

Polynomial Regression

Estimated time needed: 15 minutes

Objectives

After completing this lab you will be able to:

- Use scikit-learn to implement Polynomial Regression
- Create a model, train, test and use the model

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Importing Needed packages

```
In [1]:
         import matplotlib.pyplot as plt
         import pandas as pd
         import pylab as pl
         import numpy as np
         import wget
         %matplotlib inline
```

Downloading Data

To download the data, we will use !wget to download it from IBM Object Storage.

```
In [2]:
         url = 'https://cf-courses-data.s3.us.cloud-object-storage.appdomain.cloud/IBMDeveloperSkillsNetwork-ML0101EN-SkillsNetwork/la
         myfile = wget.download(url)
```

!wget -O FuelConsumption.csv https://cf-courses-data.s3.us.cloud-object-storage.appdomain.cloud/IBMDeveloperSkillsNetwork-ML0101EN-SkillsNetwork/labs/Module%202/data/FuelConsumptionCo2.csv

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Understanding the Data

FuelConsumption.csv:

We have downloaded a fuel consumption dataset, **FuelConsumption.csv**, which contains model-specific fuel consumption ratings and estimated carbon dioxide emissions for new light-duty vehicles for retail sale in Canada. **Dataset source**

- MODELYEAR e.g. 2014
- MAKE e.g. Acura
- MODEL e.g. ILX
- VEHICLE CLASS e.g. SUV
- **ENGINE SIZE** e.g. 4.7
- CYLINDERS e.g 6
- TRANSMISSION e.g. A6
- FUEL CONSUMPTION in CITY(L/100 km) e.g. 9.9
- FUEL CONSUMPTION in HWY (L/100 km) e.g. 8.9
- FUEL CONSUMPTION COMB (L/100 km) e.g. 9.2
- CO2 EMISSIONS (g/km) e.g. 182 --> low --> 0

Reading the data in

```
In [4]:
    df = pd.read_csv(myfile)
    # take a Look at the dataset
    df.head()
```

Out[4]:		MODELYEAR	MAKE	MODEL	VEHICLECLASS	ENGINESIZE	CYLINDERS	TRANSMISSION	FUELTYPE	FUELCONSUMPTION_CITY	FUELCONSUMPTIO
	0	2014	ACURA	ILX	COMPACT	2.0	4	AS5	Z	9.9	
	1	2014	ACURA	ILX	COMPACT	2.4	4	M6	Z	11.2	
	2	2014	ACURA	ILX HYBRID	COMPACT	1.5	4	AV7	Z	6.0	
	3	2014	ACURA	MDX 4WD	SUV - SMALL	3.5	6	AS6	Z	12.7	
	4	2014	ACURA	RDX AWD	SUV - SMALL	3.5	6	AS6	Z	12.1	
	4										•

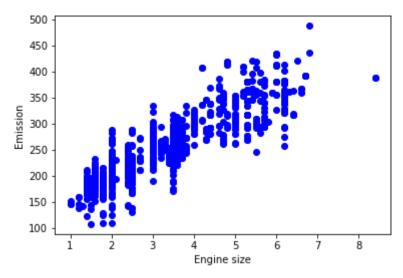
Lets select some features that we want to use for regression.

```
cdf = df[['ENGINESIZE','CYLINDERS','FUELCONSUMPTION_COMB','CO2EMISSIONS']]
cdf.head(9)
```

Out[5]:		ENGINESIZE	CYLINDERS	FUELCONSUMPTION_COMB	CO2EMISSIONS
	0	2.0	4	8.5	196
	1	2.4	4	9.6	221
;	2	1.5	4	5.9	136
:	3	3.5	6	11.1	255
	4	3.5	6	10.6	244
!	5	3.5	6	10.0	230
(6	3.5	6	10.1	232
•	7	3.7	6	11.1	255
:	8	3.7	6	11.6	267

Lets plot Emission values with respect to Engine size:

```
plt.scatter(cdf.ENGINESIZE, cdf.CO2EMISSIONS, color='blue')
plt.xlabel("Engine size")
plt.ylabel("Emission")
plt.show()
```



