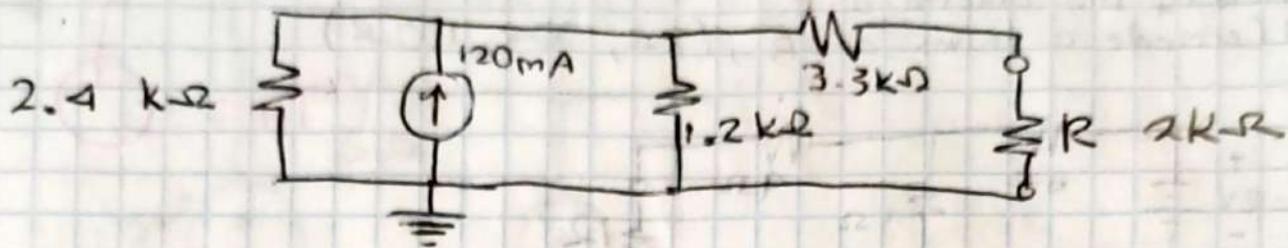
- a) (to csp TH. externa a R.  
 b) Corriente a través de  $R$ , ( $2\Omega$ ,  $3\Omega$ ,  $100\Omega$ )



$$T_H = \text{?}$$



$T_H$ , P en R cuando  $R = 2k\Omega$  y  $100k\Omega$ .

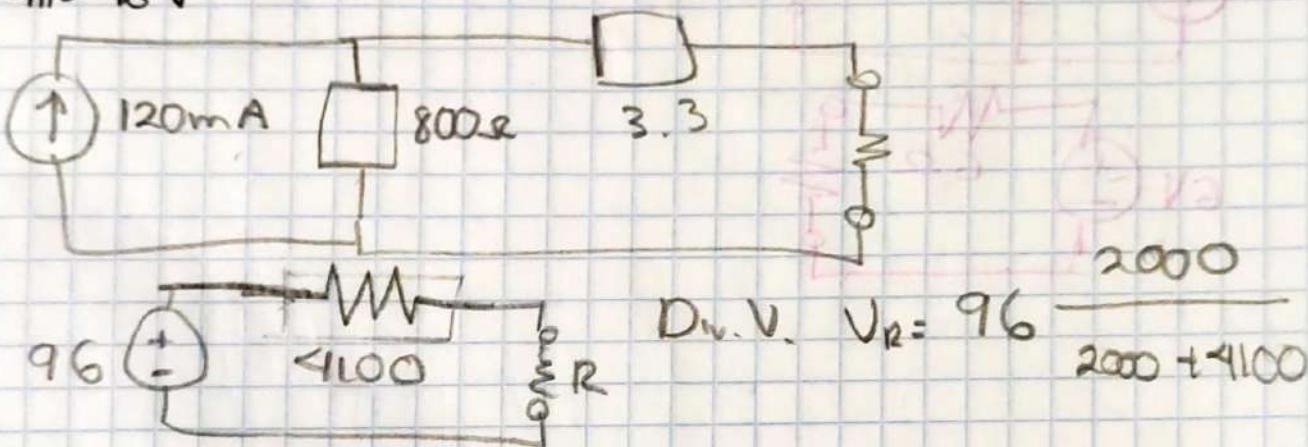


a)  $R_{TH} = 4.1 k\Omega$

$E_{TH} = 96 V$

b)  $2k\Omega \rightarrow 0.495 W$

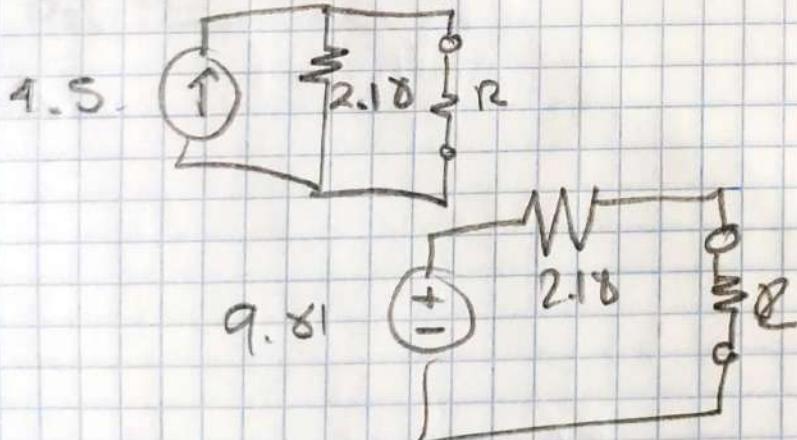
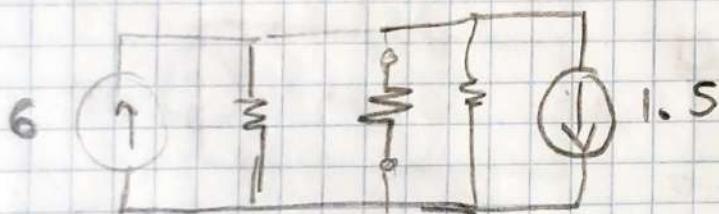
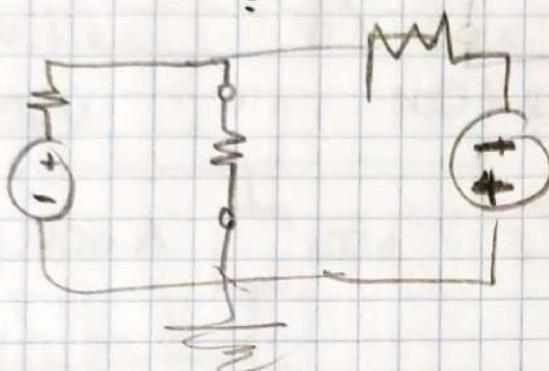
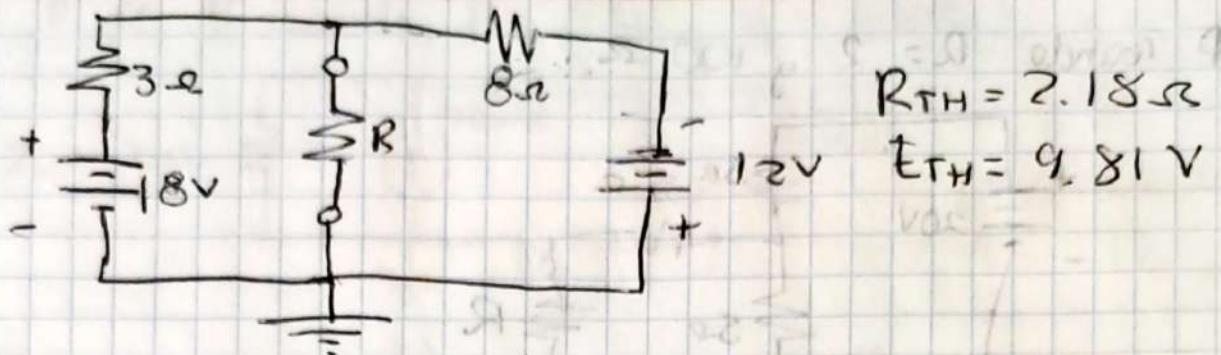
$100k\Omega \rightarrow 85mW$



