Stacks and Queues

Stack: Abstract data type with the following operations:

■ Push (Key): adds key to collection

- Push (Key): adds key to collection
- Key Top(): returns most recently-added key

- Push (Key): adds key to collection
- Key Top(): returns most recently-added key
- Key Pop(): removes and returns most recently-added key

- Push (Key): adds key to collection
- Key Top(): returns most recently-added key
- Key Pop(): removes and returns most recently-added key
- Boolean Empty(): are there any elements?

Balanced Brackets

Input: A string str consisting of ((', ')', '[', ']')'l' characters.

Output: Return whether or not the string's parentheses and square brackets are balanced.

Balanced Brackets

```
Balanced:
```

```
"([])[]()",
"((([([])]))())"
```

Unbalanced:

```
- "(\Barrier)
```

"["

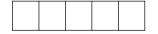
IsBalanced(str)

```
Stack stack
for char in str:
  if char in [ '(', '[']:
    stack.Push(char)
  else:
    if stack.Empty(): return False
    top \leftarrow stack.Pop()
    if (top = '[ 'and char != ']') or
       (top = '( 'and char != ')' ):
      return False
return stack.Empty()
```

numElements: 0

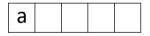


numElements: 0



Push (a)

numElements: 1



Push (a)

numElements: 1



numElements: 1

a

Push(b)

numElements: 2

a b

Push(b)

numElements: 2

a b

numElements: 2

a b

Top()

numElements: 2

 $Top() \rightarrow b$

numElements: 2

a b

numElements: 2

ab

Push(c)

numElements: 3

a b c

Push (c)

numElements: 3

a b c

numElements: 3

a b c

Pop()

numElements: 2

$$Pop() \rightarrow c$$

numElements: 2

a b

numElements: 2

ab

Push (d)

numElements: 3

a b d

Push (d)

numElements: 3

a b d

numElements: 3

a b d

Push (e)

numElements: 4

a b d e

Push (e)

numElements: 4

a b d e

numElements: 4

a b d e

Push (f)

numElements: 5

a b d e f

Push (f)

numElements: 5

a | b | d | e | f

numElements: 5

a b d e f

Push (g)

numElements: 5

a b d e f

 $Push(g) \rightarrow ERROR$

numElements: 5

a | b | d | e | f

numElements: 5

a b d e f

Empty()

numElements: 5

a b d e f

 $Empty() \rightarrow False$

numElements: 5

a | b | d | e | f

numElements: 5

a b d e f

Pop()

numElements: 4

$$Pop() \rightarrow f$$

numElements: 4

a b d e

numElements: 4

a b d e

Pop()

numElements: 3

 $Pop() \rightarrow e$

numElements: 3

a b d

numElements: 3

a b d

Pop()

numElements: 2

 $Pop() \rightarrow d$

numElements: 2

a b

numElements: 2

a b

Pop()

numElements: 1

 $Pop() \rightarrow b$

numElements: 1

a

numElements: 1

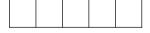
a

Pop()

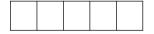
numElements: 0

 $Pop() \rightarrow a$

numElements: 0



numElements: 0



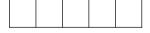
Empty()

numElements: 0



 $Empty() \rightarrow True$

numElements: 0



head

head



Push (a)





Push (b)



Push (b)



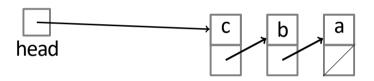




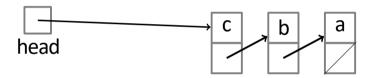


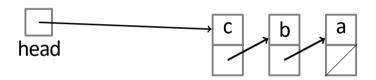


Push (c)



Push (c)



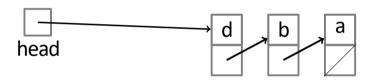




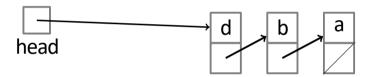


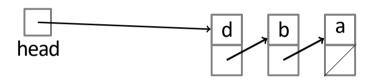


Push (d)

