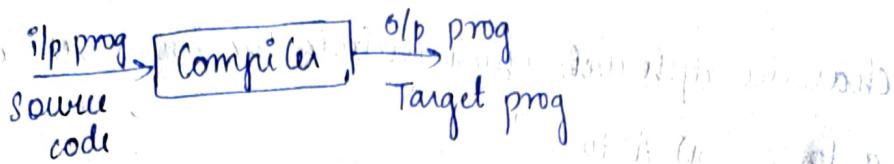
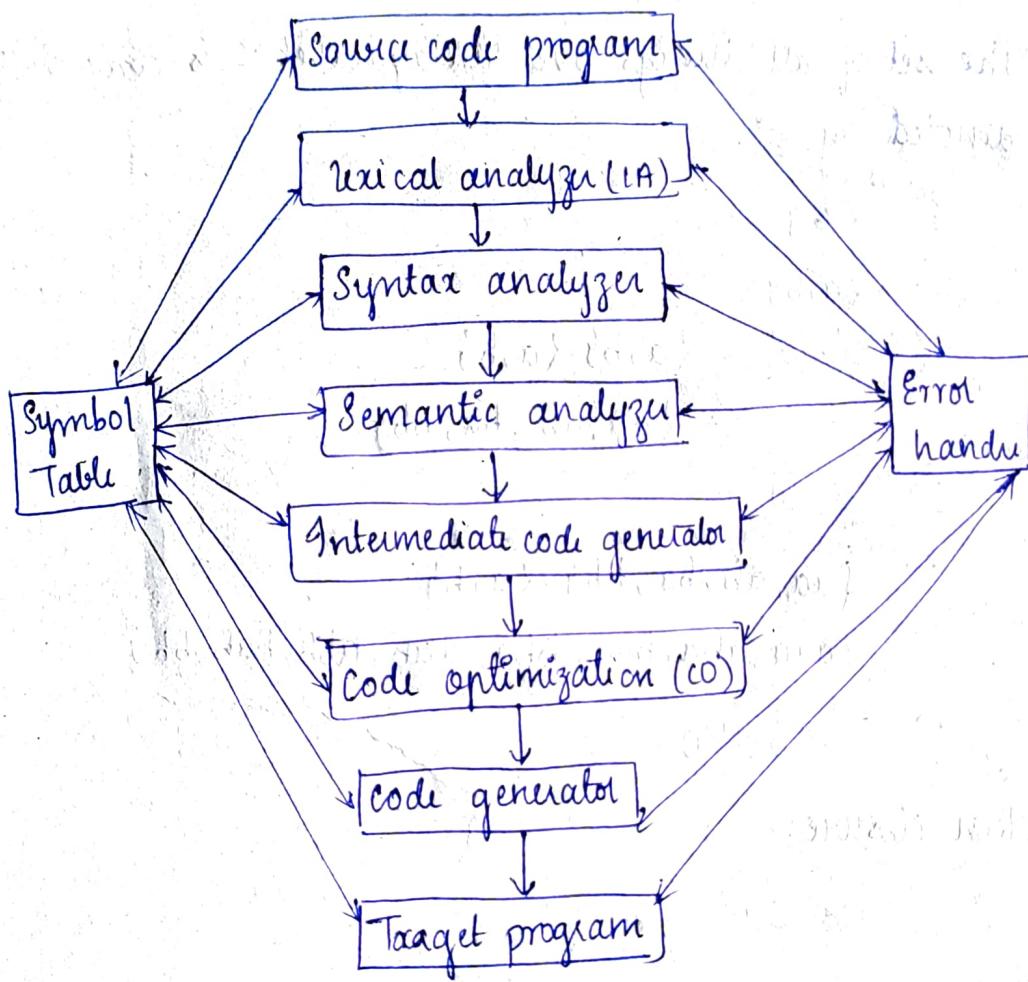


→ Compiler: a compiler is a program that helps in translating the compiler code from one programming language to another.



* Phases of a Compiler



Alphabet: An alphabet is a finite set of symbols expressed using Σ symbol

→ Alphabets can be binary alphabet which include 0, 1
(or)

character alphabet which include the lower case alphabet

a to z (or) A to Z

$$\Sigma = \{0, 1\}$$

$$\Sigma = \{a, b, \dots, z\}$$

→ The set of all strings over an alphabet Σ is conveniently denoted by Σ^* .

$$\Sigma^0 = \{\epsilon\}$$

$$\Sigma^1 = \{a, b\}$$

$$\Sigma^2 = \Sigma^1 \cdot \Sigma^1 = \{a, b\} \cdot \{a, b\}$$

$$= \{aa, ab, ba, bb\}$$

$$\Sigma^3 = \Sigma^2 \cdot \Sigma^1$$

$$= \{aa, ab, ba, bb\} \cdot \{a, b\}$$

$$\{aaa, aba, baa, bba, aab, abb, bab, bbb\}$$

$$\Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \dots$$

★ Kleen closure:

$$\Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \dots$$

★ Positive closure:

$$\Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \dots$$

The relationship between +ve closure & the kleen closure is

$$\boxed{\Sigma^* = \Sigma^+ \cup \{\epsilon\}}$$

$$0^* = \{ \epsilon, 0, 00, 000, 0000, \dots \}$$

$$1^* = \{ \epsilon, 1, 11, 111, 1111, \dots \}$$

$$0^+ = \{ 0, 00, 000, 0000 \dots \}$$

$$1^+ = \{ 1, 11, 111, 1111, \dots \}$$

$$0^* 1^* = \{ \epsilon, 1, 0, 01, 001, 011, \dots \}$$

$$0^* 1^+ = \{ 1, 01, 001, 011, \dots \}$$

$$0^* 1^- = \{ 1, 01, 001, 0001, \dots \}$$

$$0 1^* = \{ 0, 01, 011, 0111, \dots \}$$

Languages:

- A set of strings all of which are chosen from some Σ^* where Σ is a particular alphabet called as Language.
- if Σ is an alphabet & $L \subseteq \Sigma^*$ then L is a language over Σ
- ex: The language of all strings consisting of n 0's followed by n 1's for $n \geq 0$
- The set of strings of 0's & 1's with an equal no. of each
- $L = \{ 01, 10, 0011, 1100, 0101, 1010, \dots \}$
- The set of binary numbers whose value is a prime
- $L = \{ 10, 11, 101, 111, 1011, \dots \}$
- ∅ the empty language is a language over an alphabet
- {ε} the language consisting of empty string is also a lang
- $\emptyset \neq \{ \epsilon \}$
- construct a language for even no. of 0's & 1's

$$L = \{ 00, 11, 00001111, 01010101, 1010, 001, \dots \}$$

Operations :

1) Union of sets (\cup)

If A and B are the given sets then the resultant set can taking union of A & B may be represented as,

$$C = \{x | x \in A \text{ or } x \in B\}$$

2) Intersection (\cap)

$$C = \{x | x \in A \text{ and } x \in B\}$$

3) Disjoint sets

Two sets are said to be disjoint when \cap of the 2 given sets results in a null set.