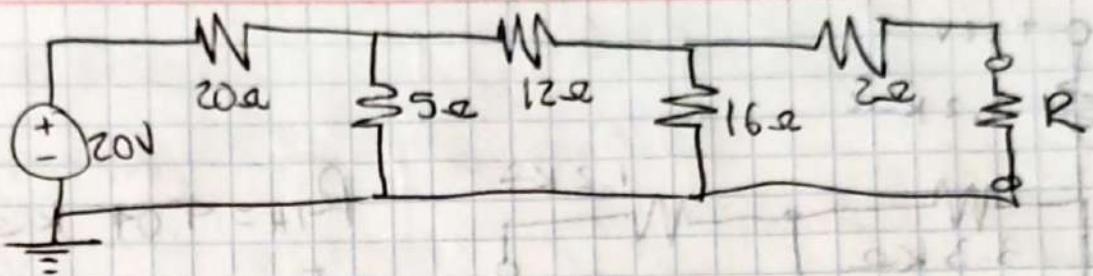
$P = U^2 =$

$V_R = 31.97$

$I = V_R$

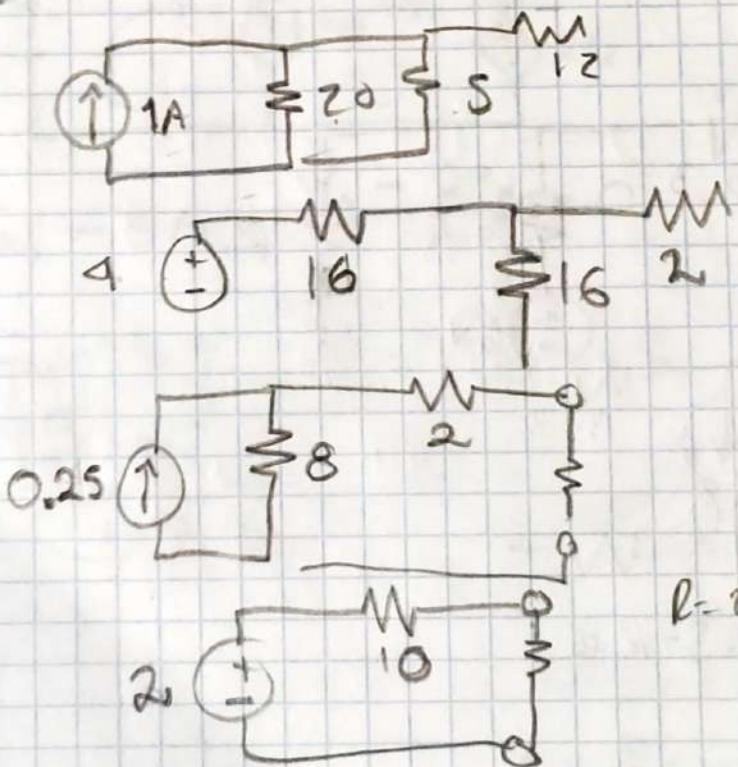


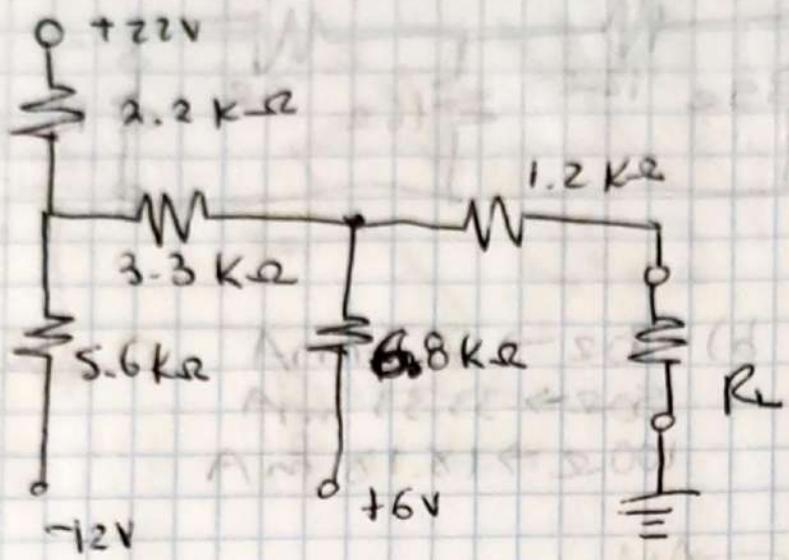
b)  $I$  si  $R = (20, 50, 100)$



a)  $R_{TH} = 10\Omega$   
 $E_{TH} = 2V$

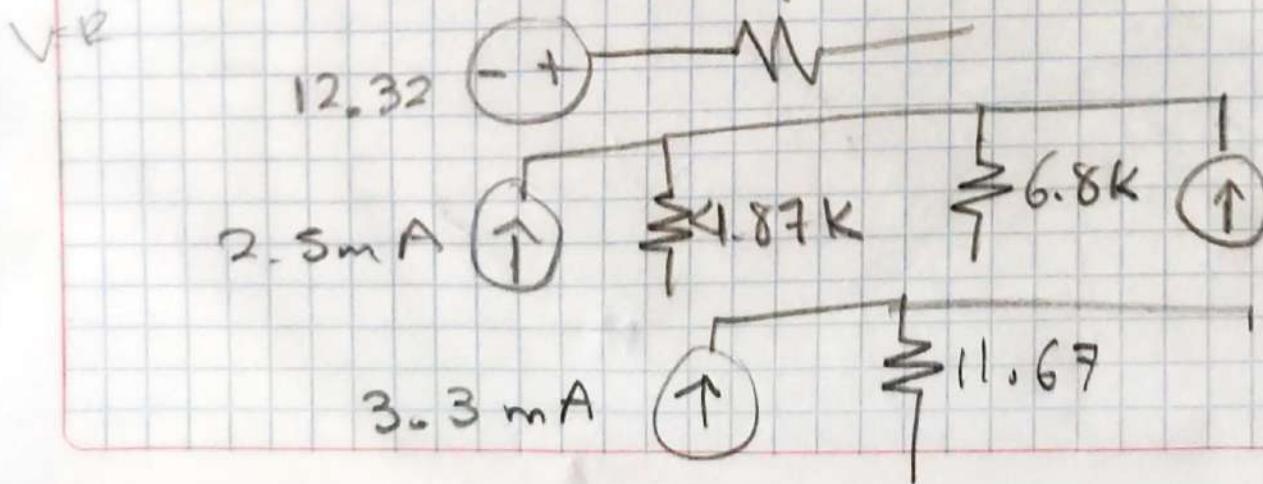
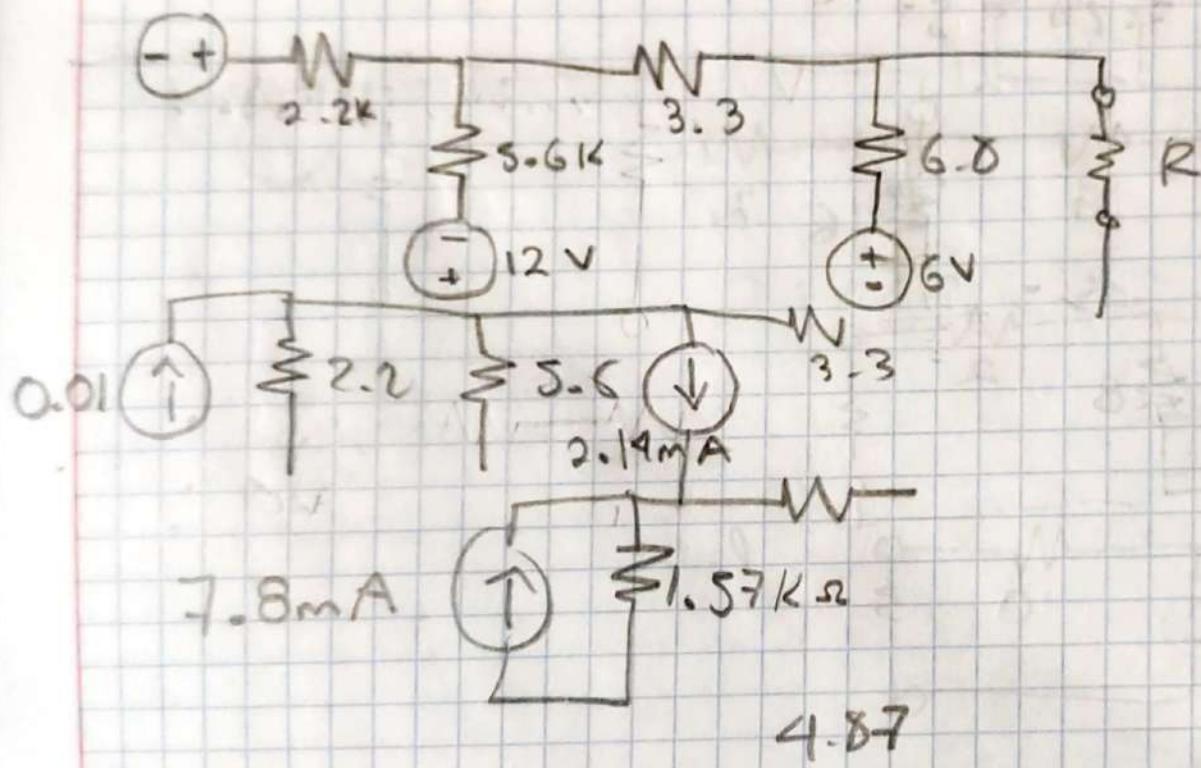
b)  $20\Omega \rightarrow 66.67mA = 0.06A$   
