

28/11/19

SEMESTER - II

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PRACTICAL NO. 1BASICS OF R-SOFTWARE

- R is a software for statistical analysis computing.
- It is an effective data handling outcome storage is possible.
- It is capable of graphical
- It is a free software

(Q1) Solve the following:

1.) $> 4 + 6 + 8 \div 2 - 5$

[1] 7.3333

2.) $> 2^2 + |-3| + \sqrt{45}$

[1] 13.7082

3.) $> 5^3 + 7 \times 5 * 8 + 46 / 5$

[1] 414.2

4.) $\sqrt{4^2 + 5 \times 3 + 7 / 6}$

[1] 5.671567

5.) Round off $(46 \div 7 + 9 \times 8)$

[1] 79

(Q2) Solve the following:

1) $a = c(2, 3, 5, 7)^* \cdot 2.$

a

[1] 4 6 10 14

2) $b = c(2, 3, 5, 7)^* \cdot c(2, 3, 5)$

b

[1] 4 9 10 21

3) $c = c(2, 3, 5, 7)^* \cdot c(2, 3, 6, 4)$

c

[1] 4 9 30 28.

4) $d = c(1, 6, 2, 3)^* \cdot c(-2, -3, -4, -1)$

d

[1] -2 -18 -8 -3

5) $e = c(2, 3, 5, 7)^* \cdot 2$

e

[1] 4 9 25 49

6) $f = c(4, 6, 8, 9, 4, 5)^* \cdot c(1, 2, 3)$

f

[1] 4 36 512 9 16 125

7) $g = c(6, 2, 7, 5) / c(4, 5)$

g

[1] 1.50 0.40 1.75 1.00

Q2

(Q5) Find $x+y$ and $2x+3y$ where,

$$x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 1 \\ 9 & -5 & 3 \end{bmatrix} \quad y = \begin{bmatrix} 10 & -5 & 1 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

$\rightarrow x = \text{matrix}(\text{row}=3, \text{ncol}=3, \text{data}=\text{c}(4, 7, 9, -2, 0, -5, 6, 7, 3))$

$$\begin{bmatrix} [1,] & [2,] & [3,] \\ 4 & -2 & 6 \end{bmatrix}$$

$$\begin{bmatrix} [2,] & 7 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} [3,] & 9 & -5 & 3 \end{bmatrix}$$

$y = \text{matrix}(\text{row}=3, \text{ncol}=3, \text{data}=\text{c}(10, 12, 15, -5, -4, -6, 7, 9, 5))$

$x = x + y$

$> a$

$$\begin{bmatrix} [,1] & [,2] & [,3] \\ [1,] & 14 & -7 & 13 \\ [2,] & 19 & -4 & 16 \\ [3,] & 24 & -11 & 8 \end{bmatrix}$$



$x = 2x + 3y$

$$\begin{bmatrix} [,1] & [,2] & [,3] \\ [1,] & 38 & -19 & 33 \\ [2,] & 50 & -12 & 41 \\ [3,] & 63 & -28 & 21 \end{bmatrix}$$

Probability Distribution

- (Q) Check whether the following one p.m.f or not.

x	0	1	2	3	4	5
P(x)	0.1	0.2	-0.5	0.4	0.3	0.5

x	1	2	3	4	5
P(x)	0.2	0.2	0.3	0.2	0.2

x	10	20	30	40	50
P(x)	0.2	0.2	0.35	0.15	0.1

Ans 1) $\because P(x) = -0.5$, can not be a probability mass function.

$\therefore P(x) \geq 0$ for all x .

Ans 2) It cannot be a probability mass function as p.m.f. is not equal to 1.

> prob = c (0.2, 0.2, 0.3, 0.2, 0.2)

> sum (prob)

[Q] 4.1

Ans 3) $\begin{aligned} &> \text{prob} = c(0.2, 0.2, 0.35, 0.15, 0.1) \\ &> \text{sum}(\text{prob}) \end{aligned}$

[A] 1.

Hence, it is a probability mass function.

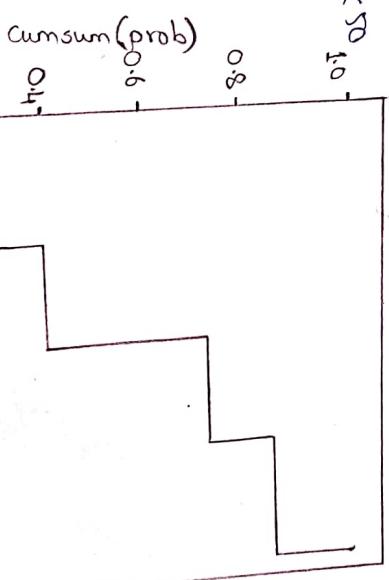
- (Q) Find c.d.f. for the following p.m.f & sketch the graph.

$$\begin{aligned} x &10 &20 &30 &40 &50 \\ p(x) &0.2 &0.2 &0.35 &0.15 &0.1 \end{aligned}$$

$$\begin{aligned} &> \text{prob} = c(0.2, 0.2, 0.35, 0.15, 0.1) \\ &> \text{sum}(\text{prob}) \\ &[A] 1. \end{aligned}$$

$$\text{cumsum}(\text{prob})$$

$$\begin{aligned} [A] &0.20 &0.40 &0.75 &0.90 &1.00 \\ &\rightarrow F(x) = 0 &x < 10 \\ &\quad 0.2 &10 \leq x < 20 \\ &\quad 0.4 &20 \leq x < 30 \\ &\quad 0.75 &30 \leq x < 40 \\ &\quad 0.90 &40 \leq x < 50 \\ &\quad 1.0 &x \geq 50. \end{aligned}$$



Check whether the following is p.d.f or not.

