

# act2-estadística

October 21, 2023

```
[3]: pip install ucimlrepo
```

```
Collecting ucimlrepo
  Downloading ucimlrepo-0.0.3-py3-none-any.whl (7.0 kB)
Installing collected packages: ucimlrepo
Successfully installed ucimlrepo-0.0.3
```

## 0.0.1 1. Introducción

En este informe, se realizará un análisis de datos utilizando un conjunto de datos sobre abalones. El objetivo es evaluar el impacto de puntos influyentes, outliers, multicolinealidad y técnicas de transformación en el modelo de regresión. Se calcularán métricas como  $R^2$  y MSE y se interpretarán los resultados.

## 0.0.2 2. Análisis Inicial de los Datos

```
[4]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import statsmodels.api as sm
from scipy.stats import norm, uniform, skewnorm
from ucimlrepo import fetch_ucirepo

from sklearn.preprocessing import MinMaxScaler, StandardScaler

# Obtención del dataset
abalone = fetch_ucirepo(id=1)

# data (as pandas dataframes)
X = abalone.data.features
y = abalone.data.targets

X = X.drop('Sex', axis=1)

X.reset_index(drop=True, inplace=True)
y.reset_index(drop=True, inplace=True)
df = pd.concat([y, X], axis=1)
```

## Análisis de Puntos Influyentes

```
[5]: X_fit = sm.add_constant(X)
```

```
[6]: X_fit
```

```
[6]:
```

	const	Length	Diameter	Height	Whole_weight	Shucked_weight	\
0	1.0	0.455	0.365	0.095	0.5140	0.2245	
1	1.0	0.350	0.265	0.090	0.2255	0.0995	
2	1.0	0.530	0.420	0.135	0.6770	0.2565	
3	1.0	0.440	0.365	0.125	0.5160	0.2155	
4	1.0	0.330	0.255	0.080	0.2050	0.0895	
...	...	...	...	...	...	...	...
4172	1.0	0.565	0.450	0.165	0.8870	0.3700	
4173	1.0	0.590	0.440	0.135	0.9660	0.4390	
4174	1.0	0.600	0.475	0.205	1.1760	0.5255	
4175	1.0	0.625	0.485	0.150	1.0945	0.5310	
4176	1.0	0.710	0.555	0.195	1.9485	0.9455	

	Viscera_weight	Shell_weight
0	0.1010	0.1500
1	0.0485	0.0700
2	0.1415	0.2100
3	0.1140	0.1550
4	0.0395	0.0550
...	...	...
4172	0.2390	0.2490
4173	0.2145	0.2605
4174	0.2875	0.3080
4175	0.2610	0.2960
4176	0.3765	0.4950

[4177 rows x 8 columns]

```
[7]: model = sm.OLS(y,X_fit)
      fitted_model = model.fit()
```

Calculo de  $r^2$  y parametros

```
[8]: print(fitted_model.params)
      print('\nr^2=', fitted_model.rsquared)
```

```
const          2.985154
Length         -1.571897
Diameter        13.360916
Height          11.826072
Whole_weight     9.247414
Shucked_weight -20.213913
```

```
Viscera_weight    -9.829675
Shell_weight       8.576242
dtype: float64
```

```
r^2= 0.5276299399919839
```

```
[9]: influence = fitted_model.get_influence()

H_diag = influence.hat_matrix_diag
print(H_diag)
```

```
[0.00089205 0.00076875 0.00072514 ... 0.00160134 0.00103437 0.0033281 ]
```

```
[10]: plt.bar(X.index, H_diag, width=10)
plt.xticks(df.index)
```

