

28/08/2023

Compiler: Compiler is a translator that converts high level language into target language (machine level / low level).
» It converts the source code into target code, all at once and creates an object file.

Assembler: Assembler is a translator that converts high level language into machine level language.

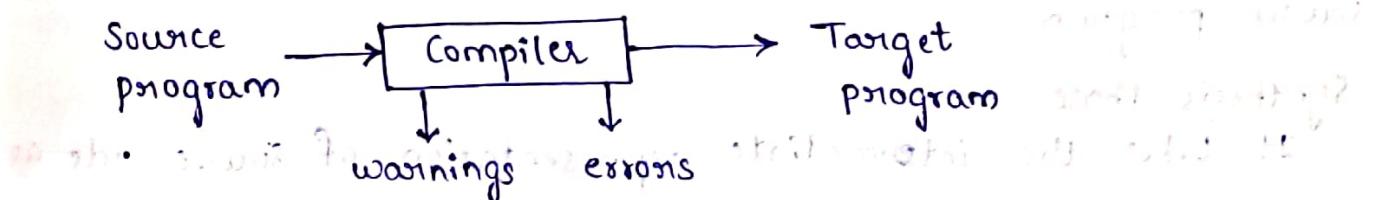
Interpreter: Interpreter is a translator that performs line by line execution.

» It is slower when compared to compiler.
→ Compilation can be done in one or many passes.

One pass :- HLL \rightarrow MLL
more passes :- HLL \rightarrow LLL, LLL \rightarrow MLL

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Compiler: It is a software or a program that converts a program written in high-level language (source code) to a low-level language (object or target code).
» It also reports errors present in the source program.



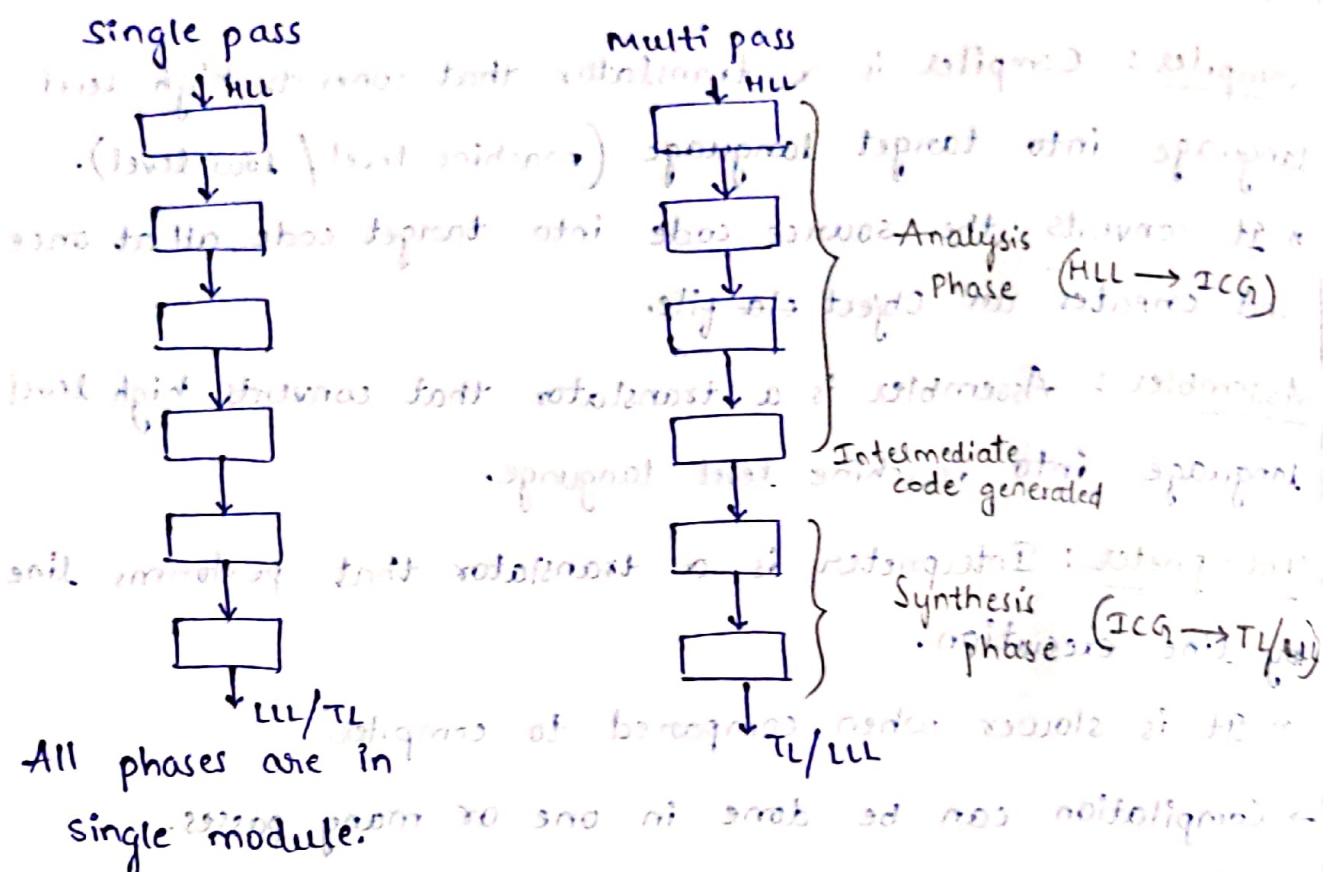
Types of compilers

1) Single pass compiler:

It is a type of compiler that processes the source code only once. (All 6 phases are performed at once).

2) Multi pass compiler:

It is a type of compiler that processes the source code multiple times i.e., to convert source code into target/object code.



There are two parts of compilation process

(phases)

Two phases

→ Analysis phase

→ Synthesis phase

(thus process) sequential level-split or multi-level merging

Analysis Phase

It breaks up the source code or program into smaller parts and creates an intermediate representation of the source program.

Synthesis Phase

It takes the intermediate representation of source code as input and creates the target code that is desired.

Properties of the compiler

When a compiler is built, it should possess the following properties.

- » The compiler itself must be bug-free.
- » It must generate correct machine code.

- » The generated machine code must run fast.
- » Compilation time must be proportional to program size.
- » The compiler must be portable.
- » It must give good diagnostics and error messages.
- » The generated code must work well with existing debuggers.
- » It must have consistent optimization.

Interpreter: An interpreter is a kind of translator which produces the result directly when the source program and data is given to it as input. It does not produce the object code; rather each time the program needs execution



* Differences between Compiler and Interpreter

Compiler

» It translates entire program as input.

» Intermediate object code is generated.

» Memory requirement is more (since object code is generated).

» Program need not be compiled every time.

» Errors are displayed after the entire program is checked.

» C, Java, C++ are compiled languages.

Interpreter

» It takes single instruction as input.

» No intermediate object code is generated.

» Memory requirement is less.

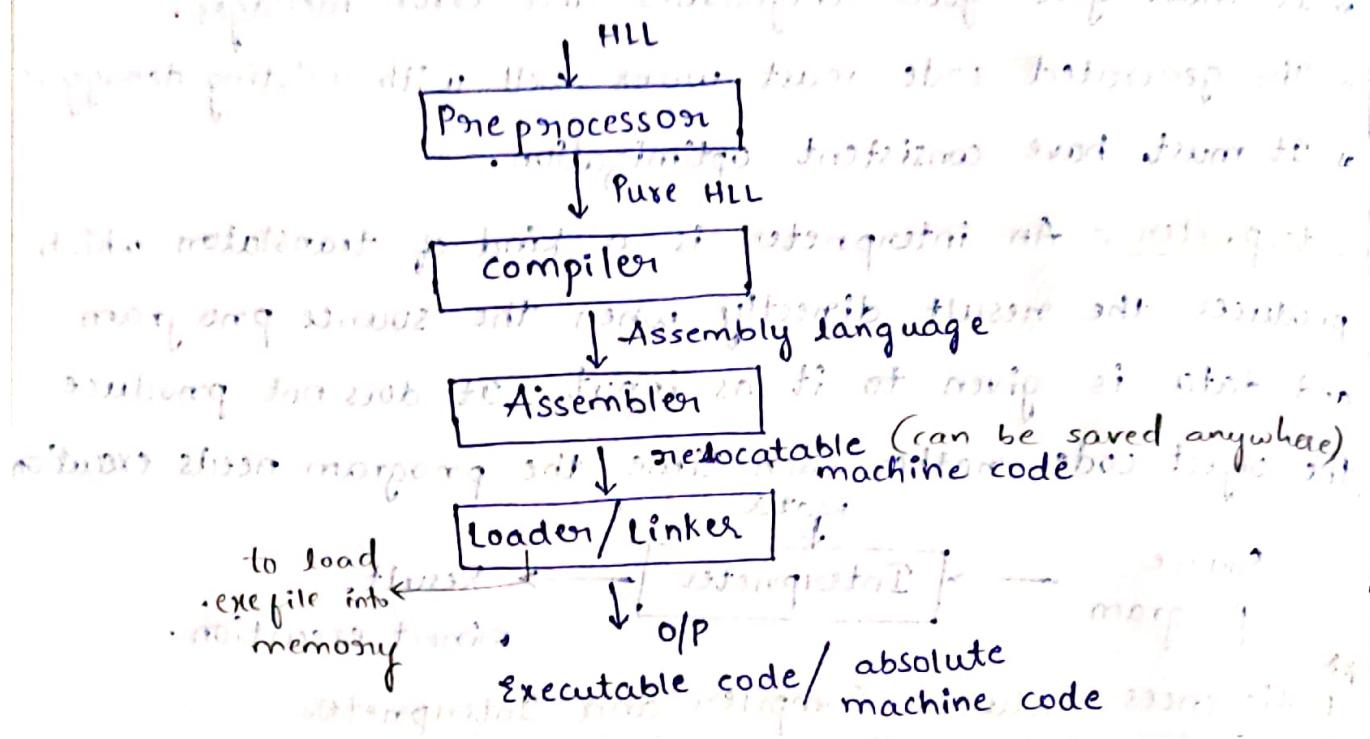
» Every time, high level program is converted into low level language.

» Errors are displayed for every instruction interpreted.

» Python is interpreted language.

→ The main goal of any translator is that, it must preserve the meaning of the source code with minimum loss.

Language Processing System



The high-level language programs are fed into a series of tools and operating system components to get the desired code that can be used by the machine. This is called language processing system.

» Preprocessor : In preprocessing, HLL is converted into pure HLL. Preprocessor removes the preprocessing directives (#include<stdio.h>) and adds the respective files i.e., file inclusions. It also performs macro expansion, conversions (ex: $a- \Rightarrow a=a-1$) and arithmetic operations.

» Compiler : During compilation, compiler converts pure HLL to assembly language.

» Assembly language : It is a low-level programming language. It is not in binary form.

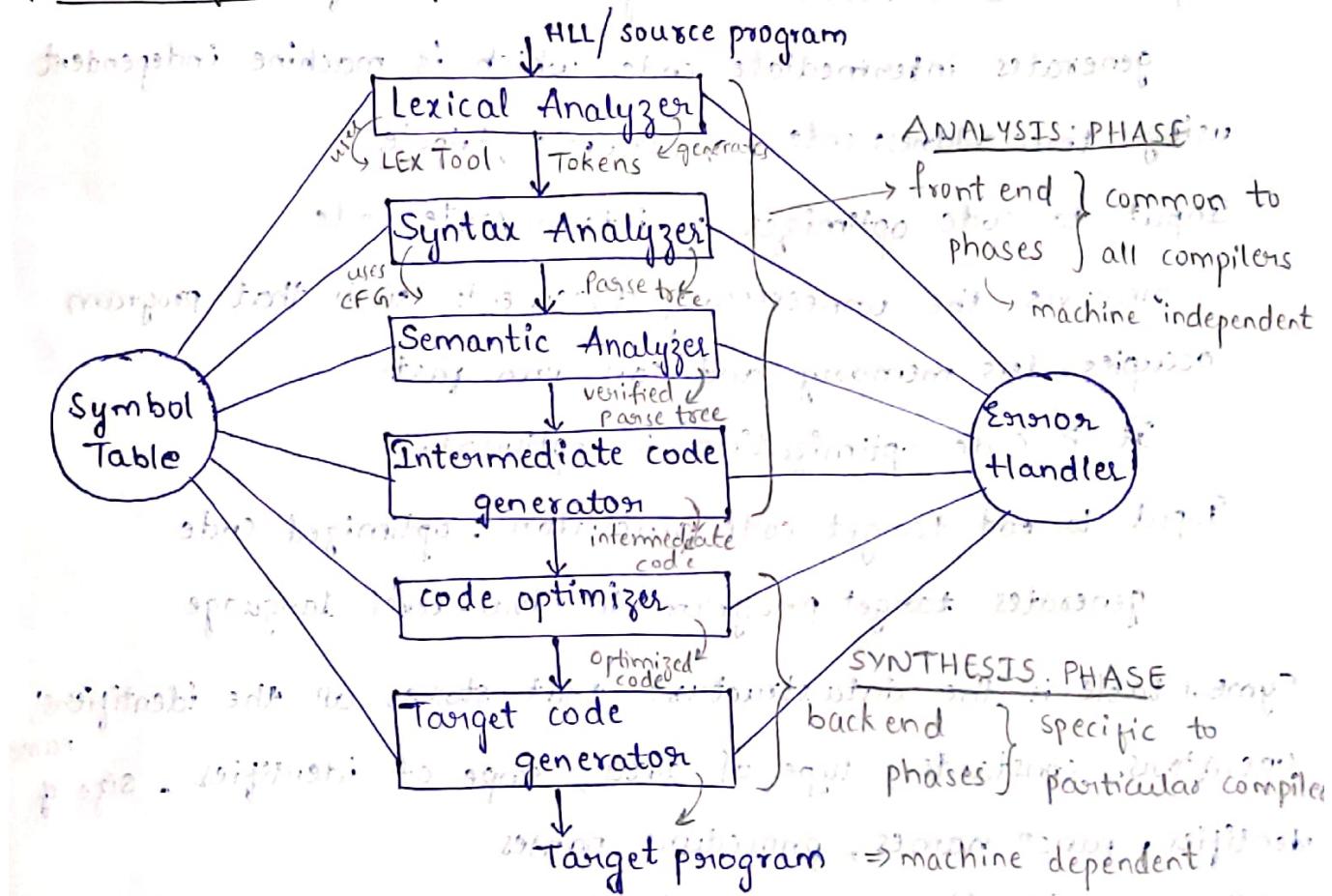
» Assembler : For every platform, we have different assemblers. Assembler for one platform will not work for another platform.

Assembly code is converted into executable machine code
» Relocatable machine code: that can be loaded anywhere in the memory.
Assembly code $\xrightarrow{\text{converted}}$ executable machine code.

- » Linker/Loader: It converts relocatable machine code into absolute machine code.
- » Linker: It links different object files into a single executable file.
- » Loader: It loads the executable file in the memory and executes it.
- » Absolute machine code: Code that is assembled to work at one specific address.

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* Phases of the Compiler



① Input to lexical analyzer: HLL source code
generates stream of tokens using LEX/TOKT that uses regular expression that has rules for a valid token.

It removes all spaces, commas, semi colons, tabs spaces.
Errors like repeated declarations, using keywords are detected.

② Input to syntax analyzer: stream of tokens from lexical analyzer
generates parse tree by bottom up LR(0) parser
uses CFG (Context Free Grammar) to check the syntax
identifies all the syntactical errors (if any)

③ Input to semantic analyzer: parse tree
checks for compatibility errors, parentheses matching,
if-else statements, control flow statements
generates verified parse tree

④ Input to Intermediate code generator: verified parse tree
generates intermediate code, which is machine independent.
using three address code, quadrapole, tripole

⑤ Input to code optimizer: intermediate code
removes the unnecessary statements such that program occupies less memory and can run fast
Code optimization is optional.

⑥ Input to code target code generator: optimized code
generates target program in low-level language.

Symbol table is the data structure that stores all the identifiers' name, operators, constants, type of data, scope of identifier, size of identifier, funcn names, procedure names.

When an identifier is encountered again, then it will not be entered into symbol table rather, it points to the already entered identifier.

It is also used to retrieve the identifiers.

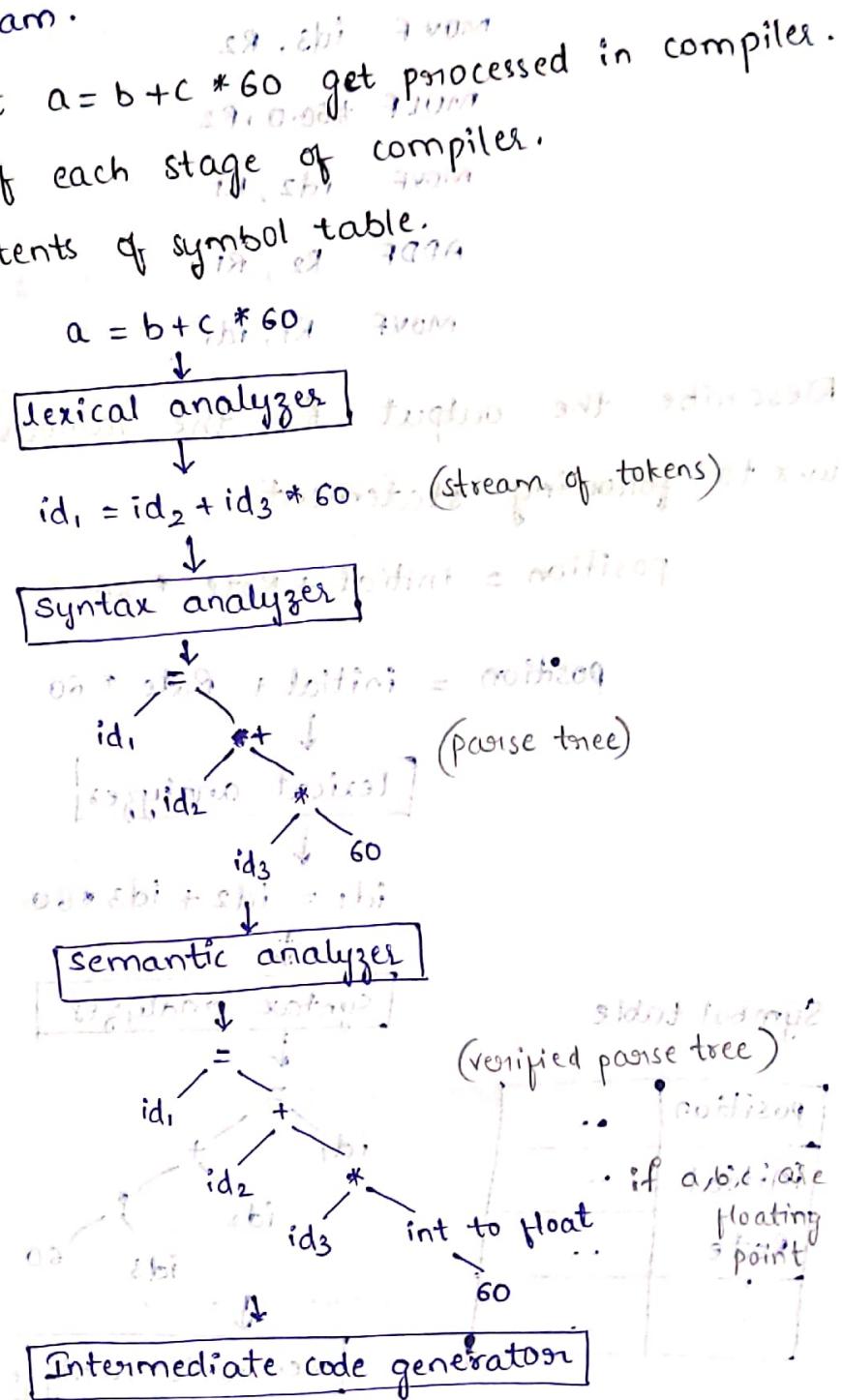
It is associated with each phase.

Error handler is associated with every phase.
It handles all the errors and ensures smooth compilation of the entire program.

Show how an input $a = b + c * 60$ get processed in compiler.
show the output of each stage of compiler.
Also show the contents of symbol table.

Symbol table

a	---
b	---
c	---
int	---



$$t_1 = \text{int to float } (60)$$

$$t_2 = id_3 * t_1$$

$$t_3 = id_2 + t_2$$

$$id_1 = t_3$$

(3-address code)

Code optimization

$$t_1 = id_3 * 60.0$$

$$id_1 = id_2 + t_1$$

target code generator

↓

`MOV F id3, R2`

`MULF #60.0, R2`

`MOVF id2, RI`

`ADDF R2, RI`

`MOVF RI, id1`

Describe the output for the various phases of the compiler w.r.t. to following statement:

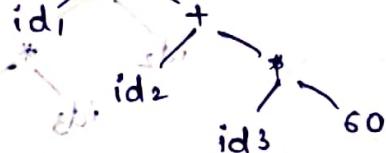
$$\text{position} = \text{initial} + \text{Rate} * 60$$

$$\text{position} = \text{initial} + \text{Rate} * 60$$

lexical analyzer

$$id1 = id2 + id3 * 60$$

syntax analyzer



stream of tokens:

Stream of tokens:

parse tree

Symbol table

position	..
initial	..
Rate	int to float
!	0.0

semantic analyzer

$$(id1) float \text{ of } id1 = id1$$

$$id1 = id2 + id3 * 60$$

$$id1 = id2 + id3 * 60$$

int to float

verified parse tree

intermediate code generator

id1 = id2 + id3 * 60

$t_1 = \text{int to float}$
 $t_2 = id_3 * t_1$
 $t_3 = id_2 + t_2$
 $t_4: id_1 = t_3$

code optimization

$t_1 = id_3 * 60.0$

$id_1 = id_2 + t_1$

target code generator

$\downarrow \quad \text{MOV F id}_3, R_2 \rightarrow \text{id}_1$

$\text{MULF} \# 60.0, R_2 \rightarrow \text{id}_1$

$\text{MOVF id}_2, R_1 \rightarrow$

~~$\text{ADD} [R_2, R_1]$~~

$\text{MOVF R}_1, id_1 \rightarrow$

$\downarrow \text{MOV A id}_1, id_1$

target code = phi

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Show the output generated by each phase for the following example.

$\text{price} = \text{amount} + \text{rate} * 50$

$\text{price} = \text{amount} + \text{rate} * 50$

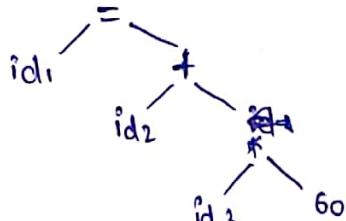
lexical analyzer

$\downarrow \text{Stream of tokens}$

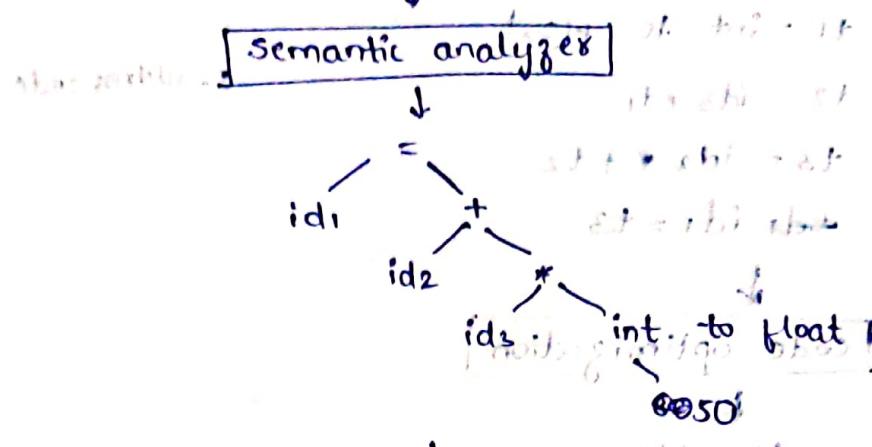
$id_1 = id_2 + id_3 * 50.0$

stream of tokens

syntax analyzer



parse tree



↓ $\text{id1} = \text{id2} + \text{id3} * 50.0$

intermediate code generator

↓

$t1 = \text{int to float}$ [float conversion]

$t2 = \text{id3} * 50.0$

$t3 = \text{id2} + t2$? var

$\text{id1} = t3 + 50.0$? sum

↓ $t3, t2$? var

code optimization [GCA pass]

↓ $t3, t2$? var

$t1 = \text{id3} * 50.0$

$\text{id1} = \text{id2} + t1$ [float]

all int already float \downarrow float conversion fusion with sum

Target code generator [ignores parentheses]

00 * 01 & float = 001001

MOVF id3, R2 [move]

MULF #50.0, R2 [float mul]

MOVF id2, R1 [move]

ADDF R2, R1 & R1 = R1

MOVF R1, id1 [move]

int move



Show the output generated by each phase for the following example.

$$x = (a+b) * (c+d)$$

$$x = (a+b) * (c+d)$$



lexical analyzer



$$id_1 = (id_2 + id_3) * (id_4 + id_5)$$



Syntax analyzer

parse tree

syntax tree

stream of tokens

parse tree

syntax tree

Intermediate code generator

3-address code

code optimization

code optimization

code optimization

code optimization

code optimization

code generator



(F1+F2) * (G1+G2)

Load id₁, id₂ (F1+G1) = X

ADD i

LOAD R_i, id₂ [load initial]

ADD R₁, id₃ i

(E1+i) + (E2+i) = rbi

LOAD R₂, id₄ i

ADD R₂, id₅ i

MUL R₁, R₂ [possible overflow?]

STORE id₁, R₁ i

Phases of the compiler

Symbol Table: It is a data structure being used by the compiler to store all the information related to identifiers.

Ex: its type, scope, size, location, name etc

» It helps the compiler to function smoothly by finding the identifiers quickly.

» All the phases interact with the symbol table manager.

Error Handler: It is a module which takes care of the events which are encountered during compilation, and it takes care to continue the compilation process even if error is encountered.

Lexical Analysis:

» Reads the program and converts it into tokens using a tool called Lex tool.

» Tokens are identified by regular expressions which are understood by the lexical analyzer.

» Removes whitespaces, comments, tab spaces etc.

» Lexical analyzer is also called as scanner

Syntax Analyzer / Parser:

» constructs parse tree

» Takes the tokens one by one and uses CFG to construct parse tree

- » If it is not possible to construct the parse tree, then input is syntactically incorrect and error messages are displayed.
- » By using Context Free Grammar (CFG), the input has to be checked whether it is in the desired format or not.
- » Syntax errors can be detected by it, if the input is not according to the grammar given.
- » It takes input as tokens and checks their syntactic correctness.

Semantic Analysis:

- » Once the syntax is checked in the syntax analysis phase, the next phase is semantic analysis, which determines the meaning of the source string. For ex^t meaning of the source string is matching of parentheses in the expression, matching of if-else statements, performing arithmetic operations of the expressions that are type-compatible, checking the scope of the operation.

Intermediate code generation:

- » The intermediate code is a kind of code, which is easy to generate and this code can be easily converted to target code.
- » This code can be in variety of forms such as 3-address code, quadruples, triples, post-fix notation.

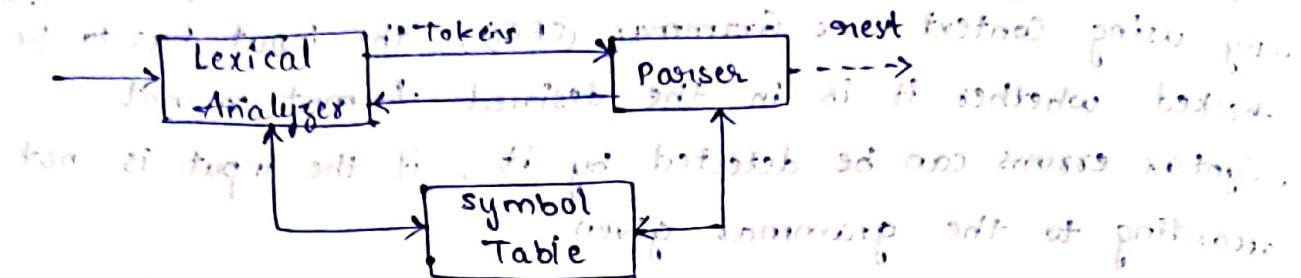
Code optimization:

- » The code optimization phase attempts to improve the intermediate code. This is necessary to have faster executing code or less consumption of memory. Thus, by optimizing the code, the overall running time of the target program can be improved.

Code generation:

- » In code generation phase, the target code gets generated. The intermediate code instructions are translated into sequence of machine instructions.

Lexical Analysis Phase



» Lexical Analysis is the first phase of the compiler, also called as Linear Analysis or Scanner Scanning.

» In this phase, the stream of characters making up source code is read from left to right and grouped into tokens that are sequence of characters having collective meaning.

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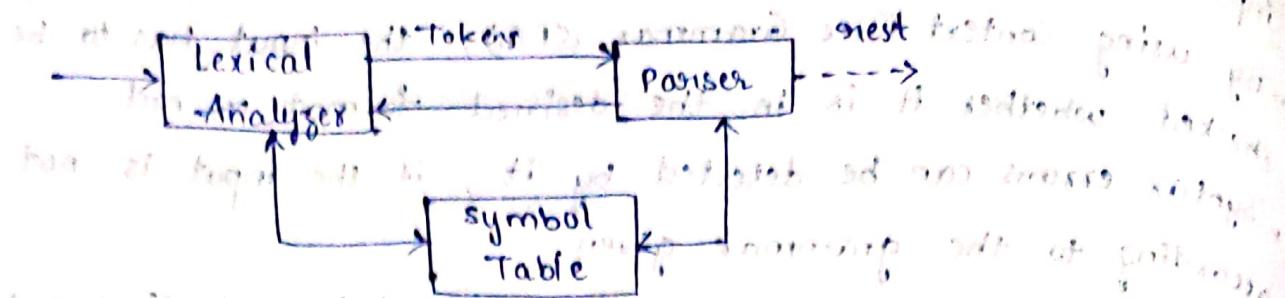
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Lexical Analysis Phase



» Lexical Analysis is the first phase of the compiler, also called as Linear Analysis or Scanner Scanning.

» In this phase, the stream of characters making up source code is read from left to right and grouped into tokens that are sequence of characters having collective meaning.

» Tokens include identifiers, operators, keywords...

4/9/2023 ~~with regards to the programming language, it can state~~ ~~in~~ ~~language~~

» Functions of Lexical Analyzer

- » It produces stream of tokens.
- » It eliminates blank spaces and comments.
- » It generates the symbol table which stores the information about identifiers, constants encountered in the input.
- » It keeps track of the line numbers.
- » It reports the errors encountered, e.g., generating the tokens.

Tokens :

» It describes the class or category of input string.

For ex :- identifiers, keywords, constants.

Patterns :

Set of rules that describe the tokens present in the program.

Lexemes :

Sequence of characters in the source program that are matched with the patterns on the tokens.

ex :- num is a valid token i.e., identifier; that follows the pattern

Ex: Identify tokens in the expression —

if ($a < b$)

if — keyword

(→ operator

. a → identifier

< → relational operator

b → identifier

) → operator

* Q) Define lexeme, token and pattern. Identify the lexemes that make up the tokens in the following program set.

Identify Indicate the corresponding token and pattern.

```

void swap(int i, &int j){
    int t;
    t = i;
    i = j;
    j = t;
}
  
```

<u>Lexeme</u>	<u>Token</u>	<u>Lexeme</u>	<u>Token</u>
void	keyword	t	identifier
swap	identifier	= (&	operator
(operator	i	identifier
int	keyword	=	operator
{	operator	j	identifier
if	identifier	=	operator
int	separation operator	j	identifier
{	operator	=	operator
int	keyword	t	identifier
{	operator	}	operator
int	identifier	↳	
if	operator	↳	
int	operator	↳	
{	operator	↳	
int	operator	↳	

Patterns

(i) Identifiers

- » Identifiers are a collection of letters
- » Identifier is a collection of alphanumeric characters)
- » The first character of an identifier must be a letter.

(ii) Operator

- » Operators can be arithmetic, logical, relational operators.
- » The parentheses, comma are considered as operators
- » assignment is denoted by operator

(iii) keyword

- » keywords are special words to which some meaning is associated with.
- » int, void are keywords for denoting data types.

Q) int max (int a, int b)
{

if (a > b)

return a;

else

return b;

}

int

max

identifier
keyword

(

operator

a

identifier

b

identifier

{

operator

if

keyword

>

relational
operator

return

keyword

else,

keyword
operator

lexeme

token

lexeme

token

lexeme

token

lexeme

token

int - keyword

token

int

int

max - identifier

token

max

max

(- operator

token

(

(

int - keyword

token

int

int

b - identifier

token

b

b

) - operator

token

)

)

{ - operator

token

{

{

if - keyword

token

if

if

(- operator

token

(

(

Lexeme operator taken

Patterns in the tokens

(i) Identifiers

Writing symbol

» Identifiers are a collection of letters

of case sensitive to writing symbol

» Identifier is a collection of alphanumeric characters

» The first character of an identifier must be a letter

but symbol is allowed as well

(ii) Operators

Writing symbol

» Operator can be arithmetic, logical, relational

» Parentheses are considered as operators

» Comma is treated as separation operator

» Assignment is denoted by operator

» greater than symbol (>) is an operator

(iii) keyword

» Keywords are special words to which some meaning is associated with.

» int, void are keywords for denoting data types.

» return is a keyword

» if, else are keywords for checking whether a condition is true.

Differences between Phases and Pass

Phase

1) The processing of compilation is carried out in various ways. These steps are preferred as Phases. The phases are:

Lexical phase

Syntax phase

Semantic phase

Intermediate code generation

code optimization

Target code generation

Pass

2) Various phases are logically grouped together to form a Pass. The process of compilation can be carried out in single pass or in multiple passes.

2) The task of compilation is carried out in analysis and synthesis phase.

3) The phases namely -
lexical analysis
syntax analysis

semantic analysis

Intermediate code generation
are machine independent.

code optimization

Target code generation

are machine dependent.

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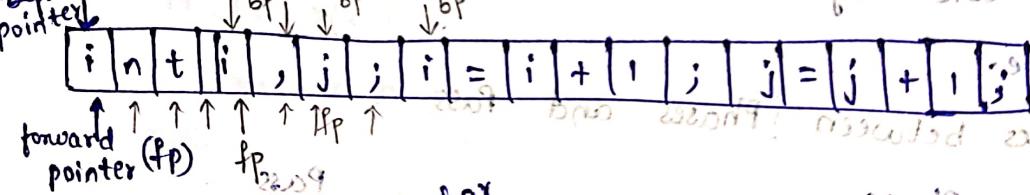
Input Buffering

int i, j; stores tokens at above lineage into buffer

i = i + ; after buffering

j = j + ; after tokens are buffered into bio. fp

lexical analyzer uses buffer to store avoid multiple system calls.



when it reads each char

when it encounters space, is identified.

a token is identified. then, is identified which is a keyword. Then, begin pointer is moved to i

both fp and bp are at i

Then, fp is incremented.

next char is ,

so, bp is also shifted to ,

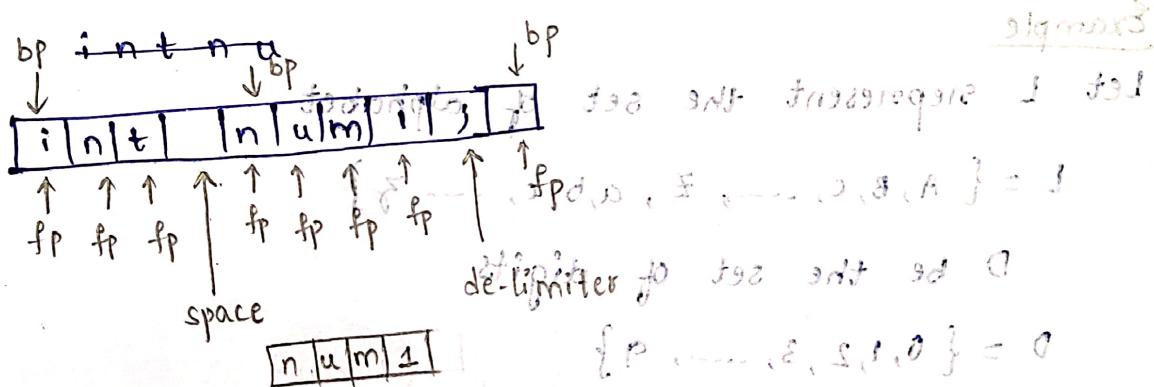
When ; is encountered it indicates end of the statement so, both bp and fp are moved to its disposal cell.

» Problem of using buffer is size. In prime programs all categories of buffer are appropriately used.

(i) one buffer
 (ii) two buffer

In single buffer, data is overwritten when buffer size is insufficient. In this method, data may be lost.

(iii) To overcome the problems of using single buffer, we use two buffer. When the end point of first buffer is reached, the remaining data is stored in second buffer. And, when second data buffer is reached to its end, it again uses first buffer. Thereby, the data of first buffer is lost.



Specifications of tokens (UNIT-I)

» To specify tokens, regular expressions are used. When a pattern is matched by some regular expression then, token can be recognized.

Language and String

» Language: finite set of non-empty strings.
 » String: collection of finite number of alphabet on letters.

- Indicates null string. i.e. concatenation of 0 words
- » The length of the string is denoted by $|s|$
 - » The empty string is denoted by ϵ
 - » The empty set of strings is denoted by \emptyset

Operations on Language

- 1) Union of two languages L_1 and L_2 i.e. $L_1 \cup L_2 = \{ \text{set of strings in } L_1 \text{ and set of strings in } L_2 \}$
- 2) Concatenation of two languages L_1 and L_2 i.e. $L_1 \cdot L_2 = \{ \text{set of strings in } L_1 \text{ followed by set of strings in } L_2 \}$
- 3) Kleen closure of language $L \Rightarrow L^* \text{ contains } \epsilon$
 - denotes 0 or more concatenations of L
 - includes ϵ This may contain ϵ
- 4) Positive closure $\Rightarrow L^+$
 - denotes 1 or more concatenations of L

Example

Let L represent the set of alphabet

$$L = \{ A, B, C, \dots, Z, a, b, c, \dots, z \}$$

D be the set of digits

$$D = \{ 0, 1, 2, 3, \dots, 9 \}$$

Then, by performing various operations the new language is generated as follows :

- 1) $L \cup D$ is a set of alphabet and digits
 - 2) $L \cdot D$ (or) LD is a set of strings consisting of alphabet followed by digits.
- No L^5 is a set of strings having length of 5 each

3) L^* is a string set of strings having all the strings including ϵ .

4) L^+ is a set of strings except ϵ .

Suppose, $L = \{a\}$ then,

$$L^* = \{\epsilon, a, aa, aaa, aaaa, \dots\}$$

$$L^+ = \{a, aa, aaa, aaaa, \dots\}$$

Suppose, $L = \{a, b\}$ then

$$L^* = \{\epsilon, a, b, ab, ba, aa, bbb, \dots\}$$

$$L^+ = \{a, b, ab, ba, aaa, bbb, \dots\}$$

- 3) L^* is a string set of strings having all the strings including ϵ .
- 4) L^+ is a set of strings except ϵ .
- suppose, $L = \{a\}$ then,
- $$L^* = \{\epsilon, a, aa, aaa, aaaa, \dots\}$$
- $$L^+ = \{a, aa, aaa, aaaa, \dots\}$$
- suppose, $L = \{a, b\}$ then
- $$L^* = \{\epsilon, a, b, ab, ba, aa, bbb, \dots\}$$
- $$L^+ = \{a, b, ab, ba, aaa, bbb, \dots\}$$

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Regular exp. has set of rules: { aab, ab, b, ϵ }

Regular Set

The finite set which denotes a regular language and the set which can be described by regular expressions is called Regular set.

