

Quiz 10 Solutions

Let's solve this
using a system of equations.

From the graph we can see that

$(-1, -1)$ $(1, -1)$ and $(0, 1)$

are our support vectors.

$$w \cdot x + b = -1$$

$$w \cdot x + b = +1$$

$$(w_1, w_2) \cdot (-1, -1) + b = -1$$

$$(w_1, w_2) \cdot (1, -1) + b = 1$$

$$(w_1, w_2) \cdot (0, 1) + b = 1$$

$$-w_1 - w_2 + b = -1 \quad (1)$$

$$w_1 - w_2 + b = 1 \quad (2)$$

$$w_2 + b = 1 \rightarrow b = 1 - w_2 \quad (3)$$

$$(3) \text{ into } (2) \rightarrow w_1 - w_2 + 1 - w_2 = 1$$

$$w_1 - 2w_2 = 0$$

$$w_1 = 2w_2$$

$$(3) \text{ \& } (2) \text{ into } (1)$$

$$\rightarrow -2w_2 - w_2 + 1 - w_2 = -1$$

$$-4w_2 = -2$$

$$w_2 = \frac{1}{2}$$

$$w_1 = 1$$

$$b = \frac{1}{2}$$