

CPE201

Digital Design

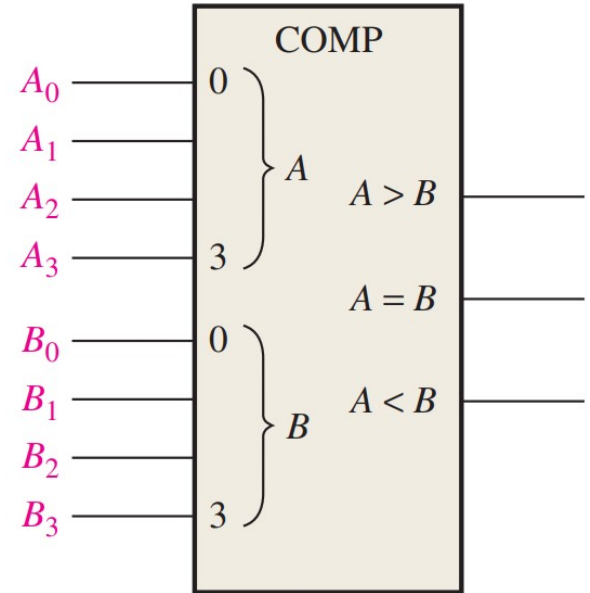
By Benjamin Haas

Class 15: Comparators and Decoders/Encoders



Comparator

- End Goal:
 - 4-bit input numbers
 - $<$, $>$, $=$ outputs



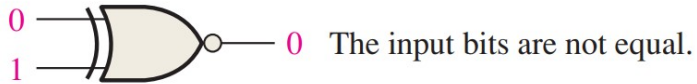
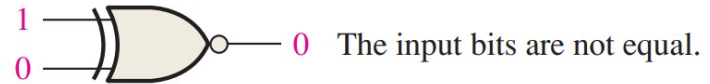
Starting Small

- 1-bit
 - $A < B$
 - $A = B$
 - $A > B$



Equality

- XNOR (A B)



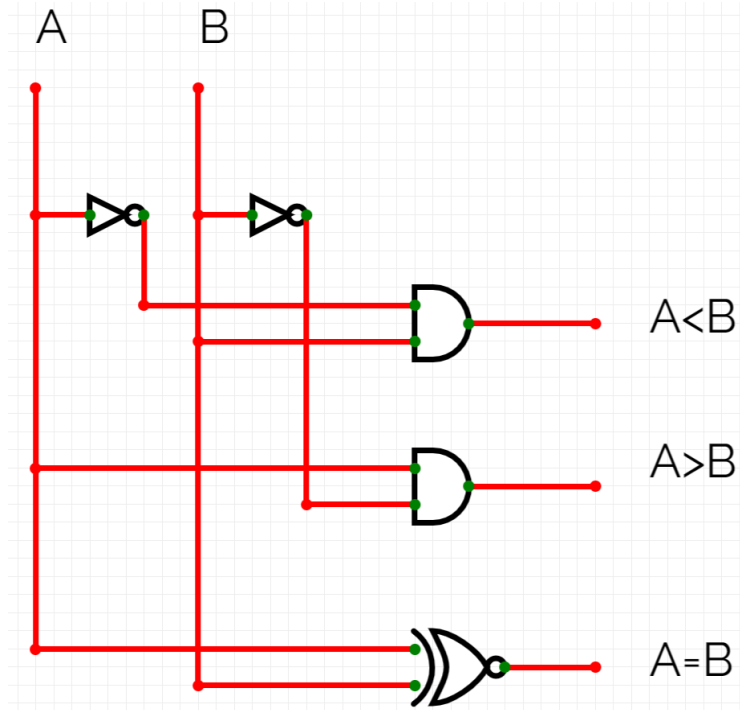
Truth Table

A	B	$A < B$	$A = B$	$A > B$
0	0	0	1	0
0	1	1	0	0
1	0	0	0	1
1	1	0	1	0

- $A < B = A'B$
- $A = B = A'B' + AB = A \oplus B$
- $A > B = AB'$



Circuit



- $A < B = A'B$
- $A = B = A'B + AB'$
- $A > B = AB'$



2-bit Comparator

- Same process

A1	A0	B1	B0	A< B	A= B	A> B
0	0	0	0	0	1	0
0	0	0	1	1	0	0
0	0	1	0	1	0	0
0	0	1	1	1	0	0
0	1	0	0	0	0	1
0	1	0	1	0	1	0
0	1	1	0	1	0	0