Creating train and test dataset

Train/Test Split involves splitting the dataset into training and testing sets respectively, which are mutually exclusive. After which, you train with the training set and test with the testing set.

```
In [7]:
    msk = np.random.rand(len(df)) < 0.8
    train = cdf[msk]
    test = cdf[~msk]</pre>
```

Polynomial regression

Sometimes, the trend of data is not really linear, and looks curvy. In this case we can use Polynomial regression methods. In fact, many different regressions exist that can be used to fit whatever the dataset looks like, such as quadratic, cubic, and so on, and it can go on and on to infinite degrees.

In essence, we can call all of these, polynomial regression, where the relationship between the independent variable x and the dependent variable y is modeled as an nth degree polynomial in x. Lets say you want to have a polynomial regression (let's make 2 degree polynomial):

$$y = b + \theta_1 1x + \theta_2 2x^2$$

Now, the question is: how we can fit our data on this equation while we have only x values, such as **Engine Size**? Well, we can create a few additional features: 1, x, and x^2 .

PolynomialFeatures() function in Scikit-learn library, drives a new feature sets from the original feature set. That is, a matrix will be generated consisting of all polynomial combinations of the features with degree less than or equal to the specified degree. For example, lets say the original feature set has only one feature, *ENGINESIZE*. Now, if we select the degree of the polynomial to be 2, then it generates 3 features, degree=0, degree=1 and degree=2:

```
In [8]:
        from sklearn.preprocessing import PolynomialFeatures
        from sklearn import linear model
        train x = np.asanyarray(train[['ENGINESIZE']])
        train y = np.asanyarray(train[['CO2EMISSIONS']])
         test x = np.asanyarray(test[['ENGINESIZE']])
        test_y = np.asanyarray(test[['CO2EMISSIONS']])
         poly = PolynomialFeatures(degree=2)
        train x poly = poly.fit transform(train x)
         train x poly
       array([[ 1. , 2. , 4. ],
Out[8]:
              [1., 2.4, 5.76],
              [1., 1.5, 2.25],
              [1., 3., 9.],
              [1., 3.2, 10.24],
              [1., 3.2, 10.24]])
```

fit_transform takes our x values, and output a list of our data raised from power of 0 to power of 2 (since we set the degree of our polynomial to 2).

The equation and the sample example is displayed below.

$$\begin{bmatrix} v_{-1} \\ v_{-2} \\ \vdots \\ v_n \end{bmatrix} \longrightarrow \begin{bmatrix} \begin{bmatrix} 1 & v_{-1} & v_{-1}^2 \\ \begin{bmatrix} 1 & v_{-2} & v_{-2}^2 \end{bmatrix} \\ \vdots & \vdots & \vdots \\ \begin{bmatrix} 1 & v_n & v_n^2 \end{bmatrix} \end{bmatrix}$$

$$\begin{bmatrix} 2. \\ 2.4 \\ 1.5 \\ \vdots \end{bmatrix} \longrightarrow \begin{bmatrix} 1 & 2. & 4. \\ 1 & 2.4 & 5.76 \\ 1 & 1.5 & 2.25 \end{bmatrix}$$

$$\vdots & \vdots & \vdots$$

It looks like feature sets for multiple linear regression analysis, right? Yes. It Does. Indeed, Polynomial regression is a special case of linear regression, with the main idea of how do you select your features. Just consider replacing the x with x_1 , x_1^2 with x_2 , and so on. Then the degree 2 equation would be turn into:

$$y=b+ heta_1x_1+ heta_2x_2$$

Now, we can deal with it as 'linear regression' problem. Therefore, this polynomial regression is considered to be a special case of traditional multiple linear regression. So, you can use the same mechanism as linear regression to solve such a problems.

so we can use **LinearRegression()** function to solve it:

```
In [9]:
    clf = linear_model.LinearRegression()
    train_y_ = clf.fit(train_x_poly, train_y)
    # The coefficients
    print ('Coefficients: ', clf.coef_)
    print ('Intercept: ',clf.intercept_)
```

