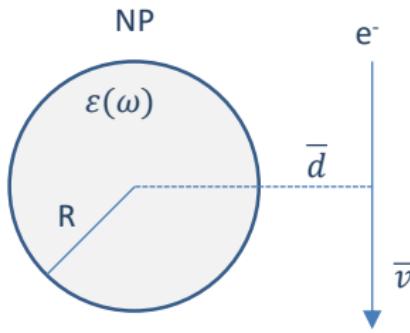


## 4. LSPR Imaging

### 4.2 Electron Energy Loss Spectroscopy (EELS)

Excitation induced by fast electrons (100 - 300 keV) passing close to a NP



Electron trajectory

$$\bar{r}(t) = \bar{d} + \bar{v} t$$

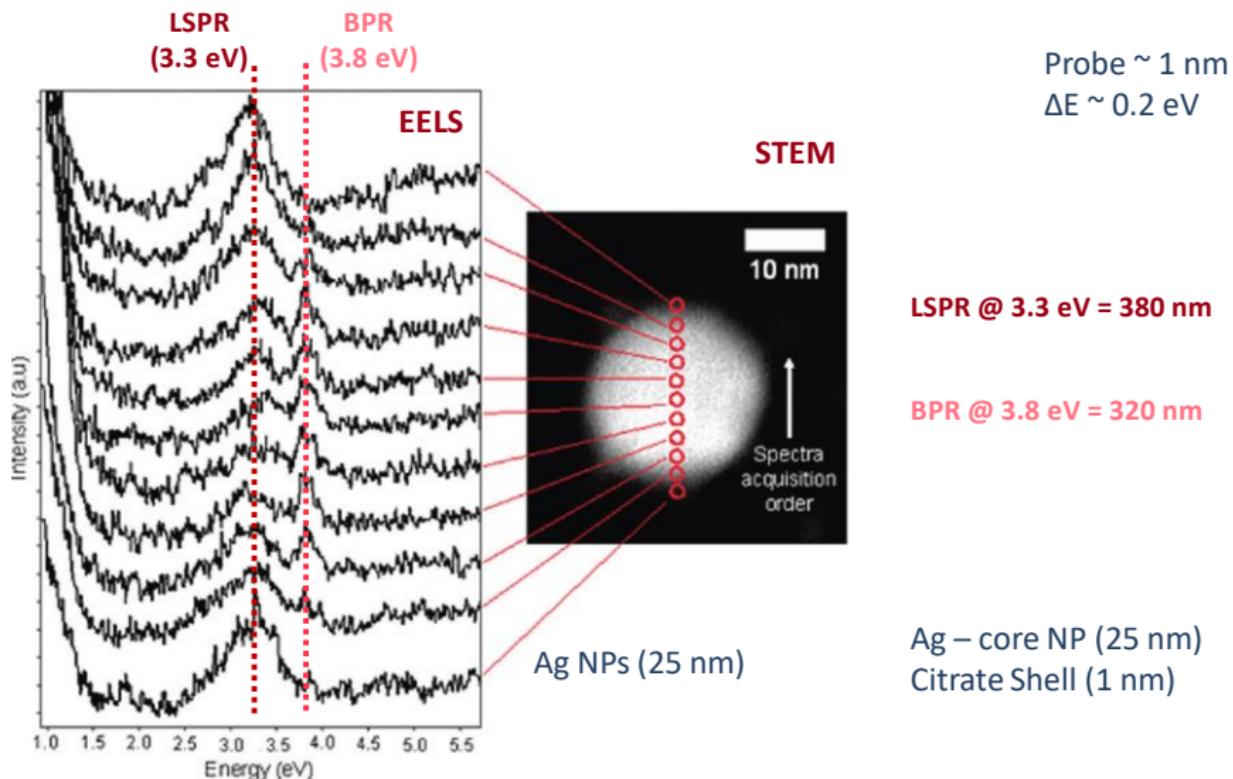
Energy Loss

$$\Delta E = \int e \bar{v} \cdot \bar{E}_{ind}[\bar{r}(t), t] dt = \int_0^{\infty} \Gamma(\omega) d\omega$$