 $50\Omega \rightarrow 33.33mA$   
 $100\Omega \rightarrow 18.18mA$



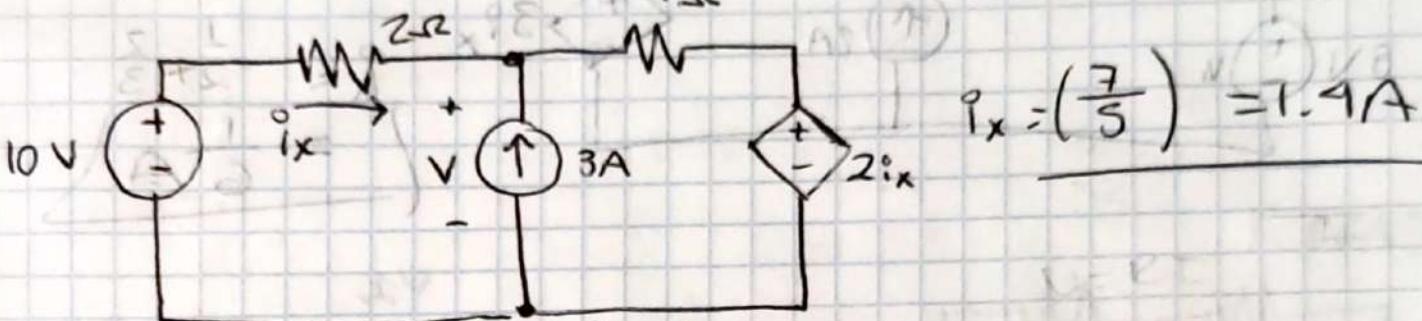


$$R_{TH} = 9.04 \text{ k}\Omega$$

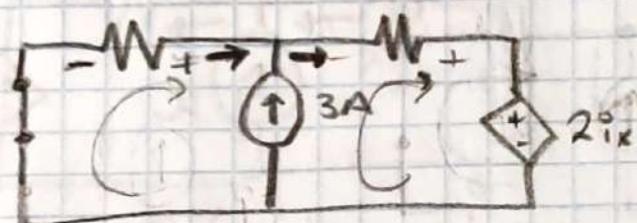
$$E_{TH} = 9.71 \text{ V}$$



Superposición.



$$i_x = \left(\frac{7}{5}\right) = 1.4A$$



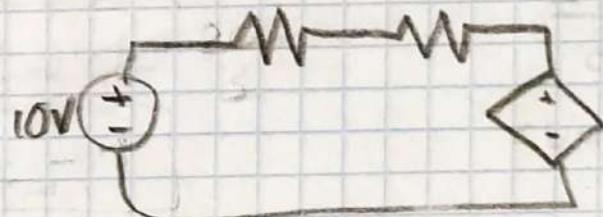
$$i_x = -\frac{V_1}{2} \Rightarrow V_1 = -2i_x$$

