

1. Run the perceptron algorithm on the following training data in the order it is provided.

sample	x_1	x_2	label
s_1	-1	-1	-1
s_2	-1	1	1
s_3	1	-1	1
s_4	1	1	1

Table 1: Training data.

$$w = (0, 0)$$

$$b = 0$$

Epoch 1

$$a_1 = 0 \cdot (-1) + 0 \cdot (-1) + 0 = 0 \quad 0 \cdot (-1) \leq 0 \quad \text{update}$$

$$w = (1, 1) \quad b = -1$$

$$a_2 = -1 \cdot 1 + 1 \cdot 1 - 1 = -1 \quad -1 \cdot 1 \leq 0 \quad \text{update}$$

$$w = (0, 2) \quad b = 0$$

$$a_3 = 0 \cdot 1 + 2 \cdot (-1) + 0 = -2 \quad -2 \cdot 1 \leq 0 \quad \text{update}$$

$$w = (1, 1) \quad b = 1$$

$$a_4 = 1 \cdot 1 + 1 \cdot 1 + 1 = 3 \quad 3 \cdot 1 \geq 0 \quad \text{no update}$$

Epoch 2

$$a_1 = 1 \cdot (-1) + 1 \cdot (-1) + 1 = -1 \quad -1 \cdot (-1) > 0 \quad \text{no update}$$

$$a_2 = -1 \cdot 1 + 1 \cdot 1 + 1 = 1 \quad 1 \cdot 1 > 0 \quad \text{no update}$$

$$a_3 = 1 \cdot 1 + 1 \cdot (-1) + 1 = 1 \quad 1 \cdot 1 > 0 \quad \text{no update}$$

$$a_4 = 1 \cdot 1 + 1 \cdot 1 + 1 = 3 \quad 3 \cdot 1 > 0 \quad \text{no update}$$

Done

$$w = (1, 1) \quad b = 1$$

$$w = w + yx$$

$$b = b + y$$