

## 1. Pawlow's result (first order TD, fTD)

$$\frac{T - T_0}{T_0} = \frac{\Delta T}{T_0} \Big|_{fTD} = -\frac{2}{LR\rho_S} \left( \gamma_S - \gamma_L \left( \frac{\rho_S}{\rho_L} \right)^{2/3} \right) = -\frac{A}{R} < 0$$

## 2. Liquid Layer Model (LLM)

$$\frac{\Delta T}{T_0} \Big|_{LLM} = -\frac{2\gamma_{SL}}{\rho_S L(R - \delta)} - \frac{2\gamma_{LV}}{\rho_S LR} \left( 1 - \frac{\rho_S}{\rho_L} \right) = -\frac{A}{R - \delta} - \frac{B}{R}$$

## 3. Smooth interfaces interaction (SII)

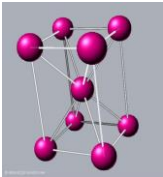
$$\frac{\Delta T}{T_0} \Big|_{SII} = -\frac{2\gamma_{SL}}{\rho_S L(R - \delta)} (1 - e^{-\delta/\xi}) - \frac{\Gamma R^2}{\rho_S L \xi (R - \delta)^2} e^{-\delta/\xi} = -\frac{A}{R - \delta} (1 - e^{-\delta/\xi}) - \frac{B \Gamma R^2}{(R - \delta)^2} e^{-\delta/\xi}$$

## 4. Thermal expansion variation (TEV)

$$\frac{\Delta T}{T_0} \Big|_{TEV} = -\frac{2}{\rho_S RL} \left( \gamma_{SM} - \gamma_{LM} \left( \frac{\rho_S}{\rho_L} \right)^{2/3} \right) + \frac{\Delta E}{L}$$

$\Delta E$  = strain energy difference  
(thermal expansion matrix-cluster)

# TSE in In NCs in silica



In = tetragonal cell

$T_M$  (bulk) = 429.8 K  
(156.6 °C)

In<sup>2+</sup> implantation in silica

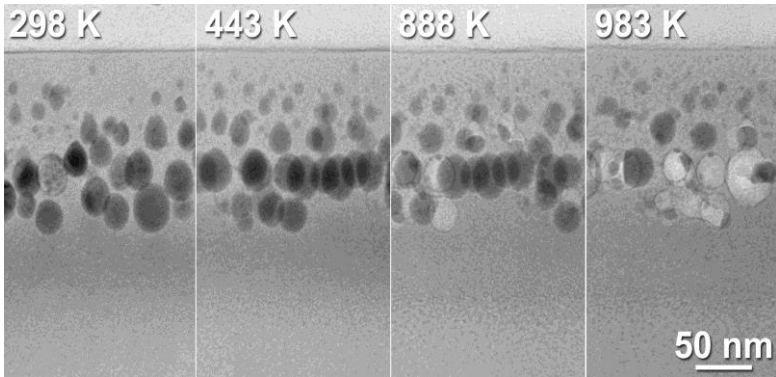
Energy: 320 keV

Fluence:  $2 \times 10^{17}$  In<sup>2+</sup>/cm<sup>2</sup>

Rp = 100nm (ion projected range )

$\Delta R_p = 70$ nm (straggling)

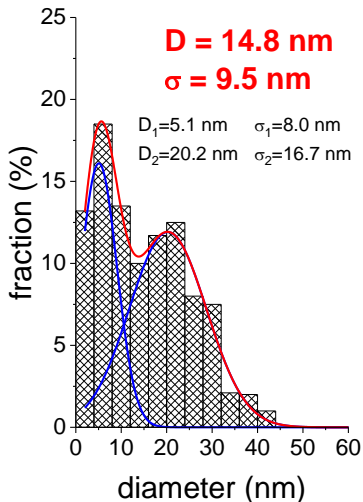
114.818	49
550.3	1.78
In	+3 +2 +1
Indium	
[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>1</sup>	



