

Linear

- 1) Data stored sequentially
- 2) All data items are stored in single level
- 3) All data can be traversed in a single run

4) Easy to implement

5) Memory utilization is not eff.

Stack, Queue, List

Non-linear

Data stored hierarchically.

Data stored in multiple levels

We can't access data in single run

Not easy to implement when compared to linear

Memory utilization is eff.

Tree, graph

Stack

Stack is a linear non-primitive data structure where insertion and deletion operations are done from the same end. The end used for insertion and deletion is termed as top of the stack

Insertion operation is termed as push and deletion operation is termed as pop

In a stack last element inserted will be the first to be retrieved out or deleted.
(LIFO)

Implementation of a stack of integer using an array.

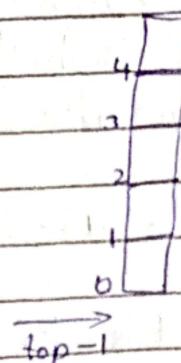
Let stack be an array of integers of size 5 denoted with a macro SIZE.

```
#define SIZE 5
int stack[SIZE]
```

Let top be the index to perform push and pop operation with an initial value of -1.

```
int top = -1;
```

An empty stack looks like



Insertion operation (PUSH)

On a stack which is full we can't perform push operation, if we do so it is called as overflow.

If top is having value SIZE-1, it denotes overflow.

If stack is not full we can push an element named item onto the stack using the statements

$\text{top} = \text{top} + 1;$
 $\text{stack}[\text{top}] = \text{item};$

* C function to perform push operation.

```
void push(int item) {
    if ( $\text{top} == \text{SIZE} - 1$ )
        printf ("\n Stack overflow");
    else {
         $\text{top} = \text{top} + 1$ ;
        stack[ $\text{top}$ ] = size;
    }
}
```

Deletion operation [pop]

On a stack which is empty we can't perform pop operation. The condition to check stack is empty.

$\text{top} == -1;$

If you do so it is termed as underflow.

On a stack which is not empty the pop operation can be performed using statement.

```
delete stack[ $\text{top}$ ];
 $\text{top} = \text{top} - 1;$ 
```

* C function to perform POP operation.

```
void pop () {
    if ( $\text{top} == -1$ ) {
        printf ("Stack Underflow");
    }
}
```

else {

printf("The Element popped is %d",
stack[top]);

top=top-1;

}

Display

```
void display () {  
    if (top <= -1) {  
        printf("stack empty");  
    }  
    else {  
        printf("The stack content are \n");  
        for (i=top ; i>=0 ; i++) {  
            printf("%d\n", stack[i]);  
        }  
    }  
}
```

C program to implement stack of integers.

```
#include <stdio.h>  
#include <stdlib.h>  
#define SIZE 5  
  
int stack[SIZE];  
int top = -1;  
  
// Push function  
// Pop function  
// display function.
```

```
int main() {  
    int ch, item;  
    while(1) {  
        printf("\n 1.push");  
        printf("\n 2.pop");  
        printf("\n 3.Display");  
        printf("\n 4.Exit");  
        printf("\n Read choice:");  
        scanf("%d", &ch);  
        switch(ch) {  
            case 1:
```

case 1 : printf("\n read item to be
pushed: ")

```
        scanf("%d", &item);  
        push(item);  
        break;
```

case 2 : pop();
 break;

Case 3 : display();
 break;

default : exit(0);

}

}

C program to implement stack of integers
using structures and point

```
#include <stdio.h>
#include <stdlib.h>
#define SIZE 5

struct stack {
    int data[SIZE];
    int top;
};

typedef struct stack STACK;

void push (STACK *s, int item) {
    if (s->top == SIZE - 1)
        printf ("\n stack overflow");
    else
        s->top = s->top + 1;
    s->data[s->top] = item;
}

void pop (STACK *s) {
    if (s->top == -1)
        printf ("\n stack underflow");
    else
        printf ("\n element popped is %d", s->data[s->top]);
    s->top = s->top - 1;
}

void display (STACK s) {
    if (s.top == -1)
        printf ("\n stack is empty");
    else
        printf ("\n stack content are\n");
}
```

```
for (i=s.top; i>=0; i--) {  
    printf("%d\n", s.data[i]);  
}
```

```
int main() {  
    STACK S ;  
    s.top = -1;  
    int ch, item ;  
    for (;;) {  
        printf("1.push");  
        printf("2.pop");  
        printf("3.Display");  
        printf("4.Exit");  
        printf("\n Read choice: ");  
        scanf("%d", &ch);
```

```
switch(ch)
```

```
{
```

```
    printf("\n");  
    case 1 : printf("\n read item to be  
                     pushed: ");  
               scanf("%d", &item);  
               push(&s, item);  
               break;
```

```
    Case 2 : pop(&s)
```

```
               break;
```

```
    Case 3 : display(s);  
               break;
```

```
    default : exit(0);
```

```
b7
```

```
return 0;
```

Applications of stack

- * Conversion of expression / +
- * Evaluation of postfix expression
- * Recursion. + -

Expr \rightarrow Prefix
 \rightarrow Postfix (suffix)
 \rightarrow Infix

Infix	Postfix	Prefix
a+b	a b +	+ a b
a+b*c	a b c * +	+ a + b c *
a+b-c	a b + c -	- a + b c
(a+b)*c	a b + * c	+ a b + * c
	a b + c *	* a b c

$$((a+(b-c)*d)^n e) + f \quad \begin{array}{l} (a + -bc * d)^n e + f \\ (a + * -bcd)^n e + f \\ (+a * -bcd)^n e + f \end{array}$$

$$(a+bc-d*)^n e + f \quad \begin{array}{l} (a + bc - d)^n e + f \\ ((a + bc - d)^n e + f)^n \\ ((a + bc - d)^n e + f)^n \end{array}$$

$$(abc-d*a*)^n e + f \quad \begin{array}{l} (abc - d * a)^n e + f \\ ((abc - d * a)^n e + f)^n \end{array}$$

$$\begin{array}{l} abc - d * e ^ n + f \\ abc - d * e ^ n f + \end{array}$$

Algorithm to convert given infix expression to post fix.

†)

Step 1 : Read the given infix expression from left to right

Step 2 : If scanned symbol is

i) operand - push it on to stack

ii) left parenthesis -

place it on post-fix expression

iii) left parenthesis - Push it on to stack,

iv) Right parenthesis - Pop the content of stack and place them

on post fix expression until you get corresponding left parenthesis

v) Operator - if stack is empty or top of stack is left parenthesis
push the operator onto stack
else

while top of stack has higher or equal precedence than the scanned symbol
and

stack is not empty
and

top of stack is not left parenthesis

Pop the content of stack and place it on postfix exp
Push the operator onto the stack.

Step 3 : Until stack becomes empty pop them and place them on post fix

Convert the following infix to postfix using stack.

$a+b*c$

Symbol

Stack

Postfix

a

Empty

a

+

+

a

b

+

ab

*

++

ab

c

++

abc

Empty

abctt

$(a+b)*c$

Symbol

Stack

Postfix

(

C

Empty

a

C

a

+

(+

a

b

(+

ab

)

Empty

ab+

*

*

ab+

c

*

ab+c

Empty

ab+c*

$((((a + (b - c) * d)^n e) + f))$

Symbol	Stack	Postfix
((-
(((-
(b c	((c	-
a	((c)	a
+	((c+)	a
(((c+c	a
b	((c+c	ab
-	((c+c-	ab
c	((c+c-	abc
)	((c+	abc-
*	((c+*	abc-
d	((c+*	abc-d
)	((abc-d*+
ⁿ	((ⁿ	abc-d*+
e	((ⁿ	abc-d*+e ⁿ
)	((abc-d*+e ⁿ
+	((+	abc-d*+e ⁿ
f	((+	abc-d*+e ⁿ f
)	-	abc-d*+e ⁿ f+

A C function to convert a given infix into post fix.

```

void infix_topostfix (char stack *s, char infix[])
{
    int i, j = 0;
    char symbol, postfix[15], temp;

    for (i=0; infix[i] != '\0'; i++)
    {
        symbol = infix[i];
        if (isalnum(symbol))
        {
            postfix[j++] = symbol;
        }
        else
        {
            switch (symbol)
            {
                Case '(': Push(s, symbol);
                break;
                Case ')': temp = pop(s);
                temp = pop(s);
                while (temp != '(')
                {
                    postfix[j++] = temp;
                    temp = pop(s);
                }
                break;
                Case '+':
                Case '-':
                Case '*':
                Case '^': if (s->top-- != 1 || s->
                               data[s->top] == '=')
                            push(s, symbol);
                        else
                        {
                    }
            }
        }
    }
}
    
```



while((preced(s->data[s->top]) >= preced(symbol))
&& s->top != -1 && s->data[s->top] != 'c')

postfix[j++] = pop(s);

push(s, symbol)

}

break;

3
4
5

while (s->top != -1)

postfix[j++] = pop(s);

Postfix[j] = '\0';

printf(") in the postfix expression %s\n",
postfix);

3.

C program infix to postfix.

```
#include <stdio.h>
#include <stdlib.h>
#include <ctype.h>
```

```
#define SIZE 15
```

```
struct stack {
    char data[SIZE];
    int top;
};
```

```
typedef struct stack STACK;
```

```
void push (stack STACK, s)
```

```
void push (STACK *s, char item) {
```

```
    s->top = item;
```

```
}
```

```
char pop (STACK *s)
```

```
{
```

```
    return s->data [s->top--];
```

```
}
```

```
int preced (char symbol) {
```

```
switch (symbol) {
```

```
    case '^' : return 5;
```

```
    case '*' :
```

```
    case '/' : return 4;
```

```
    case '+' :
```

```
    case '-' : return 3; }
```

```
b/
```

// infix to postfix function.

```
int main() {  
    STACK S;  
    S.top = -1;  
    char infix[15];  
    printf("Read infix expression: ");  
    scanf("%s", infix);  
    infix_to_postfix(&S, infix);  
    return 0;  
}
```

Algorithm to convert infix to postfix

Evaluation of postfix expression using stack

Algorithm to evaluate a given postfix exp.