Q3
 $f(x) = 3 - 2x ; 0 \leq x \leq 1$
 $P(x) = 3x^2 ; 0 < x < 1$

2) $x \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6$
 $P(x) 0.15 \quad 0.25 \quad 0.1 \quad 0.2 \quad 0.2 \quad 0.1$
 $\rightarrow > \text{prob} = c (0.15, 0.25, 0.1, 0.2, 0.2, 0.1)$
 $> \text{sum}(\text{prob})$
 $[1] \quad 1$
 $> \text{cumsum}(\text{prob})$
 $[1] \quad 0.15 \quad 0.40 \quad 0.50 \quad 0.70 \quad 0.90 \quad 1.00$

$$f(x) = 0 \quad x < 0 \\ 1$$

$$0.15 \quad 1 \leq x < 2$$

$$0.40 \quad 2 \leq x < 3$$

$$0.50 \quad 3 \leq x < 4$$

$$0.70 \quad 4 \leq x < 5$$

$$0.90 \quad 5 \leq x < 6$$

$$1.00 \quad x \geq 6$$

$> x=c(1,2,1,3,4,5,6)$

$> \text{plot}(x, x|\text{lab}=\text{"value"}, y|\text{lab}=\text{"prob"}, \text{main}=\text{"cdf"}, \text{cumsum}(\text{prob}),$

cdf.

$$(Ans) f(x) = \int_0^x f(x) dx$$

$$= \int_0^x 3x^2 dx$$

$$= 3 \int_0^x x^2 dx$$

AM

$$= 3 \int_0^1 x^2 dx$$

$$= 3 \left[\frac{x^3}{3} \right]_0^1$$

$$= (1-0)^3$$

$$= 1$$

$$= \int_0^1 3 - 2x dx$$

$$= \int_0^1 3 dx - \int_0^1 2x dx$$

$$= 3 \int_0^1 dx - 2 \int_0^1 x dx$$

$$= \left[3x \right]_0^1 - 2 \left[\frac{x^2}{2} \right]_0^1$$

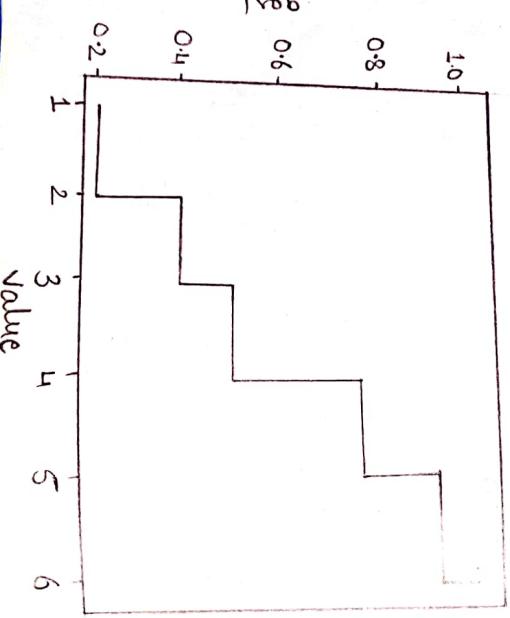
$$= 3(1-0) - (1-0)^2$$

$$= 3(1) - 1$$

$$= 3 - 1$$

$$= 2.$$

$\therefore f^o$ is not a p.d.f.



BINOMIAL DISTRIBUTION

Commands :-

$$\begin{aligned}
 1.) P(X=x) &= \text{dbinom}(x, n, p) \\
 2.) P(X \leq x) &= \text{pbinom}(x, n, p) \\
 3.) P(X > x) &= 1 - \text{pbinom}(x, n, p) \\
 4.) \text{If } x \text{ is unknown and } p = P(X \leq x)
 \end{aligned}$$

then, $\text{qbinom}(p, n, q)$

(1) Find the probability of exactly 10 success in 100 trials with $p = 0.1$.

(2) Suppose there are 12 M.C.Q., each question has 5 option out of which one is correct. Find the probability of having (a) 1) exactly 4 correct answer
 2) at most 4 correct answers.
 3) More than 5 correct answers.

(3) Find the complete distribution when $n=5$ & $p=0.1$.

(4) $n=12$, $p=0.25$, find the following probability

- 1.) $P(X=5)$
- 2.) $P(X \leq 5)$
- 3.) $P(X > 7)$
- 4.) $P(5 < X < 7) = P(X=6)$

Ans 1) $\geq \text{dbinom}(10, 100, 0.1)$

[1] 0.1318653.