Ex: A set of identifiers.

Because, it can be represented using regular expressions.

Regular Expressions

Regular expressions are mathematical symbolisms which describe the set of strings of specific language.

Rules for writing

following are the rules that describes the definition of regular expressions over the input set denoted by Σ

1. ϵ is a regular expression that denotes the set containing the empty string

2. If R_1 and R_2 are regular expressions, then

$R = R_1 + R_2$ ($R = R_1 \cdot R_2$) is also a regular expression

which represents Union operation.

3. If R_1 and R_2 are regular expressions, then

$R = R_1 R_2$ is also a regular expression which represents concatenation operation.

4. If R_1 is a regular expression, then $\{ \}$ is

$R = R_1^*$ is also a regular expression which denotes Kleen closure.

* The language denoted by regular expressions is called Regular set / Regular Language.

Q) Write a regular expression for the language accepting all the combinations of a 's including null over $\Sigma = \{a\}$.

$$L = \{\epsilon, a, aa, aaa, \dots\}$$

Ans: $L = a^*$

Q) Accept all the combinations of a except the null string.

$$L = \{a, aa, aaa, \dots\}$$

$$L = a^+$$

Q) Write a regular expression for the language containing the strings of length 2 over $\Sigma = \{0, 1\}$.

$$L = \{00, 01, 10, 11\}$$

$$RE = (0+1)(0+1)$$

Q) Write a regular expression for a language combining strings which ends with abba over $\Sigma = \{a, b\}$.

$$L = \{abb, aabb, babb, ababb, baabb, \dots\}$$

$$RE = (a+b)^* abb$$

Ans: $(a+b)^* = \{\epsilon, ab, aab, abb, bab, \dots\}$

with a and b in RE.

Q) construct a regular expression for the language containing all the strings having any number of a's and b's except ϵ .

$$RE = (a+b)^* \quad (\because L = \{a, b, aa, bb, ab, \dots\} \text{ null string})$$

Q) construct regular expression for the language accepting all the strings ending with 00 over the set $\Sigma = \{0, 1\}$

$$RE = (0+1)^* 00$$

$$L = \{000, 100, 0100, 1000, 01100, 10100, \dots\}$$

00, ...

Q) write a regular exp for the language accepting the strings which are starting with 1 and ending with 0 over the set $\Sigma = \{0, 1\}$

$$RE = 1 (0+1)^* 0$$

$$L = \{10, 1010, 1110, 100100, 1001000, \dots\}$$

Q) write RE to denote the language L over Σ^* where $\Sigma = \{a, b, c\}$ in which every string will be such that any number of a's followed by any number of b's followed by any number of c's are words.

$$RE = a^* b^* c^*$$

$$L = \{a, b, c, ab, bc, aabc, abc, \dots\}$$

Q) write a RE to denote L over Σ^* where,

$\Sigma = \{a, b\}$ such that the third character from right (end of the string) is always a.

$$RE = (a+b)^* a (a+b)^* (a+b)$$

Q) construct RE for the language which consists of exactly 2 b's over the set $\Sigma = \{a, b\}$

$$RE = a^* b a^* b a^*$$

Q) Describe the language for the following REs.

(1) $(0+1)^* 0 (0+1)^*$

The language L containing all the strings made up of 0's and 1's which contains at least one zero.

(2) $0^* 1 0^* 1 0^* 1 0^*$

The language L containing all the strings made up of 0's and 1's which contains exactly 3 ones.

12/09/2023

Finite Automata

» Finite Automata is an abstract computing device.

» It is a mathematical model of a system with discrete inputs, outputs, states and a set of transitions from state to state that occurs on input symbols from alphabet Σ .

A string is said to be Accepted String, if all the characters are accepted by the finite automata, based on the specific patterns.

To accept a string, the final state has to be reached.

num₁ num_{m1}
↑↑↑↑ ↑↑x symbol & string

Finite Automata Representations

1) Graphical representation (Transition diagram)

2) Tabular form (Transition Table)

3) Mathematical form (Transition function or
Mapping function)

Formal definition of Finite Automata

A finite Automata is a 5-tuple notation. They are

$M = (Q, \Sigma, \delta, q_0, F)$ where,

Q is a finite set of states

Σ is a finite set of input symbols or alphabet

$\delta \subseteq Q$

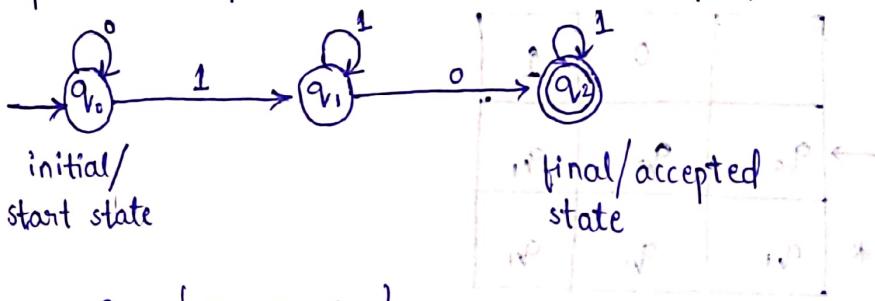
$\delta : Q \times \Sigma \rightarrow Q$ is transition function.

$q_0 \in Q$ is the start state, also called as Initial state

F is the set of accepted states, also called as final state.

Transition Diagram

It is a directed graph associated with the vertices of a graph corresponds to the state of finite automata.



$$Q = \{q_0, q_1, q_2\}$$

$$\Sigma = \{0, 1\}$$

$q_0 = \text{initial state}$

$F = q_2$ (final state)

Each state accepts one symbol at a time.

Here, q_0 takes the symbol '0' and stays at q_0 itself.

States now : (Initial, Input, State name) {

$$0\theta = (0, \varnothing) \beta$$

$$1\theta = (1, \varnothing) \beta$$

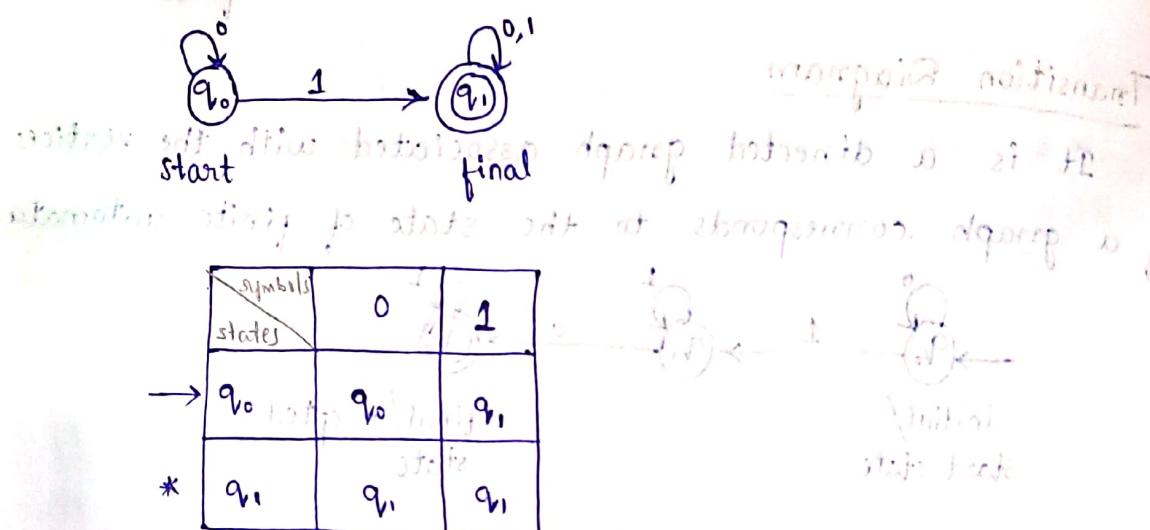
$$1\theta = (0, \varnothing) \beta$$

Transition Table

It is the tabular representation of the transition function that takes two arguments (a state, and symbol) and returning a value (the next state).
 Rows corresponds to states
 Columns correspond to input symbols
 Entries correspond to next states.

The start state is marked with an arrow $\rightarrow q_0$.

The accepted state is marked with $*$ q_1 .



Transition function / Mapping function

- » It is denoted by δ .
- » Two parameters are passed to this transition function.
 - (i) current state
 - (ii) Input symbol.
- » The transition function returns a state, which can be called as next state.

$$\delta(\text{current state}, \text{input symbol}) = \text{next state.}$$

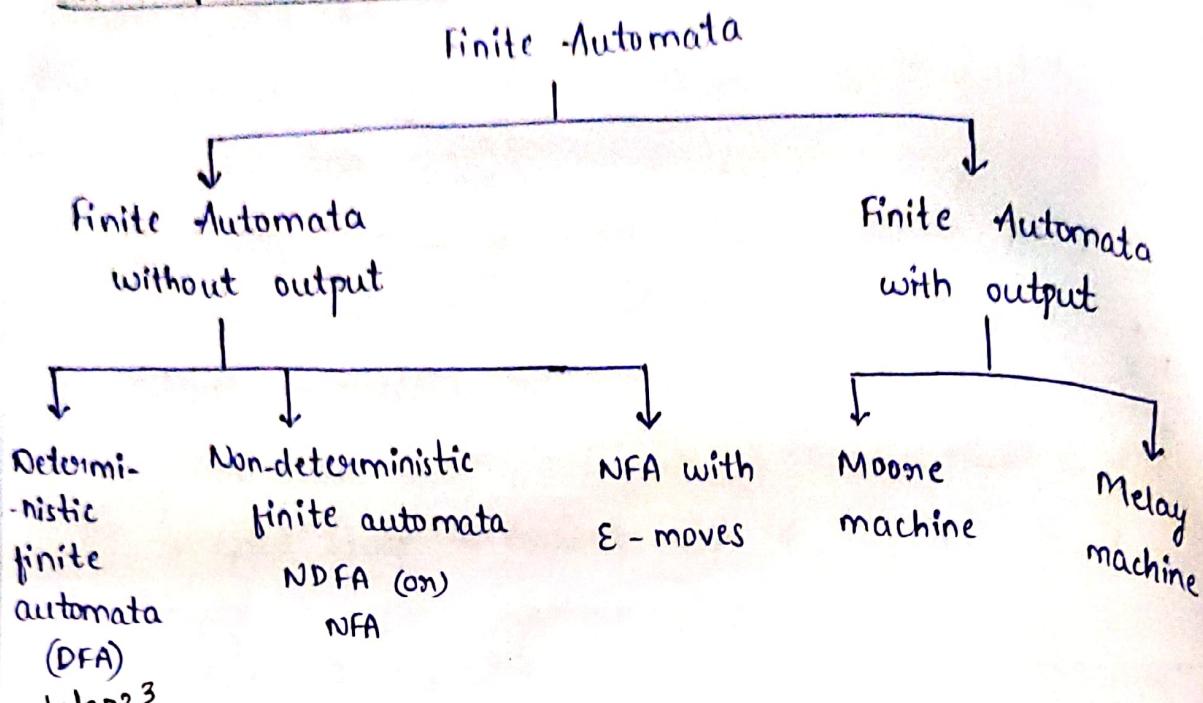
Ex:- $\delta(q_0, 0) = q_0$

$$\delta(q_0, 1) = q_1$$

$$\delta(q_1, 0) = q_1$$

$$\delta(q_1, 1) = q_1$$

Types of Finite Automata



Deterministic finite Automata (DFA)

- 1) DFA, if the machine can read an input string one symbol at a time.
- 2) In DFA, there is only one path for specific input from the current state to ~~the~~ next state.
- 3) DFA does not accept the null move ie, DFA cannot change state without any input symbol.
- 4) DFA can contain multiple final states. It is used in lexical analysis in compiler.

$$q_0 \xrightarrow{a} q_1$$

Formal Definition of DFA

DFA is a collection of 5 tuple notation,

$$M = (Q, \Sigma, \delta, q_0, f)$$

Q : finite set of states

Σ : finite set of input symbols

δ : transition function

q_0 : start state

f : final ~~set~~ state

Acceptance of a Language

Language acceptance is defined by, if a string w is accepted by machine M i.e., if it is reaching the final state F by taking the string w .

Not accepted if not reaching the final state.

Ex :-

$$\Rightarrow L = \{ \} \Rightarrow \emptyset$$

If language contains nothing $\Rightarrow q_0$ (no string)

It is represented by single state.

$\Rightarrow L = \{\epsilon\} \Rightarrow q_0$ (no move) we don't have s/p so, it will not move to initial & final state, next state.

If we are able to express neg. expr. for ϵ It means that our DFA can accept it.

\Rightarrow DFA to accept 'a'



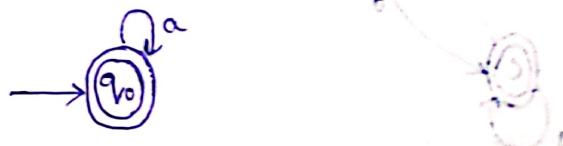
\Rightarrow DFA to accept zero or more no. of 'a's

$$L = \{ \epsilon, a, aa, aaa, \dots \}$$

regular exp. $= a^*$

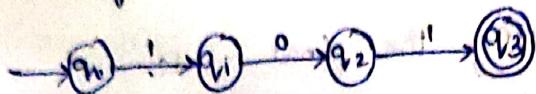
No. of states depends on min length string

NOTE : No. of states = min str. length + 1

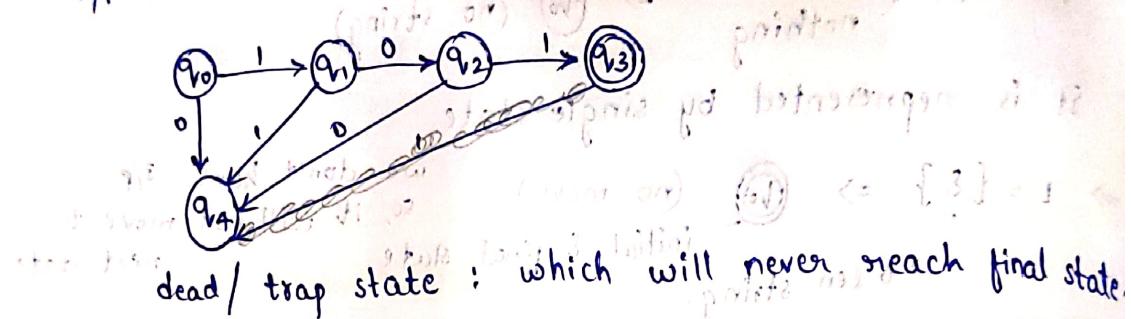


$$\{ \dots, 0001, 010, 01 \} \in L \text{ (pair of strings)}$$

Q) Design DFA which accepts 101 string over $\Sigma = \{0, 1\}$.
 $\Sigma = \{0, 1\}$, length of the string = 3
no. of states = $3 + 1 = 4$



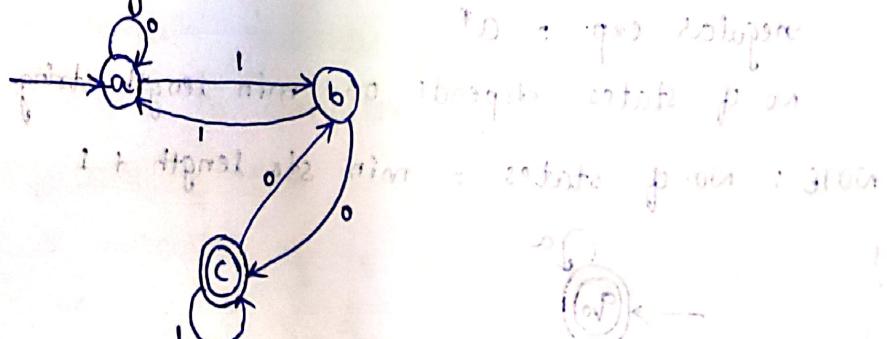
2nd S/P: 0101



Q) Let DFA be $Q = \{a, b, c\}$, $\Sigma = \{0, 1\}$, $q_0 = \{a\}$, $F = \{c\}$ and construct a DFA based on transition tabl

	0	1
a	a	b
b	c	a
c	b	c

Transition diagram:



Accepted string: $L = \{10, 010, 1000, \dots\}$

Q) Design DFA

(i) str starting with a

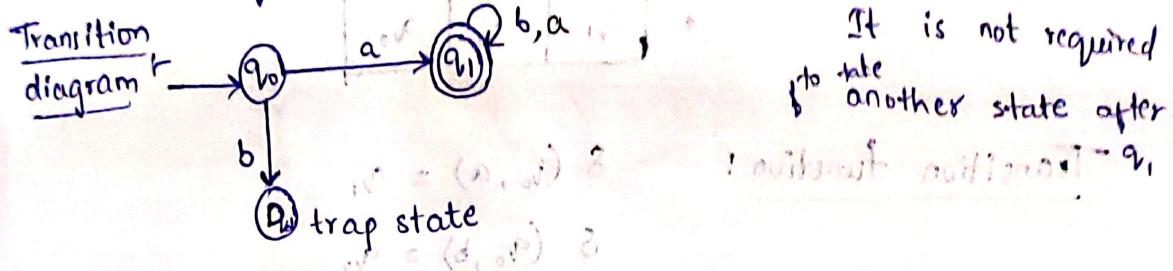
(ii) str ending with a

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$$(i) L = \{ a, ab, abb, aba, ababa, \dots \}$$

min length str = a \Rightarrow len = 1

no. of states = $1+1 = 2$



It is not required
to take another state after

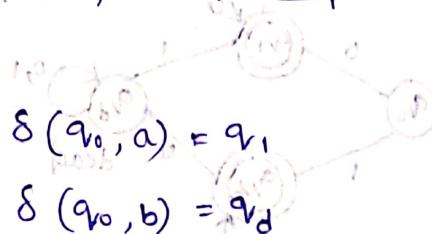
$$(ii) L = \{ a, aa \}$$

$$(iii) L = \{ a, aa, ab, abab \}$$

Transition table

	a	b
q_0	q_1	q_d
q_1	q_1	q_1
q_d	q_d	q_d

Transition function



$$\delta(q_0, a) = q_1$$

$$\delta(q_0, b) = q_d$$

$$\delta(q_1, a) = q_1$$

$$\delta(q_1, b) = q_1$$

$$(ii) L = \{ a, aa, aba, ba, baa, ababa, \dots \}$$

min length str = a \Rightarrow len = 1

no. of states = $1+1 = 2$

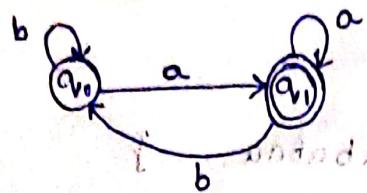
$$a^2 = (1, a) \text{ } 3$$

$$ab = (0, a) \text{ } 3$$

$$ba = (1, b) \text{ } 3$$

$$b^2 = (0, b) \text{ } 3$$

Transition diagram



Transition table

	a	b
q0	q1	q0
*	q1	q0

Transition function:

$$\delta(q_0, a) = q_1$$

$$\delta(q_0, b) = q_0$$

$$\delta(q_1, a) = q_0$$

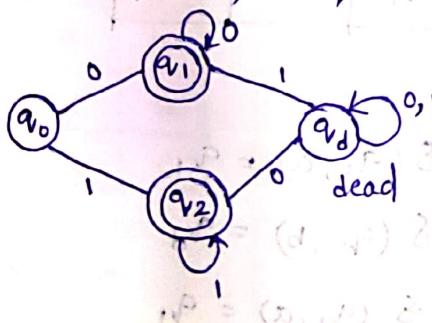
$$\delta(q_1, b) = q_1$$

Multiple final States

- Q) Draw a DFA for the lang. accepting strings with 0's and 1's only over the input alphabet, $\Sigma = \{0, 1\}$

$$L = \{0, 00, 1, 11, 000, 1111, 00000, \dots\}$$

Transition diagram



Transition Table

	0	1
q0	q1	q2
*	q1	q2

Transition function:

$$\delta(q_0, 0) = q_1$$

$$\delta(q_0, 1) = q_2$$

$$\delta(q_1, 0) = q_1$$

$$\delta(q_1, 1) = q_d$$

$$\delta(q_2, 0) = q_d$$

$$\delta(q_2, 1) = q_1$$

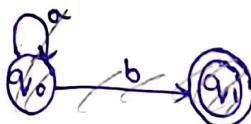
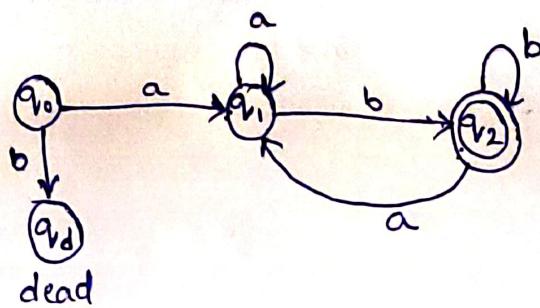
Q) Construct a DFA which accept a language of all the strings starting with 'a' and ending with 'b'.

$$L = \{ ab, aab, abb, abab, abaabb, \dots \}$$

min length str = 2

no. of states = $2+1 = 3$

Transition diagram :-



Transition Table :-

	a	b
\rightarrow	q_1	q_d
\rightarrow	q_1	q_2
*	q_2	q_1

Transition function :-

$$\delta(q_0, a) = q_1$$

$$\delta(q_0, b) = q_d$$

$$\delta(q_1, a) = q_1$$

$$\delta(q_1, b) = q_2$$

$$\delta(q_2, a) = q_2$$

$$\delta(q_2, b) = q_2$$

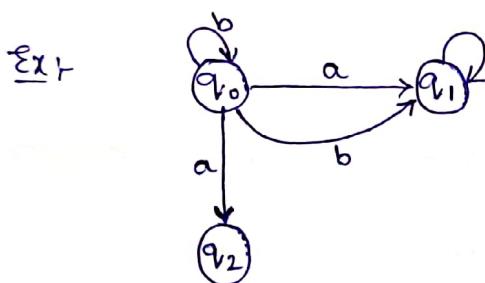
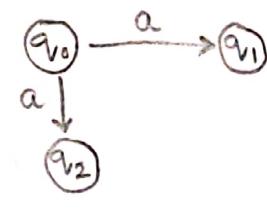
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Non-Deterministic Finite Automata (NFA)

- » NFA stands for Non-Deterministic Finite Automata.
- » It is easy to construct an NFA, when compared to DFA for a given regular expression.
- » The finite automata are called NFA, when there exists many paths for specific input from the current state to the next state.
- » Each NFA can be translated into DFA but, every NFA is non-DFA.
- » NFA is defined in the same way as DFA but, with the following two exceptions :-

(i) It contains multiple next paths

(ii) It contains ϵ -transitions



- » NFA also have 5 tuples which are same as DFA, but with different transition function

$$\delta : Q \times \Sigma \rightarrow 2^Q$$

↳ finite set of states

In DFA,

$$\delta : Q \times \Sigma \rightarrow Q$$

- » NFA is defined as a 5 tuple notation

$$M = (Q, \Sigma, \delta, q_0, F), \text{ where}$$

Q : finite set of states

Σ : finite set of input symbols

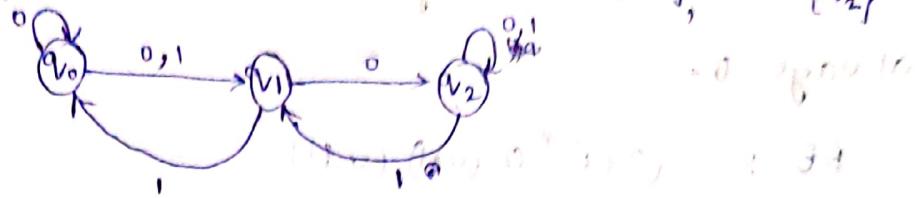
δ : transition function

q_0 : start state

F : end state

Q) Construct the transition table for the given NFA.

$\Sigma = \{q_0, q_1, q_2\}$, $\delta = \{q_1\}$, $q_0 \in F$, $F = \{q_2\}$



Transition Table :-

	0	1
q_0	$\{q_0, q_1\}$	q_1
q_1	q_2	q_0, q_2
q_2	q_2	$\{q_1, q_2\}$

Q) Design NFA transition diagram for the transition table given.

	0	1
q_0	$\{q_0, q_1\}$	$\{q_0, q_2\}$
q_1	$\{q_3\}$	
q_2	$\{q_2, q_3\}$	$\{q_3\}$
q_3	$\{q_3\}$	$\{q_3\}$

Transition diagram :-

1st row of 2nd column $\delta(q_0, 0) = \{q_0, q_1\}$

$\delta(q_0, 1) = \{q_0, q_2\}$

$\delta(q_1, 0) = \{q_3\}$

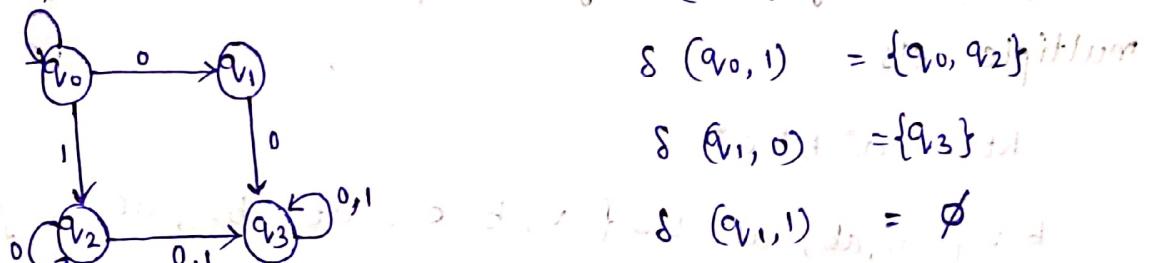
$\delta(q_1, 1) = \emptyset$

$\delta(q_2, 0) = \{q_2, q_3\}$

$\delta(q_2, 1) = \{q_3\}$

$\delta(q_3, 0) = \{q_3\}$

$\delta(q_3, 1) = \{q_3\}$

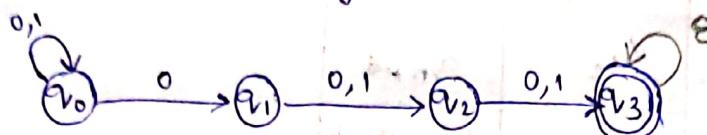


Q) Design NFA with $\Sigma = \{0,1\}$ accepting all strings in which the third symbol from the right end is always 0.

$$RE : \underline{(0+1)^*} 0 (0+1) (0+1)$$

self loop

$b \in \emptyset$ min length str = 4



NFA-ε

It is also a 5-tuple notation

$$M = (Q, \Sigma, \delta, q_0, F)$$

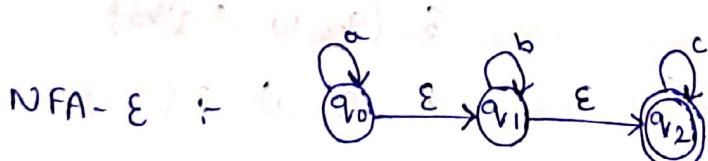
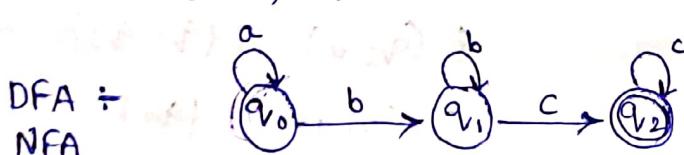
Here, $\Sigma = \{0, 1, \epsilon\}$

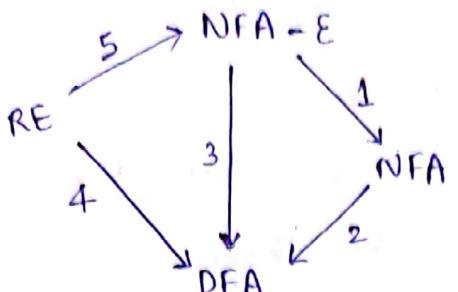
$$\begin{array}{c} \Sigma' = \Sigma \cup \{\epsilon\} \\ (\text{NFA-}\epsilon) \quad (\text{NFA}) \end{array}$$

Q) Construct NFA with ϵ which accepts all strings over the alphabet $\Sigma = \{a, b, c\}$ where, string contains multiple a's followed by multiple b's followed by multiple c's.

$$RE = a^* b^* c^*$$

$$L = \{a, ab, abc, \dots\} \quad L' = \{a, b, c, ab, bc, ac, \dots\}$$





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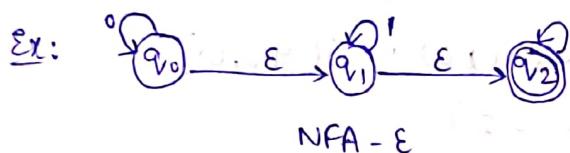
① NFA-E to NFA

2 steps

→ (i) ϵ -closure (state) = self state + ϵ -move to other state

→ (ii) $\delta'(\text{q}_v, a) = \epsilon\text{-closure}(\delta(\hat{\delta}(\text{q}_v, \epsilon), a))$

where, $\hat{\delta}(\text{q}_v, \epsilon) \Rightarrow \epsilon\text{-closure}(\text{q}_v)$



(i) find ϵ -closure of states $(\text{q}_0, \text{q}_1, \text{q}_2)$

$$\begin{aligned} \epsilon\text{-closure}(\text{q}_0) &= (\text{self state for } \text{q}_0) + \\ &\quad (\epsilon\text{-move to other state}) \rightarrow \text{q}_0 \rightarrow \text{q}_1, \text{q}_1 \rightarrow \text{q}_2 \\ &= \{\text{q}_0, \text{q}_1, \text{q}_2\} \end{aligned}$$

$$\begin{aligned} \epsilon\text{-closure}(\text{q}_1) &= (\text{self state for } \text{q}_1) + (\epsilon\text{-move to other state}) \\ &= \{\text{q}_1, \text{q}_2\} \end{aligned}$$

$$\begin{aligned} \epsilon\text{-closure}(\text{q}_2) &= (\text{self state for } \text{q}_2) + (\epsilon\text{-move to other state}) \\ &= \{\text{q}_2\} \end{aligned}$$

$$(ii) \delta'(\text{q}_0, o) = \epsilon\text{-closure}(\delta(\hat{\delta}(\text{q}_0, \epsilon), o))$$

$$= \epsilon\text{-closure}(\delta(\text{q}_0, \text{q}_1, \text{q}_2), o)$$

$$= \epsilon\text{-closure}(\delta(\text{q}_0, o) \cup \delta(\text{q}_1, o) \cup \delta(\text{q}_2, o))$$

$$= \epsilon\text{-closure}(\text{q}_0 \cup \emptyset \cup \emptyset)$$

$$= \epsilon\text{-closure}(\text{q}_0)$$

$$\delta'(\text{q}_0, o) = \{\text{q}_0, \text{q}_1, \text{q}_2\}$$

$$\begin{aligned}
 \delta'(q_0, 1) &= \text{\varepsilon-closure}(\delta(\hat{\delta}(q_0, \varepsilon), 1)) \\
 &= \text{\varepsilon-closure}(\delta(q_0, q_1, q_2), 1) \\
 &= \text{\varepsilon-closure}(\delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_2, 1)) \\
 &= \text{\varepsilon-closure}(\emptyset \cup q_1 \cup q_2) \\
 &= \text{\varepsilon-closure}(q_1 \cup q_2) \\
 &= \text{\varepsilon-closure}(q_1) \cup \text{\varepsilon-closure}(q_2) \\
 &= \{q_1, q_2\} \cup \{q_2\}
 \end{aligned}$$

$$\Rightarrow \delta'(q_0, 1) = \{q_1, q_2\}$$

$$\begin{aligned}
 \delta'(q_1, 0) &= \text{\varepsilon-closure}(\delta(\hat{\delta}(q_1, \varepsilon), 0)) \\
 &= \text{\varepsilon-closure}(\delta(q_1, q_2), 0) \\
 &= \text{\varepsilon-closure}(\delta(q_1, 0) \cup \delta(q_2, 0)) \\
 &= \text{\varepsilon-closure}(\emptyset \cup \emptyset) \\
 &= \text{\varepsilon-closure}(\emptyset)
 \end{aligned}$$

$$\Rightarrow \delta'(q_1, 0) = \emptyset$$

$$\begin{aligned}
 \delta'(q_1, 1) &= \text{\varepsilon-closure}(\delta(\hat{\delta}(q_1, \varepsilon), 1)) \\
 &= \text{\varepsilon-closure}(\delta(q_1, q_2), 1) \\
 &= \text{\varepsilon-closure}(\delta(q_1, 1) \cup \delta(q_2, 1)) \\
 &= \text{\varepsilon-closure}(q_1, q_2)
 \end{aligned}$$

$$\delta'(q_1, 1) = \{q_1, q_2\}$$

$$\begin{aligned}
 \delta'(q_2, 0) &= \text{\varepsilon-closure}(\delta(\hat{\delta}(q_2, \varepsilon), 0)) \\
 &= \text{\varepsilon-closure}(\delta(q_2), 0) \\
 &= \text{\varepsilon-closure}(\delta(q_2, 0)) \\
 &= \text{\varepsilon-closure}(\emptyset)
 \end{aligned}$$

$$\Rightarrow \delta'(q_2, 0) = \emptyset$$

$$\begin{aligned}
 \delta'(q_2, 1) &= \text{\varepsilon-closure}(\delta(\hat{\delta}(q_2, \varepsilon), 1)) \\
 &= \text{\varepsilon-closure}(\delta(q_2), 1) \\
 &= \text{\varepsilon-closure}(\delta(q_2, 1)) \\
 &= \text{\varepsilon-closure}(q_2)
 \end{aligned}$$

$$\delta'(q_2, 1) = \{q_2\}$$

Transition Table

	0	1
q_0	$\{q_0, q_1, q_2\}$	$\{q_1, q_2\}$
q_1	\emptyset	$\{q_1, q_2\}$
q_2	\emptyset	$\{q_2\}$

Equivalent NFA diagram

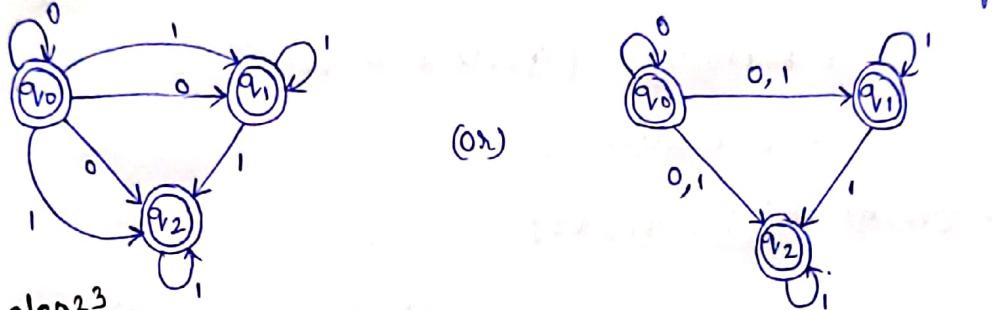
Initial state is always q_0

In NFA-E, q_2 is final state, so check for

ϵ -closure (q_0), it contains q_2 so, q_0 is final state

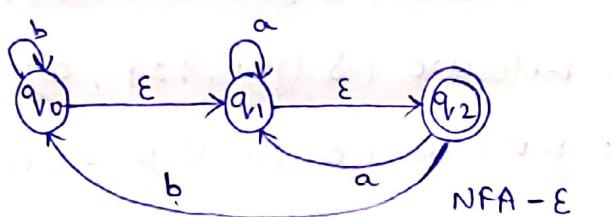
ϵ -closure (q_1), it contains q_2 so, q_1 is also final state

ϵ -closure (q_2), it contains q_2 so, q_2 is also final state



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Ex ②



i) to find ϵ -closure (state) here; q_0, q_1, q_2 are states.

= self state + ϵ -moves to other state

ϵ -closure (q_0) = self state for q_0 +

ϵ -moves to other state

$$= \{q_0, q_1, q_2\}$$

ϵ -closure (q_1) = $\{q_1, q_2\}$

ϵ -closure (q_2) = $\{q_2\}$

$$\begin{aligned}
 \delta(q_0, a) &= \text{-closure } (\delta(\delta(q_0, \epsilon), a)) \\
 &= \text{-closure } (\delta(\text{-closure}(q_0), a)) \\
 &= \text{-closure } (\delta(\{\delta(q_0, q_1, q_2\}, a)) \\
 &= \text{-closure } (\delta(q_{00}) \cup \delta(q_{10}) \cup \delta(q_{20}) \cup \delta(q_{30})) \\
 &= \text{-closure } (\emptyset \cup q_1 \cup q_2) \\
 &= \text{-closure } (q_1)
 \end{aligned}$$

$$\Rightarrow \delta'(q_0, a) = \{q_1, q_2\}$$

$$\begin{aligned}
 \delta'(q_0, b) &= \text{-closure } (\delta(\text{-closure}(q_0), b)) \\
 &= \text{-closure } (\delta(\{q_0, q_1, q_2\}, b)) \\
 &= \text{-closure } (\delta(q_0, b) \cup \delta(q_1, b) \cup \delta(q_2, b)) \\
 &= \text{-closure } (q_0 \cup \emptyset \cup q_0) \\
 &= \text{-closure } (q_0)
 \end{aligned}$$

$$\Rightarrow \delta'(q_0, b) = \{q_0, q_1, q_2\}$$

$$\begin{aligned}
 \delta'(q_1, a) &= \text{-closure } (\delta(\text{-closure}(q_1), a)) \\
 &= \text{-closure } (\delta(\{q_1, q_2\}, a)) \\
 &= \text{-closure } (\delta(q_1, a) \cup \delta(q_2, a)) \\
 &= \text{-closure } (q_1 \cup q_1) \\
 &= \text{-closure } (q_1)
 \end{aligned}$$

$$\Rightarrow \delta'(q_1, a) = \{q_1, q_2\}$$

$$\begin{aligned}
 \delta'(q_1, b) &= \text{-closure } (\delta(\text{-closure}(q_1), b)) \\
 &= \text{-closure } (\delta(\{q_1, q_2\}, b)) \\
 &= \text{-closure } (\delta(q_1, b) \cup \delta(q_2, b)) \\
 &= \text{-closure } (\emptyset \cup q_0) \\
 &= \text{-closure } (q_0)
 \end{aligned}$$

$$\Rightarrow \delta'(q_1, b) = \{q_0, q_1, q_2\}$$

$$\begin{aligned}
 \delta'(q_2, a) &= \text{-closure } (\delta(\text{-closure}(q_2), a)) \\
 &= \text{-closure } (\delta\{q_0, q_2\}, a) \\
 &= \text{-closure } (\delta(q_2, a) \cup \delta(q_2, a)) \\
 &= \text{-closure } (q_1) \cup q_1 \\
 &= \text{-closure } (q_1) \\
 \Rightarrow \delta'(q_2, a) &= \{q_1, q_2\}
 \end{aligned}$$

$$\begin{aligned}
 \delta'(q_2, b) &= \text{-closure } (\delta(\text{-closure}(q_2), b)) \\
 &= \text{-closure } (\delta(q_2, b)) \\
 &= \text{-closure } (q_0) \\
 \Rightarrow \delta'(q_2, b) &= \{q_0, q_1, q_2\}
 \end{aligned}$$

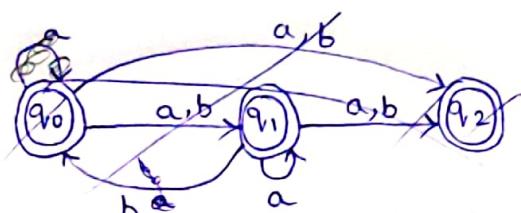
Transition Table

	a	b
q_0	$\{q_1, q_2\}$	$\{q_0, q_1, q_2\}$
q_1	$\{q_1, q_2\}$	$\{q_0, q_1, q_2\}$
q_2	$\{q_1, q_2\}$	$\{q_0, q_1, q_2\}$

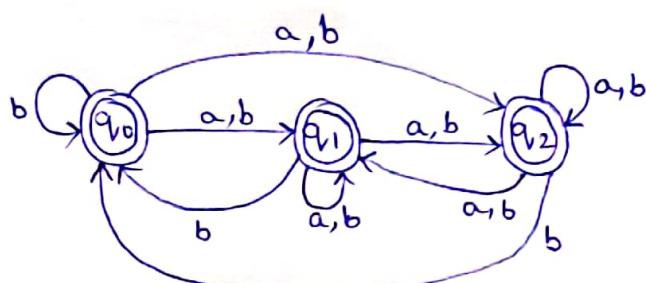
Equivalent NFA diagram

In NFA-E, q_2 is the final state.