- 1) Scan the expression from left to right.
- 2) If the scanned symbol is
 i) Operand - Push it on to stack
- 3) If Operator - Pop 2 operands, assign them to
 operand2 and operand1 respectively
 and perform the operation
 res = op1 operator op2, push the result
 on the stack
- 4) Pop the stack content to get the final result

Tracing:-

$231 * +$

Symbol	Stack	op1	op2	Result
2	2	-	-	-
3	2, 3	-	-	-
*	2, 3, 4	-	-	-
+	2, 12	3	4	$3 * 4 = 12$
	14	2	12	$2 + 12 = 14$

$$(3+2) * (6-2)$$

$$3+2 * 6-2$$

$$3+6-2 * /$$

→ $\frac{7}{6} 2 -$

	$7+4 / 7/4 = 1$	-	-	-
3	3	-	-	-
4	3, 4	-	-	-
+	7	3	4	$3+4=7$
6	7, 6	-	-	-
2	7, 6, 2	-	-	-
-	7, 4	6	2	$6-2=4$
*	1, 75	7	4	$7/4$
/				1.75

A C function to evaluate a postfix expression

```

float evaluate_postfix(STACK *S, char postfix)
{
    int i;
    float op1, op2, result;
    char symbol;
    for (i=0; postfix[i] != '\0'; i++)
    {
        symbol = postfix[i];
        if (isdigit(symbol))
            push (symbol - '0');
    }
}

```

```

else {
    op2 = pop(s);
    op1 = pop(s);
    res = operate(op1, op2, symbol);
    push(s, res);
}
return pop(s);
}
    
```

C program to evaluate postfix expression

```

#include <stdio.h>
#include <stdlib.h>
#include <ctypes.h>
#include <math.h>
#define SIZE [15]

struct stack {
    float data[SIZE];
    int top;
};

typedef struct stack *STACK;

void push(STACK *s, float item) {
    s->data[s->top] = item;
}

float pop(STACK *s) {
    return s->data[s->top];
}
    
```

```
float operate(float op1, float op2, char symbol)
```

```
{ switch(symbol) {
```

```
    case '+': return op1 + op2;
```

```
    case '-': return op1 - op2;
```

```
    case '*': return op1 * op2;
```

```
    case '/': return op1 / op2;
```

```
    case '^': return pow(op1, op2);
```

```
}
```

```
} // write evaluate_postfix function
```

```
int main () {
```

```
char postfix[SIZE]; STACK S; S.top = -1;
```

```
float result;
```

```
printf("\n Read postfix expr\n");
```

```
scanf("%s", postfix);
```

```
result = evaluate(postfix);
```

```
result = evaluate_postfix(&, postfix);
```

```
printf("\n Result = %f \n", result);
```

```
return 0;
```

```
}
```

Algorithm to convert evaluate a float prefix expression:

Step 1: Scan the expression from right to left

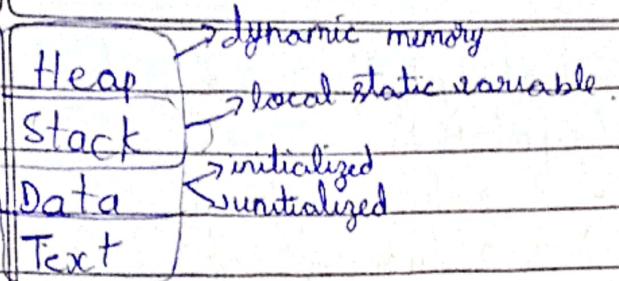
Step 2: If scanned symbol is

i) operand → push it to stack

ii) Operator → Pop 2 operands, assign them to op1 and op2 respectively and perform the operation.

res = op1 operator op2, and push result to the stack

Step 3: Pop the stack content to get final result



Recursion :-

The ability of a function to call itself is known as recursion.

→ Direct
 ↙ Indirect

Properties of a recursive function.

- Recursive function should have a base case & terminating cond'
- If no base case, it leads to overflow
- Each recursive call, solves smaller instance of the problem.

Factorial of a number.

$5! = 120$

Recursive definition for factorial

$$\text{Fact}(n) = \begin{cases} 1 & ; \text{ if } n = -1 \text{ or } n = 0 \\ n \times \text{fact}(n-1) & ; \text{ otherwise} \end{cases}$$

```
int fact(int n)
{
    IF (n == 1 || n == 0)
        return 1;
```

```
else
    return n * fact(n-1);
```

}

Difference between recursion and iteration

Recursion

- * Recursive function
- * stops on encountering base case
- * Consumes more memory
- * Slower when compared to

Iteration

- stops on encountering terminating cond.
- less memory
- Faster when compared to

To find GCD of two numbers

~~int GCD(int a, int b) {~~

$$Gcd(x, y) = \begin{cases} x & ; y=0 \\ Gcd(y, x \% y) & ; \text{otherwise} \end{cases}$$

$$Gcd(x, y) = \begin{cases} x \text{ or } y & ; x=y \\ Gcd(x-y, y) & ; x>y \\ Gcd(y-x) & ; x<y \end{cases}$$



```
int gcd (int x, int y) {  
    if (y == 0)  
        return x;  
    return gcd (y, x % y); [Tail-end recursion]  
}
```

Tail recursion is a recursive function in which the recursive call is the last statement that gets executed in the function.

Recursive function to find whether the elements are sorted or not

```
int check_sorted (int a[], int n) {  
    if (n == 1)  
        return 1;  
    return a[n-1] < a[n-2] ? 0 : check_sorted (a, n-1);  
}
```

```
int sum_array (int a[], int n) {  
    if (n == 1)  
        return a[0];  
    return a[n-1] + sum_array (a, n-1);  
}
```

Product of 2 numbers

```
int multiply [int a, int b] {  
    if (b == 0 || a == 0)  
        return 0;  
    if (a == 1)  
        return b;  
    else if (b == 1)  
        return a;
```

else

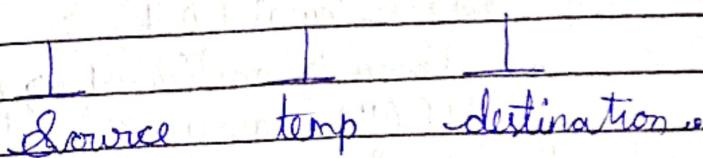
 return a + product(a, b-1);

}

Binary search

```
int binary (int a[], int n, int key, int low, int high)
{
    if (low > high)
        return -1
    else
        { int mid = (low+high)/2
            if (a[mid] == key)
                return mid+1
            else if (a[mid] > key)
                return binary (a, n, key, low, mid)
            else
                return binary (a, n, key, mid+1, high)
        }
}
```

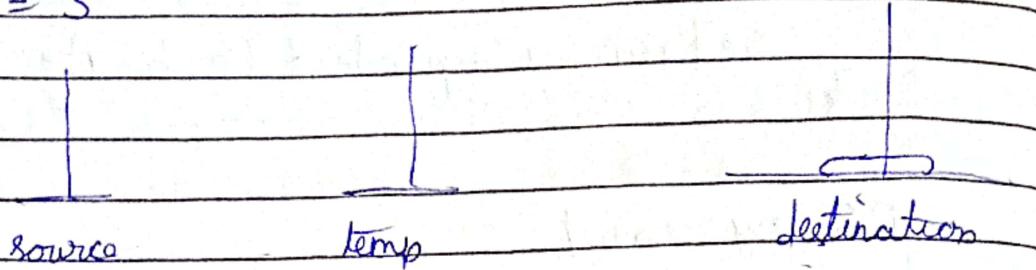
Tower of hanoi



if disc is one = no of moves is 1.

if disc is two = no of moves is 3

ii) $n = 3$



Recursively \rightarrow move $(n-1)$ disc from source to temp with help of destination $\rightarrow 3$, move n^{th} to dest
 Recursively \rightarrow move $(n-1)$ discs from temp to dest with help of source. $\rightarrow 3$

$$\therefore 2^n - 1$$

C function of towers of hanoi

```
void tower_hanoi(int n, char s, char t, char d)
{
```

if ($n == 1$)

printf("\n Move %d disc from
~~s to t~~ %c to %c", n, s, d);

else

```
{ tower_hanoi(n-1, s, t, d);
```

```
n. tower_hanoi(n-1, s, d, t);
```

```
printf("\n move %d disc from %c to  

%c", n, s, d);
```

```
tower_hanoi(n-1, t, s, d);
```

}

}

Queue :-

Queue is a linear non-primitive data structure where insertion is done from rear end and deletion is done from front end.

The insertion operation is referred as en-que and deletion is referred as deque.

In a queue, first element inserted will be first to be retrieved out [FIFO]

Types of Queue

- * Linear (or) ordinary queue:
- * Circular queue:
- * Priority queue: (heap-binary)
- * Dequeue (double ended queue):

Linear Queue:

Implementation of queue of integers:

Let SIZE denotes the size of the queue and the definition of the queue is represented with the following structure

```
STRUCT queue {
```

```
    int front;
```

```
    int data[SIZE];
```

```
}
```

```
typedef STRUCT queue QUEUE
```

The initial value of front and rear end is -1.



Insertion: (enqueue)

```
void enqueue (QUEUE *q, int item)
{
    if (q->r == (SIZE - 1))
        printf ("\n Queue full");
    else
    {
        q->r = q->r + 1;
        q->data[q->r] = item;
        if (q->f == -1)
            q->f = 0;
    }
}
```

Dequeue

```
int dequeue (QUEUE *q)
{
    int del;
    if (q->f == -1)
        printf ("\n Queue empty");
    return -1;
}
else
{
    del = q->data[q->f];
    if (q->f == q->r)
    {
        q->f = -1;
        q->r = -1;
    }
    else
    {
        q->f = q->f + 1;
    }
    return del;
}
```

Display

```
void display (QUEUE q) {  
    int i;  
    if (q.f == -1)  
        printf ("\n queue empty");  
    else {  
        printf ("\n queue data are ");  
        for (i = 0;  
             for (i = q.f; i <= q.r; i++) {  
            printf ("%d ", q.data[i]);  
        }  
    }  
}
```

CIRCULAR QUEUE;

A linear queue with 5 elements looks like

10 | 20 | 30 | 40 | 50.

On the above queue, if we perform deletion operation thrice, the queue looks like,

1 | 1 | 1 | 4 | 5
↑ ↑
f r

Even though there are some empty slots in the beginning of the queue, it is not possible to insert new elements as rear end has value of SIZE-1, to overcome this drawback we go for circular queue.

INSERTION:

```

void enqueue (QUEUE *q, int item) {
    if ( $q \rightarrow F = (q \rightarrow r + 1) \% SIZE$ )
        printf ("\n Queue full");
    else {
         $q \rightarrow r = (q \rightarrow r + 1) \% SIZE$ ;
         $q \rightarrow data[q \rightarrow r] = item$ ;
        if ( $q \rightarrow F == -1$ )
             $q \rightarrow F = 0$ ;
    }
}

```

DEQUEUE OPERATION:

```

int dequeue (QUEUE *q)
{
    int del;
    if ( $q \rightarrow F == -1$ )
        printf ("\n queue empty");
    return -1;
}
else
{
    del =  $q \rightarrow data[q \rightarrow F]$ ;
    if ( $q \rightarrow F == q \rightarrow r$ )
    {
         $q \rightarrow F = -1$ ;  $q \rightarrow r = -1$ ;
    }
    else
         $q \rightarrow F = (q \rightarrow F + 1) \% SIZE$ ;
    return del;
}

```

```
VOID DISPLAY
void display (QUEUE q)
{
    int i;
    if (q.f == -1)
        printf ("\n queue empty");
    else
        {
            printf ("\n queue content are\n");
            for (i = q.f; i != q.r; i = (i + 1) % SIZE)
                {
                    printf ("%d\t", q.data[i]);
                    printf ("%d\t", q.data[i]);
                }
        }
}
```

PROGRAM 3 :

Implementation of msg queuing system

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
```

```
#define SIZE 5
```

```
struct SIZE
struct Queue
{
    int f, r;
    char [SIZE][20];
};
```

```
typedef struct Queue QUEUE;
```

```
void sender(QUEUE *q, char item[20])
{
    if (q->f == (q->r + 1) % SIZE)
        printf("\n QUEUE full");
    else {
        q->r = (q->r + 1) % SIZE;
        strcpy(q->data[q->r], item);
        if (q->f == -1)
            q->f = 0;
    }
}
```

