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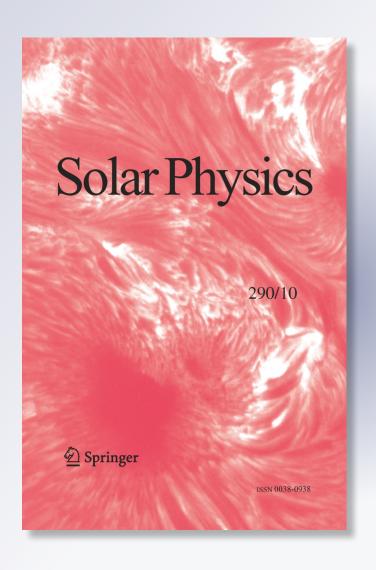
P. Kaufmann

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# Origin of the 30 THz Emission Detected During the Solar Flare on 2012 March 13 at 17:20 UT

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**Abstract** Solar observations in the infrared domain can bring important clues on the response of the low solar atmosphere to primary energy released during flares. At present, the infrared continuum has been detected at 30 THz (10 µm) in only a few flares. SOL2012-03-13, which is one of these flares, has been presented and discussed in Kaufmann *et al.* (*Astrophys. J.* **768**, 134, 2013). No firm conclusions were drawn on the origin of the mid-infrared radiation. In this work we present a detailed multi-frequency analysis of the SOL2012-03-13 event, including observations at radio-millimeter and submillimeter wavelengths, in

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hard X-rays (HXR), gamma-rays (GR), Hα, and white light. The HXR/GR spectral analysis shows that SOL2012-03-13 is a GR line flare and allows estimating the numbers of and energy contents in electrons, protons, and  $\alpha$  particles produced during the flare. The energy spectrum of the electrons producing the HXR/GR continuum is consistent with a broken power-law with an energy break at  $\sim 800$  keV. We show that the high-energy part (above  $\sim 800 \text{ keV}$ ) of this distribution is responsible for the high-frequency radio emission (> 20 GHz) detected during the flare. By comparing the 30 THz emission expected from semi-empirical and time-independent models of the quiet and flare atmospheres, we find that most ( $\sim 80\%$ ) of the observed 30 THz radiation can be attributed to thermal free-free emission of an optically thin source. Using the F2 flare atmospheric model (Machado et al. in Astrophys. J. 242, 336, 1980), this thin source is found to be at temperatures  $T \sim 8000 \text{ K}$ and is located well above the minimum temperature region. We argue that the chromospheric heating, which results in 80 % of the 30 THz excess radiation, can be due to energy deposition by nonthermal flare-accelerated electrons, protons, and  $\alpha$  particles. The remaining 20 % of the 30 THz excess emission is found to be radiated from an optically thick atmospheric layer at  $T \sim 5000$  K, below the temperature minimum region, where direct heating by nonthermal particles is insufficient to account for the observed infrared radiation.

**Keywords** Radio bursts, microwave · X-ray bursts, association with flares · X-ray burst, spectrum · Chromosphere, models · Heating, chromospheric · Heating, in flares

#### 1. Introduction

Solar flare continuum observations from the mid-infrared domain (a few tens of THz) to the millimeter-to-submillimeter radio domain in principle provide unique diagnostics of energy transport processes from the flare energy release region to the chromosphere and of the most energetic flare-accelerated particles (e.g. Trottet and Klein, 2013, and references therein). Since 2000, radio observations at 212 and 405 GHz have been routinely obtained by the Solar Submillimeter Telescope (SST), and more recently, high-cadence imaging observations of both the quiet Sun and flares have been obtained at 30 THz (Kaufmann et al., 2008, and references therein). The flare on 2012 March 13 at  $\sim$  17:22 UT (SOL2012-03-13) was the first flare observed at 30 THz (Kaufmann et al., 2013). Since then, other flares detected at 30 THz have been reported in the literature (Kaufmann et al., 2015, and references therein). During SOL2012-03-13 the time evolution of the 30 THz impulsive emission was found to be similar to that of the radio (1-212 GHz), hard X-ray, and white-light emission. The 30 THz emitting source was also cospatial with a region of flare-enhanced white-light continuum. No firm conclusion on the origin of the 30 THz infrared emission observed during SOL2012-03-13 was drawn by Kaufmann et al. (2013). Nevertheless, the authors suggested that it is consistent with heating of the flaring atmosphere below the temperature minimum region, which cannot be due to direct heating by hard X-ray emitting electrons, at least within the classic thick-target model. On the other hand, theoretical work by Ohki and Hudson (1975) raised the possibility that the infrared continuum at wavelengths shorter

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than  $\sim 20 \, \mu m$  may arise from an optically thin source at temperatures in the range of  $10^4 - 10^5 \, \text{K}$ . This latter possibility is in line with the results of time-dependent simulations of chromospheric heating by electron beams performed by Kašparová *et al.* (2009a).

The main goal of this article is to investigate the origin of the infrared continuum detected at 30 THz during SOL2012-03-13. To do this, we have performed a detailed analysis of multi-frequency observations including measurements in radio-millimeter and submillimeter wavelengths, hard X-ray (HXR) and gamma-ray (GR), H $\alpha$ , and white light (WL). The instrumentation used to collect these data is briefly described in Section 2 and an overview of the observations is presented in Section 3. Section 4 is devoted to the analysis of HXR/GR spectra from which numbers and energy contents of electrons, protons, and  $\alpha$  particles accelerated during SOL2012-03-13 are estimated. In Section 5 we discuss the relation between HXR/GR and radio-emitting electrons. The origin of the 30 THz emission is examined in Section 6 by using semi-empirical time-independent models of both the quiet and flare chromosphere. In Section 7 we provide an estimate of the energy deposited by flare-accelerated electrons, protons, and  $\alpha$  particles in the atmospheric layers that radiate the 30 THz emission, and we examine whether this can account for the energy radiated at 30 THz. The final section summarizes the main conclusions.

## 2. Instrumentation

Radio data at 45 GHz and 90 GHz were obtained by the radio polarimeters described by Valio *et al.* (2013). For the SOL2012-03-13 flare the uncertainty on flux densities is about 20 %. Observations at 212 and 405 GHz have been provided by the SST. The atmospheric opacity was estimated to be 0.47 and 2.2 Nepers at 212 and 405 GHz, respectively. At 212 GHz the flux density accuracy is estimated to be 20 %. At 405 GHz the 1- $\sigma$  detection threshold was  $\sim$  55 sfu<sup>1</sup>, and no significant emission was detected.