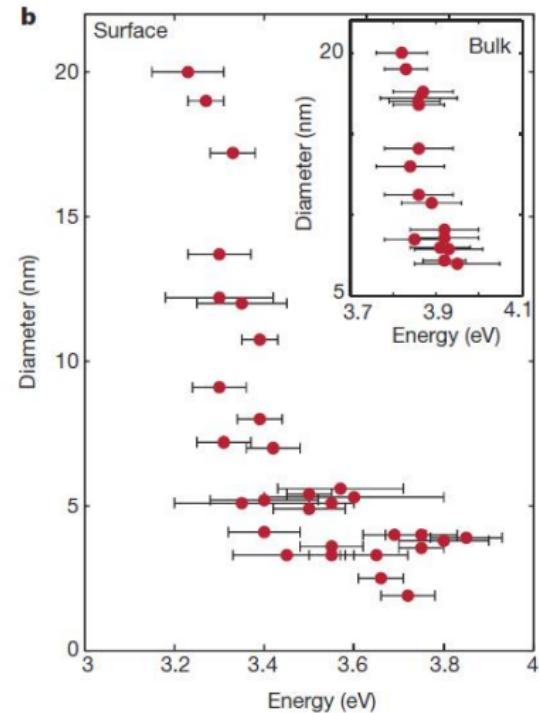
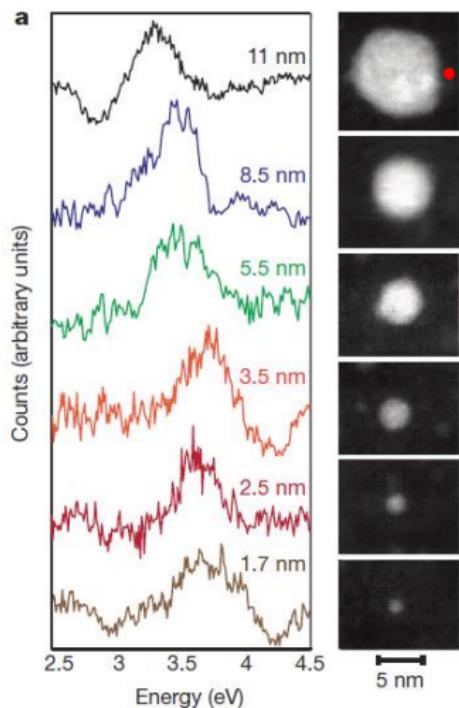
Loss Probability

$$\Gamma(\omega) = \frac{1}{\pi} \int Re(e \bar{v} \cdot \bar{E}_{ind}[\bar{r}(t), \omega] e^{-i\omega t}) dt$$

## LSPR in Ag NP: EELS



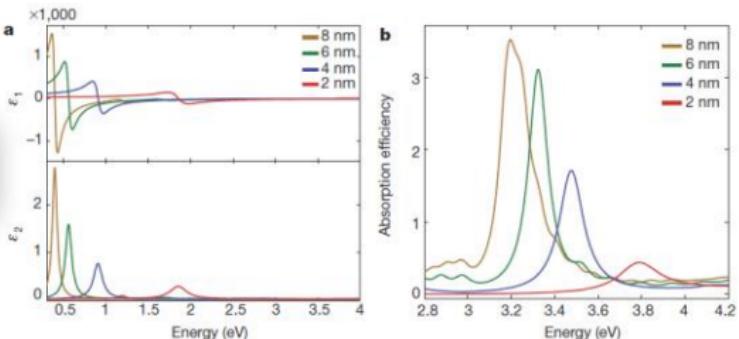
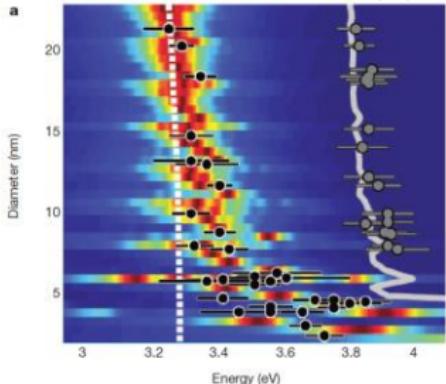
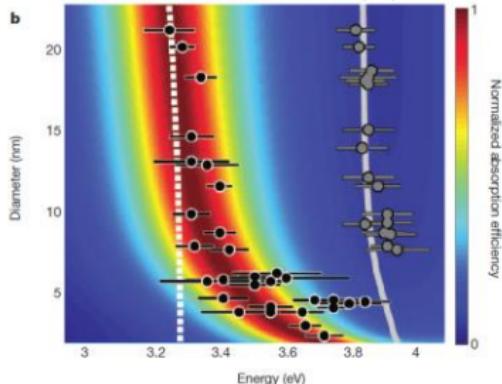
A. L. Koh, et al. "Electron Energy-Loss Spectroscopy (EELS) of Surface Plasmons in Single Silver Nanoparticles and Dimers: Influence of Beam Damage and Mapping of Dark Modes," ACS Nano 3, 3015–3022 (2009).