A1	A0	B1	B0	A< B	A= B	A> B
1	0	0	0	0	0	1
1	0	0	1	0	0	1
1	0	1	0	0	1	0
1	0	1	1	1	0	0
1	1	0	0	0	0	1
1	1	0	1	0	0	1
1	1	1	0	0	0	1



Karnaugh Maps

A > B

B1B0 \ A1A0	00	01	11	10
00	0	0	0	0
01	1	0	0	0
11	1	1	0	1
10	1	1	0	0

Groupings for A > B:

- Blue box: (01, 00), (11, 00)
- Red box: (11, 00), (11, 01)
- Black box: (11, 01), (10, 01)
- Red box: (11, 01), (11, 11)
- Black box: (11, 11), (10, 11)
- Black box: (10, 11), (10, 10)
- Black box: (10, 10), (00, 10)
- Black box: (00, 10), (00, 01)

A = B

B1B0 \ A1A0	00	01	11	10
00	1	0	0	0
01	0	1	0	0
11	0	0	1	0
10	0	0	0	1

Groupings for A = B:

- Blue circle: (00, 00)
- Green circle: (01, 01)
- Brown circle: (11, 11)
- Red circle: (10, 10)

A < B

B1B0 \ A1A0	00	01	11	10
00	0	1	1	1
01	0	0	1	1
11	0	0	0	0
10	0	0	1	0

Groupings for A < B:

- Purple box: (01, 00), (11, 00)
- Blue box: (11, 00), (11, 01)
- Blue box: (11, 01), (10, 01)
- Blue box: (11, 01), (11, 11)
- Blue box: (11, 11), (10, 11)
- Blue box: (10, 11), (10, 10)
- Blue box: (10, 10), (00, 10)
- Blue box: (00, 10), (00, 01)