If q_2 is present in ^{any} of the $\text{-closure}(q_0)$, $\text{-closure}(q_1)$, $\text{-closure}(q_2)$ then, it becomes the final state.



Here, q_2 is present in $\text{-closure}(q_0)$, $\text{-closure}(q_1)$ and $\text{-closure}(q_2)$.

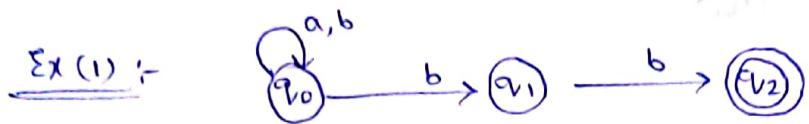


25/9/2023

② NFA to DFA

DFA transition function: $\delta: Q \times \Sigma \rightarrow Q$

NFA transition function: $\delta: Q \times \Sigma \rightarrow 2^Q$



Step 1 :- construct NFA transition table.

	a	b
q_0	q_0	q_0, q_1
q_1	\emptyset	q_2
q_2	\emptyset	\emptyset

Step 2 :- construct DFA transition table

	a	b
q_0	q_0	$\{q_0, q_1\}$
q_0, q_1	q_0	$\{q_0, q_1, q_2\}$
q_0, q_1, q_2	q_0	$\{q_0, q_1, q_2\}$

(i) 1st row in DFA π will be 1st row in NFA π

(ii) Next row in DFA π will be last col of its previous row.

$$\delta((q_0, q_1), a) \Rightarrow \delta(q_0, a) \cup \delta(q_1, a)$$

$$\Rightarrow q_0 \cup \emptyset$$

$$\Rightarrow q_0$$

$$\delta((q_0, q_1), b) \Rightarrow \delta(q_0, b) \cup \delta(q_1, b)$$

$$\Rightarrow (q_0, q_1) \cup (q_2)$$

$$\Rightarrow q_0, q_1, q_2$$

$$\delta((q_0, q_1, q_2), a) \Rightarrow \delta(q_0, a) \cup \delta(q_1, a) \cup \delta(q_2, a)$$

$$\Rightarrow q_0 \cup \emptyset \cup \emptyset$$

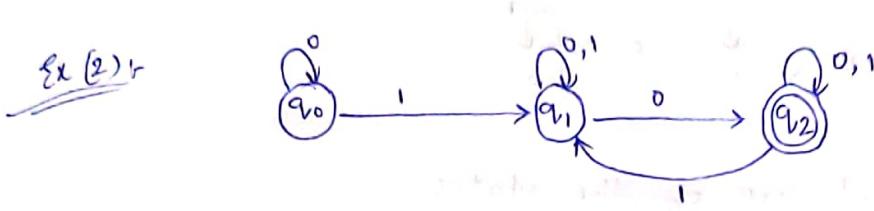
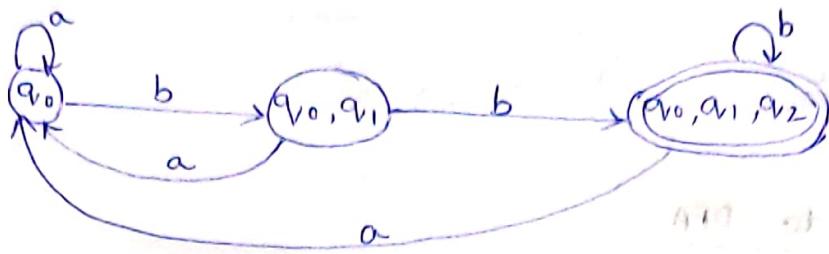
$$\Rightarrow q_0$$

$$\delta((q_0, q_1, q_2), b) \Rightarrow \delta(q_0, b) \cup \delta(q_1, b) \cup \delta(q_2, b)$$

$$\Rightarrow (q_0, q_1) \cup q_2 \cup \emptyset$$

$$\Rightarrow q_0, q_1, q_2$$

step-3 \vdash construct transition diagram for DFA



step 1 \vdash construct NFA \Rightarrow transition table

	0	1
q_0	q_0	q_1
q_1	q_1, q_2	q_1
q_2	q_2	q_1, q_2

step 2 \vdash construct DFA transition table

	0	1
q_0	q_0	q_1
q_1	q_1, q_2	q_1
q_2	q_1, q_2	q_1, q_2

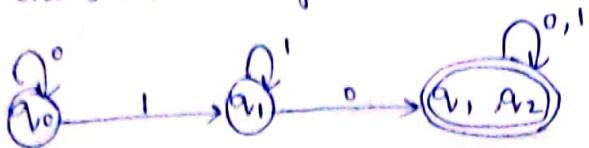
$$\delta(q_1, 0) = q_1, q_2$$

$$\delta(q_1, 1) = q_1$$

$$\begin{aligned} \delta(q_1, q_2, 0) &= \delta(q_1, 0) \cup \delta(q_2, 0) \\ &= (q_1, q_2) \cup q_2 \\ &= q_1, q_2 \end{aligned}$$

$$\begin{aligned} \delta(q_1, q_2, 1) &= \delta(q_1, 1) \cup \delta(q_2, 1) \\ &= \delta(q_1, q_2) \end{aligned}$$

step 3: DFA transition diagram.



③ NFA- ϵ to DFA



Step 1: find ϵ -closure of the states

ϵ -closure (state) = self state + ϵ -move to other state

$$\epsilon\text{-closure } (q_0) = \{q_0, q_1, q_2\}$$

$$\epsilon\text{-closure } (q_1) = \{q_1, q_2\}$$

$$\epsilon\text{-closure } (q_2) = \{q_2\}$$

Step 2: construct DFA transition table

(i) 1st state in DFA is ϵ -closure of q_0 (initial state)

	0	1
* q_0, q_1, q_2	$\{q_0, q_1, q_2\}$	$\{q_1, q_2\}$
* q_1, q_2	\emptyset	$\{q_1, q_2\}$

$$\delta((q_0, q_1, q_2), 0) = \epsilon\text{-closure } \delta((q_0, q_1, q_2), 0)$$

$$\Rightarrow \epsilon\text{-closure } (\delta(q_0, 0) \cup \delta(q_1, 0) \cup \delta(q_2, 0))$$

$$\Rightarrow \epsilon\text{-closure } (q_0) = \{q_0, q_1, q_2\}$$

$$\delta((q_0, q_1, q_2), 1) = \epsilon\text{-closure } (\delta(q_0, q_1, q_2), 1)$$

$$= \epsilon\text{-closure } (\delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_2, 1))$$

$$= \epsilon\text{-closure } (\emptyset \cup q_1 \cup q_2)$$

$$= \epsilon\text{-closure } (q_1 \cup q_2)$$

$$= \epsilon\text{-closure } (q_1) \cup \epsilon\text{-closure } (q_2)$$

$$= \{q_1, q_2\} \cup \{q_2\}$$

$$\Rightarrow \delta((q_0, q_1, q_2), 1) = \{q_1, q_2\}$$

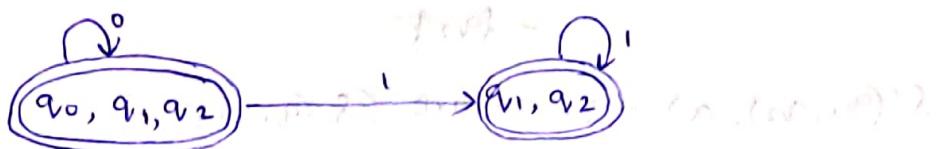
$$\delta((q_1, q_2), 0) = \epsilon\text{-closure}(\delta(q_1, q_2), 0)$$

$$\begin{aligned} &= \epsilon\text{-closure}(\delta(q_1, 0) \cup \delta(q_2, 0)) \\ &= \epsilon\text{-closure}(\emptyset \cup \emptyset) \\ &= \epsilon\text{-closure}(\emptyset) \end{aligned}$$

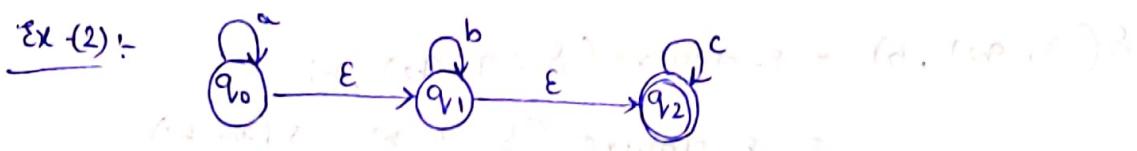
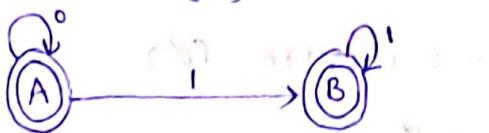
$$\delta((q_1, q_2), 1) = \epsilon\text{-closure}(\delta(q_1, q_2), 1)$$

$$\begin{aligned} &= \epsilon\text{-closure}(\delta(q_1, 1) \cup \delta(q_2, 1)) \\ &= \epsilon\text{-closure}(q_1 \cup q_2) \\ &= \epsilon\text{-closure}(q_1) \cup \epsilon\text{-closure}(q_2) \\ &= \{q_1, q_2\} \cup \{q_2\} \\ &= \{q_1, q_2\} \end{aligned}$$

step-3: Draw transition diagram for DFA



initial state can be (q0) or (q1, q2)



step 1: ϵ -closure of states

$$\epsilon\text{-closure}(q_0) = \{q_0, q_1, q_2\}$$

$$\epsilon\text{-closure}(q_1) = \{q_1, q_2\}$$

$$\epsilon\text{-closure}(q_2) = \{q_2\}$$

step 2: DFA transition table

	a	b	c
q_0, q_1, q_2			
q_1, q_2			
q_2			

$$\begin{aligned}\delta((q_0, q_1, q_2), a) &= \epsilon\text{-closure}(\delta(q_0, a_1, a_2), a) \\ &= \epsilon\text{-closure}(\delta(q_0, a) \cup \delta(q_1, a) \cup \delta(q_2, a)) \\ &= \epsilon\text{-closure}(q_0) \\ &= \{q_0, q_1, q_2\}\end{aligned}$$

$$\begin{aligned}\delta((q_0, q_1, q_2), b) &= \epsilon\text{-closure}(\delta(q_0, q_1, q_2), b) \\ &= \epsilon\text{-closure}(\delta(q_0, b) \cup \delta(q_1, b) \cup \delta(q_2, b)) \\ &= \epsilon\text{-closure}(\emptyset \cup q_1 \cup \emptyset) \\ &= \epsilon\text{-closure}(q_1) \\ &= \{q_1, q_2\}\end{aligned}$$

$$\begin{aligned}\delta((q_0, q_1, q_2), c) &= \epsilon\text{-closure}(\delta(q_0, q_1, q_2), c) \\ &= \epsilon\text{-closure}(\delta(q_0, c) \cup \delta(q_1, c) \cup \delta(q_2, c)) \\ &= \epsilon\text{-closure}(q_2) \\ &= \{q_2\}\end{aligned}$$

$$\begin{aligned}\delta((q_1, q_2), a) &= \epsilon\text{-closure}(\delta(q_1, q_2), a) \\ &= \epsilon\text{-closure}(\delta(q_1, a) \cup \delta(q_2, a)) \\ &= \epsilon\text{-closure}(\emptyset) \\ &= \emptyset\end{aligned}$$

$$\begin{aligned}\delta((q_1, q_2), b) &= \epsilon\text{-closure}(\delta(q_1, q_2), b) \\ &= \epsilon\text{-closure}(\delta(q_1, b) \cup \delta(q_2, b)) \\ &= \epsilon\text{-closure}(q_1) \\ &= \{q_1, q_2\}\end{aligned}$$

$$\begin{aligned}\delta((q_1, q_2), c) &= \epsilon\text{-closure}(\delta(q_1, q_2), c) \\ &= \epsilon\text{-closure}(\delta(q_1, c) \cup \delta(q_2, c)) \\ &= \epsilon\text{-closure}(q_2) \\ &= \{q_2\}\end{aligned}$$

$$\begin{aligned}\delta(q_2, a) &= \epsilon\text{-closure}(\delta(q_2, a)) \\ &= \epsilon\text{-closure}(\emptyset) \\ &= \emptyset\end{aligned}$$

$$\delta(q_2, b) = \epsilon\text{-closure}(\delta(q_2, b))$$

$$= \epsilon\text{-closure}(\emptyset)$$

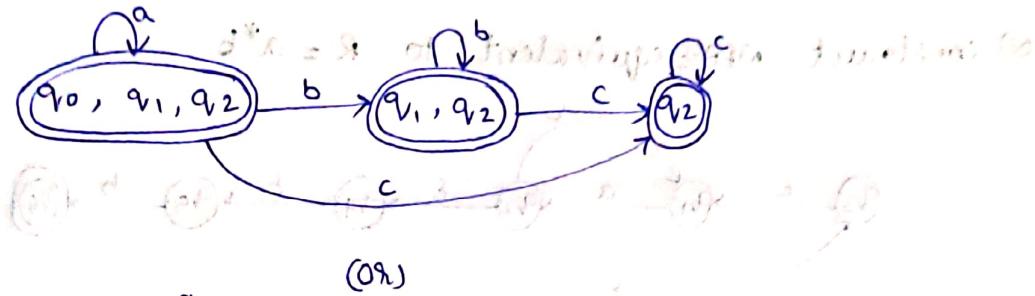
$$= \emptyset$$

$$\delta(q_2, c) = \epsilon\text{-closure}(\delta(q_2, c))$$

$$= \epsilon\text{-closure}(q_2)$$

$$= q_2$$

step 3: DFA transition diagram



27/09/2023

5.4 Regular Expression to NFA-E

(1) $RE = \epsilon$ (null string)

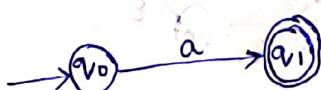
states can be changed without



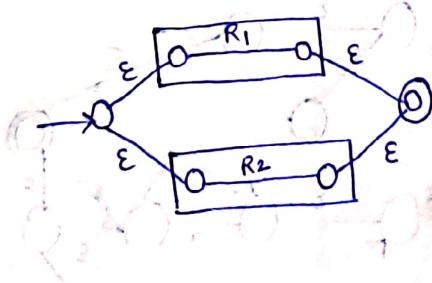
(2) $RE = \emptyset$ (empty set of strings)



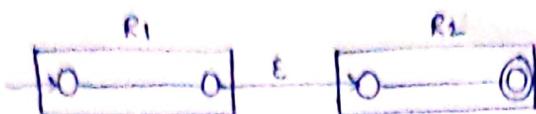
(3) $RE = a$



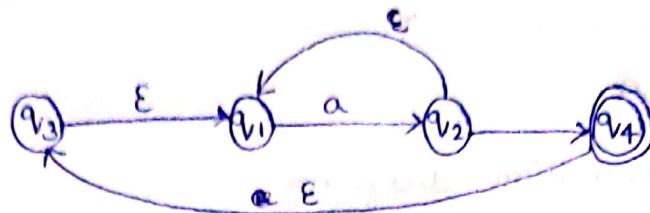
(4) union: $RE = R_1 + R_2$



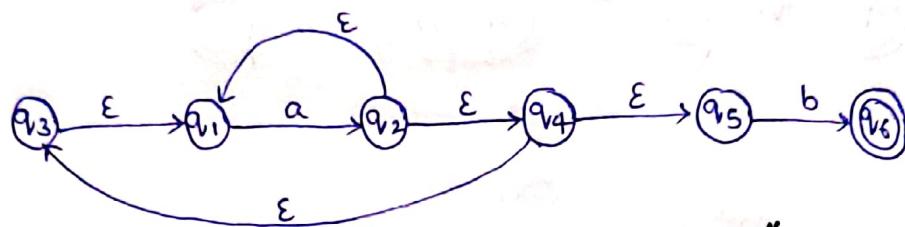
(5) concatenation: $RE = R_1 \cdot R_2$ (or) $R_1 R_2$



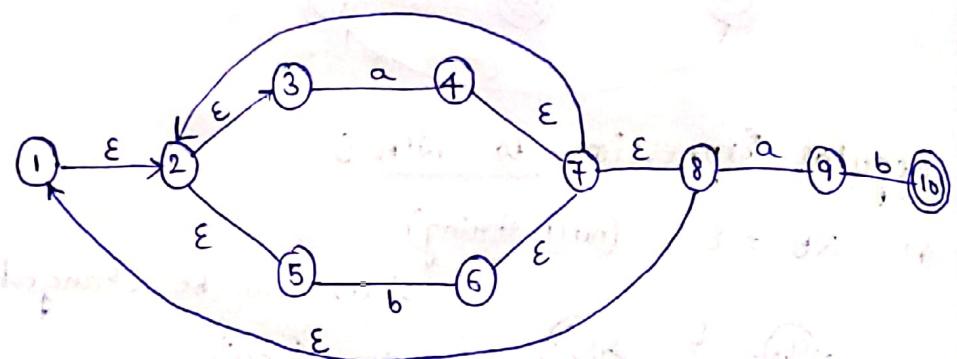
(6) closure: $RE = a^*$



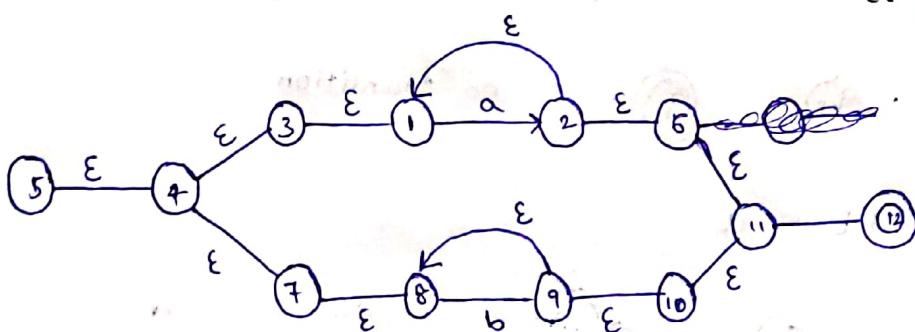
Q) construct NFA- ϵ equivalent to $R = a^*b$



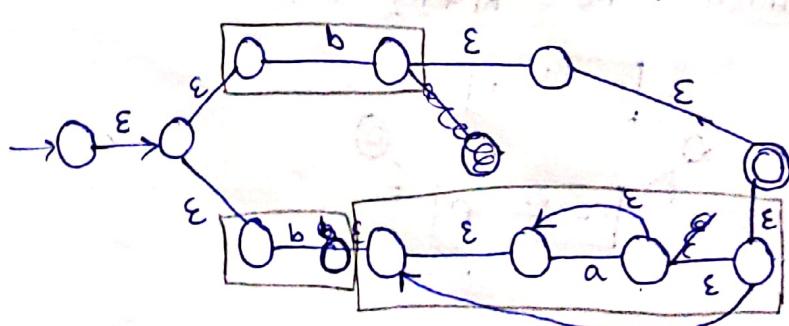
Q) construct NFA- ϵ equivalent to $R = (a+b)^* ab$



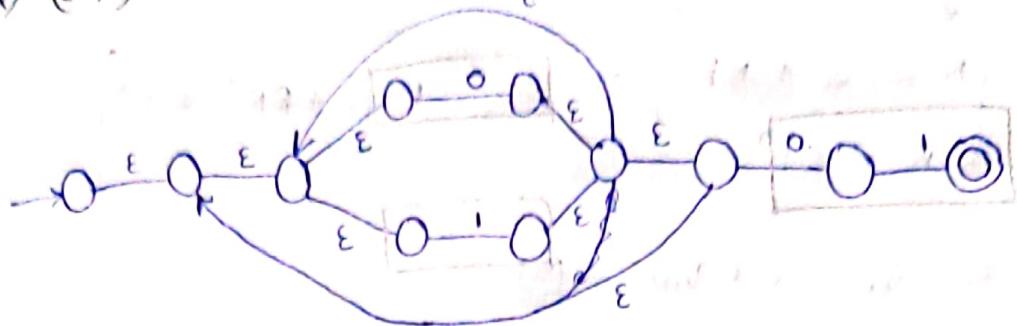
Q) construct NFA- ϵ equivalent to $R = a^* + b^*$ (or)
 $R = a^* | b^*$



Q) $RE = b + ba^*$



Q) $(0+1)^*$ 01



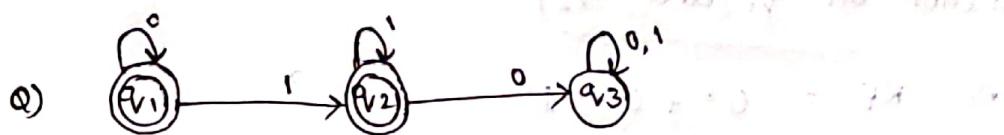
④ DFA to RE

Step i, for each state q_0, q_1, q_2 , identify all the states that comes into the state. and , write in equation format.

Step ii For initial state, add ϵ

Step iii : calculate all the equations.

Step iv : Result is the value of the final state.



(i) write "the eqns" for each state, individually by considering only incoming edges.

$$q_1 = q_1 0 + \epsilon \quad \text{--- 1} \quad q_1 \text{ is initial state}$$

$$q_2 = q_1 1 + q_2 1 \quad \text{--- 2}$$

$$q_3 = q_2 0 + q_3 0 + q_3 1 \quad \text{--- 3}$$

Now, simplify the eqns including final states.

If there are multiple final states then, apply union operation.

→ By using Arden's Theorem

$$\begin{aligned} R &= Q + RP \quad \text{--- (4)} \\ R &= QP^* \end{aligned}$$

$$\text{or (4) } \Rightarrow q_1 = \epsilon + q_1 0 \quad \text{--- (5)}$$

on comparing eq's (4), (5); we get

$$R = q_1, \quad Q = \epsilon, \quad RP = q_1 0$$

$$\therefore q_1 = 0^+$$

$$\text{or (2) } \Rightarrow q_2 = q_1 1 + q_2 1$$

$$\Rightarrow q_2 = 0^* 1 + q_2 1 \quad \text{--- (6)}$$

on comparing eq's (4), (6); we get

$$q_2 = 0^* 11^*$$

∴ Resultant Regular Expression is,

$$RE = q_1 + q_2$$

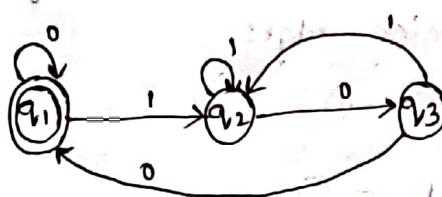
(∵ q_1 and q_2 are final states, we apply perform union operation on q_1 and q_2)

$$\Rightarrow RE = 0^* + 0^* 11^*$$

$$= 0^* (\epsilon + 11^*)$$

$$= 0^* 1^* \quad (\because \epsilon + 11^* = 1^*)$$

(Q)



$$\text{Q1} \Rightarrow q_1 = q_1 0 + q_3 0 + \epsilon \quad \text{--- (1)}$$

$$\text{Q2} \Rightarrow q_2 = q_2 1 + q_1 1 + q_3 1 \quad \text{--- (2)}$$

$$\text{Q3} \Rightarrow q_3 = q_2 0 \quad \text{--- (3)}$$

The above eqns cannot be simplified by using Arden's Theorem.

substitute eq(3) in eq(1)

$$\therefore \text{eq}(2) \Rightarrow q_2 = q_{2,1} + q_{2,1} + q_{2,01}$$
$$\Rightarrow q_2 = q_{2,1} + q_2 (1+01)$$
$$\left[R = Q + RP \right]$$
$$R = QP^*$$

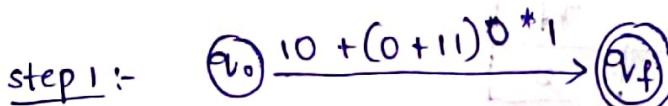
$$\Rightarrow q_2 = q_{2,1} (1+01)^* - \textcircled{4}$$

NOW, eq(3) $\Rightarrow q_3 = q_{3,1} (1+01)^* 0$ - $\textcircled{5}$

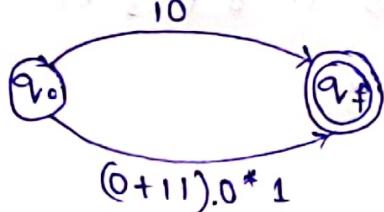
Then, eq(1) $\Rightarrow q_1 = q_{1,0} + q_{1,1} (1+01)^* 00 + \epsilon$

$$\Rightarrow q_{1,1} = (q_{1,1} (0 + 1 (1+01)^* 00)) + \epsilon$$
$$\Rightarrow q_{1,1} = \epsilon + q_{1,1} (0 + 1 (1+01)^* 00)$$
$$\left[R = Q + RP \right]$$
$$R = QP^*$$
$$\Rightarrow q_{1,1} = (0 + 1 (1+01)^* 00)^*$$

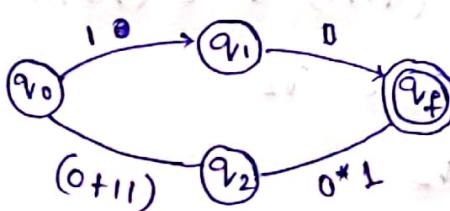
Q) Design DFA from the given RE: $10 + (0+11)0^{*1}$



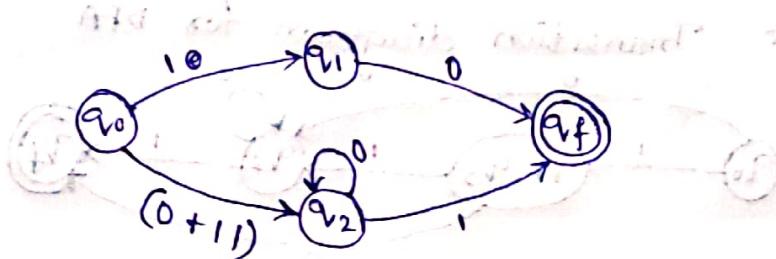
step 2 :-



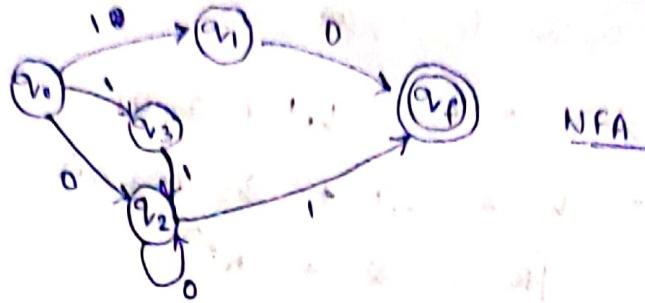
step 3 :-



step 4 :-



Step 5 :-



Step 6 :- Transition Table for NFA

	0	1
q_0	q_2, q_3	q_1, q_3
q_1	q_f	\emptyset
q_2	q_2	q_f
q_3	\emptyset	q_2

Step 7 :- Transition Table for DFA

	0	1
q_0	q_2	q_1, q_3
q_1, q_3	q_f	q_2
q_2	q_2	q_f
q_f	\emptyset	\emptyset

$$\delta((q_1, q_3), 0) = \delta(q_1, 0) \cup \delta(q_3, 0)$$

$$= q_f \cup \emptyset$$

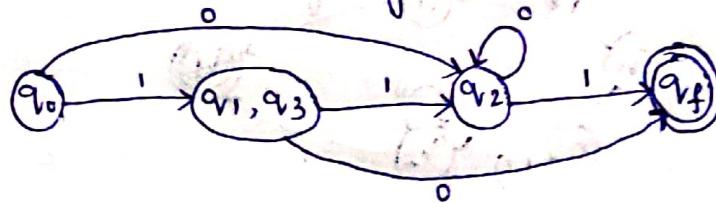
$$= q_f$$

$$\delta((q_1, q_3), 1) = \delta(q_1, 1) \cup \delta(q_3, 1)$$

$$= \emptyset \cup q_2$$

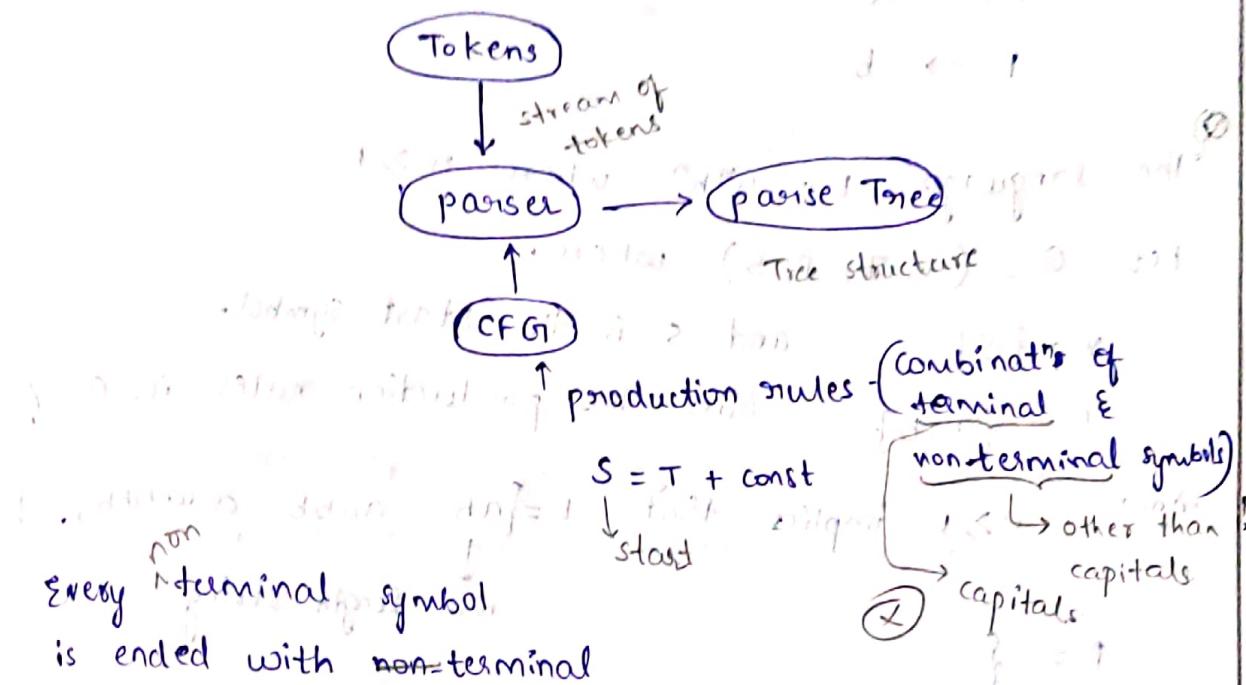
$$= q_2$$

Step 8 :- Transition diagram for DFA



Syntax Analysis

A parser or syntax analysis is a process which takes the input string w and produces either a parse tree (syntactic structure) or generates the syntactic errors.



$$\text{Ex: } a = b + 10$$

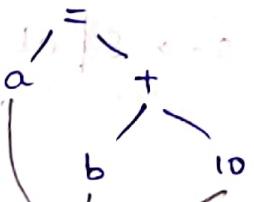
$$S \rightarrow T + \text{const}$$

$$T \rightarrow b$$

$$\text{const} \rightarrow 10$$

$$S \rightarrow a$$

Parse Tree



Parse Tree is generated by using terminal & non-terminal symbols.

Context Free Grammar (CFG)

The Context Free Grammar is a collection of the following :-

$$G = (V, T, P, S)$$

where, V : set of non-terminal symbols

T : set of terminal symbols (other than capitals)

S : start symbol

P : set of production rules

lexical analyzer
& syntax analyzer
work together

Ex: (S, V, T, P, S)

The production rules are given in the following form

Non-Terminal $\rightarrow (V \cup T)^*$

Ex: $E \rightarrow E+E \quad | \quad E * E \quad \stackrel{\text{non-ter}}{\approx} \quad E \rightarrow E+E$
 $E \rightarrow T \quad | \quad T * F$
 $T \rightarrow a$
 $F \rightarrow b$

Q)

The language $L = a^n b^n$ where $n \geq 1$

Let $G = (V, T, P, S)$ where,

$V = \{S\}$ and S is the start symbol.

$T = \{a, b\}$ Give the production rules i.e., $P = ?$

Ans: $n \geq 1$ implies that $L = \{ab, aabb, aaabbb, \dots\}$

\downarrow
min length string

$P = \{$

$S \rightarrow aSb \quad \because a \in b = ab$

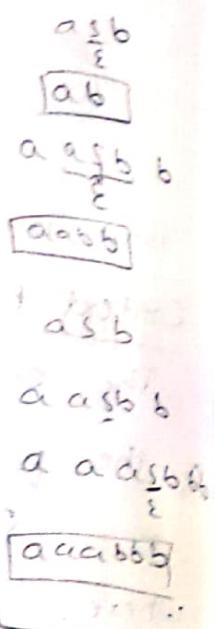
$S \rightarrow \epsilon \mid ab$ for only ab

$S \rightarrow \epsilon \mid aSb \mid$ for any no. of a's and b's

$\}$

Rules for writing CFG

- 1) A single non-terminal should be at LHS
- 2) The rule should be always in the form of $LHS \rightarrow RHS$ where, RHS may be the combination of terminal and non-terminal symbols and LHS is non-terminal symbol
- 3) The null derivation can be specified as non-terminal $\rightarrow \epsilon$
- 4) One of the non-terminals should be start symbol and conventionally, we should write the rules for these non-terminal symbols.



Q) write a CFG for while statement in C language.

Ans: $P = \{ S \rightarrow \text{while (condition) Stmt L} \mid S \}$

$\text{condition} \rightarrow \text{id } \text{relOp id}$

$\text{relOp} \rightarrow > \mid >= \mid < \mid <= \mid != \mid ==$

$S \rightarrow \text{while (condition) Stmt L}$

$\text{Stmt L} \rightarrow \text{stmtL} \mid \text{stmtL }$

$V = \{ S, \text{condition, relOp, Stmt L} \}$

$T = \{ \text{while, (,), <, >, <=, >=, !=, == } \}$

Q) what is the string generated by CFG $A \rightarrow (A) A$
Every nonterminal symbol should be ended with the terminal symbol.

Here, A is not ending with terminal symbol.

As there is no terminal symbol generation by the given CFG, we cannot derive any string from it.

$A \rightarrow (A) A$

$A \rightarrow () A$

$A \rightarrow () \mid E$

Possible strings are

take, $A \rightarrow (A) A$

$A \rightarrow (E) E$

$A \rightarrow ()$

Derivation and Parse Trees

Derivation from S means; generation of string w from S.

For constructing derivation, two rules are important.

(1) Choice of non-terminal from several others

(2) Choice of rule from production rules for corresponding non-terminal.

Derivation can be of two types

1) Left most derivation (LMD) Replace non-terminal with terminal from left side

2) Right most derivation (RMD) Replace terminal with non-terminal from right most side

Parsing:

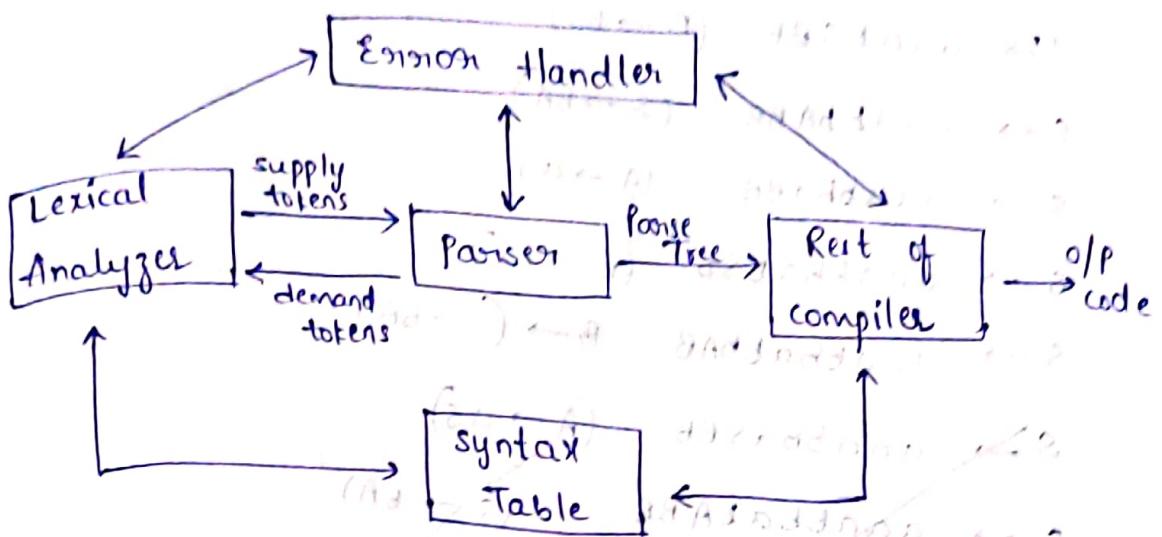
The syntax Analyzer is the second phase in compilation. The syntax analyzer (parser) basically checks for the syntax of language.

Ex: $a = b + 10$ to find the grammar tree of A.

This statement is first given to lexical analyzer. It will divide into group of tokens. Syntax analyzer takes the tokens as input and generates a tree like structure called parse tree.

Role of Parser

In the process of compilation, the parser and LA work together. That means; when parser requires stream of tokens, it invokes lexical analyzer. In return, the lexical analyzer supplies tokens to syntax analyzer.



The parser collects sufficient no. of tokens and builds a parse tree. Thus by building the parse tree, parser finds the syntactical error if any. It is also necessary that, the parser should recover from commonly occurring errors, so that remaining task of process the ifp can be continued.

Why Lexical analyzer and Syntax analyzer are separated out?

- It speeds up the process of compilation
- The errors in the source input can be identified precisely (correctly).

04/10/2023

Q) Let G be context free Grammar for which the production rules are given as below.

$$S \rightarrow aB \mid bA$$

$$A \rightarrow a \mid aS \mid bAA$$

$$B \rightarrow b \mid bS \mid aBB$$

Derive the string $aaabbabba$ using above grammar.

