INDIAN INSTITUTE OF TECHNOLOGY, GUWAHATI

POWER ENGINEERING LAB

EE 572

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ASSIGNMENT-4 (part 1)

Do write program codes to execute the 'Forward-backward sweep load flow algorithm' for 33-node, 69-node, and 52-node test distribution networks.

Procedure: For "Forward-backward sweep load flow" first we have to calculate the load current at each bus and after the load current calculation be have to calculate the line current for all line. to calculate the line current we have to start the calculation from end points of the system this procedure is called "BACKWARD" sweep. after the calculation of line current we will calculate the value of voltage at each node, this procedure is called as FORWARD sweep. after complete calculation of voltage we will find the difference between new voltage and old voltage check it's value. error should be less then our accuracy or equal. Then we will stop the iteration /calculation other wise we will continue to perform forward-backward sweep method(continue with iteration).

For performing the forward-backward sweep method first we have to calculate the end points of the system like for the 33-bus system end points are :18,22,25 & 33.similarly for the system 69 and 52 also.

The code for finding the end points is:

```
count=1;
for line_no=length(linedata)+1:-1:1
   if line_no<length(linedata)
        if linedata(line_no+1,1)~=linedata(line_no,2)
             end_point(count)=linedata(line_no,2);
             count=count+1;
   end
end
if line_no==length(linedata)+1
   end_point(count)=length(linedata)+1;
   count=count+1;</pre>
```

```
end
end
```

We know that apparent power for a bus is:

$$S = V.I^*$$

We want to calculate the load current at each bus so:

$$I_i = S_i^* / V_i^* = (P_i - j * Q_i) / V_i^*$$

this is for calculation of load current at ith bus.

for first iteration we will calculate the current at the reference voltage (reference voltage magnitude is 1 and angle is 0 $^{\rm o}$).

```
%load current at each bus
for i=1:length(linedata)+1
    load_current(i,1)=(P(i)-j*Q(i))/conj (Vlt_new(i,1));
end
For calculation of load
current at each bus
```

after load current calculation we will calculate the value of line current

Line current $_{i-1}$ = load current $_i$ + Line current $_i$

2<=i<=33, for all load bus

Code for the calculation of line current is:

```
% finding the line or bus current
    for i=1:length(end_point)
    endbus = end_point(i);
    for k= endbus:-1:1
        p=k;
        if p>0
        if p== endbus
            bus_current(p,1)=k;
            bus_current(p,2)=bus_current(p,2)+load_current(p);
        else
        if linedata(p,1)== linedata(p,2)-1

        present bus=linedata(p,1);
```

```
next bus=linedata(p,2);
            bus current(present bus,1) = present bus;
            bus current (present bus, 2) =
bus_current(present_bus, 2) + load_current(present_bus) +
bus current(next bus, 2);
        else
            present bus=linedata(p,1);
            next bus=linedata(p,2);
            bus_current(present_bus,1)=present_bus;
bus current(present bus, 2) = bus current(present bus, 2) + bus current(next bus, 2)
            break
        end
         end
         end
        end
    end
```

our backward sweep is completed and we are going to calculate the value of voltage by forward sweep the code is :

we successfully calculate the value of load current, line current and bus voltages.

now we have to calculate the error between old voltage and new voltage see the error is less the or accuracy or not, if error is less than our accuracy then we will stop the iteration other we will continue with the code:

Complete code for the forward-backward sweep is

```
while max v err r>=0.0001 & no iter<100
max v err r >= 0.0001
Vlt old=Vlt new;
bus current=zeros(length(busdata(:,1)),2);
    %load current at each bus
    for i=1:length(linedata)+1
        load current(i,1)=(P(i)-j*Q(i))/conj (Vlt new(i,1));
    end
 % finding the line or bus current
    for i=1:length(end point)
     endbus = end point(i);
        for k= endbus:-1:1
        p=k;
         if p>0
         if p== endbus
            bus current (p, 1) = k;
            bus current(p,2)=bus current(p,2)+load current(p);
        if linedata(p,1) == linedata(p,2) -1
            present bus=linedata(p,1);
            next bus=linedata(p,2);
            bus current(present bus,1) = present bus;
            bus current (present bus, 2) =
bus current (present bus, 2) + load current (present bus) +
bus current(next bus,2);
        else
            present bus=linedata(p,1);
            next bus=linedata(p,2);
            bus current(present bus,1) = present bus;
bus current(present bus, 2) = bus current(present bus, 2) + bus current(next bus, 2)
            %k=0;
            break
        end
         end
         end
        end
    end
    for point=1:length(linedata(:,1))
        starting node=linedata(point,1);
        ending node=linedata(point,2);
```

```
lineno=linedata(point,5);
    Vlt_new(ending_node,1)=Vlt_new(starting_node,1)=
bus_current(lineno+1,2)*z(point,3);

end
    error=Vlt_new-Vlt_old;

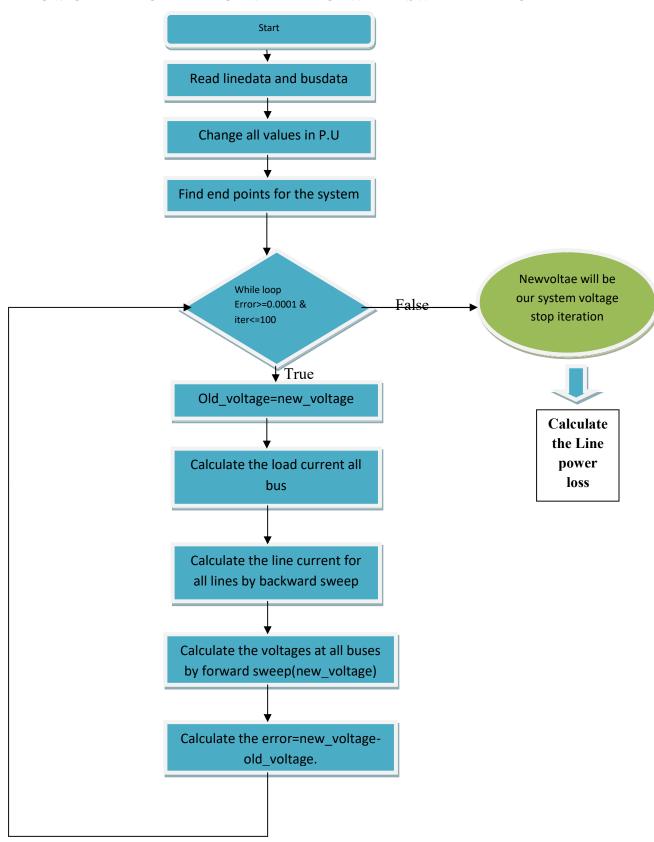
max_v_err_r=max(abs(error));
busdata(:,3)=abs(Vlt_new);

no_iter=no_iter+1;
end
```

After calculation of voltage at all node we will calculate the power loss for the system the code for power loss :

```
Ploss=0;
for point=1:length(linedata(:,1))
        lineno=linedata(point,5);
        Ploss=Ploss+abs(bus_current(lineno+1,2))^2*real(z(point,3));
end
```

FLOW CHART FOR THE FORWARD-BACKWARD SWEEP METHOD



Results for 69-bus system

- (1) End points are = 69 67 65 52 50 46 35 27
- (2) Final system voltages are

Bus no.	Voltage (complex)	Voltage in magnitude	
1	1.+ 0.0i	1.0000	
2(Max. voltage bus)	0.9999 - 2.14e-05i	1.0000	
3	0.999 - 4.28e-05i	0.9999	
4	0.999- 0.00010i	0.9998	
5	0.999 - 0.00032i	0.9990	
6	0.9900 + 0.000852i	0.9901	
7	0.98079 + 0.002074i	0.9808	
8	0.978574 + 0.0023629i	0.9786	
9	0.9774393 + 0.002511i	0.9774	
10	0.972 + 0.0039372i	0.9724	
11	0.97131 + 0.00421i	0.9713	
12	0.968142 + 0.005096i	0.9682	
13	0.965211 + 0.0058i	0.9652	
14	0.96231 + 0.00662264i	0.9623	
15	0.95944 + 0.007373i	0.9595	
16	0.95889755 + 0.00751141i	0.9589	
17	0.9580151 + 0.0077411i	0.9580	
18	0.9580 + 0.00774i	0.9580	
19	0.957539 + 0.00788i	0.9576	
20	0.957240 + 0.007971i	0.9573	
21	0.95675+ 0.00811i	0.9568	
22	0.956749 + 0.00811i	0.9568	
23	0.9566779+ 0.008139i	0.9567	
24	0.9565210 + 0.0081i	0.9566	
25	0.95634 + 0.008232i	0.9564	
26	0.956278 + 0.008253i	0.9563	
27	0.95625848 + 0.00825i	0.9563	
28	0.9999260 - 4.7230279e-05i	0.9999	
29	0.99985 - 9.260e-05i	0.9999	
30	0.99973 - 5.550e-05i	0.9997	
31	0.9997119 - 4.8956e-05i	0.9997	
32	0.99961 - 1.62101e-05i	0.9996	
33	0.999349 + 6.0997e-05i	0.9993	
34	0.99901332 + 0.000163i	0.9990	
35	0.99895 + 0.00018159i	0.9989	
36	0.99992 - 5.182e-05i	0.9999	
37	0.99975 - 0.00016365i	0.9997	
38	0.9996 - 0.00020581i	0.9996	
39	0.99955 - 0.0002179i	0.9995	
40	0.999541 - 0.0002186i	0.9995	