In the HXR and GR domain, the SOL2012-03-13 flare has been detected by the *Gamma-Ray Burst Monitor* (GBM) on *Fermi* (Meegan *et al.*, 2009). GBM is composed of twelve sodium-iodide (Na I) and two bismuth germanium oxide (BGO) detectors. In this analysis we used the most sunward Na I and BGO detectors. The Na I data consist of 128 energy channels covering the energy range 4 keV – 2000 keV, and the BGO data also consist of 128 energy channels, but in the 113 – 50 000 keV range.

The 30 THz instrumental setup at El Leoncito was reported by Marcon *et al.* (2008) and Kaufmann *et al.* (2008). For the present solar flare the data calibration and the determination of the excess flux density relative to the quiet Sun have been described in detail by Kaufmann *et al.* (2013). The accuracy of flux density measurements has been estimated to be  $\sim$ 25 %. The diffraction limit of the instrument is  $\sim$ 15" and the source position uncertainty is  $\sigma \sim$ 3", as obtained from fitting the 30 THz limb. The bandwidth of the instrument is  $\sim$ 17 THz, and in the following, we assume that the 30 THz emission does not depend on frequency within this bandwidth.

 $H\alpha$  observations were obtained with the *H-Alpha Solar Telescope for Argentina* (HASTA; Bagalá *et al.*, 1999). HASTA provides solar full-disk images with a time resolution of 5 seconds in flare mode and a spatial resolution of 2". Excess emission due to the flare was normalized to the quiet-Sun emission.



 $<sup>^{1}1 \</sup>text{ sfu} = 10^{-22} \text{W} \cdot \text{m}^{-2} \cdot \text{Hz}^{-1}$ .

The above data set was complemented by radio observations at 1.415, 2.695, 4.995, and 8.8 GHz from the Sagamore Hill-station of the US Air Force *Radio Solar Telescope Network* (RSTN)<sup>2</sup> (Guidice, 1979). There were no reliable 15.4 GHz measurements during SOL2012-03-13. We also used WL images from the *Helioseismic and Magnetic Imager* (HMI; Scherrer *et al.*, 2012) onboard the *Solar Dynamic Observatory* (SDO) obtained every 45 s with a spatial resolution better than  $\sim 1''$ .<sup>3</sup>

### 3. Observation Overview

The flare SOL2012-03-13 occurred in NOAA Active Region AR 11429 located at N18W64 on 2012 March 13 at 22:00 UT. It was associated with a M7.9 soft X-ray (SXR) event detected by the Geostationary Operational Environmental Satellite (GOES) and with a H $\alpha$ flare of importance 1B. From top to bottom, Figure 1 displays the time profile of the SXR (1-8 Å) from GOES, <sup>4</sup> radio (45 and 212 GHz), H $\alpha$ , flare excess mid-infrared (30 THz), WL, and 216-318 keV HXR emissions detected during SOL2012-03-13. Except for the  $H\alpha$  measurements, these observations have been presented in Kaufmann et al. (2013). The HXR light curve consists of an impulsive burst that started at  $\sim 17.20.53$  UT with a maximum at  $\sim 17:22:54$  UT and lasted for about ten minutes. This impulsive peak is seen from radio to optical wavelengths, i.e. from the corona down to the low chromosphere. At radio wavelengths, there are two peaks of apparently similar flux densities. There is a change of the decay slope of the HXR emission that corresponds to the second radio peak. The H $\alpha$ , 30 THz, and WL emissions show a broad peak that encompasses the two radio and HXR peaks. In addition to this impulsive phase, there is a long-lasting and slowly varying component seen at all wavelengths except in HXR and WL. For example, at 45 GHz the gradual emission is still visible after 19:00 UT, although it is weak ( $\sim 40-50$  sfu).

Figure 2 shows the projections of the  $H\alpha$ , WL, and 30 THz sources, obtained around the maximum of the impulsive peak, on a vector magnetogram recorded by SDO/HMI at 17:13:15 UT. The flare-enhanced H $\alpha$  emission arises from four sources (red contours) marked  $S_1$ ,  $S_2$ ,  $S_3$ , and  $S_4$ .  $S_1$  and  $S_2$  are close to the two WL emitting regions WL<sub>1</sub> and  $WL_2$ , shown by orange contours (see also Figures 3 and 10 in Kaufmann *et al.*, 2013). The extents of WL<sub>1</sub> and WL<sub>2</sub> are  $\sim 10''$  and 2", respectively. The projections of WL<sub>1</sub> and WL<sub>2</sub> and S<sub>1</sub> and S<sub>2</sub> are located on opposite magnetic field polarities and are connected by a bright loop shown at 211 Å in Figure 5 of Kaufmann et al. (2013). At 30 THz only the source corresponding to S1 and to WL1, the stronger WL-emitting region, is detected within the sensitivity of the present setup of the 30 THz instrument. Since the 30 THz source is not resolved by the instrument, it is shown by a green circle whose diameter is the diffraction limit of the instrument (15") in both directions. Figure 2 thus indicates that the 30 THz source and the WL barycenter emission, which is close to maximum of WL<sub>1</sub>, are located close to each other. However, the uncertainty on the 30 THz source position  $(3\sigma \sim 9'')$  prevents drawing any conclusion on the relative height of the two sources for relative heights lower than few thousands of km. While the time profiles of S<sub>1</sub> and S<sub>2</sub> show a clear impulsive phase counterpart (see Figure 1), the remote sources S<sub>3</sub> and S<sub>4</sub> only show a slowly varying emission that is not considered in the following.

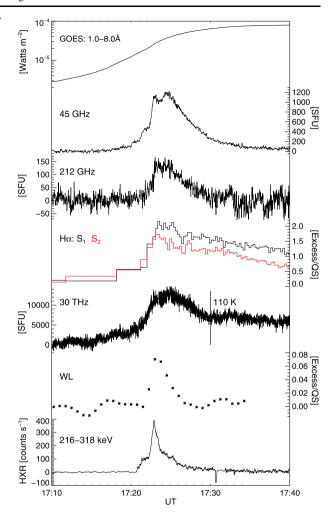
<sup>&</sup>lt;sup>4</sup>provided by NASA/GSFC at http://umbra.nascom.nasa.gov/goes/fits/.