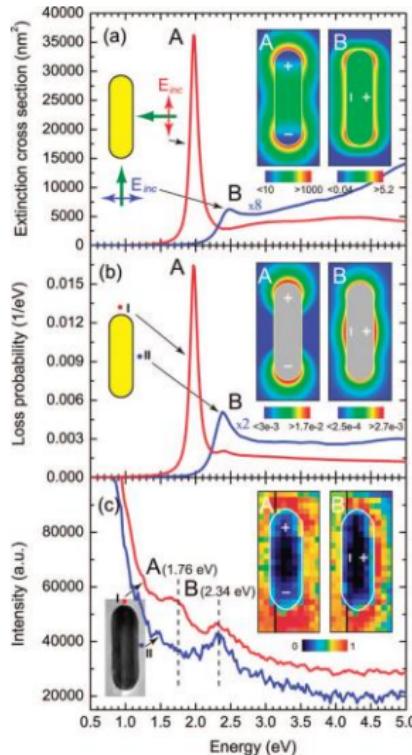
Quantum to Classical transition

**Analytic model for  $\varepsilon(\omega)$** 

$$\varepsilon(\omega) = \varepsilon_{IB} + \omega_p^2 \sum_i \sum_f \frac{S_{if}}{\omega_{if}^2 - \omega^2 - i\gamma\omega}$$


**Analytic model for  $\varepsilon(\omega)$** 

**DFT model for  $\varepsilon(\omega)$** 


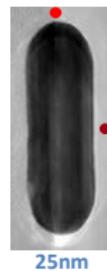
J. A. Scholl, A. L. Koh, and J. A. Dionne, "Quantum plasmon resonances of individual metallic nanoparticles," Nature **483**, 421–427 (2012).



Theory:  
Light induced  $|E|^2$

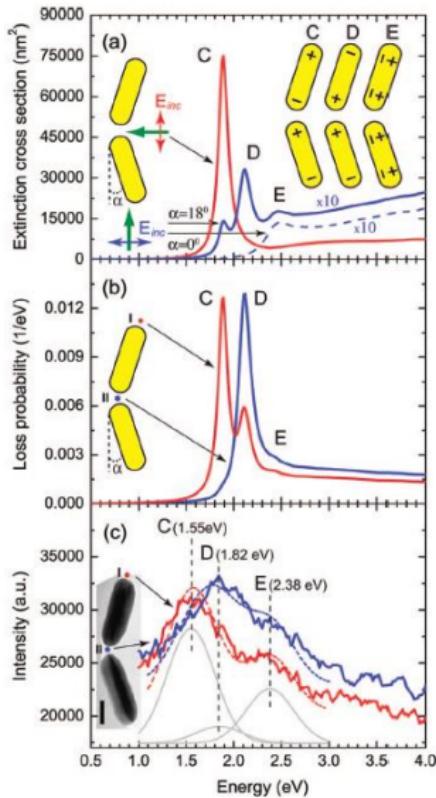
Transmission Electron Microscope  
STEM – FEI Tecnai F20

- $E=200\text{keV}$
- $\Delta E = 0.22 \text{ eV}$  (Wien-filter)
- Beam size: 2 nm