$$-i_{x1} + 3A + \frac{V_1 - 2i_x}{1\Omega} = 0$$

$$-i_{x1} - 3 + -2i_x - 2i_x = 0$$

$$-5i_x = 3$$

$$i_x = -\frac{3}{5}$$

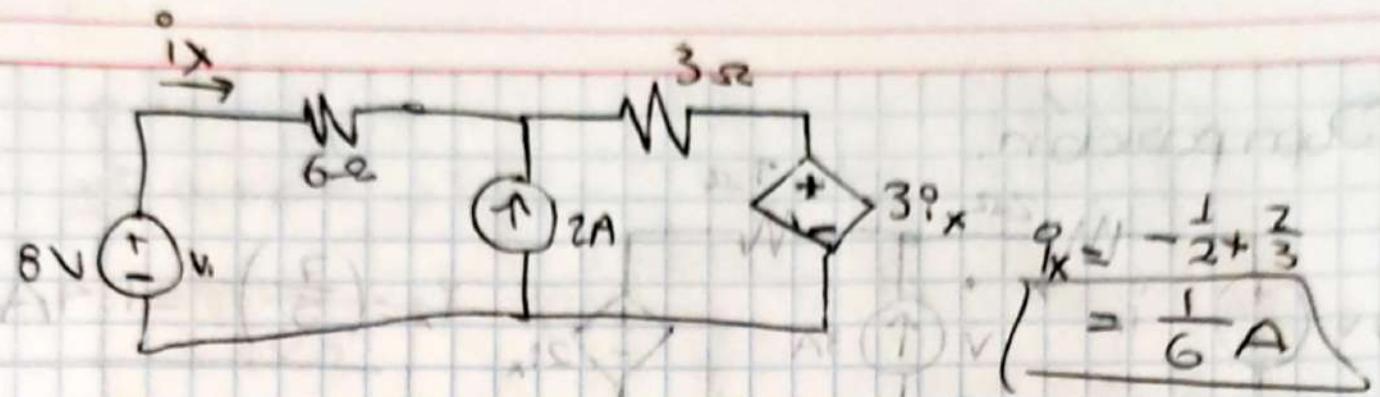


$$-10V + 3i_{x2} + 2i_{x2} = 0$$

$$5i_x = \frac{10}{3} = 2$$

$$\frac{7}{5}$$

$$11$$



Caso 1

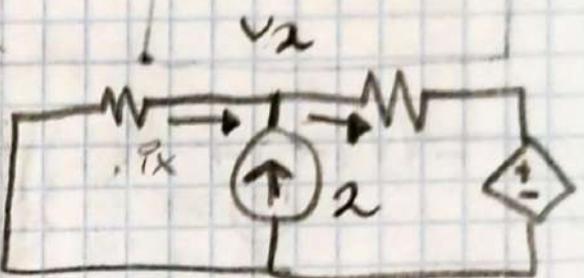


$$-8 + 9^{\circ}i_x + 3^{\circ}i_x = 0$$

$$i_x = \frac{8}{12} = \frac{2}{3}$$

$$x = -\frac{\sqrt{2}}{6}$$

$$6^{\circ}i_x = 10\sqrt{2}$$



$$-i_x - 2 + \frac{v_2 - 3^{\circ}i_x}{3}$$

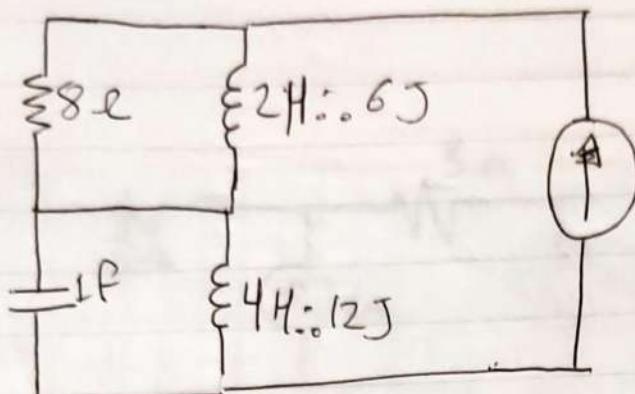
$$-\frac{v_2}{6} = i_x$$

$$+6i_x = v_2$$

$$\Rightarrow -i_x - 2 + \left( -\frac{6i_x}{3} - \frac{3^{\circ}i_x}{3} \right) = 0$$

$$-i_x - 2 - 3^{\circ}i_x = 0$$

$$-9^{\circ}i_x = 2$$



$$4 \cos(3t + 15^\circ) \text{ A}$$

$$I = 4 \angle 15^\circ$$

$$\omega = 3$$

$$\omega = 2\pi f$$

$$F = \frac{\omega}{2\pi}$$

Lo ponemos en

$$Z_{12} = \frac{(8)(6j)}{(8+6j)(8+6j)} = \frac{48j(8+6j)}{64+36}$$

$$= \frac{48j(8+6j)}{100} = \frac{384j}{100} + \frac{288}{10}$$

$$= 3.84j + 2.88$$

$$Z_{23} = \frac{(-3j)(12j)}{(-3j) + (12j)} = \frac{(-\frac{1}{3}j)(12j)}{\frac{35}{3}j}$$

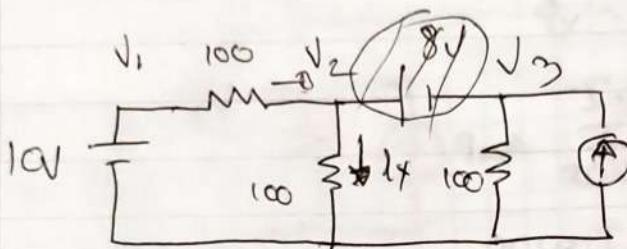
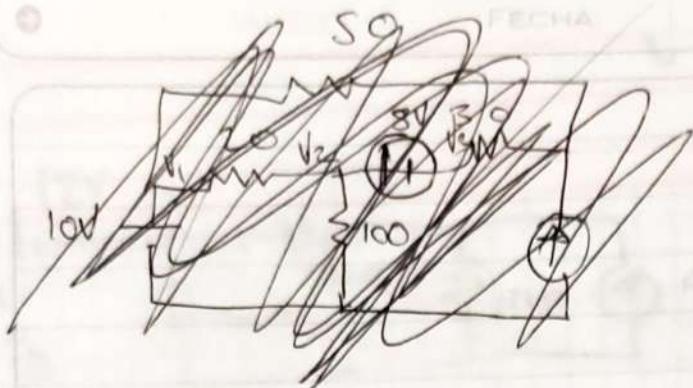
$$= \frac{(-\frac{1}{3}j)(12j)}{\frac{35}{3}j} \cancel{(\frac{35}{3}j)} = -\frac{12j}{35}$$

$$V(t) = \left( (2.88 + 3.84j) + \left( -\frac{12}{35}j \right) \right) (4 \angle 105^\circ)$$

$$V(t) = (2.88 + 3.49714288j) (4 \angle 105^\circ)$$

$$\sqrt{t} = \left( 4.53038719 \cancel{| \underline{t=1} } \right)^{50.5275} (4 \angle 0^\circ)$$

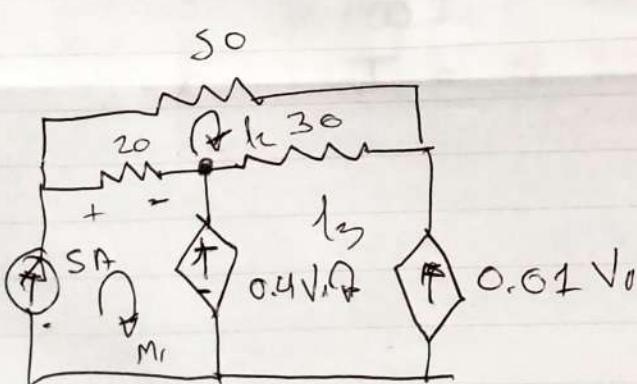
$$\sqrt{t} (18.01354 \underline{[155.5275]})$$



$$V_2 - V_3 = 8V$$

$$V_2 = 8V + \sqrt{3}$$

$$\frac{V_1 - V_2}{100} + \frac{V_2}{100} + \frac{\sqrt{3}}{100} + 3 \text{mA} = 0$$