Ans 2)*

i) $\geq \text{dbinom}(4, 12, 0.2)$

[1] 0.1328756

ii) $\geq \text{pbinom}(4, 12, 0.2)$

[1] 0.9274445

iii) $> 1 - \text{pbinom}(5, 12, 0.2)$

[1] 0.01940528

Ans 3) $\geq \text{dbinom}(0:5, 5, 0.1)$

[1] 0.59049 0.32805 0.07290 0.00810 0.00045 0.00001

Ans 4) $\text{dbinom}(5, 12, 0.25)$

[1] 0.1032414.

ii) $\geq \text{pbinom}(5, 12, 0.25)$

[1] 0.9455918.

iii) $> 1 - \text{pbinom}(7, 12, 0.25)$

[1] 0.0027185

Ans 5) $\geq \text{pbinom}(0, 10, 0.15)$
[1] 0.1968744.

Ans 6) $1 - \text{pbinom}(3, 20, 0.15)$
[1] 0.3522748

Ans 7) $\geq \text{pbinom}(0.88, 30, 0.2)$
[1] 9.

n = 10, p = 0.3

x = 0:n

> prob = $\text{dbinom}(x, n, p)$

> cumprob = $\text{pbinom}(x, n, p)$

> d = data.frame ("xvalue" = x, "probability" = prob)
> print(d)

xvalue	probability
0	0.0282

1 0.1210

2 0.2334

3 0.2668

4 0.2001

5 0.1029

6 0.0367

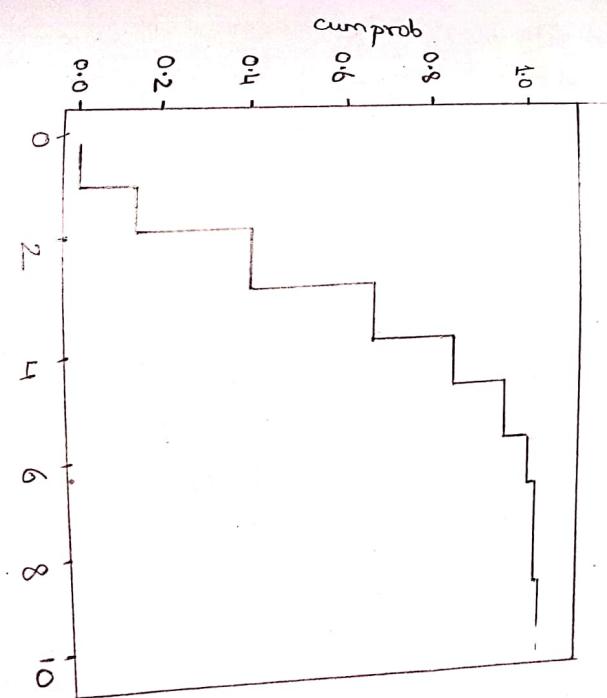
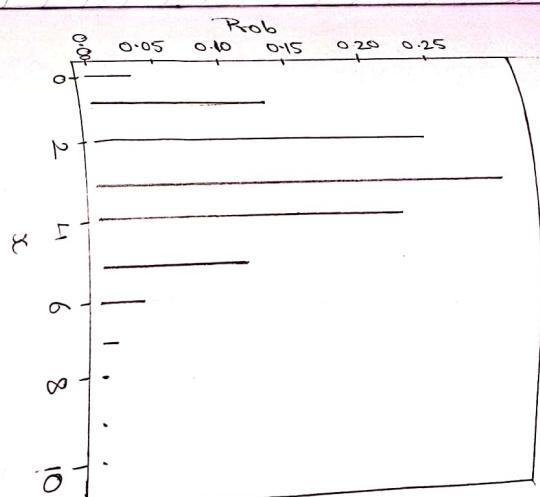
7 0.0090

8 0.0014

9 0.0001

10 0.000059

`plot (x, prob, "h")
plot (x, cumprob, "s")`



Ans
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PRACTICAL

No. 4

NORMAL

DISTRIBUTION

$$1) P(x=x) = \text{dnorm}(x, \mu, \sigma)$$

$$2) P(x \leq x) = \text{pnorm}(x, \mu, \sigma)$$

$$3) P(x > x) = 1 - \text{pnorm}(x, \mu, \sigma)$$

where, $\mu = \text{Mean}$

$\sigma = \text{Standard Deviation}$

4) To generate random numbers from a Normal Distribution (in random numbers), the R code is
 $= \text{rnorm}(n, \mu, \sigma)$

A random variable x follows Normal Distribution with mean $\mu = 12$, $\sigma = 3$. Find i) $P(x \leq 15)$ ii) $P(10 \leq x \leq 13)$ iii) $P(x > 14)$ iv) Generate 5 observations (random numbers).

