

EE 220 – Final Exam

Useful Equations:

$$V = IR$$

$$P = IV$$

$$i = \frac{dq}{dt}$$

$$q(t) = \int_{-\infty}^t i d\tau = \int_0^t i d\tau + q(0)$$

Unit Definitions:

$$1 \text{ V} = 1 \text{ J/C}$$

$$1 \text{ W} = 1 \text{ V} \cdot 1 \text{ A} = 1 \text{ J/s}$$

$$1 \text{ electron} = 1.602 \times 10^{-19} \text{ coulomb}$$

$$1 \text{ A} = 1 \text{ C/s}$$

$$1 \text{ Wh} = 1 \text{ J/s} \cdot 1 \text{ h} = 3,600 \text{ J}$$

$$1 \text{ coulomb} = 6.24 \times 10^{18} \text{ electrons}$$

Three resistors case

Parallel resistance

$$R_{eq} = (G_1 + G_2 + G_3)^{-1} = \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)^{-1}$$

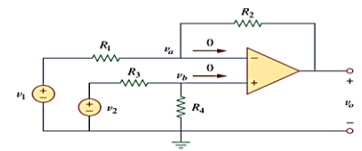
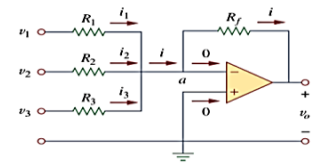
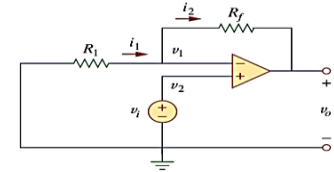
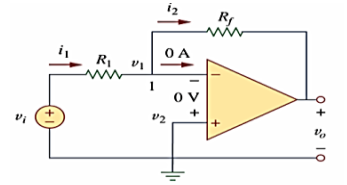
Voltage division

$$v_2 = \frac{R_2}{R_1 + R_2 + R_3} \cdot v_s$$

Current division

$$i_2 = \frac{G_2}{G_1 + G_2 + G_3} \cdot i_s$$

RC Circuits	RL Circuits
$i = C \frac{dv}{dt}$	$v = L \frac{di}{dt}$
$v = \frac{1}{C} \int_{t_0}^t i(\tau) d\tau + v(t_0)$	$i = \frac{1}{L} \int_{t_0}^t v(\tau) d\tau + i(t_0)$
$\tau = RC$	$\tau = L/R$
$v(t) = V + [v(0) - V] e^{-t/\tau}$	$i(t) = I + [i(0) - I] e^{-t/\tau}$



Standard Op-Amp

Circuits:

$$v_o = -\frac{R_f}{R_1} v_i$$

$$v_o = \left(1 + \frac{R_f}{R_1} \right) v_i$$

$$v_o = -\left(\frac{R_f}{R_1} v_1 + \frac{R_f}{R_2} v_2 + \frac{R_f}{R_3} v_3 \right)$$

$$v_o = \frac{R_2}{R_1} (v_2 - v_1)$$

$$\sin(\omega t) = \cos(\omega t - 90^\circ) = \cos\left(\omega t - \frac{\pi}{2}\right)$$

$$\cos(\omega t) = \sin(90^\circ - \omega t) = \sin\left(\frac{\pi}{2} - \omega t\right)$$

$$\sin(\omega t + 180^\circ) = -\sin(\omega t)$$

Polar to rectangular

$$x = r \cos \phi$$

$$y = r \sin \phi$$

$$z = r(\cos \phi + j \sin \phi)$$

Rectangular to polar

$$r = \sqrt{x^2 + y^2} \quad \phi = \tan^{-1} \frac{y}{x}$$

$$z = \sqrt{x^2 + y^2} \angle \tan^{-1} \frac{y}{x}$$

$$\mathbf{Z} = R$$

$$\mathbf{Z} = \frac{1}{j\omega C}$$

$$\mathbf{Z} = j\omega L$$

Maximum power transfer:

$$P_{L_{\max}} = \frac{v_s^2}{4R_t}$$