Theory:  
EEL probability map

Exp:  
EEL intensity maps and profiles



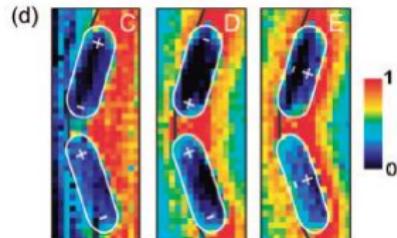
Theory:  
Light induced  $|E|^2$

Transmission Electron Microscope  
STEM – FEI Tecnai F20

- $E = 200\text{keV}$
- $\Delta E = 0.22 \text{ eV}$  (Wien-filter)
- Beam size: 2 nm

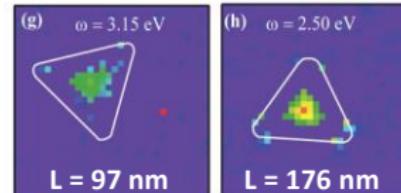
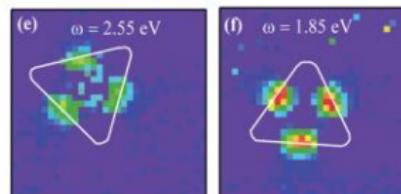
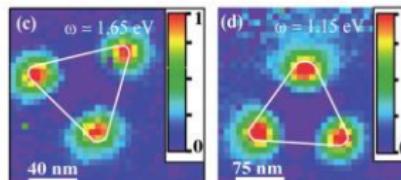
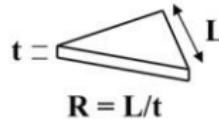
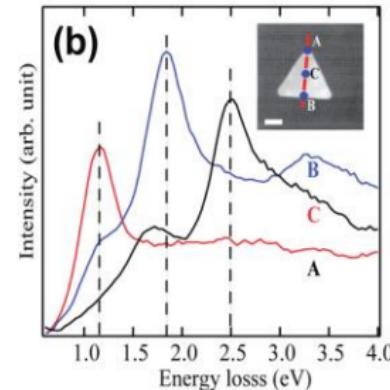
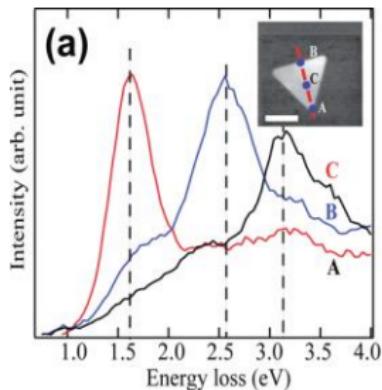
Theory:  
EEL probability map

Plasmonic  
Dark Modes (D)



Exp:  
EEL spectra and  
intensity map

# LSPR in Ag NPrisms: EELS

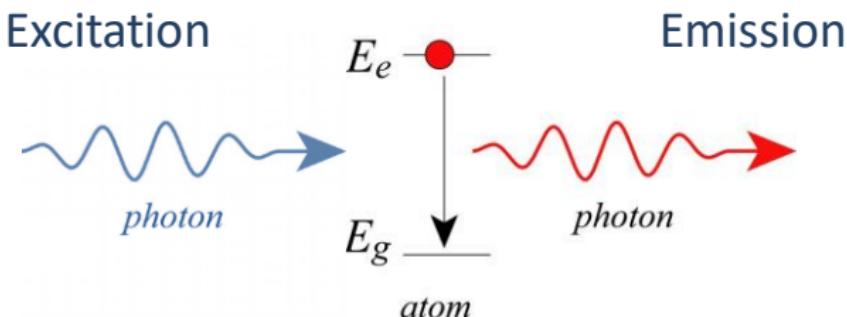


**(a)**  
 $t = 4 \text{ nm}$   
 $L = 97 \text{ nm}$

**(b)**  
 $t = 6 \text{ nm}$   
 $L = 176 \text{ nm}$



# Nanostructure - Emitter interaction



### Spontaneous emission of a two-level emitter:

**Initial state:** excited state + 0 photons.

**Final state:** ground state emitter + 1 photon in some photon state

- unperturbed emitter eigenfunction is  $|\psi_i\rangle$
- The photon field perturbs the Hamiltonian  $H_0$  as  $H = H_0 + V$

