# Online ensembles for non-stationary data streams

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## 1. INTRODUCTION

<ul> <li>Online Machine Learning (chunk/one-at-a-tim</li> </ul>	•	Online	Machine	Learning	(chunk	/one-at-a-time
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Non/stationary data streams

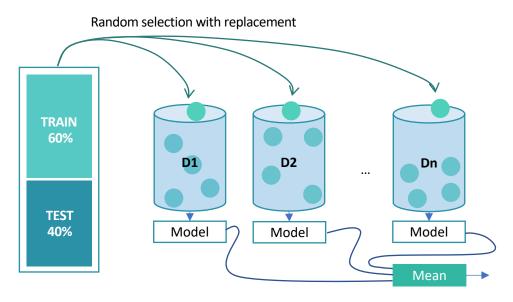
Concept drift (active/reactive)

Plasticity (learn new concepts) / Stability (retaining knowledge)

Diversity in ensembles

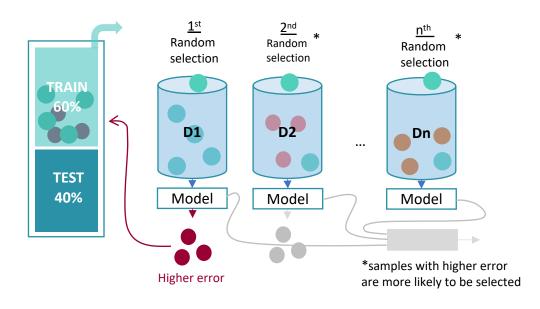
#### 1. INTRODUCTION

#### **BAGGING**



$$P(K = k) = {N \choose k} {1 \choose N}^k \left(1 - \frac{1}{N}\right)^{N-k} \bigg| \Rightarrow K \sim \frac{\exp(-1)}{k!} \qquad Poisson \\ (\lambda = 1)$$

#### **BOOSTING**



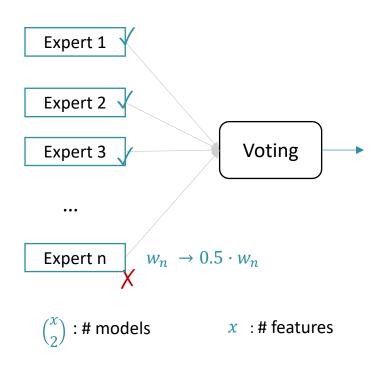
$$P(K=k) \sim {Poisson \atop (\lambda=1)} \Rightarrow \left\{egin{array}{l} {
m Correct \ classification,} & \lambda \ {
m is \ decreased} \\ {
m Misclassification,} & \lambda \ {
m is \ increased} \end{array}
ight.$$

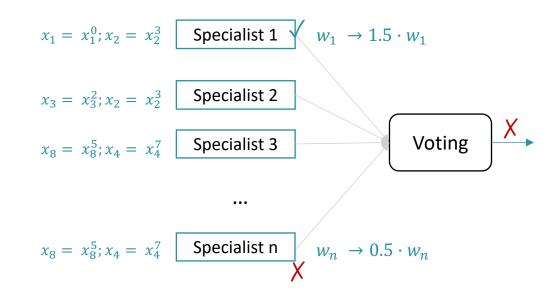
**ONLINE BAGGING (2001)** 

**ONLINE BOOSTING (2001)** 

## 1. INTRODUCTION

"Learning simple things really well." - Blum (1997)

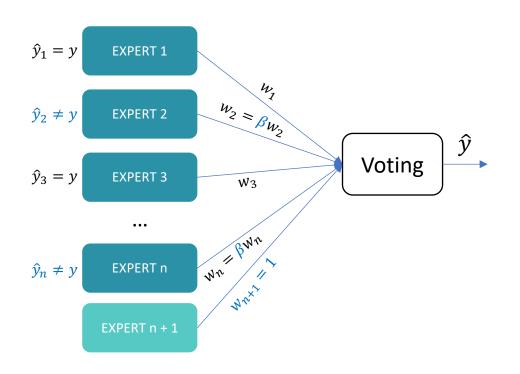




WEIGHTED MAJORITY(1988)