$$I_1 = SA$$

$$I_3 = -0.01V_1$$

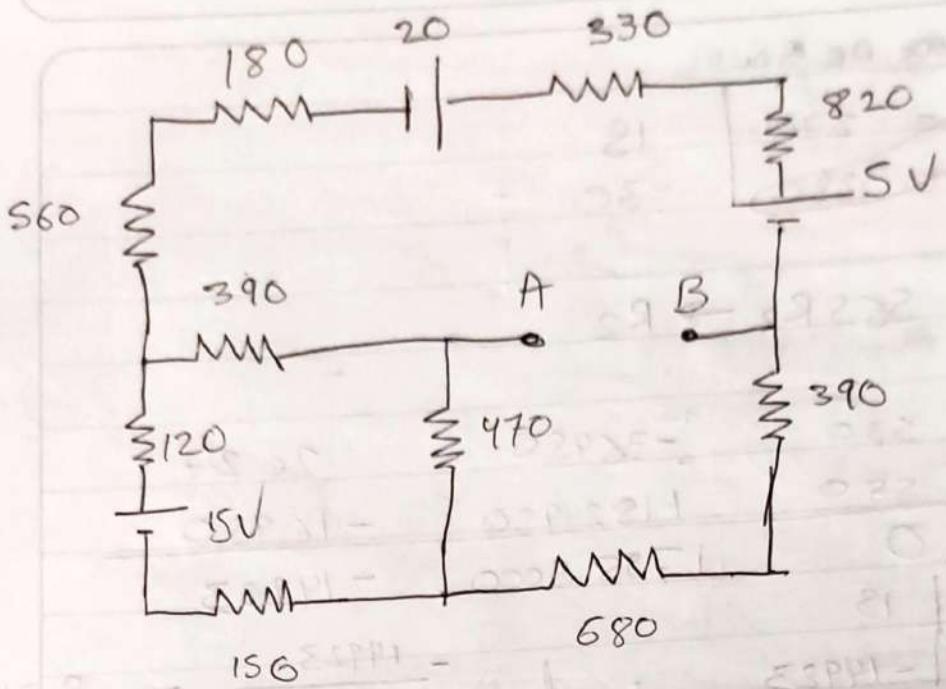
$$100I_2 - 20I_1 - 30I_3 = 0$$

$$100I_2 - 100 - 0.3V_1 = 6 \quad \checkmark$$

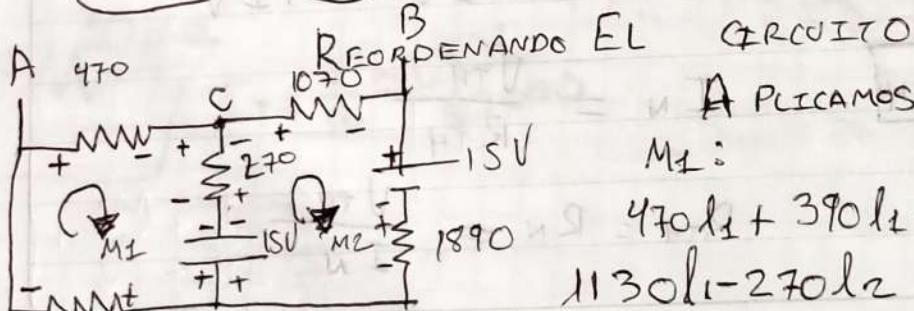
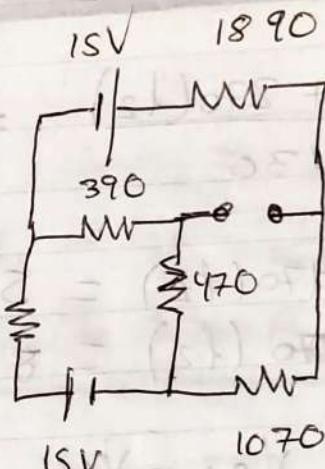
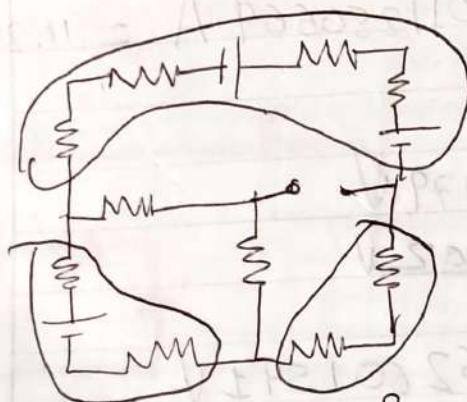
$$I_2 = \frac{100 + 0.3V_1}{100}$$

$$-V_1 + 0.4V_1 + 20I_1 - 20I_2$$

$$+ 20I_2 - 20I_2 = V_1 - 0.4V_1$$



SIMPLIFICANDO



REORDENANDO EL CIRCUITO

APLICAMOS LVIK

$M_1:$

$$470l_1 + 390l_2 + 270l_1 - 270l_2 = 15V$$

$$1130l_1 - 270l_2 = 15V$$

$M_2:$

$$1070l_2 + 1890l_2 + 270l_2 - 270l_1 + 30 \\ - 270l_1 + 3230l_2 = -30$$

Por METODO DE GAUSS

$$\begin{array}{l} R_1 \\ R_2 \end{array} \left| \begin{array}{r} 1130 - 270 \\ - 270 + 3230 \end{array} \right| \begin{array}{r} 1S \\ -30 \end{array}$$

$$13SR_1 + 56SR_2 \rightarrow R_2$$

$$\begin{array}{r} 1S2\ 550 \\ - 1S2\ 550 \\ \hline 0 \end{array} \quad \begin{array}{r} -36456 \\ +1824950 \\ \hline 1788\ 5000 \end{array} \quad \begin{array}{r} 2027 \\ -16950 \\ \hline -14923 \end{array}$$

$$\left| \begin{array}{r} 1130 - 270 \\ 0 + 788500 \end{array} \right| \begin{array}{r} 1S \\ -14923 \end{array} \quad I_2 = \frac{-14923}{1788500} = -8.34386mA$$

$$I_2 = \frac{1S + 270(I_2)}{1130} = 0.011280669A = 11.280669mA$$

$$V_{AC} = 470(I_2) = 5.30191479V$$

$$V_{BC} = 1070(I_2) = 8.9279302V$$

$$V_{AB} = V_{BC} - V_{AC} = 3.62601541V$$

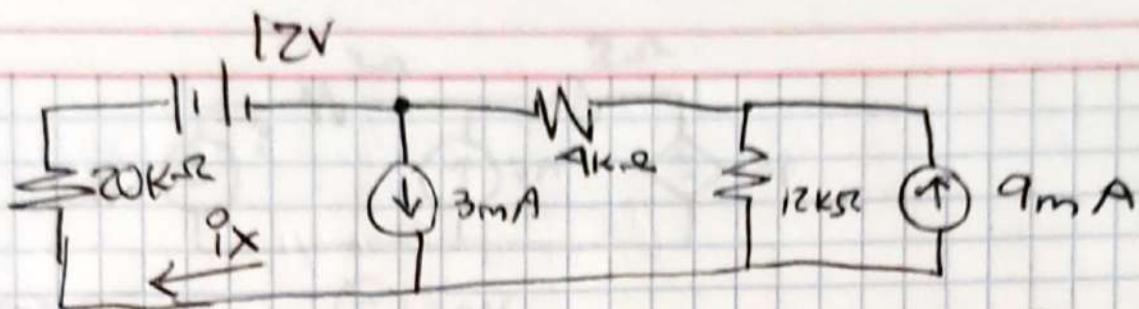
$$\boxed{V_{AB} = V_{TH}} \quad I_N = \frac{V_{TH}}{R_{TH}}$$