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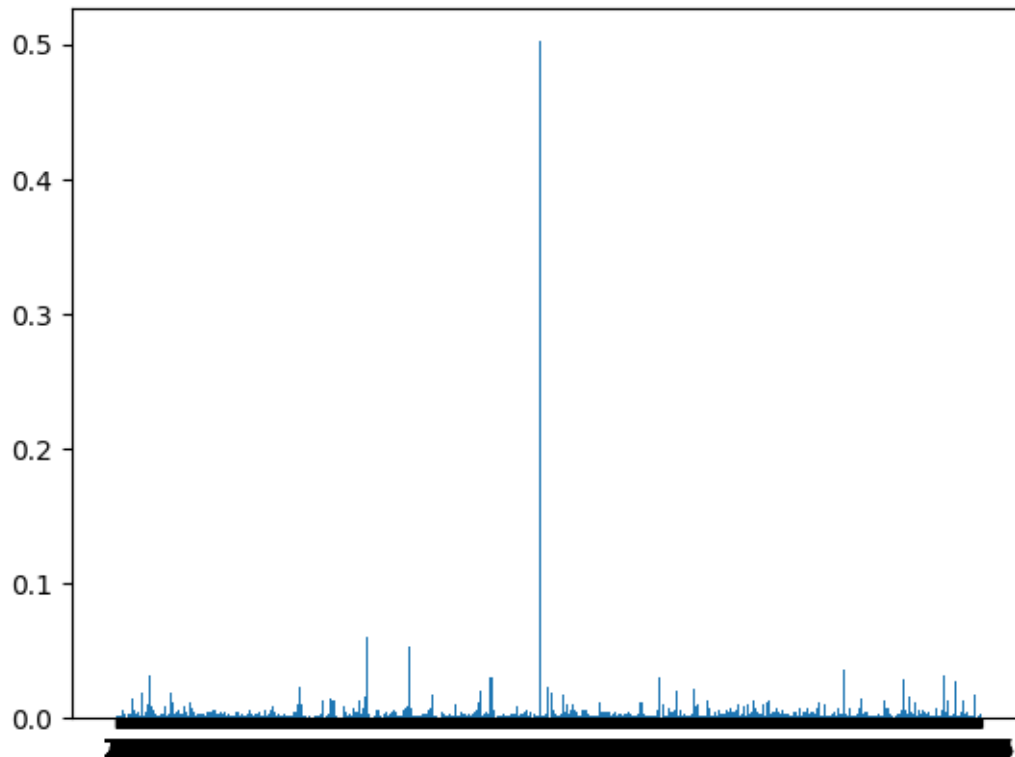
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```



```
[11]: mapping = sorted(list(enumerate(H_diag)),key = lambda item: item[1], reverse =
↳ True)
max_value_idx = [item[0] for item in mapping]

print('Top distances values')
print([item[1]for item in mapping][:3])

print('\nSample values with more leverage: \n')
print(df.iloc[max_value_idx])
```

Top distances values

[0.5019723528421322, 0.05960859244317343, 0.05295671927323318]

Sample values with more leverage:

	Rings	Length	Diameter	Height	Whole_weight	Shucked_weight	\
2051	8	0.455	0.355	1.130	0.5940	0.3320	
1210	6	0.185	0.375	0.120	0.4645	0.1960	
1417	10	0.705	0.565	0.515	2.2100	1.1075	
3518	11	0.710	0.570	0.195	1.3480	0.8985	
163	18	0.725	0.560	0.210	2.1410	0.6500	
...	...	...	...	...	...	...	

837	9	0.475	0.365	0.125	0.5465	0.2290
600	17	0.535	0.420	0.145	0.9260	0.3980
3555	8	0.535	0.415	0.135	0.7800	0.3165
2744	11	0.480	0.375	0.120	0.5895	0.2535
488	11	0.540	0.420	0.135	0.8075	0.3485

	Viscera_weight	Shell_weight
2051	0.1160	0.1335
1210	0.1045	0.1500
1417	0.4865	0.5120
3518	0.4435	0.4535
163	0.3980	1.0050
...	...	...
837	0.1185	0.1720
600	0.1965	0.2500
3555	0.1690	0.2365
2744	0.1280	0.1720
488	0.1795	0.2350

[4177 rows x 8 columns]

Distancia de Cook

```
[12]: np.set_printoptions(suppress=True)
      cooks_dist=influence.cooks_distance[0]
      summary_cooks = influence.summary_frame()

      mean_cooks = np.mean(cooks_dist)
      mean_cooks_list = [4*mean_cooks for _ in X.index]
      cooks_threshold = [4/len(cooks_dist) for _ in X.index]
```

