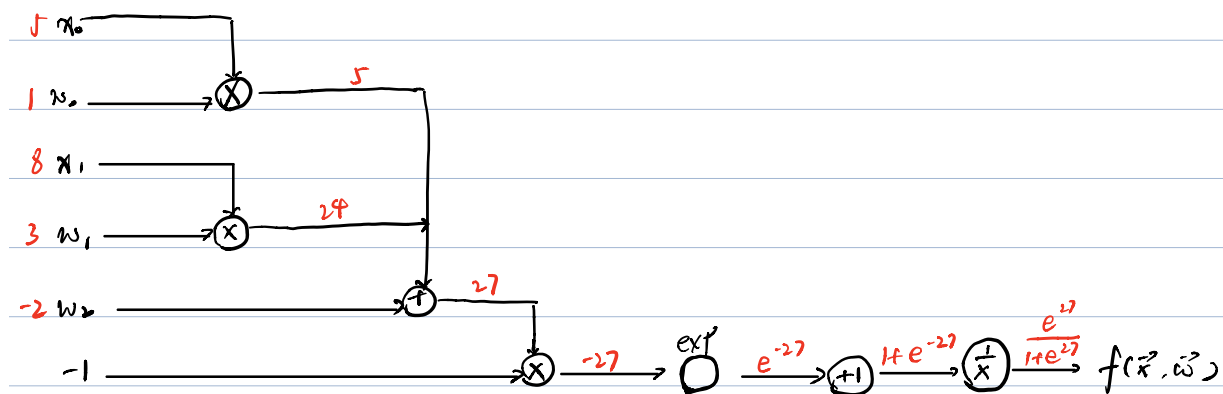


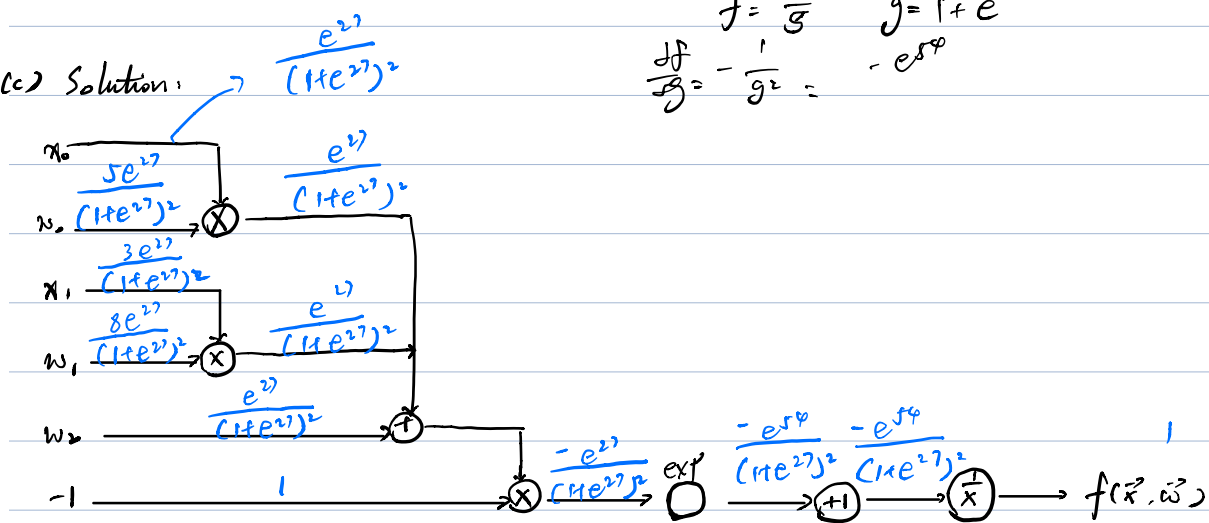
(a) Solution:



(b) Solution:

The solution of this problem is shown with red letters in (a).

(c) Solution:



$$f = \frac{1}{g} \quad g = 1 + e^{-27}$$

$$\frac{df}{dg} = -\frac{1}{g^2} = -\frac{1}{e^{54}}$$

(d) Proof, $\frac{d\sigma(x)}{dx} = -\frac{e^{-x}}{(1+e^{-x})^2} = \frac{e^{-x}}{(1+e^{-x})^2}$

$$(1-\sigma(x))\sigma(x) = \frac{1}{1+e^{-x}} \cdot \frac{e^{-x}}{1+e^{-x}} = \frac{e^{-x}}{(1+e^{-x})^2} = \frac{d\sigma(x)}{dx} \quad \text{QED}$$

(e) Solution: $\frac{e^{-2t}}{(1+e^{-2t})^2}$