$$R_{TH} = R_N = \frac{V_{TH}}{I_N}$$

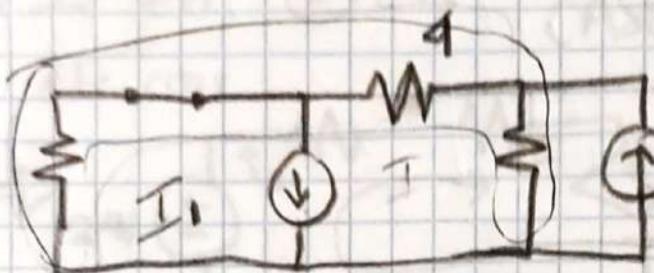
$$V_{TH} = 1070 - 1070e^{-1070/1130}$$

$$V_{TH} = 1070 - 1070e^{-1070/1130}$$

$$V_{TH} = 1070 - 1070e^{-1070/1130}$$



$$I_x = -2 \text{ mA}$$



$$I_3 = 9 \text{ mA}$$

$$I_1 - I_2 = 3 \text{ mA}$$

$$20kI_1 + 16kI_2 - 12kI_3 = 0$$

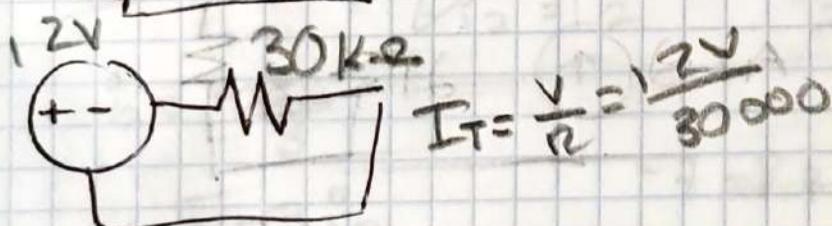
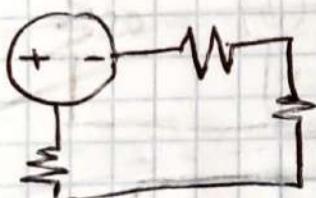
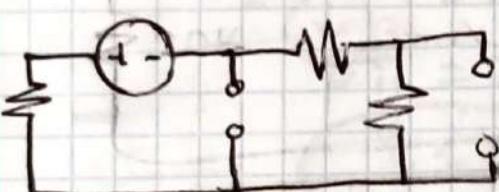
$$20000I_1 + 16000I_2 = 108$$

$$I_2 = I_1 - 3 \text{ mA}$$

$$20000I_1 + 16000(I_1 - 3 \text{ mA}) = 108$$

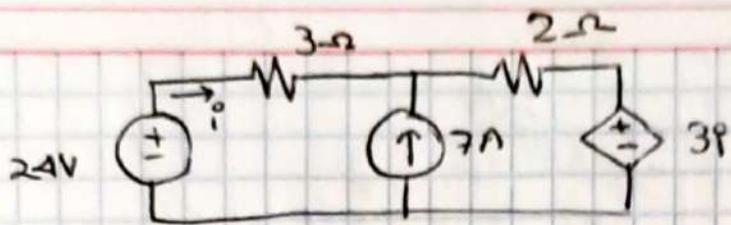
$$36000I_1 - 48 = 108$$

$$I_1 = 9.33 \text{ mA}$$

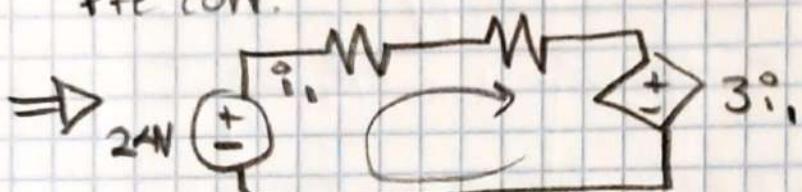


$$I_x = 6 \text{ mA}$$

$$I_x = 2.6 \text{ mA}$$



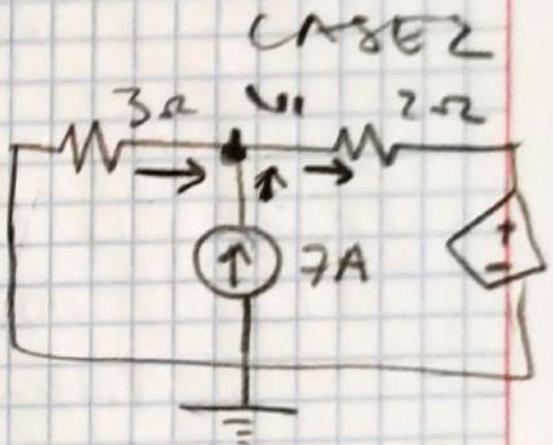
①  $I$  en  $\dot{V} = 24V$  CASE 1  
fte corr.



$$-24 + (3+2)\dot{i}_1 + 3\dot{i}_1$$

$$8\dot{i}_1 = 24$$

$$\dot{i}_1 = 3$$



$$-7 - \dot{i}_2 + \frac{V_1 - 3\dot{i}_2}{2} = 0$$

$$\begin{aligned} -\dot{i}_2 &= \frac{V_1}{2} - \frac{3\dot{i}_2}{2} \\ \dot{i}_2 &= \frac{V_1}{2} - \frac{3\dot{i}_2}{2} \end{aligned}$$

