

$$T \rightarrow T^A S^B / S$$

$$T \rightarrow ST'$$

$$T' \rightarrow , ST' / \epsilon$$

21. Compute the FIRST & FOLLOW.

$$S \rightarrow a/b/(CT)$$

$$T \rightarrow ST'$$

$$T' \rightarrow , ST' / \epsilon$$

$$\text{FIRST}(S) = \{a, b, (,)\}$$

$$\text{FIRST}(T) = \text{FIRST}(S) = \{a, b, (,)\}$$

$$\text{FIRST}(T') = \{, , \epsilon\}$$

$$\text{FOLLOW}(S) = \{ \$,), \epsilon \}$$

$$T \rightarrow ST'$$

$$\text{FOLLOW}(S) = \text{FIRST}(T') - \epsilon \cup \text{FOLLOW}(T)$$

$$\{, , \epsilon\} - \{\epsilon\} \cup \text{FOLLOW}(T)$$

$$\{, \} \cup \text{FOLLOW}(T) \Rightarrow \{, \}$$

$$T' \rightarrow , ST' / \epsilon$$

$$\text{FOLLOW}(S) = \text{FIRST}(T') - \epsilon \cup \text{FOLLOW}(T')$$

$$\{, \} \cup \text{FOLLOW}(T) \Rightarrow \{, \}$$

$$\text{FOLLOW}(T) = \{) \}$$

$$\text{FOLLOW}(T') = \{) \}$$

In $T \rightarrow ST'$ after T' there is nothing so $\text{FOLLOW}(T')$

$$\text{FOLLOW}(T)$$

$$T \rightarrow ST'$$

$$\text{FOLLOW}(T) = \text{FIRST}(\epsilon) - \{\epsilon\} \cup \text{FOLLOW}(T)$$

$$\{\epsilon\} - \{\epsilon\} \cup \{) \}$$

$$\{) \}$$

	FIRST(α)	PPT
$S \rightarrow a$	a	$M[S, a]$
$S \rightarrow b$	$FIRST(b) = b$	$M[S, b]$
$S \rightarrow (T)$	$FIRST((T)) = ($	$M[S, (]$
$T \rightarrow ST'$	$FIRST(ST') = \{a, b, (\}$	$M[T, a], M[T, b], M[T, (]$
$T' \rightarrow , ST'$	$FIRST(,ST') = \{ , \}$	$M[T', ;]$
$T' \rightarrow \epsilon$	$FOLLOW(T') = \{ \}$	$M[T', \epsilon]$

terminals	a	b	$($	$)$	$,$
S	$S \rightarrow a$	$S \rightarrow b$	$S \rightarrow (T)$		
T	$T \rightarrow ST'$	$T \rightarrow ST'$	$T \rightarrow ST'$		
T'				$T' \rightarrow \epsilon$	$T' \rightarrow ,ST'$

Stack	input	o/p
$\$ S$	$(b) \$$	$S \rightarrow (T)$
$\$ S) T X$	$(b) \$$	$T \rightarrow ST'$
$\$ S) T' s$	$b) \$$	$S \rightarrow b$
$\$ S) T' X$	$) \$$	$T' \rightarrow \epsilon$
$\$ S X$	$X \$$	
$\$$	$\$$	successful

checking whether it is or not

$$S \rightarrow a/b/(T)$$

$$T \rightarrow T/S/S$$

$$S \rightarrow (T) \quad T \rightarrow S$$

$$S \rightarrow (S) \quad S \rightarrow b$$

$$S \rightarrow (b)$$

2) Construct LL(1) Grammar

Predictive parser i.e. recursive descent parser needs no backtracking, can be constructed for a class of Grammar called LL(1). The first L indicates the scanning the input from left to right & 2nd L for producing a left most derivation & one for using one input symbol of look ahead at each step to make parsing action decision.

unique entries it of LL(1)
multiple entries it is not LL(1)

Bottom Up Parsing: (LR(1))

Constructing a parse tree from leaf node to the root node is called bottom up parsing.

