

Charotar University of Science and Technology [CHARUSAT]

Faculty of Technology and Engineering

U & P U. Patel Department of Computer Engineering

Subject: CE 349 Theory of Computation

Unit Test-I solution

Semester: 6th B.Tech. (CE)

Maximum Marks: 30

Date: 21/01/2020 (Tuesday)

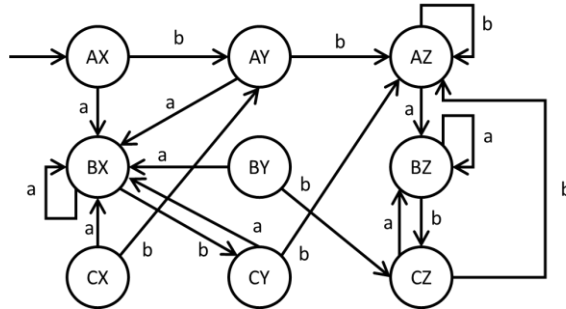
Time: 09:10 to 10:10 a.m.

Q:2	Answer following questions	[10]
(a)	Print addition of current bit and previous bit	[02]
(b)	Attempt Any TWO Questions.	[08]
1	(i) $b^* b^* a b^* b^* a b^* a b^*$ OR $b^* a^? b^* a^? b^*$ (ii) $(aa bb) (a b)^* (aa bb)$ (iii) $b^* (ab^*a)^* b^*$ OR $b^* (ab^*ab^*)^*$ (iv) $(b abb)^*$	
2	<p>$P(n) : 7 + 13 + 19 + \dots + (6n+1) = n(3n+4)$ for $n \geq 1$</p> <p>Basic step: For $n=1$ $P(1) : 6(1)+1 = 1(3(1)+4)$ $LHS = 6(1)+1 = 6+1 = 7$ $RHS = 1(3(1)+4) = 3+4 = 7$ $LHS = RHS$ For $P(1)$ is true</p> <p>Induction hypothesis: $P(k) : 7 + 13 + 19 + \dots + (6k+1) = k(3k+4)$ is true for every k where $1 \leq k \leq n$</p> <p>Statement to be prove in induction step: $P(k) : 7 + 13 + 19 + \dots + (6(k+1)+1) = (k+1) (3(k+1)+4)$</p> <p>Proof of induction step: LHS $= 7 + 13 + 19 + \dots + (6(k+1)+1)$ $= 7 + 13 + 19 + \dots + (6k+1) + (6(k+1)+1)$ $= k(3k+4) + (6(k+1)+1)$ $= 3k^2 + 4k + 6k + 6 + 1$ $= 3k^2 + 10k + 7$</p> <p>RHS $= (k+1) (3(k+1)+4)$ $= 3(k+1)^2 + 4(k+1)$ $= 3(k^2 + 2k + 1) + 4k + 4$ $= 3k^2 + 6k + 3 + 4k + 4$</p>	

