GATE

PH - 2012

EE24BTECH11061 - Rohith Sai

SINGLE CORRECT 1 MARK EACH

1) Identify the CORRECT statement for the following vectors $\mathbf{a} = 3i + 2j$ and $\mathbf{b} = i + 2j$

a) The vectors **a** and **b** are linearly independent

pendent c) The vectors **a** and **b** are orthogonal

b) The vectors **a** and **b** are linearly de-

d) The vectors **a** and **b** are normalized

2) Two uniform thin rods of equal length, L, and masses M_1 and M_2 are joined together along the length. The moment of inertia of the combined rod of length 2L about an axis passing through the mid-point and perpendicular to the length of the rod is,

a) $(M_1 + M_2) \frac{L^2}{12}$ b) $(M_1 + M_2) \frac{L^2}{6}$

c) $(M_1 + M_2) \frac{L^2}{3}$ d) $(M_1 + M_2) \frac{L^2}{2}$

3) The space-time dependence of the electric field of a linearly polarized light in free space is given by $xE_0\cos(\omega t - kz)$ where E_0 , ω and k are the amplitude, the angular frequency and the wavevector, respectively. The time averaged energy density associated with the electric field is

a) $\frac{1}{4}\epsilon_0 E_0^2$ b) $\frac{1}{2}\epsilon_0 E_0^2$

c) $\epsilon_0 E_0^2$ d) $2\epsilon_0 E_0^2$

4) If the peak output voltage of a full wave rectifier is 10 V, its d.c. voltage is

a) 10.0 V

c) 6.36 V

b) 7.07 V

d) 3.18 V

5) A particle of mass m is confined in a two dimensional square well potential of dimension a. This potential V(x, y) is given by

$$V(x, y) = 0$$
 for $-a < x < a$ and $-a < y < a$
= ∞ elsewhere

The energy of the first excited state for this particle is given by,

| a) $\frac{\pi^2 h^2}{mq^2}$ b) $\frac{2\pi^2 h^2}{ma^2}$ | c) $\frac{5\pi^2\hbar^2}{2ma^2}$ d) $\frac{4\pi^2\hbar^2}{ma^2}$ |
|---|--|
| 6) The isothermal compressibility, κ of an ideal gas at temperature T_0 and volume V_0 , is given by | |
| a) $-\frac{1}{V_0} \frac{\partial V}{\partial P} \Big _{T_0}$ b) $\frac{1}{V_0} \frac{\partial V}{\partial P} \Big _{T_0}$ | c) $-V_0 \frac{\partial P}{\partial V}\Big _{T_0}$ d) $V_0 \frac{\partial P}{\partial V}\Big _{T_0}$ |
| 7) The ground state of sodium atom $\binom{11}{Na}$ is a $^2S_{1/2}$ state. The difference in energy levels arising in the presence of a weak external magnetic field B , given in terms of Bohr magneton, μ_B , is | |
| a) μ_B b) $2\mu_B$ | c) $4\mu_B$ d) $6\mu_B$ |
| 8) For an ideal Fermi gas in three dimensions, the electron velocity v_F at the Fermi surface is related to electron concentration n as, | |
| a) $v_F \propto n^{2/3}$ b) $v_F \propto n$ | c) $v_F \propto n^{1/2}$ d) $v_F \propto n^{1/3}$ |
| 9) Which one of the following sets corresponds to fundamental particles? | |
| a) proton, electron and neutronb) proton, electron and photon | c) electron, photon and neutrinod) quark, electron and meson |
| 10) In case of a Geiger-Muller (GM) counter, which one of the following statements is CORRECT? | |
| of the order of 10^{10} | c) Energy of the particles detected can be distinguishedd) Operating voltage of the detector is few tens of Volts |
| 11) A plane electromagnetic wave traveling in free space is incident normally on a glass plate of refractive index $\frac{3}{2}$. If there is no absorption by the glass, its reflectivity is | |
| a) 4%b) 16% | c) 20% d) 50% |
| 12) A Ge semiconductor is doped with acceptor impurity concentration of 10 ¹⁵ atoms/cm ³ . For the given hole mobility of 1800 cm ² /V-s, the resistivity of this material is | |

- a) 0.288Ω cm
- b) 0.694Ω cm

- c) 3.472Ω cm
- d) 6.944Ω cm
- 13) A classical gas of molecules, each of mass m, is in thermal equilibrium at the absolute temperature, T. The velocity components of the molecules along the Cartesian axes are v_x , v_y and v_z . The mean value of $(v_x + v_y)^2$ is
 - a) $\frac{k_B T}{m}$ b) $\frac{3}{2} \frac{k_B T}{m}$

- c) $\frac{1}{2} \frac{k_B T}{m}$ d) $2 \frac{k_B T}{m}$