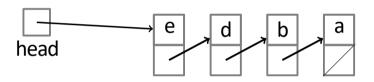


Push (d)

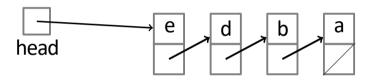


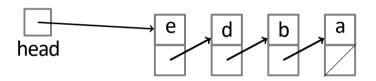


Push (e)

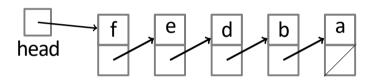


Push (e)

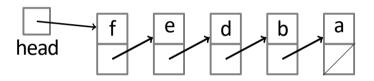


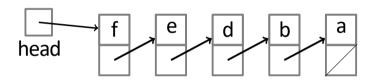


Push(f)

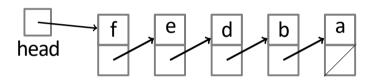


Push(f)

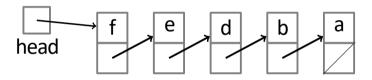


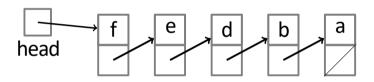


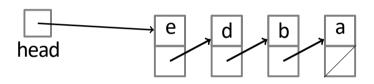
Empty()

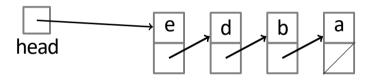


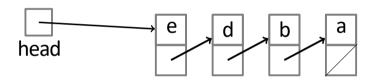
 $Empty() \rightarrow False$

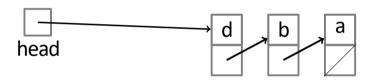


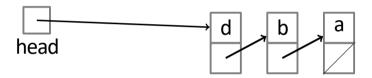


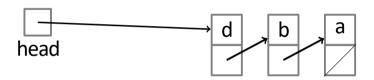
























head



head

head

 $Empty() \rightarrow True$

head

Stack Implementation with

Linked List

Stack Implementation with

Linked List

Stack Implementation with

Linked List

Summary

Stacks can be implemented with either an array or a linked list.

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- Each stack operation is O(1): Push, Pop, Top, Empty.

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- Stacks can be implemented with either an array or a linked list.
- Each stack operation is O(1): Push, Pop, Top, Empty.
- Stacks are ocassionaly known as LIFO queues.

Queues

Queue: Abstract data type with the following operations:

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- Enqueue (Key): adds key to collection
 - Key Dequeue(): removes and returns least recently-added key
- Boolean Empty(): are there any elements?

FIFO: First-In, First-Out

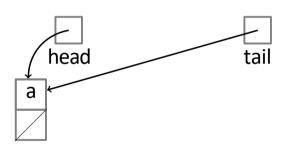
head



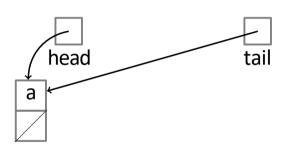
head

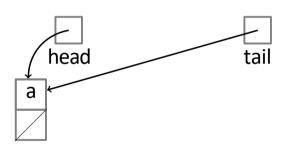
tail

Enqueue (a)

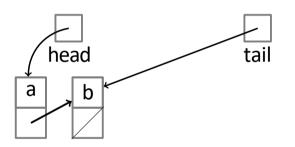


Enqueue (a)

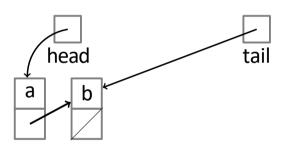


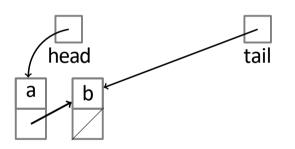


Enqueue (b)