Ans

$$w = aaabbabba$$

$$S \rightarrow aB$$

$$S \rightarrow aABB$$

$$S \rightarrow aaABB$$

$$S \rightarrow aaabBB$$

$S \rightarrow aaabsBB$ ($B \rightarrow bs$)
 $S \rightarrow aaabbABBB$ ($S \rightarrow bA$)
 $S \rightarrow aaabbbaBB$ ($A \rightarrow a$)
 ~~$S \rightarrow aaabbabBSB$ ($B \rightarrow bs$)~~
 ~~$S \rightarrow aaabbabbAB$ ($B \rightarrow (S \rightarrow bA)$)~~
 $S \rightarrow aaabbasBB$ ($A \rightarrow as$)
 ~~$S \rightarrow aaabbabABBB$ ($S \rightarrow bA$)~~
 ~~$S \rightarrow aaabbabb$ ($A \rightarrow bAA$)~~

LMD

$S \rightarrow aB$
 $S \rightarrow aaBB$ ($B \rightarrow aBB$)
 $S \rightarrow aaABBB$ ($B \rightarrow aBB$)
 $S \rightarrow aaabBB$ ($B \rightarrow b$)
 $S \rightarrow aaabbB$ ($B \rightarrow b$)
 $S \rightarrow aaabbaBB$ ($B \rightarrow aBB$)
 $S \rightarrow aaabbabB$ ($B \rightarrow b$)
 $S \rightarrow aaabbabbs$ ($B \rightarrow bs$)
 $S \rightarrow aaabbabbA$ ($S \rightarrow bA$)
 $S \rightarrow aaabbabbba$ ($A \rightarrow a$)

RMD

$S \rightarrow aB$

$S \rightarrow aABB$ ($B \rightarrow aBB$)

~~$S \rightarrow aaABBB$ ($B \rightarrow aBB$)~~

$S \rightarrow aABbs$ ($B \rightarrow bs$)

$S \rightarrow aABbbA$ ($S \rightarrow bA$)

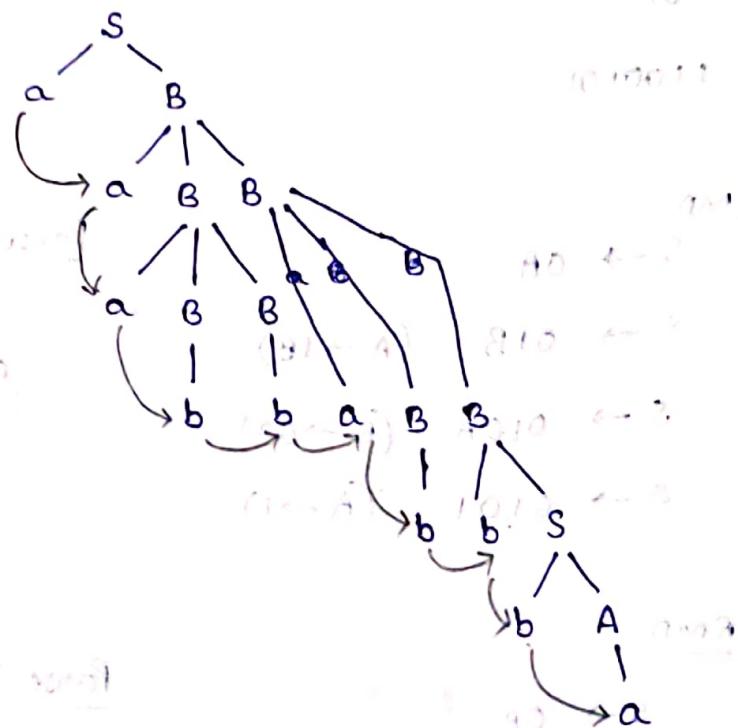
$S \rightarrow aABbbba$ ($A \rightarrow a$)

~~$S \rightarrow aaABbbba$ ($B \rightarrow aBB$)~~

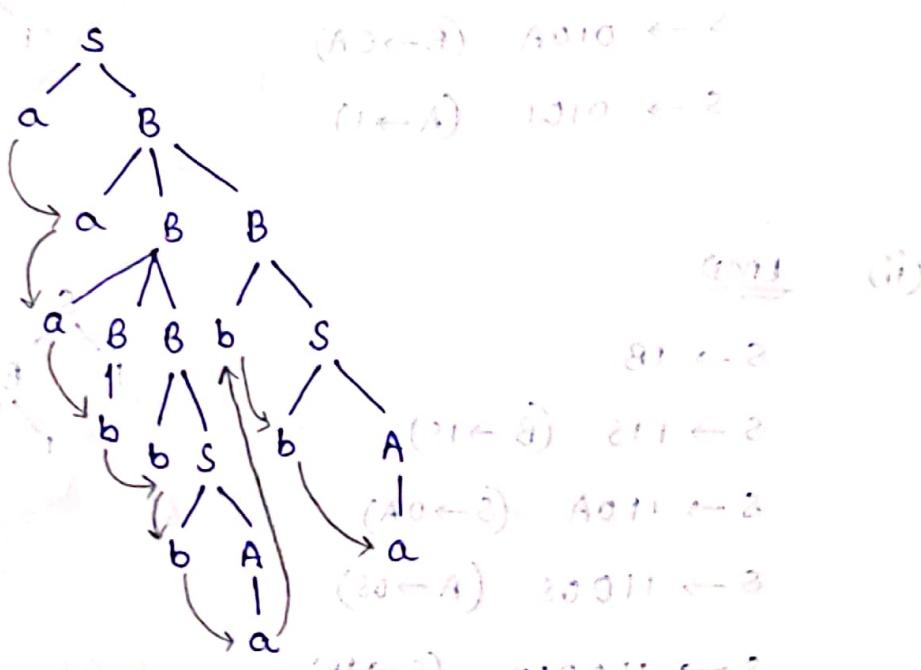
$S \rightarrow aaABbbba$ ($B \rightarrow b$)

$s \rightarrow aaabSbbA$ ($B \rightarrow bS$)
 $s \rightarrow aaabbAbba$ ($S \rightarrow bA$)
 $s \rightarrow aaabbabbba$ ($A \rightarrow a$)

Parse Tree for LMD



Parse Tree for RMB



$$Q) \quad S \rightarrow 0A \mid 1B \mid 0 \mid 1$$

$$A \rightarrow 0S \mid 1B \mid 1$$

$$B \rightarrow 0A \mid 1S$$

(ii) 0101

(iii) 1100101

Ans

(i) LMD $S \rightarrow 0A$

$$S \rightarrow 01B \quad (A \rightarrow 1B)$$

$$S \rightarrow 010A \quad (B \rightarrow 0A)$$

$$S \rightarrow 0101 \quad (A \rightarrow 1)$$

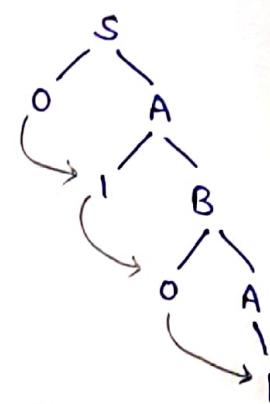
RMD $S \rightarrow 0A$

$$S \rightarrow 01B \quad (A \rightarrow 1B)$$

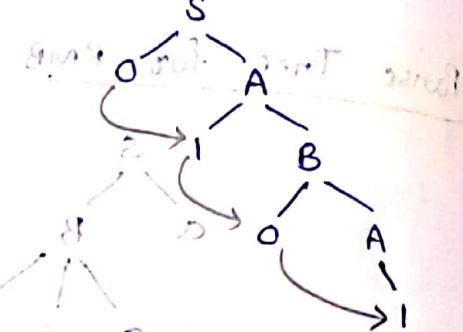
$$S \rightarrow 010A \quad (B \rightarrow 0A)$$

$$S \rightarrow 0101 \quad (A \rightarrow 1)$$

Parse Tree



Parse Tree



(ii) LMD

$$S \rightarrow 1B$$

$$S \rightarrow 11S \quad (B \rightarrow 1S)$$

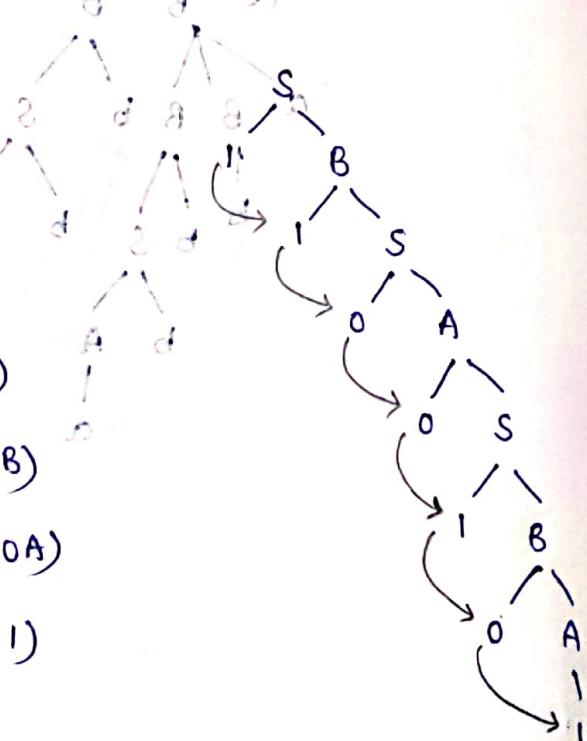
$$S \rightarrow 110A \quad (S \rightarrow 0A)$$

$$S \rightarrow 1100S \quad (A \rightarrow 0S)$$

$$S \rightarrow 11001B \quad (S \rightarrow 1B)$$

$$S \rightarrow 110010A \quad (B \rightarrow 0A)$$

$$S \rightarrow 1100101 \quad (A \rightarrow 1)$$



RMD

$S \rightarrow 1B$

$S \rightarrow 11S \quad (B \rightarrow 1S)$

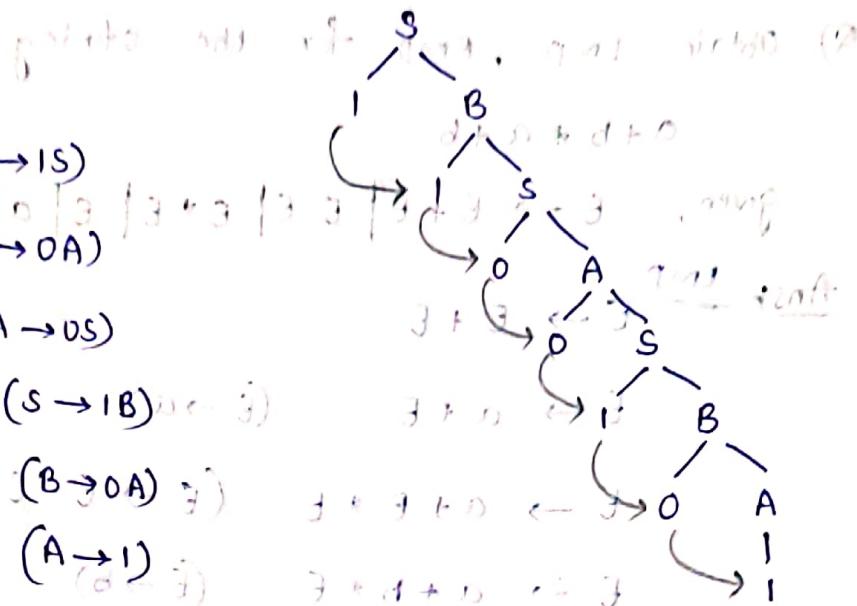
$S \rightarrow 110A \quad (S \rightarrow 0A)$

$S \rightarrow 1100S \quad (A \rightarrow 0S)$

$S \rightarrow 11001B \quad (S \rightarrow 1B) \quad (A \rightarrow 1)$

$S \rightarrow 110010A \quad (B \rightarrow 0A) \quad (A \rightarrow 0)$

$S \rightarrow 1100101 \quad (A \rightarrow 1) \quad (A \rightarrow 0) \quad (A \rightarrow 1)$



Q

consider the grammar $S \rightarrow 1d+0 \leftarrow 3$

$S \rightarrow (L) | (a \leftarrow 3) \quad 3 + d + d + a \leftarrow 3$

$L \rightarrow L, S | S' \quad 3 + d + d + a \leftarrow 3$

(i) what are the terminals and non-terminals and start symbol

(ii) find the parse trees for the following sentences.

a (a) a (a)

(2) (a, (a, a))

(3) (a, ((a, a), (a, a)))

(iii) construct LMD and RMD

(iv) what languages does the grammar generate.

Ans (iv) This grammar generates the strings with well-formedness of parentheses.

(i) Terminal symbols $\{1, 0, +, 3, (\},)\}$

$$T = \{(1, 0, +, 3), (\},)\} \quad 1 + 0 + + 3 \leftarrow 3$$

Non-terminal symbols $\{L, S\} \quad 1 + 0 + + 3 \leftarrow 3$

$$N = \{L, S\} \quad 1 + 0 + + 3 \leftarrow 3$$

start symbol $\neq S \quad 1 + 0 + + 3 \leftarrow 3$

$$S = S \rightarrow (L) | a$$

Q) Obtain LMD, RMD for the string

$$a+b+a+b$$

given, $E \rightarrow E+E | E-E | E * E | E | a | b$

Ans^{LMD} $E \rightarrow E+E$

$$E \rightarrow a+E$$

$$(E \rightarrow a)^{n-2} a 1 0 0 1 1$$

$$E \rightarrow a+E * E$$

$$(E \xrightarrow{*} E^* E)^{n-1} 0 1 0 0 1 1$$

$$E \rightarrow a+b * E$$

$$(E \xrightarrow{*} b)^{n-1} 1 0 1 0 0 1 1$$

$$E \rightarrow a+b * E + E$$

$$(E \rightarrow E+E)^{n-1} 1 0 1 0 0 1 1$$

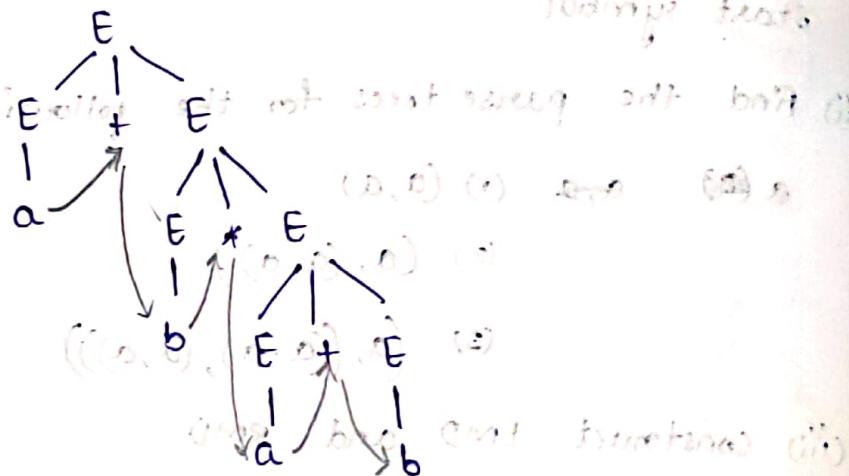
$$E \rightarrow a+b * a+E$$

$$(E \rightarrow a)^{n-1} 1 0 1 0 0 1 1$$

$$E \rightarrow a+b * a+b$$

$$(E \rightarrow b)^{n-1} 1 0 1 0 0 1 1$$

Parse Tree



RMD

$$E \rightarrow E+E \quad \text{with starting symbol } E$$

$$E \rightarrow E+b \quad (E \rightarrow b) \text{ starting with } b$$

$$E \rightarrow E * E + b \quad (E \rightarrow E * E) \text{ starting with } E$$

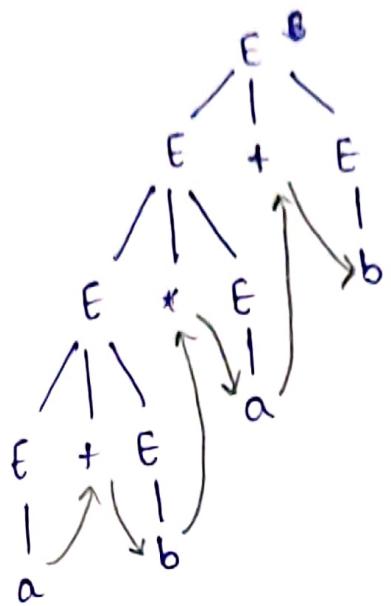
$$E \rightarrow E * a + b \quad (E \rightarrow a) \text{ starting with } a$$

$$E \rightarrow E + E * a + b \quad (E \rightarrow E+E) \text{ starting with } E$$

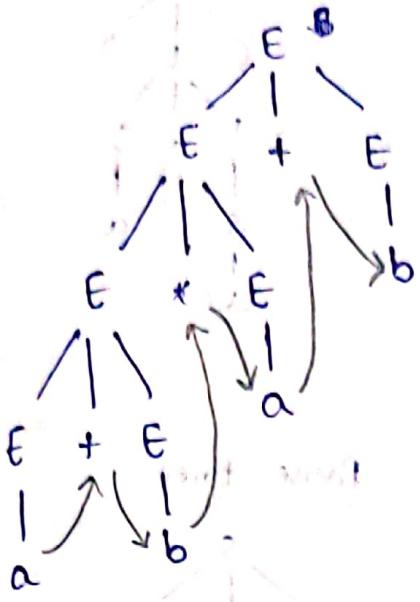
$$E \rightarrow E + b * a + b \quad (E \rightarrow b)$$

$$E \rightarrow a + b * a + b \quad (E \rightarrow a)$$

Parse Tree



Parse Tree



HW
so)
(ii), (iii)

ii) (a, a)

LMDT

- s → (L)
- s → (L, s)
- s → (s, s)
- s → (a, s)
- s → (a, a)

Parse tree :



- (a, b) → (a, b) ← a
 (a, b) → (a, b) ← b
 (a, b) → (a, b) ← a
 (a, b) → (a, b) ← b
 ((a, b), a) ← a
 ((a, b), b) ← b

((a, b), a) ← b

→ (a, b)

(a, b)

(a, b) → (a, b) ← a

((a, b), a) → a
 ((a, b), b) → b

((a, b), a) ← a

((a, b), b) ← b

(a, b) → (a, b) ← a
 ((a, b), a) → a

(a, b) → (a, b) ← b
 ((a, b), b) → b

→ (a, b)

(a, b)

(a, b) → (a, b) ← a
 ((a, b), a) → a

(a, b) → (a, b) ← b
 ((a, b), b) → b

(a, b) → (a, b) ← a
 ((a, b), a) → a

(a, b) → (a, b) ← b
 ((a, b), b) → b

(a, b) → (a, b) ← a
 ((a, b), a) → a

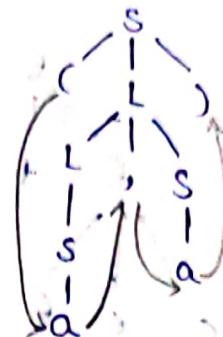
(a, b) → (a, b) ← b
 ((a, b), b) → b

(a, b) → (a, b) ← a
 ((a, b), a) → a

© RMDP

$s \rightarrow (L)$	
$s \rightarrow (L, s)$	$(L \rightarrow L, s)$
$s \rightarrow (L, a)$	$(s \rightarrow a)$
$s \rightarrow (s, a)$	$(L \rightarrow s)$
$s \rightarrow (a, a)$	$(s \rightarrow a)$

Syntax tree



$$2) (\alpha, \alpha, \alpha)$$

LMDL

$s \rightarrow (L)$

$s \rightarrow (L, s) \quad (L \rightarrow L, s)$

$s \rightarrow (s, s) \quad (L \rightarrow s)$

$s \rightarrow (a, s) \quad (s \rightarrow a)$

$s \rightarrow (a, (L)) \quad (s \rightarrow (L))$

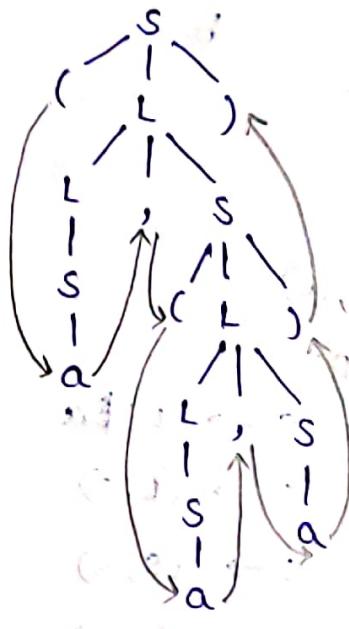
$s \rightarrow (a, (L, s)) \quad (L \rightarrow L, s)$

$s \rightarrow (a, (s, s)) \quad (L \rightarrow s)$

$s \rightarrow (a, (a, s)) \quad (s \rightarrow a)$

$s \rightarrow (a, (a, a)) \quad (s \rightarrow a)$

Parse tree



RMD :-

$s \rightarrow (L)$

$s \rightarrow (L, s) \quad (L \rightarrow L, s)$

$s \rightarrow (L, (L)) \quad (s \rightarrow (L))$

$s \rightarrow (L, (L, s)) \quad (L \rightarrow L, s)$

$s \rightarrow (L, (L, a)) \quad (s \rightarrow a)$

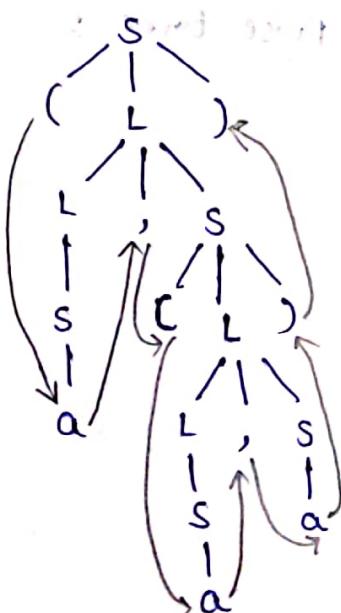
$s \rightarrow (L, (s, a)) \quad (L \rightarrow s)$

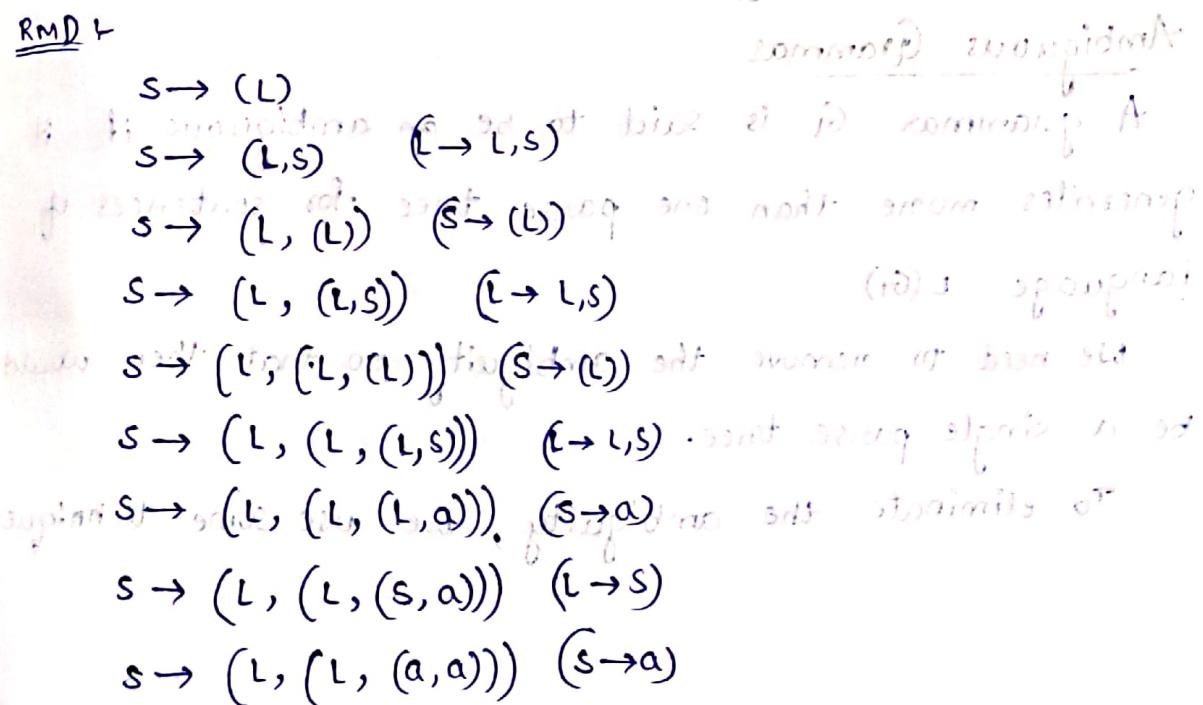
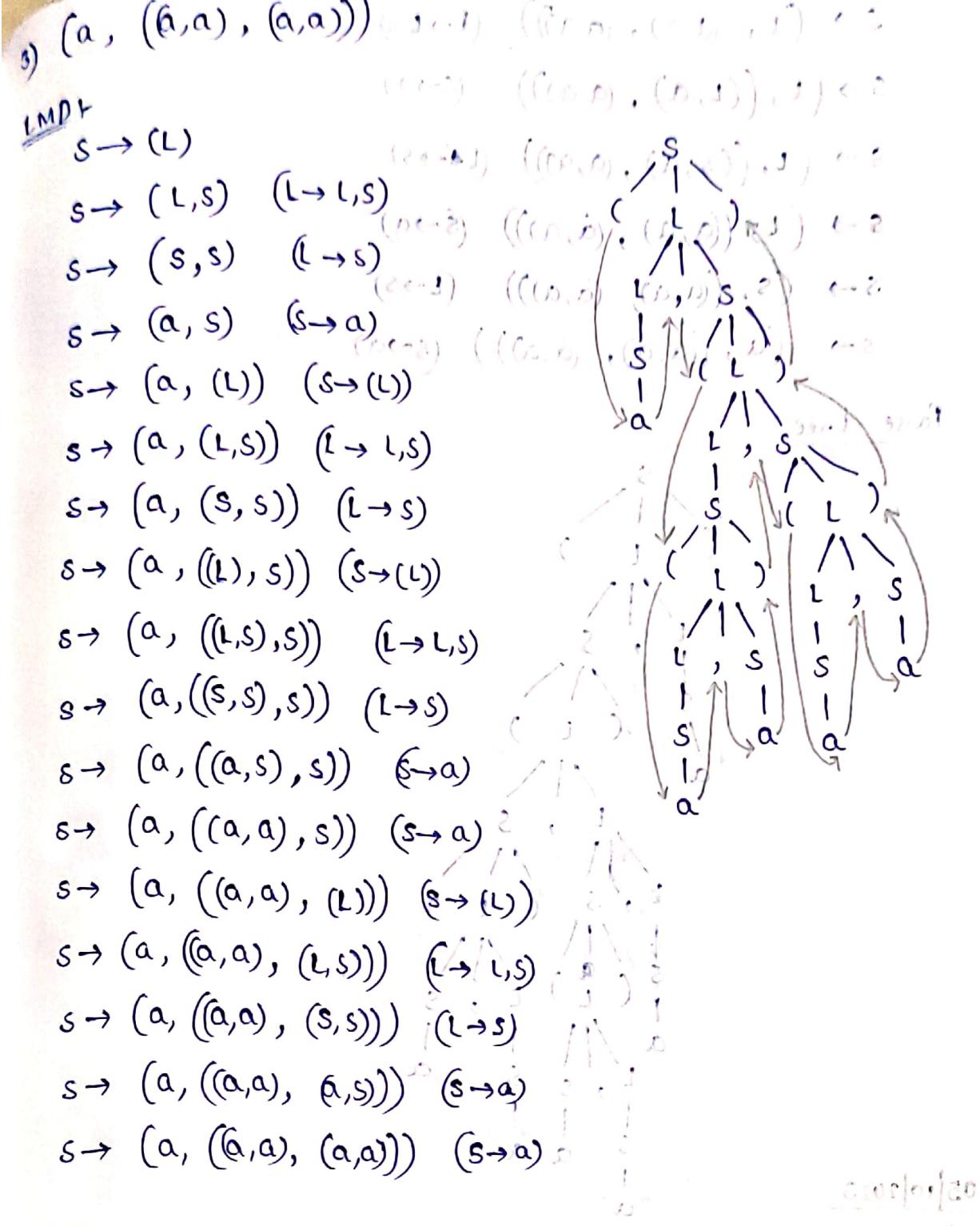
$s \rightarrow (L, (a, a)) \quad (s \rightarrow a)$

$s \rightarrow (s, (a, a)) \quad (L \rightarrow s)$

$s \rightarrow (a, (a, a)) \quad (s \rightarrow a)$

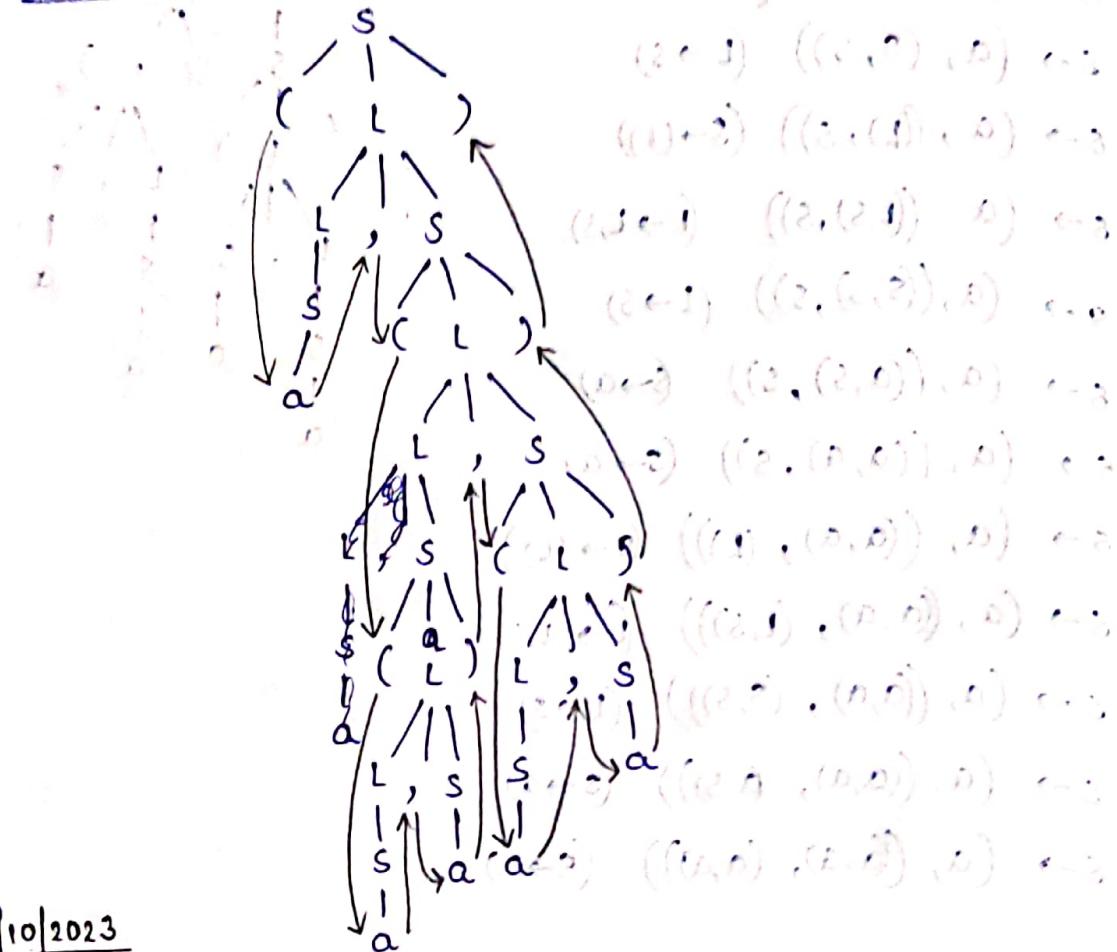
Parse tree





$s \rightarrow (L, ((L, s), (a, a))) \quad (L \rightarrow L, s)$
 $s \rightarrow (L, ((L, a), (a, a))) \quad (s \rightarrow a)$
 $s \rightarrow (L, ((s, a), (a, a))) \quad (L \rightarrow s)$
 $s \rightarrow (L, ((a, a), (a, a))) \quad (s \rightarrow a)$
 $s \rightarrow (s, ((a, a), (a, a))) \quad (L \rightarrow s)$
 $s \rightarrow (a, ((a, a), (a, a))) \quad (s \rightarrow a)$

Parse tree



05/10/2023

Ambiguous Grammar

A grammar G_1 is said to be ~~an~~ ambiguous if it generates more than one parse tree for sentences of language $L(G_1)$.

We need to remove the ambiguity so that there would be a single parse tree.

To eliminate the ambiguity, we use some techniques

$$Q) E \rightarrow E+E \mid E * E \mid (E) \mid id$$

$$(i) w = id + id + id$$

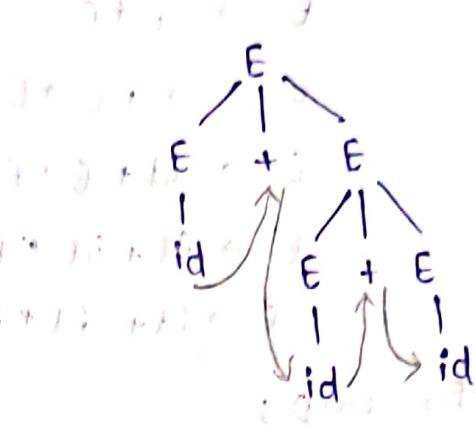
LMD $E \rightarrow E + E$

$$E \rightarrow id + E \quad (E \rightarrow id)$$

$$E \rightarrow id + E + E \quad (E \rightarrow E + E)$$

$$E \rightarrow id + id + E \quad (E \rightarrow id)$$

$$E \rightarrow id + id + id \quad (E \rightarrow id)$$



→ Met dengan selanjutnya ada yang salah

RMD $E \rightarrow E+E$

$$E \rightarrow E + id$$

$$E \rightarrow E + E + id$$

$$E \rightarrow E + id + id$$

$$E \rightarrow id + id + id$$

$$(ii) w = id + id * id$$

LMD

$$E \rightarrow E + E$$

$$E \rightarrow id + E$$

$$E \rightarrow id + E * E$$

$$E \rightarrow id + id * E$$

$$E \rightarrow id + id * id$$

met dengan \rightarrow E \rightarrow E \rightarrow E

met dengan \rightarrow E \rightarrow E \rightarrow E \rightarrow word



Parse Tree 1

RMD

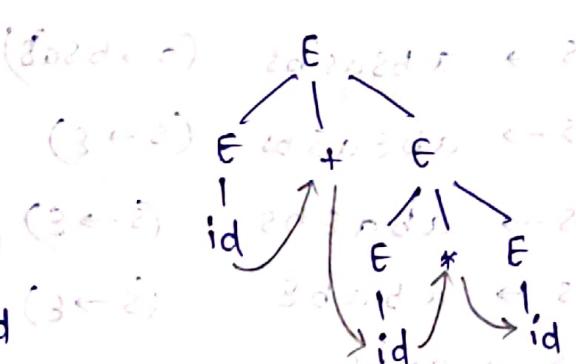
$$E \rightarrow E + E$$

$$E \rightarrow E + E * E$$

$$E \rightarrow E + E * id$$

$$E \rightarrow id + id * id$$

$$E \rightarrow id + id * id$$



LMDP

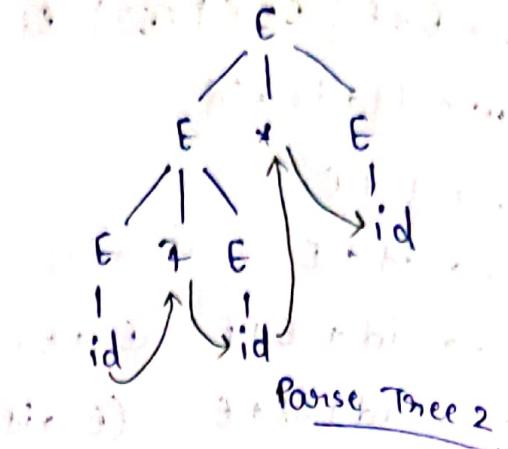
$$E \rightarrow E+E$$

$$E \rightarrow E+E * E$$

$$E \rightarrow id + E * E$$

$$E \rightarrow id + id * E$$

$$E \rightarrow id + id + id$$



for LMDP;

there are two possible parse trees.

$$\text{If } w = 2 + 3 * 5$$

$$\text{Parse Tree 1} : w = 2 + (3 * 5) \checkmark$$

$$\text{Parse Tree 2} : w = (2+3)*5 \times$$

\therefore Given grammar is ambiguous.

So, To eliminate this ambiguity \leftarrow

consider -> associativity

2) priority of operators

Q) Show that following grammar is ambiguous.

$$S \rightarrow aSbS$$

$$S \rightarrow bSaS$$

$$S \rightarrow \epsilon$$

$$S \rightarrow aSbS$$

$$S \rightarrow abSasbs \quad (S \rightarrow bSaS)$$

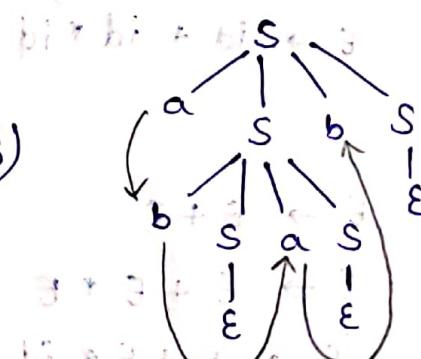
$$S \rightarrow ab\epsilon asbs \quad (S \rightarrow \epsilon)$$

$$S \rightarrow aba\epsilon bs \quad (S \rightarrow \epsilon)$$

$$S \rightarrow abab\epsilon \quad (S \rightarrow \epsilon)$$

$$S \rightarrow abab$$

$$w = abab$$



$s \rightarrow a s b s$

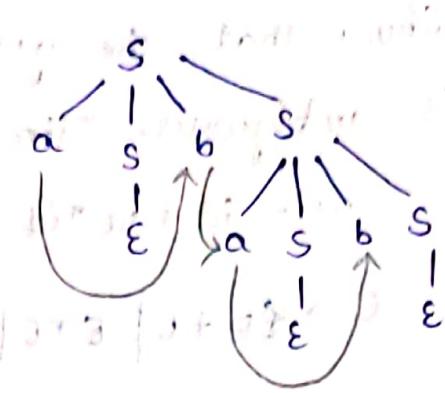
$s \rightarrow a \epsilon b s$

$s \rightarrow a b a s b s$

$s \rightarrow a b a \epsilon b s$

$s \rightarrow a b a b \epsilon$

$s \rightarrow a b a b$



Parse Tree 2

Thus, the given grammar is ambiguous.

Hence proved

Removal of Ambiguity

The ambiguity in the given grammar occurs due to use of single non-terminal more in multiple definitions on production rules.

If single non-terminal is being used repeatedly, then the ambiguity arises.

By introducing multiple non-terminals, the ambiguity can be removed.

For removing ambiguity of grammar, defining arithmetic expressions, we apply two rules.

- 1) If the grammar has left associative operators ($+, -, *, /$) then, apply Left Recursion.

Ex: $\underline{E} \rightarrow \underline{E} + T$ (Left recursive grammar)

- 2) If the grammar has right associative operator (\uparrow) (exponential operator) then, apply Right Recursion.