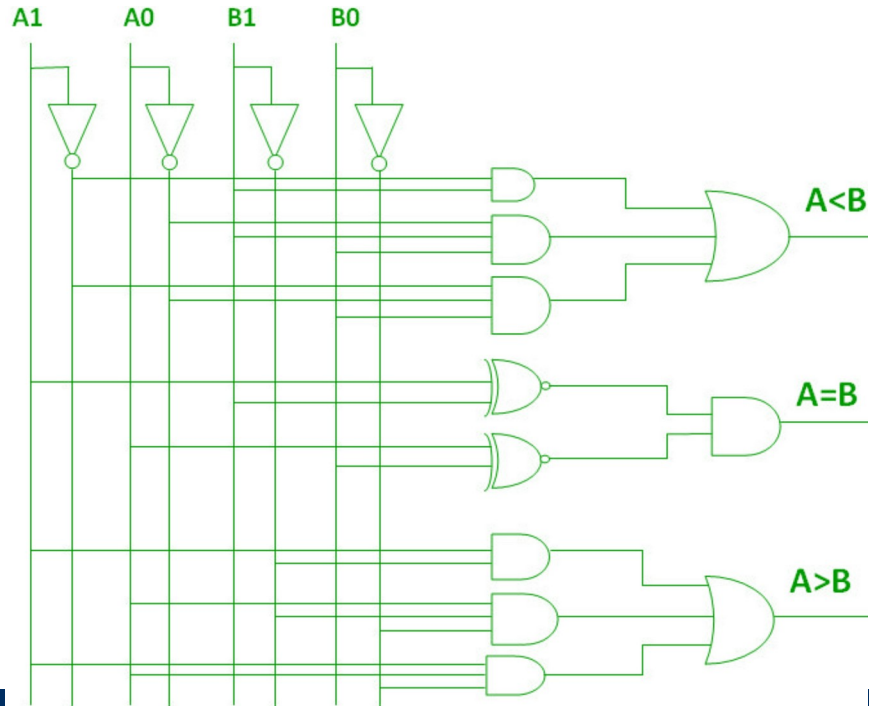


Boolean Expressions

- $A > B: A1B1' + A0B1'B0' + A1A0B0'$
- $A = B: A1'A0'B1'B0' + A1'A0B1'B0 + A1A0B1B0 + A1A0'B1B0'$
- $: A1'B1' (A0'B0' + A0B0) + A1B1 (A0B0 + A0'B0')$
- $: (A0B0 + A0'B0') (A1B1 + A1'B1')$
- $: (A0 \oplus B0) (A1 \oplus B1)$
- $A < B: A1'B1 + A0'B1B0 + A1'A0'B0$



Circuit



Generalize

- $A > B$
 - If $A_1 = 1$ and $B_1 = 0$
 - If $A_1 = B_1$ and $A_0 = 1$ and $B_0 = 0$
 - $A_1 = B_1$ means when they are both 0 and both 1
- $A < B$
 - If $A_1 = 0$ and $B_1 = 1$
 - If $A_1 = B_1$ and $A_0 = 0$ and $B_0 = 1$
- $A = B$
 - $(A_1 \ B_1) (A_0 \ B_0)$

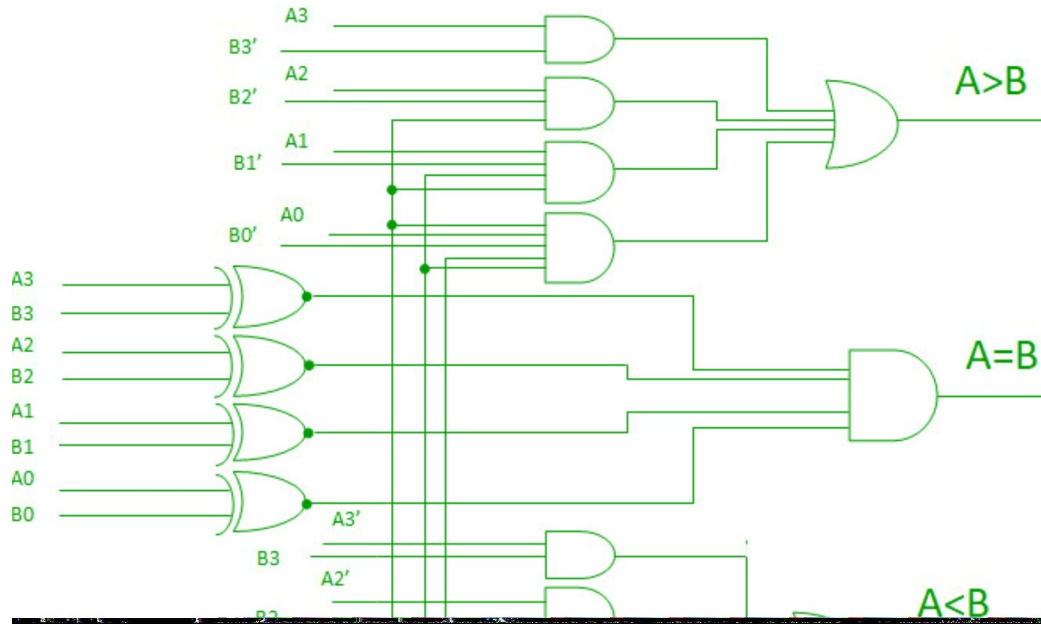


4-bit Comparator

- Use generalized rules
 - 8-bits is too many inputs for a Karnaugh map
 - Create a circuit from the rules
- $A > B$
 - If $A_3 = 1$ and $B_3 = 0$
 - If $A_3 = B_3$ and $A_2 = 1$ and $B_2 = 0$
 - If $A_3 = B_3$, $A_2 = B_2$ and $A_1 = 1$ and $B_1 = 0$
 - If $A_3 = B_3$, $A_2 = B_2$, $A_1 = B_1$ and $A_0 = 1$ and $B_0 = 0$