$$\mu = 12, \sigma = 3.$$

$$> p1 = \text{pnorm}(15, 12, 3)$$

$$> \text{cat}('P(x \leq 15) : ', p1)$$

$$P(x \leq 15) : 0.8413447$$

$$> p2 = \text{pnorm}(13, 12, 3) - \text{pnorm}(10, 12, 3)$$

$$> \text{cat}('P(10 \leq x \leq 13) : ', p2)$$

$$P(10 \leq x \leq 13) : 0.3780661$$

$$> p3 = 1 - \text{pnorm}(14, 12, 3)$$

$$> \text{cat}('P(x > 14) : ', p3)$$

$$P(x > 14) : 0.2524425.$$

$$> \text{rnorm}(5, 12, 3)$$

$$[1] 9.007282 \quad 14.034168$$

$$11.837712$$

$$14.460544$$

$$11.1125136$$

$\text{med} = \text{median}(x)$
 $\text{cat('Median is', med)}$

$n=5$

$\text{var} = (\text{n}-2) * \text{var}(x)/\text{n}$

[1] 9.399908

$\text{sd} = \text{sqrt}(\text{var})$

cat('S.D is', sd)

S.D is 3.065927.

Q3) x follows Normal Distribution, $x \sim N(30, 100)$, $\mu = 30$, $\sigma = 10$. Find i.) $P(x \leq 40)$ ii.) $P(x > 35)$ iii.) $P(5 < x < 35)$

$\rightarrow P_1 = \text{pnorm}(40, 30, 10)$
 $\rightarrow P_2 = \text{pnorm}(35, 30, 10)$
 $\rightarrow P_3 = \text{pnorm}(5, 30, 10) - \text{pnorm}(35, 30, 10)$

[1] 0.8413447.

$\rightarrow P_2 = 1 - \text{pnorm}(35, 30, 10)$

[1] 0.3085375

$\rightarrow P_3 = \text{pnorm}(5, 30, 10) - \text{pnorm}(35, 30, 10)$

[1] 0.3829249

$\rightarrow \text{pnorm}(0.6, 30, 10)$

[1] 32.53347

AM

Q3.) Generate 5 random numbers from a Normal Distribution with $\mu = 15$ & $\sigma = 4$. Find Sample mean, median, SD & print it.

$\rightarrow x = \text{rnorm}(5, 15, 4)$

[1] 17.94827 15.54403 16.86062 15.32839 24.94837

$\rightarrow \text{om} = \text{mean}(x)$

$\rightarrow \text{cat('Arithmetic Mean is', om))$

Arithmetic Mean is 18.12612.

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PRACTICAL No. 5

NORMAL AND t-TEST

Test the hypothesis $H_0: \mu = 15$ against $H_1: \mu \neq 15$.
Random sample of size 400 is drop & it is calculated the sample mean is 14 & standard deviation is 3. Test the hypothesis at 5% level of significance

$$\begin{aligned}>&m_0 = 15; m_x = 14; s_d = 3; n = 400 \\>&z_{cal} = (m_x - m_0) / (s_d / (\text{sqrt}(n)))\end{aligned}$$

z_{cal}

[1] -6.666667.

>cat ("calculated value at 2 % is ", zcal)
calculated value at 2 % is = -6.666667

>pvalue = 2 * (1 - pnorm (abs(zcal)))

>pvalue

[1] 2.616796e-11

Since, pvalue is less than 0.05 we ~~reg~~ reject
 $H_0: \mu = 15$.

"calculated value at $2^{\circ}\text{ls} = ", z_{\text{cal}}$
 calculated value at $2^{\circ}\text{ls} = -3.75$
 $\text{calculated value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

2.) Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$.

Random sample of size 400 is drawn with sample mean 10.2 & standard deviation 2.25 test the hypothesis at 5% level of significance.

$\rightarrow n_{\text{no}} = 10; m_x = 10.2; s_d = 2.25; n = 400$

$> z_{\text{cal}} = (m_x - n_{\text{no}}) / (s_d / (\sqrt{n}))$

$> z_{\text{cal}}$.

[1] 1.777778

$> \text{cat}("calculated value at 2^{\circ}\text{ls} = ", z_{\text{cal}})$

calculated value at $2^{\circ}\text{ls} = 1.777778$

$> \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

$> \text{pvalue}$

[1] 0.07544036

Since, pvalue is more than 0.05, we accept $H_0: \mu = 10$

Lost year farmers lost 20% of their crops. A random sample of 60 fields were collected & it was found that 9 fields crops were insect polluted. Guess the hypothesis at 1% level of significance.

$> p = 0.2, P = 9/60; n = 60; Q = 1 - p$

$> z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$

[1] -0.9682458

$> \text{cat}("calculated value at 2^{\circ}\text{ls} = ", z_{\text{cal}})$

calculated value at $2^{\circ}\text{ls} = -0.9682458$

$> \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

$> \text{pvalue}$

[1] 0.3329216

Test the hypothesis (H_0), proportion of smokers in our college is 0.2. A sample is collected & its sample proportion is calculated as 0.125. Test the hypothesis at 5% level of significance (sample size is 400).