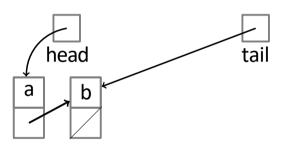


Enqueue (b)

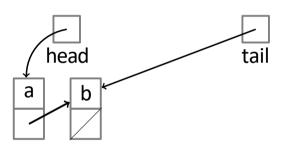


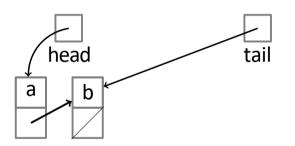


Empty()

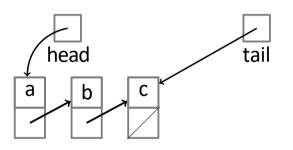


 $Empty() \rightarrow False$

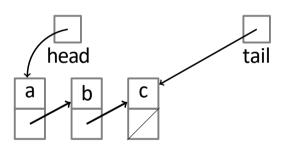


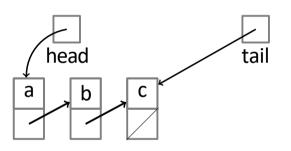


Enqueue (c)

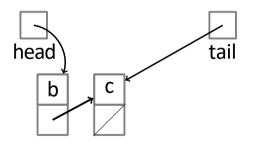


Enqueue (c)

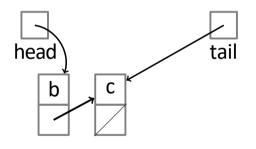


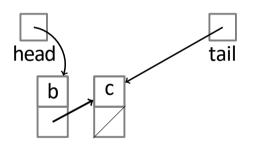


Dequeue ()

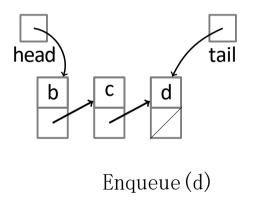


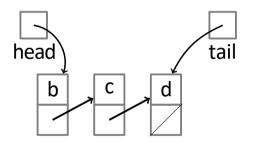
Dequeue () \rightarrow a

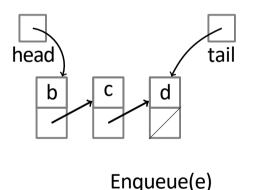


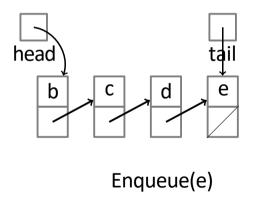


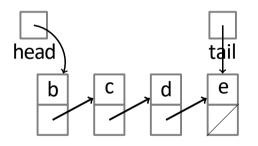
Enqueue (d)