$$V = -\mathbf{p} \cdot \mathbf{E}$$

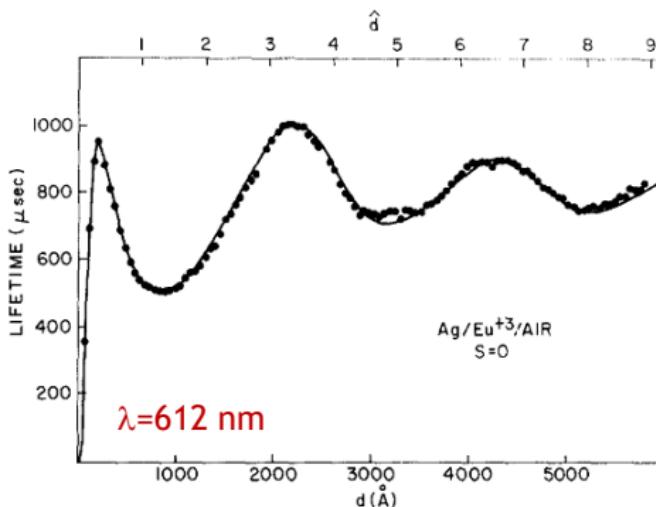
Dipole operator      Electric field

The interaction induces a transition from  $|\psi_i\rangle$  to  $|\psi_f\rangle$  (energy conservation)

**Fermi's Golden Rule:** rate of decay of the initial state  $\psi_i$

$$\gamma = \gamma_r = \frac{2\pi}{\hbar} \sum_f |\langle \psi_f | V | \psi_i \rangle|^2 \delta(\epsilon_f - \epsilon_i) = \frac{2\pi}{\hbar} \rho(\epsilon_f) |\langle \psi_f | V | \psi_i \rangle|^2$$

$$\gamma_{meas} = \gamma = \gamma_{nr} + \gamma_r \quad \text{real emitter (radiative & non-radiative decays)}$$



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### INFLUENCE OF A DIELECTRIC INTERFACE ON FLUORESCENCE DECAY TIME

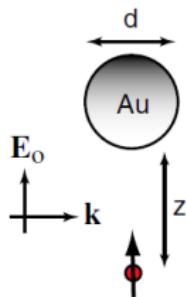
K. H. DREXHAGE\*

IBM Research Laboratory, San Jose, California, USA

When a mirror is placed near a fluorescing molecule, not only the angular distribution of the fluorescence is affected, but also the decay time. This effect is considered for the case of the reflecting interface between two dielectrics of different refractive indices. The fluorescence decay time varies markedly due to the presence of such an interface. In case of fluorescing molecules placed directly at the interface between a medium of refractive index 1.54 and air, the decay time is lengthened by a factor of 1.08 if their transition moment is oriented parallel to the interface, and by a factor of 3.61 if the transition moment is oriented perpendicular to the interface. These considerations are compared with measurements on monomolecular layers of an europium dibenzoylmethane complex which were held at a variable, but well defined distance from the interface.



fluorescence lifetime variation as a function of  
the distance of Eu ions from a Ag mirror.


 Emitter at  $\mathbf{r}_m$ 

Fluorescence rate

$$\gamma_{em} = \gamma_{exc} q_a = \gamma_{exc} \frac{\gamma_r}{\gamma_r + \gamma_{nr}} = \gamma_{exc} \frac{\gamma_r}{\gamma}$$

$$\gamma_{exc} \propto |\mathbf{p} \cdot \mathbf{E}|^2$$

$$\mathbf{E}(\mathbf{r}_m, \omega)$$

$$\mathbf{E}_m(\mathbf{r}) = (k^2/\epsilon_0) \vec{\mathbf{G}}(\mathbf{r}, \mathbf{r}_m) \mathbf{p}$$

$$\gamma = \frac{2\omega}{3\hbar\epsilon_0} |\mathbf{p}|^2 \rho(\mathbf{r}_m, \omega)$$