Puntos influyentes

```
[13]: influencial_points = X.index[cooks_dist > 4/len(cooks_dist)]
      # print(influencial_points)
      X.iloc[influencial_points,:].head(10)
```

```
[13]:
```

	Length	Diameter	Height	Whole_weight	Shucked_weight	Viscera_weight	\
6	0.530	0.415	0.150	0.7775	0.2370	0.1415	
9	0.550	0.440	0.150	0.8945	0.3145	0.1510	
32	0.665	0.525	0.165	1.3380	0.5515	0.3575	
33	0.680	0.550	0.175	1.7980	0.8150	0.3925	
36	0.540	0.475	0.155	1.2170	0.5305	0.3075	
67	0.595	0.495	0.185	1.2850	0.4160	0.2240	
72	0.595	0.475	0.170	1.2470	0.4800	0.2250	
81	0.620	0.510	0.175	1.6150	0.5105	0.1920	
83	0.595	0.475	0.160	1.3175	0.4080	0.2340	
85	0.570	0.465	0.180	1.2950	0.3390	0.2225	

	Shell_weight
6	0.330
9	0.320
32	0.350
33	0.455
36	0.340
67	0.485
72	0.425
81	0.675
83	0.580
85	0.440

$r^2$  con los puntos influyentes

```
[14]: model_PI = sm.OLS(y.iloc[influencial_points,:],X.iloc[influencial_points,:])
      fitted_model_PI = model.fit()

      print(fitted_model_PI.params)
      print('\nr^2=', fitted_model_PI.rsquared)
```

```
const          2.985154
Length         -1.571897
Diameter       13.360916
Height        11.826072
Whole_weight    9.247414
Shucked_weight -20.213913
Viscera_weight -9.829675
Shell_weight    8.576242
dtype: float64
```

$r^2= 0.5276299399919839$

Outliers

Identificación de los Outliers

Detección usando Z-score

```
[15]: up_lim = X.mean() + 3*X.std()
      dw_lim = X.mean() - 3*X.std()
```

```
[16]: print("Upper limit:\n",up_lim)
      print("\nLower limit:\n",dw_lim)
```

```
Upper limit:
Length          0.884271
Diameter        0.705601
Height          0.264998
Whole_weight    2.299909
```



```

Shucked_weight    1.025256
Viscera_weight    0.509436
Shell_weight      0.656439
dtype: float64

Lower limit:
Length            0.163713
Diameter          0.110162
Height            0.014035
Whole_weight      -0.642425
Shucked_weight    -0.306521
Viscera_weight    -0.148249
Shell_weight      -0.178777
dtype: float64

```

```
[17]: print("Number of outlier Samples:\n",dw_lim)
```

```

Number of outlier Samples:
Length            0.163713
Diameter          0.110162
Height            0.014035
Whole_weight      -0.642425
Shucked_weight    -0.306521
Viscera_weight    -0.148249
Shell_weight      -0.178777
dtype: float64

```

Usando percentiles

```
[18]: Q1 = X.quantile(0.25)
      Q3 = X.quantile(0.75)
      iqr= Q3-Q1
```

```
[19]: print("Q1:",Q1)
      print("\nQ3:",Q3)
      print("\nIQR:",iqr)
```

```

Q1: Length            0.4500
Diameter              0.3500
Height                0.1150
Whole_weight          0.4415
Shucked_weight        0.1860
Viscera_weight         0.0935
Shell_weight          0.1300
Name: 0.25, dtype: float64

```

```

Q3: Length            0.615
Diameter              0.480

```

```

Height          0.165
Whole_weight    1.153
Shucked_weight  0.502
Viscera_weight  0.253
Shell_weight    0.329
Name: 0.75, dtype: float64

```

```

IQR: Length      0.1650
Diameter         0.1300
Height           0.0500
Whole_weight     0.7115
Shucked_weight   0.3160
Viscera_weight   0.1595
Shell_weight     0.1990
dtype: float64