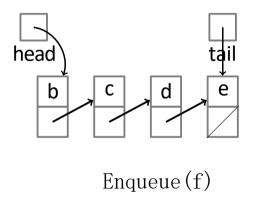


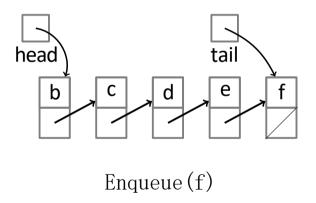


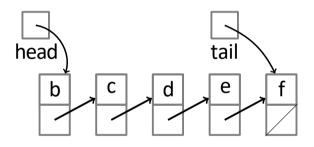


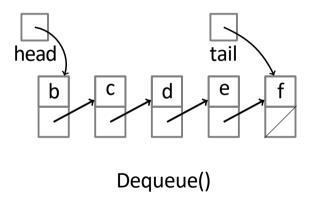


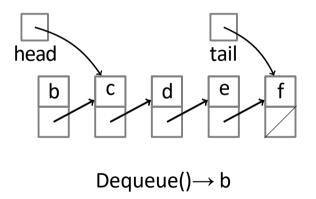


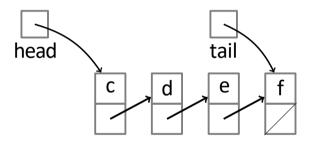


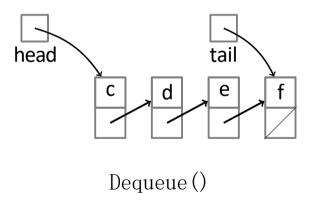


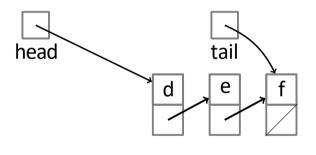




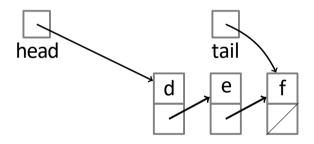


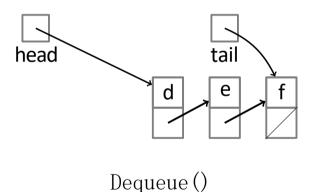


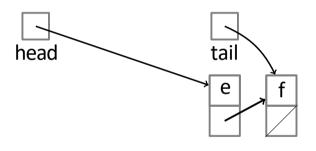




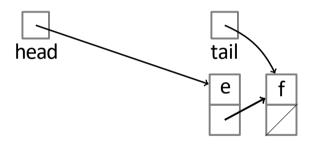
Dequeue () \rightarrow c

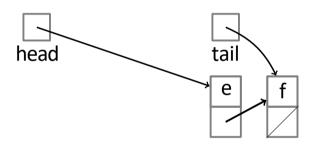




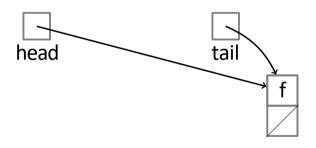


Dequeue () \rightarrow d

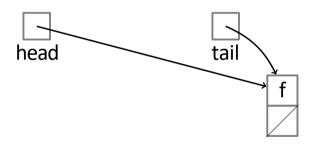


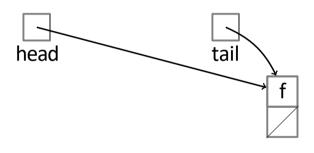


Dequeue ()



Dequeue () \rightarrow e





Dequeue ()





Dequeue () \rightarrow f

head



head

____ tail

Empty()

head



Empty() → True

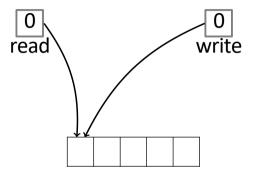
head

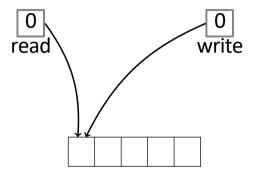


■ Enqueue: use List. PushBack

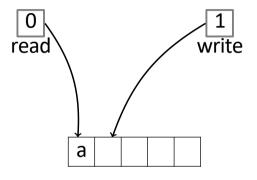
- Enqueue: use List. PushBack
- Dequeue: use List. TopFront and List. PopFront

- Enqueue: use List. PushBack
- Dequeue: use List. TopFront and List. PopFront
- Empty: use List. Empty

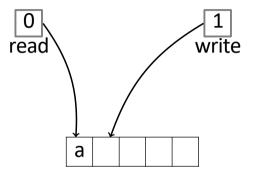


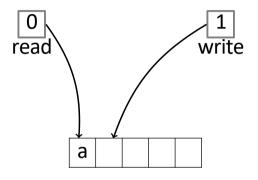


Enqueue(a)

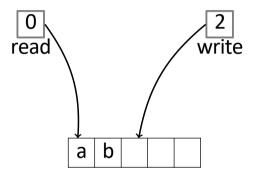


Enqueue(a)

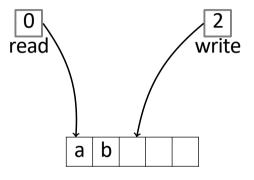


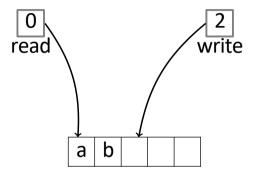


Enqueue (b)

