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17.18

g.

Suppose that the file is not ordered by the key field Ssn and we want to construct a B+-tree access structure (index) on Ssn. Calculate (i) the orders p and p_{leaf} of the B+-tree; (ii) the number of leaf-level blocks needed if blocks are approximately 69% full (rounded up for convenience); (iii) the number of levels needed if internal nodes are also 69% full (rounded up for convenience); (iv) the total number of blocks required by the B+-tree; and (v) the number of block accesses needed to search for and retrieve a record from the file—given its Ssn value—using the B+-tree.

i.

→ For order of non-leaf nodes:

- $p(P) + (p-1)(V_{\text{ssn}}) \leq 512$
- $p(6) + (p-1)(9) \leq 512$
- $6p + 9p - 9 \leq 512$
- $15p \leq 521$
- $P \leq 34.73$
- Therefore, order $(p) = 34$

→ For order of leaf node:

- $p(V_{\text{ssn}} + P_R) + P \leq 512$
- $p(9 + 7) + 6 \leq 512$
- $16p + 6 \leq 512$
- $16p \leq 506$
- $p \leq 31.62$
- Therefore, order $(p_{\text{leaf}}) = 31$

ii.

→ $0.69 * p_{\text{leaf}} = 0.69 * 31 = 22$. There will be 22 search keys per leaf node. The file is not ordered on that field so there will have to be a search record for each record in the file, i.e 30,000.

→ Number of leaf blocks = $\text{ceiling}(30,000 / 22)$
= 1364 blocks

iii.

→ $0.69 * p = 0.69 * 34 = 24$. There will be 24 block pointers per internal node

→ There are 1364 blocks in the first level of the tree, so there must be 1364 block pointers in the second level.

- $1364 / 24 = 57$ blocks in the second level.

→ Similarly, in the third level,

- $57/24 = 3$ blocks
- ➔ Finally, in the fourth level
 - $3/24 = 1$ block
- ➔ Therefore, the number of levels needed is 4.

- iv. 1st level = 1364
 2nd level = 57
 3rd level = 3
 4th level = 1

Therefore, the total blocks = $1364 + 57 + 3 + 1 = 1425$ blocks.

- v. 4 accesses are needed to traverse the levels. We also need 1 more access to get the primary record from the file. Therefore, 5 total block accesses

17.19

A PARTS file with Part# as the key field includes records with the following Part# values: 23, 65, 37, 60, 46, 92, 48, 71, 56, 59, 18, 21, 10, 74, 78, 15, 16, 20, 24, 28, 39, 43, 47, 50, 69, 75, 8, 49, 33, 38. Suppose that the search field values are inserted in the given order in a B+-tree of order $p = 4$ and pleaf = 3; show how the tree will expand and what the final tree will look like.

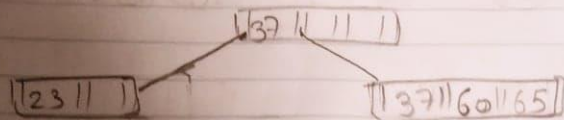
➔Please look below:

17-19 P=4, Pref=3

- Insert 23, 65, 37, 60

[23 | 37 | 65 |]