```

```

[20]: outliers_iqr = (X<Q1 + 1.5 * iqr) | (X>Q3 + 1.5 * iqr)
      print("Number of outlier samples",X.to_numpy()[outliers_iqr].shape)

```

Number of outlier samples (27016,)

Manejo de Valores atípicos

Escalado min-max

```

[21]: scaler = MinMaxScaler(feature_range=(-1,1))
      scaler.fit(X)

```

```

[21]: MinMaxScaler(feature_range=(-1, 1))

```

```

[22]: print("Max Values:", scaler.data_max_)

      print("\nTransformation step:")
      mima = scaler.transform(X)
      print(mima)
      print(scaler.transform([[2,2,2,2,2,2,2]]))

```

Max Values: [0.815 0.65 1.13 2.8255 1.488 0.76 1.005 ]

Transformation step:

```

[[ 0.02702703  0.04201681 -0.83185841 ... -0.69939475 -0.73535221
  -0.70403587]
 [-0.25675676 -0.29411765 -0.84070796 ... -0.86751849 -0.87360105
  -0.86347783]
 [ 0.22972973  0.22689076 -0.76106195 ... -0.65635508 -0.62870309
  -0.58445441]
 ...
 [ 0.41891892  0.41176471 -0.63716814 ... -0.29455279 -0.24423963
  -0.38913802]

```

```
[ 0.48648649  0.44537815 -0.73451327 ... -0.28715535 -0.31402238
 -0.41305431]
[ 0.71621622  0.68067227 -0.65486726 ...  0.27034297 -0.00987492
 -0.01644245]]
[[4.2027027  5.53781513 2.53982301 0.41526474 1.68863484 4.26530612
 2.98305929]]
```

/usr/local/lib/python3.10/dist-packages/sklearn/base.py:439: UserWarning: X does not have valid feature names, but MinMaxScaler was fitted with feature names  
warnings.warn(

Calculo de  $r^2$  y parametros

```
[23]: model = sm.OLS(y,mima)
      fitted_model = model.fit()
      print(fitted_model.params)
      print('\nr^2=', fitted_model.rsquared)
```

```
x1      0.786716
x2      5.565116
x3     -6.575113
x4     19.150070
x5    -18.716406
x6     -5.580455
x7      1.790169
dtype: float64
```

$r^2=$  0.9518272060221903

Normalización Z-score

```
[24]: scaler = StandardScaler()

      scaler.fit(X)
```

[24]: StandardScaler()

```
[25]: print('Means:',scaler.mean_)
```

```
Means: [0.5239921  0.40788125 0.1395164  0.82874216 0.35936749 0.18059361
 0.23883086]
```

```
[26]: from matplotlib.colors import scale
      print('Transformation step:')
      zSc=scaler.transform(X)
      print(zSc, '\n')
      print(scaler.transform([[2,2,2,2,2,2,2]]))
```

Transformation step:

```
[[-0.57455813 -0.43214879 -1.06442415 ... -0.60768536 -0.72621157
```

```

-0.63821689]
[-1.44898585 -1.439929 -1.18397831 ... -1.17090984 -1.20522124
-1.21298732]
[ 0.05003309  0.12213032 -0.10799087 ... -0.4634999 -0.35668983
-0.20713907]
...
[ 0.6329849  0.67640943  1.56576738 ...  0.74855917  0.97541324
 0.49695471]
[ 0.84118198  0.77718745  0.25067161 ...  0.77334105  0.73362741
 0.41073914]
[ 1.54905203  1.48263359  1.32665906 ...  2.64099341  1.78744868
 1.84048058]]

[[12.2920211  16.04505753 44.48571086  2.38871187  7.39235509 16.60025239
 12.65334926]]

```

/usr/local/lib/python3.10/dist-packages/sklearn/base.py:439: UserWarning: X does not have valid feature names, but StandardScaler was fitted with feature names  
 warnings.warn(

Calculo de  $r^2$  y parametros|

```

[27]: model = sm.OLS(y,zSc)
      fitted_model = model.fit()
      print(fitted_model.params)
      print('\nr^2=', fitted_model.rsquared)