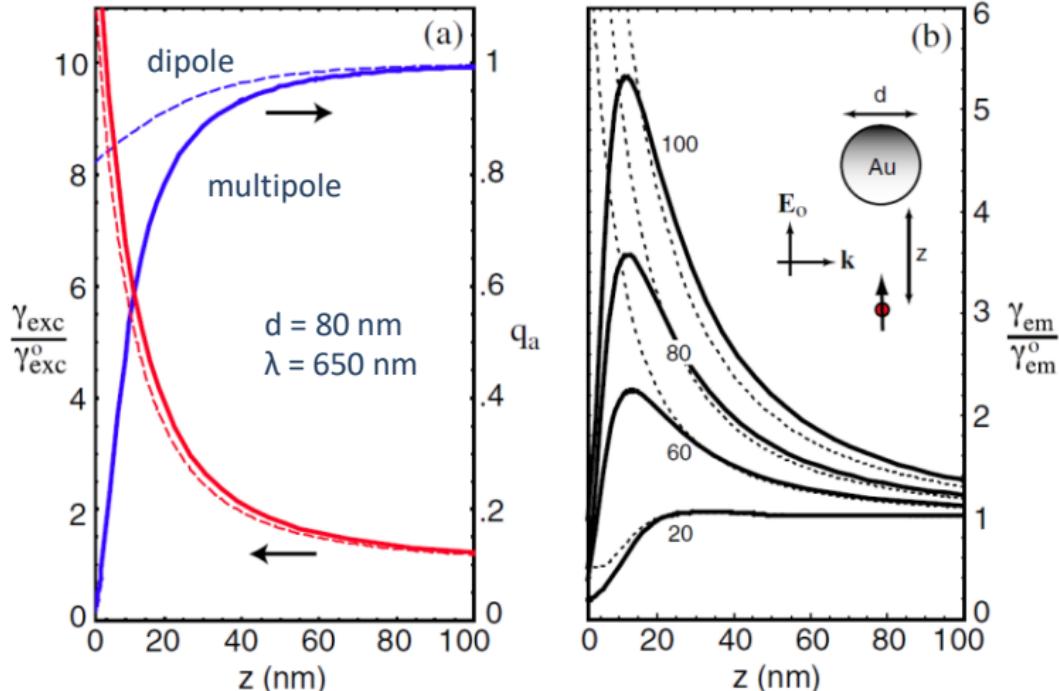
**DoS**  $\rho(\mathbf{r}_m, \omega) = \frac{6\omega}{\pi c^2} [\mathbf{n}_p \cdot \text{Im}\{\vec{\mathbf{G}}(\mathbf{r}_m, \mathbf{r}_m)\} \cdot \mathbf{n}_p]$

$$\gamma_0 = \omega^3 |\mathbf{p}|^2 / (3\pi\epsilon_0\hbar c^3)$$

$$\rho = \omega^2 / (\pi^2 c^3) \quad (\text{Vacuum})$$

$$\gamma_{exc}/\gamma_{exc}^0 = |[\mathbf{n}_p \cdot \mathbf{E}(\mathbf{r}_m)]/[\mathbf{n}_p \cdot \mathbf{E}_0(\mathbf{r}_m)]|^2$$

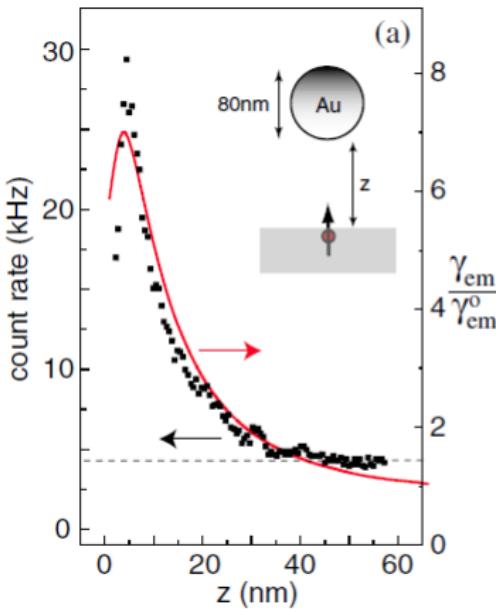
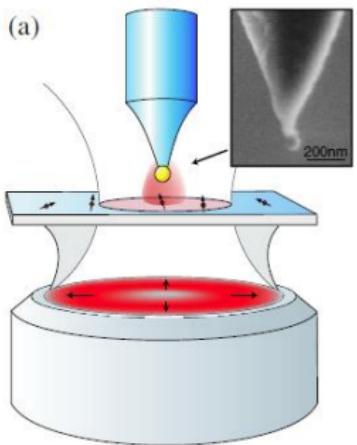
$$\frac{\gamma_{nr}}{\gamma_0} = \frac{1}{P_0} \frac{1}{2} \int_V \text{Re}\{\mathbf{j}(\mathbf{r}) \cdot \mathbf{E}_m^*(\mathbf{r})\} d\mathbf{r}^3$$