Ex: $\underline{E} \rightarrow T + \underline{E}$ (Right recursive production rule)

Q) Show that the grammar $E \rightarrow E+E | E^*E | (E) | id$ is ambiguous. Eliminate the ambiguity.

w/o $id + id * id \rightarrow$ left recursive $(id + id)^*$

$$E \rightarrow (E+E | E^*E | (E) | id)$$

$$E \rightarrow E+E$$

$$\Rightarrow E \rightarrow E+T | T$$

$$E \rightarrow E^*E$$

$$E \rightarrow T^*F$$

$$\Rightarrow E+T \rightarrow T^*F | F$$

$$\Rightarrow F \rightarrow (E) | id$$

Imp \Rightarrow all statements have significant parentheses

$$E \rightarrow E+T$$

$$E \rightarrow T + T$$

$$E \rightarrow F + T$$

$$E \rightarrow id + T^*F$$

$$E \rightarrow id + F^*F$$

$$(or E \rightarrow id + id * F)$$

$$E \rightarrow id + id * id$$

$$(also left recursive)$$

$$(also right recursive)$$

$$2 + (3 + 5)$$

$$2 + 15 \stackrel{①}{=} 17$$

RMP

$$E \rightarrow E + T$$

$$E \rightarrow E + F \quad T \leftarrow F$$

$$E \rightarrow E + T * id$$

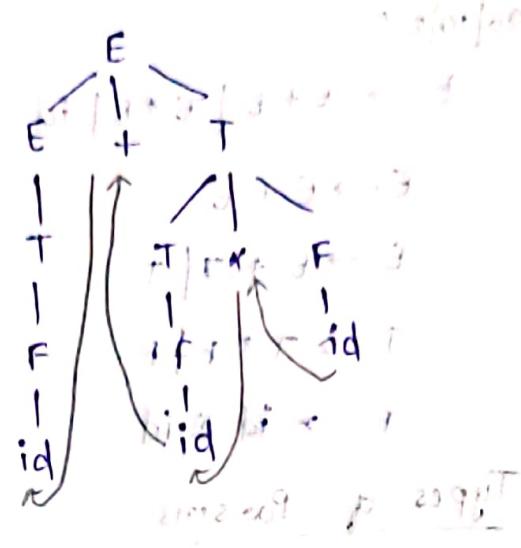
$$E \rightarrow E + F * id$$

$$E \rightarrow E + id * id$$

$$E \rightarrow T + id * id$$

$$E \rightarrow F + id * id$$

$$E \rightarrow id + id * id$$



Q) $bExp \rightarrow bExp \text{ OR } bExp$

question | $bExp \text{ AND } bExp$

| Not $bExp$

| True

| False

$bExp \rightarrow bExp \text{ OR } bExp$

~~$bExp \rightarrow T \text{ OR } bExp$~~

$bExp \rightarrow bExp \text{ OR } T \mid T$

? $T \rightarrow T \text{ OR } F \mid F$ and good enough condition

below $F \rightarrow F \text{ AND } G \mid G$ good enough of bExp's

$G \rightarrow \text{Not } H \mid H$

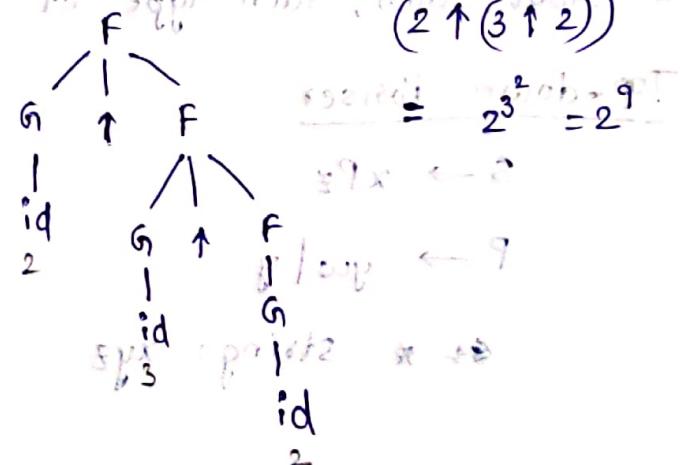
$H \rightarrow \text{True} \mid \text{False}$

so good condition, so good enough of H condition

Q) $2^{\uparrow} 3 \uparrow 2$ is good to $2^{(3 \uparrow 2)}$ or $(2 \uparrow (3 \uparrow 2))$?

$$F \rightarrow G \uparrow F \mid G$$

$$G \rightarrow id$$



06/10/2023

$$E \rightarrow E + E \mid E * E \mid id$$

$$E \rightarrow E + E$$

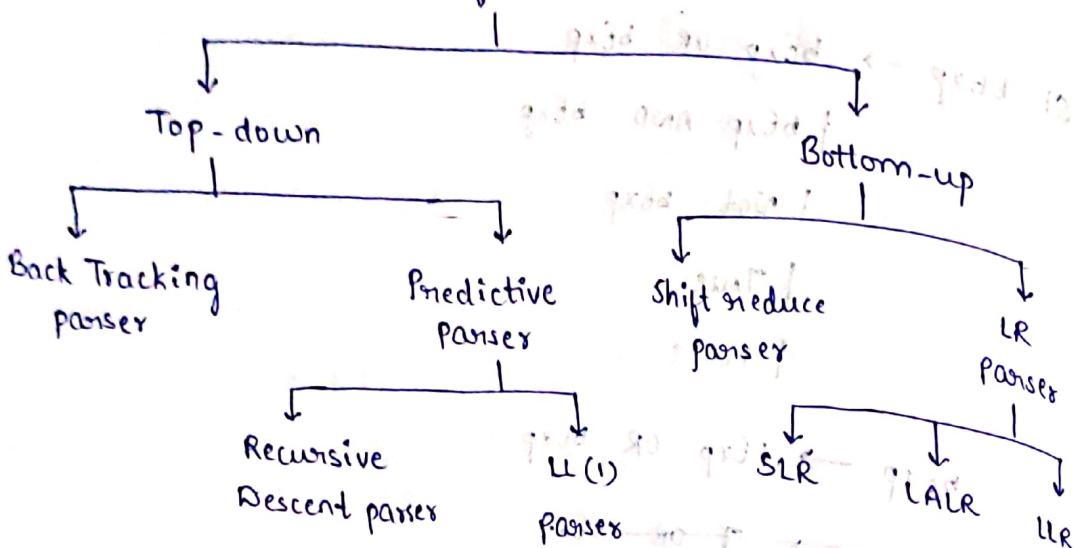
$$E \rightarrow E * E \mid T$$

$$T \rightarrow T + F \mid F$$

$$F \rightarrow M \mid id$$

Types of Parsers

Types of parsers



Top-down Parser

When parse tree can be constructed from root & expanded to leaves then, such type of parser is called Top-down parser.

Bottom-up Parser

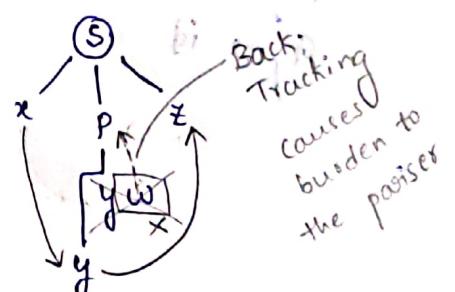
When the parse tree can be constructed from leaves to root then, such type of parser is called Bottom-up parser.

Top-down Parser

$$S \rightarrow xPz$$

$$P \rightarrow yw \mid y$$

e.g. string: xyz



Problems of Top-down Parser

- » Backtracking
- » Left Recursion
- » Left Factoring
- » Ambiguity

Left Recursion

case (i) : $A \rightarrow A\alpha | \beta$

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' | \epsilon$$

$$\begin{aligned} \text{Ex: } E &\rightarrow E + T | a \\ A &\rightarrow A\alpha \quad \beta \\ E &\rightarrow \alpha E' \\ E' &\rightarrow TE' | \epsilon \end{aligned}$$

$$\begin{aligned} \text{Q) } E &\rightarrow E + T | T \\ T &\rightarrow T^* F | F \\ F &\rightarrow (E) | id \end{aligned}$$

$$\text{Take, } E \rightarrow E + T | T$$

$$(A \rightarrow A\alpha | \beta \text{ then, } A \rightarrow \beta A')$$

eliminating left recursion

$$E' \rightarrow +TE' | \epsilon$$

Thus, left recursion is eliminated.

$$\text{Now, } T \rightarrow T^* F | F$$

$$(A \rightarrow A\alpha | \beta \text{ then, } A \rightarrow \beta A')$$

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' | \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' | \epsilon$$

$$\text{And, } F \rightarrow (E) | id$$

After removing left recursion,

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'| E$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' | \epsilon$$

$$F \rightarrow (E) | id.$$

Q) $S \rightarrow \underline{SOS1S} | 01$

$$(A \rightarrow A\alpha | \beta \text{ then } A \rightarrow PA', A' \rightarrow \alpha A' | \epsilon)$$

$$S \rightarrow 01S'$$

$$S' \rightarrow OS1SS' | \epsilon$$

Q) $S \rightarrow (L) | x$

$$L \rightarrow L, S | S$$

Take, $L \rightarrow \underline{L, S} | s$

$$(A \rightarrow A\alpha | \beta \text{ then } A \rightarrow PA', A' \rightarrow \alpha A' | \epsilon)$$

$$L \rightarrow SL'$$

$$L' \rightarrow ,SL' | \epsilon$$

After removing left recursion,

$$S \rightarrow (L) | x$$

$$L \rightarrow SL' \text{ (removing left recursion from } L \text{ with } S)$$

$$L' \rightarrow ,SL' | \epsilon$$

Q)

$$T \rightarrow F$$

$$F \rightarrow T | S \sim T$$

$$\beta((\beta) \leftarrow T \wedge \neg \beta)$$

case (ii): $A \rightarrow A\alpha_1 | A\alpha_2 \dots | B_1 | B_2$

for this $A \rightarrow B_1 A' | B_2 A' \dots$ & it makes tree in 10

$A' \rightarrow \alpha_1 A' | \alpha_2 A' \dots | \epsilon$

eliminating α_i & β_j of first part of tree

(i) $\text{expr} \rightarrow \text{expr} + \text{expr} | \text{expr} * \text{expr} | \text{id}$

for this $\text{id} \rightarrow \alpha_1 \text{id} | \alpha_2 \text{id} \dots$ & it makes tree in 10

$\text{expr} \rightarrow \text{id} \text{expr}' | \text{expr}' \dots$ & it makes tree in 10

$\text{expr}' \rightarrow + \text{expr}' | * \text{expr}' | \epsilon$

$\text{expr}' \rightarrow + \text{expr} | * \text{expr} | \epsilon$

10/10/2023

Consider the following grammar

$A \rightarrow ABB | Aa | a$ remove the left recursion.
 $B \rightarrow Be | d$

(i) $A \rightarrow \frac{ABb}{A \alpha} | a$ then $\frac{(ii) A \rightarrow Aa | a}{A \alpha} \dots$ then, $\frac{A \rightarrow \beta A'}{A \alpha} \dots$ then, $\frac{A \rightarrow a A'}{A \alpha} \dots$ then, $\frac{A \rightarrow \beta A'}{A \alpha} \dots$ then, $\frac{A \rightarrow \beta A'}{A \alpha} \dots$

$A \rightarrow a A'$

$A' \rightarrow Bb A' | \epsilon$

(ii) $B \rightarrow \frac{Bc}{A \times \beta} | d$ then, $A \rightarrow \beta A'$, $A' \rightarrow \alpha A' | \epsilon$

$B \rightarrow dB'$

$B' \rightarrow eB' | \epsilon$

\therefore The production rules after removing left recursion are:

$A \rightarrow a A'$

$A' \rightarrow a A' | Bb A' | \epsilon$

$B \rightarrow dB'$

$B' \rightarrow eB' | \epsilon$

$\alpha | A \alpha | \alpha A \alpha \rightarrow A \alpha$

$A \alpha \rightarrow A$

$\beta | A \beta | \beta A \beta \rightarrow A \beta$

Left Factoring

- (GT) is used when it is not clear that which of the two alternatives is used to expand the non-terminal.

If $A \rightarrow \alpha\beta_1 | \alpha\beta_2$ is a production, then it is not possible to take a decision whether to choose Rule 1 or Rule 2. In such situations, the above grammar can be left factored as:

$$A \rightarrow \alpha A' \quad \text{when } A \rightarrow \alpha\beta_1 | \alpha\beta_2 \text{ is given.}$$

$$A' \rightarrow \beta_1 | \beta_2$$

Ex:-

$$S \rightarrow iEts | iEtSeS | a$$

$$E \rightarrow b$$

take, $S \rightarrow \underline{iEts} | \underline{iEtSeS} | a$ then, $A \rightarrow \alpha A'$
 $A' \rightarrow \beta_1 | \beta_2$

$$S \rightarrow iEtSeS' | a$$

$$S' \rightarrow \epsilon | es$$

$$E \rightarrow b$$

- Q) Do left factoring in the following grammar

$$A \rightarrow aAB | aA | a$$

$$B \rightarrow BB | b$$

Ans:- (1) $A \rightarrow \underline{aAB} | \underline{aA} | a$

$$A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \alpha\beta_3$$

$$A \rightarrow aA'$$

$$A' \rightarrow AB | A | \epsilon$$

then, $A \rightarrow \alpha A'$
 $A' \rightarrow \beta_1 | \beta_2 | \beta_3$

$$S \rightarrow AB | A | \epsilon$$

(ii) $B \rightarrow bB$ | b , if $b \in \text{First}(A)$ then, $A \rightarrow \alpha A'$
 $A \rightarrow \alpha_1 B_1 | \alpha_2 B_2$ and $\alpha_1 \in \text{First}(A')$
 $B \rightarrow bB$ | b , if $b \in \text{First}(A)$ then, $A \rightarrow \alpha_1 B_1 | \alpha_2 B_2$ and $\alpha_1 \in \text{First}(A')$

$B \rightarrow B' | E$, if $E \in \text{First}(A)$ then, $A \rightarrow \alpha_1 B_1 | \alpha_2 B_2$ and $\alpha_1 \in \text{First}(A')$

* Predictive LL(1) parser

" For LL(1) parser, it is a parser that uses single lookahead symbol to predict the next symbol in the input string."

" the first L means that, the input is scanned from left to right."

" the second L means that, it uses left most derivation."

" for input strings, necessary left most derivation is used."

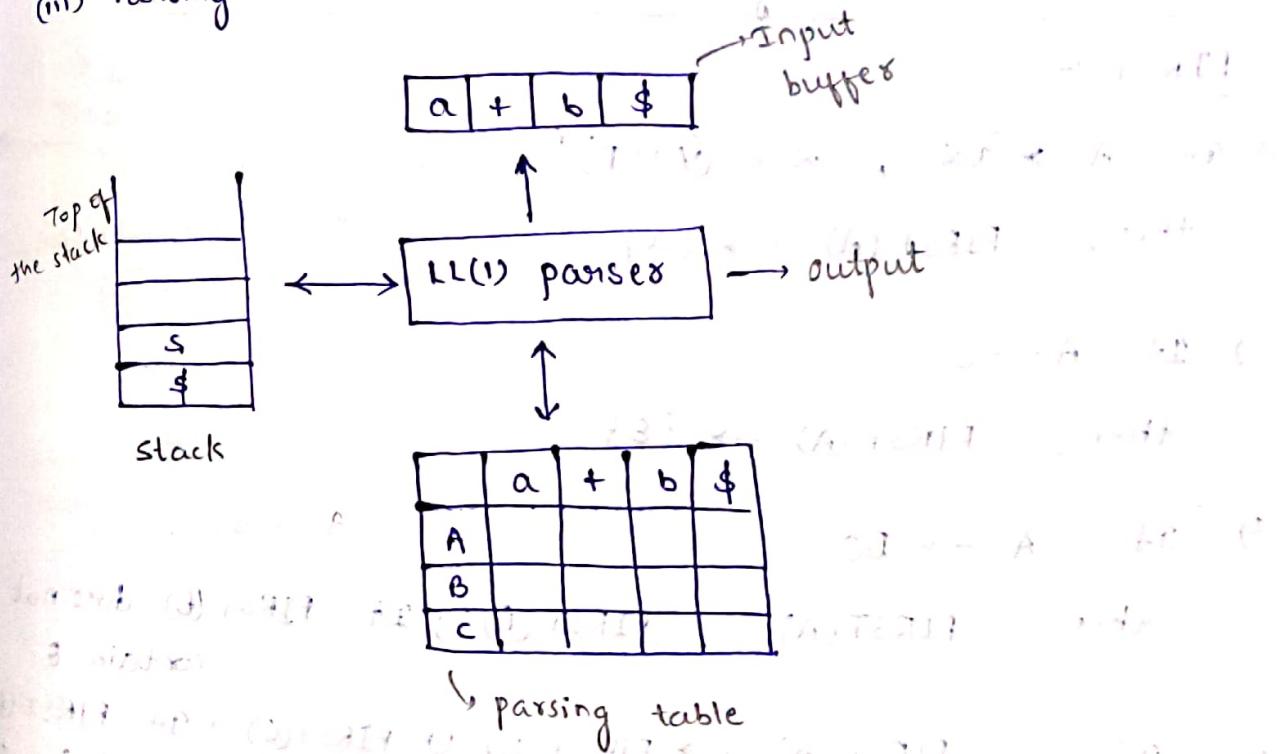
" the number 1 in the input string means that, it uses only 1 input symbol (lookahead symbol) to predict the parsing process."

" The data structures used by LL(1) parser are:

(i) Input buffer

(ii) Stack

(iii) Parsing table



- » LL(0) parser uses input buffer to store the input tokens.
- \$ indicates that, it is the end of the string.
- » Stack is used to hold the left sentential form. The symbols in the RHS of the rule, are pushed into the stack in reverse order.
- » Parsing table is a 2-D array. It has rows for the non-terminal symbols and columns for terminal symbols.

Construction of Predictive LL(1) Parser

For the construction of this parser, we need to follow the steps given below:

- 1) Computation of FIRST & FOLLOW functions
- 2) Construct the predictive parsing table using the FIRST & FOLLOW functions.
- 3) Parse the input string with the help of predictive parsing table

Rules for constructing FIRST & FOLLOW functions

FIRST :- [it is found for symbols that are on the LHS of Production rule]

1) If $A \rightarrow a\alpha$, $\alpha \in (V \cup T)^*$, Ex: $A \rightarrow aBAC$

then, $\text{FIRST}(A) \rightarrow \{a\}$

2) If $A \rightarrow \epsilon$

then, $\text{FIRST}(A) \rightarrow \{\epsilon\}$

3) If $A \rightarrow BC$

then, $\text{FIRST}(A) \rightarrow \text{FIRST}(B)$; If $\text{FIRST}(B)$ does not contain ϵ

4) ~~If~~ $\text{FIRST}(A) \rightarrow \text{FIRST}(B) \cup \text{FIRST}(C)$; If $\text{FIRST}(B)$ contains ϵ

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z

terminal combination of terminals & non-terminals



all are non-terminal symbols

$A \rightarrow \overbrace{BC}$

FOLLOW :- { it is found for symbols that are on the RHS of Production rule }

1) If 'S' is a starting symbol

then, FOLLOW(S) = { \$ }

2) If $A \rightarrow \alpha B \beta$

then, FOLLOW(B) = FIRST(β) ; if FIRST(β) doesn't contain ϵ

3) If $A \rightarrow \alpha B$

then, FOLLOW(B) \rightarrow FOLLOW(A)
 \hookrightarrow Here, B should be the last symbol.

4) If $A \rightarrow \alpha B \beta$ where $\beta \rightarrow \epsilon$ then, B becomes the last symbol.
then, FOLLOW(B) \rightarrow FOLLOW(A)

- FOLLOW :- [it is found for symbols that are on the RHS of production rule]
- 1) If 'S' is a starting symbol
then, FOLLOW(S) = { \$ } FOLLOW never contains ϵ
 - 2) If $A \rightarrow \alpha B \beta$
then, FOLLOW(B) = FIRST(β) ; if FIRST(β) doesn't contain ϵ
 - 3) If $A \rightarrow \alpha B$ \hookrightarrow Here, B should be the last symbol
then, FOLLOW(B) \rightarrow FOLLOW(A)
 - 4) If $A \rightarrow \alpha B \beta$ where $\beta \rightarrow \epsilon$ then, B becomes the last symbol.
then, FOLLOW(B) \rightarrow FOLLOW(A)

11/10/2023
Consider the following grammar. (Remove-left recursion and left factoring and construct LL(1) parsing table.)

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T * F \mid F \\ AF &\rightarrow (E) \mid id \end{aligned}$$

After removing left recursion :-
given; $E \rightarrow E + T \mid T$

$$\begin{aligned} E &\rightarrow \cdot TE' \\ E' &\rightarrow +TE' \mid \epsilon \\ T &\rightarrow FT' \\ T' &\rightarrow *FT' \mid \epsilon \\ F &\rightarrow (E) \mid id \end{aligned}$$

1) FIRST & FOLLOW functions

$$FIRST(E) \rightarrow FIRST(\underline{E'})$$

$$FIRST(T) \rightarrow FIRST(\underline{FT'})$$

$$FIRST(F) \rightarrow FIRST(\underline{(E)}) \cup FIRST(id) = \{ C, id \}$$

$$\text{FIRST}(E) = \text{FIRST}(T) = \text{FIRST}(F) = \{ C, \text{id} \}$$

Now,

$$\begin{aligned}\text{FIRST}(E') &= \text{FIRST}(+TE') \cup \text{FIRST}(E) \\ &= \{ +, \epsilon \}\end{aligned}$$

Now, $\text{FIRST}(T) = \{ C, \text{id} \}$

$$\text{FIRST}(T') \rightarrow \text{FIRST}(FT') \cup \text{FIRST}(E)$$

$$= \{ *, \epsilon \}$$

$$\text{FIRST}(F) = \{ C, \text{id} \}$$

$\text{FOLLOW}(E) = \{ \$,) \}$ ($\because E$ is the starting symbol)

$\text{FOLLOW}(E) = \text{FIRST}(T) \cup \text{Follow}(E')$

$$\text{Follow}(E') = \text{Follow}(E) = \{ \$,) \}$$

$$\text{Follow}(T) = \text{First}(E') = \{ +, \epsilon \}$$

But, Follow should not contain ϵ .
 $\text{Follow}(T) = \text{Follow}(E) = \{ +, \$,) \}$

$$\text{Follow}(T') = \text{Follow}(T)$$

$$= \{ +, \$,) \}$$

$$\text{Follow}(F) = \text{First}(T') = \{ *, \epsilon \}$$

$$\text{Follow}(F) = \text{Follow}(T) = \{ +, \$,) \}$$

$$(3) T2213 \leftarrow (3) T2211$$

$$(T) T2217 \leftarrow (T) T2211$$

$$\{ b, d \} = (b) T2211 \cup ((b) T2211 \leftarrow (T) T2211)$$

Constructing the parsing table

	+	*	()	id	\$	+	*	()	id	\$	+	*	()
E																
E'	$E' \rightarrow TE'$		$T \leftarrow T'$	$E' \rightarrow E$			$E' \rightarrow E$									
T			$T \rightarrow FT'$		$T \rightarrow FT'$											
T'			$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$											
F			$F \rightarrow (E)$		$F \rightarrow id$											

To construct the parsing table, following rules are used.

1) $M[A, a] = A \rightarrow \alpha$, if a is in FIRST(α)

2) $M[A, b] = A \rightarrow \alpha$, if ϵ is in FIRST(α)
 b is in FOLLOW(A)

3) Parsing the input string

$$w = id * id + id$$

stack	input	output
$\$ E$	<u>id</u> * id + id \$	$d / s / * \leftarrow \epsilon$
$\$ E' T$	<u>id</u> * id + id \$	$E \rightarrow TE'$
$\$ E' T' F$	<u>id</u> * id + id \$	$T \rightarrow FT'$
$\$ E' T' id$	<u>id</u> * id + id \$	$F \rightarrow id$
$\$ E' T'$	* id + id \$	
$\$ E' T' F *$	* id + id \$	$T' \rightarrow *FT'$
$\$ E' T' F$	id + id \$	
$\$ E' T' id$	id + id \$	$T \rightarrow FT' F \rightarrow id$
$\$ E' T'$	+ id \$	
$\$ E'$	+ id \$	$T' \rightarrow \epsilon$
$\$ E' T$	+ id \$	$E' \rightarrow +TE'$

$\$ E' T$	$id \notin S$	reject parsing off prefix error
$\$ E' T' F$	$id \in S$	$T \rightarrow FT'$
$\$ E' T' id$	$id \in S$	$F \rightarrow id$
$\$ E' T'$	$\$$	$T' \rightarrow E$
$\$ E'$	$\$$	
$\underline{\$}$	<u>$\\$</u>	$E' \xrightarrow{*} \$$

E

T

E'

$(\beta) \leftarrow T$

$F \quad T' \quad + \quad T \quad E'$

$id \quad * \quad F \quad T' \quad F \quad T'$

$(A) \leftarrow id \quad E \quad id \quad E$

$(B) \leftarrow id \quad E \quad id \quad E$

Q) Construct the predictive parsing table for given grammar

$$E \rightarrow E + T \mid T \quad \text{bit} + bi \neq bi = \alpha$$

$$T \rightarrow TF \mid F \quad \text{tugai} \quad \text{dotki}$$

$$F \rightarrow F^* \mid a \mid b \quad \text{bit} + bi \neq bi = \beta$$

$$\text{sol: } \begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

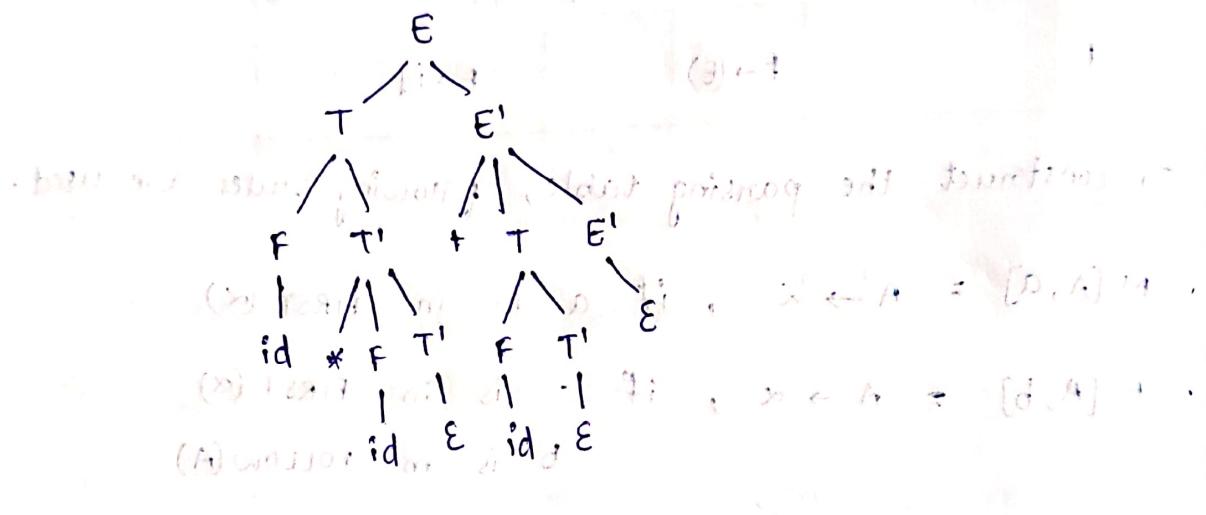
$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$$\begin{array}{l|l} \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \alpha \\ \text{bit} \leftarrow T & \text{bit} + bi \neq bi = \beta \end{array} \quad T^* \beta \neq$$

$\$ E' T$ id \$ $E' \rightarrow T$
 $\$ E' T' F$ id \$ $T \rightarrow FT'$
 $\$ E' T' id$ id \$ $F \rightarrow id$
 $\$ E' T'$ \$ $T' \rightarrow E$
 $\$ E'$ \$ $E' \rightarrow E$
 $\$$ \$ $E' \rightarrow E$



Q) Construct the predictive parsing table for given grammar

$$E \rightarrow E + T | T$$

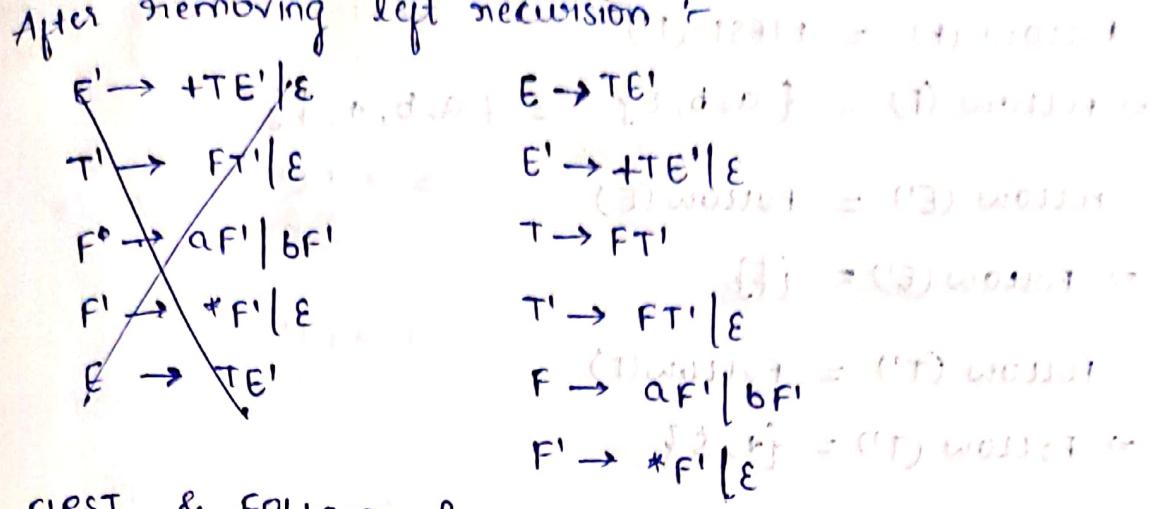
$$T \rightarrow TF | F$$

$$F \rightarrow F^* | a | b$$

sol:-

$E \rightarrow E + T T$ $E \rightarrow T E'$ $E' \rightarrow id + TE' \epsilon$	$T \rightarrow TF F$ $T \rightarrow FT' F$ $T' \rightarrow F T' \epsilon$	$F \rightarrow F^* a b$ $F \rightarrow a F'$ $F' \rightarrow F^* F' \epsilon$
---	---	---

$F \rightarrow F^* a$ $F \rightarrow a F'$ $F' \rightarrow F^* F' \epsilon$	$F \rightarrow F^* b$ $F \rightarrow b F'$ $F' \rightarrow F^* F' \epsilon$	$T' \rightarrow F T' \epsilon$ $T' \rightarrow F T' \epsilon$ $T' \rightarrow F T' \epsilon$
---	---	--



1) FIRST & FOLLOW functions

$$\text{FIRST}(E) = \text{FIRST}(\underline{\underline{TE'}}) \{ \text{FIRST}(T), \text{FIRST}(E') \} = \{a, b\}$$

$$\text{FIRST}(T) = \text{FIRST}(\underline{\underline{FT'}})$$

$$\text{FIRST}(F') = \text{FIRST}(\underline{\underline{\alpha F'}}) \cup \text{FIRST}(\underline{\underline{\beta F'}})$$

$$F' = \{a, b\}$$

$$\Rightarrow \text{FIRST}(E) = \{a, b\}$$

$$\Rightarrow \text{FIRST}(T) = \{a, b\}$$

$$\Rightarrow \text{FIRST}(F') = \{a, b\}$$

Now,

$$\text{FIRST}(E') = \text{FIRST}(\underline{\underline{+TE'}}) \cup \text{FIRST}(\underline{\underline{\epsilon}})$$

$$\Rightarrow \text{FIRST}(E') = \{+, \epsilon\}$$

$$\text{FIRST}(T') = \text{FIRST}(\underline{\underline{FT'}}) \cup \text{FIRST}(\underline{\underline{\epsilon}})$$

$$\Rightarrow \text{FIRST}(T') = \{a, b, \epsilon\} \quad (\because \text{FIRST}(F) = \{a, b\})$$

$$\text{FIRST}(F') = \text{FIRST}(*F') \cup \text{FIRST}(\epsilon)$$

$$\Rightarrow \text{FIRST}(F') = \{* , \epsilon\}$$

$$\Rightarrow \text{FOLLOW}(E) = \{ \$ \}$$

$$\text{FOLLOW}(T) = \text{FIRST}(E')$$

$$= \{+, \epsilon\}$$

$$\Rightarrow \text{FOLLOW}(E)$$

$$\Rightarrow \text{FOLLOW}(T) = \{+, \$\}$$

$$E \rightarrow \underline{\underline{TE'}} \\ \alpha \beta \beta$$

$$E \rightarrow \underline{\underline{TE\$}} \\ \alpha \beta \beta$$

$\text{FOLLOW}(F) = \text{FIRST}(T')$	$T \rightarrow FT' \quad \text{with } T \in \{a, b\}$	$T \rightarrow FE \quad \text{with } F \in \{a, b\}$
$\Rightarrow \text{FOLLOW}(F) = \{a, b, \$\} \setminus \{a, b, +, \$\}$		
$\text{FOLLOW}(E') = \text{FOLLOW}(E)$	$E \rightarrow TE'$	$E \rightarrow TEE'$
$\Rightarrow \text{FOLLOW}(E') = \{\$\}$		
$\text{FOLLOW}(T') = \text{FOLLOW}(T)$	$T \rightarrow FT' \quad \text{with } F \in \{a, b\}$	$T \rightarrow FT' \quad \text{with } F \in \{a, b\}$
$\Rightarrow \text{FOLLOW}(T') = \{+, \$\}$		
$\text{FOLLOW}(F) = \text{FOLLOW}(F')$	$F \rightarrow aF' \quad \text{with } a \in \{a, b\}$	$F \rightarrow aF' \quad \text{with } a \in \{a, b\}$
$\Rightarrow \text{FOLLOW}(F') = \{a, b, \$\} \setminus \{a, b, +, \$\}$		

2) Constructing parsing table.

	$+ (1)$	$(2)* (3)$	$(4)a (5)$	$b (6)$	$\$ (7)$
E			$E \rightarrow TE'$	$E \rightarrow TE'$	
E'	$E' \rightarrow +TE'$				$E' \rightarrow \epsilon$
T				$T \rightarrow FT' \quad (1)$	$T \rightarrow FT' \quad (2)$
T'	$T' \rightarrow \epsilon$			$T' \rightarrow FT' \quad (3)$	$T' \rightarrow FT' \quad (4)$
F			$F \rightarrow aF' \quad (5)$	$F \rightarrow bF' \quad (6)$	
F'	$F' \rightarrow \epsilon \quad (7)$	$F' \rightarrow *F' \quad (8)$	$F' \rightarrow \epsilon \quad (9)$	$F' \rightarrow \epsilon \quad (10)$	$F' \rightarrow \epsilon \quad (11)$

12/10/2023

Consider the grammar

$S \rightarrow i[E(S)]^*a \quad (1) \text{ First } \quad (2) \text{ Follow } \quad (3) \text{ Term }$

$S' \rightarrow eS \mid \epsilon \quad \text{Check whether it is a well-formed grammar.}$

$E \rightarrow b$

Step 1 :- FIRST & FOLLOW functions.

$\text{FIRST}(S) = \{i, \$, a\} \quad (1) \text{ First } \quad (2) \text{ Follow }$

$\text{FIRST}(S') = \{e, \epsilon\} \quad (3) \text{ First } \quad (4) \text{ Follow }$

$\text{FIRST}(E) = \{b\} \quad (5) \text{ First } \quad (6) \text{ Follow }$

$\text{follow}(S) = \{\$, e, E\}$ replace S' by S

if $S' \in \text{FIRST}(S)$, $\text{FIRST}(S') = \{e, E\}$

$\text{follow}(S) = \{\$, e\}$

$S \rightarrow tEtS'$

$\text{follow}(S) = \{t, \$\}$

$S \rightarrow Es$

$\text{follow}(S) = \{e, \$\}$

$S \rightarrow t$

$\text{follow}(S) = \{t, \$\}$

$\text{FOLLOW}(S') = \text{FOLLOW}(S) = \{\$, e\}$

$\text{FOLLOW}(E) = \text{FIRST}(tSS') = \{t\}$

Step 2

	i	t	a	e	b	*	\$
s	$s \rightarrow iEtSS'$		$s \rightarrow a$				
S'				$S' \rightarrow eS$			$S' \rightarrow E$
E					$E \rightarrow b$		

Here, one of the cells of parsing table contains more than one production rule.

Hence, given grammar is not an LL(1) grammar

② Find FIRST & FOLLOW functions. ③ Q) Construct the predictive parsing table

$$S \rightarrow ABCDE$$

$$A \rightarrow a | \epsilon$$

$$B \rightarrow b | \epsilon$$

$$C \rightarrow c | \epsilon$$

$$D \rightarrow d | \epsilon$$

$$E \rightarrow e | \epsilon$$

for the grammar

$$S \rightarrow (L) | a$$

$$L \rightarrow L, S | S,$$

② Q) $S \rightarrow ACB | CbB | Ba$

$$A \rightarrow da | BC$$

$$B \rightarrow g | \epsilon$$

$$C \rightarrow h | \epsilon$$

$$\text{① } \text{FIRST}(S) \cup \text{FIRST}(ABCDE) = \text{FIRST}(A) \cup \text{FIRST}(B) \cup \text{FIRST}(C) \cup \text{FIRST}(D) \cup \text{FIRST}(E)$$

$$\text{FIRST}(A) = \{a, \epsilon\} \quad \text{FIRST}(S) = \{a, b, c, d, e, \epsilon\}$$

$$\text{FIRST}(B) = \{b, \epsilon\}$$

$$\text{FIRST}(C) = \{c\}$$

$$\text{FIRST}(D) = \{d, \epsilon\}$$

$$\text{FIRST}(E) = \{e, \epsilon\}$$

$$\text{FIRST}(S) = \text{FIRST}(ABCDE)$$

$$= \text{FIRST}(A) \cup \text{FIRST}(B) \cup \text{FIRST}(C) \cup \text{FIRST}(D) \cup \text{FIRST}(E)$$

$$= \{a, \epsilon\} \cup \{b, \epsilon\} \cup \{c\} \cup \{d, \epsilon\} \cup \{e, \epsilon\}$$

$$= \{a, b, c, d, e\}$$

~~Follow(S) = { \$ }
Follow(A) = FIRST(BCDE) = FIRST(B) ∪ {b, ε} = {b, ε}
= {b}, FIRST(CDE) = FIRST(C)
= {c};
= {b, c}~~

~~Follow(B) = FIRST(CDE)
= FIRST(C) = {c}~~

~~Follow(C) = FIRST(DE)
= FIRST(D) ∪ FIRST(E)
= {d, FIRST(BCE)} ∪ {e, FIRST(E)}~~

~~Follow(D) = {d, FIRST(BCE) ∪ FIRST(E)} ∪ {e, d, \$}~~

~~Follow(E) = {d, {b, FIRST(DE)}} ∪ {c} ∪ {e, d, \$}~~

~~Follow(E) = {d, {b, FIRST(D) ∪ FIRST(E)}} ∪ {c} ∪ {e, d, \$}~~

~~Follow(E) = {d, b, d, \$}~~

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$$\text{FOLLOW}(S) = \{\$\}$$

$$\text{FOLLOW}(A) = \text{FIRST}(BCDE) = \{b, c\}$$

$$\text{FOLLOW}(B) = \text{FIRST}(CDE) = \{c\}$$

$$\text{FOLLOW}(C) = \text{FIRST}(DE) = \{d, e, \$\}$$

$$\text{FOLLOW}(D) = \text{FIRST}(E) = \{e, \$\}$$

$$\text{FOLLOW}(E) = \{\$, \$\}$$

$$\textcircled{2} \quad \text{FIRST}(S) = \text{FIRST}(ACB) \cup \text{FIRST}(CBB) \cup \text{FIRST}(BA) \\ = \{d, g, \epsilon\} \cup \{h, \epsilon\} \cup \{g, \epsilon\} \\ = \{d, g, h, \epsilon\}$$

$$\text{FIRST}(A) = \text{FIRST}(da) \cup \text{FIRST}(BC) \\ = \{d\} \cup \{g, h\} \\ = \{d, g, h, \epsilon\}$$

$$\text{FIRST}(B) = \{g, \epsilon\}$$

$$\text{FIRST}(C) = \{h, \epsilon\}$$

$$\text{FOLLOW}(S) = \{\$\}$$

$$\text{FOLLOW}(A) = \text{FIRST}(CB) = \{h, \epsilon\} \cup \text{FIRST}(B) \cup \text{FOLLOW}(S)$$

$$\text{FOLLOW}(B) = \text{FOLLOW}(S) \cup \{a\} = \{h, g, \$\}$$

$$\text{FOLLOW}(C) = \text{FIRST}(B) = \{g, \epsilon\} = \{h, g, \$, a\}$$

$$\text{FOLLOW}(C) = \text{FIRST}(B) \cup \text{FIRST}(bb) \cup \text{FOLLOW}(A) \\ S \rightarrow ACB \quad S \rightarrow CBB \quad A \rightarrow BC \\ = \{h, b, h, \$\}$$

(3) $S \rightarrow (L) | a$
 $L \rightarrow L, S | S$
 Removing left recursion
 $S \rightarrow (L) | a$
 $L \rightarrow SL'$
 $L' \rightarrow , SL' | \epsilon$

FIRST & FOLLOW functions

$$\text{FIRST}(S) = \text{FIRST}(L) \cup \text{FIRST}(a) = \{\epsilon, a\}$$

$$\text{FIRST}(L) = \text{FIRST}(SL') = \{\epsilon, a\}$$

$$\text{FIRST}(L') = \text{FIRST}(SL') \cup \text{FIRST}(\epsilon) = \{\epsilon, \epsilon\}$$

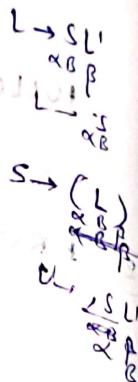
$$\text{FOLLOW}(S) = \{\$, \$,)\}$$

$$\text{FOLLOW}(L) = \text{FIRST}()) = \{)\}$$

$$\text{FOLLOW}(L') = \text{FOLLOW}(L) = \{)\}$$

Passing table.