WINNOW SPECIALIST (1997) — version of WINNOW (1988)

#### 2. REACTIVE APPROACHES

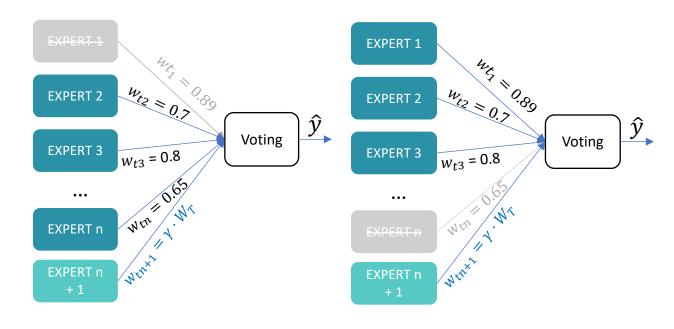


Hyperparameters:

 $\beta$  (reduction factor),  $\theta$ (threshold), p(period)

MISTAKE'S  $BOUND \qquad M_{t_2} - M_{t_1} \leq \frac{\log \left(W_{t_1}/W_{t_2}\right)}{\log (\frac{2}{1+\beta+2\gamma})} \\ \qquad where \ \beta+2\cdot\gamma<1$ 

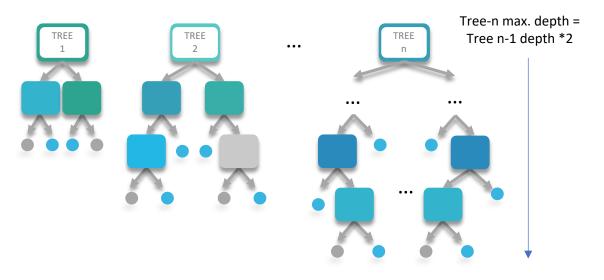
#### **PRUNING TECHNIQUES:**



Dynamic Weighted Majority (2003)

Additive Expert Ensembles (2005)

#### 2. REACTIVE APPROACHES



HOEFFDING'S BOUND

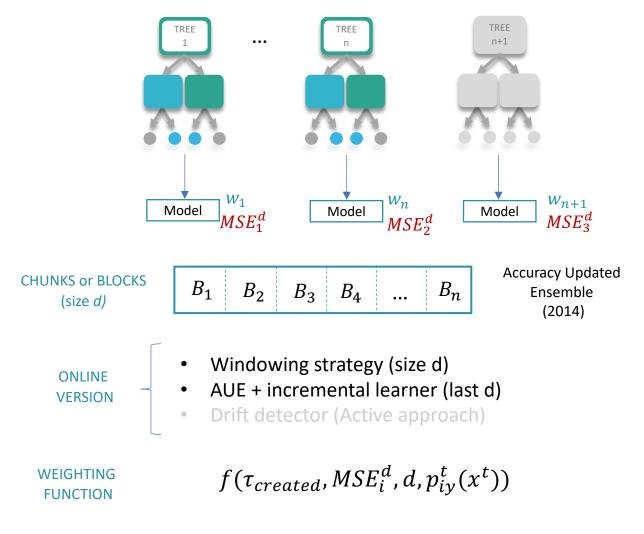
$$P(\overline{X} - E[\overline{X}] \ge t) \le e^{-2\pi t^2}$$

DELETE NODES

Two options:

- Delete oldest node (top)
- Restart Tree

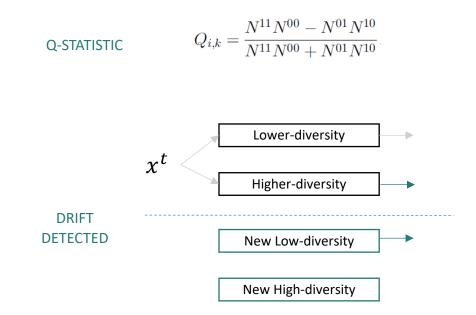
Adaptive Size Hoeffding Trees (2009)



Online Accuracy Updated Ensemble (2014)