$$\text{ex: } E \rightarrow E + T / T$$

$$T \rightarrow T * F / F$$

$$F \rightarrow (E) / \text{id}$$

$$\text{"id + id"}$$

$$\begin{array}{c} 4) \quad T * F \\ \quad \mid \quad \mid \\ \quad F \quad \text{id} \\ \quad \mid \\ \quad \text{id} \end{array}$$

$$1) \text{id} * \text{id}$$

$$2) F * \text{id}$$

$$\mid$$

$$\text{id}$$

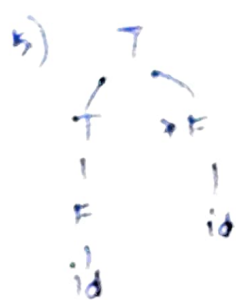
$$3) T * \text{id}$$

$$\mid$$

$$F$$

$$\mid$$

$$\text{id}$$



xx Handle Pruning (2m)

Bottom up parsing during a left to right scan of the constructs a Right most derivation (RMD) in reverse

A handle is a substring that matches the body of a production & whose reduction represents one step of the reverse of RMD

For the above Ques

Right sentential form

Handle

Reduced production

id * id

id

$F \rightarrow id$

F * id

F

$T \rightarrow F$

T * id

id

$F \rightarrow id$

T * F

T * F

$T \rightarrow T * F$

T

T

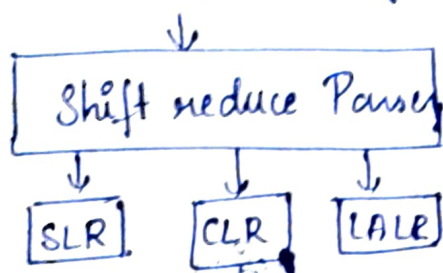
$E \rightarrow T$

[E]

Start symbol of the grammar

Bottom up parsing techniques

Bottom up parsing



SLR → Simple LR Parsers

CLR → Canonical LR Parsers

LALR → Look ahead LR Parser

Shift Reduce Parser

The following actions are performed in shift reduce parser.

- i) Shift:
The next input symbol is shifted into the top of the stack.
- ii) reduce:
The parser replaces the handle within a stack with a non terminal.
- iii) Accept:
The parser announces the successful completion of parsing.
- iv) Error:
The parser discovers an error & calls an error recovery routine.

Q) Construct shift Reduce Parser for the following grammar

$$E \rightarrow E + T / T$$

$$T \rightarrow T * F / F$$

$$F \rightarrow (e) / id$$

ip: id * id

stack	l/p	Action
\$id	id + id \$	shift
\$ id	* id \$	$F \rightarrow id$ (reduce)
\$ F	* id \$	$T \rightarrow F$ (reduce)
\$ T	* id \$	shift
\$ T + id	id \$	shift
\$ T * F	\$	$F \rightarrow id$ (reduce)
\$ T * F	\$	$T \rightarrow T * F$ (reduce)
\$ T	\$	$T \rightarrow E$ (reduce)
\$ E	\$	Accept

Q) Construct shift Reduce Parser for the following

$$M \rightarrow R + R / R + C / R$$

$$R \rightarrow C$$

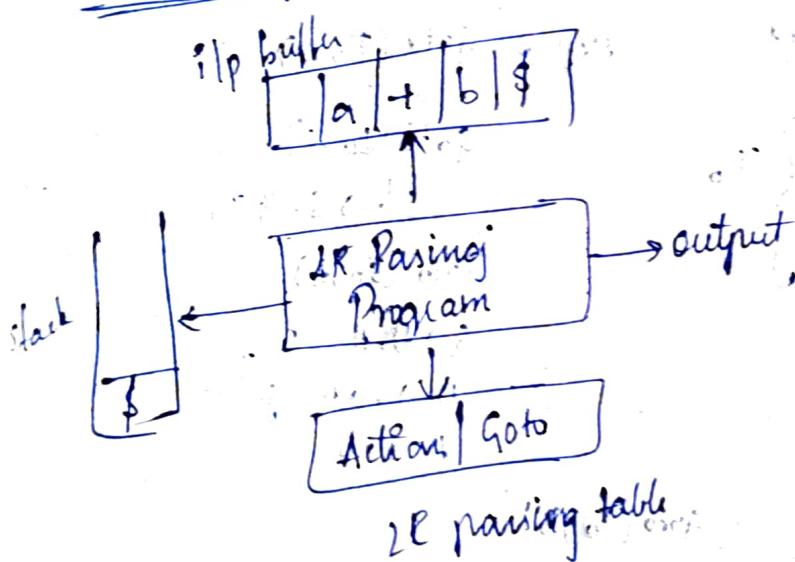
string "C + C"

stack	id	Action
\$	c+c\$	shift
\$c	+c\$	R→c (reduce)
\$R	+c\$	shift
\$R+	c\$	shift
\$R+c	\$	M→R+c
\$M	\$	Accept