```
char *receiver(QUEUE *q)
{
    char *del;
    if (q->f == -1)
    {
        printf("\n Queue empty");
        return NULL;
    }
    else
    {
        del = q->data[q->f];
        if (q->f == q->r)
        {
            q->f = -1;
            q->r = -1;
        }
        else
            q->f = (q->f + 1) % SIZE;
    }
    return del;
}
```

```
void display(QUEUE q)
{
    int i;
    if (q.f == -1)
        printf ("\n Queue empty");
    else
    {
        printf ("\n Queue content are \n");
        for (i = q.f; i != q.r; i = (i + 1) % SIZE)
            printf ("%s\n", q.data[i]);
        printf ("%s\n", q.data[i]);
    }
}
```

```
void main ()
{
    QUEUE q;
    q.f = -1;
    q.r = -1;
    char item[20];
    char *d;
    int ch;
    for (;;)
    {
        printf ("\n 1.Send \n 2.read \n 3.exit");
        receive
        if (ch == 1)
            exit(0);
        printf ("\n read choice:");
        scanf ("%d", &ch);
        getch();
    }
}
```

```
switch (ch)
{
    case 1: printf ("\n read msg to be
                    cent\n");
              gets (item);
              sender (&q, item);
              break;
}
```

```
Case 2 : d = receiver(q) ;  
if (d) = NULL)  
printf("\n msg received is  
%s\n", d);  
break;  
Case 3 : display(q);  
break;  
default : exit(0);  
}  
}  
return 0;  
}
```

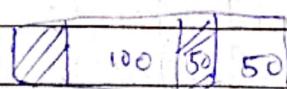
Dynamic memory : (heap)

Allocation of memory during runtime.

UNIX - alloca - allocated dynamic memory from static.

i) malloc()

↳ allocates single block of memory from heap region



malloc(100)

success

malloc(150)

failure

→ by default will be having some garbage values

On success → return starting address,

On failure → it returns NULL

Syntax

void *malloc(size_t n bytes)

→ malloc function needs one argument

Write syntax for following to allocate memory dynamically

1) 1 integer :

```
int *ptr;  
ptr = (int *)malloc(sizeof(int));
```

2) n integers :

```
int *ptr;  
ptr = (int *)malloc(n * sizeof(int));
```

3) n students where a student is represented by a structure struct student

```
struct student *ptr;  
ptr = (struct student *)malloc(n * sizeof(struct  
student));
```

Program to add n elements using n elements using dynamic allocation.

```
int main()  
{  
    int *ptr; n, sum=0, i=0;  
    //  
}
```

```

printf("Read 'n' value");
scanf("%d", &n);
ptr = (int*) malloc(n * sizeof(int));
printf("\n Read elements\n");
for(i=0; i<n; i++)
{
    scanf("%d", ptr+i);
    sum = sum + *(ptr+i);
}
printf(sum);

```

Calloc

allocates memory dynamically with multiple blocks on success returns static address and on failure returns NULL

Syntax

void *malloc

void *calloc (int nblocks, size_t nbytes)

number of blocks

size of
each block

Calloc function has 2 arguments, by default a value of 0 will be stored in the calloc

Realloc();

Can be used to either increase or decrease the memory allocated previously either by malloc or calloc.

Syntax

void *realloc(void *ptr, size_t newsize)

free();

It deallocates the memory which was allocated dynamically.

void *free(void *ptr);

realloc(ptn, s)

realloc(ptn, 0);

Linked List :

→ collection of sequential data items.

referred as "nodes".

1 node of a linked list has 2 fields (parts)

data address
↓ ↓

store the address of next-node information

Representation of a node.

struct node {

int data;

struct node *addr;

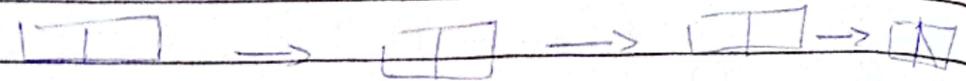
};

typedef struct node *Node;



Types of linked list.

* Singly linked list.



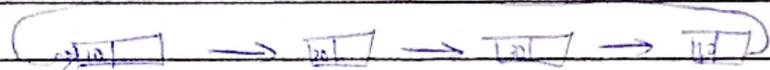
reference \rightarrow start \rightarrow holds address of the first node
start

[2050]

start is NULL - list is empty

start \rightarrow address is NULL - only one node.

* Circular singly linked list.



reference node \rightarrow last \rightarrow ~~last node~~ \rightarrow ~~address of last node~~
~~before last node~~

last is NULL - list is empty.

last \rightarrow address is pointing to last \rightarrow one node.

iii) Double linked list.



reference = start \rightarrow holds the address of first node

start is NULL - list is empty

start of next is null \rightarrow only one node



single linked list :

To insert a new node at beginning of the list.

```
NODE *insertbegin (NODE start,int item) {  
    NODE temp;  
    temp = (NODE)malloc(sizeof(struct Node));  
    temp->data = item;  
    temp->address = NULL;  
    if (start == NULL)  
        return temp;  
    temp->address = start;  
    return temp;
```

}

To insert a new node at end of the list.

```
* NODE insertend (NODE start,int item) {  
    NODE temp,cur, last; // last -> start  
    temp = (NODE)malloc(sizeof(struct Node));  
    temp->data = item;  
    temp->address = NULL;  
    if (start == NULL)  
        return temp;  
    cur = start;  
    while (cur->address != NULL)  
        cur = cur->address;  
    cur->address = temp;  
    return start;
```

}

To delete node at the beginning of the list :

```

NODE deletebegin (NODE start)
{
    if (start == NULL) {
        printf("The list is empty");
        return NULL;
    }
    temp = start;
    start = start->addr;
    printf("The deleted node is %d", temp->data);
    free(temp);
    return start;
}
    
```

To delete node at the end of the list.

```

NODE deletedend (NODE start)
{
    NODE
    if (start == NULL) {
        printf("The list is empty");
        return NULL;
    }
    prev = NULL;
    cur = start;
    while (cur->addr != NULL) {
        prev = cur;
        cur = cur->addr;
    }
}
    
```

```

prev->addr = NULL;
printf("The deleted node is %d",
       cur->data);
    
```

For e.g (cusi) :-
Sierung start;

7

Display content of the list.

void display (NODE start)

{ NODE temp;

if (start == NULL) {

printf("List is empty"); }

else {

printf("\n list data are \n");

temp = start;

while (temp != NULL)

{

printf("%d \t", temp->data);

temp = temp->address;

}

7

7

Stack → insert begin, delete begin, display
↳ insert end, delete end, display

Queue → insert end, delete begin display

Multiplication of polynomial using linked list

```

    #include <stdio.h>
    #include <stdlib.h>

    struct node {
        int co, po;
        struct node *addr;
    };

    typedef struct node *NODE;

    //Write insert end function
    //Write display function
    //Write add term function
    //Write multiply function.

    int main() {
        int m, n, i, j, co, po;
        NODE poly1 = NULL, poly2 = NULL, poly = NULL;
        printf("Read number of term for 1st poly\n");
        scanf("%d", &m);
        printf("Read number of term for 2nd poly\n");
        scanf("%d", &n);
        for (i = 0; i <= m; i++) {
            printf("\n") + Read CO and PO for %term;
            scanf("%d %d", &co, &po);
            poly1 = insertend(Poly1, co, po);
        }
        printf("\n First polynomial is \n");
        display(poly1);

        printf("Read number of terms for second poly");
        scanf("%d", &m);
    }

```

```

for (i=1 ; i<=n ; i++) {
    printf ("\n") + Read CO and PO for %d term. i)
    scanf ("%d %d", &CO, &PO);
    poly2 = insertend (poly2, CO, PO);
}

```

```

printf ("\n") + First second polynomial is \n;
display (poly2);
poly = multiply (poly1, poly2);
printf ("\n") + The resultant polynomial is \n;
display (poly);
return 0;
}

```

```

NODE insertend (NODE start, int CO, int PO) {
    NODE temp, current;
    temp = (NODE) malloc (sizeof (struct node));
    temp->CO = CO;
    temp->PO = PO;
    temp->addr = NULL;
    if (start == NULL)
        return temp;
    else {
        current = start;
        while (current->addr != NULL)
            current = current->address;
        current->addr = temp;
    }
    return start;
}

```

}



```
void display(NODE start) {
    NODE temp;
    if (start == NULL)
        printf("\nList empty");
    else {
        temp = start;
        while (temp->addr != NULL)
            printf("%d * %d + ", temp->c,
                   temp->p0);
        temp = temp->addr;
    }
}
```

```
NODE multiply(NODE poly1, NODE poly2) {
    NODE first, sec, res = NULL;
    for (first = poly1; first != NULL; first = first->addr)
        for (sec = poly2; sec != NULL; sec = sec->addr)
            res = addterm(res, first->c * sec->c,
                           first->p0 + sec->p0);
    return res;
}
```

```
NODE addterm(NODE start, int c0, int p0) {
    NODE temp, current;
    int flag = 0;
    temp = (NODE) malloc(sizeof(struct node));
    temp->c0 = c0;
    temp->p0 = p0;
}
```



```
if (start == NULL)
    return temp;
else {
    current = start;
    while (current != NULL) {
        if (current->PO == PO) {
            current->CO = current->CO + CO;
            flag = 1;
            return start;
        }
        current = current->addr;
    }
    if (flag == 0)
        start = insertend(start, CO, PO);
    return start;
}
```

C function to create a single linked list in ascending ordered list.

```
NODE orderlist(NODE start, int item) {
    NODE temp;
    start->head = 1;
    temp = (NODE) malloc(sizeof(struct node));
    temp->data = item;
    temp->addr = NULL;
    if (start == NULL)
        return temp;
    if (item <= start->data) {
        temp->addr = start;
        return temp;
    }
}
```

A B Diff borrow

$\text{prev} = \text{NULL};$

$\text{cur} = \text{start};$

$\text{while}(\text{cur} \neq \text{NULL} \& \& \text{item} > \text{cur} \rightarrow \text{data})$

5

$\text{prev} = \text{cur};$

$\text{cur} = \text{cur} \rightarrow \text{address}$

}

$\text{prev} \rightarrow \text{address} = \text{temp};$

$\text{temp} \rightarrow \text{address} = \text{current};$

$\text{return start};$

7

~~XXXXX~~ C function to reverse single list (Non recursive)

NODE reverse (NODE start) {

 NODE cur, prev, temp;

 if (start \rightarrow address == NULL)

 return start;

 temp = NULL;

 prev = NULL;

 cur = start;

 while (cur != NULL)

 temp = prev;

 prev = cur;

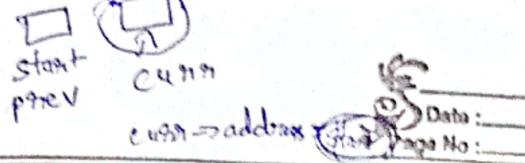
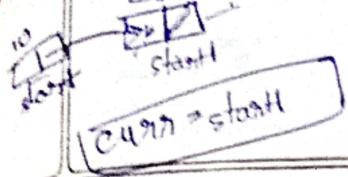
 cur = cur \rightarrow address;

 prev \rightarrow address = temp;

}

 return prev;

}



reverse linked list using recursion

NODE reverse_rec (NODE start)

NODE cur, prev, temp

~~if (start->address == NULL)~~

~~return start~~

~~curr = temp = NULL reverse_rec (start->address)~~

~~prev = NULL prev = start~~

~~curr = start curr->address = prev->start~~

To count the number of nodes in a simple linked list.

C function to delete a node based on info[~~key~~]

NODE deletenode (NODE start, int key) {

NODE temp, curr, prev

if (key == start->data)

temp = start;

start = start->address;

printf ("\n Node %d is deleted ", key);

free (temp); }

```
prev=NULL;  
curr=start;  
while (curr!=NULL && key!=curr->key)  
{  
    previous=curr;  
    prev=curr;  
    curr=curr->addr;  
}  
if (curr==NULL)  
{  
    printf ("\n Key not found");  
    return start;  
}  
prev->addr=curr->addr;  
printf ("\n NODE %d is deleted", curr->id);  
free(curr);  
return start;  
}
```

C function to delete a node based on position

C function based on position insertion

NODE insertposition (NODE start, int key, int pos)

{

NODE temp, prev, curr

int count = 1;

temp = (NODE) malloc (sizeof(struct node));

temp → data = item;

temp → addr = NULL;

if (start = NULL)

return temp;

if (pos == 1)

{

temp → add₇ = start;

return temp;

}

prev = NULL

cur = start;

while (cur != NULL && count != pos)

{

prev = cur;

cur = cur → add₇;

count ++;

}

if (cur == NULL && pos != count)

{ printf("\n Invalid pos");

return start;

}

prev → add₇ = temp;

temp → add₇ = cur;

return start;

}

The representation of a node in doubly linked list is as follows:

```
struct node {  
    int data;  
    struct node *prev;  
    struct node *next;  
};  
typedef struct node *NODE;  
start == NULL // list is empty  
start->next == NULL // list is having only one node
```

Function to insert node at beginning.

