Worksheet Week VIII

Write the series representation of the following functions and indicate the values of |z| (annular domain) for which this representation is valid:

(a)
$$z \cos(z^2)$$
:

(b)
$$\cos(1/z^2)$$
:

(c)
$$z \cos(1/z^2)$$
:

(d) Find a representation of the function

$$f(z) = \frac{1}{1+z}$$

in negative powers of z that is valid when $1 < |z| < \infty$.

(e) Give two Laurent series expansions for the funcion

$$f(z) = \frac{1}{z^2(1-z)}.$$