

Q4b.1) For input (0,0,1)

Step 1:

Multiply input (0,0,1) with the wts of edges b/w input layer & hidden layer.

$$\text{neuron \#1 input} = 0 * (5.42528022) + 0 * (5.70308771) \\ + 1 * (-0.90768267)$$

$$= \boxed{-0.90768267}$$

$$\text{neuron \#1 output on sigmoid func} \frac{1}{1+e^{-x}}$$

$$\text{neuron \#1 output} = \boxed{\frac{1}{1+e^{-(-0.90768267)}}} = \boxed{0.287474268}$$

$$\text{neuron \#2 input} = 0 * (7.3600876) + 0 * (-3.0020293) + 1 * (-0.18642696) \\ = \boxed{-0.18642696}$$

~~neuron \#2 output~~

$$\text{neuron \#2 output} = \boxed{\frac{1}{1+e^{-(-0.18642696)}}} = \boxed{0.453527777}$$

$$\text{neuron \#3 input} = 0 * (1.96396178) + 0 * (2.34302462) + 1 * (1.98738418) \\ = \boxed{1.98738418}$$

$$\text{neuron \#3 output} = \boxed{\frac{1}{1+e^{-1.98738418}}} = \boxed{0.879466121}$$

$$\text{neuron \#4 input} = 0 * (-5.19346698) + 0 * (7.69309775) + 1 * (1.80612328) \\ = \boxed{1.80612328}$$

$$\text{neuron \#4 output} = \boxed{\frac{1}{1+e^{-1.80612328}}} = \boxed{0.858892684}$$

Output Layer:

neuron input = $(0.287474268 * 10.32045098) + (0.453527777 * -9.82575226) + (0.879466121 * 4.65760254) + (0.858892684 * (-9.83285897))$.

$$= \boxed{-5.838554482}$$

$$Y(0,0,1) = \frac{1}{1 + e^{(-5.838554482)}} = \boxed{0.00290459}$$

2) for input (0 1 1)

Hidden Layer:

$$\text{neuron #1 input} = 0 * 5.42528022 + 1 * (5.7030877) + 1 * (-0.90768267)$$

$$= \boxed{4.79540504}$$

$$\text{neuron #1 output} = \frac{1}{1 + e^{-4.79540504}} = \boxed{0.991800144}$$

$$\text{neuron #2 input} = 0 * (7.3600876) + 1 * (-3.0020293) + 1 * (-0.18642615)$$

$$= \boxed{-3.18845626}$$

$$\text{neuron #2 output} = \frac{1}{1 + e^{-(-3.18845626)}} = \boxed{0.039602452}$$

$$\text{neuron #3 input} = 0 * (1.96396178) + 1 * (2.84302462) + 1 * (1.98738418)$$

$$= \boxed{4.3304088}$$

$$\text{neuron #3 output} = \frac{1}{1 + e^{-4.3304088}} = \boxed{0.987008826}$$

$$\text{neuron #4 input} = 0 * (-5.19346698) + 1 * (7.69309775) + 1 * (1.80612328)$$

$$= \boxed{9.49922103}$$

$$\text{neuron #4 output} = \frac{1}{1 + e^{-9.49922103}} = \boxed{0.999925095}$$

Output Layer:

$$\begin{aligned}
 \text{neuron input} &= (0.991800144 * 10.32045098) + (0.039602452 * (-9.82575226)) + (0.987008826 * 4.65760254) + \\
 &+ (0.999925095 * (-9.83285897)) \\
 &= 10.23582477 + (-0.389123882) + 4.597094815 \\
 &\quad + (-9.83212244) \\
 &= \boxed{4.611673263}
 \end{aligned}$$

$$Y(0, 1, 1) = \frac{1}{1 + e^{-4.611673263}} = \boxed{0.99016256}$$

3) For input (101)