#### 3. ACTIVE APPROACHES

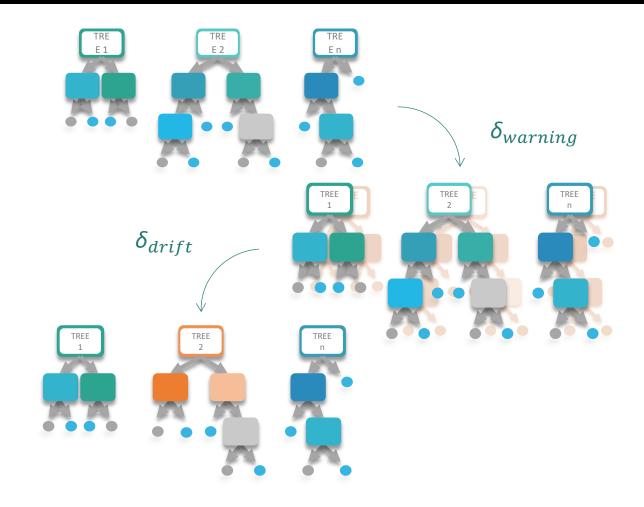
#### **ONLINE BAGGING** Random selection with replacement Dn **TEST** Model Model Model 40% Mean $P(K = k) = {N \choose k} {1 \choose N}^k \left(1 - \frac{1}{N}\right)^{N-k} \implies K \sim \frac{\exp(-1)}{k!}$ Poisson $(\lambda = 1)$ Window **ADWIN** $W_0$ $W_1$



Hyperparameters:  $p_l$  (diversity), drift detector,  $W_{old/new}$ 

Diversity for Dealing with Drifts (2012)

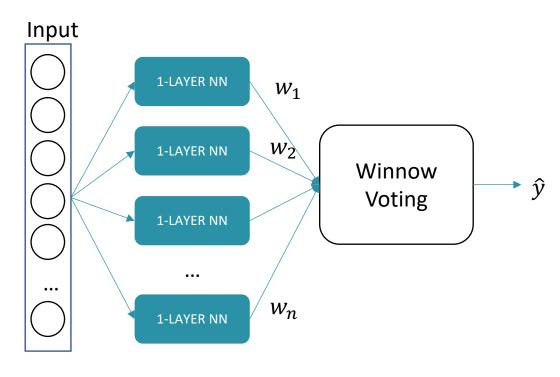
## 3. ACTIVE APPROACHES



- Hoeffding Trees
- ADWIN
- $(\delta_w)$ : warning sent
- $(\delta_d)$ : drift is confirmed

Adaptive random forests for evolving data stream classification (2017)

#### 4. OTHER APPROACHES



$$FUNCTION_{j} = \sum_{s=1}^{s} c_{j}(s) \left( f'_{j}(d_{js}) \left( f_{j}^{-1}(d_{js}) - \sum_{i=0}^{l} w_{ji} x_{is} \right) \right)^{2}$$

Ensemble of online neural networks for non-stationary and imbalanced datastreams (2013)

#### Original Winnow algorithm:

If 
$$\hat{y} = y$$
:
Do nothing
Elif  $\hat{y} = 1$  and  $y = 0$ :
$$\forall x_i = 1, w_i = 0 \qquad \text{(demotion)}$$
Elif  $\hat{y} = 0$  and  $y = 1$ :
$$\forall x_i = 1, w_i = \alpha \cdot w_i \quad \text{(promotion)}$$

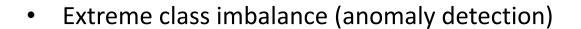
#### **Proposed Winnow algorithm:**

Separate weights for each class (wmin and wmaj):

$$\hat{y} = arg \max \left( \sum_{j=1}^{n} (p_j^t = 1) \cdot (\gamma \cdot wmin_j + wmaj_j) + (p_j^t = 2) \cdot (wmin_j + wmaj_j) \right)$$

Three parameters:  $\alpha$  (promotion),  $\beta$  (demotion) and  $\gamma$  (imbalance)

## 5. CONCLUSION & FUTURE RESEARCH



Delayed or non-available data

Online cross-validation

Concept-drift interdependencies (HMM?)

Fine-tuning online heuristics

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