<sup>&</sup>lt;sup>2</sup>http://www.ngdc.noaa.gov/stp/space-weather/solar-data/solar-features/solar-radio/rstn-1-second/.

 $<sup>^3</sup> http://hmi.stanford.edu/Description/HMI\_Overview.pdf.$ 

**Figure 1** Temporal evolution of the flare SOL2012-03-13 in various wavelength domains.



# 4. Electron and Ion Numbers and Energy Contents Around the Maximum of SOL2012-03-13

Figure 3 shows the mean excess count rate spectrum in the  $20-10\,000$  keV range recorded by the most sunward Na I (black error bars) and the most sunward BGO (blue error bars) detectors for a 80 s time interval around the peak of the HXR/GR emission. In the 36-1000 keV range, the observed Na I count rate spectrum is well represented by the expected count rate spectrum shown by the green line. This latter spectrum was obtained by convolving a triple power-law photon spectrum with the Na I detector calibration matrix. The triple power-law spectrum represents the electron bremsstrahlung spectrum in the  $\sim 35-1000$  keV range. It is defined by the normalization factor at 50 keV, the power-law indices  $\gamma_1$ ,  $\gamma_2$ , and  $\gamma_3$ , and the break energies Ebr<sub>1</sub> and Ebr<sub>2</sub> displayed in Table 1. In the  $216-10\,000$  keV range, the BGO count rate spectrum is well represented by the expected count rate spectrum (red line) obtained for a photon spectrum that is the sum of a broken power-law of the 2.2 MeV neutron capture line and of a template of narrow nuclear lines. We used the nuclear line template, included as standard within OSPEX (Schwartz *et al.*, 2002), calculated



**Figure 2** Projections of Hα (17:22:53 UT, red contours), WL (17:23:00 UT, orange contours) and 30 THz (17:22:54 UT, green circle) sources on an SDO/HMI vector magnetogram obtained at 17:13:15 UT.

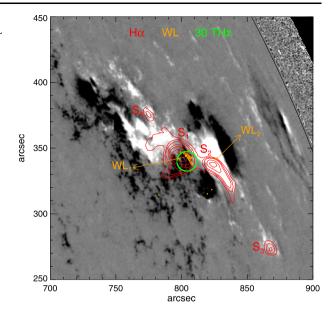
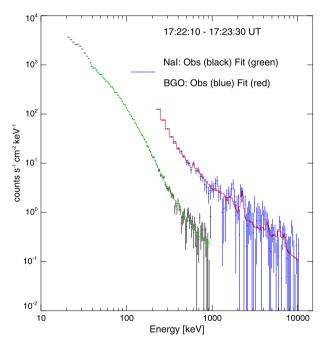


Figure 3 HXR/GR spectrum around the maximum of SOL2012-03-13 obtained by combining BGO and Na I measurements of the GBM instrument on *Fermi* (error bars). The green and red curves show the model spectrum fitted to GBM observations (see text).



for a flare at a heliocentric angle of  $60^{\circ}$  by assuming a downward isotropic distribution of ions with a power-law energy distribution of index 4 and an  $\alpha/p$  ratio of 0.22. The broken power-law represents the electron bremsstrahlung spectrum in the  $200-10\,000$  keV range. It is defined by the normalization factor at 50 keV, the power-law indices  $\Gamma_1$  and  $\Gamma_2$ , and the break energy Ebra (see Table 2). For the fitting procedure we used the OSPEX package of SolarSoft.



| Table 1 | Parameters of the photon | spectrum fitted to the Na 1 | I measurements in the 35 – | 1000 keV  |
|---------|--------------------------|-----------------------------|----------------------------|-----------|
| Table 1 | Parameters of the photon | spectrum mued to the iva-   | i measurements in the 55 – | IUUU KEV. |

| photon/s/cm <sup>2</sup> /keV<br>at 50 keV | γ1            | Ebr <sub>1</sub><br>[keV] | $\gamma_2$    | Ebr <sub>2</sub><br>[keV] | γ3            |
|--|---------------|---------------------------|---------------|---------------------------|---------------|
| $4.7 \pm 1.5$                              | $3.3 \pm 0.2$ | 94 ± 10                   | $3.8 \pm 0.2$ | $282 \pm 20$              | $2.4 \pm 0.2$ |

Table 2 Parameters of the photon spectrum fitted to the BGO measurements in the 200 – 10 000 keV.

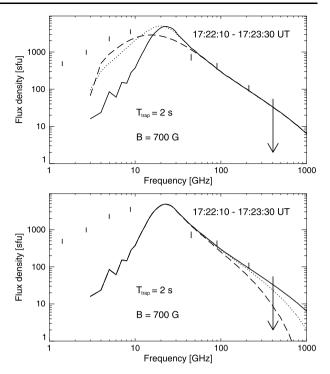
| photon/s/cm <sup>2</sup> /keV<br>at 50 keV | $\Gamma_1$                  | Ebra<br>[keV] | $\Gamma_2$    | 2.2 MeV line photon/s | narrow lines<br>photon/s |
|--|-----------------------------|---------------|---------------|-----------------------|--------------------------|
| $5.7 \pm 1.9$                              | $3.6\pm0.2$                 | $388 \pm 50$  | $2.3 \pm 0.2$ | $0.054 \pm 0.018$     | $0.11 \pm 0.04$          |
|  | electron/s/keV<br>at 50 keV | $\delta_1$    | Ebre<br>[keV] | $\delta_2$            |                          |
|  | $5.6 \times 10^{33}$        | 4.7           | 800           | 3.5                   |                          |