Ex: $A = \{1, 2\}$ $B = \{3, 4\}$

$$A \cap B = \{\emptyset\}$$

4) Set difference:

$$A - B$$

It is a binary operation performed on 2 sets & result in a set of elements that are present in the 1st set & not present in the 2nd set.

5) Compliment of a set (S')

$$S' = U - S \quad [U = \text{universe}]$$

This can be defined as set difference of universe set & given set.

6) Symmetric difference (\oplus)

$$A \oplus B = (A - B) \cup (B - A)$$

7) Cartesian product (\times)

CP of 2 sets A & B is a set of all possible ordered pairs (a, b) where $a \in A, b \in B$

Strings

A string is finite sequence of symbols chosen from some alphabet.

Ex: 01101 is a string from the binary alphabet

$$\Sigma = \{0, 1\}$$

empty string: This is a string with 0 occurrences of symbols. This is represented by ' ϵ '.

length of a string: The no. of positions for symbols in the string.

Ex: 01101 length = 5

Concatenation of string: Let x & y be strings. Then xy

denotes the concatenation of x & y .

sub string: A string x is a substring of another string y if there are strings w & z either 1 or both of which may be null exist such that

$$y = wxz$$

If w is null then x is said to be prefix.

If z is null then x is said to be suffix.

25/8/23

Automata: automata deals with definitions & properties of mathematical models used in computation.

These models play a major role in areas of computer science.

- i) Finite automata (FA) used in compilers
ii) CFG (context free grammar) used in programming lang
Ex: automatic door in office

front pad rear pad

open close

front pad: the sensor detects the person who is about to enter

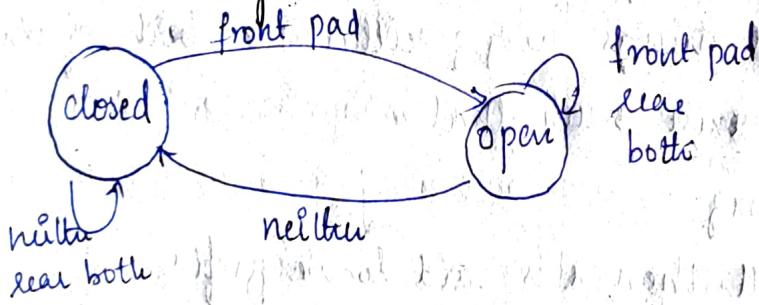
rear pad: the sensor detects the person behind the door

There are 2 states in automatic door - open & close.

four probabilities are:

- 1) front pad
- 2) rear pad
- 3) Both
- 4) neither

Transition diagram:



Transition Table:

Status \ possibility	front	rear	neither	Both
	closed	0	c	c
opened	0	0	c	0



a finite automata has 3 states

3 states q_1, q_2, q_3 are given in above transition diagram

initial state q_1 is indicated by arrow

accept or final state q_2 is represented with double circles

the arrows going from 1 state to another state are called transitions

I/p string 1101, check whether the o/p is accepted or rejected

- i) start with q_1
- ii) read '1', follow transition from $q_1 \rightarrow q_2$
- iii) read '1', follow transition from $q_2 \rightarrow q_2$
- iv) read '0', follow transition from $q_2 \rightarrow q_3$
- v) read '1', follow transition from $q_3 \rightarrow q_2$
- vi) accept

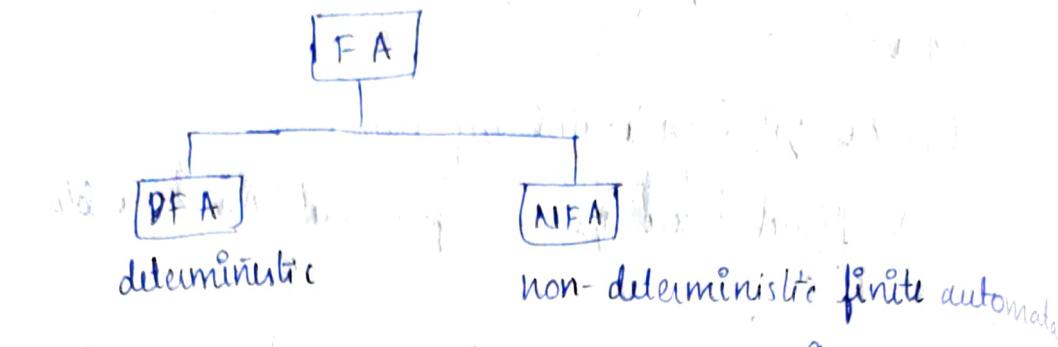
Ex: 1, 01, 11, 0101010101, 100, 0100, 110000, 01010000 →
are accepted strings

0, 10, 10100 → These are not accepted

Finite State Machine:

- This sys represents a mathematical model of a sys with certain i/p, the model finally gives some certain o/p
- The i/p when is given to the machine it is processed by various states
- These states are called intermediate states