	()	.	,	;	a	b	*	\$
S	$S \rightarrow (L)^*$					$S \rightarrow a$			
L		$L \rightarrow SL'$					$L \rightarrow SL'$		
L'				$L' \rightarrow \epsilon$		$L' \rightarrow SL'$			



Grammar G3: $G3 = \{a, b, \$\} \cup \{(), , ;, , *\} \cup \{(,)\}$
 $\{a, b, \$\} \cup \{(), , ;, , *\} \cup \{(), ()\}$
 $\{a, b, \$\} \cup \{(), , ;, , *\} \cup \{(), (), ()\}$
 $\{a, b, \$\} \cup \{(), , ;, , *\} \cup \{(), (), (), ()\}$

{(,), ;, *}

LR(0) Parser

$$S \rightarrow AA \rightarrow 1$$

$$A \rightarrow aA \rightarrow 2$$

$$A \rightarrow b \rightarrow 3$$

include new production rule
⇒ Augmented grammar is the result

step 1 + Include new production rule

Augmented grammar \vdash

$$\begin{aligned} S' &\rightarrow S \\ S &\rightarrow AA \\ A &\rightarrow aA \\ A &\rightarrow b \end{aligned}$$

step 2 + Closure operation Introduce \cdot at the RHS

Initial grammar becomes at leftmost.

closure of the production rules

$$\left. \begin{aligned} S' &\rightarrow \cdot S \\ S &\rightarrow \cdot AA \\ A &\rightarrow \cdot aA \\ A &\rightarrow \cdot b \end{aligned} \right\}$$

step 3 + Apply goto operation (move \cdot towards right)

(no I/P symbol is scanned) $S \rightarrow \cdot AA$

(if I/P symbol is scanned) $S \rightarrow A \cdot A$

(all I/P symbols are scanned) $S \rightarrow AA \cdot$

Check symbols that are after \cdot & include its production rule

$A \rightarrow \cdot aA \xrightarrow{a} A \rightarrow a \cdot A$

$A \rightarrow \cdot aA \xrightarrow{a} A \rightarrow \cdot aA$

$A \rightarrow \cdot b \xrightarrow{b} A \rightarrow b \cdot$

$S \rightarrow S.$ \xrightarrow{A} (no S/P symbol)

$S \rightarrow A.A \xrightarrow{A} (S \rightarrow AA.)$

$A \rightarrow aA \xrightarrow{a} A \rightarrow a.A$ already exists.

$A \rightarrow bA \xrightarrow{b} A \rightarrow b.$ already exists. A

$A \rightarrow a.A \xrightarrow{A} (A \rightarrow AA.)$

$A \rightarrow .aA \xrightarrow{+} A \rightarrow a.A$

$A \rightarrow .bA \xrightarrow{+} A \rightarrow b.$

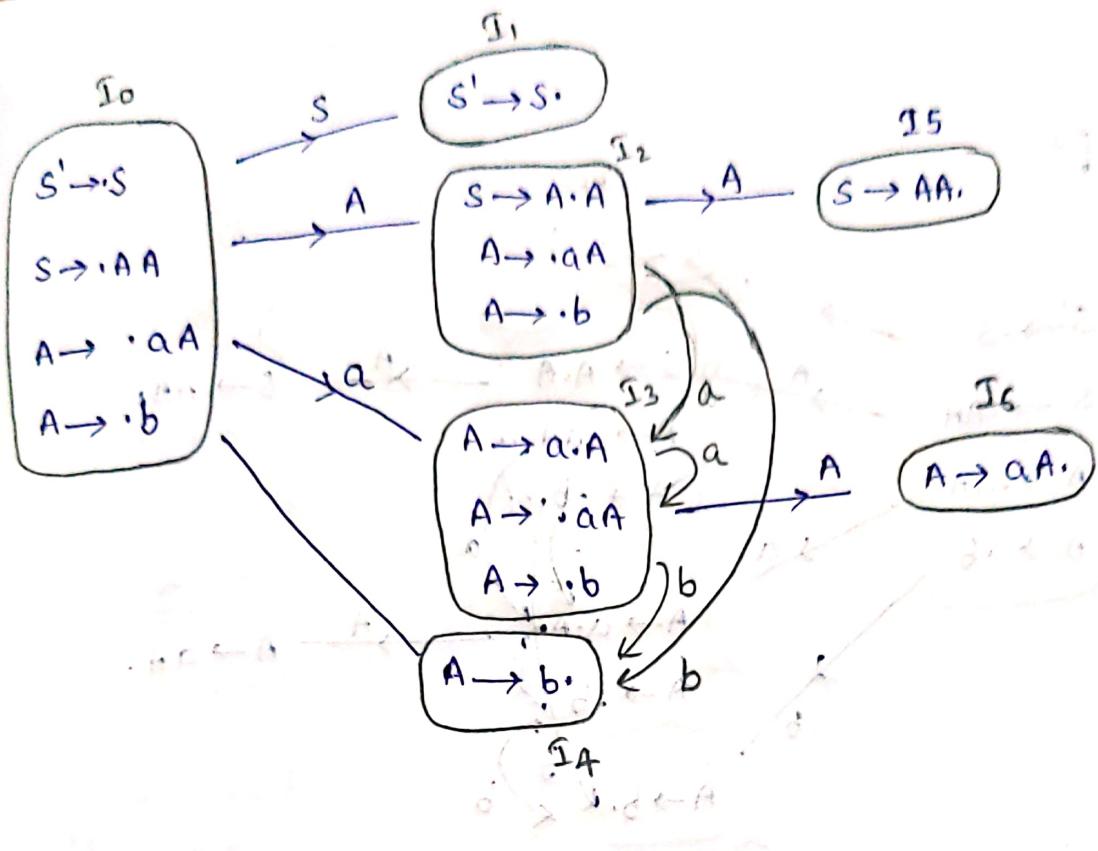
$A \rightarrow b. \xrightarrow{+} (\text{no S/P symbol})$

Step 4: Construct parsing table.

$$\text{FOLLOW}(S) = \{\$\}$$

$$\text{FOLLOW}(A) = \text{FIRST}(A) \cup \text{FOLLOW}(S) = \{a, b, \$\}$$

	Action			goto	
	a	b	\$	A	S
0	S_3	S_4		2	1
1			accept		
2	S_3	S_4		5	
3	S_3	S_4		6	
4	γ_3	γ_3	γ_3	$\leftarrow A$	
5	γ_1	γ_1	γ_1	$\leftarrow A$	
6	γ_2	γ_2	γ_2		



SLR (1) parser

$S \rightarrow AA$

$A \rightarrow aA$

$A \rightarrow b$

step 1

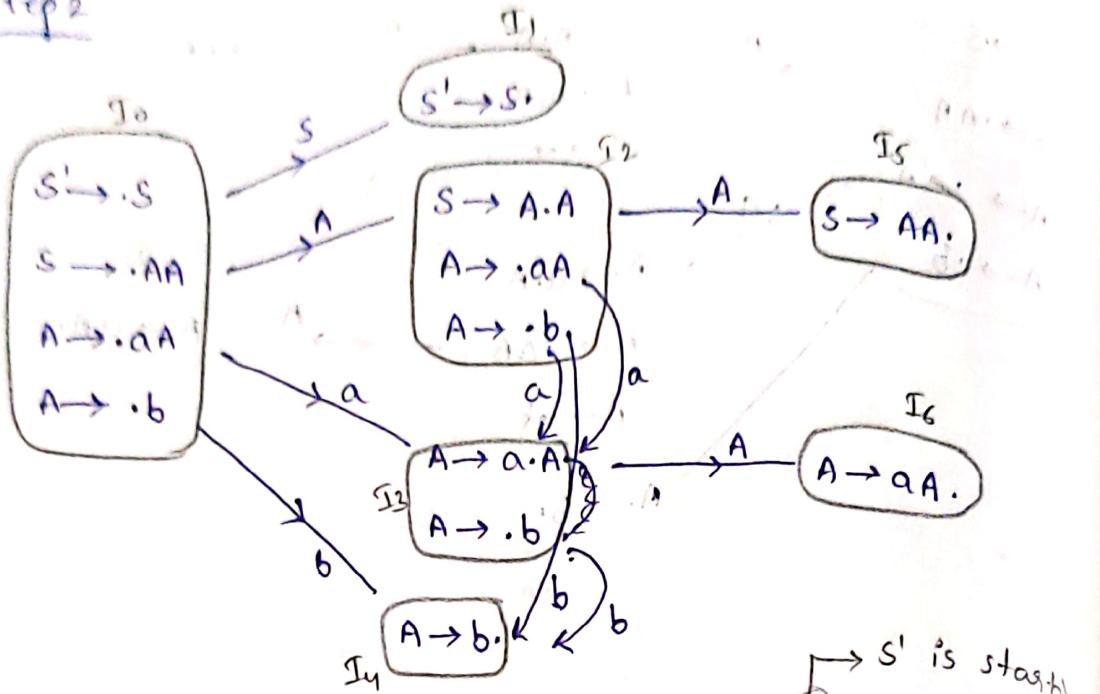
$S' \rightarrow S$

$S \rightarrow AA$

$A \rightarrow aA$

$A \rightarrow b$

Step 2



Step 3

	a	b	\$	Action	goto
0	s_3	s_4			2 1
1				(accept)	
2	s_3	s_4			5
3	s_3	s_4			6
4	γ_3	γ_3	γ_3		
5				γ_1	
6	γ_2	γ_2	γ_2		

I1 : $s'_1 \rightarrow s.$
 s'_1 is starting symbol
so write accept

$I_6 \Rightarrow (A) \rightarrow aA. \quad \text{--- (2)}$

→ A is not starting symbol

so, late FOLLOW(A) = {a, b, \$}

In these places,
write γ_2

UNIT - 3

Syntax Directed Definition (SDD)

$$SDD = \text{CFG} + \text{Semantic Rules}$$

all with

$$E \rightarrow E + T \Rightarrow E.\text{val} = E.\text{val} + T.\text{val} \quad \xrightarrow{\text{attribute}}$$

$$E \rightarrow T \Rightarrow E.\text{val} = T.\text{val} \quad \xrightarrow{\text{semantic rule}}$$

An SDD is a Context Free Grammar together with semantic rule.

Attributes are associated with grammar symbols and semantic rules are associated with production rules.

Attributes may be numbers, strings, references, datatypes etc.

Ex: Production rule semantic rules.

$$E \rightarrow E + T \quad E.\text{val} = E.\text{val} + T.\text{val}$$

Types of Attributes (2)

1) Synthesized Attribute: If a ^{parent} node takes value from its children, then it is called Synthesized Attribute.

Ex: $A \rightarrow B C D$

$$\begin{aligned} A.S &= B.S \\ A.S &= C.S \\ A.S &= D.S \end{aligned}$$

2) Inherited Attribute: If a node takes a value from its parent or sibling nodes then, it is called Inherited Attribute.

Ex: $A \rightarrow B C D$

$$\begin{aligned} C.i &= A.i \\ C.i &= B.i \\ C.i &= D.i \end{aligned}$$

Types of SDDs (2)

- 1) S-attributed SDD
- 2) L-attributed SDD

3) S-Attributed SDD

- » An SDD that uses only synthesized attributes is called S-Attributed SDD.

Ex: $A \rightarrow BCD$

$$A.S = B.S$$

$$A.S = C.S$$

» $A.S \neq D.S$ (numerical value assigned to attribute)

- » Semantic actions are always placed at the right end of the productions.

Ex: $A \rightarrow BCD \{ \dots \}$

- » Attributes are evaluated with Bottom-up Parsing

2) L-Attributed SDD

- » It uses both synthesized and inherited attributes.

Inherit attributes can inherit values from either parent or left sibling only.

Ex: $A \rightarrow BCD$

$$C.i = A.i$$

$$C.i = B.i$$

$$D.i = C.i$$

$$C.i = D.i (X)$$

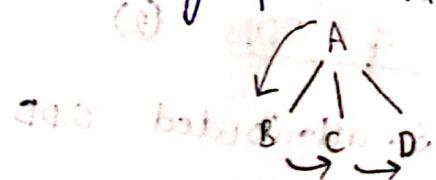
- » Semantic actions are placed anywhere on RHS.

Ex: $A \rightarrow \{ \dots \} BCD$ (right to left grid is not possible)

$$A \rightarrow BCD \{ \dots \} A \Rightarrow i.i$$

$$A \rightarrow B \{ \dots \} CD \quad B \Rightarrow i.i$$

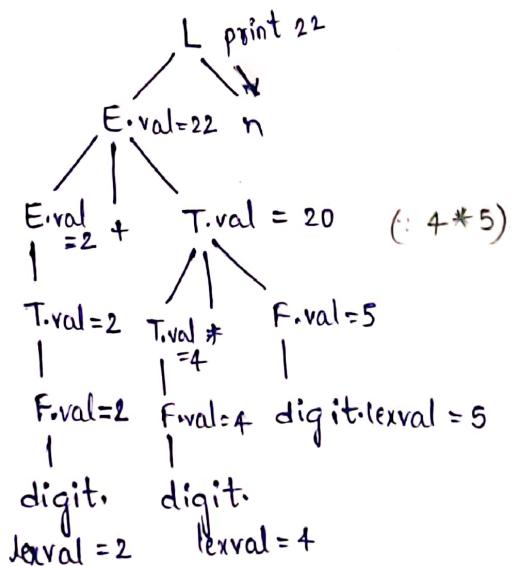
- » Attributes are evaluated by traversing parse string depth-first, left to right



Ques: bottom up -> L-Attributed SDD

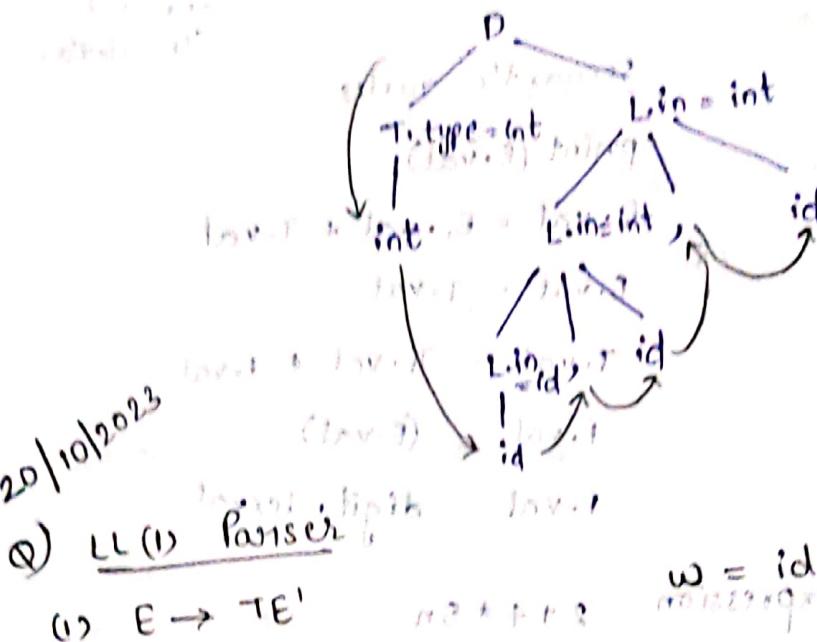
<u>Examples</u>	<u>S - attributed SDD</u>	<u>SDT</u> Syntax Directed Translation
(i)	Production rules for Desktop calc.	
	→ new line	
$L \rightarrow E_n$		<u>Semantic rules</u>
$E \rightarrow E_1 + T$		$E.\text{val} = E_1.\text{val} + T.\text{val}$
$E \rightarrow T$		$E.\text{val} = T.\text{val}$
$T \rightarrow T_1 * F$		$T.\text{val} = T_1.\text{val} * F.\text{val}$
$F \rightarrow (E)$		$F.\text{val} = (E.\text{val})$
$F \rightarrow \text{digit}$		$F.\text{val} = \text{digit.lexval}$

evaluate the expression $2 + 4 * 5n$



<u>(ii) L-attributed SDD</u>	<u>Production</u>	<u>Semantic rules</u>
	$D \rightarrow TL$	$L.\text{in} = T.\text{Type}$
	$T \rightarrow \text{int}$	$T.\text{Type} = \text{integer}$
	$T \rightarrow \text{real}$	$T.\text{Type} = \text{real}$
-	$L \rightarrow L_1, id$	$L_1.\text{in} = L.\text{in}$
	$L \rightarrow id$	$\text{add type}(\text{id.entry}, L.\text{in})$
		$\text{add type}(\text{id.entry}, L.\text{in})$

Evaluate int id1, id2, id3



(2) $E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id$

SOL

Step 1 → FIRST & FOLLOW, if functions

$$\text{FIRST}(E) = \text{FIRST}(TE')$$

$$\text{FIRST}(T) = \text{FIRST}(FT')$$

$$\text{FIRST}(F) = \text{FIRST}(E) \cup \text{FIRST}(id)$$

$$= \{+, id\}$$

Now,

$$\text{FIRST}(E') = \text{FIRST}(+TE') \cup \text{FIRST}(E)$$

$$= \{+, \epsilon\}$$

$$\text{FIRST}(T) = \text{FIRST}(FT')$$

$$= \{(id)\}$$

$$\text{FIRST}(T') = \text{FIRST}(FT') \cup \text{FIRST}(E)$$

$$= \{\ast, \epsilon\}$$

$$\text{FIRST}(F) = - \text{FIRST}$$

$$\text{FOLLOW}(E) = \{\$,)\}$$

$$\text{FOLLOW}(E') = \text{FOLLOW}(E) = \{+,)\}$$

$$\text{FOLLOW}(T) = \text{FIRST}(E)$$

$$= \{+, \epsilon\}$$

$$= \{+, \$,)\}$$

$$\text{FOLLOW}(T') = \text{FOLLOW}(T) = \{+, \$,)\}$$

$$\begin{aligned} \text{FOLLOW}(F) &= \text{FIRST}(T') = \{\ast, \epsilon\} \\ &= \{\ast, \$, +,)\} \end{aligned}$$

$$f \rightarrow (E)$$

$$\alpha \beta \beta$$

$$E \rightarrow TE'$$

$$\alpha \beta \beta$$

$$T \rightarrow FT'$$

$$\alpha \beta$$

$$T \rightarrow FE$$

$$\alpha \beta \beta$$

step 2 → parsing table.

	+	*	()	id	\$
E			$E \rightarrow TE'$		$E \rightarrow TE'$	
E'	$E' \rightarrow +TE'$			$E' \rightarrow E$		
T			$T \rightarrow FT'$		$T \rightarrow FT'$	
T'	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow E$		$T' \rightarrow E$
F			$F \rightarrow (E)$		$F \rightarrow id$	

step 3 → Parsing the input string.

$$w = id + id * id$$

stack

input

output

$\$ E$

id + id * id \$

$\$ E' T$

id + id * id \$

$E \rightarrow TE'$

$\$ E' T' F$

id + id * id \$

$T \rightarrow FT'$

$\$ E' T' id$

id + id * id \$

$F \rightarrow id$

$\$ E' T'$

id + id * id \$

$T' \rightarrow E$

$\$ E'$

id + id * id \$

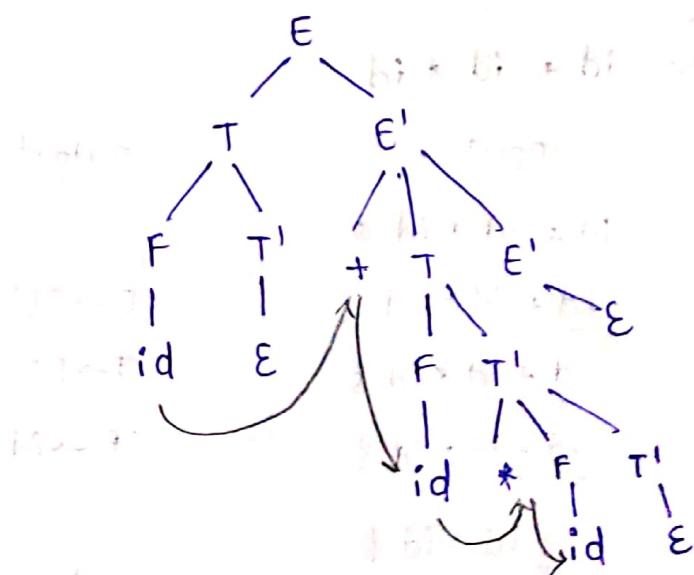
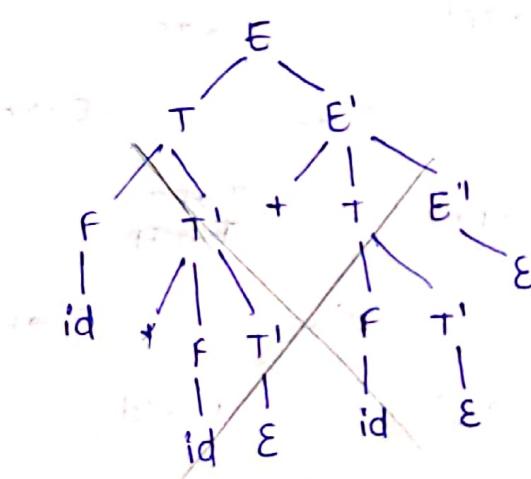
$E' \rightarrow +TE'$

$\$ E' T +$

id + id * id \$

=

$$\begin{array}{ll}
 \$ E T = & id * id \$ \\
 \$ E' T' F = & id * id \$ \\
 \$ E' T' id = & id * id \$ \\
 \\
 \$ E' T' = & * id \$ \\
 \$ E' T' F * = & * id \$ \\
 \\
 \$ E' T' F = & id \$ \\
 \$ E' T' id = & id \$ \\
 \\
 \$ E' T' = & \$ \\
 \$ E' = & \$ \\
 \\
 \$ = & \$
 \end{array}
 \quad
 \begin{array}{l}
 T \rightarrow F T I \\
 \cancel{F \rightarrow id} \\
 F \rightarrow id \\
 \\
 T' \rightarrow * F T I \\
 \\
 F \rightarrow id \\
 \\
 T' \rightarrow \epsilon \\
 E' \rightarrow \epsilon
 \end{array}$$



Q) construct SLR Parser

$$S \rightarrow AA$$

$$A \rightarrow aA$$

$$A \rightarrow b$$

03/11/2023

Q) SLR Parser.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

SOL \Rightarrow step 1: Augmented Grammar

$$\cdot E \leftarrow E' \rightarrow E \quad \text{P: } E \leftarrow \cdot$$

$$\cdot E + T \leftarrow E \rightarrow E + T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } T \leftarrow \cdot$$

$$E \rightarrow T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } T \leftarrow \cdot$$

$$T \rightarrow T * F \quad \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$\begin{array}{l} \text{R: } T \rightarrow F \\ \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot \end{array}$$

$$F \rightarrow (E) \quad \text{P: } F \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$F \rightarrow id \quad \text{P: } F \leftarrow \cdot \quad \text{I: } id \leftarrow \cdot$$

step 2 closure \leftarrow

$$\cdot E \leftarrow E' \rightarrow \cdot E \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$(3) \leftarrow E \rightarrow \cdot E + T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

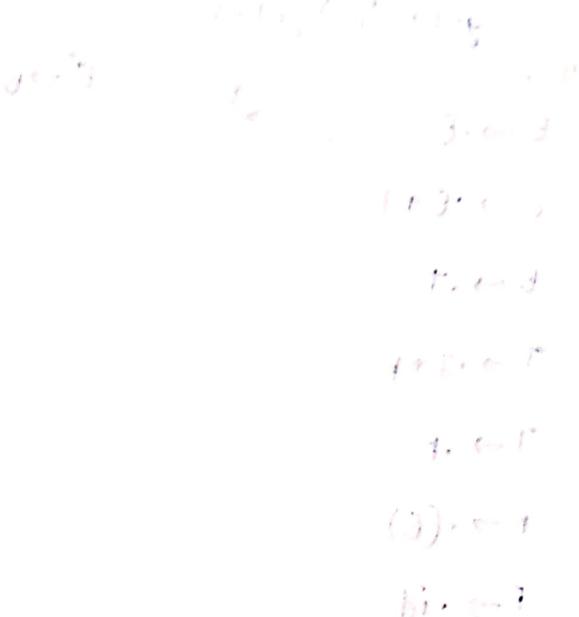
$$\cdot E \leftarrow \cdot E + T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$T \rightarrow \cdot T * F \quad \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$T \rightarrow \cdot F \quad \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$F \rightarrow \cdot (E) \quad \text{P: } F \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$F \rightarrow \cdot id \quad \text{P: } F \leftarrow \cdot \quad \text{I: } id \leftarrow \cdot$$



SOL \Rightarrow step 1: Augmented Grammar

$$\cdot E \leftarrow E' \rightarrow E \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$\cdot E + T \leftarrow E \rightarrow E + T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } T \leftarrow \cdot$$

$$E \rightarrow T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } T \leftarrow \cdot$$

$$T \rightarrow T * F \quad \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$\begin{array}{l} \text{R: } T \rightarrow F \\ \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot \end{array}$$

$$F \rightarrow (E) \quad \text{P: } F \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$F \rightarrow id \quad \text{P: } F \leftarrow \cdot \quad \text{I: } id \leftarrow \cdot$$

$$\cdot E \leftarrow E' \rightarrow \cdot E \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$(3) \leftarrow E \rightarrow \cdot E + T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$\cdot E \leftarrow \cdot E + T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$T \rightarrow \cdot T * F \quad \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$T \rightarrow \cdot F \quad \text{P: } T \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$F \rightarrow \cdot (E) \quad \text{P: } F \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$F \rightarrow \cdot id \quad \text{P: } F \leftarrow \cdot \quad \text{I: } id \leftarrow \cdot$$

SOL \Rightarrow step 2: closure

$$(3) \leftarrow E \rightarrow \cdot E + T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$(3) \leftarrow E \rightarrow \cdot T \quad \text{P: } E \leftarrow \cdot \quad \text{I: } T \leftarrow \cdot$$

$$(3) \leftarrow E \rightarrow \cdot T * F \quad \text{P: } E \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$(3) \leftarrow E \rightarrow \cdot F \quad \text{P: } E \leftarrow \cdot \quad \text{I: } F \leftarrow \cdot$$

$$(3) \leftarrow E \rightarrow \cdot (E) \quad \text{P: } E \leftarrow \cdot \quad \text{I: } E \leftarrow \cdot$$

$$(3) \leftarrow E \rightarrow \cdot id \quad \text{P: } E \leftarrow \cdot \quad \text{I: } id \leftarrow \cdot$$

closure for E $\leftarrow \{ (3) \}$

closure for T $\leftarrow \{ (3), (3) \}$

closure for F $\leftarrow \{ (3), (3) \}$

closure for (E) $\leftarrow \{ (3), (3) \}$

goto³(3) goto⁴

I₀:

E' → E.

E → ·E + T

E → ·T

T → ·T * F

T → ·F

F → ·(E)

F → ·id

I₁: goto (I₀, E) :

E' → E ·

E → E · + T

I₂: goto (I₀, T) :

E → T ·

T → T · * F

I₃: goto (I₀, F) :

T → F ·

I₄: goto (I₀, ()) :

F → (· E)

E → · E + T

E → · T

I₅: goto (I₀, id) :

T → · T * F (I₁)

T → · F

F → · (E) (I₂)

F → · id (I₅)

F → id.

I₆: goto (I₁, +) :

E → E + · T

T → · T * F

T → · F
F → · (E)
F → · id

I₇: goto (I₂, *) :

T → T * F.

T → · T * · F
F → (· E)
F → · (E), I₄
F → · id I₅

I₈: goto (I₄, E) :

F → (E ·)

E → E + + T (I₆)

E → T + + T .

(I₄, T) .

(3), .

b · .

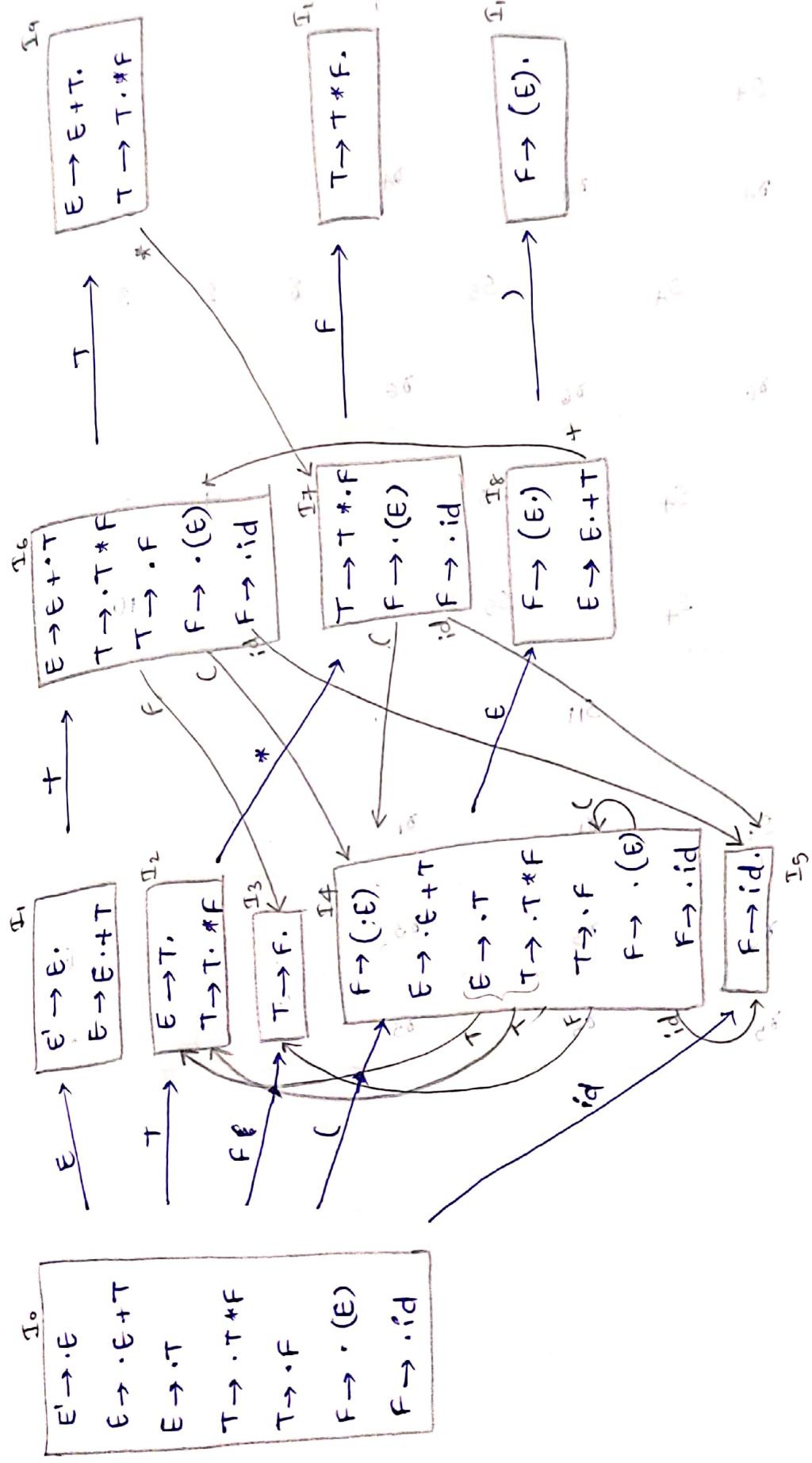
step (4) ← FIRST & FOLLOW

step (4) ← FOLLOW functions.

FOLLOW(E) = { \$, +,) }

FOLLOW(T) = { \$, +,), * }

FOLLOW(F) = { \$, +,), * }



Step 5 ← parsing table.

	+	*	()	id	\$	E	T	F
0			s_4		s_5		1	2	3
1	s_6					accept			
2		s_7							
3	γ_4	γ_4		γ_4		γ_4			
4			s_4		s_5		8	2	3
5	γ_6	γ_6		γ_6		γ_6			
6			s_4		s_5		9	3	
7			s_4		s_5			10	
8	s_6			s_{11}					
9	γ_1	s_7		γ_1		γ_1			
10	γ_3	γ_3		γ_3		γ_3			
11	γ_5	γ_5		γ_5		γ_5			

07/11/2023

Input string: id * id + id

stack	input	reduce & shift output/Action
0	id * id + id \$	shift, NO: shift
0 id 5	* id + id \$	reduce by F → id
OF3 (from table)	* id + id \$	reduce by T → F, P = 2
OT2	* id + id \$	shift, P = 2
OT2 * F	id + id \$	shift
OT2 * F id 5	+ id \$	reduce by F → id
OT2 * F 10	+ id \$	reduce by T → T * F
OT2	+ id \$	reduce by E → T
OE1	+ id \$	shift
OE1 + G	id \$	shift
OE1 + G id 5	\$	reduce by F → id
OE1 + G F 3	\$	reduce by T → F
OE1 + G T 9	\$	reduce by E → ETT
OE1	\$	Accept

(0, 1) stop

b, 0, 0 ← 3

f, 0, 0 ← 3

f, b, 0 ← 3

(0, 2) stop : r

b1, 0, 0 ← 3

b1, 0, 0 ← 3

b1, 0, 0 ← 3

08/11/2023

CLR Parser

$$\begin{array}{l} S \rightarrow CC \quad -\textcircled{1} \\ C \rightarrow cC \quad -\textcircled{2} \\ C \rightarrow \#d^+ \quad -\textcircled{3} \end{array}$$

for + pt grammar

 $LR(1) = LR(0)$ items + look ahead symbols.

SLR(1), no look ahead symbols.
CLR(0) items
CLR(1), we write look ahead symbols.

» $LR(1)$ items.↓
 $LR(0)$ +

look ahead symbols.

step1: Augmented grammar

$S' \rightarrow S$

$S' \rightarrow CC$

for + pt grammar

$C \rightarrow cC$

for + pt grammar

$C \rightarrow d$

step2: write look ahead symbols.

