



Algebra 1 Workbook Solutions

Polynomials

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MATH

ADDING AND SUBTRACTING POLYNOMIALS

- 1. What stays the same when adding and subtracting like terms?

Solution:

The exponent stays the same when adding and subtracting like terms.

- 2. Simplify the expression.

$$(2x^3 - 5x^2 + x - 3) - (x^2 - 2x + 7)$$

Solution:

Simplify the expression by combining like terms.

$$(2x^3 - 5x^2 + x - 3) - (x^2 - 2x + 7)$$

$$2x^3 - 5x^2 + x - 3 - x^2 + 2x - 7$$

$$2x^3 - 6x^2 + 3x - 10$$

- 3. What went wrong in the following set of steps?

$$6x^3 + 7 + x^2$$



$$7x^3 + 7$$

Solution:

The terms $6x^3$ and x^2 were added together but they are not like terms. The exponents are not the same, so they cannot be added together.

■ 4. What is the coefficient in the following expression?

$$5x^8$$

Solution:

The coefficient is 5.

■ 5. Simplify the expression.

$$(10a^2b + 3ab^2 - ab) + (2ab^2 - a^2b + ab)$$

Solution:

Simplifying the expression by combining like terms.

$$(10a^2b + 3ab^2 - ab) + (2ab^2 - a^2b + ab)$$



$$10a^2b + 3ab^2 - ab + 2ab^2 - a^2b + ab$$

$$9a^2b + 5ab^2$$

- 6. What is the exponent in the following expression?

$$3z^8$$

Solution:

The exponent is 8.

- 7. Simplify the expression.

$$(x^4 - 5y^3 + z - xy) - (2y^4 + 6xy - z + x^4)$$

Solution:

Simplifying the expression by combining like terms.

$$(x^4 - 5y^3 + z - xy) - (2y^4 + 6xy - z + x^4)$$

$$x^4 - 5y^3 + z - xy - 2y^4 - 6xy + z - x^4$$

$$-5y^3 + 2z - 7xy - 2y^4$$



- 8. What is the variable in the following expression?

$$-y^4$$

Solution:

The variable is y .

- 9. What went wrong in the following set of steps?

$$9 - x^3 + 3 + 4x^3$$

$$12 + 3x^6$$

Solution:

The terms $-x^3$ and $4x^3$ were added together. That's correct since they are like terms, but when the terms were added, the exponents were added as well. The term should be $3x^3$, not $3x^6$.



MULTIPLYING POLYNOMIALS

- 1. Expand the expression.

$$(2x - y)^2$$

Solution:

The expression is expanded and simplified as

$$(2x - y)(2x - y)$$

$$4x^2 - 2xy - 2xy + y^2$$

$$4x^2 - 4xy + y^2$$

- 2. What does FOIL stand for?

Solution:

FOIL stands for **F**irst, **O**uter, **I**nnner, **L**ast.

- 3. What went wrong in the following set of steps?

$$(a - 2)^2$$



$$a^2 - 4$$

Solution:

The expression was not interpreted correctly. The exponent was just distributed to both terms directly, but the expression should have been expanded as

$$(a - 2)^2$$

$$(a - 2)(a - 2)$$

From there, you would then need to FOIL in order to expand and simplify.

■ 4. Expand the expression.

$$(3x + 2y)(3x - 2y)$$

Solution:

The expression is expanded and simplified as

$$(3x + 2y)(3x - 2y)$$

$$9x^2 - 6xy + 6xy - 4y^2$$

$$9x^2 - 4y^2$$



■ 5. Fill in the blank.

$$(3 - a)(5 + a) = 15 + \underline{\hspace{1cm}} - a^2$$

Solution:

If we FOIL the product on the left, we get

$$(3 - a)(5 + a)$$

$$15 + 3a - 5a - a^2$$

$$15 - 2a - a^2$$

The value that goes in the blank is therefore $-2a$.

■ 6. Expand the expression.

$$(x^2 - 3)(2 - x)$$

Solution:

The expression is expanded and simplified as

$$(x^2 - 3)(2 - x)$$

$$2x^2 - x^3 - 6 + 3x$$



$$-x^3 + 2x^2 + 3x - 6$$

■ 7. What went wrong in the following set of steps?

$$(x - y)(x + y)$$

$$x^2 - 2xy - y^2$$

Solution:

When using FOIL to expand and simplify the expression, the like terms were not combined correctly. It should be

$$(x - y)(x + y)$$

$$x^2 + xy - xy - y^2$$

$$x^2 - y^2$$



DIVIDING POLYNOMIALS

- 1. In words, what is the first question you should ask when solving the problem using long division?

$$(2x^2 + 4x - 4) \div (x - 1)$$

Solution:

“What do I multiply by x in order to get $2x^2$?”