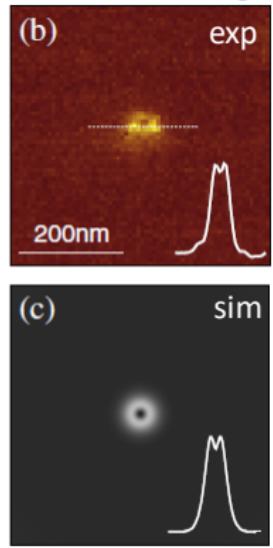
Fluorescence rate

$$\gamma_{em} = \gamma_{exc} q_a = \gamma_{exc} \frac{\gamma_r}{\gamma_r + \gamma_{nr}}$$

# Nano-antennas



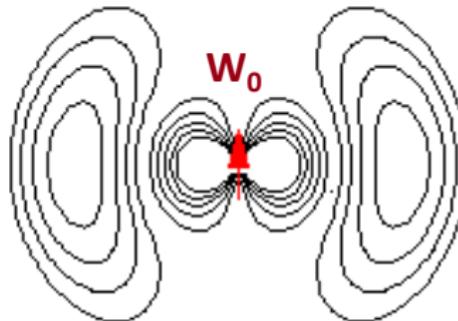
Fluorescence imaging



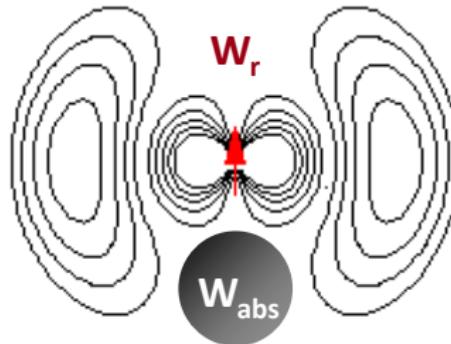
$z = 2 \text{ nm}$   
central dark spot =  
quenching

Fluorescence rate

$$\gamma_{em} = \gamma_{exc} q_a = \gamma_{exc} \frac{\gamma_r}{\gamma_r + \gamma_{nr}}$$



$$q_0 = \frac{\gamma_{r,0}}{\gamma_{r,0} + \gamma_{nr,0}}$$



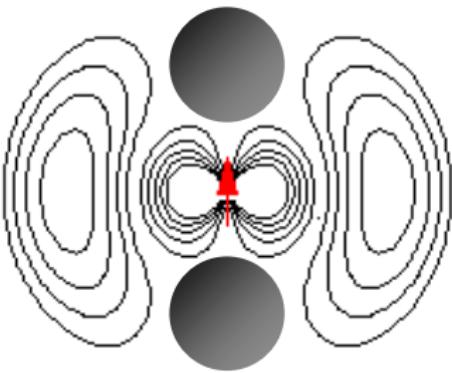
$$q = \frac{\gamma_r / \gamma_{r,0}}{\gamma_r / \gamma_{r,0} + \gamma_{abs} / \gamma_{r,0} + (1 - q_0) / q_0}$$

$$\frac{\gamma_r}{\gamma_{r,0}} = \frac{W_r^{na}}{W_{r,0}} \quad \frac{\gamma_{abs}}{\gamma_{r,0}} = \frac{W_{abs}^{na}}{W_{r,0}}$$

$$\frac{\gamma_{nr}}{\gamma_{r,0}} = \frac{\gamma_{abs} + \gamma_{nr,0}}{\gamma_{r,0}}$$

