Convergence

P₁ close to ring:

```
circloopel.m × circloopel_plot.m × +
            clear all
     2
            close all
            format long
     3
     4
     5
            R=10;
     6
            M=10;
     7
     8
            rP=10;
     9
            phiP=pi/6;
    10
            zP=0.1;
    11
    12
            [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
    13
            Er=sqrt(Ex^2+Ey^2)
   Command Window
   New to MATLAB? See resources for Getting Started.
        0.006282242947179
     >> circloopel plot
     Ex =
        3.227722117712293
     Ey =
       -4.506377564176808
     Ez =
        0.548066268007510
     Er =
        5.543070342336026
```

```
circloopel.m × circloopel_plot.m × +
            clear all
     2
            close all
     3 M
            format long
     4
     5
           R=10;
            M=100;
     6
     7
     8
            rP=10;
     9
            phiP=pi/6;
    10
            zP=0.1;
    11
            [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
    12
    13
            Er=sqrt(Ex^2+Ey^2)
   Command Window
   New to MATLAB? See resources for Getting Started.
        0.006282242947179
     >> circloopel plot
     Ex =
       -3.322267220677585
     Ey =
        6.935259995671693
     Ez =
        6.033320001230522
     Er =
        7.689947379088682
```

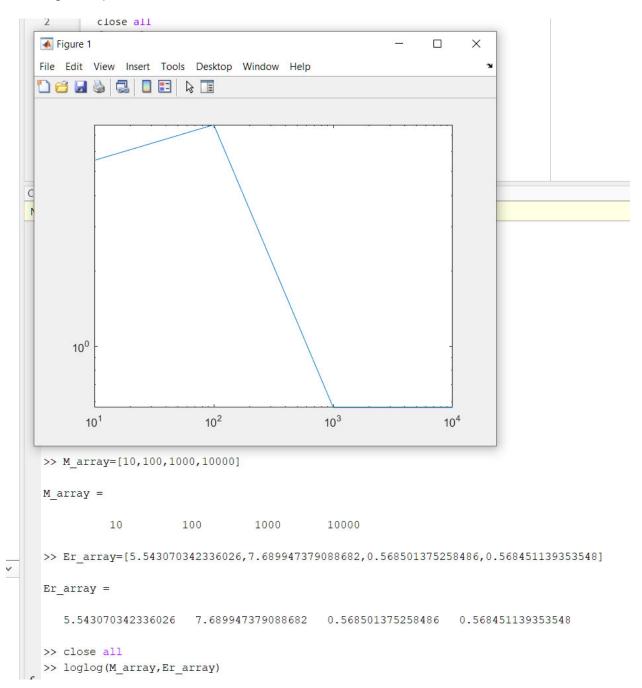
```
circloopel.m × circloopel_plot.m × +
     1
            clear all
     2
            close all
     3
            format long
     4
     5
            R=10;
     6
            M=1000;
     7
     8
            rP=10;
     9
            phiP=pi/6;
    10
            zP=0.1;
    11
            [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
    12
    13
            Er=sqrt(Ex^2+Ey^2)
   Command Window
   New to MATLAB? See resources for Getting Started.
        0.006282242947179
     >> circloopel plot
     Ex =
        0.489228233498501
     Ey =
        0.289567866343497
     Ez =
       19.997566035457115
     Er =
        0.568501375258486
```

```
© Z Editor - D:\OneDrive - University of Waterloo\Matteo_D\MATLABDrive\PHYS242_EM01\circloopel_plot.m
   circloopel.m × circloopel_plot.m × +
               clear all
      2
                close all
                format long
      3
      4
      5
              R=10;
               M=10000;
      6
      7
      8
               rP=10;
      9
               phiP=pi/6;
     10
               zP=0.1;
     11
     12
                [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
                Er=sqrt(Ex^2+Ey^2)
     13
   Command Window
    New to MATLAB? See resources for Getting Started.
          0.006282242947179
      >> circloopel_plot
      Ex =
          0.492293127491485
      Ey =
          0.284225569674862
      Ez =
         20.001296115891442
```

Er =

0.568451139353548

convergence plot P₁:

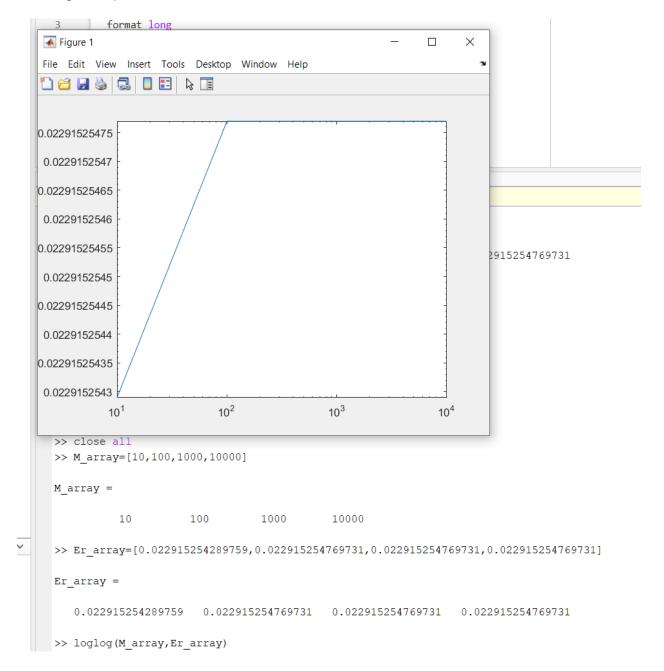


P₂ far way:

```
© Z Editor - D:\OneDrive - University of Waterloo\Matteo_D\MATLABDrive\PHYS242_EM01\circloopel_plot.m
       circloopel_m × circloopel_plot.m ×
                clear all
       1
                close all
       2
                format long
       3
       4
       5
                R=10;
       6
                M=10;
       7
       8
                rP=10;
       9
                phiP=0;
      10
                zP=25;
      11
      12
                [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
                Er=sqrt(Ex^2+Ey^2)
      13
   Command Window
    New to MATLAB? See resources for Getting Started.
          0.080466084168676
      >> circloopel plot
      Ex =
          0.022915254289759
      Ey =
           -8.673617379884035e-19
      Ez =
          0.070165268110281
       Er =
          0.022915254289759
```

and similarly for M=100, 1000, 10000

convergence plot P2:



Comparison with analytical result on z axis:

```
Z Editor - D:\OneDrive - University of Waterloo\Matteo_D\MATLABDrive\PHYS242_EM01\circloopel_plot.m
   circloopel_m × circloopel_plot.m × +
            clear all
   2
            close all
            format long
   3
   4
   5
            R=10;
   6
            M=100;
   7
   8
            rP=0;
   9
            phiP=0;
  10
            zP=0;
  11
  12
            [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
  13
            Er=sqrt(Ex^2+Ey^2)
            Ez_{anal=2*pi*R*zP/(R^2+zP^2)^(3/2)}
  14
  15
            %
Command Window
New to MATLAB? See resources for Getting Started.
   >> circloopel plot
   Ex =
        -9.454242944073599e-17
   Ey =
        -1.951563910473908e-17
   Ez =
         0
   Er =
         9.653564696122859e-17
   Ez anal =
         0
```

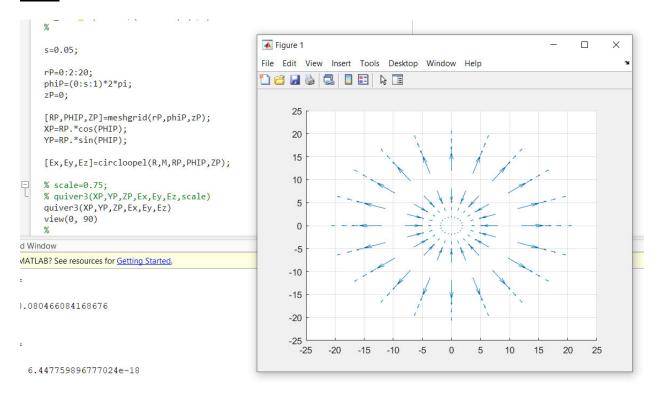
```
circloopel.m × circloopel_plot.m × +
            clear all
            close all
     2
     3
            format long
     4
     5
            R=10;
     6
            M=100;
     7
            rP=0;
     8
     9
            phiP=0;
    10
            zP=25;
    11
    12
            [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
    13
            Er=sqrt(Ex^2+Ey^2)
    14
            Ez_{anal=2*pi*R*zP/(R^2+zP^2)^(3/2)}
    15
   Command Window
   New to MATLAB? See resources for Getting Started.
     >> circloopel plot
     Ex =
         -5.095750210681871e-18
     Ey =
         -3.950561665994057e-18
     Ez =
        0.080466084168676
     Er =
```