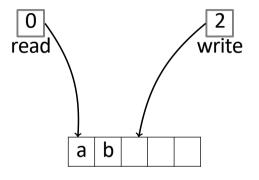


Enqueue (b)

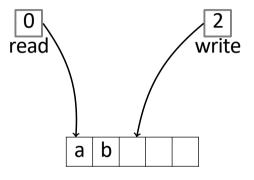


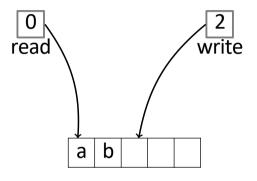


Empty()

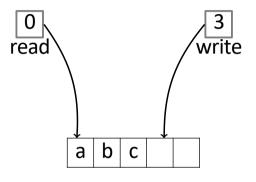


 $Empty() \rightarrow False$

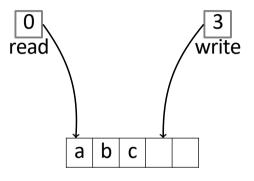


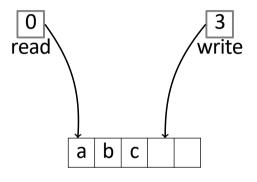


Enqueue (c)

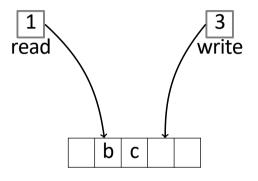


Enqueue (c)

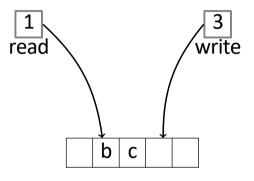


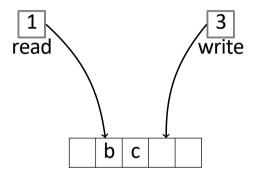


Dequeue ()

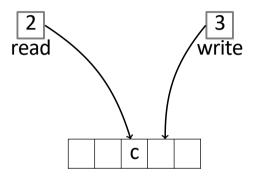


Dequeue () \rightarrow a

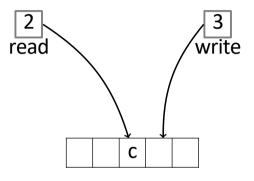


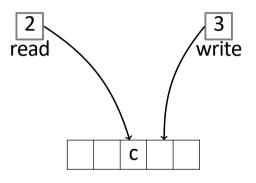


Dequeue ()

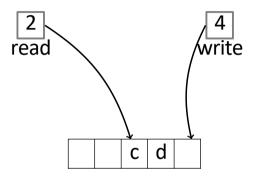


Dequeue () \rightarrow b

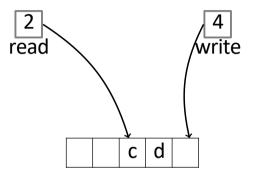


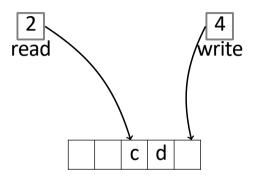


Enqueue (d)

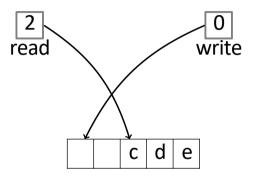


Enqueue (d)

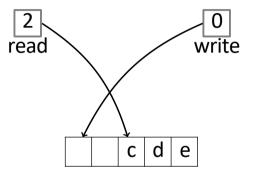


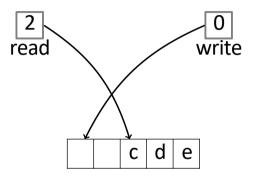


Enqueue (e)

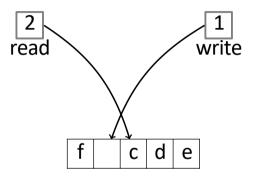


Enqueue (e)