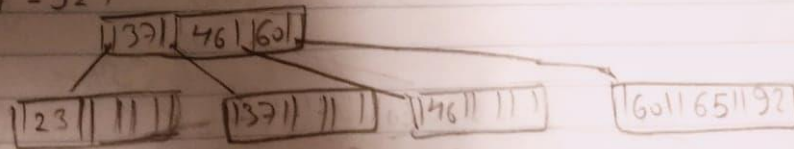
- Insert 60, 100



- Insert 46,



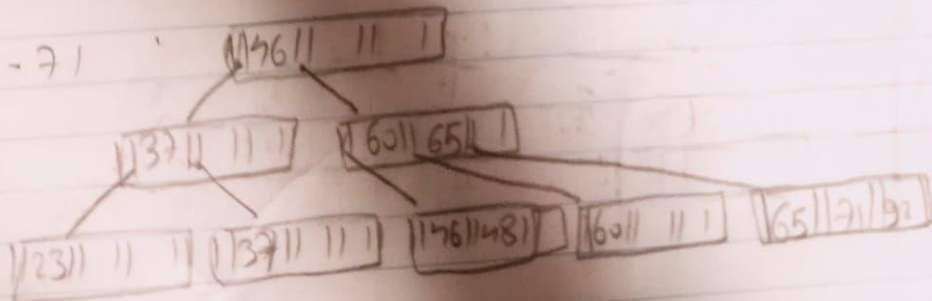
- Insert -92,



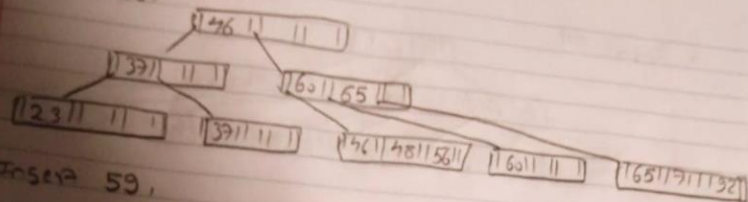
- Insert -48



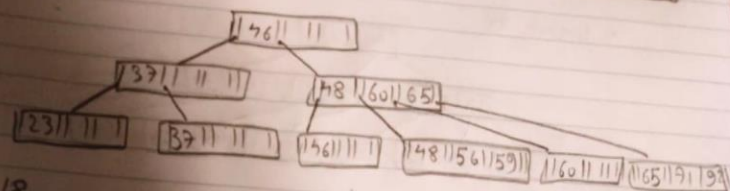
- Insert -71



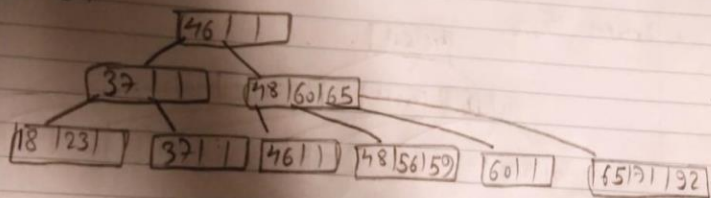
Insert 36,



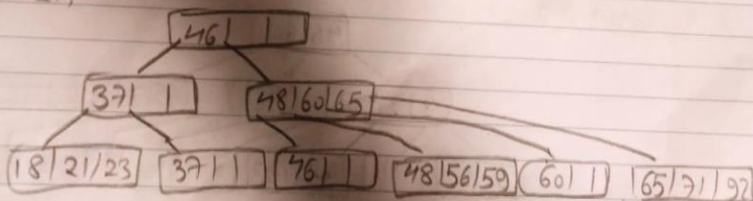
Insert 59,



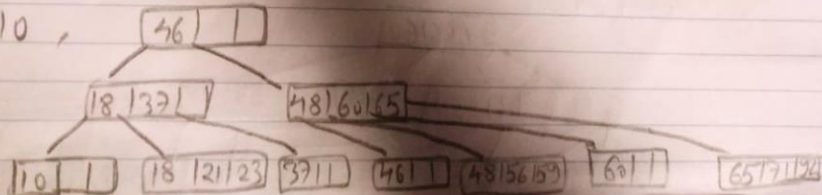
Insert 18,



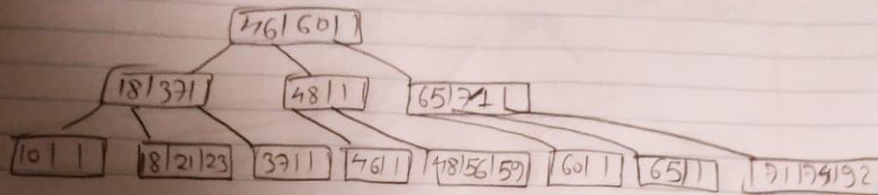
Insert 21,



