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**Experiment No: 2** 

#### Title:

Consider a suitable dataset. For clustering of data instances in different groups, apply different clusteringtechniques (minimum 2). Visualize the clusters using suitable tool.

## **Objective:**

- 1. Understand the various clustering types and how to implement the same using suitable tool (R Studio)
- 2. Use R functions to create K-means Clustering models and hierarchical clustering models

## **Hardware Requirement**

Any CPU with Pentium Processor or similar, 256 MB RAM or more, 1 GB Hard Disk or more

## **Software Requirements:**

32/64-bit Linux/Windows Operating System, latest R Studio

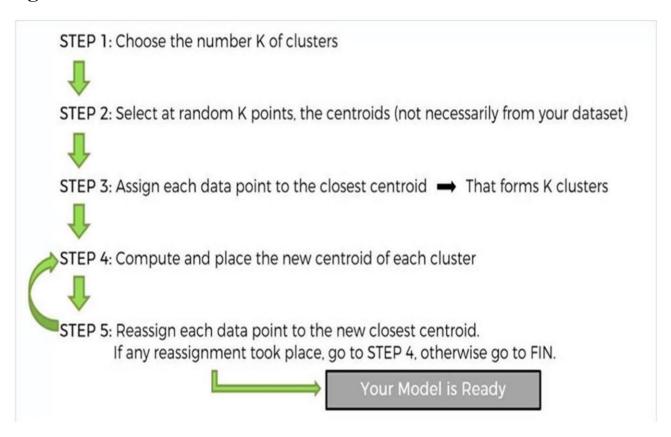
#### **Theory:**

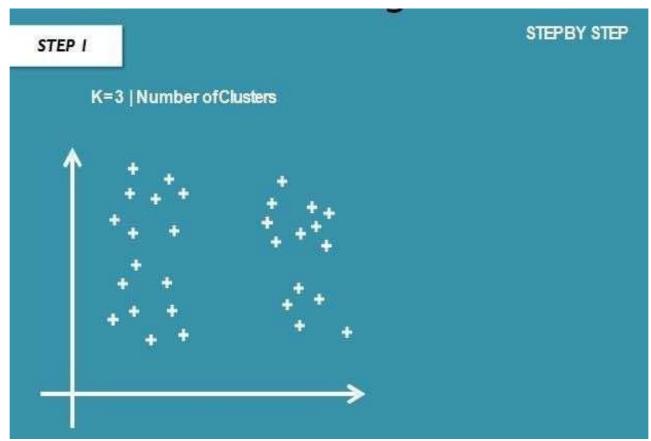
## What is K-means clustering?

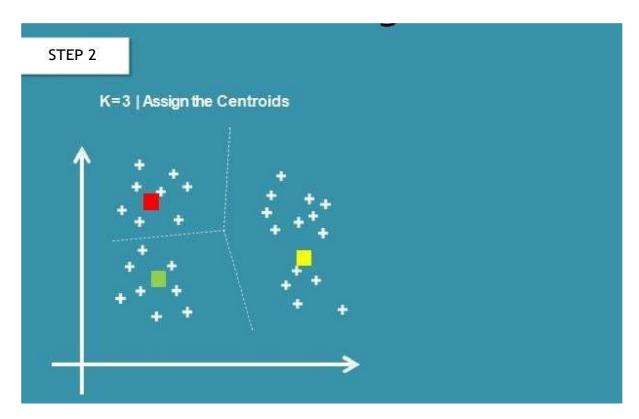
*K*-means clustering is a type of unsupervised learning, which is used when you have unlabeled data (i.e., data without defined categories or groups). The goal of this algorithm is to find groups in the data, with the number of groups represented by the variable *K*. The algorithm works iteratively to assign eachdata point to one of *K* groups based on the features that are provided. Data points are clustered based on feature similarity. The results of the *K*-means clustering algorithm are:

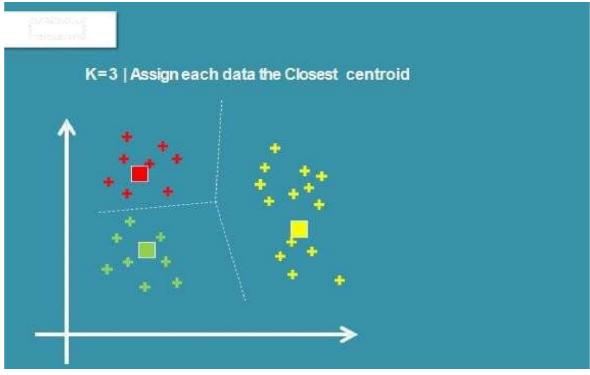
- 1. The centroids of the K clusters, which can be used to label new data
- 2. Labels for the training data (each data point is assigned to a single cluster) Rather than defining groups before looking at the data, clustering allows you to find and analyze the groups that have formed organically. The "Choosing K" section below describes how the number of groups can be determined. Each centroid of a cluster is a collection of feature values which define the resulting groups. Examining the centroid feature weights can be used to qualitatively interpret what kind of group each cluster represents.