Figure 3 shows that (i) the electron bremsstrahlung continuum extends up to at least 10 000 keV and (ii) there is clear 2.2 MeV line emission and weak narrow GR line emission, indicating that  $\sim 1-100$  MeV protons and  $\sim 1-100$  MeV/nucleon ions have been accelerated during SOL2012-03-13. The photon fluxes derived from both the Na I and BGO data agree well (within better than 25 %) between 200 – 700 keV. However, because the responses of the Na I and BGO detectors are quite different, a given incident photon spectrum will produce different count spectra in the two detectors, as shown in Figure 3. Above  $\sim 400 \text{ keV}$ , the  $1-\sigma$  uncertainty is smaller for BGO than for Na I. In the following we only consider the photon spectrum derived from BGO data since we are interested in microwave-emitting electrons and in GR line radiation. To derive the spectrum of electrons from this photon spectrum, we furthermore assume that this electron spectrum is also a broken power-law. The electron spectrum is then derived by using an electron-to-thick-target bremsstrahlung code including both relativistic effects and electron-electron bremsstrahlung<sup>5</sup> and by varying its parameters until a good agreement with the photon spectrum is reached. The obtained parameters: electron flux at 50 keV, the low- and high energy spectral indices  $\delta_1$  and  $\delta_2$  and the break energy Ebre, are displayed in Table 2. The mean flux of > 50 keV electrons between 17:22:10 and 17:23:30 UT is found to be  $F_e$  (> 50 keV)  $\sim 8 \times 10^{34}$  electron s<sup>-1</sup> corresponding to a mean energy flux  $\Phi_e$  (> 50 keV)  $\sim 9 \times 10^{27}$  erg s<sup>-1</sup>. The nuclear line template is normalized so that an amplitude of 1 corresponds to  $8.5946 \times 10^{29}$  protons with energies above 30 MeV. Here the amplitude of the nuclear line template is  $0.11 \pm 0.04 \text{ s}^{-1}$ (see Table 2). It is well documented that ions with energies down to almost 1 MeV/nucleon contribute to the GR line emission. For the assumed energy power-law index of 4 we then obtain mean proton and  $\alpha$  fluxes at the top of the atmosphere:  $F_p$  (> 1 MeV)  $\sim 2.6 \times 10^{33}$ protons s<sup>-1</sup>,  $F_{\alpha}$  (> 1 MeV/nucl)  $\sim 5.6 \times 10^{32} \ \alpha \ s^{-1}$ . These correspond to energy fluxes of  $\Phi_{\rm p}$  (> 1 MeV) = 6.2 × 10<sup>27</sup> erg s<sup>-1</sup> and  $\Phi_{\alpha}$  (> 1 MeV)  $\sim 5.4 \times 10^{27}$  erg s<sup>-1</sup>, respectively. Since the uncertainty on the determination of photon fluxes is about 30 %, the above values of particle and energy fluxes suffer from the same uncertainty. The broad GR line emission has not been taken into account to derive the above estimates because as a result of the poor statistics, the observed GR line spectrum is only poorly defined. Nevertheless,



<sup>&</sup>lt;sup>5</sup>N. Vilmer, private communication.

Figure 4 Radio spectrum: in both panels the vertical error bars show the radio spectrum observed in the 1-212 GHz frequency range around the maximum of the impulsive phase of SOL2012-03-13: At 405 GHz the arrow indicates the upper limit of the flux density. The gyrosynchrotron spectra computed for B = 700 G and  $T_{trap} = 2 \text{ s}, E_{max} = 10000 \text{ keV}$ and  $E_{min} = 30 \text{ keV}$  (solid line), 400 keV (dotted line) and 800 keV (dashed line) are overplotted in the upper panel, while results for  $E_{min} = 30 \text{ keV}$  and  $E_{\text{max}} = 10000 \text{ keV}$  (solid line), 7000 keV (dotted line) and 4000 keV (dashed line) are overplotted in the lower panel (see text).



we checked that including broad lines leads to estimates of proton and  $\alpha$  particle fluxes and energy fluxes that stay within the 30 % uncertainty. We note that  $\Phi_p \sim \Phi_\alpha$  and that  $\Phi_e \, (> 50 \, \text{keV}) \sim \Phi_p \, (> 1 \, \text{MeV}) + \Phi_\alpha \, (> 1 \, \text{MeV})$ .

# 5. Relation Between Radio and HXR/GR Emitting Electrons During the Impulsive Phase

Figure 4 displays the averaged radio spectrum (vertical error bars) observed during the same time interval (17:22:10-17:23:30 UT) as the HXR/GR spectrum analyzed in Section 4. Its shape is reminiscent of a gyrosynchrotron spectrum with a turnover frequency somewhere between 10 and 30 GHz. It is generally admitted that the 1-200 GHz (cm-mm) radio emission and the HXR/GR continuum are both radiated by a closely related population of electrons accelerated in the corona (e.g. Bastian, Benz, and Gary, 1998; Pick and Vilmer, 2008). Briefly stated: (i) the gyrosynchrotron emission is radiated by the instantaneous population of electrons present in the coronal portion of magnetic loops connected to the acceleration region, while (ii) the HXR/GR bremsstrahlung continuum is produced by thick-target interactions of precipitating electrons at the chromospheric footpoints of these loops. It is also well documented that for a magnetic field of a few hundred Gauss the cmmm emission is radiated by electrons with energies ranging from a few hundreds of keV to a few MeV (e.g. Ramaty, 1969; Pick, Klein, and Trottet, 1990; Ramaty et al., 1994). As a first approximation, we thus assume that the instantaneous spectrum of radio-emitting electrons is given by (e.g. Trottet et al., 1998)  $N_R(E) \approx F_X(E) T_{trap}$  electron keV<sup>-1</sup>, where  $T_{trap}$  is the time spent by the accelerated electrons in the cm-mm radio-emitting region and  $F_X(E)$ 



is the electron flux spectrum displayed in Table 2. Without multi-frequency cm–mm imaging observations it is not possible to constrain radio source models with an inhomogeneous magnetic field B and an ambient density  $N_{amb}$ . In the following we therefore compute the gyrosynchrotron emission produced by  $N_R(E)$  in a radio-emitting region of constant  $N_{amb}$  and uniform B. Such a simple model is not able to account for the < 10 GHz optically thick radio emission, but in principle it allows matching reasonably well the optically thin part of the radio spectrum observed at 45, 90, and 212 GHz during the present flare. The gyrosynchrotron emission was then computed for B = 700 G,  $T_{trap} = 2$  s and  $N_{amb} = 5 \times 10^{10}$  cm<sup>-3</sup>. The diameter and thickness of the radio source normal to and along the line of sight were set to 14 000 and 2000 km, respectively, and the angle between B and the line of sight to 45°. The gyrosynchrotron code used is that developed by Ramaty (1969), Ramaty *et al.* (1994) adapted to take into account a broken power-law electron spectrum.