Conflicts during shift Reduce Parser (2m)

- 1) shift reduce conflict
- 2) Reduce-Reduce conflict

LR Parsing:



SLR (Simple LR Parser)

Algorithm for SLR Parser

St1: Augmented grammar (G')

If G is a grammar with start symbol S then the augmented grammar (G') with a new start symbol S'
 i.e. $S' \rightarrow SS$

Step 2: LR(0) items

An LR(0) item of a grammar G with a dot at position on the right hand side

$$\text{ex. } A \rightarrow XYZ$$

$$A \rightarrow \cdot XYZ \quad (0) \quad A \rightarrow X \cdot YZ \quad (1) \quad A \rightarrow XY \cdot Z \quad (2)$$

Step 3: closure set of items (I)

$$A \rightarrow a \cdot Bb \quad 2) \text{ GOTO}(I_0, a)$$

$$B \rightarrow \cdot c$$

Step 4: SLR parsing table

Q) Construct SLR parsing table for given grammar

$$S \rightarrow AA$$

$$A \rightarrow aA$$

$$A \rightarrow b$$

Step 1: Augmented Grammar G'

$$S' \rightarrow S$$

Step 2: LR(0) items

$$S' \rightarrow \cdot S$$

$$S \rightarrow \cdot AA$$

$$A \rightarrow \cdot aA$$

$$A \rightarrow \cdot b$$

$\left. \begin{matrix} S' \rightarrow \cdot S \\ S \rightarrow \cdot AA \\ A \rightarrow \cdot aA \\ A \rightarrow \cdot b \end{matrix} \right\} I_0$

Step 3: Goto (I_0, a)

$$\text{Goto}(I_0, a)$$

$$S' \rightarrow S \cdot \quad I_1$$

$$\text{Goto}(I_0, b)$$

$$S \rightarrow A \cdot A \quad I_2$$

$$A \rightarrow \cdot aA \quad I_3$$

$$A \rightarrow \cdot b \quad I_4$$

goto (I_0, a)

$$A \rightarrow a \cdot A$$

$$A \rightarrow \cdot aA$$

$$A \rightarrow \cdot b$$

$\left. \begin{matrix} A \rightarrow a \cdot A \\ A \rightarrow \cdot aA \\ A \rightarrow \cdot b \end{matrix} \right\} I_5$

goto (I_0, b)

$$A \rightarrow b \cdot \quad I_6$$

goto (I_2, A)

$$S \rightarrow AA \cdot \quad I_7$$

goto (I_2, A)

$$A \rightarrow a \cdot A$$

$$A \rightarrow \cdot aA$$

$$A \rightarrow \cdot b$$

$\left. \begin{matrix} A \rightarrow a \cdot A \\ A \rightarrow \cdot aA \\ A \rightarrow \cdot b \end{matrix} \right\} I_8$

goto(I₂, b)

A → b. 3 I₁

goto(I₃, a)

A → aA. 3 I₆

goto(I₃, a)

A → a.A

A → .aA

A → .b

} I₃

goto(I₃, b)

A → b. 3 I₁

st 4: SLR parsing table

States	Goto				
	a	b	\$	S	A
I ₀	S ₃	S ₄	Error	1	2
I ₁	Error	Error	Accept	Error	Error
I ₂	S ₃	S ₄	Error	Error	S ₅
I ₃	S ₃	S ₄	Error	Error	C
I ₄	r ₃	r ₃	r ₃	Error	Error
I ₅	Error	Error	r ₁	Error	Error
I ₆	r ₂	r ₂	r ₂	Error	Error