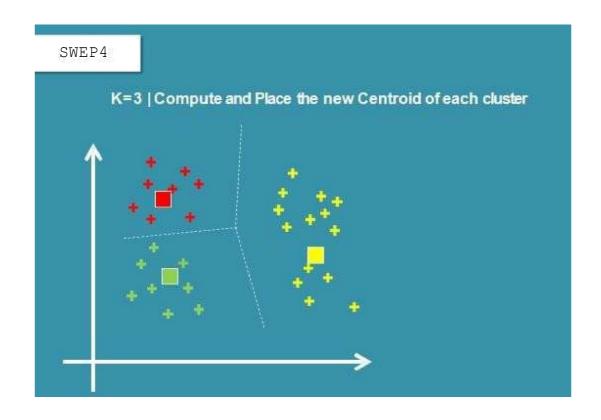
# **Algorithm:**

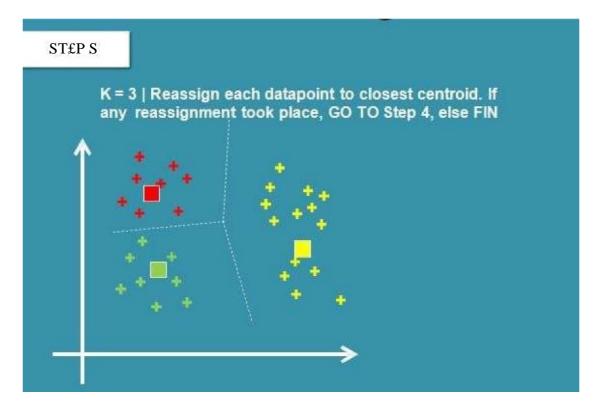






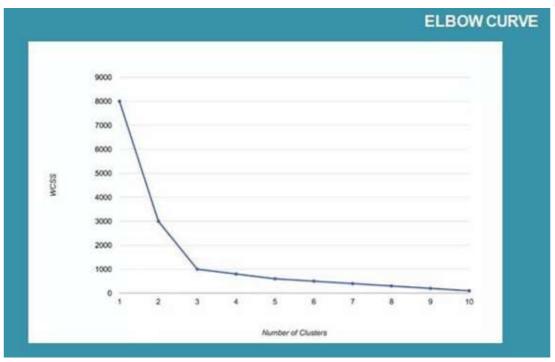






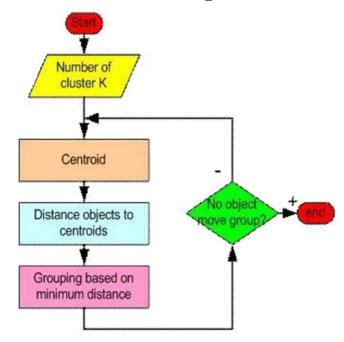
# WITHIN CLUSTER SUM of SQUARES

$$WCSS = \sum_{P_i \text{ in Cluster 1}} distance(P_i, C_1)^2 + \sum_{P_i \text{ in Cluster 2}} distance(P_i, C_2)^2 + \sum_{P_i \text{ in Cluster 3}} distance(P_i, C_3)^2$$



# **Numerical Example**

# **Steps to Perform K-Means Clustering**



As a simple illustration of a k-means algorithm, consider the following data set consisting of

the scores oftwo variables on each of seven individuals:

Subje ct	A	В
ct		
1	1. 0	1.0
2	1. 5	2.0
3	3. 0	4.0
4	5. 0	7.0
5	3. 5	5.0
6	4. 5	5.0
7	3. 5	4.5

This data set is to be grouped into two clusters. As a first step in finding a sensible initial partition, let the A& B values of the two individuals furthest apart (using the Euclidean distance measure), define the initial cluster means, giving:

	Individu al	Mean Vector (centroid)
Group 1	1	(1.0, 1.0)
Group 2	4	(5.0, 7.0)