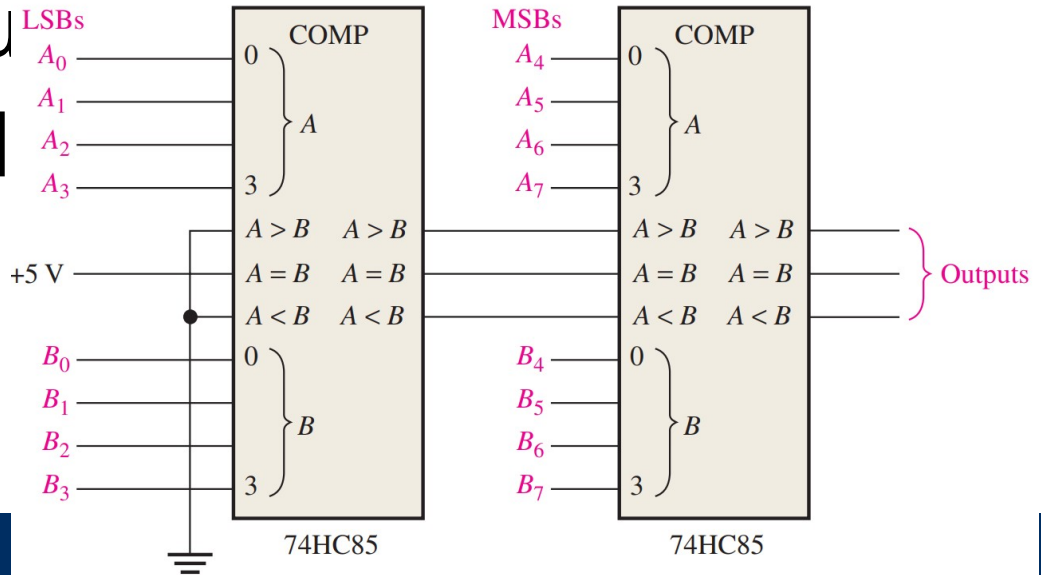


4-bit Comparator



Larger Comparators

- Input AND output comparator signals to ripple the result
- Inputs treated as 5th bit



An 8-bit magnitude comparator using two 74HC85s.

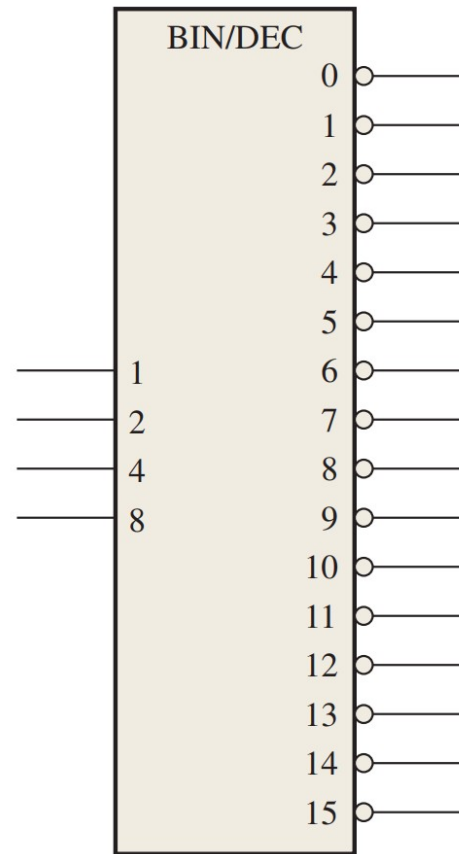
Comparator Applications

- Sensors
 - Temperature, position compared to a setting
- Motor control
 - Like in 3-D printers
- Password verification