42 0.998 43 0.998	385 - 0.00041007i 3551 - 0.00049i 351 - 0.00050148i 350 - 0.0005041i 34051 - 0.000535597i	0.9988 0.9986 0.9985 0.9985	
43 0.999	351 - 0.00050148i 350 - 0.0005041i	0.9985	
0.55	350 - 0.0005041i		
44 0.00		0.9985	
0.330	2/051 _ 0 000525507;		
45 0.998	34031 - 0.0003333371	0.9984	
46 0.998	3404765 - 0.0005358i	0.9984	
47 0.999	97894 - 0.0001345i	0.9998	
48 0.998	35431 - 0.00091552i	0.9985	
49 0.994	16932 - 0.003326i	0.9947	
50 0.994	1146 - 0.00366i	0.9942	
51 0.978	35377 + 0.002367i	0.9785	
	35280 + 0.002371i	0.9785	
	1652 + 0.0028763i	0.9747	
54 0.97	141 + 0.003305i	0.9714	
	593 + 0.00389i	0.9669	
56 0.965	256 + 0.004456i	0.9626	
	00 + 0.0108582i	0.9401	
	3935 + 0.0140144i	0.9290	
59 0.924	163 + 0.0152i	0.9248	
60 0.919	958 + 0.01685i	0.9197	
61 0.913	21 + 0.01781i	0.9123	
62 0.91	188 + 0.017853i	0.9121	
	14895 + 0.01791i	0.9117	
64 0.909	0.909585 + 0.018149i 0.9098		
65(minimum voltage bus) 0.909	901 + 0.018223i	0.9092	
66 0.97	12511 + 0.004237i	0.9713	
67 0.97	0.971250 + 0.0042364i 0.9713		
68 0.96	781 + 0.005197i	0.9678	
69 0.96	781 + 0.005197i	0.9678	

Results for 33-bus system

(1) End points are = 33 25 22 18

(2) Final system voltages are

Bus no.	Voltage (complex)	Voltage in magnitude	
1	1.0000 + 0.0000i	1.0000	
2(Max. voltage bus)	0.9970 + 0.0003i	0.9970	
3	0.9829 + 0.0016i	0.9829	
4	0.9755 + 0.0028i	0.9755	
5	0.9681 + 0.0039i	0.9681	
6	0.9497 + 0.0022i	0.9497	
7	0.9462 - 0.0016i	0.9462	
8	0.9413 - 0.0010i 0.9413		
9	0.9351 - 0.0022i	0.9351	

10	0.9292 - 0.0032i	0.9292
11	0.9284 - 0.0031i	0.9284
12	0.9269 - 0.0029i	0.9269
13	0.9208 - 0.0043i	0.9208
14	0.9185 - 0.0056i	0.9185
15	0.9171 - 0.0062i	0.9171
16	0.9157 - 0.0065i	0.9157
17	0.9137 - 0.0077i	0.9137
18(minimum voltage bus)	0.9131 - 0.0079i	0.9131
19	0.9965 + 0.0001i	0.9965
20	0.9929 - 0.0011i	0.9929
21	0.9922 - 0.0014i	0.9922
22	0.9916 - 0.0018i	0.9916
23	0.9794 + 0.0011i	0.9794
24	0.9727 - 0.0004i	0.9727
25	0.9694 - 0.0011i	0.9694
26	0.9477 + 0.0029i	0.9477
27	0.9452 + 0.0038i	0.9452
28	0.9337 + 0.0051i	0.9337
29	0.9255 + 0.0063i	0.9255
30	0.9219 + 0.0080i	0.9220
31	0.9178 + 0.0066i	0.9178
32	0.9169 + 0.0062i	0.9169
33	0.9166 + 0.0061i	0.9166

Results for 52-bus system

- (1) End points are = 52 50 48 46 44 42 40 38 37 34 31 29 26 24 19 17 14 13 15 12 7 5 3
- (2) Final system voltages are