Figure 4 (upper panel) shows the results for an electron population with a high-energy cutoff  $E_{max}=10\,000$  keV and different low-energy cutoffs  $E_{min}=30$  keV (solid line), 400 keV (dotted line) and 800 keV (dashed line). In Figure 4 (lower panel), we show  $E_{min}=30$  keV and  $E_{max}=10\,000$  keV (solid line), 7000 keV (dotted line) and 4000 keV (dashed line). Figure 4 shows that the optically thin part of the observed radio spectrum is emitted by electrons in the energy range of  $\sim 800$  to  $7000-10\,000$  keV, that is, above the break energy of the electron spectrum deduced from the HXR/GR photon spectrum. This is consistent with earlier findings (Trottet *et al.*, 1998, 2000, 2008). B and  $T_{trap}$ , which fix the value of  $N_R$ , are not independent parameters in the data-fitting process. Indeed, the same flux densities can be obtained for higher B and lower  $T_{trap}$  and *vice versa*. B  $\sim 700$  G and  $T_{trap} \sim 2$  s appears to be a reasonable set of values. On one hand, a substantial increase of B would lead to a too high turnover frequency. On the other hand, a decrease of B would imply an increase of  $N_R$ . Since there is no physical reason for  $E_{min}$  to be higher than a few tens of keV, a too low value of B would lead to an unreasonably high density of nonthermal electrons in the radio source compared to  $N_{amb}$ .

### 6. Origin of the 30 THz Emission

In the following we assume that both the quiet and flare 30 THz emission is thermal emission from the chromosphere. The aim of this section is to determine from which atmospheric layer(s) the 30 THz emission observed during the SOL2012-03-13 flare arises (see Section 3 and Kaufmann *et al.*, 2013). As we do not know the actual flaring atmosphere, a first approach to achieve this employs time-independent models of both the flaring and quiet lower atmospheres of the Sun. These semi-empirical models are based on hydrostatic and statistical equilibria. For a given temperature structure the full non-LTE radiative transfer is solved numerically to obtain the synthetic flare spectrum. This synthetic spectrum is compared to observed spectral features (both lines and continuum), and the temperature structure is adjusted to obtain a good agreement with observations.

To compare expectations from flare models with quiet-Sun conditions we used the C7 model for the quiet solar atmosphere (Avrett and Loeser, 2008). The flare atmospheric models considered hereafter are the FLA model constructed by Mauas, Machado, and Avrett (1990) to account for the WL continuum emission observed during the SOL1983-06-15 flare, and the F1 and F2 models that are representative of weak and medium-size flares (Machado *et al.*, 1980). We have restricted our analysis to these models because they are well documented in the literature and because SOL2012-03-13 is a medium-size flare. We took their temperature height profiles as inputs and used the PAKAL radiative transfer code



**Table 3** Height (h<sub>max</sub>) and opacity ( $\tau_{30}$ ) at the maximum of CF<sub>30</sub>. The altitudinal range  $\Delta h$  over which CF is higher than half its maximum value. T<sub>b30</sub> is the derived brightness temperature at 30 THz.  $\Delta T_{b30}$  is the increase of T<sub>b30</sub> with respect to C7 and  $\Delta S_{30}$  is the excess flux density with respect to C7 for a 30 THz emitting source of 10" diameter.

| Model | h <sub>max</sub> [km] | $\tau_{30}$ | Δh [km]    | T <sub>b30</sub> [K] | $\Delta T_{b30} [K]$ | ΔS <sub>30</sub> [sfu] |
|-------|-----------------------|-------------|------------|----------------------|----------------------|------------------------|
| C7    | 180                   | 1.1         | 130-270    | 4700                 |                      |                        |
| FLA   | 180                   | 1.1         | 130 - 270  | 4900                 | 200                  | 1000                   |
| F1    | 180                   | 1.4         | 140 - 300  | 5000                 | 300                  | 1500                   |
| F2    | 1070                  | 0.2         | 960 - 1100 | 7100                 | 2400                 | 12300                  |

(De la Luz *et al.*, 2010; De la Luz, Lara, and Raulin, 2011), which is similar to the PAN-DORA code used by Avrett and Loeser (2003), to (i) compute the densities of electrons and of the most important ion species, including  $H^-$ , as a function of height h, and (ii) to determine the absorption coefficient  $\kappa_{30}$ (h) and the opacity  $\tau_{30}$ (h) for a 30 THz emitting region at a longitude of 60°. Following Heinzel and Avrett (2012), we then computed the contribution function  $CF_{30}$ (h) as a function of h, given by

$$CF_{30}(h) = \eta_{30}(h)e^{-\tau_{30}(h)}, \quad \eta_{30}(h) = \kappa_{30}(h)B_{30}(T(h)),$$
 (1)

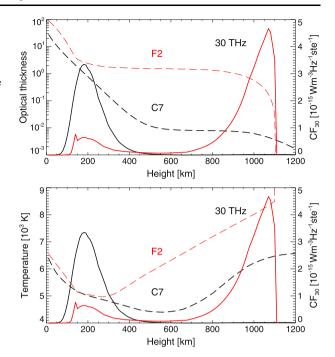
where T(h) is the local temperature and  $B_{30}(T(h))$  the Planck source function.  $CF_{30}(h)$  allows us to identify for each model the atmospheric layers that contribute most to the 30 THz emission. For a given model the brightness temperature at 30 THz is given by

$$T_{b30} = \int Te^{-\tau_{30}} d\tau_{30}. \tag{2}$$

For each atmospheric model Table 3 displays  $h_{max}$  and  $\tau_{30}$  at the maximum of CF<sub>30</sub>, the altitude range  $\Delta h$  at half of the CF<sub>30</sub> maximum, the expected brightness temperature T<sub>b30</sub>, the excess brightness temperature  $\Delta T_{b30}$ , and the corresponding excess flux density  $\Delta S_{30}$ (for a 10" source) with respect to values obtained for C7. The dashed lines in Figure 5 show  $\tau_{30}$  (top) and T (bottom) as a function of h for C7 (black) and F2 (red). The corresponding height profiles of CF<sub>30</sub>(h) (solid lines) are overplotted in both panels. The 30 THz emission from C7, FLA and F1 arises from an atmospheric layer LC7<sub>1</sub> centered at  $h_{max} \sim 180$  km, where  $\tau_{30} \sim 1$ , which extends from  $\sim 130-140$  to 270-300 km. Thus, for these models, the 30 THz radiation arises from an optically thick layer located below the temperature minimum region at temperatures of about 5000 K. For the quiet Sun, this is consistent with earlier results (see e.g. Figure 2 in Deming et al., 1991). FLA and F1 cannot explain the 30 THz emission observed during SOL2012-03-13 because they lead to  $\Delta S_{30} \sim 1000-1500$  sfu, which is about one order of magnitude lower than the observed value  $\sim 12\,000$  sfu at the maximum of the 30 THz burst. In contrast, F2 leads to  $\Delta S_{30} \sim 12300$  sfu, which agrees with the observed value. In F2, the maximum of CF<sub>30</sub> occurs at  $h_{max} \sim 1070$  km where  $\tau_{30}$  < 1, so that the 30 THz radiation arises mostly (~80 %) from an atmospheric layer LF2,  $\Delta h_h \sim 960-1100$  km, located above the temperature minimum region at temperatures around 8000 K. Figure 5 shows that for F2, in addition to the LF2 layer, there is an optically thick 30 THz emitting layer slightly below the temperature minimum in the altitude range  $\Delta h_1 \sim 130-270$  km. This latter source contributes moderately ( $\sim 20$  %) to the total emission. Its temperature is a few tens of kelvin higher than that of the quiet Sun, so that it represents only less than 1 % of the quiet-Sun emission. This is in line with earlier theoretical expectations by Ohki and Hudson (1975), which indicated that the contrast between