$\rightarrow p = 0.2; p = 0.125; n = 400; Q = 1 - p$

$> z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$

[1] -3.75

Q) **One Sample Test** the hypothesis $H_0: \mu_0 = 12.5$ from the following sample at 5% level of significance.

```
>>> x=c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)  
>n=length(x)  
>n  
[1] 10  
> mx=mean(x)  
> mx  
[1] 12.107  
> variance=(n-1)* var(x)/n  
> variance  
[1] 0.019521
```

```
> sd=sqrt(var)
```

```
> sd  
[1] 0.1391176
```

```
>zcal=(mx-m0)/(sd/(sqrt(n)))  
>zcal  
[1] -8.894909  
>cat ("calculated value is", zcal)  
Calculated value is -8.894909.  
>pvalue=2*(1-pnorm(abs(zcal)))  
>pvalue  
[1] 0
```

\therefore pvalue is less than 0.05, we reject H_0 .

PRACTICAL No. 6

Q) Let the population mean (the amt. spent per customer in a restaurant) is 250. A sample of 160 customers selected. The sample mean is calculated as 275 & S.D is 30. Test the hypothesis at the population mean is 250 or not at 5% level of significance.

In a random sample of 1000 student, it is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.8 at 1% level of significance.

H₀: $\mu = 275$ against H₁: $\mu \neq 275$
>m0=250; mx=275; n=160; sd=30
>zcal=(mx-m0)/(sd/(sqrt(n)))
>zcal

```
[1] 8.333333  
>cat ("calculated value at 2 is", zcal)  
Calculated value at 2 is 8.333333
```

```
>pvalue=2*(1-pnorm(abs(zcal)))  
>pvalue  
[1] 0
```

\therefore pvalue is less than 0.05, we reject H_0 at 5% level of significance.

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\rightarrow 2) $H_0: p = 0.8$ against $H_1: p \neq 0.8$

$p = 0.8$, $q = 1 - p$

[1] 0.2
 $> p = 750/1000 = 0.75$
 $> n = 1000$
 $> zcal = (p - P) / (\sqrt{P * Q / n})$
 $> zcal$
[2] -3.952847.
 $> cat("calculated value at 2 is =", zcal)$
calculated value at 2 is -3.952847.
 $> pvalue = 2 * (1 - pnorm(abs(zcal)))$
 $> pvalue$
[1] 7.72268e-05.

" pvalue is less than 0.05, we reject H_0 at 1% level of significance.

(3) Two random sample of size 1000 & 2000 are drawn from 2 population with same S.D i.e. 25. The sample means are 67.5 & 62 respectively. Test the hypothesis $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$ at 5% level of significance.

(4) A study of noise level in 2 hospital given below. Test the claim that the 2 hospital has some level of noise at 1% level of significance.

	Hospital A	Hospital B
size	84	34
Mean	61.2	59.4
S.D	7.9	7.5

(5) In a sample of 600 student in a clg, 400 use blue ink another college from a sample of 900 student use blue ink. Test the hypothesis that the proportion of student using blue ink in 2 colleges are equal or not at 1% level of significance.

✓
 1. Null hypothesis
 2. Alternative hypothesis
 3. Test statistic
 4. Level of significance

$\rightarrow 3)$ $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$

$$n_1 = 1000; n_2 = 2000, \bar{m}_{x_1} = 67.5, \bar{m}_{x_2} = 68; s_{d1} = s_{d2} = 2.5.$$

$$>z_{cal} = (\bar{m}_{x_1} - \bar{m}_{x_2}) / \sqrt{s_{d1}^2/n_1 + s_{d2}^2/n_2})$$

$$[1] -5.163978.$$

$$>z_{cal} ("calculated" is = "", z_{cal})$$

$$\text{calculated } is = -5.163978$$

$$>pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

>pvalue

$$[1] 2.4117564e-07$$

" pvalue is less than 0.05, we reject H_0 at 5% level of significance.

$\rightarrow 4)$ $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$

$$n_1 = 84; n_2 = 34; \bar{m}_{x1} = 61.2; \bar{m}_{x2} = 59.4; s_{d1} = 7.9; s_{d2} = 7.5$$

$$>z_{cal} = (\bar{m}_{x_1} - \bar{m}_{x_2}) / \sqrt{s_{d1}^2/n_1 + s_{d2}^2/n_2})$$

>z_{cal}

$$[1] 1.162528$$

>z_{cal} ("calculated" is = "", z_{cal})

$$\text{calculated } is = 1.162528$$

$$>pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

>pvalue

$$[1] 0.2450211$$

\therefore pvalue is greater than 0.05, \therefore we accept H_0 . at 100% level of significance

$H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

$$n_1 = 600, n_2 = 900$$

$$u_{100} / 600 = 0.666667$$

$$p_1 = u_{50} / 900 = 0.5$$

$$p_2 = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2) = 0.5666667$$

$$p = 1 - p = 0.4333333$$

$$q_{z_{cal}} = (p_1 - p_2) / \sqrt{p * q * (\gamma_{n_1} + \gamma_{n_2})}$$

$$>z_{cal}$$

$$[1] 6.381534$$

>z_{cal} ("calculated" is = "", z_{cal})

$$\text{calculated } is = 6.381534$$

$$>pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

$$[1] 1.753222e-10$$

" pvalue is less than 0.05, we reject H_0 at 1% level of significance

b) $\alpha =$ first, $n_1 = n_2 = 200, p_1 = 44/200, p_2 = 30/200$. Test hypothesis at 5% level of significance.