Types of automata:



a. TA is a collection of 5 tuple $(Q, \Sigma, \delta, q_0, F)$

Q - finite set of state which is non empty

Σ - input alphabet

δ - transition

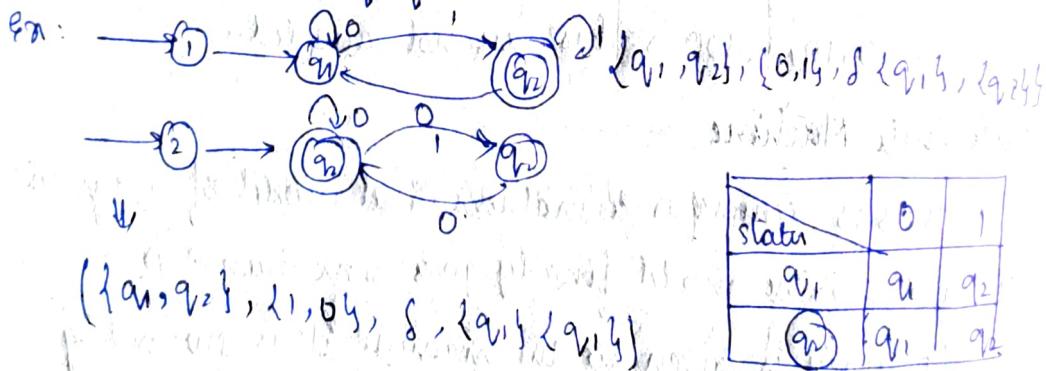
q_0 - initial state i.e. $q_0 \in Q$

F - set of final states $F \subseteq Q$

DFA:

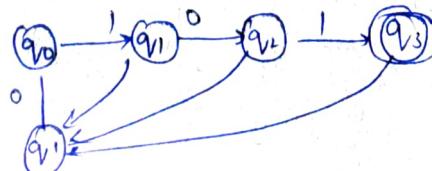
In DFA there is only one part of specific i/p from current state to next state.

The DFA can be represented by the same 5 tuple described in the definition of finite automata

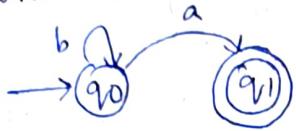


* define FA which accepts the i/p 101 over the i/p alphabet

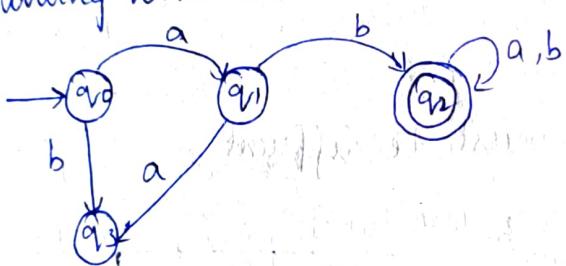
$$\Sigma = \{0, 1\}$$



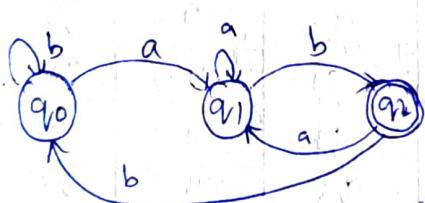
- * design DFA in which set of all string can be accessed which ends with 'a' where $\Sigma = a, b$



starting with ab



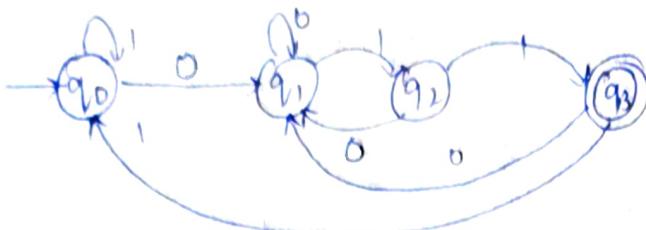
end with ab



self loop nearest state
it has to go one state
in DFA

s \ b	a	b
q0	q1	q0
q1	q1	q2
q2	q1	q0

- * Draw a DFA to access string of 0's & 1's ending with the string 011

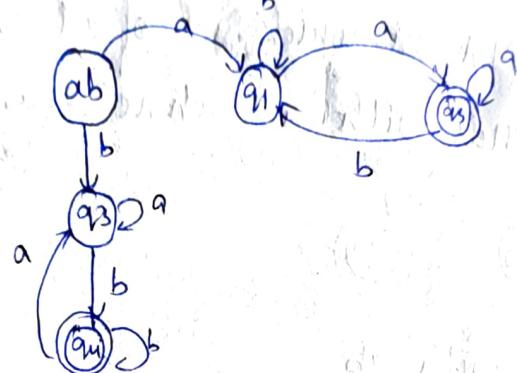


$\{(q_0, q_1, q_2, q_3), (0, 1), S, q_0, q_3\}$

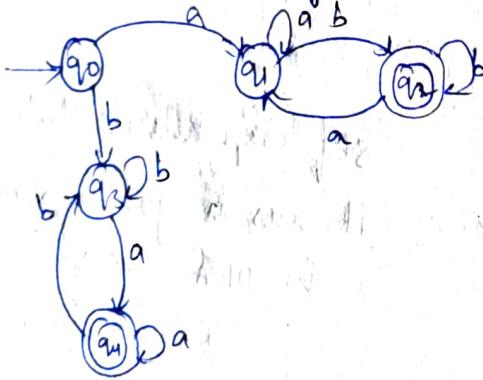
S	P	a	b
q0	q1	q3	
q1	q1	q2	
q2	q1	q3	
q3	q1	q0	

Q) start & end must be same S, a, b

S	P	a	b
q0	q1	q3	
q1	q2	q1	
q2	q2	q1	
q3	q3	q0	
q4	q3	q0	



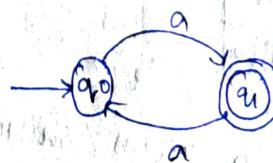
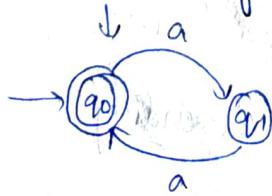
start and end symbol must be different



S	P	a	b
q0	q1	q3	
q1	q1	q2	
q2	q1	q2	
q3	q1	q3	
q4	q1	q3	

Q) all binary numbers are divisible by 2.

