



# Lab Manual

## Practical and Skills Development

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# CERTIFICATE

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THE ASSIGNMENT ENTERED IN THIS REPORT HAVE BEEN  
SATISFACTORILY PERFORMED BY

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**Course Code** : CSE1021

**School Name** : VIT BHOPAL

**Slot** : B11+B12+B13

**Class ID** : BL2025260100796

**Semester** : FALL 2025/26

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### Practical Index

S. No.	Title of Practical	Date of Submission	Signature of Faculty
1	Write a function Lucas Numbers Generator <code>lucas_sequence(n)</code> that generates the first n Lucas numbers (similar to Fibonacci but starts with 2, 1).	16-11-2025	
2	Write a function for Perfect Powers Check <code>is_perfect_power(n)</code> that checks if a number can be expressed as $a^b$ where $a > 0$ and $b > 1$ .	16-11-2025	
3	Write a function Collatz Sequence Length <code>collatz_length(n)</code> that returns the number of steps for n to reach 1 in the Collatz conjecture.	16-11-2025	

<b>4</b>	Write a function Polygonal Numbers <code>polygonal_number(s, n)</code> that returns the n-th s-gonal number.	<b>16-11-2025</b>	
<b>5</b>	Write a function Carmichael Number Check <code>is_carmichael(n)</code> that checks if a composite number n satisfies $a^{n-1} \equiv 1 \pmod n$ for all a coprime to n.	<b>16-11-2025</b>	
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**Practical No: 1**

**Date: 16-11-2025**

**TITLE: Lucas Numbers**

**AIM/OBJECTIVE(s) :** Write a function Lucas Numbers Generator `lucas_sequence(n)` that generates the first n Lucas numbers (similar to Fibonacci but starts with 2,1).

**METHODOLOGY & TOOL USED:**

The Lucas sequence

was generated by applying an iterative approach that begins from the known base values of the Lucas series: 2 and 1. Instead of using a recursive method (which is slower and consumes more memory), a loop was used to efficiently compute the next terms using the formula:

```
main.py  Run  Output
1 # Online Python compiler (interpreter) to run Python online.
2 # Write Python 3 code in this online editor and run it.
3 import time
4 import tracemalloc
5
6 def lucas_sequence(n):
7     if n <= 0:
8         return []
9     if n == 1:
10        return [2]
11    seq = [2, 1]
12    for _ in range(2, n):
13        seq.append(seq[-1] + seq[-2])
14    return seq
15
16 n = int(input("Enter n for Lucas Sequence: "))
17
18 tracemalloc.start()
19 start = time.time()
20
21 result = lucas_sequence(n)
22
23 end = time.time()
24 current, peak = tracemalloc.get_traced_memory()
25 tracemalloc.stop()
26
27 print("Lucas Sequence:", result)
28 print("Execution Time:", end - start, "seconds")
29 print("Memory Used:", peak/1024, "KB")
30
```

```
Enter n for Lucas Sequence: 6
Lucas Sequence: [2, 1, 3, 4, 7, 11]
Execution Time: 3.0517578125e-05 seconds
Memory Used: 0.1015625 KB

=== Code Execution Successful ===
```

$$L(n) = L(n-1) + L(n-2).$$

The algorithm stores each computed term in a list so that the entire sequence up to the nth term can be returned. Time and memory measurements were added to evaluate performance.

### Tool Used:

**Programming Language:** Python

**IDE / Environment:** IDLE (Python 3.x) or any Python-supported IDE  
such as Jupyter Notebook

### BRIEF DESCRIPTION:

The Lucas sequence is similar to the Fibonacci sequence but has different starting values. This question demonstrates the concept of linear recurrence relations and how sequences can be built using previously computed elements.

### RESULTS ACHIEVED:

#### Example Output:

Enter n for Lucas Sequence: 6

Lucas Sequence: [2, 1, 3, 4, 7, 11]

Execution Time:

2.2172927856445312e-05 seconds

Memory Used: 0.1015625 KB

**DIFFICULTY FACED BY STUDENT:**

- ❑ Understanding why Lucas numbers begin with 2 and 1 instead of 0 and 1.
- ❑ Avoiding recursion to prevent stack overflow for large n.
- ❑ Managing list indexing carefully.

**SKILLS ACHIEVED:**

- ❑ Understanding of recurrence relations.
- ❑ Ability to convert mathematical formulas into iterative algorithms.
- ❑ Measuring algorithm performance.

**Practical No: 2****Date: 16-11-2025****TITLE:** Perfect Power Detection**AIM/OBJECTIVE(s):** Write a function for Perfect Powers Check

is\_perfect\_power( $n$ ) that checks if a number can be expressed as  $ab$  where  $a > 0$  and  $b > 1$ .

**METHODOLOGY & TOOL USED:**

The method involves checking if a number  $n$  can be expressed as  $a^b$ , where  $a > 1$  and  $b > 1$ . The algorithm calculates possible exponents using logarithms and tests each base by estimating  $a$  and verifying that  $a^b$  equals  $n$ . The approach limits the exponent range to  $\log_2(n)$ , which optimizes the process.