```
NODE insertbegin(NODE start, int item){  
    NODE temp;  
    temp = (NODE)malloc(sizeof(struct node));  
    temp->data = item;  
    temp->prev = NULL;  
    temp->next = NULL;  
    if (start == NULL)  
        return temp;  
    temp->next = start;  
    start->prev = temp;  
    return temp;}
```

Function to insert end

```
NODE insertend(NODE start, int item){  
    NODE temp, cur;  
    temp->data = item;  
    temp->prev = NULL;  
    temp->next = NULL;  
    if (start == NULL)  
        return temp;  
    cur = start; next  
    while (cur->address != NULL)  
        cur = cur->next;  
    cur->next = temp;  
    temp->prev = cur;  
    return start;}
```



Function to display content of double linked list.

```
void display(NODE start) {  
    NODE temp;  
    if (start == NULL)  
        printf("\nlist empty");  
    else {  
        printf("\n list content are \n");  
        temp = start;  
        while (temp != NULL) {  
            printf("\t %d", temp->data);  
            temp = temp->next; } }  
}
```

Function to delete node at end

```
NODE deleteend(NODE start) {  
    NODE temp, cur, prev;  
    temp = start;  
    if (temp == NULL)  
        printf("\nlist empty"); return NULL;  
    else {  
        if (start->next == NULL) {  
            cur = start;  
            prev->next = cur;  
            printf("Element deleted is %d from  
node(%d)\n", start->data, start);  
            free(start);  
            return NULL; }  
        while (cur->next != NULL) {  
            cur = cur->next;  
            prev = prev->next; }  
        free(cur);  
        prev->next = NULL;  
        return start; } }
```

To deletenode in a single linked list whose address is stored in ptr.

```
void delete(NODE ptr)
```

```
{  
    temp = ptr->addr;  
    ptr->data = temp->data;  
    ptr->addr = temp->addr;  
    free(temp); }
```

Sparse matrix.

It is a moderately dense matrix when majority of the element is 0.

problem to rep a sparse matrix with DLL

```
#include <stdio.h>
#include <stdlib.h>
```

```
struct node {
```

```
    int col, row, data;
```

```
    struct node *prev;
```

```
    struct node *next;
```

```
};
```

```
typedef struct node *NODE;
```

```
struct in NODE insertend (NODE start, int row, int col, int item) {
```

```
    NODE temp;
```

```
    temp = (NODE)malloc(sizeof(struct node));
```

```
    temp->data = item;
```

```
    temp->row = row;
```

```
    temp->col = col;
```

```
    /* remaining same code */;
```

```
}
```

```
void display (NODE start) {
```

```
    NODE temp;
```

```
    temp = start;
```

```
    if (start == NULL) {
```

```
        printf("\nlist kaali");
```

```
    else {
```

```
        printf("\n Row\t Col\t Value\n");
```

```
        while (temp != NULL) {
```

```
            printf("%d\t %d\t %d\n", temp->row, temp->col,
```

```
            temp->data);
```

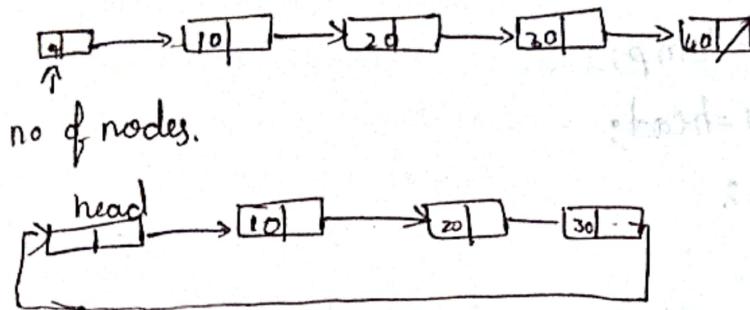
```
            temp = temp->next;
```

```
}
```



```
d.displaymatrix(gOODE start, int m, int n){\n    node temp;\n    int i,j=0;\n    temp=start;\n    for(i=1; i<=m; i++){\n        for(j=1; j<=n; j++){\n            if(temp!=NULL && temp->row==i && temp->\n                col==j){\n                printf("%d\t", temp->data);\n                temp=temp->next;\n            }\n            else\n                printf("0\t");\n        }\n        printf("\n");\n    }\n}
```

Header node is a special node in a list where in the address part of the header node will hold the address of first node of list and data part of header node will hold information about the list.



Write a C function to insert a node at the beginning of a S.L.L with a header node.

```
NODE insertbegin (NODE head, int item) {
```

```
    NODE *temp;
    temp = (NODE)malloc(sizeof(struct node));
    temp->data = item;
    temp->addr = NULL;

    if (head->addr == NULL) {
        head->addr = temp;
        return head;
    }

    temp->addr = head->addr;
    head->addr = temp;
    return head;
}
```

Insert a node at end in C.L.L with head node.

```
NODE insertend (NODE head, int item)
```

```
{    NODE temp; cur;
    temp = (NODE)malloc(sizeof(struct node));
    temp->data = item

    if (head->addr == head) {
        temp->addr = head;
        head->addr = temp;
    }
```

```

    return head;
}
curr = head->addr;
while (curr->addr != head)
    curr = curr->addr;
    curr->addr = temp;
    temp->addr = head;
    return head;
}

```

Addition of 2 long integers using S. L. L with header node:

```

NOTE #include <string.h>
#include <stdlib.h>
#include <stdlib.h>

```

```

struct node {
    int data;
    struct node *addr;
};

```

```

typedef struct node * NODE;

```

```

NODE insertbegin (NODE head, int item) {

```

```

    NODE temp;

```

```

    temp = (NODE) malloc (sizeof(struct NODE));

```

```

    temp->data = item;

```

```

    temp->addr = NULL;

```

```

    if (head->addr == NULL) {

```

```

        head->addr = temp;

```

```

        return head;
    }

```

```

    temp->addr = head->addr;

```

```

    head->addr = temp;

```

```

    return head;
}

```

```

}

```



```
NODE insertend(NODE head, int item) {  
    NODE temp; cur;  
    temp = (NODE) malloc(sizeof(struct NODE));  
    temp->data = item;  
    temp->addr = NULL;  
    if (head->addr == NULL) {  
        head->addr = temp;  
        return head;  
    }  
    cur = head->addr;  
    while (cur->addr != NULL)  
        cur = cur->addr;  
    cur->addr = temp;  
    return head; }
```

```
NODE reverse ( NODE head ) {  
    NODE cur, prev, temp, next;  
    cur = head->addr;  
    prev = NULL;  
    while (cur != NULL) {  
        next = cur->addr;  
        cur->addr = prev;  
        prev = cur; if (prev == head)  
        cur = next;  
    }  
    head->addr = prev; if (prev == head)  
    return head; if (prev == head)
```

```
void display ( NODE head ) {  
    NODE temp;  
    if (head == NULL)  
        if (head->addr == NULL)  
            printf("List empty");  
        else { temp = head->addr;
```

```

while (temp!=NULL) {
    printf("%d", temp->data);
    temp = temp->addr;
}
}

void appendzero ( NODE head1, NODE head2 ) {
NODE cur1
int count=0, c1=0, c2=0;
cur1 = head1->addr;
while (cur1!=NULL) {
    c1=c1+1;
    cur1 = cur1->addr;
}
cur1 = head2->addr;
while (cur1!=NULL) {
    c2++;
    cur1 = cur1->addr;
}
if (c1>c2) {
    for(int i=0; i<(c1-c2); i++) {
        head2 = insertbegin (head2, 0);
    }
} else {
    for(int i=0; i<(c2-c1); i++) {
        head1 = insertbegin (head1, 0);
    }
}
}

```

```

void add ( NODE head1, NODE head2 ) {
NODE head, t1, t2;
int sum = 0, carry = 0;
head = (NODE) malloc (sizeof(struct node));
head->addr = NULL;

```

```

t1 = head1 → address;
t2 = head2 → address;
while (t1 != NULL)

head1 = reverse(head1);
head2 = reverse(head2);
t1 = head1 → addn;
t2 = head2 → addn;
while (t1 != NULL) {
    sum = t1 → data + t2 → data + carry;
    sum = carry = sum / 10;
    sum = sum % 10;
    head = insertbegin(head, sum);
    t1 = t1 → addn;
    t2 = t2 → addn;
}
if (carry > 0)
    head = insertbegin(head, carry);
printf("Resultant is\n");
display(head);
}

int main() {
    NODE head1, head2;
    char first[20], second[20];
    int i;
    printf("Read first num\n");
    scanf("%s", first);
    printf("Read 2nd\n");
    scanf("%s", second);
    head1 = (NODE) malloc (sizeof(struct node));
    head1 → addn = NULL;
    for (i = 0; first[i] != '\0'; i++)