- 2. Simplify the expression using polynomial long division.

$$(3x^3 - x^2 + 5) \div (x + 2)$$

Solution:



$$\begin{array}{r}
 3x^2 - 7x + 14 \\
 \hline
 x + 2 \overline{) 3x^3 - x^2 + 5} \\
 \underline{-3x^3 - 6x^2} \\
 -7x^2 \\
 \underline{7x^2 + 14x} \\
 14x + 5 \\
 \underline{-14x - 28} \\
 -23
 \end{array}$$

Therefore, the solution is

$$3x^2 - 7x + 14 - \frac{23}{x + 2}$$

- 3. What went wrong in setting up the long division problem?

$$(5x^4 - 3x^2 + x - 2) \div (x^2 + 1)$$

$$5x^4 - 3x^2 + x - 2 \overline{) x^2 + 1}$$

Solution:

The dividend and divisor were placed incorrectly. It should be



$$x^2+1 \overline{) 5x^4-3x^2+x-2}$$

- 4. Given the following long division, write the answer as

$$\text{quotient} + \frac{\text{remainder}}{\text{divisor}}$$

$$\begin{array}{r} 3x-1 \\ x^2-3 \overline{) 3x^3-x^2+x-5} \\ \underline{-3x^3} \\ -x^2+10x-5 \\ x^2 \\ \hline 10x-8 \end{array}$$

Solution:

The answer is written as

$$3x-1 + \frac{10x-8}{x^2-3}$$



- 5. Use long division to simplify the expression.

$$(2x^5 - 3x^3 + x^2 + 4x - 1) \div (x^2 + 2)$$

Solution:

The long division would be

$$\begin{array}{r}
 2x^3 \qquad -7x + 1 \\
 \hline
 x^2 + 2 \overline{) 2x^5 - 3x^3 + x^2 + 4x - 1} \\
 \underline{-2x^5 - 4x^3} \\
 -7x^3 + x^2 + 4x \\
 \underline{7x^3 + 14x} \\
 x^2 + 18x - 1 \\
 \underline{-x^2 - 2} \\
 18x - 3
 \end{array}$$

Therefore, the solution is

$$2x^3 - 7x + 1 + \frac{18x - 3}{x^2 + 2}$$



- 6. How would you rewrite the expression before starting the long division process?

$$(6x^3 - x + 7) \div (x + 1)$$

Solution:

You would rewrite the expression and set up the long division as

$$x + 1 \overline{) 6x^3 + 0x^2 - x + 7}$$

- 7. Set up but do not solve the following division problem.

$$\frac{x^5 - x^3 + 4x^2 - x + 6}{2x^3 - 5}$$

Solution:

The above problem is set up as

$$2x^3 - 5 \overline{) x^5 + 0x^4 - x^3 + 4x^2 - x + 6}$$

- 8. Simplify the expression using polynomial long division.



$$(3x^2 + 2x + 5) \div (3x + 5)$$

Solution:

The long division is set up as

$$\begin{array}{r} x-1 \\ 3x+5 \overline{) 3x^2+2x+5} \\ \underline{-3x^2-5x} \\ -3x+5 \\ \underline{3x+5} \\ 10 \end{array}$$

Therefore, the solution is

$$x - 1 + \frac{10}{3x + 5}$$



MULTIPLYING MULTIVARIABLE POLYNOMIALS

- 1. Why can we not add the following two terms?

$$2x^3y + x^3y^2$$

Solution:

We can't add these terms because they aren't like terms. The exponents on both x and y do not match since there is a y in the first term and a y^2 in the second term.

- 2. Simplify the expression.

$$(a - 3y)(2a + y)$$

Solution:

The expression is simplified as

$$2a^2 + ay - 6ay - 3y^2$$

$$2a^2 - 5ay - 3y^2$$



- 3. What went wrong in the following set of steps?

$$(x + 3b)(-2x - b)$$

$$-2x^2 - bx - 6bx + 3b^3$$

Solution:

The negative sign was not used when multiplying the last terms $+3b$ and $-b$, in order to give the last term of the product, $-3b^2$.

- 4. Simplify the expression.

$$(x - 2y)(x + y) + (3x - y)(4x + 4y)$$

Solution:

The expression is simplified as

$$(x - 2y)(x + y) + (3x - y)(4x + 4y)$$

$$(x^2 + xy - 2xy - 2y^2) + (12x^2 + 12xy - 4xy - 4y^2)$$

$$13x^2 + 7xy - 6y^2$$

- 5. Fill in the blanks with the correct terms.



$$(5a - b)(7b - 3a)$$

$$35ab - 15a^2 + \underline{\hspace{1cm}} + 3ab$$

$$\underline{\hspace{1cm}} - 15a^2 + \underline{\hspace{1cm}}$$

Solution:

Expanding and simplifying the expression gives

$$(5a - b)(7b - 3a)$$

$$35ab - 15a^2 - 7b^2 + 3ab$$

$$38ab - 15a^2 - 7b^2$$

The first blank should be filled with $-7b^2$, the second blank with $38ab$, and the last blank with $-7b^2$.

■ 6. What does FOIL stand for when used in multiplying multivariable polynomials?

Solution:

FOIL stands for **F**irst, **O**uter, **I**nnner, **L**ast.