6.447759896777024e-18

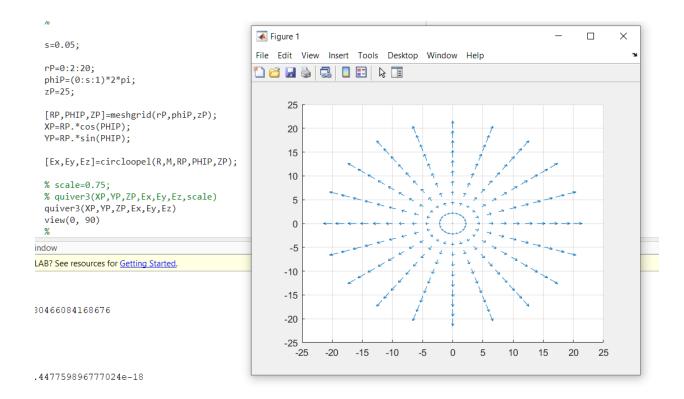
0.080466084168676

Ez anal =

Plots



ring "visible" where arrows are missing arrows point away from ring arrows are symmetric with respect to z axis



CODE:

```
function [Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
% ,phiQ_vec
% Ke=\lambda/(4*pi*epsilon0)=1;
% R=10;
% M=100;
Delta phi=2*pi/M;
Delta_ell=R*Delta_phi;
% rP=0;
% phiP=0;
% zP=0.1;
m=0;
phiQ=0;
DeltaEx=0;
Ex=0;
DeltaEy=0;
Ey=0;
DeltaEz=0;
Ez=0;
for m=1:M
    phiQ=-Delta_phi+m*Delta_phi;
    % phiQ_vec(m)=phiQ;
    DeltaEx=Delta ell*(rP.*cos(phiP)-R*cos(phiQ))./(rP.^2+R^2-2*R*rP.*cos(phiQ-
phiP)+zP.^2).^(3/2);
    Ex=Ex+DeltaEx;
    DeltaEy=Delta_ell*(rP.*sin(phiP)-R*sin(phiQ))./(rP.^2+R^2-2*R*rP.*cos(phiQ-
phiP)+zP.^2).^(3/2);
    Ey=Ey+DeltaEy;
    DeltaEz=Delta ell*zP./(rP.^2+R^2-2*R*rP.*cos(phiQ-phiP)+zP.^2).^(3/2);
    Ez=Ez+DeltaEz;
end
end
% DDD
clear all
close all
format long
R=10;
M=100;
```

```
rP=0;
phiP=0;
zP=25;
[Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
Er=sqrt(Ex^2+Ey^2)
Ez_anal=2*pi*R*zP/(R^2+zP^2)^(3/2)
s=0.05;
rP=0:2:20;
phiP=(0:s:1)*2*pi;
zP=25;
[RP,PHIP,ZP]=meshgrid(rP,phiP,zP);
XP=RP.*cos(PHIP);
YP=RP.*sin(PHIP);
[Ex,Ey,Ez]=circloopel(R,M,RP,PHIP,ZP);
% scale=0.75;
% quiver3(XP,YP,ZP,Ex,Ey,Ez,scale)
quiver3(XP,YP,ZP,Ex,Ey,Ez)
view(0,90)
% DDD
```

OLD CODE:

```
clear all
close all
format long
R=10;
M=10; % 20
rP=15;
phiP=pi/6;
zP=20;
[Ex,Ey,Ez]=circloopel(R,M,rP,phiP,zP)
Er=sqrt(Ex^2+Ey^2)
Ez anal=2*pi*R*zP/(R^2+zP^2)^(3/2)
% rP=0;
% phiP=pi;
% zP=20; % 9; 20; 0
s=0.05; % 0.01
% rP=(0:s:1)*20; % 15
rP=0:2:20;
% phiP=[0:2*pi/s:2*pi];
phiP=(0:s:1)*2*pi;
zP=0; % 1; 25
% [XP,YP,ZP]=meshgrid(rP.*cos(phiP),rP.*sin(phiP),zP);
[RP,PHIP,ZP]=meshgrid(rP,phiP,zP);
XP=RP.*cos(PHIP);
YP=RP.*sin(PHIP);
% [Bx,By,Bz] = circloopmag(R,M,rP,phiP,zP);
[Ex,Ey,Ez]=circloopel(R,M,RP,PHIP,ZP);
% [BX,BY,BZ]=meshgrid(Bx,By,Bz);
% Br=sqrt(Bx.^2+By.^2);
% Bphi=zeros(1,length(Br));
% scale=0.75;
% quiver3(XP,YP,ZP,Ex,Ey,Ez,scale)
% quiver3(XP,YP,ZP,Bx',By',Bz')
quiver3(XP,YP,ZP,Ex,Ey,Ez)
% view(0, 90)
```