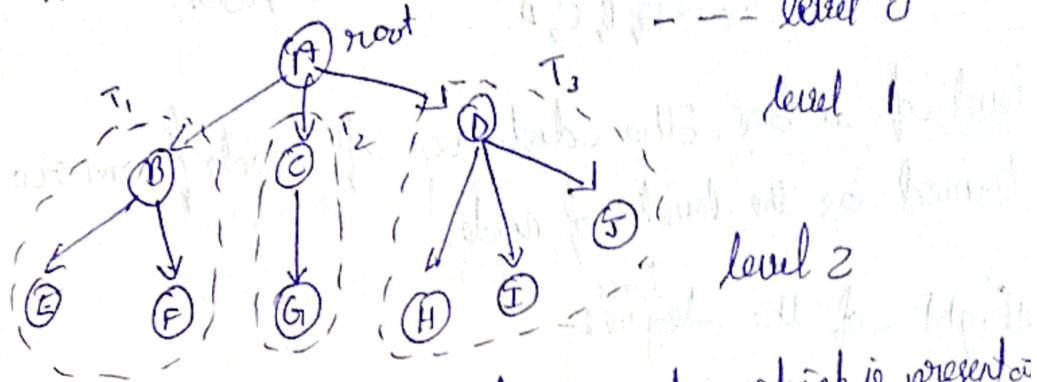
```

```
head1 = insertend (head1, first[i] - '0');  
printf("First num is : ");  
display(head1);  
allocat  
read2 → for (i = 0; second[i] != '\0'; i++)  
    head2 = insertend (head2, first[i] - '0');  
display(head2);  
appendZero (head1, head2);  
add (head1, head2);  
}  
} // main
```



TREES :-

- Trees is a finite set of one or more nodes that exhibits the parent and child relation such that
- 1) There is a special node termed root node
 - 2) The remaining nodes are partitioned into disjoint subset of nodes like $T_1, T_2, \dots, T_n (n \geq 0)$ which are termed as sub-tree



Root node: It is the reference for first node which is present at top of the tree. Root node doesn't have a parent.

Child node: Nodes obtained from the parents

A parent can have 0 or more child nodes. (E & F are child nodes of B)

Siblings: Two or more nodes having common parent are termed as siblings.

I and J siblings of H

The nodes obtained in the path from a specific node X by moving upwards towards root node are termed as ancestors

A and C are ancestors of G.

Parent node:

Leaf node: Leaf nodes are those nodes which have degree of 0 (External node)

Ex:- E, F, G, H, I, J

degree of a node: The number of sub trees for a given node is the degree of a node.

Internal node: all nodes of a tree apart from leaf node is termed as internal node.

Ex:- A, B, C, D.

level of a tree: The distance of node from root node is termed as the level of node.

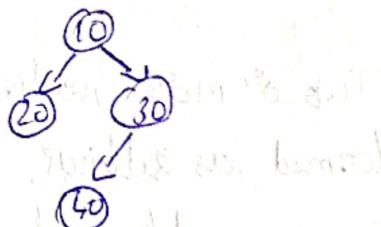
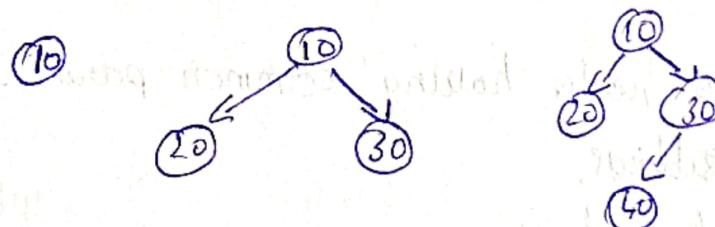
Height of the tree:-

$$\text{Height} = \max \text{ level} + 1$$

The maximum number of nodes processed to reach a leaf node at last level starting from root node is the height of the tree.

Binary Tree

A tree in which each node have either 0, 1 or 2 subtrees.



Types of binary trees:-

1) Strictly binary tree (FULL) :-

A binary tree having 2^i nodes at any given level i is termed as strictly binary tree.

~~It is a binary tree in w~~

2) Complete binary tree

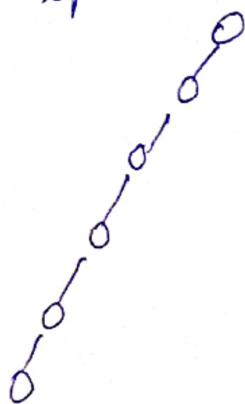
It is a binary tree in which every level apart from last level should have 2^i and last level should be

left filled

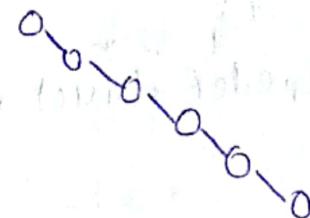


3) Skewed binary tree.

left skewed



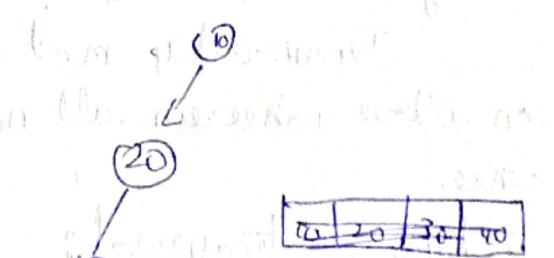
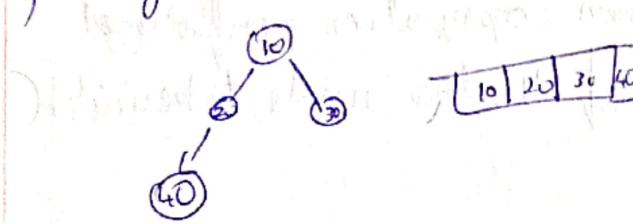
Right skewed



Representation of binary tree.

There are 2 ways of representing a binary tree. Array representation, list representation

Array representation.



For any node stored at index(i)

left child $\rightarrow 2i + 1$

right child $\rightarrow 2i + 2$

2) List representation:

In this representation we create a node which contains the following info.

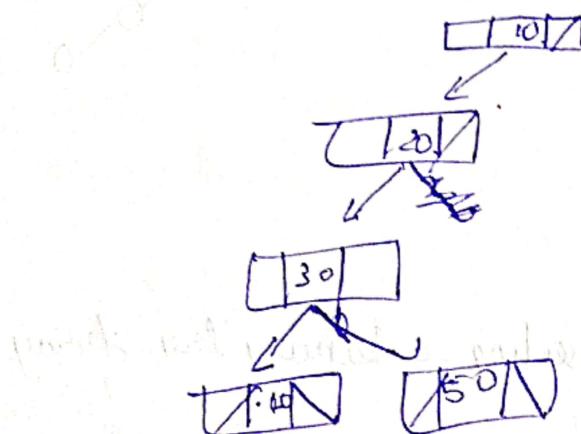
1) Data field \rightarrow stores data

- 2) Left field \rightarrow address of left subtree (Pointe^r) (Pointer)
 - 3) Right field \rightarrow address of right subtree, i.e., (P^tn)
- ```

struct node {
 int data;
 struct node *left;
 struct node *right;
};

typedef struct node *node;

```



### binary tree traversal :

Traversal is most common operation performed on a tree wherein all nodes of the tree needs to be visited once.

3 types of traversals:

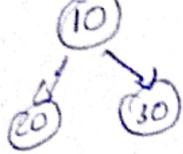
- 1) Pre-order
- 2) In-order
- 3) Post-order.

#### Pre-order:

The recursive definition is given the root node

- i) Traverse left subtree in preorder
- ii) Traverse right subtree in preorder.

Ex:



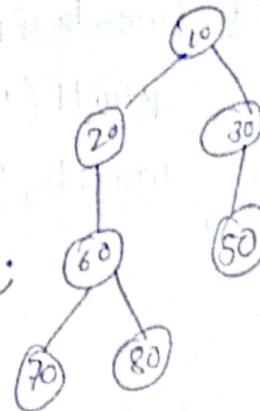
10, 20, 30



10 20 40 50

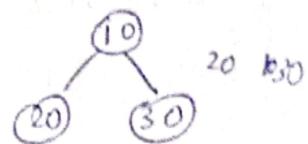
\* C function to perform preorder recursively.

```
Void preorder (NODE *root) {
 if (root != NULL) {
 printf ("%d\t", root->data);
 preorder (root->left);
 preorder (root->right);
 }
}
```

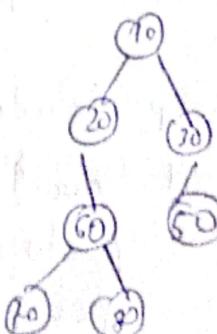


— Recursive definition for in-order traversal (in-order traversal)

- i) visit the left subtree recursively in inorder.
- ii) visit the root node.
- iii) visit right subtree in inorder.



20 70 80 10 50 30



- 2) Left
- 3) Right

C function to perform inorder

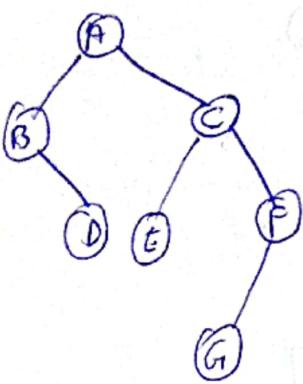
```
Void inorder(NODE root) {
 if (root != NULL) {
 inorder(root->left);
 printf("%d ", root->data);
 inorder(root->right);
 }
}
```

Recursive definition for post-order traversal

- i) Visit left subtree recursively in post order
- ii) Visit right subtree recursively in post order
- iii) Visit root node

70 80 60 20 50 30 10