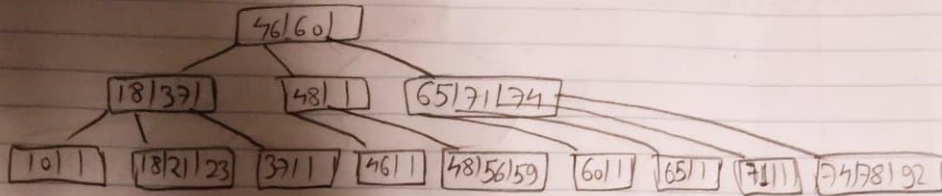
Insert 10,



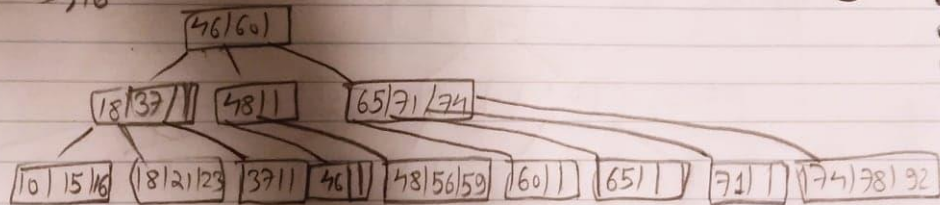
• Insert 74



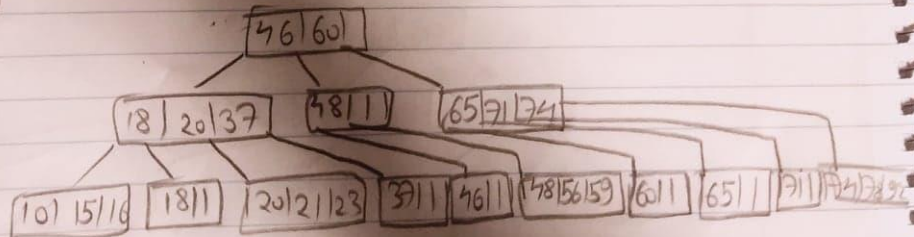
• Insert 78



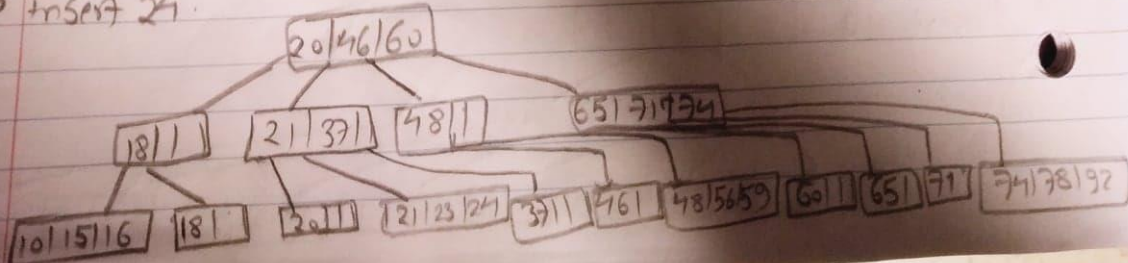
• Insert 15, 16



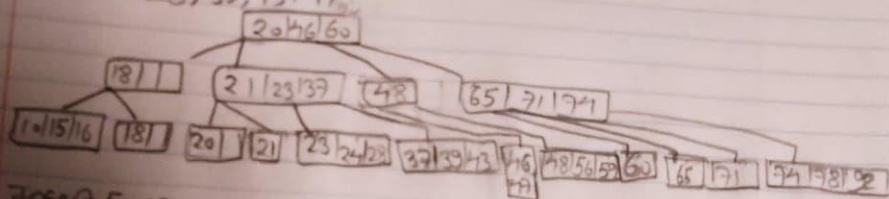
• Insert 20



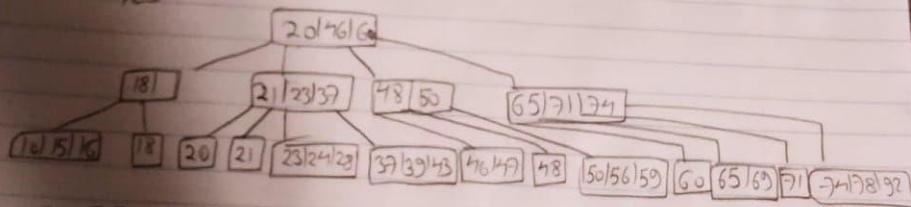
• Insert 21



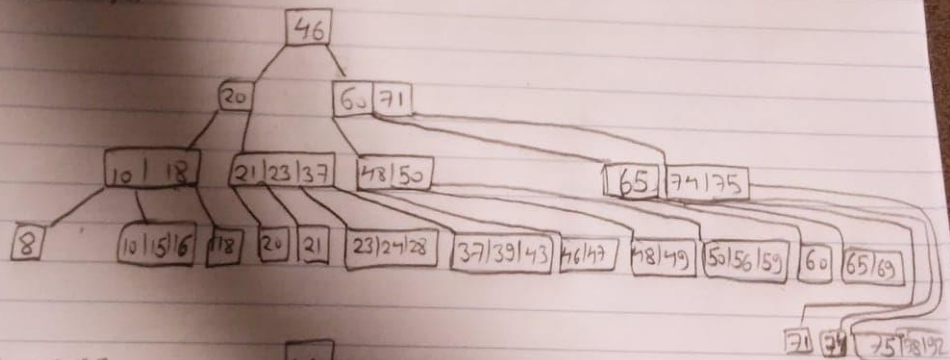
• Insert 28, 39, 43, 47



• Insert 50, 60



• Insert 75, 8, 49



• Insert 33, 38