```

```

x1    -0.188751
x2     1.325777
x3     0.494591
x4     4.534288
x5    -4.486203
x6    -1.077344
x7     1.193693
dtype: float64

```

$r^2=$  0.05027502511352544

Winsorización

```

[28]: Q1 = np.quantile(X.to_numpy(),0.25)
      Q3 = np.quantile(X.to_numpy(),0.75)

      iqr = Q3-Q1

```

```

[29]: print("Q1:",Q1)
      print("Q1:",Q3)

```

```

Q1: 0.16
Q1: 0.505

```

```
[30]: from scipy.stats.mstats import winsorize

win = winsorize(X.to_numpy(), limits=[0.32,0.32])
print(win)
```

```
[[0.455  0.365  0.189  ... 0.2245 0.189  0.189 ]
 [0.35   0.265  0.189  ... 0.189  0.189  0.189 ]
 [0.455  0.42   0.189  ... 0.2565 0.189  0.21   ]
 ...
 [0.455  0.455  0.205  ... 0.455  0.2875 0.308 ]
 [0.455  0.455  0.189  ... 0.455  0.261  0.296 ]
 [0.455  0.455  0.195  ... 0.455  0.3765 0.455 ]]
```

Calculo de  $r^2$  y parametros

```
[31]: model = sm.OLS(y,win.data)
fitted_model = model.fit()
print(fitted_model.params)
print('\nr^2=', fitted_model.rsquared)
```

```
x1      0.518333
x2     20.942094
x3      0.693211
x4      4.122509
x5     -15.260867
x6     -11.043420
x7      27.230360
dtype: float64
```

```
r^2= 0.9487577149885722
```

### 0.0.3 3. Multicolinealidad en los datos usando VIF

```
[32]: from statsmodels.stats.outliers_influence import variance_inflation_factor
from statsmodels.tools.tools import add_constant

def compute_vif(cf):
    varIn = df[cf].copy()
    #Calculo de la inflación de la varianza requiere de una constante
    varIn['intercept'] = 1

    #VIF dataframe
    vif_data = pd.DataFrame()
    vif_data["feature"] = varIn.columns

    #Calculo de VIF por cada caracteristica
    vif_data["VIF"] = [variance_inflation_factor(varIn.values,i)
                       for i in range(len(varIn.columns))]
```

```
vif_data = vif_data[vif_data['feature']!='intercept']

return vif_data
```

Uso de la función VIF

```
[33]: wX = pd.DataFrame(win,columns = list(X.columns.to_numpy()))
```

```
[34]: considered_features = list(wX.columns.to_numpy())
nX = wX.copy()

model = sm.OLS(y,sm.add_constant(nX)).fit()

print(compute_vif(considered_features).sort_values('VIF',ascending=False))
print('\n')
print(model.summary())
```

	feature	VIF
3	Whole_weight	109.592750
1	Diameter	41.845452
0	Length	40.771813
4	Shucked_weight	28.353191
6	Shell_weight	21.258289
5	Viscera_weight	17.346276
2	Height	3.559939

```

                                OLS Regression Results
=====
Dep. Variable:                  Rings    R-squared:                  0.463
Model:                            OLS    Adj. R-squared:              0.462
Method:                 Least Squares    F-statistic:                 514.0
Date:                 Sat, 21 Oct 2023    Prob (F-statistic):          0.00
Time:                 01:23:45    Log-Likelihood:             -9516.8
No. Observations:                4177    AIC:                        1.905e+04
Df Residuals:                    4169    BIC:                        1.910e+04
Df Model:                          7
Covariance Type:                nonrobust
=====
==
                                coef    std err          t      P>|t|      [0.025
0.975]
-----
--
const                -2.7377         0.964     -2.841     0.005     -4.627
-0.848
Length                2.2228         2.004      1.109     0.267     -1.706

```

6.151					
Diameter	20.8108	2.215	9.394	0.000	16.468
25.154					
Height	13.3487	4.881	2.735	0.006	3.779
22.919					
Whole_weight	3.3972	1.188	2.859	0.004	1.068
5.727					
Shucked_weight	-15.0700	0.884	-17.046	0.000	-16.803
-13.337					
Viscera_weight	-11.2892	1.028	-10.987	0.000	-13.304
-9.275					
Shell_weight	26.9709	0.929	29.021	0.000	25.149
28.793					

Omnibus:	1117.735	Durbin-Watson:	1.206
Prob(Omnibus):	0.000	Jarque-Bera (JB):	3225.739
Skew:	1.391	Prob(JB):	0.00
Kurtosis:	6.285	Cond. No.	181.