```
void postorder(NODE root) {
 if (root == NULL) {
 postorder(root->left);
 postorder(root->right);
 printf("%d ", root->data);
 }
}
```



AB D C E F G  
B D A E C G F  
D B ~~E~~ F C A  
E G

pre-order - A B D C E F G

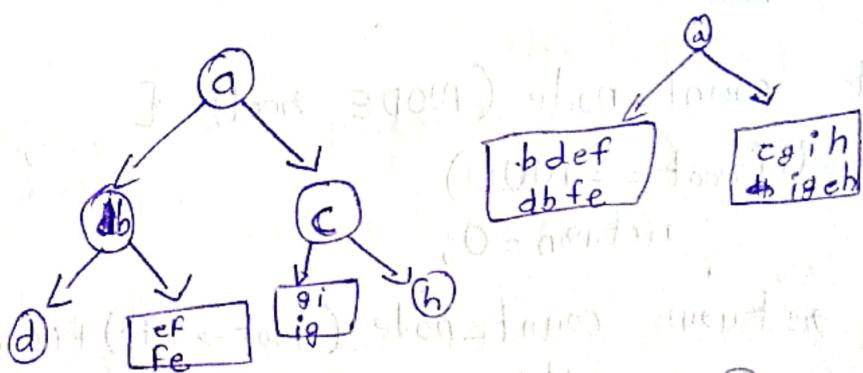
in-order - B D A E C B G F

Post-order - D B E G F C A

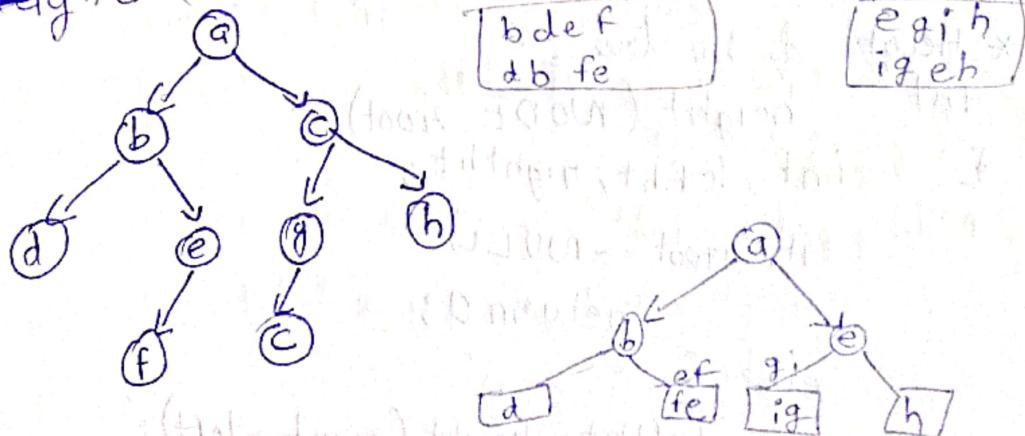
= From given traversal construct the binary tree

pre-order  $\rightarrow$  a b d e f c g i h

inorder  $\rightarrow$  d b f e @ i g h c

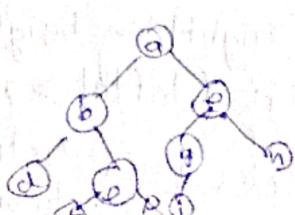


d f e b ~~e~~ i g h c a



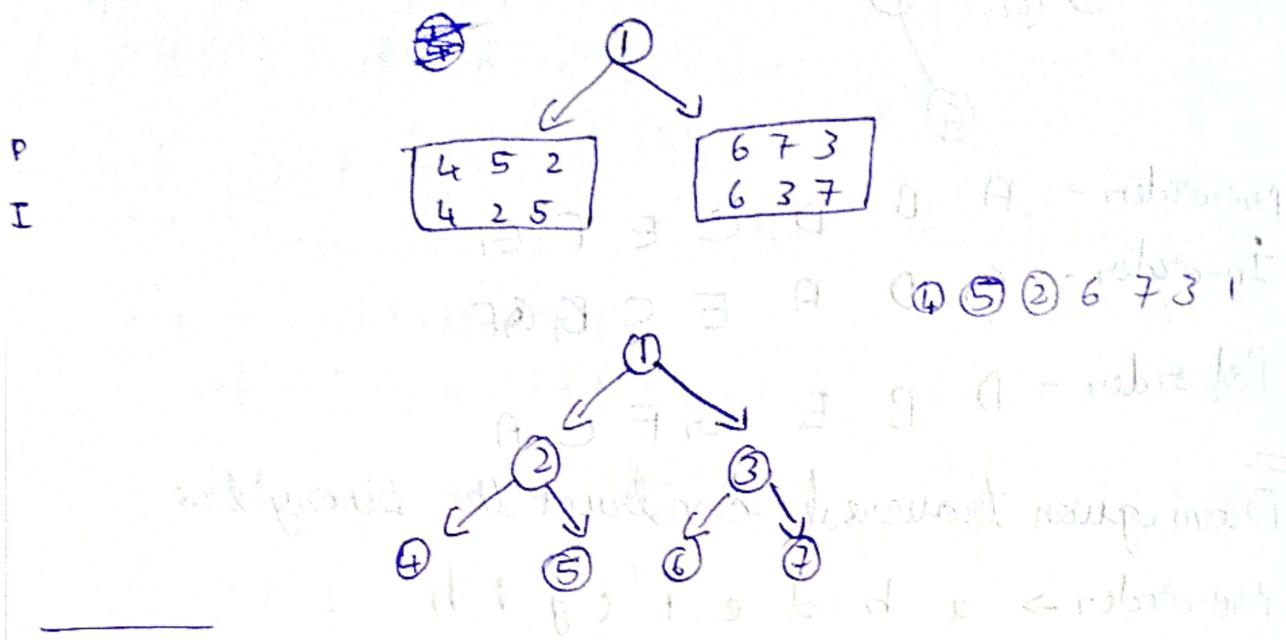
~~a b d f c~~

a b d e f g i h  
d b f e a @ g h c



Postorder : 4 5 2 6 7 3 ①

Inorder : 4 2 5 1 6 3 7



\* C function to find number of nodes in a binary tree

int count\_node (NODE root) {

    if (root == NULL)  
        return 0;

    return count\_node (root->left) + count\_node (root->right) + 1;

}

\* Height of the tree :-

int height (NODE root)

{ int leftht, rightht;

    if (root == NULL)

        return 0;

    else {

        leftht = height (root->left);

        rightht = height (root->right);

        if (leftht > rightht)

            return leftht + 1;

        else return rightht + 1;



C function to count number of leaf nodes.

```
int count_leaf(NODE root) {
 if (root == NULL)
 return 0;
 else if (root->left == NULL && root->right == NULL)
 return 1;
 else
 return count_leaf(root->left) + count_leaf(
 root->right);
```

C function to count non-leaf nodes.

```
int count_nonleaf(NODE root) {
 if (root == NULL)
 return 0;
 else if (root->left == NULL && root->right == NULL)
 return 0;
 else
 return count_nonleaf(root->left) + count_nonleaf(
 root->right) + 1;
```

C function to create a node for a binary tree / bst.

```
NODE createnode (NODE root, int item) {
 NODE temp;
 temp = (NODE) malloc (sizeof (struct node));
 temp->data = item;
 temp->left = NULL;
 temp->right = NULL;
 return temp;
```

7



Scanned with OKEN Scanner

Create binary tree and perform operation on binary tree.

```
#include <stdio.h>
#include <stdlib.h>
```

```
struct node {
 int data;
 struct node *left;
 struct node *right;
};

typedef struct node *NODE;
```

```
void display(NODE root) {
 if (root != NULL) {
 display(root->left);
 printf("%d\n", root->data);
 display(root->right);
 }
}
```

```
}
```

```
// write create-node function
```

```
NODE insertleft(NODE root, int item) {
 root->left = create_node(item);
 return root->left;
}
```

```
NODE insertright(NODE root, int item) {
 root->right = create_node(item);
 return root->right;
}
```

```
}
```

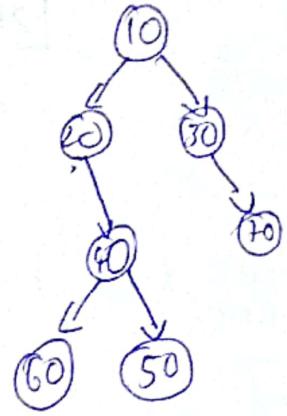
```
// write count-nodes function
```

```
// write height function
```

```

int main () {
 NODE root=NULL;
 root=createNode(10);
 insertleft(root, 20);
 insertright(root, 30);
 insertleft(root->left, 40);
 insertright(root->right, 70);
 insertleft(root->left->left, 60);
 insertright(root->left->right, 50);
 insertright(-
 printf("\nTree data are\n");
 display(root);
 printf("\nNumber of node S=%d\n", countNodes(root));
 printf("\n Height of tree = %d\n", height(root));
 return 0;
}

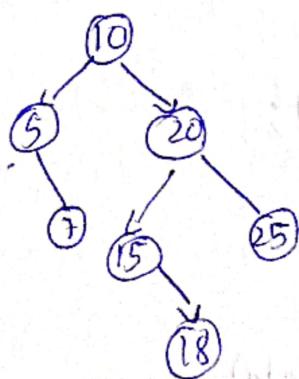
```



### Binary search tree

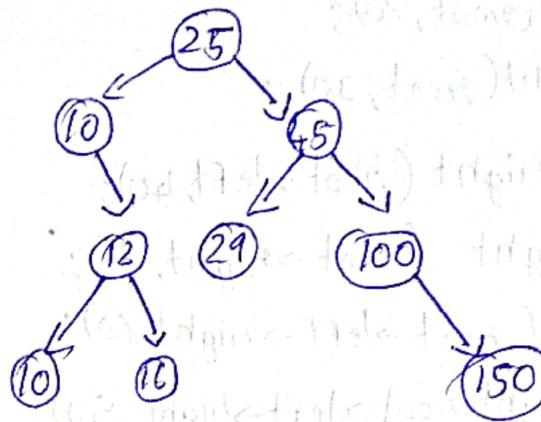
It is a binary tree wherein each node  $x$  has a property such that left child of  $x$  should have less value and right child  $x$  can have either greater or equal value.

Traversal → sorted



Construct B.S.T for elements

[25, 45, 10, 29, 100, 12, 16, 10, 150]



#### 10) B.S.T and operations

```
#include <stdio.h>
#include <stdlib.h>

typedef struct node {
 int data;
 struct node *left;
 struct node *right;
};

typedef struct node *NODE;

// write create_node function
// preorder, inorder, postorder.

NODE InsertBST(NODE root, int item) {
 NODE temp;
 temp = create_node(item);
 if (root == NULL)
 return temp;
 else {
 if (item < root->data)
 root->left = insertBST(root->left, item);
 else
 root->right = insertBST(root->right, item);
 }
}
```

else  
     $\text{root} \rightarrow \text{right} = \text{insertBST}(\text{root} \rightarrow \text{right}, \text{item})$

}

Inorder NODE inorderSuccessor (NODE root) {  
    NODE cur;  
    cur = root;  
    while (cur  $\rightarrow$  left != NULL)  
        cur = cur  $\rightarrow$  left;  
    return cur;  
}

NODE deletenode (NODE root, int key)  
    NODE temp;  
    if (root == NULL)  
        return NULL;  
    if (key < root  $\rightarrow$  data)  
        root  $\rightarrow$  left = deletenode (root  $\rightarrow$  left, key);  
    else if (key > root  $\rightarrow$  data)  
        root  $\rightarrow$  right = deletenode (root  $\rightarrow$  right, key);  
    else {  
        if (root  $\rightarrow$  left == NULL) {  
            temp = root  $\rightarrow$  right;  
            free (root);  
            return temp;  
        }  
        if (root  $\rightarrow$  right == NULL) {  
            temp = root  $\rightarrow$  left;  
            free (root);  
            return temp;  
        }  
        temp = inorderSuccessor (root  $\rightarrow$  right);  
        root  $\rightarrow$  data = temp  $\rightarrow$  data;  
    }



Scanned with OKEN Scanner

```

root->right = deleteNode(root->right, temp->data);
}
return root;
}

int main() {
NODE root=NULL;
int ch,item,key;
for(;;) {
printf("1. Insert \n 2. Inorder\n 3. Preorder\n 4. Postorder\n 5. Traversal\n 6. Delete\n");
printf("Read choice\n");
scanf("%d", &ch);
switch(ch) {
Case 1 : printf("Read item");
scanf("%d", &item);
root=insertBst(root, item);
break;
Case 2 : printf("\n Preorder\n");
preorder(root);
break;
/* Similarly for inorder and post-order */
Case 6 : printf("Node to be deleted");
scanf("%d", &key);
root=deleteNode(root, item);
break;
Default : exit(0);
}
}
return 0;
}