Coefficients: [[0. 50.53065979 -1.43786495]] Intercept: [107.48902094]

As mentioned before, **Coefficient** and **Intercept**, are the parameters of the fit curvy line. Given that it is a typical multiple linear regression, with 3 parameters, and knowing that the parameters are the intercept and coefficients of hyperplane, sklearn has estimated them from our new set of feature sets. Lets plot it:

```
In [10]:
    plt.scatter(train.ENGINESIZE, train.CO2EMISSIONS, color='blue')
    XX = np.arange(0.0, 10.0, 0.1)
    yy = clf.intercept_[0]+ clf.coef_[0][1]*XX+ clf.coef_[0][2]*np.power(XX, 2)
    plt.plot(XX, yy, '-r' )
```

```
plt.xlabel("Engine size")
            plt.ylabel("Emission")
          Text(0, 0.5, 'Emission')
Out[10]:
              500
              450
              400
              350
           Emission
              300
              250
              200
              150
              100
                                                                     10
                                         Engine size
```

Evaluation

```
from sklearn.metrics import r2_score

test_x_poly = poly.fit_transform(test_x)
test_y_ = clf.predict(test_x_poly)

print("Mean absolute error: %.2f" % np.mean(np.absolute(test_y_ - test_y)))
print("Residual sum of squares (MSE): %.2f" % np.mean((test_y_ - test_y) ** 2))
print("R2-score: %.2f" % r2_score(test_y,test_y_ ) )
```

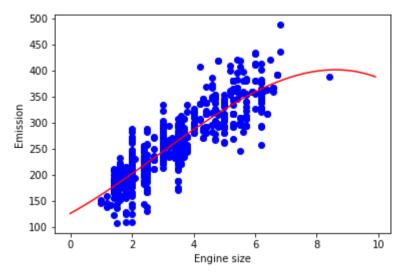
Mean absolute error: 23.35
Residual sum of squares (MSE): 933.62

R2-score: 0.74

Practice

Try to use a polynomial regression with the dataset but this time with degree three (cubic). Does it result in better accuracy?

```
In [20]:
          # write your code here
          poly3 = PolynomialFeatures(degree=3)
          train x poly3 = poly3.fit transform(train x)
          clf3 = linear model.LinearRegression()
          train y3 = clf3.fit(train_x_poly3, train_y)
          # The coefficients
          print ('Coefficients: ', clf3.coef )
          print ('Intercept: ',clf3.intercept )
          plt.scatter(train.ENGINESIZE, train.CO2EMISSIONS, color='blue')
          XX = np.arange(0.0, 10.0, 0.1)
          yy = clf3.intercept [0]+ clf3.coef [0][1]*XX + clf3.coef [0][2]*np.power(XX, 2) + clf3.coef [0][3]*np.power(XX, 3)
          plt.plot(XX, vy, '-r')
          plt.xlabel("Engine size")
          plt.ylabel("Emission")
          test x poly3 = poly3.fit transform(test x)
          test y3 = clf3.predict(test x poly3)
          print("Mean absolute error: %.2f" % np.mean(np.absolute(test y3 - test y)))
          print("Residual sum of squares (MSE): %.2f" % np.mean((test y3 - test y) ** 2))
          print("R2-score: %.2f" % r2 score(test y,test y3 ))
         Coefficients: [[ 0.
                                      32.52974171 3.60601294 -0.42601376]]
         Intercept: [126.3192442]
         Mean absolute error: 23.25
         Residual sum of squares (MSE): 924.80
         R2-score: 0.74
```



► Click here for the solution

Want to learn more?

IBM SPSS Modeler is a comprehensive analytics platform that has many machine learning algorithms. It has been designed to bring predictive intelligence to decisions made by individuals, by groups, by systems – by your enterprise as a whole. A free trial is available through this course, available here: SPSS Modeler

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Thank you for completing this lab!

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