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# CHAPTER - 1 Vector Arithmetic

### EE24BTECH11061 - Rohith Sai

#### 1 1.10 Unit Vector

1.10.5 If  $\mathbf{a} = \mathbf{i} + \mathbf{j} + 2\mathbf{k}$  and  $\mathbf{b} = 2\mathbf{i} + \mathbf{j} - 2\mathbf{k}$ , find the unit vector in the direction of

- a) 6**a**
- b)  $2\mathbf{a} \mathbf{b}$

## **Solution:**

Variable	Description	Formula
a	First point	$\mathbf{a} = \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$
b	Second point	$\mathbf{b} = \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix}$

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a) According to the question:

$$6\mathbf{a} = 6 \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix},\tag{1}$$

$$\|6\mathbf{a}\| = 6\|\mathbf{a}\| = 6\sqrt{(\mathbf{a})^{\top}(\mathbf{a})},\tag{2}$$

$$\implies ||6\mathbf{a}|| = 6\sqrt{6} \tag{3}$$

We know that, to find the unit vector:

$$\implies \frac{6\mathbf{a}}{\|6\mathbf{a}\|} = \frac{1}{6\sqrt{6}} \begin{pmatrix} 6\\6\\12 \end{pmatrix} \tag{4}$$

Therefore, the required unit vector is:

$$\Rightarrow \frac{1}{\sqrt{6}} \begin{pmatrix} 1\\1\\2 \end{pmatrix} \tag{5}$$

b) According to the question:

$$2\mathbf{a} - \mathbf{b} = 2 \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix} - \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 6 \end{pmatrix}, \tag{6}$$

$$||2\mathbf{a} - \mathbf{b}|| = \sqrt{(2\mathbf{a} - \mathbf{b})^{\mathsf{T}} (2\mathbf{a} - \mathbf{b})},\tag{7}$$

$$\implies ||2\mathbf{a} - \mathbf{b}|| = \sqrt{37} \tag{8}$$

We know that, to find the unit vector:

$$\implies \frac{2\mathbf{a} - \mathbf{b}}{\|2\mathbf{a} - \mathbf{b}\|} = \frac{1}{\sqrt{37}} \begin{pmatrix} 0 \\ 1 \\ 6 \end{pmatrix} \tag{9}$$

Therefore, the required unit vector is:

$$\implies \frac{1}{\sqrt{37}} \begin{pmatrix} 0\\1\\6 \end{pmatrix} \tag{10}$$