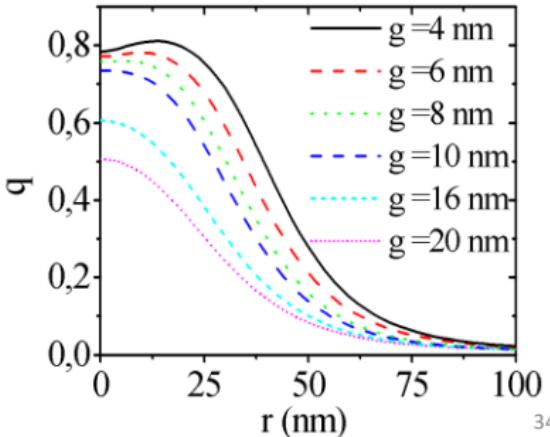
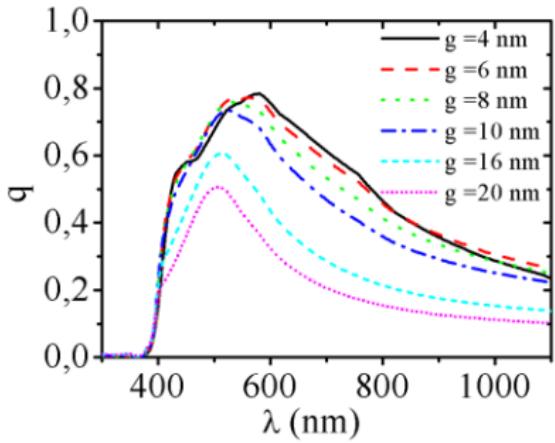
Quantum Efficiency enhancement

$q_0=0.01$   
 $D=60 \text{ nm}$

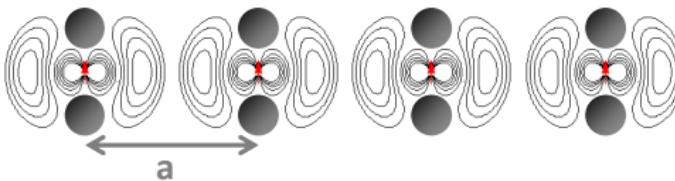


$q \sim 0.8$

$(q > 0.5 \text{ if } r < 25 \text{ nm})$



- $D = 100 \text{ nm}$
- $N_S = 1200$
- $a \text{ variable}, g = 20 \text{ nm}$
- $\lambda_{\text{res}} \sim n \times a$

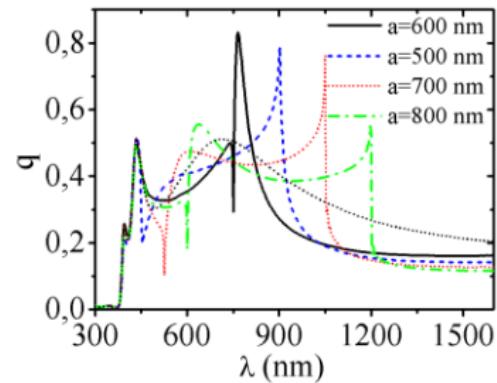


$$q \sim 0.8$$

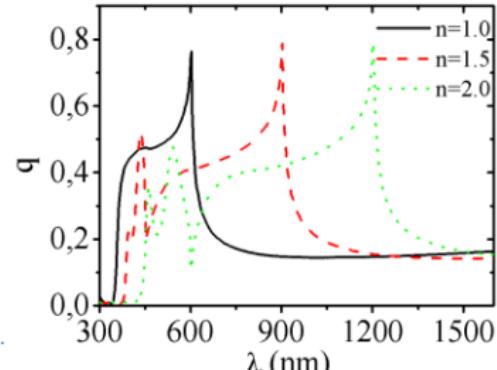
$$\lambda \sim 500 \text{ nm}$$

$$\lambda = 1.5 \mu\text{m}$$

$a \text{ variable}, n=1.5$



$n \text{ variabile}, a=600 \text{ nm}$



Pellegrini, G., Mattei, G. & Mazzoldi, P. Tunable, directional and wavelength selective plasmonic nanoantenna arrays. *Nanotechnology* **20**, 065201 (2009).