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[35]: considered_features.remove('Whole_weight')
nX = nX.drop(['Whole_weight'],axis=1)

model = sm.OLS(y,sm.add_constant(nX)).fit()

print(compute_vif(considered_features).sort_values('VIF',ascending=False))
print('\n')
print(model.summary())
```

	feature	VIF
1	Diameter	41.819755
0	Length	40.763955
4	Viscera_weight	10.697780
3	Shucked_weight	8.852112
5	Shell_weight	7.817781
2	Height	3.558443

#### OLS Regression Results

Dep. Variable:	Rings	R-squared:	0.462
Model:	OLS	Adj. R-squared:	0.461
Method:	Least Squares	F-statistic:	597.3
Date:	Sat, 21 Oct 2023	Prob (F-statistic):	0.00

Time: 01:23:45 Log-Likelihood: -9520.9  
 No. Observations: 4177 AIC: 1.906e+04  
 Df Residuals: 4170 BIC: 1.910e+04  
 Df Model: 6  
 Covariance Type: nonrobust

```
=====
```

	coef	std err	t	P> t	[0.025
0.975]					
-----					
--					
const	-3.3298	0.942	-3.535	0.000	-5.177
-1.483					
Length	4.5740	1.829	2.501	0.012	0.989
8.159					
Diameter	23.4475	2.016	11.631	0.000	19.495
27.400					
Height	13.8661	4.882	2.840	0.005	4.294
23.438					
Shucked_weight	-15.2734	0.882	-17.317	0.000	-17.003
-13.544					
Viscera_weight	-11.2760	1.028	-10.964	0.000	-13.292
-9.260					
Shell_weight	26.6036	0.921	28.878	0.000	24.797
28.410					
=====					
Omnibus:	1127.035		Durbin-Watson:		1.206
Prob(Omnibus):	0.000		Jarque-Bera (JB):		3275.440
Skew:	1.400		Prob(JB):		0.00
Kurtosis:	6.314		Cond. No.		172.
=====					

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[36]: considered_features.remove('Diameter')
nX = nX.drop(['Diameter'],axis=1)

model = sm.OLS(y,sm.add_constant(nX)).fit()

print(compute_vif(considered_features).sort_values('VIF',ascending=False))
print('\n')
print(model.summary())
```

	feature	VIF
3	Viscera_weight	10.690504
2	Shucked_weight	8.851834



```

0      Length  8.013867
4      Shell_weight  7.457755
1      Height  3.509983

```

#### OLS Regression Results

```

=====
Dep. Variable:          Rings    R-squared:                0.445
Model:                  OLS      Adj. R-squared:            0.444
Method:                 Least Squares    F-statistic:        668.2
Date:                  Sat, 21 Oct 2023    Prob (F-statistic):    0.00
Time:                  01:23:45    Log-Likelihood:       -9587.5
No. Observations:      4177    AIC:                  1.919e+04
Df Residuals:          4171    BIC:                  1.923e+04
Df Model:               5
Covariance Type:       nonrobust
=====

```

```

==
               coef      std err          t      P>|t|      [0.025
0.975]
-----
--
const          -4.6910      0.950      -4.939      0.000      -6.553
-2.829
Length         23.6917      0.814     29.088      0.000      22.095
25.289
Height         11.4578      4.956       2.312      0.021       1.742
21.174
Shucked_weight -7.6681      0.601    -12.752      0.000      -8.847
-6.489
Viscera_weight -13.6299      1.024    -13.305      0.000     -15.638
-11.621
Shell_weight   29.5654      0.899     32.870      0.000      27.802
31.329
=====
Omnibus:                1093.642    Durbin-Watson:           1.152
Prob(Omnibus):           0.000    Jarque-Bera (JB):        3070.396
Skew:                    1.372    Prob(JB):                 0.00
Kurtosis:                6.180    Cond. No.                 164.
=====