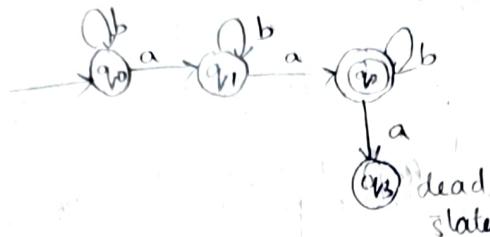
Q) even no. of a's



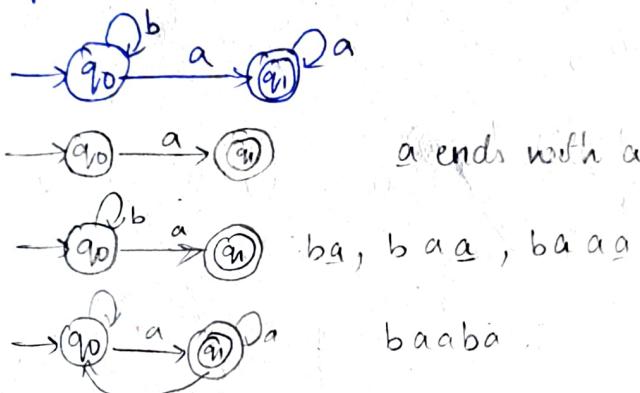
Q) Design a DFA such that number of 'a' is equal to 2 & there is no restriction over length of 'b'

DFA: 5-tuple = $\{a, b\}$

$\{\Delta, \Sigma, S, q_0, F\}$



Q) Design a DFA in which set of all strings can be accepted which ends with a, where $\Sigma = a, b$

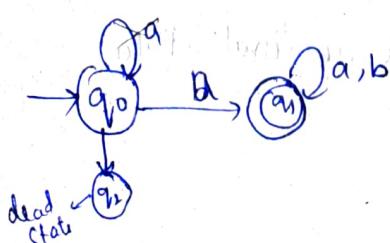


$\{q_0, q_1, \{a, b\}, S, q_0, q_2\}$

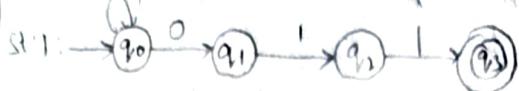
S can be represented as

IP state	a	b
q_0	q_1	q_0
q_1	q_1	q_0

* starts with a,



Q) Draw a DFA to accept set of strings {0,1} ending string 011.



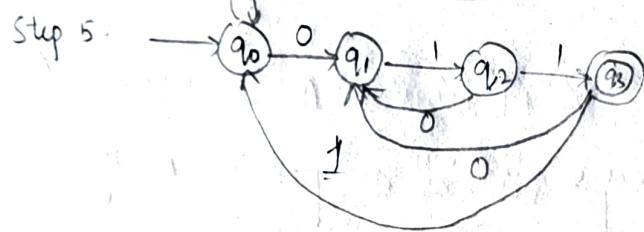
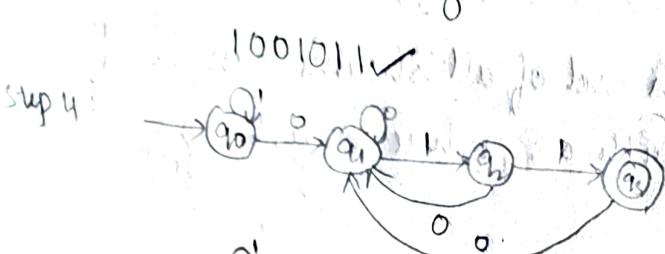
1011 ✓



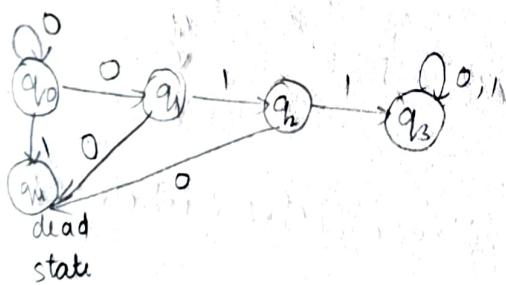
1000111 ✓



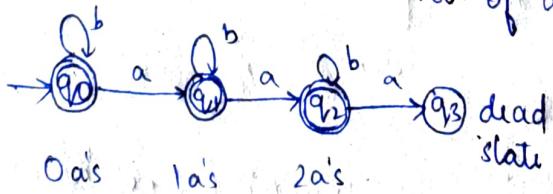
10010111 ✓



starts with 011

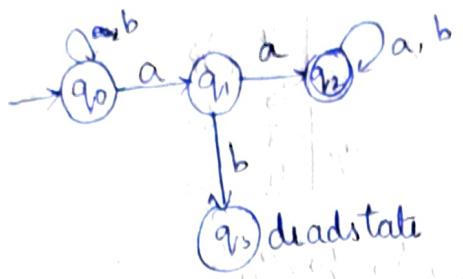


Q) design a DFA in which no. of a's in string are ≤ 2



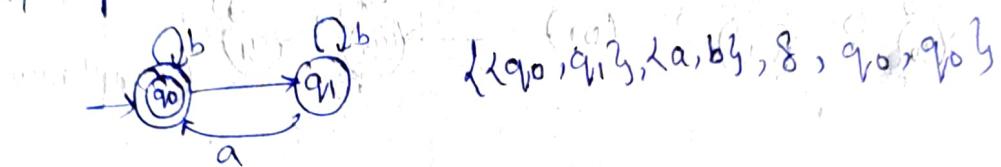
since it should accept 0, 1, 2 a's all are final states

Q) Design a DFA such that LHS is 'a' over $\Sigma = a, b$



31/8/23

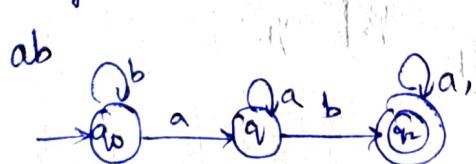
Q) Design DFA in which no. of a's are divided by 2 & alphabet is a, b