I_0 : $S' \rightarrow \cdot S, \$$ → $\cdot S$ is starting symbol. → after S there's no symbol
 $S' \rightarrow \cdot CC, \$$ → $\cdot CC$ (FIRST(C))

$C \rightarrow \cdot cC, c/d$ → $\cdot cC$ (FIRST(c)) → after C there's a symbol c

$C \rightarrow \cdot d, c/d$ → $\cdot d$ (FIRST(d))

 I_1 : goto (I_0, S)

$S' \rightarrow S \cdot, \$$

 I_2 : goto (I_0, C)

$S' \rightarrow C \cdot C, \$$

$C \rightarrow \cdot cC, \$$ → $\cdot cC$ (FIRST(c))

$- C \rightarrow \cdot d, \$$

 I_3 : goto (I_0, c)

$C \rightarrow c \cdot C, c/d$

$C \rightarrow \cdot cC, c/d$ → $\cdot cC$ (I₃)

$C \rightarrow \cdot d, c/d$ → $\cdot d$ (I₄)

\cdot is separator
 not a terminal

$I_4 : \text{goto } (I_0, d)$

$C \rightarrow d., \text{ cld}$

$I_5 : \text{goto } (I_2, C)$

$S \rightarrow CC., \$$

$I_6 : \text{goto } (I_2, C)$

$C \rightarrow c.C, \$$

$C \rightarrow .cC, \$ (I_6)$

$C \rightarrow .d, \$ (I_7)$

$I_7 : \text{goto } (I_2, d)$

$C \rightarrow d., \$$

$I_8 : \text{goto } (I_3, C)$

$C \rightarrow CC., \text{ cld}$

$I_9 : \text{goto } (I_3, C)$

~~$C \rightarrow c.C, \text{ cld}$~~

~~$C \rightarrow .cC, \text{ cld}$~~

~~$C \rightarrow .d, \text{ cld}$~~

$I_{10} : \text{goto } (I_3, d)$

~~$C \rightarrow d., \text{ cld}$~~

I_0 initial state

$S' \rightarrow S, \$$
$S \rightarrow .CC, \$$
$C \rightarrow .cC, \text{ cld}$
$C \rightarrow .d, \text{ cld}$

$I_1 : S' \rightarrow S., \$$

C

$I_2 : S \rightarrow CC., \$$

$C \rightarrow c.C, \$$

$C \rightarrow .cC, \$$

$C \rightarrow .d, \$$

C

$I_3 : C \rightarrow CC., \$$

C

$I_4 : C \rightarrow c.C, \$$

C

$I_5 : C \rightarrow .cC, \$$

C

$I_6 : C \rightarrow .d, \$$

C

$I_7 : C \rightarrow CC., \text{ cld}$

C

$I_8 : C \rightarrow d., \text{ cld}$

C

$I_9 : C \rightarrow c.C, \text{ cld}$

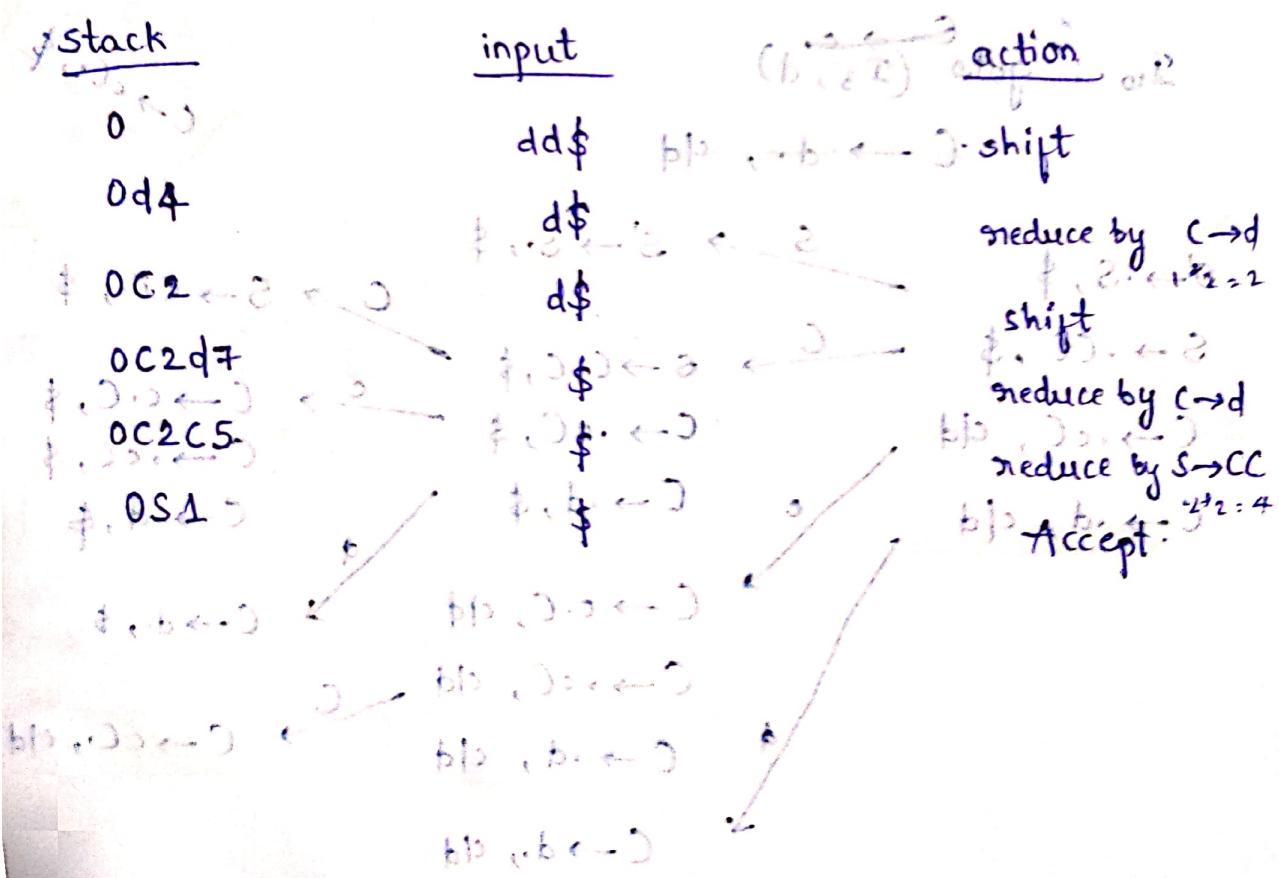
C

$I_{10} : C \rightarrow .cC, \text{ cld}$

C

	Action			(b, c) goto p : pL
	c	d	\$	b p S · b · c
0	S_3	S_4		(b, c) stop : $\frac{1}{2} \epsilon L$
1			Accept	$\frac{1}{2} \epsilon L \leftarrow \epsilon$
2	S_6	S_7		(b, c) stop : $\frac{1}{2} \epsilon L$
3	$\emptyset, \cdot b \cdot \leftarrow \cdot$ S_3	$\cdot S_4$		$\emptyset, \cdot b \cdot \leftarrow \cdot$
4	τ_3	τ_3		$\tau_3, \emptyset, b \cdot \leftarrow \cdot$
5			τ_1	$\tau_1, (b, c) stop : pL$
6	S_6	S_7		$\emptyset, \cdot b \cdot \leftarrow \cdot$
7			τ_3	$\tau_3, (b, c) stop : \frac{1}{2} \epsilon L$
8	τ_2	τ_2		$\tau_2, \cdot b \cdot \leftarrow \cdot$
9			τ_2	$\tau_2, (b, c) stop : pL$

Parse the input string $w = dd\$, b, b \cdot$ (same as SLR)



10/11/2023

LALR Parser

$$S \rightarrow CC$$

$$C \rightarrow cC \text{ or } d$$

$$C \rightarrow d$$

$$S_{36} : C \rightarrow c \cdot C, \quad cd|\$$$

$$C \rightarrow \cdot cC, \quad cd|\$$$

$$C \rightarrow \cdot d, \quad cd|\$$$

$$S_{47} : C \rightarrow d \cdot, \quad cd|\$$$

$$S_{89} : C \rightarrow cC, \quad cd|\$$$

Parsing table

Instead of writing 3 & 6 separately ; write 36 as single state

	c	d	\$	S	C
0	S_{36}	S_{47}		1	2
1			Accept		
2	S_{36}	S_{47}		5	
36	S_{36}	S_{47}			89
47	δ_3	δ_3	δ_3		
5	S_{36}	S_{47}	δ_1		9
89	δ_2	δ_2	δ_2		

Minimum length string: cd\\$
dd\$

Same states with diff look ahead symbols are combined.

Aug 11, 2023

$\delta_3, \delta_6 \rightarrow$ same states but
 $\delta_4, \delta_7 \rightarrow$ same states but
 $\delta_8, \delta_9 \rightarrow$ same states but
 look ahead symbols

MS DOC 10

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In shift to S_{36}
 But not in reduce.
 Combine the states
 $3 + 4 = 2$

2 + 8

3 + 9

6 + 7

4 + 9

combined to single

3

Parse the input string cd\$.

<u>stack</u>	<u>input</u>	<u>action</u>
0	cd\$	shift b ← ?
0C36	d\$	shift b ← ?
0C36d47	\$	shift b ← ? reduce by C → d
0 <u>C</u> 36 <u>C</u> 89	\$	shift b ← ? reduce by C → CC
0C2	\$	shift b ← ? reduce by C → CC

to show, what are the patterns of tokens
stack appears

as follows
initial stack
Construct LALR parser and parse the input string w=id=id

$$S \rightarrow L=R$$

$$S \rightarrow R$$

$$L \rightarrow *R$$

$$BL \rightarrow id$$

$$R \rightarrow L$$

Augumented Grammar :-

$$S' \rightarrow S$$

$$S \rightarrow L=R \quad -1$$

$$S \rightarrow R \quad -2$$

$$L \rightarrow *R \quad -3$$

$$L \rightarrow id \quad -4$$

$$R \rightarrow L \quad -5$$

before parse algorithm

I₀:

$$S' \rightarrow \cdot S, \$$$

$$S \rightarrow \cdot L = R, \$$$

$$S \rightarrow \cdot R, \$$$

$$L \rightarrow \cdot *R, = | \$$$

$$L \rightarrow \cdot id, = | \$$$

$$R \rightarrow \cdot L, \$$$

I₁: goto (I₀, S)

$$S' \rightarrow S., \$$$

I₂: goto (I₀, L)

$$S \rightarrow L. = R, \$$$

$$R \rightarrow L., \$$$

I₃: goto (I₀, R)

$$S \rightarrow R., \$$$

I₄: goto (I₀, *)

$$L \rightarrow * . R, = | \$$$

$$R \rightarrow \cdot L, = | \$$$

$$L \rightarrow \cdot * R, = | \$ \text{ (I}_4\text{)}$$

$$L \rightarrow \cdot id, = | \$ \text{ (I}_5\text{)}$$

I₅: goto (I₀, id)

$$L \rightarrow id., = | \$$$

I₆: goto (I₂, =)

$$S \rightarrow L = \cdot R, \$$$

$$R \rightarrow \cdot L, \$$$

$$L \rightarrow \cdot * R, \$$$

$$L \rightarrow \cdot id, \$$$

I₇: goto (I₄, R)

$$L \rightarrow * R., = | \$$$

I₈: goto (I₄, L)

$$R \rightarrow L., = | \$$$

I₉: goto (I₆, R)

$$S \rightarrow L = R., \$$$

I₁₀: goto (I₆, L)

$$R \rightarrow L., \$$$

I₁₁: goto (I₆, *)

$$L \rightarrow * . R, \$$$

$$R \rightarrow \cdot L, \$ \text{ (I}_{10}\text{)}$$

$$L \rightarrow \cdot * R, \$ \text{ (I}_{11}\text{)}$$

$$L \rightarrow \cdot id, \$ \text{ (I}_{12}\text{)}$$

I₁₂: goto (I₆, id)

$$L \rightarrow id., \$$$

I₁₃: goto (I₁₁, R)

$$L \rightarrow * R., \$$$

$I_{411} : L \rightarrow *R$, $\{a, b\} \rightarrow \{a, b\}$
 $R \rightarrow \cdot L$, $\{a, b\} \rightarrow \{a, b\}$
 $L \rightarrow \cdot *R$, $\{a, b\} \rightarrow \{a, b\}$
 $L \rightarrow \cdot id$, $\{a, b\} \rightarrow \{a, b\}$

$I_{512} : L \rightarrow id$, $\{a, b\} \rightarrow \{a, b\}$
 $L \rightarrow \cdot id$, $\{a, b\} \rightarrow \{a, b\}$

$I_{713} : L \rightarrow *R$, $\{a, b\} \rightarrow \{a, b\}$
 $R \rightarrow \cdot L$, $\{a, b\} \rightarrow \{a, b\}$

$I_{810} : R \rightarrow L$, $\{a, b\} \rightarrow \{a, b\}$
 $L \rightarrow \cdot R$, $\{a, b\} \rightarrow \{a, b\}$

Parsing table, $\{a, b\} \rightarrow \{a, b\}$

	id	=	*	\$	S	L	R
0	S_{812} S_{12}		S_{411} S_{11}			2	3
1				Accept			
2		S_6		S_5			
3				S_2			
411	S_{312} S_{412}		S_{411} S_{412}		S_{10}	S_{13}	
512	S_{512}			S_4			
6	S_{812} S_{512}		S_{411} S_{412}		S_{10} S_{10}	S_{10}	
713			S_3		S_3		
810			S_5		S_5		
9				S_1			



Input string : id = id	Action
stack	shift
0	id = id \$
0 id 512	= id \$
0 L 2	reduce by L \rightarrow id
0 L 2 = 6	shift
0 L 2 = 6 id 512	shift
0 L 2 = 6 L 810	reduce by L \rightarrow id
0 L 2 = 6 R 9	reduce by R \rightarrow L - 0
0 S 1	reduce by S \rightarrow L = R
	Accept.

Shift - Reduce Parser

- » Shift - Reduce Parsing is a process of reducing a string to the start of a grammar.
- » It uses a stack to hold the grammar and an input to hold the string.

A string $\xrightarrow{\text{reduced to}}$ the starting symbols

- » Shift - Reduce parsing performs two actions.

1) Shift

2) Reduce.

- » At shift action, the current symbol/string is pushed to stack.
- » At each reduction, the symbol will be replaced by the non-terminals.
- » The symbol is the right side of the production and non-terminal is the left side of the production.

Ex -

$$S \rightarrow S + S$$

$$S \rightarrow S - S$$

$$S \rightarrow (S)$$

$$S \rightarrow a$$

Input string : $a_1 - (a_2 + a_3)$

<u>Stack content</u>	<u>Input string</u>	<u>Action</u>
\$	$a_1 - (a_2 + a_3) \$$	shift a_1
$\$ a_1$	$- (a_2 + a_3) \$$	reduce by $S \rightarrow a_1 + a_2 + a_3$
\$	$- (a_2 + a_3) \$$	shift -
$\$ S -$	$(a_2 + a_3) \$$	shift (
$\$ S - ($	$a_2 + a_3) \$$	shift a_2
$\$ S - (a_2$	$+ a_3) \$$	reduce by $S \rightarrow a$
$\$ S - (S$	$+ a_3) \$$	shift +
$\$ S - (S + a_3$	$) \$$	shift a_3
$\$ S - (S + a_3$	$) \$$	reduce by $S \rightarrow a_1$
$\$ S - (S + S$	$) \$$	shift)
$\$ S - (S + S$	$) \$$	reduce by $S \rightarrow S1S$
$\$ S - (S$	$) \$$	reduce by $S \rightarrow S1S$
$\$ S - S$	$) \$$	reduce by $S \rightarrow S - S$
$\$ S$	$) \$$	Accepted

- Q) Consider the grammar of two digit numbers.
- $$E \rightarrow 2E2 \quad \text{I/P: } 32423 \quad \text{O/P: } 32423$$
- $$E \rightarrow 3E3$$
- $$E \rightarrow 4E4$$

<u>Stack content</u>	<u>Input string</u>	<u>Action</u>
\$	32423 \$	shift 3
\$3	2423 \$	shift 2
\$32	423 \$	shift 4
\$324	23 \$	reduce by $E \rightarrow 4$
\$32E	23 \$	shift 2
\$32E2	3 \$	reduce by $E \rightarrow 2E2$

$\$ 3 E$ $3 \$$
 $\$ 3 E 3$ $\$$
 $\$ E$ $\$$
 Accepted

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UNIT - IV

formats of Intermediate code

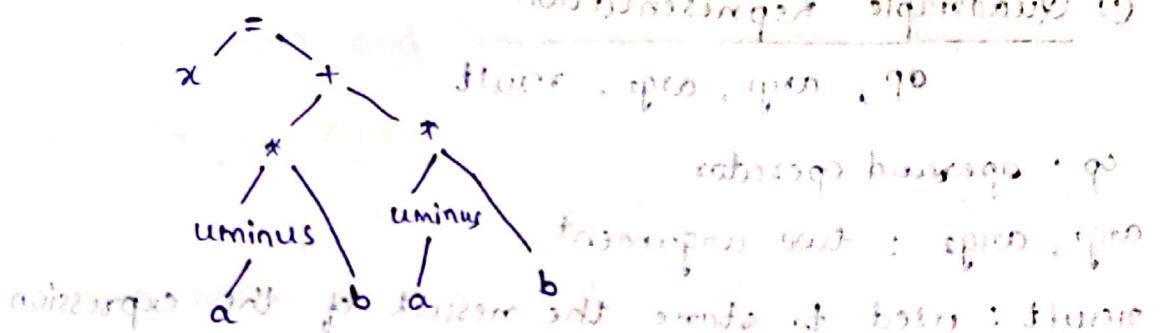
1) Abstract syntax tree

2) Polish Notation

3) 3-address code

1) Abstract Syntax Tree

$$x = (-a * b) + (-a * b)$$



2) Polish Notation

It is also called as Prefix notation, in which operators occur first and then operands are arranged.

$$+ a b * c d$$

$$** * + ab cd$$

3) Three Address Code

In three-address code form, at most 3 addresses are used to represent any statement.

General form of the 3-address code is:

$$a = b \text{ op } c$$

where, a, b, c are operands

op is operator

» Only single operation at RHS of the expression is allowed at a time.

Write 3-address code for the statement $a = b + c + d$

$$a = b + c + d$$

↓

$$t_1 = b + c$$

$$t_2 = c$$

$$t_2 = t_1 + d$$

$$a = t_2$$

3 address code

3

VI - T1U6

3

abs assignment to storage

not valid directed

multiple assign.

same variable

not valid directed

(a =) + (a =)

Implementation of 3-address code

1) Quadruples

2) Triple representation

3) Indirect triple representation.

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① Quadruple Representation

op, arg₁, arg₂, result

op : operand operator

arg₁, arg₂ : two argument

result : used to store the result of the expression.

$$(Q) \quad x = -a * b * -a * b$$

t₁ = uminus a (multiple assign. in function)

disadv temp

t₂ = t₁ * b (multiple variables)

t₃ = uminus a (hence multiple temp is used)

t₄ = t₃ * b (mem. is wasted)

t₅ = t₂ * t₄ (mem. is wasted)

(Mem is wasted).

Quadruple representation

	op	arg ₁	arg ₂	result
(0)	uminus	a		t ₁
(1)	*	t ₁	b	t ₂
(2)	uminus	a		t ₃
(3)	*	t ₃	b	t ₄
(4)	*	t ₂	t ₄	t ₅
(5)	=	t ₅		x

② Triple Representation

OP, arg1, arg2

address is used instead of temp variables.

	OP	arg1	arg2
(0)	uminus	a	
(1)	*	(0)	b
(2)	uminus	a	
(3)	*	(2)	b
(4)	*	(1)	(3)
(5)	=	(4)	

Disadv becomes difficult when an error is occurred.
When value in a mem. loc is changed, it gets overwritten and the actual value may be lost.

③ Indirect Triple Representation

Instead of using direct mem locations, we use indirect addresses that has the same value in it.
Thus, even if the values are changed, result is not affected.

	OP	arg1	arg2
(10)	uminus	a	
(11)	*	(10)	b
(12)	uminus	a	
(13)	*	(12)	b
(14)	*	(11)	(13)
(15)	=	(14)	

n	*	10
(10)	(10)	
(11)	(11)	
(12)	(12)	
(13)	(13)	
(14)	(14)	
(15)	(15)	

$$Q) \gamma = a * (b + c)$$

Quadruple:

$$\gamma = a * - (b + c)$$

$$t_1 = b + c$$

$$t_2 = \text{uminus } t_1$$

$$t_3 = a * t_2$$

~~$$\gamma = a * - (b + c)$$~~

	op	arg1	arg2	result
(0)	+ +	b	c	t1
(1)	uminus	t1		t2
(2)	*	a	t2	t3
(3)	=	t3		γ

Triplet:

	op	arg1	arg2
(0)	+	b	c
(1)	uminus	(0)	
(2)	*	a	(1)
(3)	=	(2)	

Indirect Triplet:

	op	arg1	arg2
(10)	+	(b)	c
(11)	uminus	(10)	
(12)	*	a	(11)
(13)	=	(12)	

(6)	(10)
(7)	(11)
(8)	(12)
(9)	(13)

(a) $x = - (a * b) + (c + d) - (a + b + c + d)$

Quadruple

$t_1 = a * b$	(0) $t_1 = a * b$
$t_2 = \text{uminus } t_1$	(1) $t_2 = \text{uminus } t_1$
$t_3 = c + d$	(2) $t_3 = c + d$
$t_4 = t_2 + t_3$	(3) $t_4 = t_2 + t_3$
$t_5 = a + b$	(4) $t_5 = a + b$
$t_6 = c + d$	(5) $t_6 = t_3 + t_5$
$t_7 = t_5 + t_6$	(6) $t_7 = t_4 - t_6$
$t_8 = \text{uminus } t_7$	(7) $x = t_7$
$t_9 = t_4 - t_7$	
$t_{10} = t_4 - t_7$	

	op	arg1	arg2	result
(0)	*	a	b	t_1
(1)	uminus	t_1		t_2
(2)	+	c	d	t_3
(3)	+	t_2	t_3	t_4
(4)	+	a	b	t_5
(5)	+	t_3	t_5	t_6
(6)	-	t_4	t_6	t_7
(7)	=	t_7		x

Triplet

	op	arg1	arg2	result
(0)	*	a	b	
(1)	uminus	(0)	(0)	
(2)	+	c	d	
(3)	+	(1)	(2)	
(4)	+	a	b	
(5)	+	(2)	(4)	
(6)	-	(3)	(5)	
(7)	=	* (6)	(6)	

Indirect Triple $(\text{uminus} \circ \text{add}) \circ (\text{mult} \circ \text{add}) = 0$ (1)

op	arg1	arg2	res	(o)	(o) pushing
(10)	* (1)	a + (1)	b	d + a	(1)
(11)	- uminus	c	(10)	c + d	(2)
(12)	+ b + c	(1)	d	b + c	(3)
(13)	+ a + b	(11)	(12)	a + b	(4)
(14)	+ a	b	(12)	b + a	(5)
(15)	+ (12)	(1)	(14)	d + a	(6)
(16)	+ b + c	(13)	(15)	b + c	(7)
(17)	= (16)	d + a	(17)	d + a	(8)

(Q) $a = b * -c + b * -c$ multiple minus sign

Quadruplet

$$t_1 = \text{uminus } c$$

$$t_2 = b * t_1$$

$$t_3 = t_2 + t_2$$

$$\frac{a}{b} = t_3$$

op	arg1	arg2	results	f	(o)
----	------	------	---------	---	-----

(o)	uminus	c	t1	*	(o)
(1)	*	b	t2	*	(1)
(2)	+	t2	t3	*	(2)
(3)	=	t3	a	*	(3)

Triple f

op	arg1	arg2	res	f	(o)
(o)	uminus	c	t1	*	(o)
(1)	*	b	t2	*	(1)
(2)	+	t1	t3	*	(2)
(3)	=	t2	b	*	(3)

Indirect Triplet

op	arg1	arg2	res	(o)	(o)
(10)	uminus	c	t1	*	(1)
(11)	*	b	t2	*	(2)
(12)	+	t1	t3	*	(3)
(13)	=	t2	t3	*	(4)

$$Q) x - (a+b) * (c+d) - (a+b+c)$$

$$t_1 = a+b$$

$$t_2 = c+d$$

$$t_3 = t_1 + t_2$$

$$t_4 = t_1 + c$$

$$t_5 = t_3 - t_4$$

$$x = t_5$$

$$(3+y+z) * (5+p) * (y+s) \quad (1)$$

$$y+s = t_1$$

$$y+p = s+t$$

$$s+t+p = s+t$$

$$s+t = p$$

$$3+y = p$$

$$3+y+z = p$$

Quadruples

op	arg1	arg2	result	exp	alg
(0)	+	a	b	t1	
(1)	+	c	d	t2	1000
(2)	+	t1	t2	t3	1000
(3)	+	t1	c	t4	1000
(4)	-	t3	t4	t5	1000
(5)	=	t5	x	t5	1000

Triples

op	arg1	arg2	exp	alg
(0)	+	a	b	1000
(1)	+	c	d	1000
(2)	+	(0)	(1)	1000
(3)	+	(0)	(2)	1000
(4)	-	(2)	(3)	1000
(5)	=	(4)		1000

Indirect Triples

(0)	(0)	op	arg1	arg2	x	y	z	1000
(0)	(0)	+	a	b	y	0	0	1000
(1)	(1)	+	c	d	0	1000	0	1000
(2)	(2)	+	(10)	(11)	0	0	1000	1000
(3)	(3)	+	(10)	(12)	0	0	1000	1000
(4)	(4)	-	(12)	(13)	0	0	1000	1000
(5)	(5)	=	(14)					1000

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$$(x+y+z) = (x+y) + z \text{ (associativity)}$$

$$x+y+z = x+y$$

$$x+y+z = x+z$$

$$x+y+z = y+x$$

$$x+y+z = y+z$$

$$x+y+z = z+x$$

$$x+y+z = z+y$$

$$x+y+z = z+y$$

$$x+y+z = z+y$$

$$x+y+z = z+y$$

Q) $(x+y) * (y+z) + (x+y+z) = ?$

$$t_1 = x+y$$

$$t_2 = y+z$$

$$t_3 = t_1 + t_2$$

$$t_4 = t_1 + z$$

$$t_5 = t_3 + t_4$$

$$\star y = t_5$$

Quadruplet

op	arg1	arg2	result	exp	q	o
(0)	+	x	y	t1	15	1
(1)	+	y	z	t2	15	2
(2)	*	t1	t2	t3	15	3
(3)	+	t1	z	t4	15	4
(4)	+	t3	t4	t5	15	5
(5)	=	t5	y			0

Triplet

op	arg1	arg2	exp	q	o
(0)	x	y	15	1	1
(1)	y	z	15	2	2
(2)	(0)	(1)	15	3	3
(3)	(0)	z	15	4	4
(4)	(2)	(3)	15	5	5
(5)	(4)	(5)	15	6	6

Indirect Triplet

op	arg1	arg2	exp	q	o
(10)	x	y	15	1	10
(11)	y	z	15	2	11
(12)	(10)	(11)	15	3	12
(13)	(10)	z	15	4	13
(14)	(12)	(13)	15	5	14
(15)	(14)	(15)	15	6	15

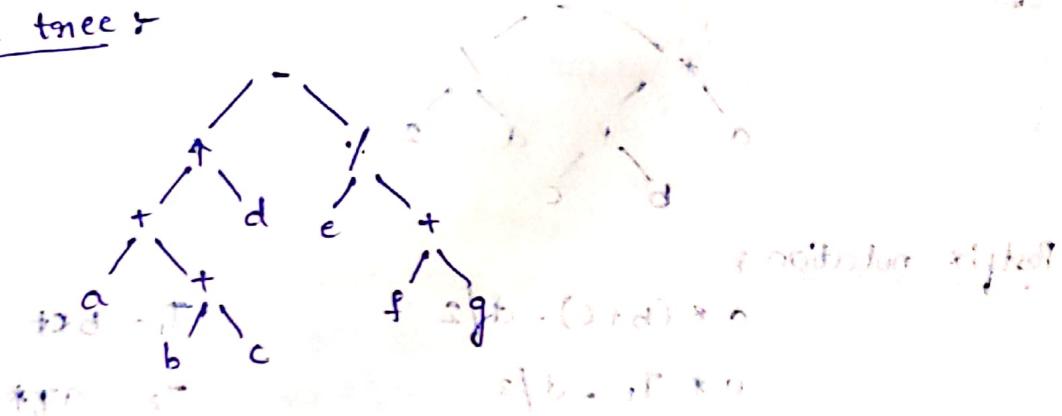
$$(10) = 15$$

$$15 = 15$$

$$15 = 15$$

Construct the syntax tree and post fix notation for the following expression $r = (a + (b + c)) \uparrow d - e / (f + g)$

Syntax tree r



Postfix notation : In this expression, the arrangement is
op₁, op₂, op

$$a + (b + c) \uparrow d - e / (f + g) \text{ where } T_1 = bc +$$

$$a + T_1 \uparrow d - e / (f + g) \text{ where } T_2 = aT_1 +$$

$$T_2 \uparrow d - e / (f + g) \text{ where } T_3 = T_2 d \uparrow$$

$$T_3 - e / (f + g) \text{ where } T_4 = fg +$$

$$T_3 - e / T_4 \text{ where } T_5 = eT_4 /$$

$$\text{and } T_6 = T_3 T_5 -$$

(and) arranging by T₆ & substituting the values of temp. variables

Now, backward substituting the values of temp. variables

$$T_6 \quad (c, g, f, v) = 0$$

$$\Rightarrow T_3 T_5 - \quad \text{both b and e are op}$$

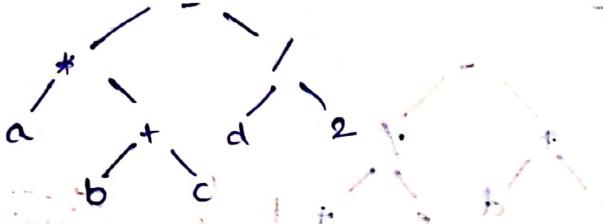
$$T_3 e T_4 / - \quad \text{both c and d are op}$$

$$T_3 e f g + / - \quad \text{both f and g are op}$$

$$T_2 d \uparrow e f g + / - \quad \text{both a and b are op}$$

$$a T_1 + d \uparrow e f g + / - \quad \text{both a and b are op}$$

$$a b c + d \uparrow e f g + / - \quad \text{both a and b are op}$$

Q) $a * (b+c) - d/2$ having three root categories with 3 children each
syntax tree: 

Postfix notation:

$$a * (b + c) - d / 2$$

$$a * T_1 - d / 2$$

$$T_1 = b + c$$

$$T_2 = a * T_1$$

$$\begin{aligned} & \text{Transformations: } T_1 = b + c \rightarrow T_2 = T_1 - d / 2 \rightarrow T_3 = d / 2 / \text{fixed} \\ & T_2 = T_3 \\ & T_4 = T_2 T_3 - \\ & T_4 = 90, 270, 180 \end{aligned}$$

$$\Rightarrow abd = T_4 \cdot T_1 \cdot (p+q) \cdot \{p + b\} \cdot (p+q) \cdot ab$$

$$abd = T_2 T_3 - (p+q) \cdot \{p + b\} \cdot T \cdot ab$$

$$abd = T_2 d / 2 - (p+q) \cdot \{p + b\} \cdot ab$$

$$abd = T_2 d / 2 - (p+q) \cdot \{p + b\} \cdot ab$$

$$abd = T_2 d / 2 - (p+q) \cdot \{p + b\} \cdot ab$$

UNIT - 2 (last topic)

* Chomsky hierarchy of languages and recognizers (5m).

The grammar is represented with four tuples notation.

$$G = (V, T, P, S)$$

These grammars are divided into 4 types based on Chomsky hierarchy.

Type - 0 : unrestricted grammar

Type - 1 : Context sensitive grammar

Type - 2 : Context free grammar

Type - 3 : Regular grammar

- Type - 0 (Unrestricted Grammars) :-
- The languages accepted by these grammars are called Recursively enumerable languages.
 - The languages are accepted by Turing machine.
 - Each production is in the form of $\alpha \rightarrow \beta$ where;
 $\alpha, \beta \in (VUT)^*$ comb' q \leftarrow
terminal & non-terminal
 - α must contain atleast one non-terminal symbol.
 - Ex:- $aA \rightarrow aBCd$ (✓) $ab \rightarrow dC$ (✗)
 $D \rightarrow F$ (✓)

Type - 1 (Context Sensitive Grammar) :-

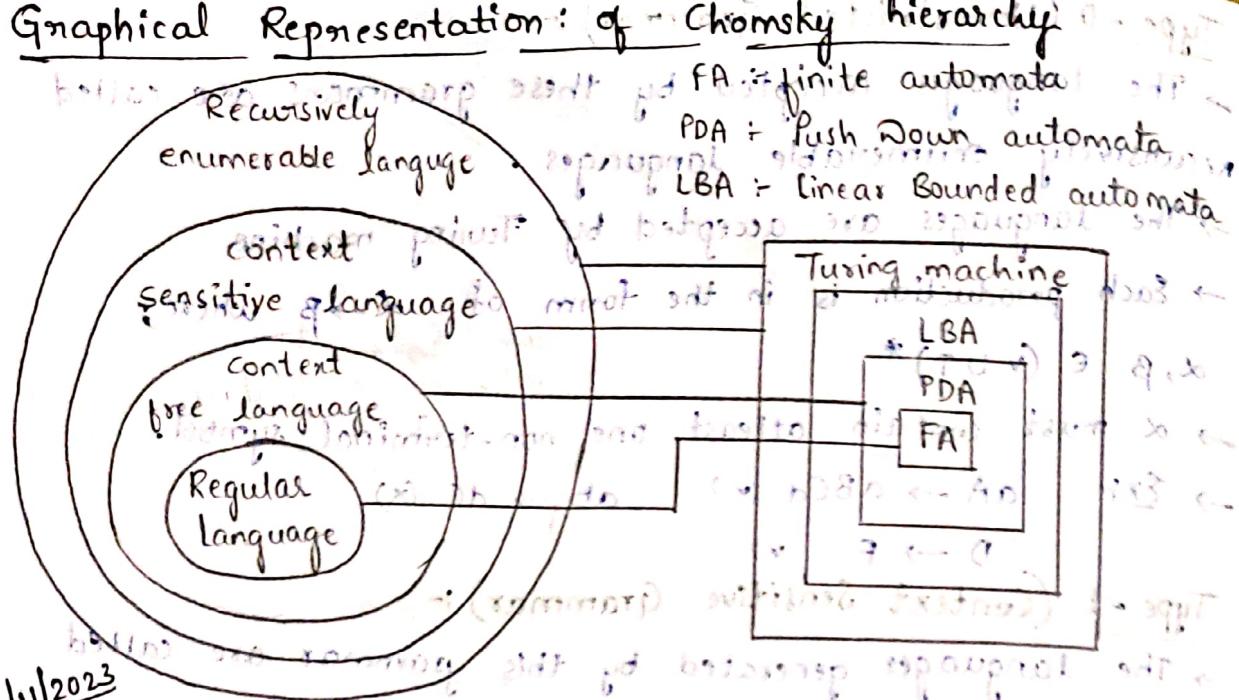
- The languages generated by this grammar are called Context Sensitive languages.
- The automata that accepts context sensitive languages is Linear bounded automata.
- The production rule is in the form of $\alpha \rightarrow \beta$ where;
 $\alpha, \beta \in (VUT)^*$ and $|\alpha| \leq |\beta|$
- Ex:- $aA \rightarrow aAB$ (✓)
 $aA \rightarrow B$ (✗)

Type - 2 (Context Free Grammar) :-

- The language generated by this grammar is called Context free language.
- These grammars are accepted by Push Down Automata.
- The production rule is in the form of $\alpha \rightarrow \beta$ where;
 $\alpha \in V^*$ only. and $|\alpha| = |\beta|$ or $|\alpha| > |\beta|$
- Ex:- $E \rightarrow E + T$ or $E \rightarrow E * T$

Type - 3 (Regular Grammars) :-

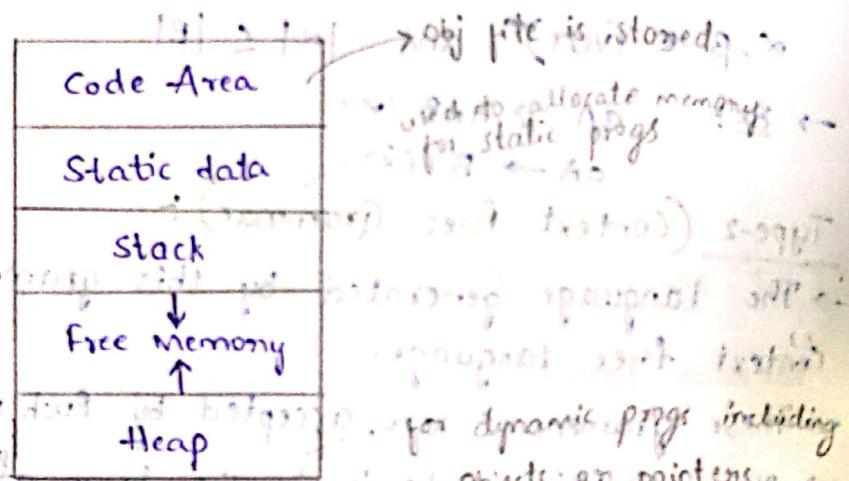
- This grammar generates regular languages.
- Regular languages are accepted by finite automata.
- The production rule is in the form of $\alpha \rightarrow \beta$ where;
 $\alpha \in V^*$ and $|\alpha| = 1$
- Ex:- $S \rightarrow a1aA$ Right linear (a followed by A)
- or $S \rightarrow a1Aa$ Left linear (A followed by a)



Storage Organization

Runtime environment / Runtime Storage management

* Sub-division of Runtime memory



Code Area: It stores the target executable code (object code)

Static Data: It is mainly useful to store static variables as well as global variables. Global variables are used throughout the program. Static variables means, the value of variable is persistent between different function calls.

Stack & Heap: In order to utilize the space in effective manner Heap and stack are used. They grow opposite to each other.

Stack: It works on the principle Last In First Out. Whenever a function is called activation record is created. To store the activation record information, stack is used. The record is pushed onto the top of the stack.

- Heap: To allocate the memory dynamically.
- These two data structures are used, depending on the situations.
 - If there are too many functions or procedures, then stack is used more often.
 - The free memory is mostly occupied by the stack.
 - If there are too many pointers on dynamic variables, then we need to allocate memory. This is done by using Heap.

Activation Record **

- The activation record is a block of memory used for managing information needed by a single execution of a func/proc.
- The content of activation record is shown below:
- Various fields of activation record are:

Temporary values: The temporary variables are needed during the evaluation of expressions, such variables are stored in the temporary field of activation record.

Local variables: The local data is a data that is global to the execution of a procedure. This field stores the local data.

Saved Machine registers: This field holds the info regarding the status of the machine just before the procedure is called. This field contains machine registers & program control.

Control link: This field is optional. It points to the activation record of the calling procedure. Also called as Dynamic Link

Access link: It is optional. It refers to the non-local data in other activation record. Also called as static link.

Actual Parameters: It holds the info about the actual parameters. These params are passed to the called procedures.

Return value: This field is used to store the result of a function call.

at Return Value
Actual Parameters
Control link (Dynamic Link)
Access link static (link)
saved machine status
local variables
Temporaries

The size of each field of activation record is determined at the time when a procedure is called for the first time.

* Storage Allocation Strategies

24/11/2023

Parameter Passing

1. Call by value: ~~Actual part of passing parameter is passed to function~~. ~~No change in original parameter~~.
2. Call by reference: ~~Actual part of passing parameter is passed to function~~. ~~parameter storage of bus~~.
3. Copy storage
4. Call by name: ~~parameter to field n is because material of call to function~~

Two types of parameters:

- (1) Actual Parameters are the variables specified in function call.
- (2) Formal Parameters are the variables declared in the definition of the called function.

1-value : refers to the storage.

or value : ref content in the storage. 1-value & value

- 1) Call by Value
- Actual parameters are evaluated and their r-values are passed to the called procedures.

Caller evaluates the actual parameters and places or-value in the storage for formals.

Call has no effect on the activation record of the caller.

Ex: void swap(int x, int y){

 int t;
 t = x;
 x = y;
 y = t;
}

void main(){
 int a=1, b=2;
 swap(a, b);
 printf("a=%d, b=%d", a, b);

}

Output : a=1, b=2

3) call by reference / call by address
The caller passes a pointer to each location of actual parameters. If actual parameter is a name then, l-value is passed. If actual parameter is an expression, then it is evaluated in a new location and the address of that location is passed.

Ex: void swap (int *x, int *y){

```
    int t;  
    t = *x;  
    *x = *y;  
    *y = t;  
}
```

void main() {

```
    int a=1, b=2;
```

```
    swap (&a, &b);
```

printf ("a=%d, b=%d", a, b);

Output: a=2, b=1

3) copy/mestone It is a hybrid method b/w call by value & call by reference.

It is also called by "copy in - copy out" (CIO). Value + result. Caller evaluates actuals and passes r-values to formals. l-values of actual parameters are determined before function call.

When control returns, r-values of formals are copied back into l-values of the actuals.

Ex: int y;

```
copymestone (int x){
```

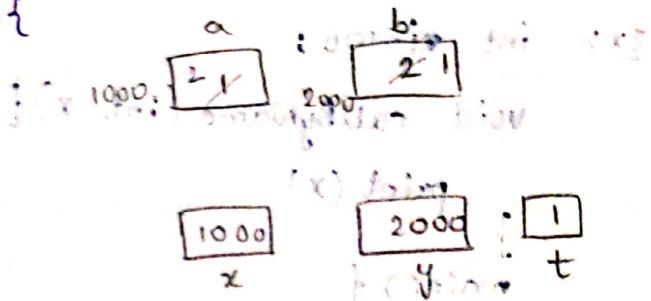
```
    int y=20;  
}
```

```
main() {  
    y=10;
```

```
    copymestone(y);  
    print(y);
```

```
}
```

Output: y=2



After control is returned to the main procedures, the r-value of $f(x)$ must be copied to the l-value of y .

4) Call by name

Actual parameters are substituted for their formals.

It is also called as Macro Expansion (in) Inline Expansion.

Ex:- int $i=100;$

```
void callByName (int x){  
    print (x)  
}  
main() {  
    callByName (i=i+1)  
}
```

$i(i+1)$ gave $i=101$

$\boxed{101} + \boxed{i}$

$i^* + i$

$i \boxed{101} + i^*$

↓ creation bias

↓ add, i = $i+1$.