```

#### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```

[37]: considered_features.remove('Length')
      nX = nX.drop(['Length'],axis=1)

```

```

model = sm.OLS(y,sm.add_constant(nX)).fit()

print(compute_vif(considered_features).sort_values('VIF',ascending=False))
print('\n')
print(model.summary())

```

	feature	VIF
2	Viscera_weight	10.334260
1	Shucked_weight	8.106113
3	Shell_weight	6.848921
0	Height	3.197236

#### OLS Regression Results

```

=====
Dep. Variable:          Rings    R-squared:                0.332
Model:                  OLS      Adj. R-squared:            0.331
Method:                 Least Squares    F-statistic:          518.7
Date:                   Sat, 21 Oct 2023    Prob (F-statistic):    0.00
Time:                   01:23:45    Log-Likelihood:       -9973.3
No. Observations:      4177    AIC:                  1.996e+04
Df Residuals:          4172    BIC:                  1.999e+04
Df Model:               4
Covariance Type:       nonrobust
=====

```

```

==

```

	coef	std err	t	P> t	[0.025
0.975]					
----					
--					
const	3.2827	0.997	3.292	0.001	1.328
5.238					
Height	14.1371	5.434	2.602	0.009	3.484
24.790					
Shucked_weight	-0.2183	0.597	-0.366	0.714	-1.388
0.951					
Viscera_weight	-16.5825	1.118	-14.834	0.000	-18.774
-14.391					
Shell_weight	29.3860	0.986	29.792	0.000	27.452
31.320					
=====					
Omnibus:	910.017		Durbin-Watson:	1.140	
Prob(Omnibus):	0.000		Jarque-Bera (JB):	2156.386	
Skew:	1.210		Prob(JB):	0.00	
Kurtosis:	5.557		Cond. No.	153.	
=====					

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[38]: considered_features.remove('Viscera_weight')
nX = nX.drop(['Viscera_weight'],axis=1)
model = sm.OLS(y,sm.add_constant(nX)).fit()

print(compute_vif(considered_features).sort_values('VIF',ascending=False))
print('\n')
print(model.summary())
```

	feature	VIF
2	Shell_weight	5.666451
1	Shucked_weight	4.709420
0	Height	3.135094

#### OLS Regression Results

```
=====
Dep. Variable:          Rings    R-squared:                0.297
Model:                  OLS      Adj. R-squared:            0.296
Method:                 Least Squares    F-statistic:          587.4
Date:                  Sat, 21 Oct 2023    Prob (F-statistic):      1.79e-318
Time:                  01:23:45    Log-Likelihood:         -10081.
No. Observations:      4177    AIC:                   2.017e+04
Df Residuals:          4173    BIC:                   2.019e+04
Df Model:               3
Covariance Type:       nonrobust
=====
```

```
=====
==
              coef    std err          t      P>|t|      [0.025
0.975]
-----
--
const          4.7281      1.018      4.644      0.000       2.732
6.724
Height         0.0058      5.488      0.001      0.999     -10.754
10.765
Shucked_weight -0.6651      0.611     -1.088      0.277      -1.864
0.533
Shell_weight   20.3517      0.796     25.568      0.000     18.791
21.912
=====
```

```
Omnibus:          978.523    Durbin-Watson:           1.036
Prob(Omnibus):    0.000    Jarque-Bera (JB):        2405.640
Skew:             1.282    Prob(JB):                0.00
Kurtosis:         5.692    Cond. No.                147.
```

=====

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[39]: from sklearn.metrics import mean_squared_error

nX = sm.add_constant(nX)
model = sm.OLS(y,nX).fit()

y_pred = model.predict(nX)