S can be represented as

states	a	b
final	q_1	q_0
q_1	q_0	q_1

Q) Design a DFA such that it has/contain the substring as ab



a	b	
q_0	q_1	q_0
q_1	q_1	q_2

$\{q_0, q_1, q_2\}, \{a, b\}, S, q_0, q_2\}$

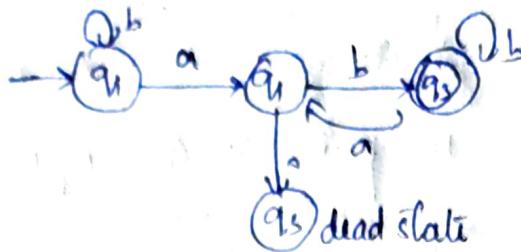
Q) Design a DFA such that a should never be followed by



a	b	
q_0	q_1	q_0
q_1	q_1	q_2

$\{q_0, q_1\}, \{a, b\}, S, q_0, q_1\}$

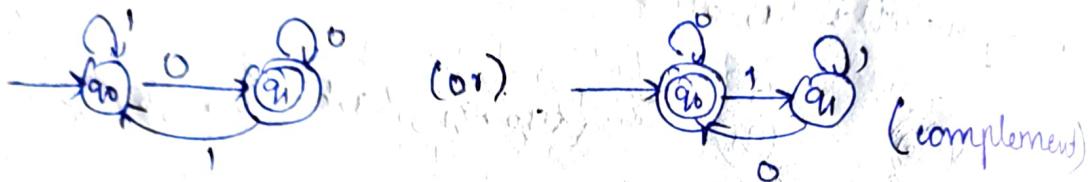
→ Every 'a' should be followed by 'b'



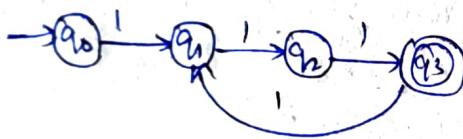
	a	b
q0	q1	q0
q1	q0	q2
q2	q1	q3

{ {q0, q1, q2}, {a, b}, 8, q0, q2 }

Q) Design DFA such that all binary no's are divided by 2.



Q) Design a FA (consider DFA) which checks whether the given binary no is divisible by 3.



	1
q0	q1
q1	q2
q2	q3
q3	q0

{ {q0, q1, q2, q3}, {1}, 8, q0, q3 }

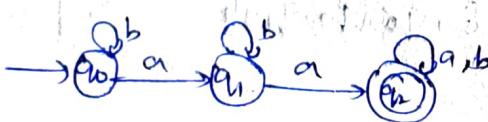
Q) that accepts the string with atleast 1 'a'



	a	b
q0	q1	q0
q1	q0	q1

{ {q0, q1}, {a, b}, 8, q0, q1 }

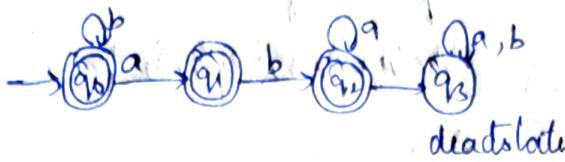
Q) Atleast 2 a's



$\{(q_0, q_1, q_2, q_3), \{a, b\}, \{0, 1\}, \{q_0, q_1, q_2, q_3\}\}$

a	b
q_0	q_1
q_1	q_2
q_2	q_3
q_3	q_2

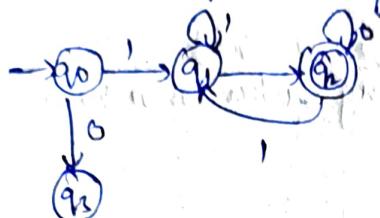
Q) such that 'a' should never be followed by 'b'



$\{(q_0, q_1, q_2, q_3), \{0, 1\}, \{0, 1\}, \{q_0, q_1, q_2, q_3\}\}$

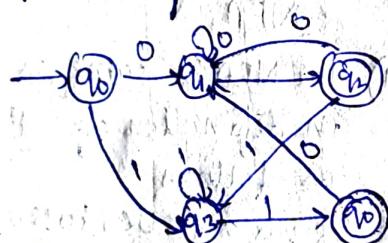
a	b
q_0	q_1
q_1	q_2
q_2	q_3

Q) which accepts strings & starts with 1 & ends with 0



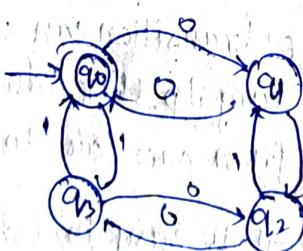
$\{(q_0, q_1, q_2, q_3), \{0, 1\}, \{1, 0\}, \{q_0, q_1, q_2, q_3\}\}$

Q) accept strings that ends with 01 or 10



$\{(q_0, q_1, q_2, q_3, q_4), \{0, 1\}, \{01, 10\}, \{q_0, q_1, q_2, q_3, q_4\}\}$

Q) Which accepts even no of 0's & 1's



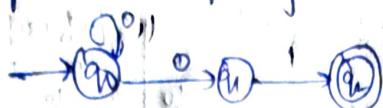
0	1
q_0	q_1
q_1	q_2
q_2	q_3
q_3	q_0

This DFA will consider 4 diff stages for 0/1 input

- 1) Even no of 0's & even no of 1's $\leftrightarrow q_0$ (Final state)
- 2) Even no of 0's & odd no of 1's $\leftrightarrow q_3$
- 3) Odd no of 0's & even no of 1's $\leftrightarrow q_1$
- 4) Odd no of 0's & odd no of 1's $\leftrightarrow q_2$

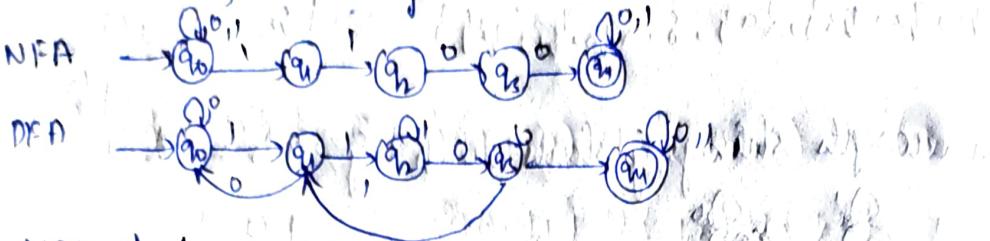
NFA : (Non deterministic finite automata) - An NFA is represented essentially like a DFA i.e. a 5 tuple representation $(Q, \Sigma, \delta, q_0, F)$. In NFA we can go to set of states over the current input symbol.

Ex: Design NFA accepting all strings ending with 0.