Figure 5 Top: Opacity  $\tau_{30}$  (dashed lines) and contribution function CF (solid lines) as a function of height above the photosphere. Red curves represent F2 model results, while black curves are for C7. Bottom: Atmospheric local temperature (dashed lines) and CF (solid lines) as a function of height.



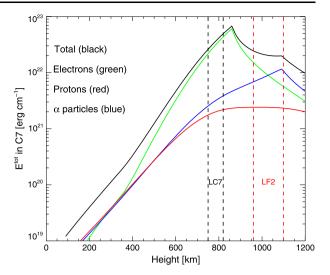
the quiet and flare infrared emission in the 10-40 THz range is about ten times higher for an optically thin source at about  $10^4$  K than for an optically thick source around 5000 K. This is also consistent with results of time-dependent numerical simulations (see Figure 3 in Kašparová *et al.*, 2009a). The F2 flare model therefore appears to be a plausible atmospheric model to account for the 30 THz emission radiated during SOL2012-03-13.

## 7. 30 THz Chromospheric Response to Flare-Accelerated Particles

The 30 THz time profile (see Figure 1) exhibits an impulsive emission that encompasses the two radio and HXR peaks, superimposed on a long-lasting and slowly varying component (see Section 3). This suggests that the 30 THz impulsive burst results, directly or indirectly, from chromospheric heating due to energy deposition by nonthermal particles (electrons, protons, and  $\alpha$  particles), while the slowly varying emission is generated by some slower process, e.g., conduction fronts. In the following we focus on the chromospheric heating by particles accelerated during SOL2012-03-13. A proper treatment of this problem, which is beyond the scope of the present study, should account for the temporal evolution of the flaring atmosphere due to time-dependent heating by particles, as in Kašparová et al. (2009a,b). Here, we simply consider C7 as the initial atmosphere model at  $t_0 \sim 17:20:45$  UT (beginning of the HXR and 30 THz radiation) and F2 as the atmosphere model that is reached at  $t_1 \sim 17:24:50$  UT (maximum of the observed 30 THz radiation). For a given atmosphere model we calculated the energy deposition per centimeter by nonthermal particles  $\Theta(N)$  (erg cm<sup>-1</sup>) as a function of the hydrogen column depth N (see Equation (8) in the Appendix). In the following we use the height h to parametrize the altitude above the photosphere in a given atmosphere, considering  $\Theta(h)$  rather than  $\Theta(N)$ . These computations are presented in detail in the Appendix. They extend previous works (e.g. Emslie,



Figure 6 Energy deposition per unit of height in C7 ( $E^{tot}$ ) by flare-accelerated particles as a function of height. The dashed vertical lines in red show the F2 atmospheric layer (LF2) from which  $\sim 80$  % of the 30 THz emission arises. The black vertical lines show the C7 layer (LC7), which covers the same mass column density as the LF2 layer.



1978) by considering that the degree of ionization varies with N and by retaining the energy dependence of the Coulomb logarithm, which is particularly important for ions.

As a first approach, we computed the total energy deposited by particles accelerated between  $t_0$  and  $t_1$  as a function of h in C7. To do this, we integrated the BGO count-rate spectrum from  $t_0$  to  $t_1$  and estimated the mean flux of electrons, protons, and  $\alpha$  particles in the same way as in Section 4 and multiplied by  $t_1-t_0=245$  s. This leads to  $\mathcal{F}_{0e}$  (> 50 keV)  $\sim$  $10^{37}$ ,  $\mathcal{F}_{0p}$  (> 30 MeV)  $\sim 8.5 \times 10^{30}$  and  $\mathcal{F}_{0\alpha}$  (> 30 MeV/nucl)  $\sim 1.9 \times 10^{30}$  for the total numbers of > 50 keV electrons, > 30 MeV protons, and > 30 MeV/nucl  $\alpha$  particles accelerated between  $t_0$  and  $t_1$ . We then used these normalizations in Equation (8) to calculate the energy deposited per cm that is due to electrons, protons, and ions, and summed over them to obtain the total energy deposited by particles per cm E<sup>tot</sup>(h). Figure 6 shows E<sup>tot</sup>(h) as a function of h in the pre-flare atmosphere C7 for the ensemble of accelerated particles as well as the contributions from electrons, protons, and  $\alpha$  particles separately. As stated in Section 6, most of the 30 THz emission arises from the LF2 layer indicated by red vertical dashed lines in Figure 6. The altitude range of the C7 layer LC7 (750-820 km), which covers the same range of mass column densities  $(3.5 \times 10^{-3} - 6.2 \times 10^{-3} \text{ g cm}^{-2})$  as LF2, is shown by the black dashed lines in the Figure 6. This range of the column density is consistent with that indicated by Machado, Emslie, and Avrett (1989). As a rough approximation, we assumed that the total energy deposited by particles between  $t_0$  and  $t_1$  in LC7,  $E_{par}^{LC7}$ , may account for the 30 THz emission from LF2. By integrating E<sup>tot</sup>(h) over the LC7 altitude range, we derive  $E_{par}^{LC7} \sim 3 \times 10^{29}$  erg. The total amount of energy radiated at 30 THz between  $t_0$  and t<sub>1</sub> is given by

$$E_{30}^{\text{tot}} = 10^{-15} \, 4\pi \, R^2 \Delta \nu \int_{t_0}^{t_1} \Delta S_{30}(t) \, dt \sim 10^{28} \, \text{erg},$$
 (3)