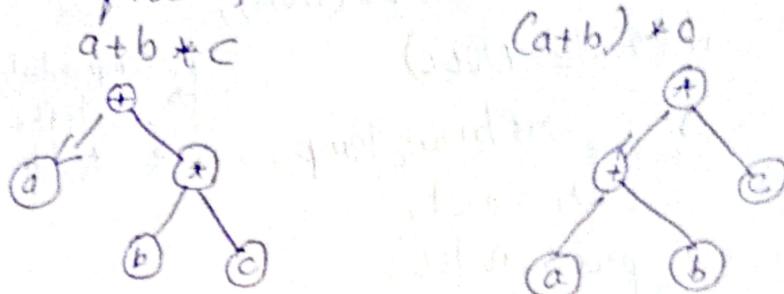
```

write a function to create BST (Non-recursive)

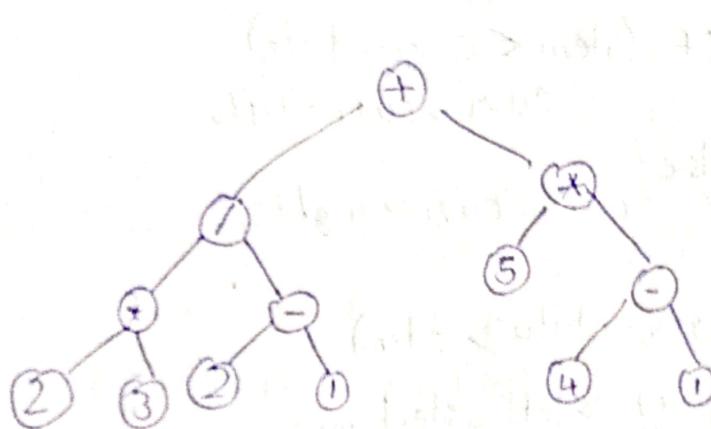
```
NODE insertBST (NODE root, int item) {
 NODE temp, prev, cur;
 temp = create-node(item);
 if (root == NULL) {
 return temp;
 }
 cur = root;
 prev = NULL;
 while (cur != NULL) {
 prev = cur;
 if (item < cur->data)
 cur = cur->left;
 else
 cur = cur->right;
 }
 if (prev->data > item)
 prev->left = temp; temp;
 else
 prev->right = temp;
 return root;
}
```

Expression tree (Pakka)

↳ is a binary tree wherein the given expression (infix) represented in a form of tree where operators are internal nodes and operands are leaf nodes.



$$2 * 3 / (2 - 1) + 5 * (4 - 1)$$



Algorithm to construct an expression tree for a given infix expression (parenthesis free)



- 1) Initialize 2 stacks by name tree stack and operator stack.
- 2) Scan the given infix expression from left to right.
- 3) Create a node for the scanned symbol.
- 4) If scanned symbol is

operand : Push corresponding node onto  
tree stack

operator : Push corresponding node onto

ii) If operator stack is empty push to corresponding node to operator stack.

else

until operator stack is not empty check the precedence of topmost operator on operator stack with precedence of scanned symbol.

If it is greater than or equal.

pop one node from operator stack and pop (2) nodes from 2 stacks and have them as right and left child of the operator node.

Push the <sup>resultant tree</sup> ~~scanned~~ node to tree stack.

5) Until operator stack becomes empty the procedure

6) Pop the tree stack.

| symbol | Tree stack | operator stack | Final tree |
|--------|------------|----------------|------------|
| (      | ①          | empty          |            |
| )      | ②          | ⊕              |            |
| *      | ③(②)       | ⊕              |            |
| /      | ④, ⑤       | ⊕              |            |
| *      | ⑥          | ⊕              |            |
| /      | ⑦          | ⊕              |            |

### Program 8:

```
#include <stdio.h>
#include <stdlib.h>
#include <ctype.h>

struct node {
 char item;
 struct node *left;
 struct node *right;
};

typedef struct node *NODE;

struct stack {
 int top;
 NODE data[10];
};

typedef struct stack STACK;

NODE createnode (char item) {
 NODE temp;
 temp = (NODE) malloc (sizeof (struct node));
 temp->data = item;
 temp->left = NULL;
 temp->right = NULL;
 return temp;
}

void push (STACK *s, NODE item) {
 s->data[++(s->top)] = item;
}

NODE pop (STACK *s) {
 return s->data[(s->top)--]; }
```

```
int precedence(char symbol) {
 switch(symbol) {
 case '#': return 5;
 case '*':
 case '/': return 4;
 case '+':
 case '-': return 3;
 }
}
```

```
void preorden (NODE root) {
 if (root != NULL) {
 printf("%c", root->data);
 preorden (root->left);
 preorden (root->right);
 }
}
```

```
void inorder (NODE root) {
 if (root != NULL) {
 //printf("%c", r-
 inorder (root->left);
 printf("%c", root->data);
 inorder (root->right);
 }
}
```

```
void postorden (NODE root) {
 if (root != NULL) {
 postorden (root->left);
 postorden (root->right);
 printf("%c", root->data);
 }
}
```

```

Node create_exptree (NODE root, char infix[10]) {
 STACK TS, OS; char symbol;
 TS.top = -1;
 OS.top = -1;
 NODE temp, t
 int i;
 for (i=0; infix[i] != '\0'; i++) {
 symbol = infix[i];
 temp = createnode (symbol);
 if (isalnum (symbol))
 push (&TS, temp);
 else {
 if (OS.top == -1)
 push (&OS, temp);
 else {
 while (OS.top != -1 && preced (OS.data[OS.top].data) >
 preced (symbol)) {
 t = pop (&OS);
 if (t->right == pop (&TS));
 if (t->left == pop (&TS));
 push (&TS, t);
 }
 push (&OS, temp);
 }
 }
 }
}

```

```
while(OS.top != -1) {
 t = pop(&OS);
 t->left = pop(&TS);
 t->right = pop(&TS);
 push(t, &TS, t);
}
return pop(&TS);
}
```