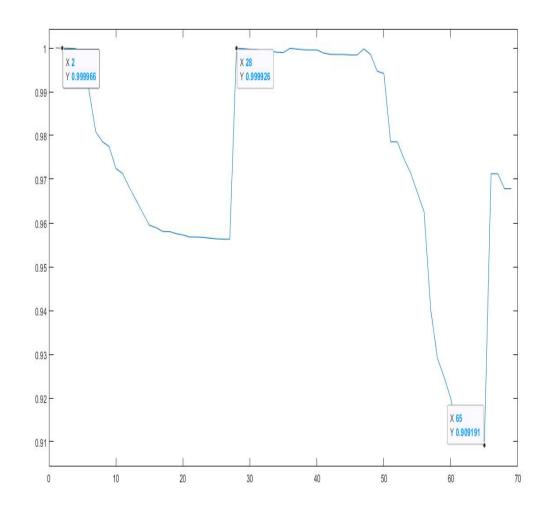
Bus no.	Voltage (complex)	Voltage in magnitude	
1	1.+ 0.0i	1.0000	
2	0.956 + 0.001693i	0.9560	
3	0.94864 + 0.00199i	0.9486	
4	0.93754 + 0.002338i	0.9375	
5	0.935741 + 0.002404i	0.9357	
6	0.927634 + 0.002711i	0.9276	
7	0.92642 + 0.00276i	0.9264	
8	0.905112 + 0.00351i	0.9051	
9	0.882758+ 0.0043454i	0.8828	
10	0.850264 + 0.005557i	0.8503	
11	0.847771 + 0.0056364i	0.8478	
12	0.84644 + 0.005685i	0.8465	
13	0.8442 + 0.005764i	0.8441	