where R = 1 AU = 1.5  $\times$  10<sup>11</sup> m,  $\Delta\nu$  is the observed frequency bandwidth in Hz (see Section 2) and  $\Delta S_{30}(t)$  the excess flux density at 30 THz in sfu.  $E_{par}^{LC7}$  is about thirty times higher than  $E_{30}^{tot}$ . Thus, direct heating by nonthermal particles appears to be a possible mechanism to account for the  $\sim$ 80 % of the impulsive 30 THz emission that arises from LF2. This latter statement remains valid even if we include a range of initial pitch angles, mirroring and pitch-angle scattering in the energy deposition calculation (see Appendix). On the other



hand, the energy  $6 \times 10^{26}$  erg deposited by particles in LC7<sub>1</sub>, which corresponds to about the same mass column density and altitude ranges as the equivalent layer in F2 (see Section 6), is too low to account for the remaining 20 % of the 30 THz radiation. The heating in the LC7<sub>1</sub> layer may thus be due to some indirect mechanism, such as radiative backwarming of the deep chromosphere from the LF2 layer (e.g., Metcalf, Canfield, and Saba, 1990; Kerr and Fletcher, 2014) or radiative coupling of the upper chromosphere and temperature minimum regions (Machado, Emslie, and Avrett, 1989). A harder ion distribution (e.g.  $\delta = 2$ ) would deposit a greater fraction of its total energy content in the deeper atmosphere. To this extent, the calculations here, with a fixed value of  $\delta = 4$ , should be regarded as illustrative. The statistical quality of the  $\gamma$ -ray spectrum for this event does not justify more detailed investigation, however.

Figure 1 shows that the evolution of the  $H\alpha$  emission from the  $S_1$  and  $S_2$  kernels (see Figure 2) is similar to that of the 30 THz excess flux density. Because the  $H\alpha$  emission arises from a  $\sim 10^4$  K plasma, the altitudes of  $S_1$  and  $S_2$  should be close to that of the 30 THz source at  $\sim 8000$  K. This suggests that direct heating by particles is also responsible for the impulsive  $H\alpha$  radiation, while, like for the 30 THz emission, the slowly varying, long-lasting component is due to some other process. A detailed and quantitative analysis of the WL emission is beyond the scope of this study. Nevertheless, as remarked in Section 3, the WL time profile only exhibits the impulsive emission and not the slowly varying, long-lasting component. This suggests that the mechanism responsible for the 30 THz and  $H\alpha$  slowly varying, long-lasting component is not efficient enough to produce WL emission, whether it arises from direct particle heating from a LF2-like layer or from indirect heating of the deep chromosphere (LC7<sub>1</sub> layer). The former hypothesis is consistent with the heights of WL sources,  $\sim 800-1000$  km above the photosphere estimated by *e.g.* Krucker *et al.* (2015) for some flares.

## 8. Summary

The SOL2012-03-13 flare is the first event that has been detected in the mid-infrared domain at 30 THz (Kaufmann *et al.*, 2013). The combined analysis of the 30 THz data with HXR/GR, WL, H $\alpha$ , and 1–400 GHz radio observations has allowed us to estimate the numbers of electrons, protons, and  $\alpha$  particles accelerated during the flare and to discuss the origin of the 30 THz emission. The main findings can be summarized as follows:

- The HXR/GR observations of the Gamma-ray Burst Monitor on Fermi have revealed that SOL2012-03-13 is a gamma-ray line flare detected up to at least 10 MeV. The numbers and energy contents of HXR/GR emitting electrons, protons, and α particles were estimated. The energy content in protons and α particles with energies above 1 MeV/nucl. was found to be similar to the energy content in > 50 keV electrons. This indicates that in addition to electrons, protons and α particles may substantially contribute to the heating of the chromosphere during flares such as SOL2012-03-13.
- The observed 1-200 GHz radio spectrum is reminiscent of gyrosynchrotron radiation. The optically thin part of the radio spectrum (> 10-20 GHz) is radiated by HXR/GR emitting electrons with energies greater than ~800 keV. The spectrum of these highenergy electrons is harder than that of lower energy electrons.
- Assuming that the 30 THz emission is thermal emission from the chromosphere, we used time-independent semi-empirical models of both the quiet and flaring atmospheres to identify the atmospheric layers from which the 30 THz emission arises. In agreement with



earlier works, we find that the quiet-Sun 30 THz radiation is emitted by an optically thick layer at temperatures around 5000 K, below the temperature minimum region. During the flare, the measured flux density excess at 30 THz is consistent with that expected from the F2 model by Machado *et al.* (1980), which is representative of medium-size flares. In this model, about 80 % of the 30 THz emission arises from an atmospheric layer LF2 ( $\sim$ 960–1100 km above the photosphere) at temperatures of about 8000 K, well above the temperature minimum region. At 30 THz, this layer is not optically thick ( $\tau$  < 1). The remaining 20 % of the 30 THz emission arises from an optically thick layer, slightly below the temperature minimum region in F2, which covers altitude and mass column density ranges similar to those of the emitting layer in the quiet Sun.

- The energy deposited by electrons, protons, and  $\alpha$  particles in the quiet-Sun layer that covers the same range of mass column density  $(3.5-6.2\times10^{-3}~{\rm g\,cm^{-2}})$  was calculated by taking into account that the degree of ionization varies with height and by retaining the energy dependence of the Coulomb logarithm. This energy is found to be about thirty times greater than that radiated at 30 THz. Thus energy deposition by accelerated particles is a plausible mechanism responsible for the heating of the LF2 layer, which gives rise to ~80 % of the observed 30 THz emission during the impulsive phase of SOL2012-03-13. On the other hand, the energy deposited by particles in the deep chromosphere is too low to account for the remaining 20 % of the 30 THz flux density radiated from below the temperature minimum region in F2. A possible, but not unique, scenario is that the impulsive WL emission and 20 % of the 30 THz radiation arises from an optically thick layer, below the temperature minimum region, heated *e.g.* by backwarming from the upper chromosphere where most of the energy transported by accelerated particles is deposited.
- The 30 THz and Hα exhibit a long-lasting and slowly varying component that is not observed in the WL and HXR/GR domains. This indicates that the chromospheric heating giving rise to this component is due to a different mechanism than energy deposition by accelerated particles and that the efficiency of this mechanism is not sufficient to produce long-lasting WL emission.