To perform reduce operation, the given prodn sh be in

Reduce A. A → ab

Given Question

S' → S. 3 I₁

A → b. 3 I₄

S → AA. 3 I₅

A → aA. 3 I₆

① S → AA

② A → aA

③ A → b

In order to perform reduce operation for LR
Follow for the given grammar

$$\text{FIRST}(S) = \text{FIRST}(A) = \{a, b\}$$

$$\text{FIRST}(A) = \{a, b\}$$

$$\text{FOLLOW}(S) = \{\$ \}$$

$$\text{FOLLOW}(A) = \{\$, a, b\}$$

$$S \rightarrow AA$$

$$S \rightarrow A \odot A$$

$$\text{FOLLOW}(A) = a$$

$$S \rightarrow AA$$

$$\uparrow$$

$$\dots S \rightarrow Ab \dots$$

$$\text{FOLLOW}(A) = b$$

$$3) A \rightarrow b \cdot \} I_4$$

$$\text{FOLLOW}(A) = \{\$, a, b\}$$

$$\uparrow \text{ on } \$ = r_3$$

$$\uparrow \text{ on } a = r_3$$

$$\uparrow \text{ on } b = r_3$$

$$1) S \rightarrow AA \cdot \} I_5 \quad \text{FOLLOW}(S) = \{\$ \}$$

$$\uparrow \text{ on } \$ = r_1$$

$$2) A \rightarrow aA \cdot \} I_6 \quad \text{FOLLOW}(A) = \{\$, a, b\}$$

$$\uparrow \text{ on } \$ = r_2$$

$$\uparrow \text{ on } a = r_2$$

$$\uparrow \text{ on } b = r_2$$

Step 5: derive the string abba

stack	Y	
O_1	abba	S_3 (0 on a)
$Oa3$	bb	S_4 (3 on b)
$Oa3bA$	b	r_5 ($A \rightarrow b$) pop the ele in rlt & 2nd
$Oa3bA$	b	r_2 ($A \rightarrow aA$) 2+1=4 4th elem pop
$Oa3bA$	a	S_4 (2 on b)
$Oa2b4$	a	r_3 ($A \rightarrow b$) 2+1=3
$Oa2AS$		r_1 ($S \rightarrow AA$) 2+2=4
OSI		Accept

Construct SLR, CLR, LAR for the following.

$$S \rightarrow CC, C \rightarrow cC, C \rightarrow d$$

Step 1: Augmented Grammar

$$\left. \begin{array}{l} S' \rightarrow \cdot S \\ S \rightarrow \cdot CC \\ C \rightarrow \cdot cC \\ C \rightarrow \cdot d \end{array} \right\} I_0$$

goto(I_0, S)

$$S' \rightarrow S \cdot \quad \{ I_1 \}$$

goto(I_0, C)

goto(I_0, c)

$$\left. \begin{array}{l} S \rightarrow C \cdot C \\ C \rightarrow \cdot cC \\ C \rightarrow \cdot d \end{array} \right\} I_2 \quad \left. \begin{array}{l} C \rightarrow c \cdot C \\ C \rightarrow \cdot cC \\ C \rightarrow \cdot d \end{array} \right\} I_3$$

goto(I_0, d)

goto(I_2, d)

$$C \rightarrow d \cdot \quad \{ I_4 \} \quad C \rightarrow d \cdot \quad \{ I_4 \}$$

goto(I_2, c)

goto(I_3, c)

$$S \rightarrow (C \cdot \quad \{ I_5 \} \quad C \rightarrow cC \cdot \quad \{ I_6 \}$$

goto(I_2, c)

goto(I_3, c)

$$\left. \begin{array}{l} C \rightarrow c \cdot C \\ C \rightarrow \cdot cC \\ C \rightarrow \cdot d \end{array} \right\} I_2 \quad \left. \begin{array}{l} C \rightarrow c \cdot C \\ C \rightarrow \cdot cC \\ C \rightarrow \cdot d \end{array} \right\} I_3$$

goto(I_3, d)

$$C \rightarrow d \cdot \quad \{ I_4 \}$$

SLR parsing table

State	Action			Goto
	c	d	\$	
I_0	S_3	S_4	error	1
I_1	error	error	Accept	error
I_2	S_3	S_4	error	error
I_3	S_3	S_4	error	error
I_4	r_3	r_3	r_3	error
I_5	error	error	r_1	error
I_6	r_2	r_2	r_2	error

To perform reduce operation the production chain

$A \rightarrow d$.