15	14	0.841805 + 0.00583i	0.8418
17	15	0.8411 + 0.00588i	0.8411
18 0.8324068 + 0.00618i 0.8324 19 0.82835 + 0.0063251i 0.8284 20(Max. voltage bus) 0.987756 + 0.0005356i 0.9878 21 0.9790725 + 0.00088532i 0.9791 22 0.96474 + 0.00149i 0.9647 23 0.95295 + 0.001972i 0.9529 24 0.9499 + 0.002085i 0.9500 25 0.9600762 + 0.001717i 0.9601 26 0.9583 + 0.001798i 0.9583 27 0.9823 + 0.0007716i 0.9824 28 0.97876 + 0.000928i 0.9788 29 0.976942 + 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673	16	0.844220 + 0.0057711i	0.8442
19	17	0.839226 + 0.00599i	0.8392
20(Max. voltage bus) 0.987756 + 0.0005356i 0.9878 21 0.9790725 + 0.00088532i 0.9791 22 0.96474 + 0.00149i 0.9647 23 0.95295 + 0.001972i 0.9529 24 0.9499 + 0.002085i 0.9500 25 0.9600762 + 0.001717i 0.9601 26 0.9583 + 0.001798i 0.9583 27 0.9823 + 0.0007716i 0.9824 28 0.97876 + 0.000928i 0.9788 29 0.976942 + 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7949 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544	18	0.8324068 + 0.00618i	0.8324
21 0.9790725 + 0.00088532i 0.9791 22 0.96474 + 0.00149i 0.9647 23 0.95295 + 0.001972i 0.9529 24 0.9499 + 0.002085i 0.9500 25 0.9600762 + 0.001717i 0.9601 26 0.9583 + 0.001798i 0.9583 27 0.9823 + 0.0007716i 0.9824 28 0.97876 + 0.000928i 0.9788 29 0.976942+ 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.72056	19	0.82835 + 0.0063251i	0.8284
22 0.96474 + 0.00149i 0.9529 23 0.95295 + 0.001972i 0.9529 24 0.9499 + 0.002085i 0.9500 25 0.9600762 + 0.001717i 0.9601 26 0.9583 + 0.001798i 0.9583 27 0.9823 + 0.0007716i 0.9824 28 0.97876 + 0.000928i 0.9788 29 0.976942+ 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42	20(Max. voltage bus)	0.987756 + 0.0005356i	0.9878
23 0.95295 + 0.001972i 0.9529 24 0.9499 + 0.002085i 0.9500 25 0.9600762 + 0.001717i 0.9601 26 0.9583 + 0.001798i 0.9583 27 0.9823 + 0.0007716i 0.9824 28 0.97876 + 0.000928i 0.9788 29 0.976942 + 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43	21	0.9790725 + 0.00088532i	0.9791
24 0.9499 + 0.002085i 0.9500 25 0.9600762 + 0.001717i 0.9601 26 0.9583 + 0.001798i 0.9583 27 0.9823 + 0.0007716i 0.9824 28 0.97876 + 0.000928i 0.9788 29 0.976942+ 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9087 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.70567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.70149 44	22	0.96474 + 0.00149i	0.9647
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27 0.9823 + 0.0007716i 0.9824 28 0.97876 + 0.000928i 0.9788 29 0.976942 + 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667 + 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7544 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7014 46 0.7071 + 0.009327i 0.7072 47	25	0.9600762 + 0.001717i	0.9601
28 0.97876 + 0.000928i 0.9788 29 0.976942+ 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7014 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48	26	0.9583 + 0.001798i	0.9583
29 0.976942+ 0.0010054i 0.9769 30 0.9754581 + 0.0010769i 0.9755 31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7012 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	27	0.9823 + 0.0007716i	0.9824
30	28	0.97876 + 0.000928i	0.9788
31 0.970371 + 0.00129729i 0.9704 32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	29	0.976942+ 0.0010054i	0.9769
32 0.90874 + 0.00305481i 0.9087 33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	30	0.9754581 + 0.0010769i	0.9755
33 0.7970129 + 0.0067i 0.7970 34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667 + 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	31	0.970371 + 0.00129729i	0.9704
34 0.794866 + 0.006854i 0.7949 35 0.781674 + 0.0073428i 0.7817 36 0.7699667 + 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7014 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	32	0.90874 + 0.00305481i	0.9087
35 0.781674 + 0.0073428i 0.7817 36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	33	0.7970129 + 0.0067i	0.7970
36 0.7699667+ 0.007808i 0.7700 37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	34	0.794866 + 0.006854i	0.7949
37 0.767211 + 0.007919i 0.7673 38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	35	0.781674 + 0.0073428i	0.7817
38 0.7798 + 0.00741i 0.7799 39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	36	0.7699667+ 0.007808i	0.7700
39 0.75735 + 0.007919i 0.7574 40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	37	0.767211 + 0.007919i	0.7673
40 0.754382 + 0.00801i 0.7544 41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	38	0.7798 + 0.00741i	0.7799
41 0.724679 + 0.008854i 0.7247 42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	39	0.75735 + 0.007919i	0.7574
42 0.720567 + 0.008986i 0.7206 43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	40	0.754382 + 0.00801i	0.7544
43 0.71482 + 0.009144i 0.7149 44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	41	0.724679 + 0.008854i	0.7247
44 0.70584 + 0.009421i 0.7059 45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	42	0.720567 + 0.008986i	0.7206
45 0.7113 + 0.009211i 0.7114 46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	43	0.71482 + 0.009144i	0.7149
46 0.7071 + 0.009327i 0.7072 47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	44	0.70584 + 0.009421i	0.7059
47 0.6959 + 0.00965i 0.6960 48 0.6949 + 0.00967i 0.6951	45	0.7113 + 0.009211i	0.7114
48 0.6949 + 0.00967i 0.6951	46	0.7071 + 0.009327i	0.7072
	47	0.6959 + 0.00965i	0.6960
40 0.0001 + 0.0000; 0.0003	48	0.6949 + 0.00967i	0.6951
49 U.6891 + U.00981 U.6892	49	0.6891 + 0.0098i	0.6892
50(minimum voltage bus) 0.6842 + 0.00995i 0.6843	50(minimum voltage bus)	0.6842 + 0.00995i	0.6843
51 0.6857 + 0.00991i 0.6858	51	0.6857 + 0.00991i	0.6858
52 0.6851 + 0.00993i 0.6852	52	0.6851 + 0.00993i	0.6852

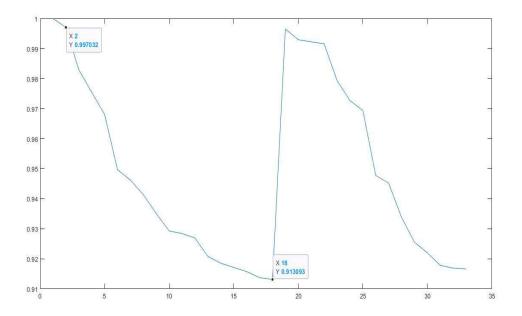
Final results for the all system

Bus-system	33-bus system	69-bus system	52-bus system
Min. voltage bus	18 th Bus	65 th Bus	50 th Bus
Min. voltage (p.u)	0.9131	0.9092	0.6842
Max. voltage bus	2 th Bus	2 th Bus	20 th Bus
Max. voltage(p.u)	0.9970	1	0.9877
Power loss(kw)	202.6650	224.9783	791.9124

Voltage plot for each bus for 69-bus system



Voltage plot for each bus for 33-bus system



Voltage plot for each bus for 52-bus system