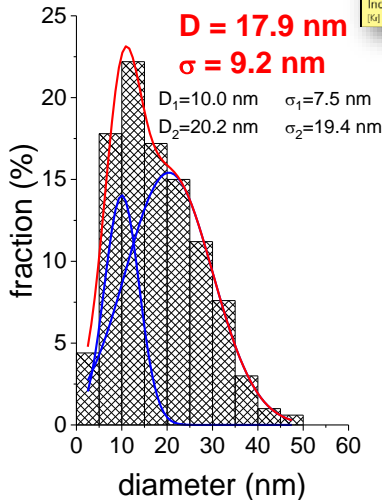
M. A. Tagliente, G. Mattei, L. Tapfer, M. Vittori Antisari, and P. Mazzoldi, Phys. Rev. B 70 (2004) 075418

G.Mattei

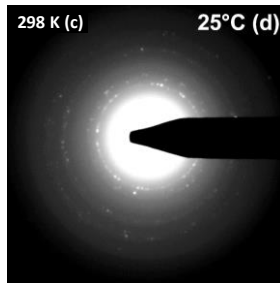
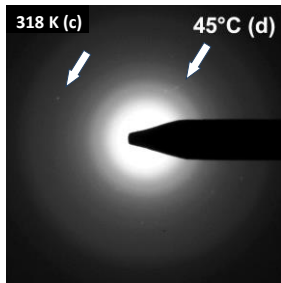
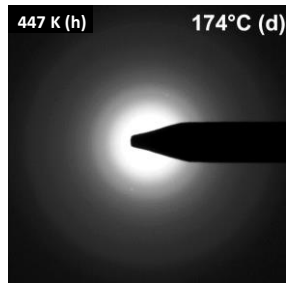
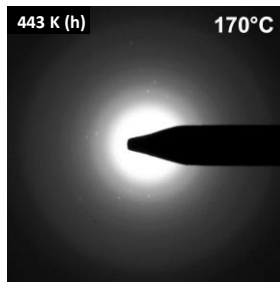
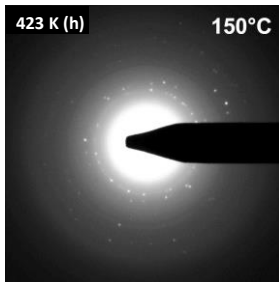
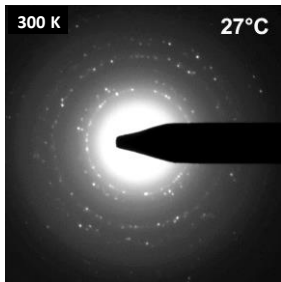
**T = 300 K**



**T = 443 K**

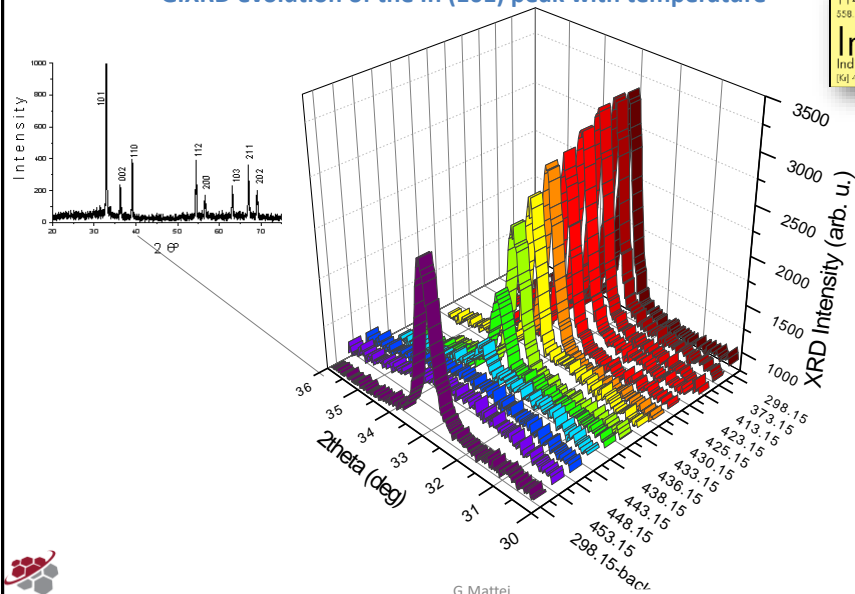


114.818	49
558.3	1.78
In	+3
Indium	12
[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>1</sup>	11