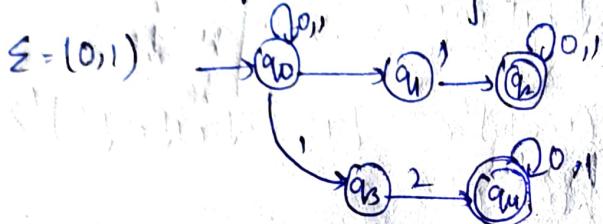


$\{q_0, q_1, q_2, q_3, q_4\}, \{0\}, \delta = \{(q_0, 0, q_1), (q_1, 0, q_2), (q_2, 0, q_3), (q_3, 0, q_4), (q_4, 0, q_0)\}$

$\rightarrow 11$ is followed by 00



NFA that accepts the string containing either 01 or 10 over



DFA

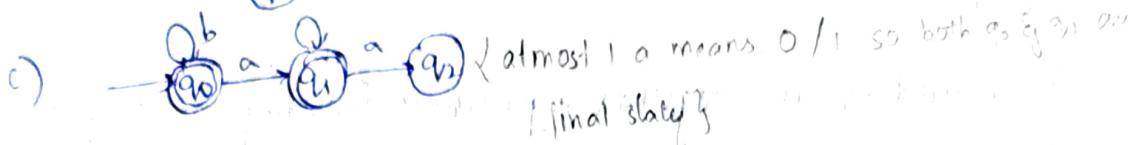
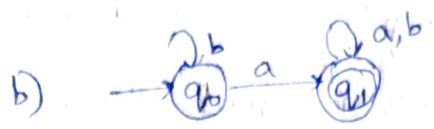
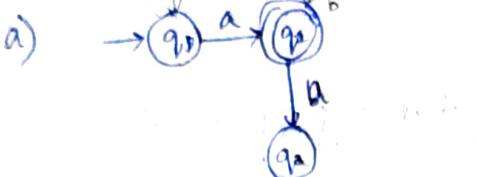
NFA

- 1) It is a 5 tuple representation i.e. $1) \text{The NFA is same as DFA}$
- $M = (Q, \Sigma, \delta, q_0, F)$ $2) \text{in definition of } S. \text{ Hence, as follows}$
- $\delta : Q \times (\Sigma \cup \{\epsilon\}) \rightarrow P(Q)$
- 2) There can be 0, 1 transition on input symbol $2) 0 \text{ or more transitions}$
- 3) No ϵ transition exists, i.e. there should not be any transition on input symbol $3) \epsilon \text{ transition can exist i.e. with any input these can be transition from one state to another}$
- 4) It is difficult to construct $4) \text{It is easy to construct}$
- 5) It takes more space but have speed of computation $5) \text{NFA's are more compact but takes more time}$
- 6) Can recognize a regular language.
- 6) NFA is

Construct DFA for the following things

- a) Exactly one 'a'
- b) atleast one 'a'
- c) almost one 'a'

$$\Sigma = \{a, b\}$$



→ Construct DFA that doesn't contain substring $abab$



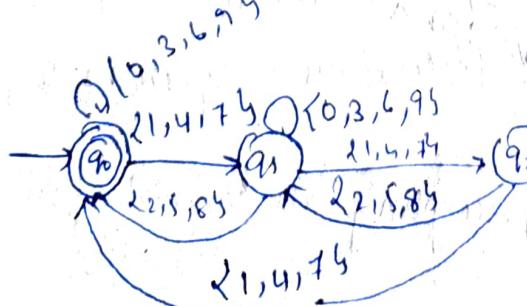
* Construct DFA for decimal nos divisible by 3

$$\Sigma = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$$

$$\text{rem } 0 \rightarrow \{0, 3, 6, 9\}$$

$$\text{rem } 1 \rightarrow \{1, 4, 7\}$$

$$\text{rem } 2 \rightarrow \{2, 5, 8\}$$



Regular Expressions:

- Let Σ be an alphabet which is used to denote input the regular exp of Σ can be defined as follows
- \emptyset is a regular exp which is the empty set.
- ϵ is a regular exp and denotes set ϵ (epsilon) and it denotes a null string.
- For each a in Σ R_a is regular exp & denotes the set a .
- If r and s are regular expressions denoting the languages L_1 and L_2 respectively then
 - $r+s$ is equivalent to $L_1 \cup L_2$ i.e union
 - rs is equivalent to $L_1 \cdot L_2$ i.e concatenation
 - r^* is equivalent to L_1^* i.e closure

Note: r^* is known as clean closure or closure which indicates occurrence of r for infinity no. of times.

Ex: $R \cdot E = a^* = \{\epsilon, a, aa, \dots\}$

+ve closure of L can be shown as L^+ . The L^+ denotes set of all the strings except the epsilon / null string.

The null string is denoted by ϵ or λ

$R \cdot E = a^+ = \{a, aa, \dots\}$

Ex: Write a RE for the lang accepting all combinations of a 's over the set $\Sigma = a$.

$RE = a^*$

Design a RE for the lang accepting all the combination of a 's over $\Sigma = a$.

Design RE for lang containing all the strings containing any no. of a's & b's

$$RE = (a+b)^*$$

Construct RE for lang containing all string having any no. of a's & b's except the null string

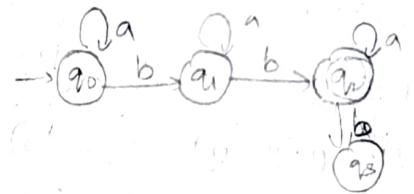
$$RE = (a+b)^+$$

(a) all the strings which are ending 00 over the set $\Sigma = \{0,1\}$

$$RE = (0+1)^* 00$$

ex: consisting of exactly 2 b's over the set $\Sigma = \{a,b\}$

$$RE = a^* b a^* b$$



ex: write RE which denotes a lang 'L' over the set $\Sigma = \{1\}$ having odd length of strings.

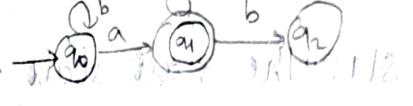
$$RE = 1(11)^*$$

ex: construct RE which denotes lang over the $\Sigma = \{0,1\}$ having even length of strings

$$RE = (00)^*$$

ex: write RE to denote lang 'L' over $\Sigma = \{a,b\}$ such that all the strings do not contain the sub string ab

$$RE = b^* a a^*$$



Identity Rules:

→ The two R.E P & q , are equivalent if & only if p represents the same set of strings as q does.