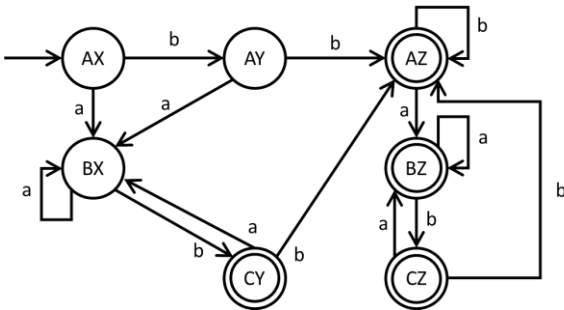
	$=3k^2 + 10k + 7$ So LHS = RHS So $P(K+1)$ is true So $P(n)$ is true for all $n \geq 1$																															
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4	<table border="1"> <thead> <tr> <th></th><th>0</th><th>1</th></tr> </thead> <tbody> <tr> <td>$\rightarrow \{q_0\}$</td><td>$\{q_0, q_3\}$</td><td>$\{q_0, q_1\}$</td></tr> <tr> <td>$\{q_0, q_3\}$</td><td>$\{q_0, q_3, q_4\}$</td><td>$\{q_0, q_1\}$</td></tr> <tr> <td>$\{q_0, q_1\}$</td><td>$\{q_0, q_3\}$</td><td>$\{q_0, q_1, q_2\}$</td></tr> <tr> <td>* $\{q_0, q_3, q_4\}$</td><td>$\{q_0, q_3, q_4\}$</td><td>$\{q_0, q_1, q_4\}$</td></tr> <tr> <td>* $\{q_0, q_1, q_2\}$</td><td>$\{q_0, q_2, q_3\}$</td><td>$\{q_0, q_1, q_2\}$</td></tr> <tr> <td>* $\{q_0, q_1, q_4\}$</td><td>$\{q_0, q_3, q_4\}$</td><td>$\{q_0, q_1, q_2, q_4\}$</td></tr> <tr> <td>* $\{q_0, q_2, q_3\}$</td><td>$\{q_0, q_2, q_3, q_4\}$</td><td>$\{q_0, q_1, q_2\}$</td></tr> <tr> <td>* $\{q_0, q_1, q_2, q_4\}$</td><td>$\{q_0, q_2, q_3, q_4\}$</td><td>$\{q_0, q_1, q_2, q_4\}$</td></tr> <tr> <td>* $\{q_0, q_2, q_3, q_4\}$</td><td>$\{q_0, q_2, q_3, q_4\}$</td><td>$\{q_0, q_1, q_2, q_4\}$</td></tr> </tbody> </table>		0	1	$\rightarrow \{q_0\}$	$\{q_0, q_3\}$	$\{q_0, q_1\}$	$\{q_0, q_3\}$	$\{q_0, q_3, q_4\}$	$\{q_0, q_1\}$	$\{q_0, q_1\}$	$\{q_0, q_3\}$	$\{q_0, q_1, q_2\}$	* $\{q_0, q_3, q_4\}$	$\{q_0, q_3, q_4\}$	$\{q_0, q_1, q_4\}$	* $\{q_0, q_1, q_2\}$	$\{q_0, q_2, q_3\}$	$\{q_0, q_1, q_2\}$	* $\{q_0, q_1, q_4\}$	$\{q_0, q_3, q_4\}$	$\{q_0, q_1, q_2, q_4\}$	* $\{q_0, q_2, q_3\}$	$\{q_0, q_2, q_3, q_4\}$	$\{q_0, q_1, q_2\}$	* $\{q_0, q_1, q_2, q_4\}$	$\{q_0, q_2, q_3, q_4\}$	$\{q_0, q_1, q_2, q_4\}$	* $\{q_0, q_2, q_3, q_4\}$	$\{q_0, q_2, q_3, q_4\}$	$\{q_0, q_1, q_2, q_4\}$	
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1	0-equivalent [1 2 3 4 5] [6 7] 1-equivalent [1 2] [3] [4 5] [6 7] 2-equivalent [1] [2] [3] [4 5] [6 7]																															

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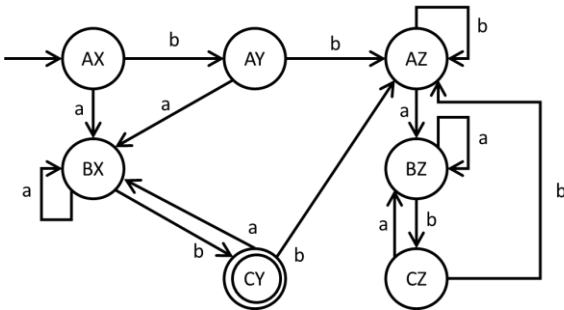
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AX	BX	AY
AY	BX	AZ
AZ	BZ	AZ
BX	BX	CY
BY	BX	CZ
BZ	BZ	CZ
CX	BX	AY
CY	BX	AZ
CZ	BZ	AZ



For L1 U L2



For L1 - L2



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