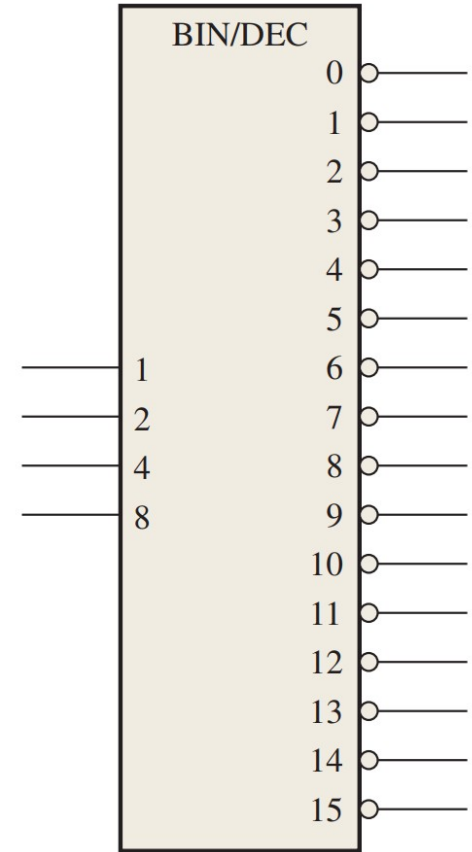
Decoders

- An input combination activates one output
- n inputs, 2^n outputs
 - 1 to 2, 2 to 4, 3 to 8, 4 to 16



Active High vs Active Low

- Active High = ON means 1
- Active Low = ON means 0
- This chip is active low



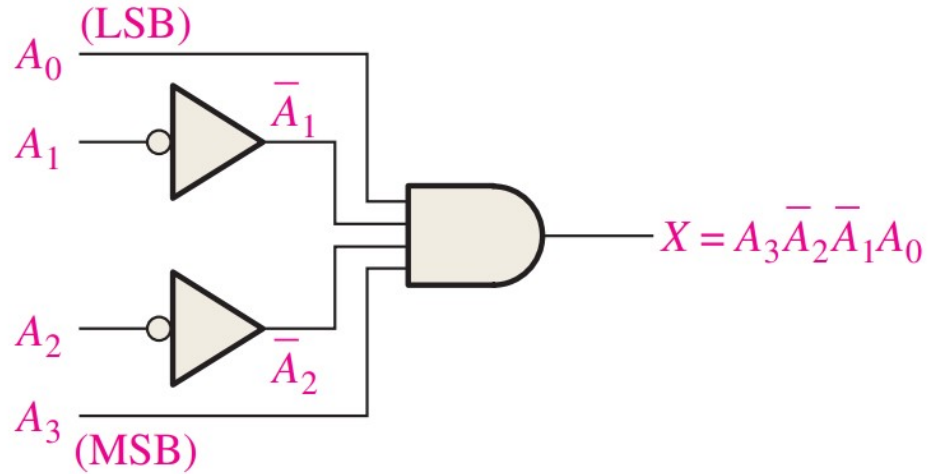
Active Low Decoder

Decimal Digit	Binary Inputs				Decoding Function	Outputs															
	A ₃	A ₂	A ₁	A ₀		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	$\overline{A_3}\overline{A_2}\overline{A_1}\overline{A_0}$	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
1	0	0	0	1	$\overline{A_3}\overline{A_2}\overline{A_1}A_0$	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	
2	0	0	1	0	$\overline{A_3}\overline{A_2}A_1\overline{A_0}$	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	
3	0	0	1	1	$\overline{A_3}\overline{A_2}A_1A_0$	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	