→ Let P, Q, R are R.E then the identity rules are as given below.

$$1. \epsilon R = R\epsilon = R$$

$$8) (R^*)^* = R^*$$

$$2. \epsilon^* = \epsilon$$

$$9) \epsilon + RR^* = R^*$$

$$3. \emptyset^* = \epsilon$$

$$10) (P+Q)R = PR + PQ + QR$$

$$4. \emptyset R = R\emptyset = \emptyset$$

$$11) (P+Q)^* = (P^*Q^*)^* = (P^* + Q^*)^*$$

$$5. \emptyset + R = R$$

$$12) R^*(\epsilon + R) = (\epsilon + R)R^* = R^*$$

$$6. R + R = R$$

$$13) R + (\epsilon)^* = R^*$$

$$7. RR^* = R^*R = R$$

$$14) \epsilon + R^* = R^*$$

$$15) (PQ)^*P = P(QP)^*$$

$$16) R^*R + R = R^*R$$

6/9/23

* NFA to DFA conversion:

Let $M = (Q, \Sigma, \delta, q_0, F)$ is a NFA which accepts the language $\mathcal{L}(M)$ there should be equivalent DFA denoted by $M' = (Q', \Sigma', \delta', q'_0, F')$ such that $\mathcal{L}(M) = \mathcal{L}(M')$

The conversion method will follow the following steps.

St 1: The start state of NFA will be start state for DFA
Hence add q_0 of NFA to Q' then find the transitions from this start state

St 2: For each state $[q_0, q_1, q_2, \dots]$ in Q' for each
(i) the transitions for each input symbol Σ can be obtained as

$$s'([q_1, q_2, \dots], a) = s(q_1, a) \cup s(q_2, a) \cup \dots$$

- Step b) Add the state $[q_1, q_2, \dots]$ to DFA if it is not already added in Q'
- c) Then find the transitions for every input symbol from Σ for state $[q_1, q_2, \dots]$
 If we get some state $[q_1, q_2, q_3, \dots]$ which is not in Q' of DFA, then add the state to Q' .
- d) If there is no new state generating then stop the process after finding all the transitions.

Step 3: For the state $[q_1, q_2, \dots]$ in Q' of DFA if any state is a final state of NFA then $[q_1, q_2, \dots]$ becomes a final state. Thus the set of all the final states belongs to F' of DFA.

Q) Convert the given NFA to DFA.

state	0	1
q_0	$\{q_0, q_1\}$	q_0
q_1	$\{q_2\}$	q_1
q_2	q_3	q_3
q_3	\emptyset	q_2

q_0 is the initial state in NFA so q_0 is initial state in DFA.

$$s'([q_0], 0) = s(q_0, 0) = \{q_0, q_1\}$$

$$s'([q_0], 1) = \{q_2\}$$

$$s^1(\{q_0, q_1\}, 0) = s(q_0, 0) \cup s(q_1, 0)$$

$$= \{q_0, q_1\} \cup \{q_2\}$$

$$= \{q_0, q_1, q_2\}$$

$$s^1(\{q_0, q_1\}, 1) = s(q_0, 1) \cup s(q_1, 1)$$

$$= \{q_0\} \cup \{q_1\}$$

$$= \{q_0, q_1\}$$

$$s^1(\{q_0, q_1, q_2\}, 0) = s^1(q_0, 0) \cup s^1(q_1, 0) \cup s^1(q_2, 0)$$

$$= \{q_0, q_1\} \cup \{q_2\} \cup \{q_3\}$$

$$= \{q_0, q_1, q_2, q_3\}$$

$$s^1(\{q_0, q_1, q_2\}, 1) = s^1(q_0, 1) \cup s^1(q_1, 1) \cup s^1(q_2, 1)$$

$$= \{q_0\} \cup \{q_1\} \cup \{q_3\}$$

$$= \{q_0, q_1, q_3\}$$

$$s^1(\{q_0, q_1, q_2, q_3\}, 0) = s^1(q_0, 0) \cup s^1(q_1, 0) \cup s^1(q_2, 0) \cup s^1(q_3, 0)$$

$$= \{q_0, q_1\} \cup \{q_2\} \cup \{q_3\} \cup \{q_4\}$$

$$= \{q_0, q_1, q_2, q_3, \emptyset\}$$

$$s^1(\{q_0, q_1, q_2, q_3\}, 1) = s^1(q_0, 1) \cup s^1(q_1, 1) \cup s^1(q_2, 1) \cup s^1(q_3, 1)$$

$$= \{q_0\} \cup \{q_1\} \cup \{q_3\} \cup \{q_4\}$$

$$= \{q_0, q_1, q_2, q_3\}$$

$$s^1(\{q_0, q_1, q_2, q_3\}, 0) = s^1(q_0, 0) \cup s^1(q_1, 0) \cup s^1(q_2, 0) \cup s^1(q_3, 0)$$

$$= \{q_0, q_1\} \cup \{q_2\} \cup \{q_3\}$$

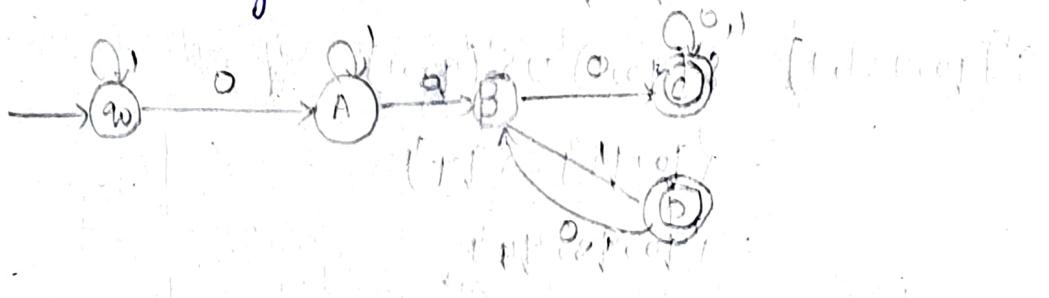
$$= \{q_0, q_1, q_2\}$$

$$\begin{aligned}
 s^1((q_0, q_1, q_3), 1) &= s^1(q_0, 1) \cup s^1(q_1, 1) \cup s^1(q_3, 1) \\
 &= \{q_0\} \cup \{q_1\} \cup \{q_3\} \\
 &\quad \{q_0, q_1, q_2\} \\
 &\quad \{q_0, q_1, q_3\} \\
 &\quad \{q_0, q_2, q_3\} \\
 &\quad \{q_1, q_2, q_3\} \\
 &\quad \{q_0, q_1, q_2, q_3\}
 \end{aligned}$$