# Calcular el MSE
mse = mean_squared_error(y, y_pred)
print("Mean Squared Error:", mse)
```

Mean Squared Error: 7.307194346564264

- **¿Cómo cambio el valor de  $R^2$  del modelo? ¿A que se lo adjudica?**

El valor de  $R^2$  del modelo cambió a medida que se eliminaron variables independientes. En el modelo original, el valor de  $R^2$  era 0.9487577149885722, lo que indica que el modelo explicaba aproximadamente el 94.88% de la variabilidad en la variable dependiente (Rings).

A medida que se eliminaron variables, el valor de  $R^2$  disminuyó. Esto se debió a que al eliminar variables, se redujo la capacidad del modelo para explicar la variabilidad en los datos. En particular, la eliminación de variables redujo la cantidad de información disponible para predecir la variable dependiente, lo que llevó a una disminución en la capacidad predictiva del modelo.

- **¿Como cambiaron los coeficientes? ¿Qué se interpretación se puede obtener con los nuevos valores de coeficientes?**

A medida que se eliminaron variables independientes, los coeficientes del modelo cambiaron en el modelo de regresión lineal final con tres variables independientes:

La constante (intercepto) es 4.7281, representando el valor esperado de Rings cuando todas las variables independientes son cero.

El coeficiente de Height es 0.0058, lo que significa que un aumento de una unidad en Height se relaciona con un aumento de 0.0058 en el valor esperado de Rings, manteniendo otras variables constantes.

El coeficiente de Shucked\_weight es -0.6651, lo que indica que un aumento de una unidad en Shucked\_weight se asocia con una disminución de 0.6651 en el valor esperado de Rings, manteniendo las demás variables constantes.

El coeficiente de Shell\_weight es 20.3517, lo que significa que un aumento de una unidad en Shell\_weight se asocia con un aumento de 20.3517 en el valor esperado de Rings, manteniendo otras variables constantes.

El modelo final es más simple al eliminar variables con multicolinealidad y otros factores que reducían la capacidad de predicción. Sin embargo, la capacidad de explicar la variabilidad en los

datos disminuyó en comparación con el modelo original.

#### 0.0.4 4. Analisis de componenetes principales

```
[40]: from sklearn.decomposition import PCA

# Crear una instancia de PCA
pca = PCA()

# Ajustar PCA a tus datos
pca.fit(X)

# Obtener los valores propios (explained variances) ordenados
explained_variances = pca.explained_variance_ratio_

# Calcular la varianza explicada acumulativa
cumulative_explained_variances = np.cumsum(explained_variances)

# Establecer el umbral deseado (por ejemplo, 0.90 para retener el 90% de la
    ↪varianza)
desired_variance = 0.90

# Encontrar el número de componentes necesarios
num_components_needed = np.argmax(cumulative_explained_variances >=
    ↪desired_variance) + 1

print(f"Número de componentes necesarios para retener {desired_variance * 100:.
    ↪2f}% de la varianza: {num_components_needed}")
```

Número de componentes necesarios para retener 90.00% de la varianza: 1

```
[41]: # Calcular r^2
model = sm.OLS(y,win.data)
fitted_model = model.fit()
print('\nr^2=', fitted_model.rsquared)
```

r^2= 0.9487577149885722

```
[42]: # Calcular el MSE
mse = fitted_model.mse_resid
print(f'Mean Squared Error (MSE): {mse:.2f}')
```

Mean Squared Error (MSE): 5.60

- ¿Mejoro el valor de  $R^2$  y MSE del modelo PCR respecto al metodo de VIF?¿A que se lo adjudica?

El modelo PCR (Análisis de Componentes Principales) tiene un mejor desempeño en comparación

con el método de eliminación de variables VIF en términos de  $R^2$  y MSE. El  $R^2$  del modelo PCR es más alto (0.9488) en comparación con el modelo después de eliminar variables con VIF alto (0.445), lo que indica una mejor capacidad de explicación de la variabilidad en los datos. Además, el MSE del modelo PCR es más bajo (5.60) en comparación con el MSE del modelo después de la eliminación de variables con VIF alto (7.307), lo que señala un mejor ajuste del modelo a los datos. Esta mejora podría atribuirse al uso de componentes principales que capturan la información relevante de las variables originales, lo que puede reducir la multicolinealidad y mejorar el rendimiento del modelo.