$$\rightarrow n_1 = n_2 = 200; p_1 = 44/200; p_2 = 30/200$$

$$>p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$[1] 0.185$$

$$>q = 1 - p$$

[1] 0.815

$$> zcal = (p1 - p2) / \sqrt{p * q * (1/n1 + 1/n2)}$$

> zcal

[1] 1.802741

$$P(Z > 1.802741) = 0.0319$$

> cat ("calculated is = ", zcal)

$$\text{calculated is} = 1.802741$$

> pvalue = 2 * (1 - pnorm (abs(zcal)))

> pvalue

[1] 0.07142888

\therefore pvalue is not greater than 0.05, \therefore we accept H_0 at 5% level of significance.

$$\frac{29}{27} \times 10^{-2}$$

significance

$$0.1 - 0.02888 = 0.07111$$

and $0.07142888 = 0.07142888 - 0.02888 = 0.04254888$, which is less than 0.05, \therefore null hypothesis is rejected.

$$0.07142888 - 0.02888 = 0.04254888$$

PRACTICAL No. 7

Topic :- Small sample Test

The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that sample comes from population with the average 66.

$$H_0: \mu = 66 > x = c (63, 63, \dots, 71, 72)$$

> n = length(x)

> n

[1] 10

> t.test(x),

One sample t-test

Q.2)

Two groups of student score the following marks, Test the hypothesis that there is no level of significance difference between 2 groups.

Group A : 18, 22, 21, 17, 20, 17, 23, 20, 22, 21
Group B : 16, 20, 14, 21, 20, 18, 13, 15, 17, 21.

H_0 : There is no difference between two groups

$x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$.
 $y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

t.test(x, y)

Welch Two sample t-test.

data : x and y
 $t = 2.2573$, $df = 16.376$, p-value = 0.03998.

alternative hypothesis : true difference in means is greater than 0.

-6.035547 Inf.

Sample estimates:
mean of the differences

-3.5

>pvalue = 0.9806
>if (pvalue > 0.05) fcat("Accept H₀") else fcat("Reject H₀")
Accept H₀.

Q.3) Two medicines are applied to 2 group of patient

Group 1: 10, 12, 13, 11, 14
Group 2: 8, 9, 12, 14, 15, 10, 9

is there any significance difference between two groups.

> if (pvalue > 0.05). fcat("Accept H₀") else fcat("Reject H₀")
Reject H₀.

H₀: There is no significance difference of sales before and after the campaign.

66

>x = c(53, 28, 31, 48, 50, 42)
>y = c(58, 29, 30, 55, 56, 45)

>t.test(x ~ y, paired = T, alternative = "greater")
Paired t-test.

data : x & y
 $t = -2.7815$, $df = 5$, p-value = 0.9806

alternative hypothesis : true difference in means is greater than 0.

0.01

-6.035547 Inf.

Sample estimates:
mean of the differences

-3.5

>pvalue = 0.9806
>if (pvalue > 0.05) fcat("Accept H₀") else fcat("Reject H₀")
Accept H₀.

Q.4) Two medicines are applied to 2 group of patient

Group 1: 10, 12, 13, 11, 14
Group 2: 8, 9, 12, 14, 15, 10, 9

is there any significance difference between two groups.

> if (pvalue > 0.05). fcat("Accept H₀") else fcat("Reject H₀")
Reject H₀.

Tables data of 6 shop before and after one special campaign given below:-

Before : 53, 28, 31, 48, 50, 42.
After : 58, 29, 30, 55, 56, 45.

Test the hypothesis the campaign is effective or not.

→ 4) H_0 = There is no significance difference between medicines

> $\alpha = c(10, 12, 13, 11, 14)$

> $\beta = c(8, 9, 12, 14, 15, 10, 9)$

> t.test(a,b)

welch Two sample t-test.

data : a and b.

t = 0.65591, df = 9.567, pvalue = 0.5273.

alternative hypothesis: true difference in mean is not equal to 0.

95 percent confidence interval:

-1.934382 3.534382

Sample estimates:

mean of x mean of y

11.8 11.0.

> pvalue = 0.5273

> if (pvalue > 0.05) dcat("Accept H_0 ") else dcat("Reject H_0 ")

Accept H_0 .

→ Q5) H_0 = There is no difference between before and after.

> A = c(120, 125, 115, 130, 123, 119)

> B = c(100, 114, 95, 90, 115, 99)

> t.test(A,B, paired=T, alternative = "less")

Paired t-test.

data : A and B.

t = 4.3458, df = 5, pvalue = 0.9963.

alternative hypothesis: true difference in mean is less than 0,

95 percent confidence interval:

-Inf 29.0295

Sample estimates:
mean of the differences
19.83333

pvalue = 0.9963.