■ 7. Fill in the following chart for the multiplication of the following two expressions.

$$(2x - 3y)(x^2 + y)$$

	$2x$	$-3y$
x^2		
y		

Solution:

The chart is filled in as

	$2x$	$-3y$
x^2	$2x^3$	$-3x^2y$
y	$2xy$	$-3y^2$

■ 8. What went wrong in the following set of steps?

$$(a^2 + 6b)(-a - b^2)$$

$$-a^3 - a^2b^2 - 6ab - b^3$$

$$-a^3 - 7ab - b^3$$

Solution:



In the first step, the terms $6b$ and $-b^2$ were multiplied incorrectly. Their product was shown as $-b^3$, but it should have been $-6b^3$. In the second step, the terms $-a^2b^2$ and $-6ab$ were added, but they shouldn't have been added because they're not like terms.

■ 9. Fill in the blanks of the multiplication chart with the correct terms when given the following problem.

$$(4a + 3b)(-a + 2b^2)$$

		3b
-a		-3ab

Solution:

The chart is filled in as

	4a	3b
-a	-4a ²	-3ab
2b²	8ab ²	6b ³

■ 10. Simplify the following expression.

$$(5ax - 3by)(a + y) - (a - y)(2ax + 4by)$$



Solution:

The expression is simplified as

$$(5ax - 3by)(a + y) - (a - y)(2ax + 4by)$$

$$(5a^2x + 5axy - 3aby - 3by^2) - (2a^2x + 4aby - 2axy - 4by^2)$$

$$5a^2x + 5axy - 3aby - 3by^2 - 2a^2x - 4aby + 2axy + 4by^2$$

$$3a^2x + 7axy - 7aby + by^2$$

■ 11. What went wrong in this set of steps?

$$(-2x)(3y - x^2)$$

$$-6xy - 2x^3$$

Solution:

The negative sign wasn't distributed to the second term. The product should be

$$-6xy + 2x^3$$



DIVIDING MULTIVARIABLE POLYNOMIALS

- 1. Set up but do not solve the long division problem.

$$\frac{y^3 - 3yx^2 + x^3}{y - x}$$

Solution:

The division is set up as

$$y - x \overline{) y^3 - 3yx^2 + x^3}$$

- 2. Find the quotient.

$$\frac{3x^2 + 6xy - 2y^2}{x - 2y}$$

Solution:

The quotient is given by



$$\begin{array}{r}
 3x + 12y + \frac{22y^2}{x-2y} \\
 x-2y \overline{) 3x^2 + 6xy - 2y^2} \\
 \underline{-(3x^2 - 6xy)} \\
 12xy - 2y^2 \\
 \underline{-(12xy - 24y^2)} \\
 22y^2
 \end{array}$$

3. Given the following long division, write the answer as

$$\text{quotient} + \frac{\text{remainder}}{\text{divisor}}$$

$$\begin{array}{r}
 x^2 - xy + y^2 \\
 x+y \overline{) x^3 + 0x^2y + 0xy^2 + y^3} \\
 \underline{x^3 + x^2y} \\
 -x^2y \\
 \underline{-x^2y - xy^2} \\
 xy^2 \\
 \underline{xy^2 + y^3} \\
 -y^3
 \end{array}$$



Solution:

The quotient is written as

$$x^2 - xy + y^2 - \frac{y^3}{x + y}$$

■ 4. How would you rewrite the expression before starting the long division process?

$$\frac{2y^3 - xy^2 + x^3}{x - y}$$

Solution:

The quotient would be rewritten as

$$x - y \overline{) x^3 + 0x^2y - xy^2 + 2y^3}$$

■ 5. Find the quotient.

$$\frac{6x^2 - xy + 2y^2}{2x - y}$$



Solution:

The quotient is given by

$$\begin{array}{r}
 3x + y + \frac{3y^2}{2x-y} \\
 2x-y \overline{) 6x^2 - xy + 2y^2} \\
 \underline{-(6x^2 - 3xy)} \\
 2xy + 2y^2 \\
 \underline{-(2xy - y^2)} \\
 3y^2
 \end{array}$$

- 6. In words, what is the first question you should ask when solving this long division problem?

$$2x+3y \overline{) 6x^4 - x^2y + xy^2 + 4y^4}$$

Solution:

“What do I need to multiply $2x$ by to get $6x^4$?”



- 7. What went wrong in setting up the long division?

$$\frac{7x^3 + x^2y - 2xy^2 + y^3}{x - 2y}$$

$$7x^3 + x^2y - 2xy^2 + y^3 \overline{) x - 2y}$$

Solution:

The dividend was written as the divisor. Instead, it should be

$$x - 2y \overline{) 7x^3 + x^2y - 2xy^2 + y^3}$$

- 8. Fill in the blanks with the correct terms.

$$(2x - y)(\underline{\hspace{1cm}}) = 6x^2 - 3xy$$

Solution:

The blank should be filled in with $3x$.

- 9. Find the quotient.



$$(y^2 + xy - 3x^2) \div (y + x)$$

Solution:

The quotient is

$$\begin{array}{r}
 -3x + 4y - \frac{3y^2}{x+y} \\
 x+y \overline{) -3x^2 + xy + y^2} \\
 \underline{-(-3x^2 - 3xy)} \\
 4xy + y^2 \\
 \underline{-(4xy + 4y^2)} \\
 -3y^2
 \end{array}$$