```
int main() {
 NODE root = NULL;
 char infix[10];
 printf("\n Read the infix expression");
 scanf("%s", infix);
 root = create_exp_tree(root, infix);
 printf("\n Preorder : ");
 preorder(root);
 /* Inorder and Postorder */
 return 0;
}
```

## HEAP

Heap is a binary tree with the following property

- 1) Structural property
- 2) Parent dominant property

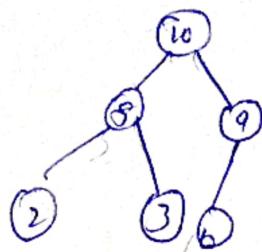
It should be a complete binary tree.

Parent dominant property means parent node should be

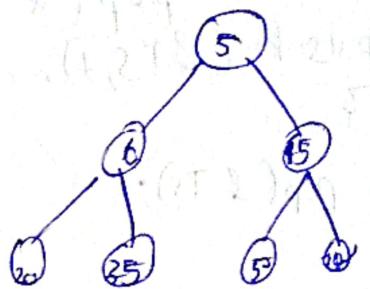
more dominant than its children.

Two types of heap:

1) MAX HEAP:



2) MIN HEAP:

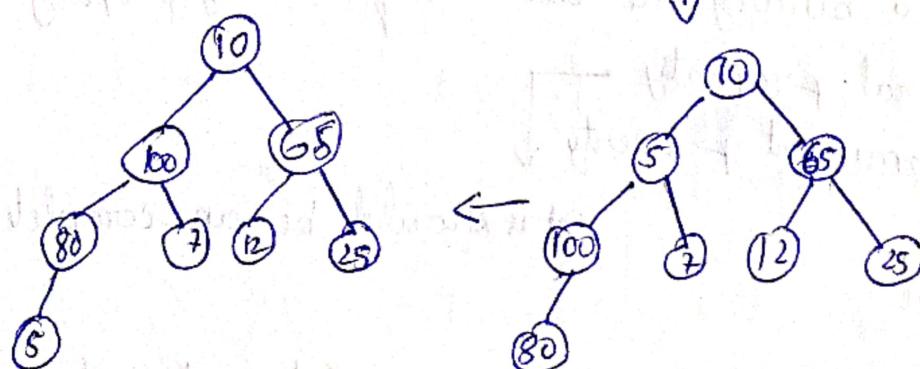
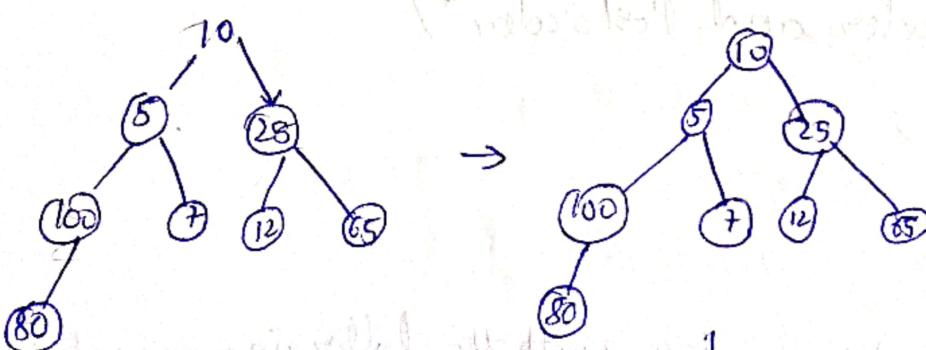


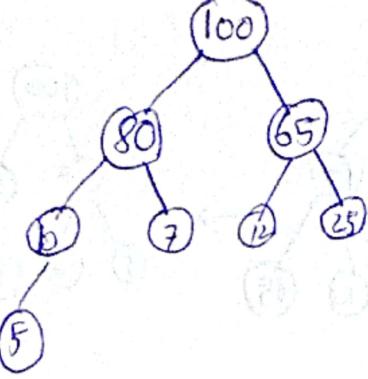
Two methods of constructing a heap

- 1) Bottom up approach
- 2) Top down approach

Construct max and a min heap using bottom up approach

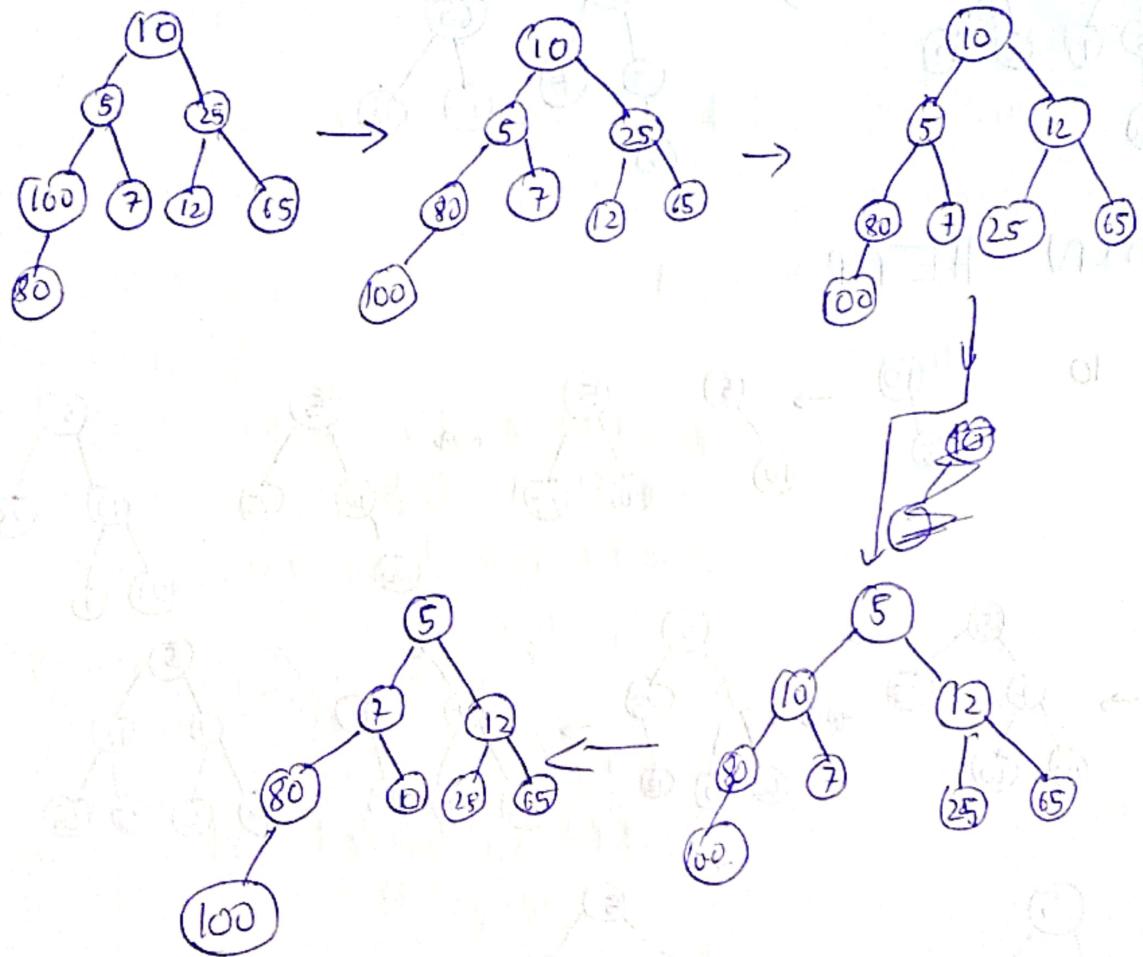
10 5 25 100 7 12 65 80





Transform and Conquer

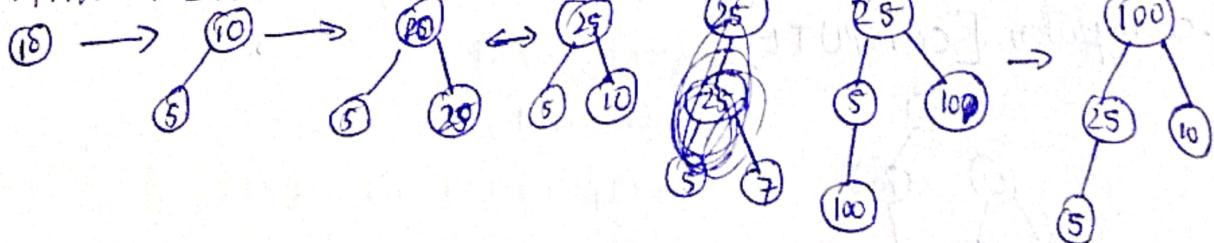
min heap

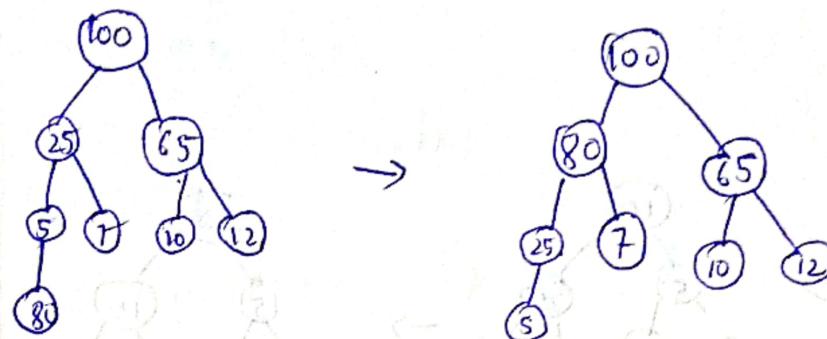
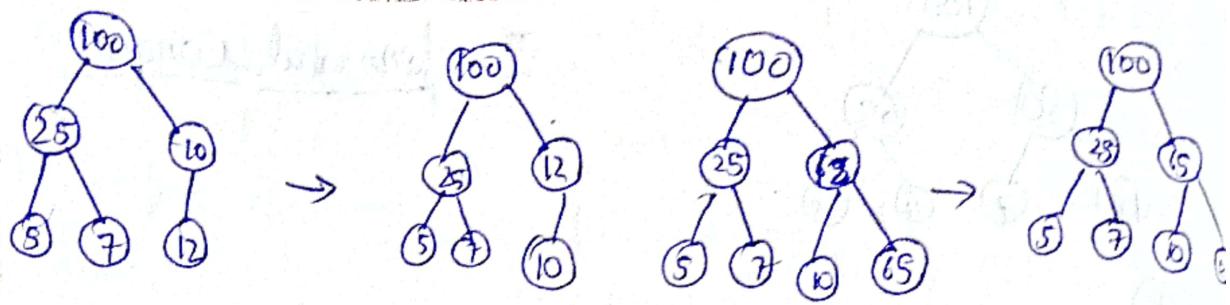


Top down approach  
construct max heap and min heap using

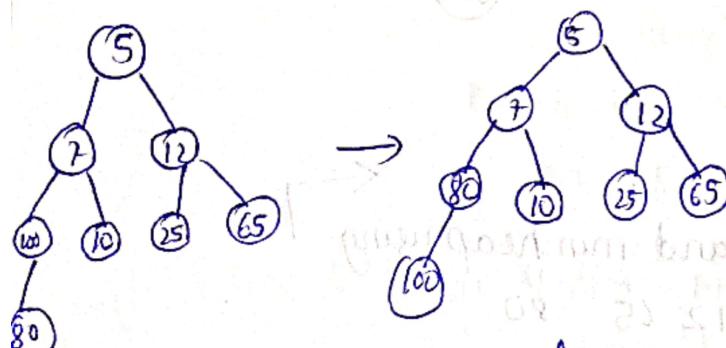
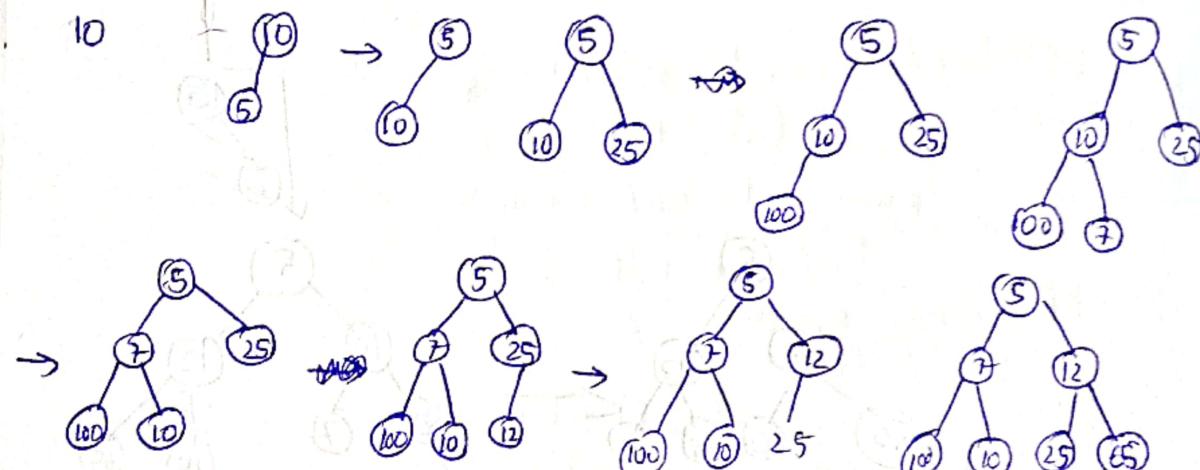
10 5 25 100 7 12 15 80

MAX HEAP

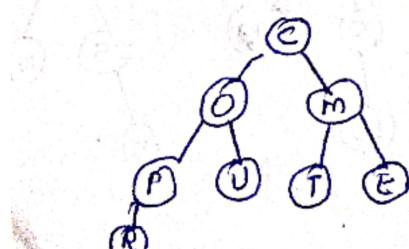


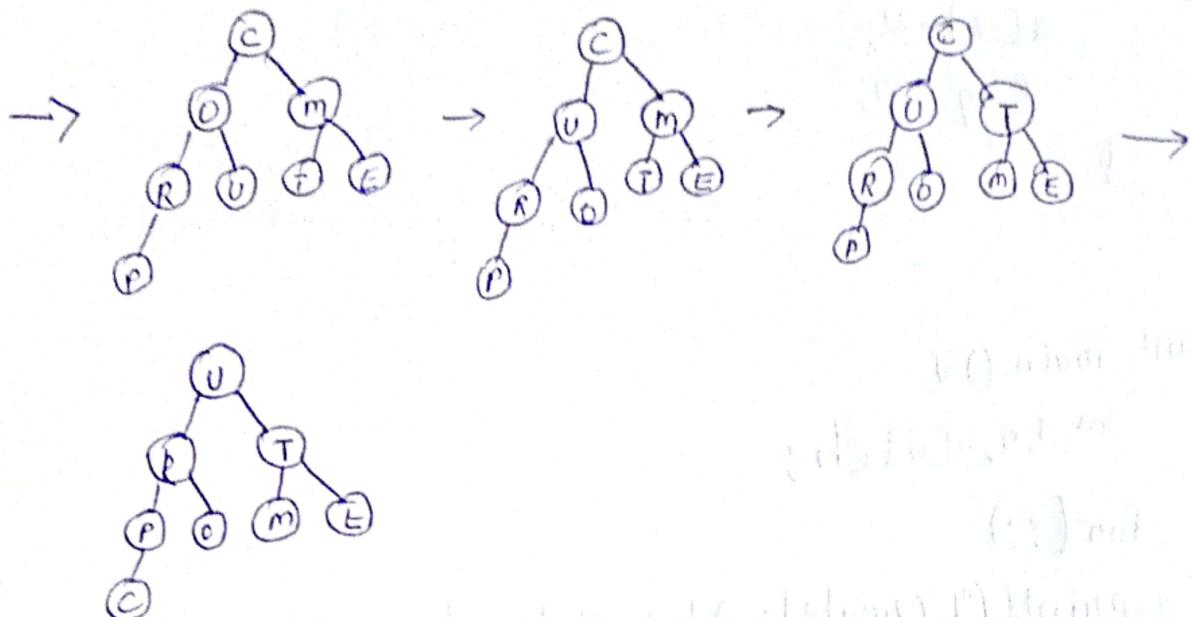


MIN HEAP



construct a max heap for the characters of the word computer [COMPUTER]





### Program - 7

To implement priority queue, using heap tree.

```
#include <stdio.h>
#include <stdlib.h>
void heapify(int t a[10], int n){
 int i, j, k, v, flag = 0;
 for(i = n/2; i >= 1; i--) {
 k = i;
 v = a[k];
 while(!flag && 2 * k <= n) {
 j = 2 * k;
 if(j < n) {
 if(a[j] < a[j + 1])
 j = j + 1;
 }
 if(v >= a[j])
 flag = 1;
 else {
 if(a[k] >= a[j])
 k = j;
 }
 }
 }
}
```

$a[k] = v;$

Flag = 0;

}

int main () {

int i, n, a[100], ch;

for ( ; )

printf("1. Create heap \t 2. Extract max \t 3. Exit");

~~printf("Read choice : \n");~~

scanf("%d", &ch);

switch(ch) {

case 1 : printf("Read no of elements");

scanf("%d", &n);

printf("\n Read elements");

for (i=0; i<n; i++)

scanf("%d", a[i]);

heapify(a, n);

printf("\n Elements after construction of heap\n");

for (i=0; i<n; i++)

printf("%d\t", a[i]);

case 2 : if (n >= 1)

printf("\n Elements deleted is

%d", a[0]);

a[0] = a[n]

n=n-1;

heapify(a, n); if (n == 0) {

printf("Elements after reconstruction");

for (i=0; i<n; i++)



```
printf("%d\n", a[i]);
break;
default:
 exit(0);
}
return 0;
}
```