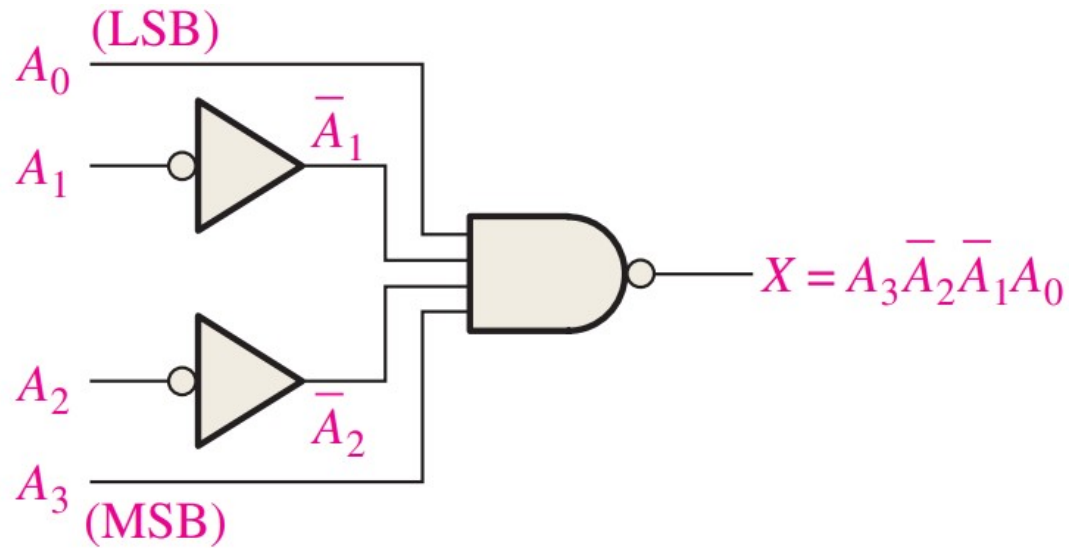
Basics

- Input = 1001
- Active high output
- AND



Basics

- Input = 1001
- Active low output
- NAND
- Chip would have 16 of these



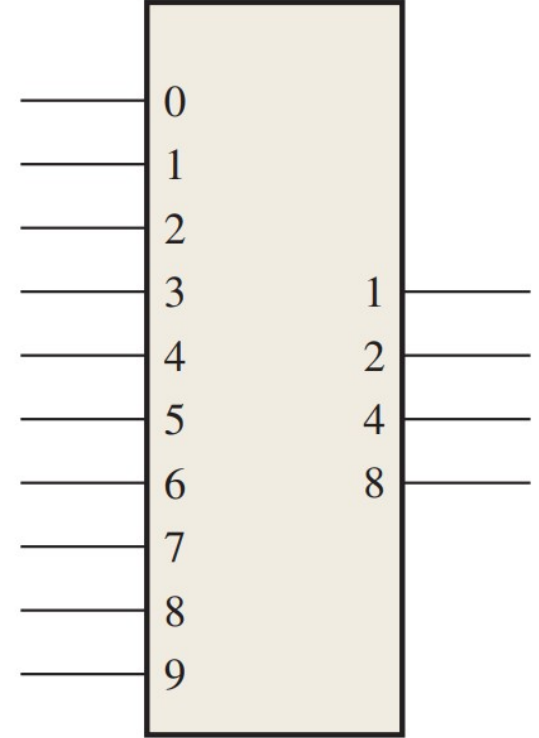
Applications

- Memory Addressing
 - Turn on a specific bank of memory
- Turn specific things on and off
 - Ex TV vs projector screen