The remaining individuals are now examined in sequence and allocated to the cluster to which they are closest, in terms of Euclidean distance to the cluster mean. The mean vector is recalculated each time a new member is added. This leads to the following series of steps:

	Cluster 1		Cluster 2	
Ste p	Individu al	Mean Vecto r (centroi d)	Individu al	Mean Vect or (centroi d)
1	1	(1.0, 1.0)	4	(5.0, 7.0)
2	1, 2	(1.2, 1.5)	4	(5.0,

				7.0)
3	1, 2, 3	(1.8, 2.3)	4	(5.0, 7.0)
4	1, 2, 3	(1.8, 2.3)	4, 5	(4.2, 6.0)
5	1, 2, 3	(1.8, 2.3)	4, 5, 6	(4.3, 5.7)
6	1, 2, 3	(1.8, 2.3)	4, 5, 6, 7	(4.1, 5.4)

Now the initial partition has changed, and the two clusters at this stage having the following characteristics:

	Individual	Mean Vector (centroid)
Cluster 1	1, 2, 3	(1.8, 2.3)
Cluster 2	4, 5, 6, 7	(4.1, 5.4)

But we cannot yet be sure that each individual has been assigned to the right cluster. So, we compare each

individual's distance to its own cluster mean and to that of the opposite cluster. And we find:

Individu	Distance	Distance
	to mean	to mean
al	(centroid)	(centroid)
ui ui	of	of
	Cluster	Cluster
	1	2
1	1.5	5.4
2	0.4	4.3
3	2.1	1.8
4	5.7	1.8
5	3.2	0.7
6	3.8	0.6
7	2.8	1.1

Only individual 3 is nearer to the mean of the opposite cluster (Cluster 2) than its own (Cluster 1). In other words, each individual's distance to its own cluster mean should be smaller that the distance to the other cluster's mean (which is not the case with individual 3). Thus, individual 3 is relocated to Cluster 2 resulting in the new partition:

	Individua 1	Mean Vector (centroid)
Cluster 1	1, 2	(1.3, 1.5)
Cluster 2	3, 4, 5, 6, 7	(3.9, 5.1)

The iterative relocation would now continue from this new partition until no more relocations occur. However, in this example each individual is now nearer its own cluster mean than that of the other cluster and the iteration stops, choosing the latest partitioning as the final cluster solution.

## R implementation

The K-Means function, provided by the *clustep* ackage, is used as follows:

kmeans 
$$(x, centers, iter.max = 10, nstart = 1)$$

- Where,

\_ x

numeric matrix of data, or an object that can be coerced to such a matrix (such as a numeric

vector or a dataframe with all numeric columns).

centers

either the number of clusters, say k, or a set of initial (distinct) cluster centers. If a number, a random set of(distinct) rows in x is chosen as the initial centers.

- iter.max

the maximum number of iterations allowed.

- nstart

if centers are a number, how many random sets should be chosen?

#### **IRIS** dataset

This is perhaps the best-known database to be found in the pattern recognition literature. The data setcontains 3 classes of 50 instances each, where each class refers to a type of iris plant.

#### **Attribute Information:**

- sepal length in cm
- sepal width in cm
- petal length in cm
- petal width in cm
- · class:
- 1 Iris Setosa
- 2 Iris Versicolour

## **Steps**

3 Iris Virginica

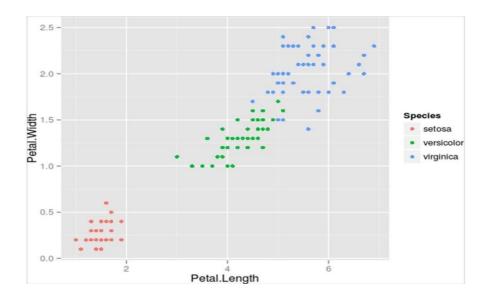
- 1. Set working directory
- 2. Get data from datasets
- 3. Execute the model
- 4. View the output
- 5. Plot the results

#### **CODE:**

```
library(ggplot2)
ggplot(iris, aes(Petal.Length, Petal.Width, color
= Species)) +
geom_point()
set.seed(20)
irisCluster <- kmeans(iris[, 3:4], 3, nstart = 20) irisCluster</pre>
```

### **Output:**

```
K-means clustering with 3 clusters of sizes 50, 52, 48
Cluster means:
Petal.Length Petal.Width
  1.462000
       0.246000
2
  4.269231
       1.342308
  5.595833 2.037500
Clustering vector:
Within cluster sum of squares by cluster:
[1] 2.02200 13.05769 16.29167
(between_SS / total_SS = 94.3 %)
```



## **Hierarchical Clustering**

# What is Hierarchical clustering?

Given a set of N items to be clustered, and an NxN distance (or similarity) matrix, the basic process of Johnson's (1967) hierarchical clustering is this:

- Start by assigning each item to its own cluster, so that if you have N items, you now have N clusters, each containing just one item. Let the distances (similarities) between the clusters equal the distances(similarities) between the items they contain.
- Find the closest (most similar) pair of clusters and merge them into a single cluster, so that now youhave one less cluster.
- Compute distances (similarities) between the new cluster and each of the old clusters.
- Repeat steps 2 and 3 until all items are clustered into a single cluster of size N.