> if (pvalue > 0.05) dcat("Accept H_0 ") else dcat("Reject H_0 ")

Accept H_0 .

* PRACTICAL No. 8 *

Topic :- Large and small sample tests.

$H_0: \mu = 55$ against $H_1: \mu \neq 55$

$n = 100$, $m_x = 52$, $m_o = 55$, $s_d = 7$.

$$z_{\text{cal}} = (m_x - m_o) / (s_d / \sqrt{n})$$

$z_{\text{cal}} = -4.285714$

> cat("calculated value at 2 is ", zcal)

calculated value at 2 is = -4.285714.

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue
1.82153e-05

∴ pvalue is less than 0.05, we reject H_0 at 5% level of significance.

2) $H_0: P = 0.5$ against $H_1: P \neq 0.5$

> P = 0.5

> Q = 1 - P

> Q

[2] 0.5

> P = 350 / 700

> P

[2] 0.5

> n = 700

> zcal = (P - Q) / sqrt(P * Q / n)

5) $n = 66$
 $H_0: \mu = 63, 63, 68, 69, 71, 71, 72$
 $\mu = c$
 $x = \text{length}(x)$
 $r_n = \text{length}(x)$

[1] 0
> cat ("calculated value at 2 is = ", zcal)

> calculated value at 2 is = 0
> pvalue = 2 * (1 - pnorm (abs (zcal)))

[1] 1

∴ pvalue is greater than 0.5, we accept H_0 at 5% level of significance.

[2] 1
n = 400, $H_0: \mu = 99$ against $H_1: \mu \neq 99$

m0 = 99
mx = 100
var = 64
> sd = sqrt (64)

> sd

[1] 8
zcal = (mx - m0) / sd / sqrt (n)

> zcal

[1] -2.5
> cat ("calculated value at 2 is = ", zcal)

> calculated value at 2 is = 2.5
> pvalue = 2 * (1 - pnorm (abs (zcal)))

> pvalue
[1] 0.01241933

∴ pvalue is less than 0.5, we reject H_0 at 5% level of significance.

[1] t.test (x)
one sample t-test.

data : x
t = 17.94, df = 6, pvalue = 5.522e-09
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
64.66479 71.62002

sample estimates:

mean of x

68.14286

: pvalue if (pvalue > 0.05) {cat ("Accept H_0 ")}
else {cat ("Reject H_0 ")}

Reject H_0 .

[1] 1
 $H_0: \mu = 1150$ against $H_1: \mu \neq 1150$.

n = 100

> mx = 1150

> m0 = 1200

> sd = 125

> zcal = (mx - m0) / (sd / sqrt(n))

> zcal

[1] -4.
> cat ("calculated value at 2 is = ", zcal)

> calculated value at 2 is = -4.

> pvalue = 2 * (1 - pnorm (abs (zcal)))

[1] 6.334248e-05

83.

∴ p-value is less than 0.5, we reject H_0 .

6.) $H_0: \sigma_1 = \sigma_2$ against $H_1: \sigma_1 \neq \sigma_2$.

> $x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$

> $y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

F-test to compare two variance

data : x and y

$F = 0.78803$, num df = 7, denom df = 10, pvalue = 0.7737

alternative hypothesis : true ratio of variances is not equal to
1. 95 percent confidence interval:

0.199509 3.751881

Sample estimates:
ratio of variance

0.7880255

∴ p-value is greater than 0.05, Hence we accept H_0 .

8.) $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$.

> $n_1 = 200, n_2 = 300$

> $p_1 = 44/200, p_2 = 50/300$

> $p = (n_1 p_1 + n_2 p_2) / (n_1 + n_2)$

> p

[1] 0.2.

> $q = 1-p$.

[1] 0.8

> $z_{\text{cal}} = (p_1 - p_2) / \sqrt{p_1 q_1 (1/n_1 + 1/n_2)}$

> z_{cal}

[1] 0.9128709.

3) Perform ANOVA for the following data.

Type

Observations

Type	Observations
A	50, 52, 50, 52
B	53, 55, 53
C	60, 53, 57, 56
D	52, 54, 54, 55

→ H_0 : The means are equal for A, B, C, D.

> $x1 = c(50, 52)$

> $x2 = c(53, 55, 53)$

> $x3 = c(60, 53, 57, 56)$

> $x4 = c(52, 54, 54, 55)$

> $d = stock$

(list(b1=x1, b2=x2, b3=x3, b4=x4))

> names(d)

[1] "values" "ind"

> one-way.test(values ~ ind), data=d, var.equal=T

One-way analysis of means.

data : values and ind.
 $F = 11.735$, num df = 3, denom df = 9, pvalue = 0.00133

> anova = anova(values ~ ind, data=d)

> summary(anova)

df	sum_sq	mean_sq	F value	P > F
Ind	71.06	23.68	12.73	0.00133
Residual	9	12.17		

Residuals

∴ pvalue is less than 0.05, we reject H_0 at 5%

LOS

data gives the lives of the 4 types
 & brands.