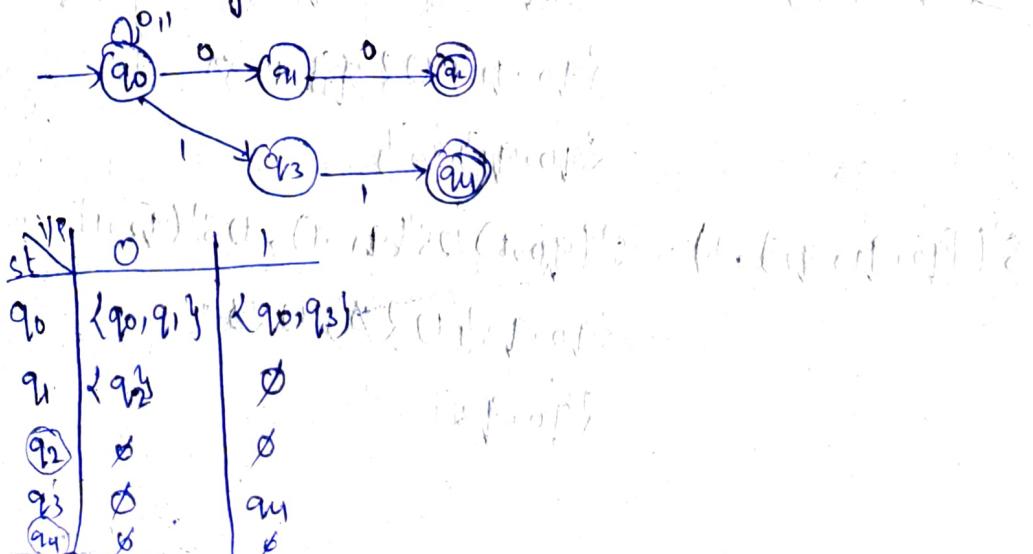
Transition table for DFA $S^1((q_0, q_1, q_3), 1)$

state	0	1
q_0	$\{q_0, q_1\}$ A	q_0
$\{q_0, q_1\}$	$\{q_0, q_1, q_2\}$ B	$\{q_0, q_1, q_3\}$
$\{q_0, q_1, q_2\}$	$\{q_0, q_1, q_2, q_3\}$ C	$\{q_0, q_1, q_3\}$
$\{q_0, q_1, q_2, q_3\}$	$\{q_0, q_1, q_2, q_3\}$ C	$\{q_0, q_1, q_2, q_3\}$ C
$\{q_0, q_1, q_3\}$	$\{q_0, q_1, q_2, q_3\}$ C	$\{q_0, q_1, q_2, q_3\}$ C

Transition diagram.



Q) Convert the given NFA to equivalent DFA



Initial state in DFA is q_0 , so initial state in DFA

$$\delta'(q_0, 0) = \{q_0, q_1\}$$

$$\delta'(q_0, 1) = \{q_0, q_3\}$$

$$\cdot \delta'([q_0, q_1], 0) = \delta'(q_0, 0) \cup \delta'(q_1, 0)$$
$$= \{q_0, q_1\} \cup \{q_2\}$$
$$= \{q_0, q_1, q_2\}$$

$$\delta'([q_0, q_1], 1) = \delta'(q_0, 1) \cup \delta'(q_1, 1)$$
$$= \{q_0, q_3\} \cup \emptyset$$
$$= \{q_0, q_3\}$$

$$\delta'([q_0, q_3], 0) = \delta'(q_0, 0) \cup \delta'(q_3, 0)$$
$$= \{q_0, q_1\} \cup \emptyset$$
$$= \{q_0, q_1\}$$

$$\cdot \delta'([q_0, q_3], 1) = \delta'(q_0, 1) \cup \delta'(q_3, 1)$$
$$= \{q_0, q_3\}, \{q_4\}$$
$$= \{q_0, q_3, q_4\}$$

$$\delta'([q_0, q_1, q_2], 0) = \delta'(q_0, 0) \cup \delta'(q_1, 0) \cup \delta'(q_2, 0)$$
$$= \{q_0, q_1\} \cup \{q_2\} \cup \emptyset$$
$$= \{q_0, q_1, q_2\}$$

$$\delta'([q_0, q_1, q_2], 1) = \delta'(q_0, 1) \cup \delta'(q_1, 1) \cup \delta'(q_2, 1)$$
$$= \{q_0, q_3\} \cup \{q_4\} \cup \emptyset$$
$$= \{q_0, q_3, q_4\}$$

$$\begin{aligned}
 s^1([q_0, q_3, q_4], 0) &= s^1(q_0, 0) \cup s^1(q_3, 0) \cup s^1(q_4, 0) \\
 &= \{q_0, q_1\} \cup \emptyset \cup \emptyset
 \end{aligned}$$

$\{q_0, q_1\}$

$$\begin{aligned}
 s^1([q_0, q_3, q_4], 1) &= s^1(q_0, 1) \cup s^1(q_3, 1) \cup s^1(q_4, 1) \\
 &= \{q_0, q_3\} \cup \{q_4\} \cup \emptyset
 \end{aligned}$$

$\{q_0, q_3, q_4\}$

Transition table for DFA

state	0	1
q_0	$\{q_0, q_1\}^A$	$\{q_0, q_3\}^B$
$\{q_0, q_1\}^A$	$\{q_0, q_1, q_2\}^C$	$\{q_0, q_3\}^B$
$\{q_0, q_3\}^B$	$\{q_0, q_1\}^A$	$\{q_0, q_3, q_4\}^D$
$\{q_0, q_1, q_2\}^C$	$\{q_0, q_1, q_2\}^C$	$\{q_0, q_3\}^B$
$\{q_0, q_3, q_4\}^D$	$\{q_0, q_1\}^A$	$\{q_0, q_3, q_4\}^D$