# **R** Implementation

```
hclust(d, method = "complete", members = NULL)
## S3 method for class 'hclust'
plot(x, labels = NULL, hang = 0.1, check =
    TRUE, axes = TRUE, frame.plot =
    FALSE, ann = TRUE,main = "Cluster
    Dendrogram",
    sub = NULL, xlab = NULL, ylab = "Height", ...)
```

### **Arguments**

d a dissimilarity structure as produced by dist.

method the agglomeration method to be used. This should be (an unambiguous

abbreviation of) one of "ward.D", "ward.D2", "single", "complete",

"average" (= UPGMA), "mcquitty" (=WPGMA), "median" (= WPGMC) or

"centroid" (= UPGMC).

members NULL or a vector with length size of d. See the

'Details' section.x an object of the type produced by hclust.

hang The fraction of the plot height by which labels should hang below the rest

of the plot. Anegative value will cause the labels to hang down from 0.

check logical indicating if the x object should be checked for validity. This

check is not necessary when x is known to be valid such as when it is the direct result of hclust(). The default is check=TRUE, as invalid inputs may

crash **R** due to memory violation in the internal C plotting code.

labels A character vector of labels for the leaves of the tree. By default the row

names or rownumbers of the original data are used. If labels = FALSE no

labels at all are plotted.

axes, logical flags as in

plot.default.frame.plot,

ann

main, sub, character strings for title. sub and xlab have a non-NULL default when there's axlab, ylab tree\$call.

... Further graphical arguments. E.g., cex controls the size of the labels (if plotted) in the same way as text.

Step 3 can be done in different ways, which is what distinguishes *single-linfk*rom *complete-link*d *average-link*ustering

#### Mtcars dataset

The data was extracted from the 1974 *Motor TrenUS* magazine, and comprises fuel consumption and 10 aspects of automobile design and performance for 32 automobiles (1973–74 models)

A data frame with 32 observations on 11 variables.

[, 1] mpg Miles/(US) gallon [, 2] cyl Number of cylinders [, 3] disp Displacement (cu.in.)[, 4] hp Gross horsepower [, 5] drat Rear axle ratio [, 6] wt Weight (lb/1000)

```
[, 7] qsec 1/4-mile
time[, 8] vs
V/S
[, 9] am Transmission (0 = automatic, 1 = manual)
[,10] gear Number of forward
gearsNumber of
carburetors
[,11] carb
```

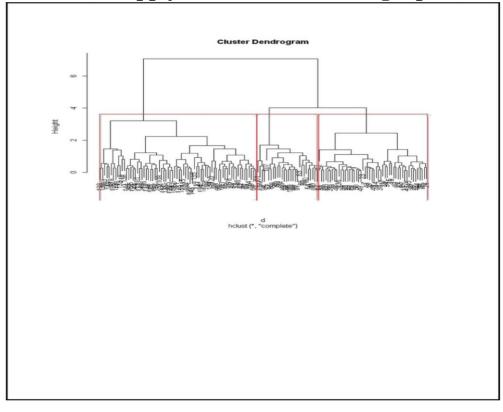
In general, there are many choices of cluster analysis methodology. The hclust function in R uses the complete linkage method for hierarchical clustering by default. This particular clustering method defines

the cluster distance between two clusters to be the maximum distance between their individual components. At every stage of the clustering process, the two nearest clusters are merged into a newcluster.

With the **distance materix**d in previous tutorial, we can use various techniques of cluster analysis for relationship discovery. For example, in the data set mtcars, we can run the distance matrix with hclust, and plot a dendrogram that displays a hierarchical relationship among the vehicles.

> d <- dist(as.matrix(mtcars)) # find distance matrix

> hc <- hclust(d) # apply hirarchical clustering > plot(hc) # plot the



# dendrogram

Conclusionence we a	re able to der	monstrate variou	s clustering	method using	R Tool.
			$\mathcal{C}$	0	