$$\dot{i}_2 = -\frac{V_1}{3}$$

$$V_1 = -3\dot{i}_2$$

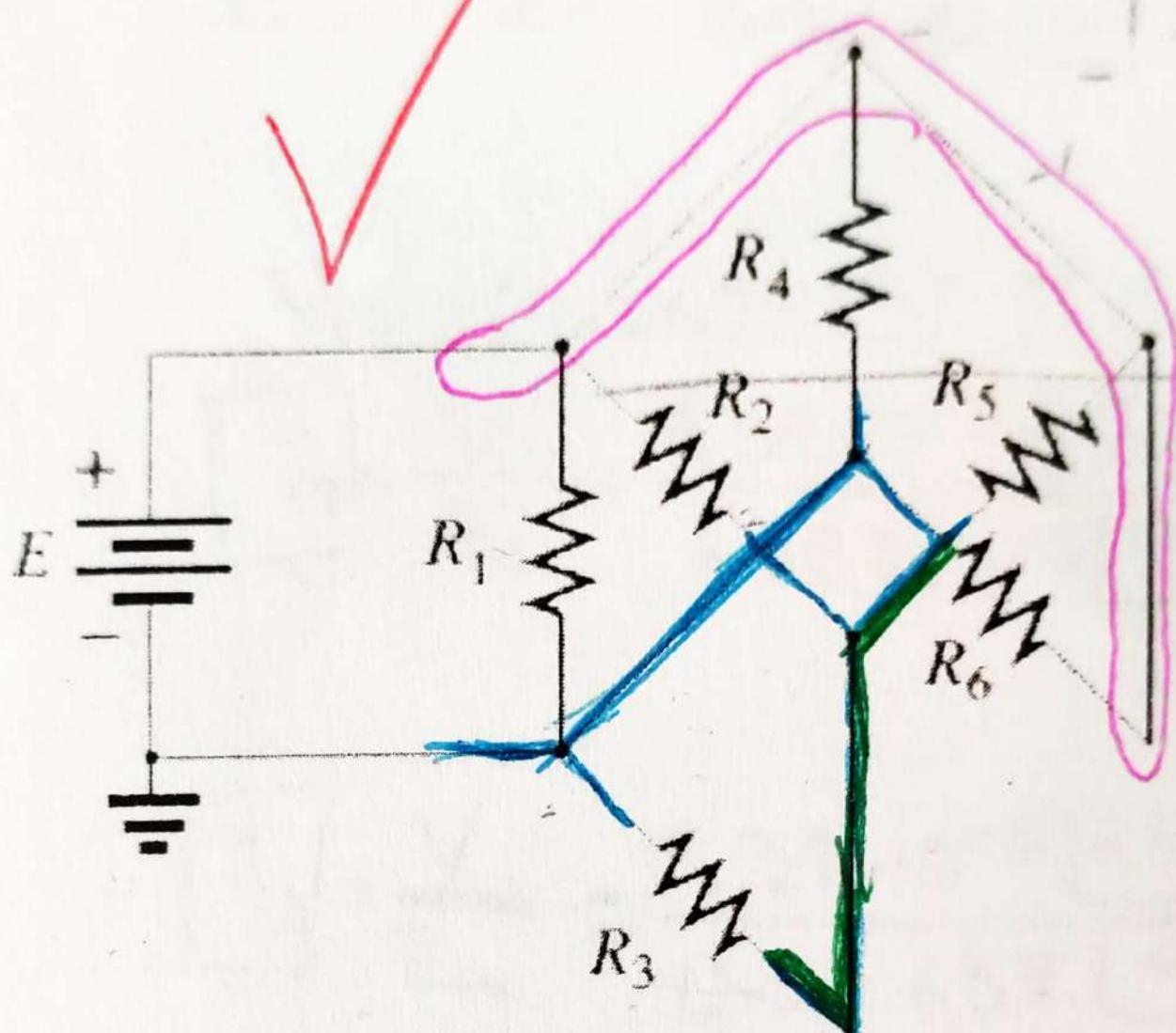
$$-7 - \dot{i}_2 + \frac{(-3\dot{i}_2)}{2} - 3\dot{i}_2 = 0$$

$$-7 - \dot{i}_2 - 3\dot{i}_2 = 0$$

$$\dot{i}_2 = -\frac{7}{4}$$

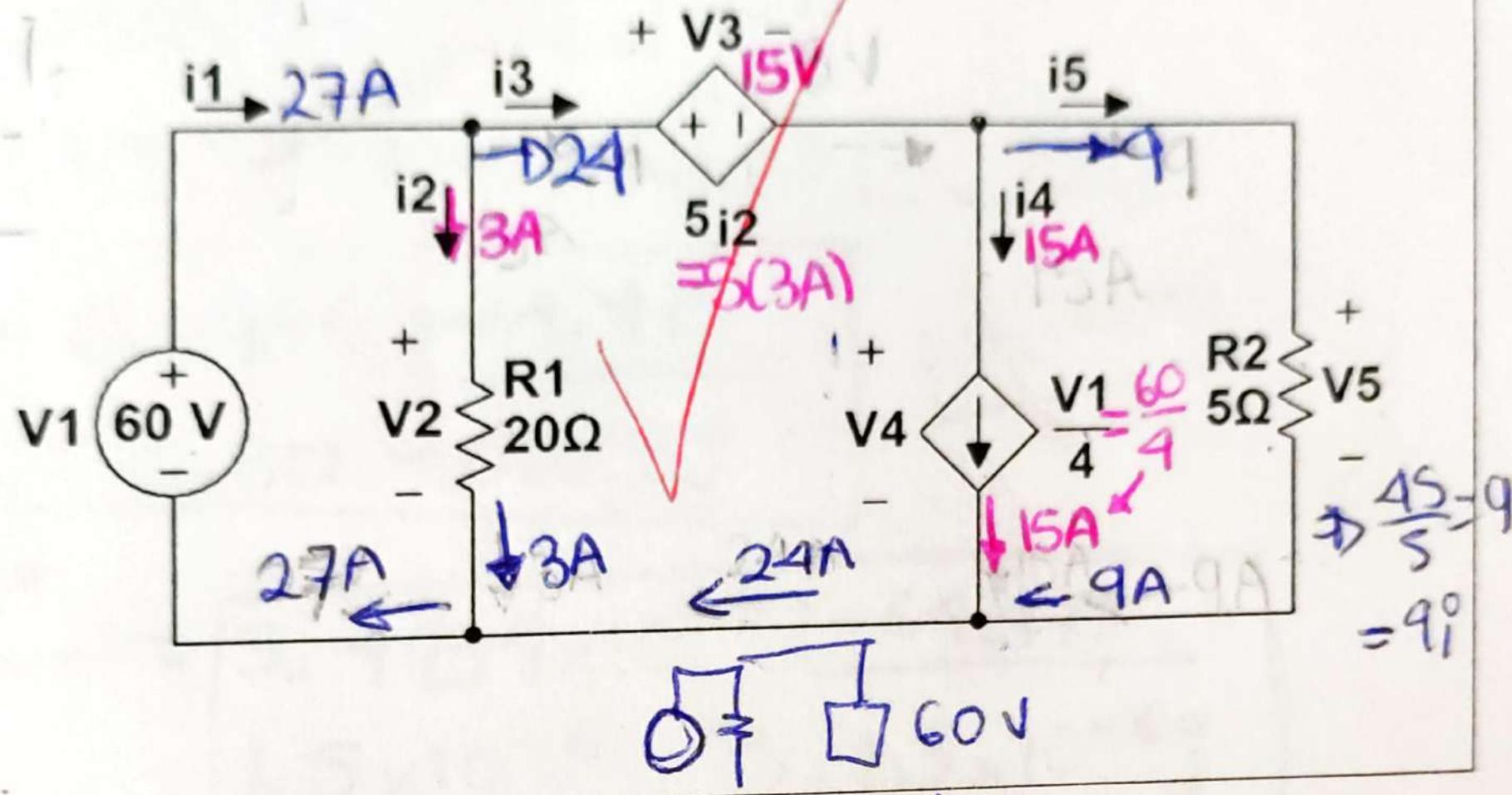
$$\dot{V} = \dot{i}_1 + \dot{i}_2 =$$

3. Considere  $R_1=R_2=R_3=R_4=R_5=R_6=100\Omega$ .  
Calcule la resistencia equivalente.



4. a) Evaluar todas las corrientes y las tensiones.

b) Calcular la potencia que absorbe cada uno de los cinco elementos del circuito y mostrar que la suma es cero.

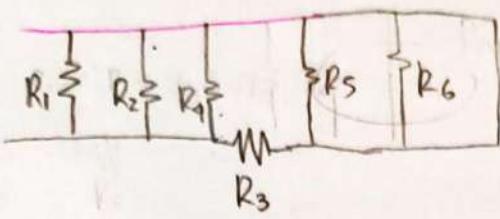


Notas:

nen sucio menos un punto.

s desordenados menos un punto.