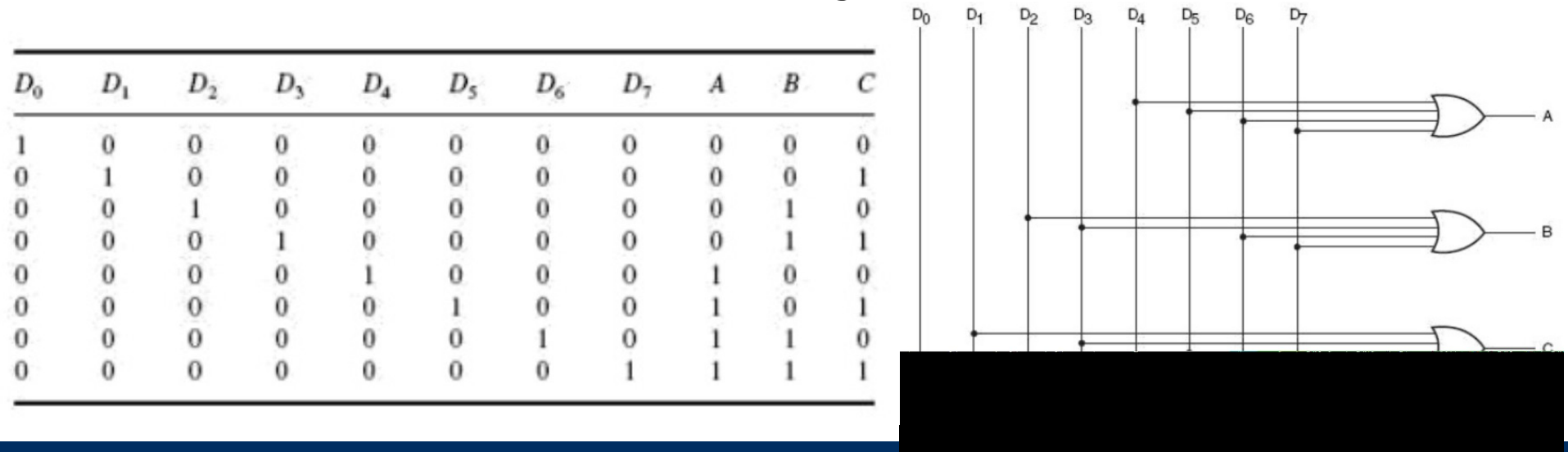
Encoders

- Reverse of decoder
- 2^n inputs, n outputs



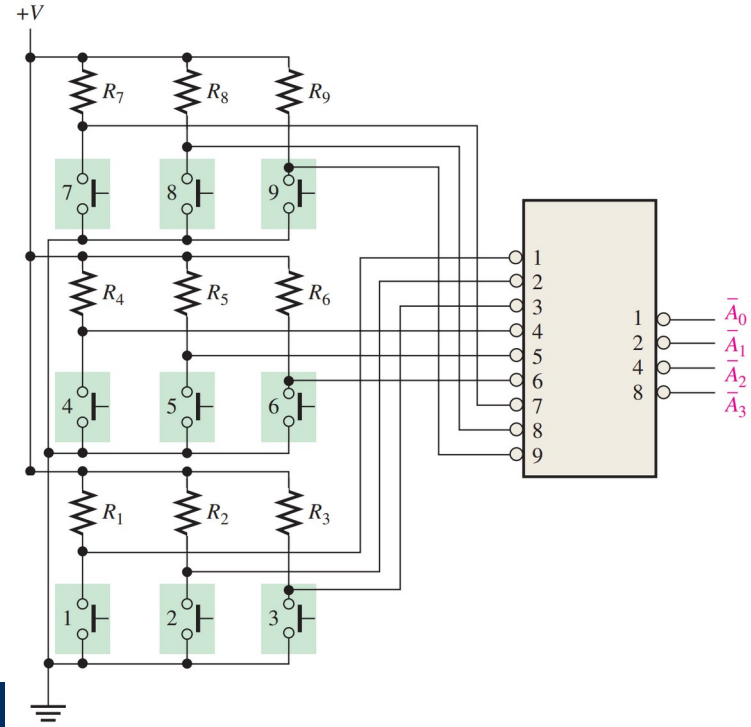
Basics

- 8 to 3 encoder (binary to octal)



Application

- Keypad
- Encoded output is easier to transmit and use



Reading

- This lecture
 - Sections 6.4-6.6
- Next lecture
 - Sections 6.8-6.10