O/P :- 101

Language facilities for Dynamic Storage Allocation

The data under program control can be allocated dynamically.

This allocation is done from heap memory.

There are two types of approaches used to allocate.

(1) Implicit Allocation

(2) Explicit Allocation

Explicit Allocation

This is a kind of memory allocation that can be done with the help of some procedures. For example, In Pascal, memory allocation is done using "new" function, and deallocation is done using "dispose".

Implicit Allocation

It is a kind of allocation that can be done automatically for storing the results of expression evaluation.

Ex:- LISP

SNOBOL

(12) Garbage Collection

It is a substantial amount of memory which gets allocated dynamically but, it is unreachable memory.

If this memory remains unreachable then, it becomes waste of memory. Hence, a new technique called Garbage collection is introduced.

Java and Lisp are the languages that use this technique.

* Dangling reference

It is a kind of complication that occurs due to explicit deallocation of memory. The dangling reference is a kind of reference that gets de-allocated which is referred to.

```
int dangle() {  
    int i = 20; // i is local to dangle().  
    return &i;  
}  
  
main() {  
    int *p;  
    p = dangle();  
}
```

Block Structure & Non-Block Structure Storage allocation

The storage allocation can be done for two types of data variables.

(i) Local data

(ii) Non-local data

Local data can be handled using activation records.

Non-local data can be handled using scope information.

Access to non-local names / data:

Scope rules of a language can be determined by references to non-local names.

There are two types of scope rules.

(1) Lexical / static scope rules.

(2) Dynamic scope rules.

Lexical or static scope rules & Dynamic scope rules

- » Determinates the declarations applicable to a name at compile time.
↳ Lexical scope/static scope
- Determinates the declarations applicable to a name at run time.
↳ Dynamic scope

» static scope is implemented by two methods:

- (1) Access Link
- (2) Display

• Dynamic scope is implemented by two methods:

1. (1) Deep access for non-local variables.
2. (2) Shallow access for local variables.

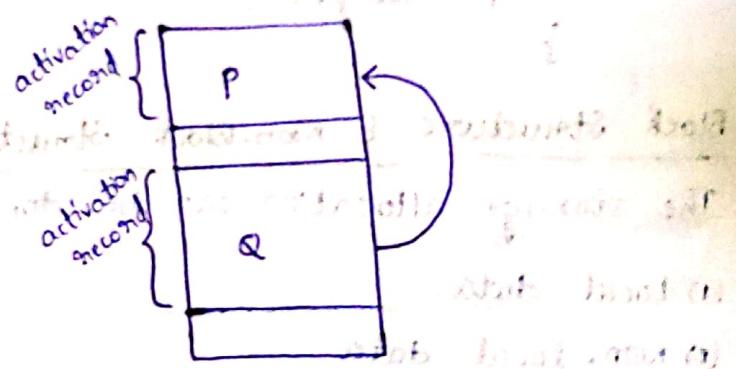
(1) Access Link :-

The implementation of lexical scope can be obtained by using pointer to each activation record. These pointers are called Access Link.

If a procedure Q is nested within procedure P, then access link of Q points to access link of most recent activation record of procedure P.

Ex:- P {

```
    Q {
        .
        .
        .
    }
```



(2) Display :-

It is expensive to traverse down access link everytime when a particular non-local variable is accessed.

To speed up the access to non-locales, it can be achieved by maintaining an array of pointers called Display.

In display :-

- » an array of pointers to activation records is maintained.
- » array is indexed by nesting levels.
- » the pointers point to only accessible activation record.

"the display changes when a new activation occurs and it must be reset when the control returns from the new activation."

Ex:- P₀ depth = 1

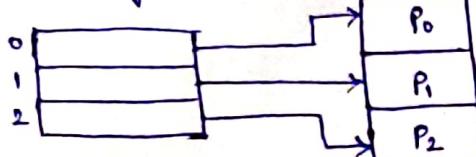
P₁ depth = 2

[P₂ depth = 3]

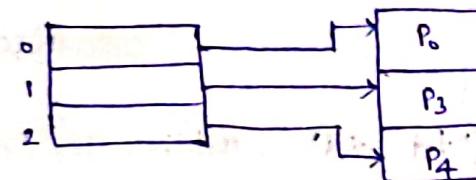
P₃ depth = 2

[P₄ depth = 3]

Display



If procedure is main's then, depth = 1



Procedures

Comparison between Access Link & Display

Access Link

- 1) Access link will take more time to access especially when non-local variables are at many levels.
- 2) It requires less space.

Display

- 1) Display is used to generate the code efficiently.
- 2) It requires more space at run time.

(1) Deep Access

To keep the stack of active variables, use control link instead of access link.

When you want to find a variable, then search the stack from top to bottom looking for most recent activation record that contains the space for desired variables.

In this method, a symbol table needs to be used at runtime.

(2) Shallow Access

Keep a central storage with one slot for every variable name. If the names are not created at run time, then the storage layout can be fixed at compile time. Otherwise, when new activation of procedure occurs, then that procedure changes the storage entries for its locals at entry and exit.

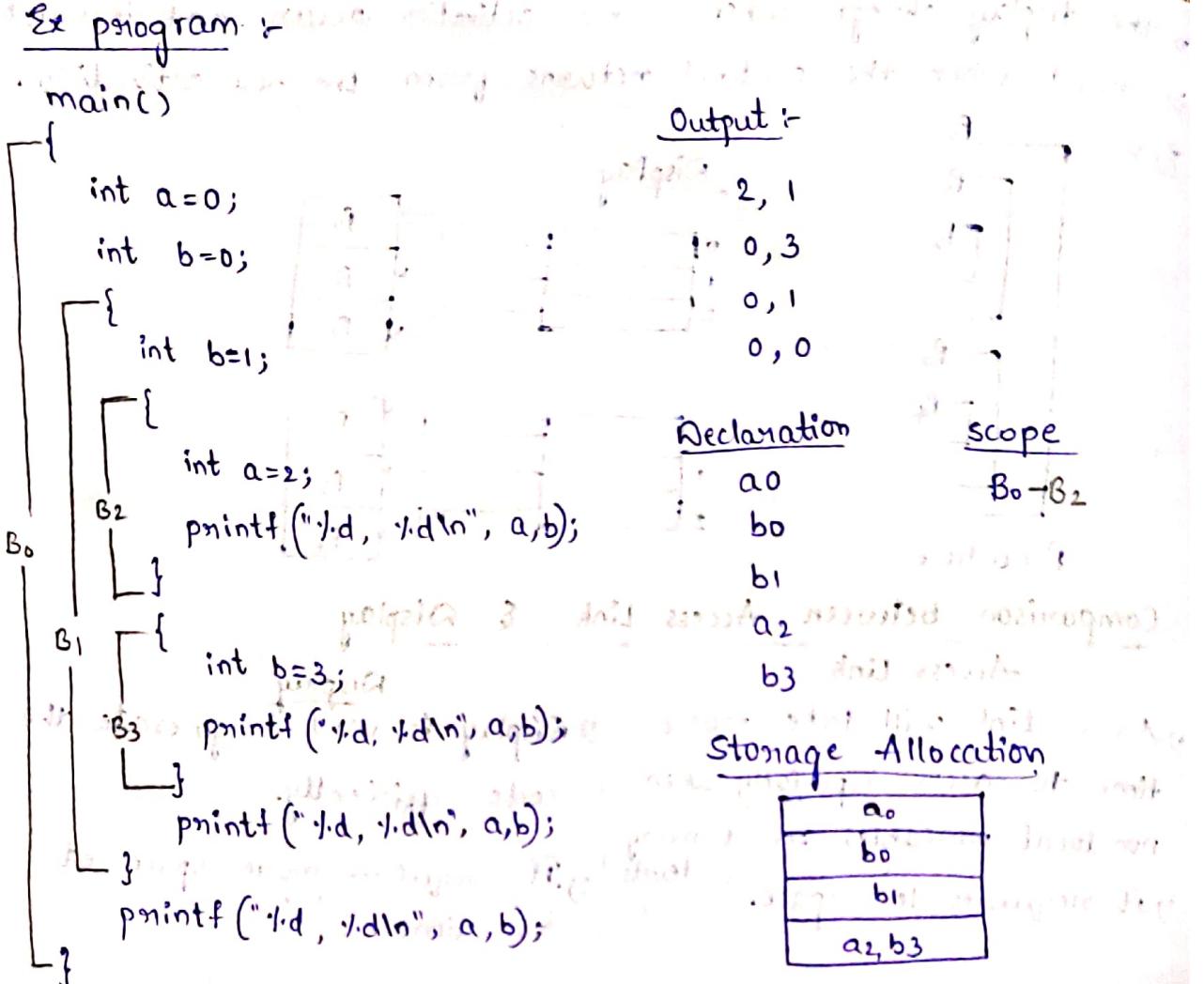
Difference b/w Deep Access and Shallow Access.

Deep Access

- 1) It takes longer time to access the non-locales
- 2) It needs a symbol table at run time

Shallow Access

- 1) It allows fast access.
- 2) It has overhead of handling procedures entry & exit.



* 6/12/2023

UNIT - 5

Principle sources of Optimization / Code Optimization Techniques

Machine Independent & Dependent Optimization Codes :- properties of target code uses

→ Machine independent optimizations are program transformations that improve target code without taking into consideration any properties of target machine.

→ Machine dependent optimizations are based on register allocation and utilization of special machine instruction sequences.

Advantages of Code Optimization

- » Takes less time to execute the optimized code.
- » Less consumption of memory.

The meaning shall
be preserved.

Code Optimization Techniques

- 1) Common sub-expression elimination
- 2) Constant folding
- 3) Copy propagation
- 4) Dead code elimination
- 5) Code motion
- 6) Induction variable elimination & Reduction in strength.

① Common sub-expression elimination

It is done if -

- it was previously computed

- values of variables have not changed.

Ex: $a = b + c$

$b = \boxed{a-d} \Rightarrow$ value of b is changed

$c = b + c \Rightarrow$ since b is changed, $(b+c)$ is not common sub-expression

$d = \boxed{a-d} \Rightarrow$ both a & d values are not changed.

& $(a-d)$ is already computed as $b = a-d$.

So, the optimized code is -

$a = b + c$ common sub-ex

$b = a-d$ common sub-ex

$c = b + c$ common sub-ex

$d = b$ common sub-ex

If the value of an expression is constant, use the

② Constant folding (performed at compile time)

Evaluate the expression & submit the result of expression.

Ex: $\text{area} = \left(\frac{22}{7}\right) * \pi * r$

Here, $\frac{22}{7}$ is evaluated & and the result 3.14 is used.

$\Rightarrow \text{area} = 3.14 * \pi * r$

③ Copy propagation

Here, the constant value replaces a variable

Ex: $\pi = 3.14, r = 5$

$\text{area} = \pi * \pi * r$

$\Rightarrow \text{area} = 3.14 * 5 * 5$

no need of degrading when values are known in advance

Copy propagation :- duplication is not required.

④ Dead code elimination

It includes elimination of the statements which are never executed or even if executed, when the o/p is never used.

Ex: $i=0;$ Here, when i is initialized as 0
 $\text{if } (i==1) \{$ the expression $(i==1)$ never becomes true
 $\quad\quad\quad a=x+i; \quad \&$ its statements are never executed.
 $\}$

So, $\text{pri} \text{int } i=0; \text{ int } a=0; \text{ if } (i==1) \{ \text{ print } a; \}$ will not print anything.

Ex: int add (int x, int y){

int z;
 $\quad\quad\quad z = x+y;$
 $\quad\quad\quad \text{return } z;$
 $\}$ $\text{print } ["\cdot.d", z];$

so, int add (int x, int y){
 $\quad\quad\quad \text{int } z;$
 $\quad\quad\quad z = x+y;$
 $\quad\quad\quad \text{return } z;$
 $}$

the further stmts are not executed.
 Here, print statement is never executed.

A variable is live, if its value can be used subsequently in the program; otherwise it is called dead.

$$\begin{array}{l} \text{dead } \\ \quad\quad\quad x = a+b \\ \quad\quad\quad y = a+b \end{array}$$

⑤ Code motion:

It is a technique which moves the code outside the loop; if it doesn't make any difference, in the values before or after when executed inside or outside the loop.

Ex: $\text{for } (i=0; i<100; i++) \{$ for loop has no effect on $x=y+z.$
 $\quad\quad\quad x = y+z;$ Its value is not effected even if it outside the loop.
 $\quad\quad\quad a[i] = 6*i;$ it outside the loop.
 $\}$ If it is loop invariant computation, only then we can move it outside the loop.

so, $x = y+z;$

$\text{for } (i=0; i<100; i++) \{$

$a[i] = 6*i;$

Moves the code outside of a loop

$\cdot x = y+z$ is called as

"Loop Invariant computation"

$i = i+1$ is "Loop Variant computation"

⑥ Induction variable elimination & reduction in strength:

To reduce the strength; we replace the complex expensive operators with those having less strength. Expensive operators are replaced with cheaper operators.

Ex: $b = a * 2$

Instead, $b = a+a.$

Replace exponential Induction variable is the by multiplication loop control variable.

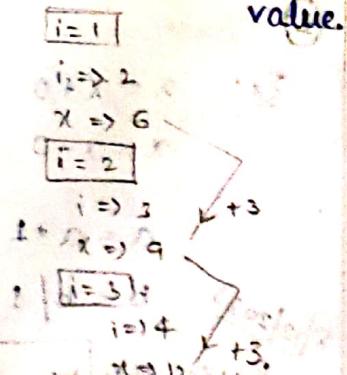
If the value of any variable in any loop gets changed every time, then the variable is called as Induction Variable. With each iteration, its value either gets incremented or decremented by some constant value.

Ex: B1 upon every increment of i by 1,
 $i := i + 1$ $x := x + 3$ gets incremented by 3
 $x := 3 * i$

$y := a[x]$ So, instead of using
 $y := a[x]$ i in $x := 3 * i$
if $y < 15$, goto B2 we can use,

So, B1 $i := i + 1$
 $x := x + 3$.

$y := a[x]$
if $y < 15$, goto B2



B1

Ex: $i = 1;$ initial value $t = 0;$ $t \leq 10$
while ($i < 10$) while ($t < 36$)
{ {
 $t = i * 4;$ $t = t + 4;$
 $i = i + 1;$ }
}

Transformation on Basic block

It is classified into 2 types:

- Structure preserving transformation
- Algebraic preserving transformation

- (i) Common sub expression elimination
- (ii) Dead code elimination
- (iii) Renaming of temp vars
- (iv) Interchange of 2 independent adjacent stmts

i)

$$\text{(i)} \quad \begin{array}{l} \text{Ex: } x = y + z \\ y = z - w \\ z = y + z \\ w = x - w \end{array} \quad \Rightarrow \quad \begin{array}{l} x = y + z \\ y = x - w \\ z = y + z \\ w = y \end{array}$$

$$\text{(ii)} \quad \begin{array}{l} \text{B1: } \begin{cases} a = a + 2 \\ b = b + c \end{cases} \\ \text{B2: } \begin{cases} b = b + c \\ c = b + 2 \end{cases} \end{array} \quad \Rightarrow \quad \begin{array}{l} \{b = b + c\} \\ \{b = b + c \\ c = b + 2\} \end{array}$$

$$\text{(iii)} \quad \begin{array}{l} t_1 = x * y \\ t_2 = z - t_1 \\ t_3 = t_1 * w \end{array} \quad \Rightarrow \quad \begin{array}{l} t_1 = x * y \\ t_2 = z - t_1 \\ t_3 = t_1 * w \end{array}$$

preserving $x * y$ in t_1 &
 $x * y * z$ in t_3

(iv) $t_1 = x * y$, $t_2 = z - t_1$, $t_3 = t_1 * w$

$$t_1 = x * y \Rightarrow t_1 = x * y$$

$$t_2 = z - t_1 \Rightarrow t_2 = z - t_1$$

$$t_3 = t_1 * w \Rightarrow t_3 = t_1 * w$$

$$w = t_2 + t_3$$

Ex: $x = x + 0$
 $x = x - 0$
 $a = a * 1$
 $b = b / 1$

Basic Blocks and control flow Graphs

Algorithm to make Basic Blocks

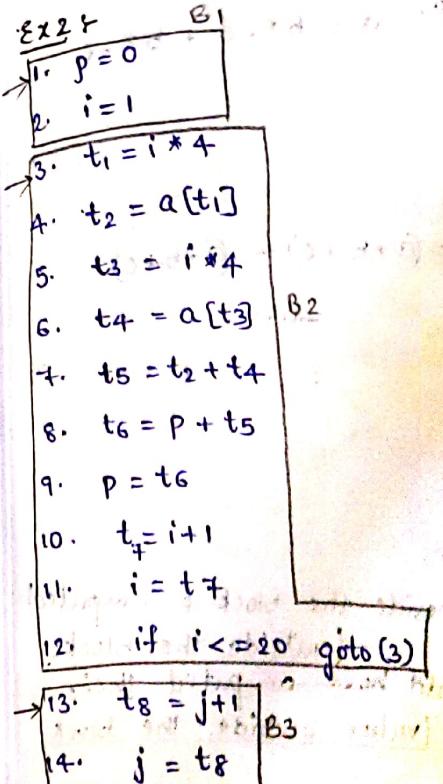
- Identify the leader (1st line of code)
- First line of the code is leader.
- Address of conditional and unconditional goto are leaders.
- Immediate next line of goto are leaders.
- Make basic block from leader to line before next leader.

Exit Basic Blocks

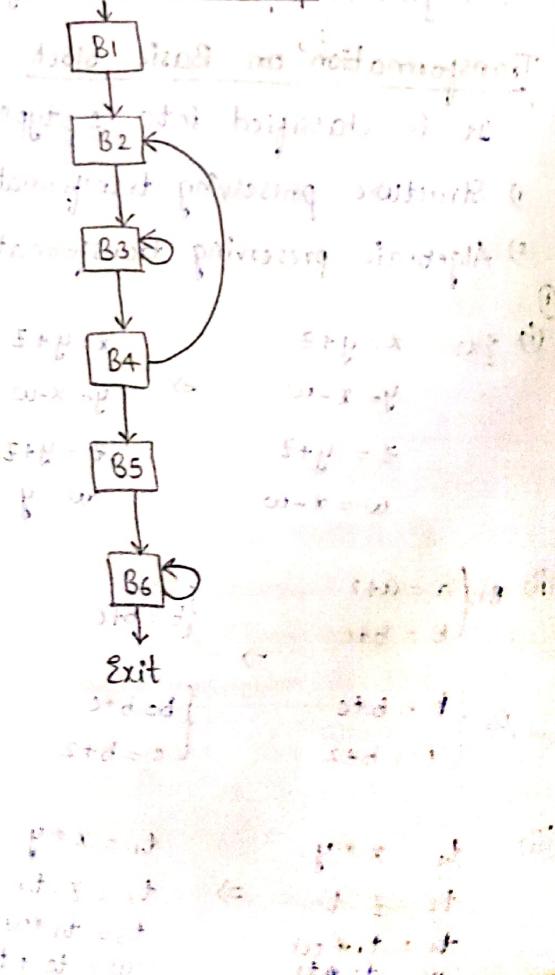
- 1. $i = 1$ B1
- 2. $j = 1$ B2
- 3. $t_1 = 10 + j$
- 4. $t_2 = t_1 + j$
- 5. $t_3 = 8 * t_2$
- 6. $t_4 = t_3 - 8$
- 7. $a[t_4] = 00$
- 8. $j = j + 1$
- 9. if $j < 10$ goto (3)
- 10. $i = i + 1$
- 11. if $i < 10$ goto (2) B4
- 12. $i = 1$ B5
- 13. $t_5 = i - 1$
- 14. $t_6 = 8 * t_5$
- 15. $a[t_6] = 10$
- 16. $i = i + 1$
- 17. if $i \leq 10$ goto (13) B6

These type of algebraic transformations can be done for improving the basic blocks.

Control flow graph
represent basic block and
» We can draw directed edges
, there is conditional or
Block 2 immediately follows Block 1



Control Flow Graph



DAG representation of the expression

- DAG \Rightarrow Directed Acyclic Graph
- DAG determines common subexpression elimination
 - In DAG, heads are leaf nodes
 - Interior nodes are operators
 - Internal nodes also represent common subexpressions

Ex3 $a = b + c$
Here, $b = a - d$,
 $(a-d)$ is common subexpression.
the common subexpression $c = b + c$
 $d = a - d$



Control Flow Graph: It is a directed graph, in which nodes represent basic block and edges represent flow of control.
 "We can draw directed edge from Block 1 to Block 2 if it
 , there is conditional or unconditional jump from block 1 to
 , Block 2 immediately follow Block 1

Ex2: B_1

1. $p = 0$
2. $i = 1$
3. $t_1 = i * 4$
4. $t_2 = a[t_1]$
5. $t_3 = i * 4$
6. $t_4 = a[t_3]$
7. $t_5 = t_2 + t_4$
8. $t_6 = p + t_5$
9. $p = t_6$
10. $t_7 = i + 1$
11. $i = t_7$
12. if $i \leq 20$ goto (3)
13. $t_8 = j + 1$
14. $j = t_8$

code :

begin

$p = 0$

$i = 1$

do begin

$p = p + a[i] * b[i]$

$i = i + 1$

end

while ($i \leq 20$)

$j = j + 1$

end

block 2

Entry

B_1

B_2

B_3

Exit

* DAG representation of the Basic Blocks

DAG \Rightarrow Directed Acyclic Graph

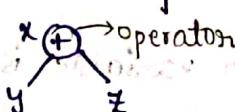
» DAG determines common sub-expressions.

, In DAG, leaves are labelled by variable names or constants.

» Interior nodes are operators.

» Internal nodes also represent the result of the expression.

Ex1: $x = y + z$

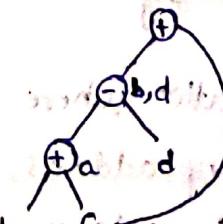


Ex2: $a = y + z$

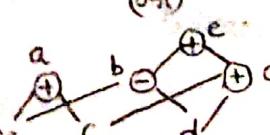
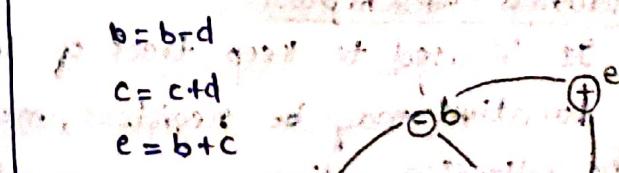


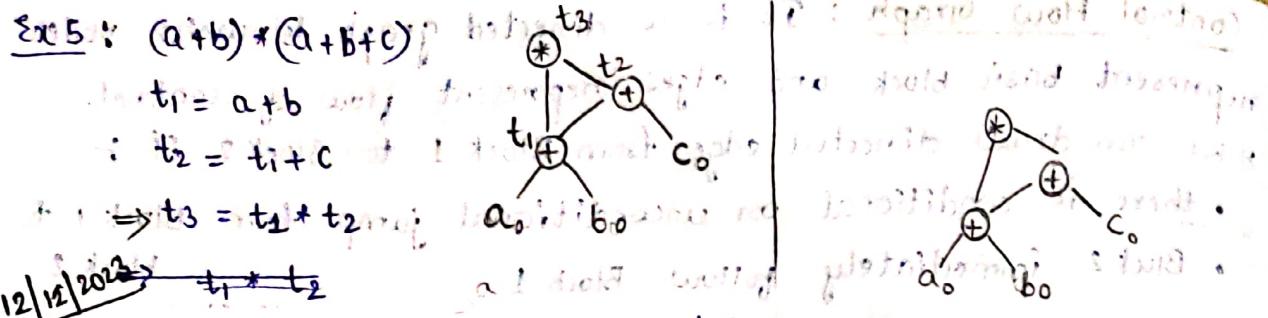
Ex3: $a = b + c$

$b = a + d$,
 $c = b + d$,
 $d = a - d$



Ex4: $a = b + c$

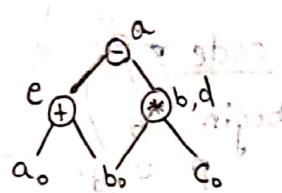




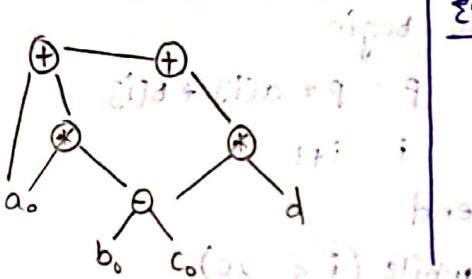
12/12/2023 $t_1 = t_1 + t_2$

Ex 6:

$$\begin{aligned} d &= b * c \\ e &= a + b \\ b &= b * c \\ a &= e - d \end{aligned}$$



Ex 7: $a + a*(b-c) + (b-c)*d$



Applications of DAG

- » Determines the common sub-expressions.
- » Determining which names are used inside the block & computed outside the block.
- » Determining which stmts of the block could have computed their value outside the block.
- » Simplifying one list of quadruples by eliminating the common sub-expressions.

Code Generation Algorithm

A simple code generator algorithm :-

- » It generates the target code for a sequence of instructions.
- » It uses a function getReg() to assign registers to variables.
- » It uses two data structures → register descriptor ; address descriptor

Register Descriptor

It is used to keep track of which variable is stored in register.

Initially, all the registers are empty.

Address Descriptor

It is used to keep track of location where variable is stored.

Location may be registers, memory addrs, stack, etc.

The following actions are performed by code generator for an instruction $x = y \text{ op } z$ assumes that 'L' is location where the addr of $y \text{ op } z$ is stored

- 1) Call the function generate to get the location of L, register descriptor.
- 2) Determine the present location of y by consulting its address.
- If y is not present in location L, then generate the instruction [descriptor].
- 3) mov y, L to copy the value of y to L
- 4) The present location of z is determined using step 2, and the instruction is generated as ~~mov z to op z~~ op_z', L
- 5) Now, L contains the value of $y op' z$ that is assigned to x
- If L is a register then, update its descriptor that it contains the value of x. Update the address descriptor of x to indicate that it is stored in address L. x is now available.
- 6) If y and z have no future use, then update the descriptors to remove y and z from memory. This marking has ended.

$$\text{ex: } d = (a-b) + (a-c) + (a-c)$$

$$t_1 = a-b$$

$$t_2 = a-c$$

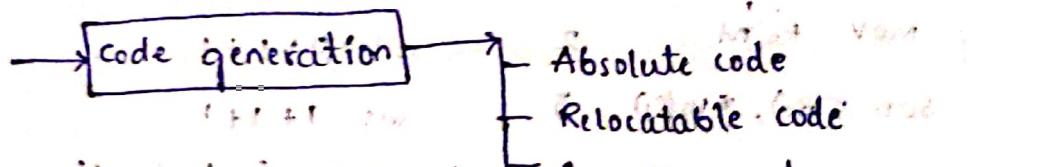
$$t_3 = t_1 + t_2$$

$$t_4 = t_3 + t_2$$

$$d = t_4$$

Statement	Code generation	Register descriptor	Address descriptor
$t_1 = a-b$	MOV a, R ₀ SUB b, R ₀	R ₀ contains t ₁	t ₁ in R ₀
$t_2 = a-c$	MOV a, R ₁ SUB c, R ₁	R ₁ contains t ₂ R ₀ contains t ₁	t ₂ in R ₁ t ₁ in R ₀
$t_3 = t_1 + t_2$	ADD R ₁ , R ₀	R ₀ contains t ₃ R ₁ contains t ₂	t ₃ in R ₀ t ₂ in R ₁
$d = t_3 + t_2$	ADD R ₁ , R ₀	R ₀ contains d	d in R ₀

3/12/2022 Object Code forms



Absolute code: It is a machine code that contains references to actual addresses within program's address space. The generated code can be placed directly in the memory and the execution starts immediately.

Relocatable code: Producing a pre-locatable machine language program

as output allows sub-programs to be compiled separately. A set of relocatable object modules can be linked together and loaded for execution with the help of linker/loader.

The advantages of generating relocatable machine language code is that the flexibility to compile sub-programs separately and to call other previously compiled program from an object module.

Assembler code: Producing an assembly language program as opposed to handwritten code makes the process of code generation easier - we can generate symbolic instructions and use the macro facilities of the assembler to help in generation of code. But, generating assembler code all by hand makes code generation slower, because assembling, linking & loading is required.

Cost of the Instruction

<u>Addressing mode</u>	<u>(src)</u> <u>from</u>	<u>(dest)</u> <u>address</u>	<u>Added Address cost</u>
Absolute	M (memory)	M	1
Register	R	R	0
Indexed	c(R)	c + content (R)	1
Indirect register	*R	content (R)	0 + 1 = 1
Indirect indexed	* c(R)	content + content (R)	1
Literal	#C	C	1

The cost of the instruction can be computed as,

1 + cost associated with source & destination addressing modes given by the added cost:

<u>Ex:</u>	<u>MOV R0, R1</u>	<u>cost</u>	<u>interpretation</u>
		1	cost: 0 + 0 + 1
	<u>MOV R0, M</u>	2	cost: 0 + 1 + 1

SUB S(R0), *10(R1) cost: 1 + 1 + 1

Q) Compute the cost of following set of instructions.

- Given cost & interpretation
- a) MOV a, R0, cost: 1 + 0 + 1
 - b) ADD b, R0, cost: 1 + 0 + 1
 - c) MOV R0, C cost: 0 + 1 + 1

Total cost: 6

a) Compute the cost of following set of instructions.

MOV *R1, *R0; cost: $0+0+1 = 1$, read + write
ADD *R2, *R1; cost: $0+0+1 = 1$, read + write
Total cost: 2

Mov B, R0 $1+0+1 = 2$ (for "BX = R0") reading
Add C, R0 $1+0+1 = 2$ writing
Mov R0, A $0+1+1 = 2$ writing with R0
Total cost: 6

Mov B, A $1+1+0 = 3$ reading + writing with R0
Add C, A $1+1+0 = 3$ reading + writing with R0
Total cost: 6

4/12/2023

Peephole Optimization (done on target code)

This technique works locally on source code to small portion

transform it into an optimized code.

Peephole optimization is a short sequence of peephole-target instructions that can be replaced by short or longer faster sequence of instructions.

It examines at most a few instructions transforming into other less expensive ones, such as turning multiplication of x by 2 into an addition of x with itself. ($x \times 2 \Rightarrow x+x$)

Characteristics

- Redundant instruction elimination
- Unreachable code
- Flow of control optimization
- Algebraic simplification

1. Redundant Instruction elimination: At source code level, the following can be done by the user:

Ex 1: $y = x + y$ if $y = x + 5$
constant: $i = y$; $\Rightarrow k = y + 10$
 $z = i$
 $K = z + 10$

Ex 2:
int.add_ten(int x){
 int add_ten(int x)
 {
 int y, z;
 y = 10;
 z = x + y;
 return z;
 }
}

2. Unreachable Code: It is a part of program code that is never accessed because of program constructs. Programmers may have accidentally written a piece of code, that can never be reached.

Ex: int add_ten(int x){
 return x+10; } → return x+10;
 printf("x=%d", x); }.

In this function, printf statement is never executed as program control returns before its execution. Hence printf can be removed.

3. Flow of control Optimization: These are instances in a code where the program control jumps back & forth without performing any significant task. So, these jumps can be removed.

Ex: goto L1
 L1: goto L2
 L2: goto L3
 L3: Mov a, R0

goto L3
 L1: goto L3
 L3: Mov a, R0

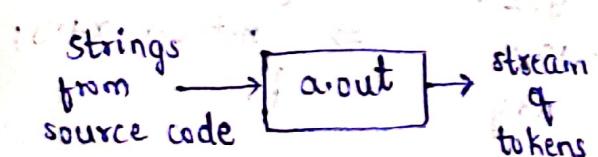
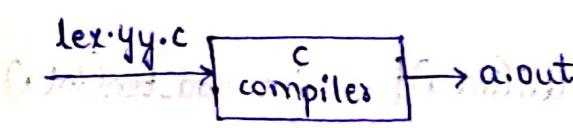
4. Algebraic Simplification: There are some situations where algebraic expressions can be made simple.

Ex: $y = x + 0 \Rightarrow y = x$
 $y = x - 0 \Rightarrow y = x$
 $y = x + 1 \Rightarrow y = x + 1$
 $y = x / 1 \Rightarrow y = x$

5. Machine Idioms

Ex: $a = a + 1 \Rightarrow \text{INC } a$
 $a = a - 1 \Rightarrow \text{DEC } a$

LEX Tool

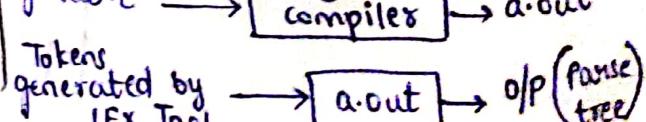
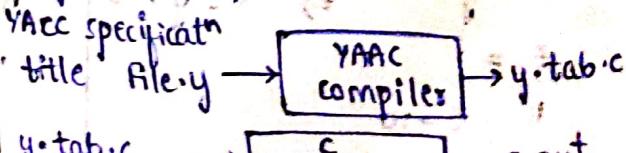


LEX tool is used in first phase of compilation i.e., lexical analysis.

YACC Tool (Yet Another Compiler-Compiler).

It is a tool for generating look-ahead left to right parser (LALR).

It takes S/P from lexical analyzer & generates parse tree.



Tokens generated by Lex Tool → a.out → o/p (Parse tree)

10/12/2023

Recursive Descent Parser

A parser that uses collection of recursive procedures for parsing the given input string is called Recursive Descent Parser. Here, the CFG is used to build the recursive procedures.

The RHS of the production rule is directly converted to a program. for each non-terminal, a separate procedure is written and body of the procedure is RHS of the corresponding non-terminal. Basic steps for the construction of RD parser

The RHS of the rule is directly converted into program code symbol by if S/P symbol is non-terminal, then a call to the procedure corresponding to the non-terminal is made.

If S/P symbol is terminal, then it is matched with the lookahead from I/P. The lookahead ptr has to be advanced on matching of the S/P symbol.

If the production rule has many alternatives, then all its these alternatives have to be combined into a single body of the procedure.

The parser should be activated by the procedure corresponding to the start symbol.

Ex: $E \rightarrow \text{num } T$
 $T \rightarrow * \text{ num } T / E$

procedure $E()$
{
if lookahead (num) {
match (num);
T();
}
else
error();
if lookahead = '\$' then
declare success;
}
// End of procedure E

procedure match (token t)
{
if token = t
if lookahead = t then
lookahead = new_token; // lookahead
ptr is advanced
else
error();

procedure $T()$
{
if lookahead = '*' then {
match ('*');
}
if lookahead = 'num' then
match (num);
else
error();
}
else NULL; // indicates E
}

The other alternative is combined into procedure $T()$

procedure error()
{
print("ERROR!");

Ex:

3	*	4	\$
---	---	---	----

step-by-step process

Advantages of RD parsers

- » They are simple to build
- » They can be built with the help of parse trees.

Limitations

- » They are not very efficient as compared to other parser techniques.
- » There are chances that program for RD parser may enter in infinite loop for some inputs.

» It is difficult to parse the string; if lookahead symbol is arbitrarily long.

Q) $E \rightarrow T + E \mid T$ write procedures for non-terminals of the grammar to make a recursive descent parser.

$T \rightarrow V \cdot T \mid V$

$V \rightarrow id$

procedure $E()$

{
 $T()$;
 if lookahead = '+' then

 match '+';

procedure $T()$

{
 $V()$;
 if lookahead = 'id' then

 match 'id';

 else error

 else error

(a) $bexpr \rightarrow bexpr \text{ or } bterm \mid bterm$ Write RD parser where,
 $bterm \rightarrow bterm \text{ and } bfactor \mid bfactor$ or, and, (,), ~~true~~,
 $bfactor \rightarrow bfactor \mid (bexpr) \mid \text{true} \mid \text{false}$ false are terminals.

$bexpr = E$; $bterm = T$; $bfactor = F$; $\text{or} = +$; $\text{and} = *$
 $E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow F \mid (E) \mid \text{true} \mid \text{false}$

Operator Precedence.

Symbol Table

1

Comparison b/w static, stack and heap Allocation.

static allocation

1. Stack allocation is done for all data objects at compile time

2. Data structures can not be created dynamically bcoz in static allocation compiler can determine the amount of storage required by each data objects.

3. Memory allocation: The names of data objects are bound to storage at compile time.

Merits and Limitations:-

This allocation strategy, is simple to implement but supports static allocation only. Similarly recursive procedures are not supported by static allocation strategy.

stack allocation

In stack allocation stack is used to manage runtime storage

Data structures and data objects can be created dynamically.

Memory Allocation: Using LIFO activation records and data objects are pushed onto the stack. The memory addressing can be done using index and registers.

Merits and Limitations:-

It supports dynamic memory allocation but it is slower than static allocation strategy.

Supports recursive procedures but references to non local variables after activation record can not be retained.

Heap allocation

In heap allocation, heap is used to manage dynamic memory allocation.

Data structures and data objects can be created dynamically.

Memory Allocation: A contiguous block of memory from heap is allocated for activation record or data object. A linked list is maintained for free blocks.

Merits and Limitations:-

Efficient memory management is done using linked list. The deallocated space can be reused. But since memory block is allocated using best fit, holes may get introduced in the memory.

The heap allocation allocates the continuous block of memory when required for storage of activation records or other data objects. This allocated memory can be deallocated when activation ends. This deallocated (free) space can be further reused by heap manager.

3. The efficient heap management can be done by
1. creating a linked list for the free blocks and when any memory is deallocated that block of memory is appended in the linked list
 2. Allocate the most suitable block of memory from the linked list. i.e. use best fit technique for allocation of block.

Storage Allocation Strategies:-

There are 3 different storage allocation strategies based on the division of run time storage. The strategies are:

1. Static allocation:- The static allocation is for all the data objects of compile time.
2. Stack allocation:- In this stack allocation a stack is used to manage the runtime storage.
3. Heap allocation:- In heap allocation the heap is used to manage the dynamic memory allocation.

1. Static allocation:-

1. The size of data objects is known at compile time.
2. The names of these objects are bound to storage at compile time only and such an allocation of data objects is done by static allocation.
3. In static allocation the compiler can determine the amount of storage required by each data object. And therefore it becomes easy for a compiler to find the addresses of these data in the activation record.
4. At compile time compiler can fill the addresses at which the target code can find the data it operates on.
5. FORTRAN uses the static allocation strategy.

Limitations of static Allocation:-

1. The static allocation can be done only if the size of the data objects is known at compile time.

2. The data structures can not be created dynamically.
It means that, the static allocation can not manage the allocation of memory at run-time.
3. Recursive procedures are not supported by this type of allocation.

2. Stack Allocation:-

1. The stack allocation strategy is a strategy in which the storage is organized as stack. The stack is also called control stack.
2. As the activation begins, the activation records are pushed onto the stack and on completion of this activation the corresponding activation records can be popped.
3. The locals are stored in the each activation record. Hence locals are bound to corresponding activation record on each fresh activation.
4. The data structures can be created dynamically for stack allocation.

Limitations of Stack allocation:-

- The memory addressing can be done using pointers and index registers. Hence this type of allocation is slower than static allocation.

3. Heap Allocation:-

1. If the values of non local variables must be retained even after the activation record, then such a retaining is not possible by stack allocation. This limitation of stack allocation is because bcoz of its Last-in FIRST Out nature. For retaining of such local variables heap allocation strategy is used.