In summary, using time-independent semi-empirical models of the quiet and flare atmosphere, we have shown that thermal emission from the chromosphere heated by accelerated particles provides a plausible quantitative interpretation of the 30 THz emission in general agreement with that observed during the impulsive phase of SOL2012-03-13. Time-dependent numerical models of energy deposition by accelerated particle such as developed by Kašparová *et al.* (2009a) are needed to confirm our conclusion. Moreover, if the 30 THz emission arises from a quasi optically thin chromospheric layer like LF2, the emission spectrum between ~ 10–100 THz is expected to be rather flat or even slightly decreasing with increasing frequencies (see Figure 2 in Ohki and Hudson, 1975). Observations at frequencies above 30 THz such as those recently obtained from the *McMath-Pierce Solar Facility* at Kitt Peak (Penn *et al.*, 2015) should allow us to test the validity of this expectation, and thus of the thermal interpretation of the infrared emission from flares proposed in this work. In the near future, the combination of McMath observations and measurements at 3 and 7 GHz by *Solar-T* (Kaufmann *et al.*, 2014) should allow completing our understanding of the chromospheric response to flare energy release.

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## Appendix

To compute the energy deposited by accelerated electrons, protons, and  $\alpha$  particles in the chromosphere as a function of depth, we injected particles with an energy spectrum  $F_0(E)$  (MeV<sup>-1</sup>) at the top of the atmosphere. We parametrized the position in the atmosphere using the *hydrogen* column depth N. The energy deposited (erg cm<sup>-1</sup>) at depth N is (following Emslie, 1978)

$$\Theta(N) = \int_{E_{\min}(N)}^{\infty} \frac{F_0(E_0)}{v(E)} \left| \frac{\mathrm{d}E}{\mathrm{d}t}(E, N) \right| \mathrm{d}E_0. \tag{4}$$

Here  $E_{\min}(N)$  is the minimum energy of a particle that can reach depth N. In Equation (4) E should be understood as depending on  $E_0$  and N: it is the energy that a particle of initial energy  $E_0$  has when it has reached depth N.

An ion of energy E and charge z loses energy with depth at a rate given by (Gould, 1972b; Emslie, 1978; Olive and Particle Data Group, 2014)

$$\frac{\mathrm{d}E}{\mathrm{d}N} = -\frac{K}{\beta^2} \Lambda_{\mathrm{eff}}(E, N). \tag{5}$$

Here  $\beta$  is the particle speed in units of the speed of light, K is given by

$$K = \frac{4\pi e^4}{m_e c^2} z^2,$$

$$\Lambda_{\text{eff}}(E, N) = x\Lambda + (1 - x)\Lambda',$$
(6)

where x is the degree of ionization and  $\Lambda$  and  $\Lambda'$  are the Coulomb logarithms appropriate for slowing on electrons and on neutral atoms, respectively. For ions, expressions for  $\Lambda$  are given e.g. by Butler and Buckingham (1962), Gould (1972a). For  $\Lambda'$  we used the Bethe-Bloch form (Olive and Particle Data Group, 2014), neglecting the correction for the polarization of the medium, which is negligible in the low-density conditions of the solar atmosphere. We estimated the effects of the atmospheric chemical composition on energy loss by multiplying  $\Lambda'$  by

$$\sum_{n} \frac{a_n}{a_H} \frac{Z_n}{A_n} = 1.16,$$

where n sums over atomic species and  $A_n$ ,  $Z_n$  and  $a_n$  are the atomic number, atomic weight, and abundance relative to hydrogen of species n. We also generalized  $x = n_e/n_H$  so that it is no longer quite the degree of ionization and may take values > 1, dependent on the local electron density.

 $\Lambda$  and  $\Lambda'$  for electrons are given by Gould (1972a), Emslie (1978). By using only Equation (5), we neglected pitch-angle scattering. Scattering in angle is unimportant for fast ions and relativistic electrons – the only particles that can reach the LC7<sub>1</sub> layer. For nonrelativistic electrons it reduces the mean range by two thirds (Brown, 1972), although dispersion means that electrons will stop and deposit energy over a range of depths up to their full vertical stopping depth (Bai, 1982). For the present purposes of estimation, we completely neglected pitch-angle scattering.



Figure 7 The effective Coulomb logarithm,  $\Lambda_{eff}$  through the atmosphere for protons of energy 1, 10 and 100 MeV.

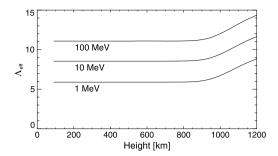


Figure 7 shows the value of  $\Lambda_{eff}$  throughout the chromospheric portion of the C7 atmosphere of Avrett and Loeser (2003) for protons of energies 1, 10, and 100 MeV. The importance of retaining the energy dependence of  $\Lambda$  has been emphasized elsewhere (MacKinnon and Toner, 2003). The variable degree of ionization means that  $\Lambda_{eff}$  also strongly depends on position. Thus the energy loss rate of Equation (5) is not separable in energy and depth, and analytical heating rates like those of Emslie (1978) may not be used (although an energy loss rate appropriate to a completely neutral atmosphere would give a good approximation below about 1000 km).

To evaluate the energy deposition  $\Theta$ , we need to assume a form for  $F_0(E_0)$ , e.g. a single power-law:

$$F_0(E_0) = \frac{\mathcal{F}_0}{E_*} (\delta - 1) \left(\frac{E_0}{E_*}\right)^{-\delta},\tag{7}$$

where  $\mathcal{F}_0$  is the number of particles injected above energy  $E_*$ . Then applying Equation (5) in Equation (4) gives

$$\Theta(N) = 8.16 \times 10^{-31} z^2 n_H(N) \mathcal{F}_0 E_*^{\delta - 1} (\delta - 1) \int_{E_{\min}(N)}^{\infty} E^{-\delta} \frac{\Lambda_{\text{eff}}(E, N)}{\beta^2(E)} dE_0.$$
 (8)

Again, E in the integrand of Equation (8) is understood to be a function of  $E_0$  and N: the energy at depth N of a particle that had energy  $E_0$  at injection. Since we cannot obtain analytical expressions for  $E(E_0, N)$ , we calculated it by numerical integration of Equation (5), with numerical interpolation as necessary between the tabulated points of a given atmosphere model, as needed for each of the abscissae of a numerical evaluation of the energy deposition (Equation (8)). More elaborate forms of  $F_0(E_0)$ , e.g. the broken power-law deduced for electrons, are straightforwardly substituted in Equation (4) as necessary.

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