**Tool Used:****Programming Language:** Python

**IDE / Environment:** IDLE (Python 3.x) or any Python-supported IDE  
such as Jupyter Notebook

**BRIEF DESCRIPTION:**

A perfect power is a number that can be written in exponential form. This code systematically checks for such a representation by iterating through possible exponents and testing candidate bases.

**RESULTS ACHIEVED:****Example Output:**

Enter a number: 9

Perfect Power? True

Execution Time: 4.863739013671875e-05 seconds

Memory Used: 0.8203125 KB

```
main.py 1 # Online Python compiler (interpreter) to run Python online.
2 # Write Python 3 code in this online editor and run it.
3 import time
4 import tracemalloc
5 import math
6
7 def is_perfect_power(n):
8     if n <= 1:
9         return False
10    for b in range(2, int(math.log2(n)) + 2):
11        a = round(n ** (1 / b))
12        if a ** b == n:
13            return True
14    return False
15
16 n = int(input("Enter a number: "))
17
18 tracemalloc.start()
19 start = time.time()
20
21 result = is_perfect_power(n)
22
23 end = time.time()
24 current, peak = tracemalloc.get_traced_memory()
25 tracemalloc.stop()
26
27 print("Perfect Power?", result)
28 print("Execution Time:", end - start, "seconds")
29 print("Memory Used:", peak/1024, "KB")
30
31
```

Output

```
Enter a number: 9
Perfect Power? True
Execution Time: 4.863739013671875e-05 seconds
Memory Used: 0.8203125 KB

=== Code Execution Successful ===
```

### DIFFICULTY FACED BY STUDENT:

- ❑ Handling floating-point rounding issues when extracting roots.
- ❑ Understanding the concept of expressing numbers in exponential form.
- ❑ Ensuring that bases and exponents remain valid integers.

### SKILLS ACHIEVED:

Working with logarithmic functions.

Improving code efficiency by reducing unnecessary checks.

Handling numerical precision and rounding behavior.



### Practical No: 3

Date: 16-11-2025

**TITLE:** Collatz\_Length(n)

**AIM/OBJECTIVE(s):** Write a function Collatz Sequence Length collatz\_length(n) that returns the number of steps for n to reach 1 in the Collatz conjecture.

#### METHODOLOGY & TOOL USED:

Used the generalized polygonal number formula:

**$P(s, n) = ((s-2) \cdot n \cdot (n-1)) / 2 + n$**  The program takes two inputs:

s → number of sides

n → term index

The formula was applied directly for fast computation, followed by performance measurement.

#### Tool Used:

**Programming Language:** Python

**IDE / Environment:** IDLE (Python 3.x) or any Python-supported IDE  
such as Jupyter Notebook

#### BRIEF DESCRIPTION:

The multiplicative\_persistence(n) function measures how many steps it takes for a number's digits to multiply into a single digit. For instance, if  $n = 39$ , the process goes as follows:  $3 \times 9 = 27$ ,  $2 \times 7 = 14$ ,  $1 \times 4 = 4$ . Thus, the persistence is 3. This function provides insights into digit manipulation, repetition, and convergence in mathematics and programming.

## RESULTS ACHIEVED:

### Example Output:

Enter number: 8

Steps: 3

Execution Time: 1.0967254638671875e-05 seconds

Memory Used: 0.0 KB

```
main.py  [Icons]  Run  Output  Clear
1 # Online Python compiler (interpreter) to run Python online.
2 # Write Python 3 code in this online editor and run it.
3 import time
4 import tracemalloc
5
6 def collatz_length(n):
7     steps = 0
8     while n != 1:
9         n = n//2 if n%2==0 else 3*n+1
10        steps += 1
11    return steps
12
13 n = int(input("Enter number: "))
14
15 tracemalloc.start()
16 start = time.time()
17
18 result = collatz_length(n)
19
20 end = time.time()
21 current, peak = tracemalloc.get_traced_memory()
22 tracemalloc.stop()
23
24 print("Steps:", result)
25 print("Execution Time:", end - start, "seconds")
26 print("Memory Used:", peak/1024, "KB")
27
28
```

Enter number: 8  
Steps: 3  
Execution Time: 1.1444091796875e-05 seconds  
Memory Used: 0.0 KB  
=== Code Execution Successful ===

## DIFFICULTY FACED BY STUDENT:

- ❑ Understanding how values can rapidly grow before shrinking.
- ❑ Avoiding infinite loops by setting correct conditions.
- ❑ Handling large integers efficiently.

## SKILLS ACHIEVED:

- ❑ Iterative algorithm design.

- ❑ Problem-solving with conditional logic.
- ❑ Understanding unpredictable mathematical behavior in sequences.

