Charotar University of Science and Technology [CHARUSAT] Faculty of Technology and Engineering

U & P U. Patel Department of Computer Engineering

Subject: CE 349 Theory of Computation Unit Test-I

Semester: 6th B.Tech. (CE) Maximum Marks: 30
Date: 21/01/2020 (Tuesday) Time: 09:10 to 10:10 a.m.

Q:1 Answer following questions

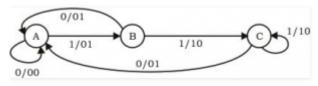
[10]

- **1** Why Theory of Computation is included as one of the core subjects of Bachelors of Computer Engineering under any university?
- **2** Power of DFA, NFA and NFA-^ is same, justify the statement.
- 3 Complement of NFA is not necessarily complement of that language, justify the statement.
- 4 Define finite automata. List out the practical applications of finite automata.
- **5** What is the usefulness of NFA with ϵ move? Why is minimization of finite automata necessary?

Q:2 Answer following questions

[10]

(a) The Finite state machine described by the following state diagram with A as starting state, where an arc label is x / y and x stands for 1-bit input and y stands for 2- bit output. What is the output generated by following mealy machine and also give justification for the same?



(b) Attempt Any TWO Questions.

[80]

- **1** Assume that $\epsilon \in \{a, b\}^*$. Write down regular expression (RE) for the string that
 - (i) contains almost two a's.
 - (ii) begin or end with aa or bb.
 - (iii) contains even number of a's.
 - (iv) a is immediately followed by bb.
- **2** Prove with PMI that for every $n \ge 1$,

$$7 + 13 + 19 + \dots + (6n + 1) = n(3n + 4)$$

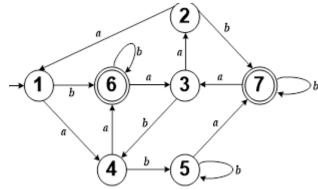
3 Draw the minimal DFA for the language $L = \{a^n b^m \mid n \ge 2, m \ge 1\}$

4 Design an equivalent DFA corresponding to the following NFA. NFA M =< { q_0, q_1, q_2, q_3, q_4 }, {0,1}, $\delta, q_0, \{q_2, q_4\}$ > where δ is as follows.

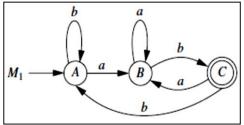
	Next State	
Present State	0	1
q_0	$\{q_0,q_3\}$	$\{q_0,q_1\}$
q_1	Ø	q_2
q_2	q_2	q_2
q_3	q_4	Ø
\overline{q}_4	q_4	q_4

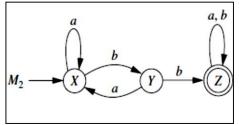
Q:3 Answer following questions [Any Two]

1 Apply Minimization method of DFA on the following DFA.



 $\begin{tabular}{lll} \bf 2 & Let \ M_1 \ and \ M_2 \ are \ the \ FA \ recognizing \ the \ languages \ L_1 \ and \ L_2 \ respectively \ , \\ shown \ in \ following \ figure: \ Draw \ FAs \ accepting \ L_1 \cup L_2 \ \ and \ \ L_1 - L_2. \end{tabular}$





3 Using Kleene's Theorem, Convert $(00 + 1)^*(10)^*(110)^*$ regular expression into NFA- $^{\circ}$.

[10]