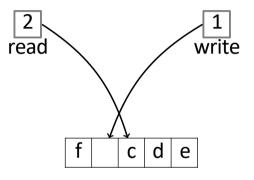


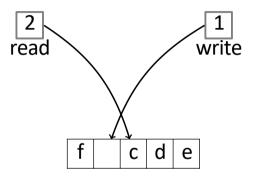


Enqueue (f)

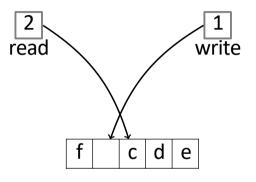


Enqueue (f)

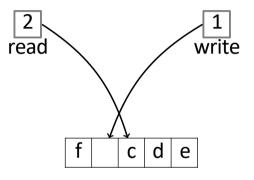


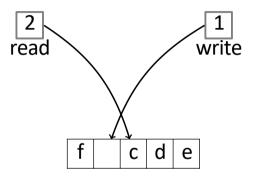


Enqueue (g)

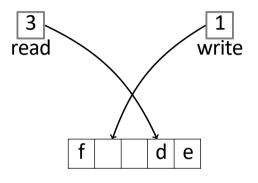


Enqueue $(g) \rightarrow ERROR$

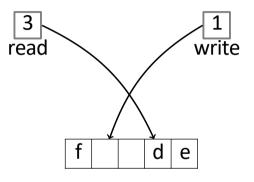


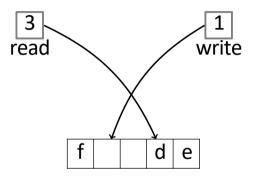


Dequeue ()

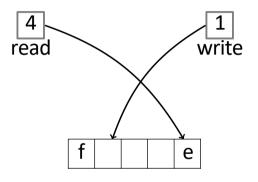


Dequeue () \rightarrow c

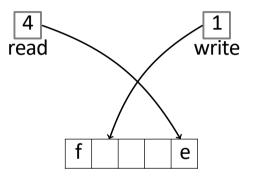


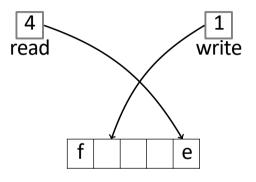


Dequeue ()

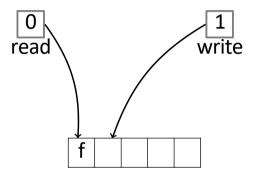


Dequeue () \rightarrow d

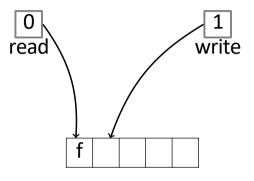


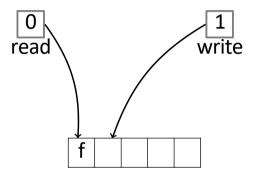


Dequeue ()

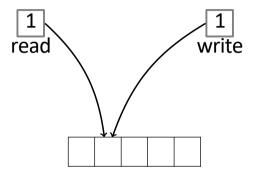


Dequeue () \rightarrow e

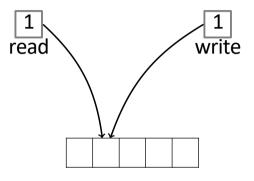


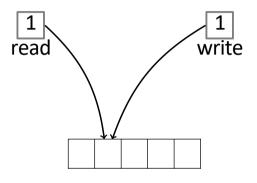


Dequeue ()

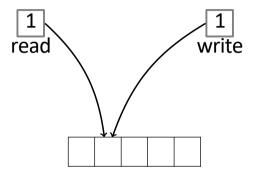


Dequeue () \rightarrow f





Empty()



 $Empty() \rightarrow True$

Summary

Summary

 Queues can be implemented with either a linked list (with tail pointer) or an array.

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- Queues can be implemented with either a linked list (with tail pointer) or an array.
- Each queue operation is O(1): Enqueue, Dequeue, Empty.