③ $C \rightarrow d$. I_4

① $S \rightarrow CC$.

① $S \rightarrow CC$. I_5

① $C \rightarrow cC$

② $C \rightarrow cC$. I_6

③ $C \rightarrow d$

In order to perform reduce operation FIRST of follow

for given grammar

$FOLLOW(S) = \{\$ \}$

$FOLLOW(C) = \{c, d, \$ \}$

states	input	Remarks
0	cdd\$	S ₃
0C3	dd\$	S ₄
0C3d4	d\$	r ₃ c→d
0C3d4	dd	r ₂ C→cC
0C2	d\$	S ₄
0C2d4	d	r ₃ c→d
0C2d4	d	r ₁ S→cc
0S1	d	Accept

* CLR (Canonical LR Pairs)

$S \rightarrow cC$

$C \rightarrow cC$

$C \rightarrow d$

$S' \rightarrow \cdot S, \$$

$S \rightarrow \cdot cC$

$C \rightarrow \cdot cC$

$C \rightarrow \cdot d$

$A \rightarrow \cdot B\beta, a$

$S \rightarrow \cdot S, \$$

$S \rightarrow \cdot cC, \$$

$C \rightarrow \cdot cC, c/d$

$C \rightarrow \cdot d, c/d$

On CLR given grammar should be in form of

$A \rightarrow \alpha \cdot B\beta, a$

$B \rightarrow \cdot \gamma, \text{first}(\beta a)$

goto (I₀, S)

S' → S., \$ } I₀

goto (I₀, c)

S → ^Ac. ^Bc, ^a\$

c → .c c, \$ } I₁

c → .d, \$

goto (I₀, c)

^Ac → ^Ac. ^Bc, ^ac/d

c → .c c, c/d } I₂

c → .d, c/d

goto (I₀, d)

c → d., c/d } I₄

goto (I₂, c)

S → cc., \$ } I₅

goto (I₂, c)

c → ~~cc.~~ ^Bc, ^a\$

c → .c c, \$ } I₆

c → .d, \$

goto (I₂, d)

c → d., \$ } I₄

goto (I₃, c)

c → ^Ac. ^Bc, ^ac/d } I₃

goto (I₃, c)

^Ac → ^Ac. ^Bc, ^ac/d

c → .c c, c/d } I₃

c → .d, c/d

goto (I₃, d)

c → d., c/d } I₄

goto (I₆, c)

c → cc., \$ } I₄

goto (I₆, c)

^Ac → ^Ac. ^Bc, ^a\$

c → .c c, \$ } I₆

c → .d, \$

goto (I₆, d)

c → d., \$ } I₄

	c	d	\$	S	C
I_0	S_3	S_4		1	2
I_1			Accept		
I_2	S_6	S_7			5
I_3	S_3	S_4			8
I_4	r_3	r_3			
I_5			r_1		
I_6	S_6	S_7			9
I_7			r_3		
I_8	r_2	r_2			
I_9		r_2	r_2		

③ $c \rightarrow d, c/d \} I_4$

① $S \rightarrow cC, \beta \} I_5$

② $C \rightarrow d, \$ \} I_7$

② $C \rightarrow cC, c/d \} I_8$

② $C \rightarrow cC, \text{for } \} I_9$

Input string dd

State	I/P buffer	Remarks
0	dd\$	S4
0d\$	d\$	r3c → d
002	d\$	S7
002d\$	\$	r3c → d
00205	\$	r1 S → c
001	\$	Accept

LALR (Look ahead LR Parser)

if look ahead are diff ^{& production are same} we can combine

	c	d	\$	S	c
0	S36	S17		1	2
1			accept		
2	S36	S47			5
36	S36	S17			89
47	r3c	r36	r36		
5			r1		
89	r2	r2	r2		

Check whether the given string is accepted or not
dd\$

state	Vp Buffer	Remark
0	dd\$	S47
0/47	d\$	r3 C→d
0C2	d\$	S47
0C2/47	\$	r3 C→d
0C2/47	\$	r1 S→cc
0S1	\$	accepted