







# Exercises Sheet

## Sizing and Probabilities

Systems Configuration and Management  
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1. A router handles 100 packets per second and the processing time of each packet is 2ms. What is the router utilization? 
2. A new VoIP system is composed of multiple IP-PBX devices. IP-PBX can have at most 4 pending requests and the average delay of each request is 50ms. How many IP-PBX devices will be required to handle 500 calls per second? 
3. Consider a cache placed in front of a web server. The system receives 60 requests/s. The cache is able to reply on average to 80% of the requests.
  - (a) How many requests are handled by the cache and how many are handled by the web server? 
  - (b) Assume instead that a load balancer equally distributes the load to 3 replicas of the cache. How many requests are handled by each component? 
  - (c) Finally assume that only a cache exists and the load balancer is placed between the cache and 3 replicas of the web server. How many requests are handled by each component in this case? 
4. A company is planning a web site that must be able to cope with 100 requests/s and a variance of more or less 30 requests/s. Which hardware option is cheaper?
  - (a) A load balancer that can handle 500 requests/s (cost 2000) and small servers that can handle 50 requests/s each (cost of each: 2000);
  - (b) A unique server (cost 8000); 

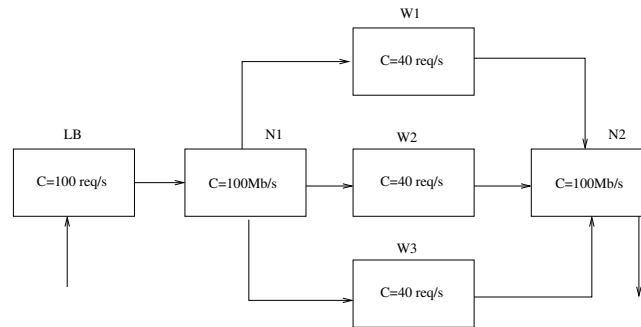


Figure 1:

5. Consider the system depicted in Fig. 1 and assume that 60 requests/s are received. Each request uses a 1Kb packet and replies have on average 100Kb. Finally, assume that the system's flow can be modeled using M/M/1 queues.
  - (a) What is the average delay of each request?
  - (b) How many requests will be at the Load Balancer and Web Server?
  - (c) Repeat your calculations considering that replies are routed through N1 and LB.
6. Assuming that the probability of failure of the components in the network of Fig. 1 is  $10^{-4}$  for the web servers,  $10^{-6}$  for network components and  $10^{-5}$  for the load balancer, determine:
  - (a) the probability of the system being correct
  - (b) discuss the scenarios in which the system will operate in degraded mode
  - (c) discuss approaches to increase system reliability. Would a combination of 2 LB and 2 WS increase or decrease system reliability?

## Formulas

**Queues M/M/1** For an arrival rate  $\lambda$  and service rate  $\mu$ :

**utilization**  $\rho = \frac{\lambda}{\mu}$

**average delay**  $\frac{1}{\mu(1-\rho)}, \rho < 1$

**requests in system**  $\frac{\rho}{1-\rho}, \rho < 1$