Following 4 types

of

Type	Life
A	20, 23, 18, 17, 12, 20, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 20, 17, 20
D	15, 14, 16, 13, 14, 16

> Ho: Average life of A, B, C, D are equal.

> $x1 = c(20, 23, 18, 17, 12, 20, 24)$

> $x2 = c(19, 15, 17, 20, 16, 17)$

> $x3 = c(21, 19, 20, 17, 20)$

> $x4 = c(15, 14, 16, 13, 14, 16)$

> $d = stock$ (list(b1=x1, b2=x2, b3=x3, b4=x4))

> names(d)

[1] "values" "ind"

> oneway.test(values ~ test, data=d, var.equal=T)

One-way analysis of means.

data : values and ind.
 $F = 6.1135$, num df = 3, denom df = 20, pvalue = 0.002349

∴ pvalue is less than 0.05, we reject H_0 at 5%.

R

72

$$\text{median} = \text{median}(x \$ \text{maths})$$

$$\text{median} = 37.$$

5.) > x = read.csv ("C:/Users/admin/Desktop/marksheet.csv")

> x

stats	maths
1	40
2	45
3	42
4	15
5	37
6	36
7	49
8	59
9	20
10	27

> am = mean(x \$ stats)

> am.

[1] 37.

> median = median(x \$ stats)

> median.

[1] 38.5.

> n = length(x \$ stats)

> n

[1] 10

> sd = sqrt((n-1) * var(x \$ stats)/n)

[1]

12. 64911

> am1 = mean(x \$ maths)

> am1

[1] 39.4

$$\text{median} = \frac{\text{am} + \text{median}}{2}$$

$$\text{sd} = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

$$\text{sd} = \sqrt{\frac{1}{10-1} \sum_{i=1}^{10} (x_i - 37)^2}$$

PRACTICAL No. 10

Topic :- Non - Parametric test.

Following are the amount of sulphur oxide emitted by some industry in 20 days. Apply sign test to test the hypothesis that the population median is 21.5 at 5% L.O.S.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26

→ H_0 : Population median is 21.5

→ $x = c(17, 15, \dots, 24, 26)$

→ $m_e = 21.5$

→ $s_p = \text{length}(x[x > m_e])$

→ $s_n = \text{length}(x[x < m_e])$

→ $n = s_p + s_n$

→ n

[1] 20

→ $p_r = \text{pbinom}(s_p, n, 0.5)$

→ p_v

[1] 0.4119015

∴ pvalue is ^{greater} than 0.05, we accept H_0 at 5% L.O.S

Note:- If a alternative is $(H_1): m_e \neq$ not equal to or $m_e <$ then $p_r = \text{pbinom}(s_p, n, 0.5)$ & $H_1: m_e >$ then $p_v = \text{pbinom}(s_n, n, 0.5)$

52

2.) Following is the data of 10 observations. Apply sign test, Test the hypothesis that the population median is 625 against the alternative which is more than 625.

\rightarrow H₀: population median is 625
 612, 619, 631, 628, 643, 640, 655, 649, 670, 663

data: x
 $\bar{x} = 128$, pvalue = 0.03338
 alternative hypothesis: true location is greater than 60.
 pvalue is less than 0.05, we reject Ho.

∴ p-value is less than 0.05, we reject H_0 at 5% L.O.S.

Note: If alternative is equal to then, alter = less

$\geq n = sp + sn$
 $\geq n = s(p + n)$

[T] 10

$$\begin{aligned} >_{PV} &= p_{\text{biom}}^{\circ} (s_n, n, 0.5) \\ >_{PV} & \\ [1] & 0.0546875 \end{aligned}$$

\therefore p-value is greater than 0.05, \therefore we accept H_0

Following are a sample. Test the hypothesis, that the population median is \$60 against the alternative which is more than \$60 at 5% L.O.S using Wilcoxon Signed Rank Test.

x.) Using Wilcoxon test, Test the hypothesis, population median is 12 or less than 12.

$x = c(15, 17, \dots, 26)$
 $\text{wilcox.test}(x, \text{alter} = "less", \text{mu} = 12)$

Wilcoxon signed rank test with continuity correction

$V = \frac{68}{455}$, p-value = 0.9986
alternative hypothesis: true

"p-value" is greater than 0.05, \therefore we accept H_0 at 5% loss.

~~alternative hypothesis: true location is less than 12.~~

private is greater than public, \therefore we expect the private

5) The weights of students before and after they stop smoking are given below. Using WSRT test, there is no significance change.

Weight before	Weight after
65	72
75	74
62	72
72	66
	73

→ H_0 : Before & after, there is no change.
 H_1 : There is change.

> $x = c(65, \dots, 72)$

> $y = c(72, \dots, 73)$

> $d = x - y$

> `wilcox.test(d, after = "two.sided", mu = 0)`

Wilcoxon signed rank test with continuity correction.

data: d

V = 4.5, pvalue = 0.4982.

alternative hypothesis: true location is not equal to 0

∴ pvalue is greater than 0.05, ∴ we accept H_0 at 5% LOS.

AM
27/2