Hidden Layer:

$$\begin{aligned}
 \text{neuron #1 input} &= 1 * (5.42528022) + 0 * (5.70308771) + \\
 &\quad 1 * (-0.90768267) \\
 &= \boxed{4.51759755}
 \end{aligned}$$

$$\text{neuron #1 output} = \frac{1}{1 + e^{-4.51759755}} = \boxed{0.98920264}$$

$$\begin{aligned}
 \text{neuron #2 input} &= 1 * (7.3600876) + 0 * (-3.0020293) + \\
 &\quad 1 * (-0.18642696) \\
 &= \boxed{7.17366064}
 \end{aligned}$$

$$\text{neuron #2 output} = \frac{1}{1 + e^{-7.17366064}} = \boxed{0.999234075}$$

$$\begin{aligned}
 \text{neuron #3 input} &= 1 * (1.96396178) + 0 * (2.34302462) + 1 * (1.98738418) \\
 &= \boxed{3.95134596}
 \end{aligned}$$

$$\text{neuron #3 output} = \frac{1}{1 + e^{-3.95134596}} = \boxed{0.981133968}$$

$$\text{neuron \#4 input} = 1 * (-5.19346698) + 0 * (7.69309775) + 1 * (1.80612328)$$

$$= \boxed{-3.3873437}$$

$$\text{neuron \#4 output} = \frac{1}{1 + e^{-(-3.3873437)}} = \boxed{0.032693355}$$

Output Layer:

$$\text{neuron input} = (0.98920264 * 10.32045098) + (0.999234075 * (-9.82575226)) + (0.981133968 * 4.65760254) + (0.032693355 * (-9.83285897))$$

$$= 10.20901736 - 9.818226471 + 4.569732061$$

$$= \boxed{4.639053801}$$

$$Y(1,0,1) = \frac{1}{1 + e^{-4.639053801}} = \boxed{0.990425713}$$

A) For Input (1,1,1)

Hidden Layer:

$$\text{neuron \#1 input} = 1 * (1.42528022) + 1 * (5.70308771) + 1 * (-0.90768267)$$

$$= \boxed{10.22068526}$$

$$\text{neuron \#1 output} = \frac{1}{1 + e^{-10.22068526}} = \boxed{0.999963592}$$

$$\text{neuron \#2 input} = 1 * (7.3600876) + 1 * (-3.0020293) + 1 * (-0.18642696)$$

$$= \boxed{4.17163134}$$

$$\text{neuron \#2 output} = \frac{1}{1 + e^{-4.17163134}} = \boxed{0.984807306}$$

$$\text{neuron \#3 input} = 1 * (1.96396178) + 1 * (2.84302462) + 1 * (1.98738418)$$

$$= \boxed{6.29437058}$$

$$\text{neuron \#3 output} = \frac{1}{1 + e^{-6.29437058}} = \boxed{0.998156732}$$

$$\text{neuron \#4 Input} = 1 * (-5.19346698) + 1 * (7.69309775) + 1 * (1.8061232) \\ = \boxed{4.30575405}$$

$$\text{neuron \#4 output} = \frac{1}{1+e^{-4.30575405}} = \boxed{0.986688867}$$

Output Layer:

$$\text{neuron input} = (0.999963592 * 10.32045098) + (0.984807306 * (-9.82575226)) + (0.998156732 * 4.65760254) \\ + (0.986688867 * (-9.83285897)) \\ = 10.32007523 + (-9.876472613) + 4.64901733 \\ - 9.701972476 \\ = \boxed{-4.409352529} = (1, 0, 1) Y$$

$$Y(1, 1, 1) = \frac{1}{1+e^{(-4.409352529)}} = \boxed{0.012016888}$$

$$(0.999963592 * 10.32045098) + (0.984807306 * (-9.82575226)) + (0.998156732 * 4.65760254) \\ + (0.986688867 * (-9.83285897)) \\ = \boxed{0.35068256} =$$

$$(0.999963592 * 10.32045098) + (0.984807306 * (-9.82575226)) + (0.998156732 * 4.65760254) \\ + (0.986688867 * (-9.83285897)) \\ = \boxed{0.35068256} =$$

$$(0.999963592 * 10.32045098) + (0.984807306 * (-9.82575226)) + (0.998156732 * 4.65760254) \\ + (0.986688867 * (-9.83285897)) \\ = \boxed{0.35068256} =$$

$$(0.999963592 * 10.32045098) + (0.984807306 * (-9.82575226)) + (0.998156732 * 4.65760254) \\ + (0.986688867 * (-9.83285897)) \\ = \boxed{0.35068256} =$$

$$(0.999963592 * 10.32045098) + (0.984807306 * (-9.82575226)) + (0.998156732 * 4.65760254) \\ + (0.986688867 * (-9.83285897)) \\ = \boxed{0.35068256} =$$