



SRM Institute of Science and Technology
Department of Mathematics
21MAB204T-Probability and Queueing Theory
Unit – I
Tutorial Sheet - 2

S.No.	Part – B (Each question carries 8 marks)												
1	When a die is thrown, X denotes the number that turns up. Find $E(X)$, $E(X^2)$, $\text{Var}(X)$, and Standard Deviation (SD).												
2	<p>The Probability Distribution Function of a RV X is given below:</p> <table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>p_x</td><td>1/16</td><td>4/16</td><td>6/16</td><td>4/16</td><td>1/16</td></tr></table> <p>Find the MGF of X and hence find (i) the mean of X (ii) the variance of X (iii) μ'_3</p>	x	0	1	2	3	4	p_x	1/16	4/16	6/16	4/16	1/16
x	0	1	2	3	4								
p_x	1/16	4/16	6/16	4/16	1/16								
3	The r th moment of a Random Variable (RV) X is given as $\mu'_r = (r + 1)! 2^r$. Find (i) the mean (ii) the variance and (iii) the MGF of the RV X												
4	Find the Moment Generating Function of the continuous RV X whose density function is $f(x) = \begin{cases} 2e^{-2x}, & x \geq 0 \\ 0, & \text{otherwise} \end{cases}$ Hence find the first four central moments.												
5	The first three moments of a distribution about $X = 4$ are 1, 4, 10 respectively. Find the first three moments about the origin and also find the Standard Deviation (SD).												
6	<p>The Random Variable X has the following probability distribution:</p> <table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>$p(x)$</td><td>K</td><td>$3K$</td><td>$5K$</td><td>$7K$</td><td>$9K$</td></tr></table> <p>Find (i) K, (ii) mean of X (iii) variance of X (iv) $E(3X - 4)$ and (v) $\text{Var}(3X - 4)$</p>	x	0	1	2	3	4	$p(x)$	K	$3K$	$5K$	$7K$	$9K$
x	0	1	2	3	4								
$p(x)$	K	$3K$	$5K$	$7K$	$9K$								
	Part – C (Each question carries 15 marks)												
7	<p>The Probability Distribution Function of a discrete RV X is given by</p> <table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>$p(x)$</td><td>k</td><td>$3k$</td><td>$5k$</td><td>$7k$</td></tr></table> <p>Find (i) k, (ii) CDF (iii) $E(X)$ (iv) $V(X)$ (v) $E(4X + 5)$ (vi) $V(4X + 3)$ and (vii) MGF of X</p>	x	0	1	2	3	$p(x)$	k	$3k$	$5k$	$7k$		
x	0	1	2	3									
$p(x)$	k	$3k$	$5k$	$7k$									
8	<p>A continuous RV X has pdf $f(x) = \begin{cases} k(1 - x), & 0 < x < 1 \\ 0, & \text{otherwise} \end{cases}$</p> <p>Find (i) k (ii) the rth moment about the origin. Hence find the first four central moments.</p>												