### Practical No: 4

**Date: 16-11-2025**

**TITLE:** Polygonal Number Calculator

**AIM/OBJECTIVE(s):** Write a function Polygonal Numbers  
polygonal\_number(s,n) that returns the n-th s-gonal number.

**METHODOLOGY & TOOL USED:**

Used the generalized polygonal number formula:

$$P(s, n) = \frac{(s-2) \cdot n \cdot (n-1)}{2} + n$$

The

program takes two inputs:

$s \rightarrow$  number of sides

$n \rightarrow$  term index

The formula was applied directly for fast computation, followed by performance measurement.

**Tool Used:**



**Programming Language:** Python

**IDE / Environment:** IDLE (Python 3.x) or any Python-supported IDE  
such as Jupyter Notebook

**BRIEF DESCRIPTION:**

Polygonal numbers generalize triangular, square, and pentagonal numbers. The formula produces the  $n$ th term for any polygon with  $s$  sides.

**RESULTS ACHIEVED:**

**Example Output:**

Enter s: 8

Enter n: 8

Polygonal Number: 176

Execution Time: 1.3828277587890625e-05 seconds

Memory Used: 0.75 KB

### DIFFICULTY FACED BY STUDENT:

Understanding generalization from simple shapes to s-sided shapes.

```
main.py  [Icons]  Share  Run  Output  Clear
1 # Online Python compiler (interpreter) to run Python online.
2 # Write Python 3 code in this online editor and run it.
3 import time
4 import tracemalloc
5
6 def polygonal_number(s, n):
7     return ((s - 2) * n * (n - 1)) // 2 + n
8
9 s = int(input("Enter s: "))
10 n = int(input("Enter n: "))
11
12 tracemalloc.start()
13 start = time.time()
14
15 result = polygonal_number(s, n)
16
17 end = time.time()
18 current, peak = tracemalloc.get_traced_memory()
19 tracemalloc.stop()
20
21 print("Polygonal Number:", result)
22 print("Execution Time:", end - start, "seconds")
23 print("Memory Used:", peak/1024, "KB")
24
```

Enter s: 8  
Enter n: 8  
Polygonal Number: 176  
Execution Time: 1.4066696166992188e-05 seconds  
Memory Used: 0.75 KB  
=== Code Execution Successful ===

Deriving confidence in using the formula without deriving it manually.

### Skills Achieved:

Using mathematical formulas in programming.

Handling multi-parameter

functions.

Applying generalizations across number families.

### **Practical No: 5**

**Date: 16-11-2025**

**TITLE:** Carmichael Number Checker

**AIM/OBJECTIVE(s):** Write a function Carmichael Number  
Check `is_carmichael(n)` that checks if a composite number  
`n` satisfies  $a^{n-1} \equiv 1 \pmod n$  for all `a` coprime to `n`.

**METHODOLOGY & TOOL USED:**

Implemented **Korselt's Criterion**, which states that a composite number  $n$  is Carmichael if:

It is square-free

$(n - 1)$  is divisible by  $(p - 1)$  for every prime divisor  $p$  of  $n$

The program performs primality checks, factor checks, and the required modular conditions.

**Tool Used:**

**Programming Language:** Python

**IDE / Environment:** IDLE (Python 3.x) or any Python-supported IDE  
such as Jupyter Notebook

**BRIEF DESCRIPTION:**

Carmichael numbers are special composite numbers that pass Fermat's primality test, making them important in cryptography.

**RESULTS ACHIEVED:****Example Output:**

Enter number: 9

Carmichael? False

Execution Time: 4.38690185546875e-05 seconds

Memory Used: 0.75 KB

```
2 # Please Python 3 code in this online editor and run it.
3 import time
4 import tracemalloc
5
6 def is_prime(x):
7     if x < 2:
8         return False
9     for i in range(2, int(x**0.5)+1):
10         if x % i == 0:
11             return False
12         return True
13
14 def is_carmichael(n):
15     if n < 2 or is_prime(n):
16         return False
17     temp = n
18     for p in range(2, int(n**0.5) + 1):
19         if temp % p == 0:
20             if (temp // p) % p == 0:
21                 return False
22             if (n - 1) % (p - 1) != 0:
23                 return False
24     return True
25
26 n = int(input("Enter number: "))
27
28 tracemalloc.start()
29 start = time.time()
30
31 result = is_carmichael(n)
32
33 end = time.time()
34 current, peak = tracemalloc.get_traced_memory()
35 tracemalloc.stop()
36
37 print("Carmichael?", result)
38 print("Execution Time:", end - start, "seconds")
39 print("Memory Used:", peak/1024, "KB")
40
```

```
* Enter number: 9
Carmichael? False
Execution Time: 7.03348083496094e-05 seconds
Memory Used: 0.75 KB
*** Code Execution Successful ***
```

### **DIFFICULTY FACED BY STUDENT:**

**Conceptual confusion between primes and Carmichael numbers.**

**Understanding “square-free” requirement.**

**Implementing multiple mathematical conditions together.**

### **SKILLS ACHIEVED:**

**Deep number theory understanding.**

**Composite number characterization.**



**Testing multiple**



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**conditions efficiently.**