A simplified diagram of the circuit is shown, consisting of a dependent voltage source  $60V - 15V = 45V$  in series with a dependent current source  $i_1 = 27A$ . This represents the equivalent circuit for calculating the note value.



$$R_{S,6} = \frac{(100)(100)}{200} = 50$$

$$R_{S,6,3} = 150$$

$$R_{eq} = \frac{1}{\frac{1}{100} + \frac{1}{100} + \frac{1}{100} + \frac{1}{150}} = \underline{\underline{27.272}}$$

4.  $V = RI$      $I_{R1} = \frac{60}{20} = 3A$

$$V_{i2} = 5(3A) = 15V$$

$$\frac{V_1}{4} = 15A$$

$$V_3 + V_{A,S} = 60V$$

$$V_{A,S} = 60V - 15V$$

$$V_{A,S} = 45V$$

$$I = \frac{V}{R} = \frac{15V}{5} = 9A$$

$$I_2 = 9A$$

$$\Rightarrow I_3 = 27A$$

$$I_1 = 27A$$

$$I_2 = 3A$$

$$I_1 = 15A$$

$$P = VI$$

$$P_{V1} = (60V)(27A) = 1620W$$

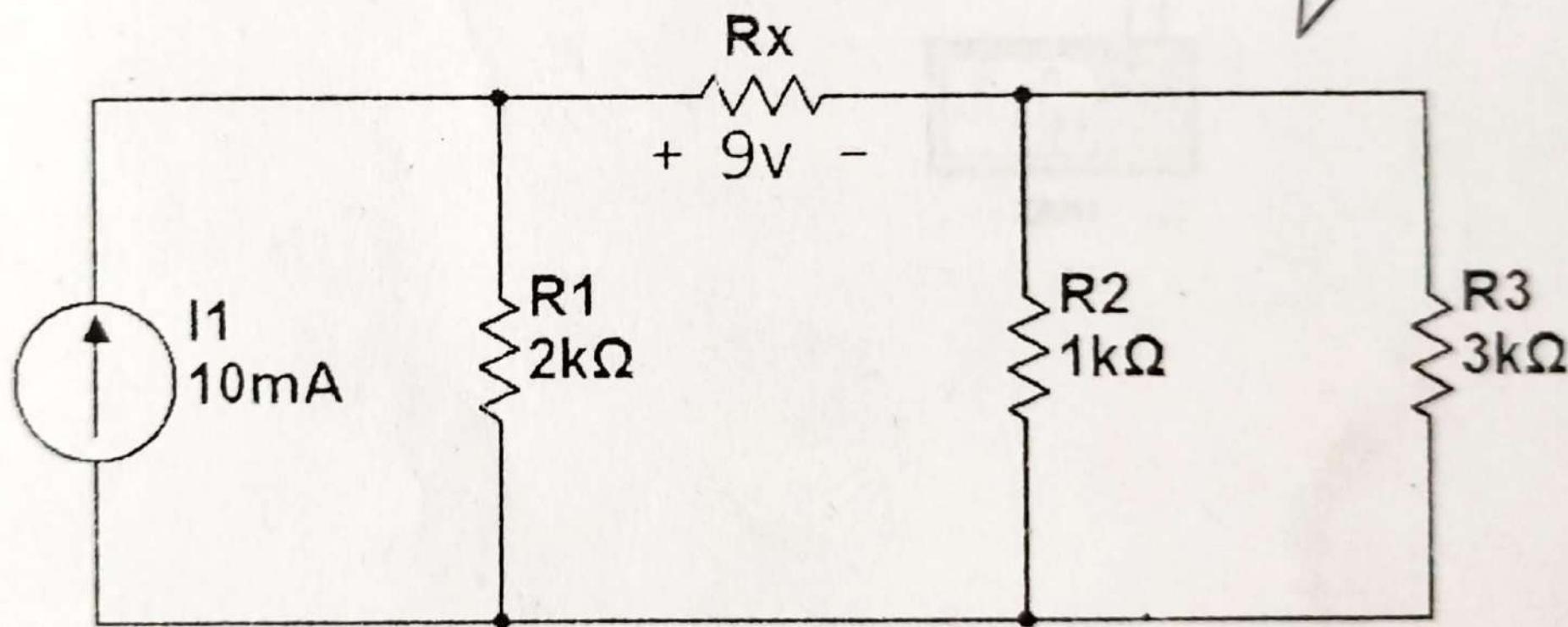
$$P_{V2} = (60V)(3A) = 180W$$

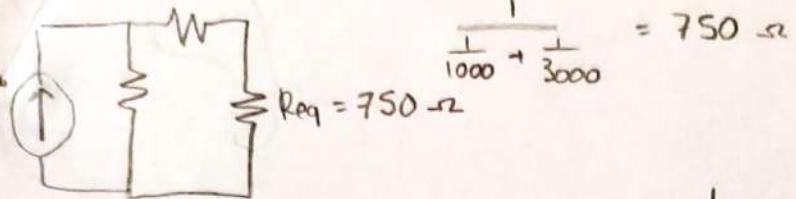
$$P_{V3} = (15V)(24A) = 360W$$

$$P_{V4} = (45V)(15A) = 675W$$

$$P_{V5} = (45V)(9A) = 405W$$

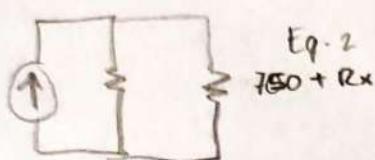
5. Utilizando divisor de corriente, determine la potencia que absorbe la resistencia Rx.





$$\frac{1}{1000} + \frac{1}{3000} = 750 \Omega$$

$$V - \frac{R_x}{R_x + Req}$$



$$I_{eq2} = 10mA \cdot \frac{\frac{1}{Rx+750}}{\frac{2000}{2000} + \frac{1}{Rx+750}}$$

$$\frac{\frac{1}{Rx}}{\frac{1}{R1} + \frac{1}{Rx}}$$

$$I_{eq} = (10 \times 10^{-3}) \cdot \frac{\frac{1}{(Rx+750)}}{\frac{2000}{2000} + \frac{1}{Rx+750+2000}}$$

$$I_{eq} = I_{Rx}$$

$$= (10 \times 10^{-3}) \cdot \frac{2000 (750 + Rx)}{(Rx+750)(Rx+750+2000)}$$

$$I_{Rx} = \frac{20}{Rx + 750 + 2000}$$

$$V = RI$$

$$I_{Rx} = \frac{V_{Rx}}{Rx}$$

$$\Rightarrow \frac{V_{Rx}}{Rx} = \frac{20}{Rx + 750 + 2000}$$

$$9(Rx + 750 + 2000) = 20Rx$$

$$9Rx + 6750 + 18000 = 20Rx$$

$$24750 = 11Rx$$

$$Rx = \frac{24750}{11} = 2250 \Omega \Rightarrow I_{Rx} = \frac{9V}{2250 \Omega} = 9 \times 10^{-3} = 1mA$$

$$P = V^2 / R \quad P = 9V(1mA) = 0.036 W$$