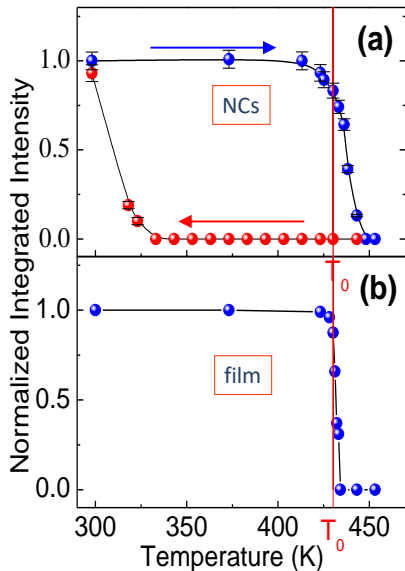


## GIXRD evolution of the In (101) peak with temperature

114.818	49
558.3	1.78
In	+3
Indium	+2
[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>1</sup>	+1



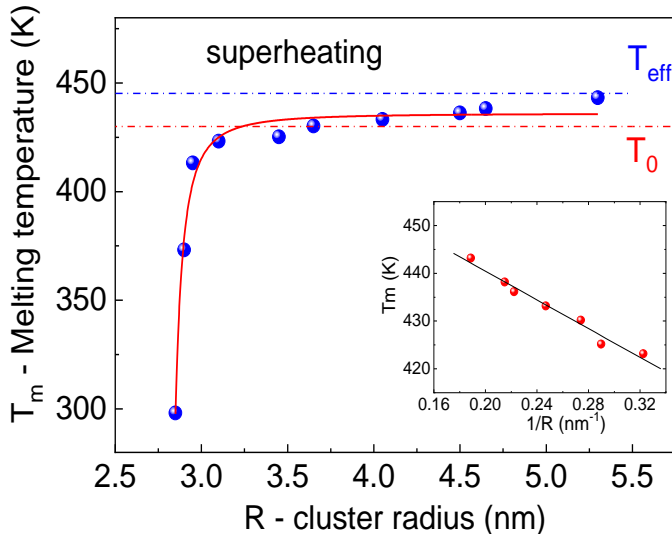
## GIXRD analysis



(a) Normalized integrated intensity of the nanoclusters In (101) GIXRD peak versus the temperature for the thermal cycle between RT and 453 K. Blue and red solid circles represent data obtained during the heating and cooling sequences, respectively.  $T_0$  indicates the In bulk melting point (430 K)

(b) Normalized integrated intensity of a In film evaporated on a glass substrate.  $T_0$  indicates the In bulk melting point.

Thermal hysteresis loop for In NCs in  $\text{SiO}_2$ :  
Superheating of  $13 \pm 1$  K  
Supercooling of  $107 \pm 1$  K



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## Some basic thermodynamics...

114.818	49
550.3	1.78
In	+3 +2 +1
Indium	
[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>1</sup>	

Pressure on In NCs?

$$K \equiv -\frac{1}{V} \frac{\partial V}{\partial P} \bigg|_T$$

$$\Delta P = -\frac{\Delta V}{K V} = -\frac{3}{K} \frac{\Delta d}{d}$$

$$\frac{\Delta d_{(101)}}{d_{(101)}} \bigg|_{XRD} = 1.5 \cdot 10^{-3}$$

$K = 0.00273 \text{ GPa}^{-1}$  (bulk isothermal compressibility)

$\Delta P = 0.17 \text{ GPa}$

Clausius-Clapeyron  
(from Gibbs-Duhem):

$$\frac{dP}{dT} = \frac{L_{mol}}{T_0 \Delta V_{mol}}$$

$$\Delta T = \frac{\Delta P}{L} T_0 \Delta V_{mol}$$

$$L_{mol} = 3.25 \text{ kJ/mol}$$

$$\Delta V_{mol} = 0.32 \text{ cm}^3/\text{mol}$$

$$\Delta P = 0.17 \text{ GPa}$$

$$T_0 = 430 \text{ K}$$



$$\Delta T_{\text{theo}} \sim 7 \text{ K}$$

$$\Delta T_{\text{exp}} \sim 13 \text{ K}$$