



Aa



# GRAPHS...

video-33

"let's make it easy too"



If you have tried my  
Graph Concepts & Qns playlist,  
these Qns, will seem very easy.  
Do try it once ;)

## Find Critical and



## Pseudo-Critical Edges In Minimum Spanning Tree



Aa



companies :-

 Meta

*Am,*

Pre-requisite for this video :-

Minimum Spanning Tree | Easy Theory Full Detail | Amazon, Microsoft | Graph Concepts & Qns - 33  
codestorywithMIK

Prim's Algorithm | Minimum Spanning Tree | Full Dry Run | INTUITION | Graph Concepts & Qns - 34  
codestorywithMIK

Min Cost to Connect All Points | Prim's Algorithm | META | Graph Concepts & Qns - 35 | Leetcode-1584  
codestorywithMIK

Kruskal's Algorithm | Minimum Spanning Tree | Full Dry Run | INTUITION | Graph Concepts & Qns - 36  
codestorywithMIK

DSU

Kruskal's , DSU

Even if you don't revise them, I am going to make this easy. let's go...

# 1489. Find Critical and Pseudo-Critical Edges in Minimum Spanning Tree

Hard 844 71 Add to List Share

Given a weighted undirected connected graph with  $n$  vertices numbered from  $0$  to  $n - 1$ , and an array `edges` where `edges[i] = [ai, bi, weighti]` represents a bidirectional and weighted edge between nodes  $a_i$  and  $b_i$ . A minimum spanning tree (MST) is a subset of the graph's edges that connects all vertices without cycles and with the minimum possible total edge weight.

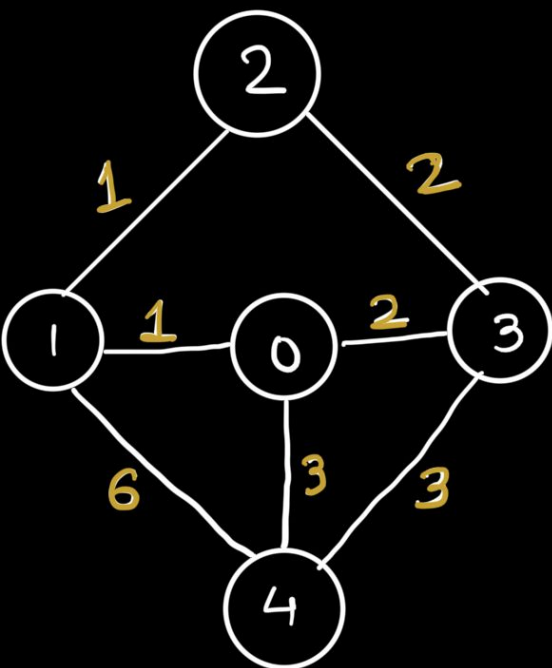
Find all the critical and pseudo-critical edges in the given graph's minimum spanning tree (MST). An MST edge whose deletion from the graph would cause the MST weight to increase is called a critical edge. On the other hand, a pseudo-critical edge is that which can appear in some MSTs but not all.

Note that you can return the indices of the edges in any order.

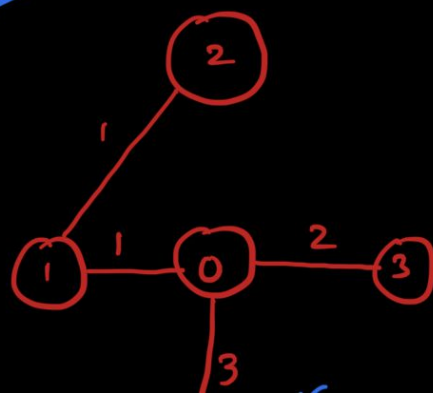
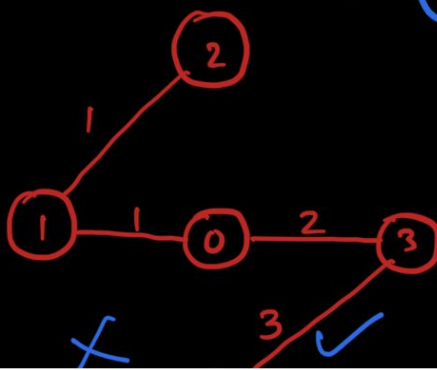
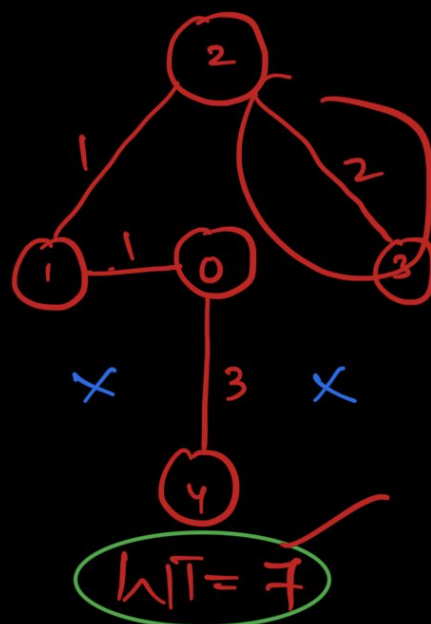
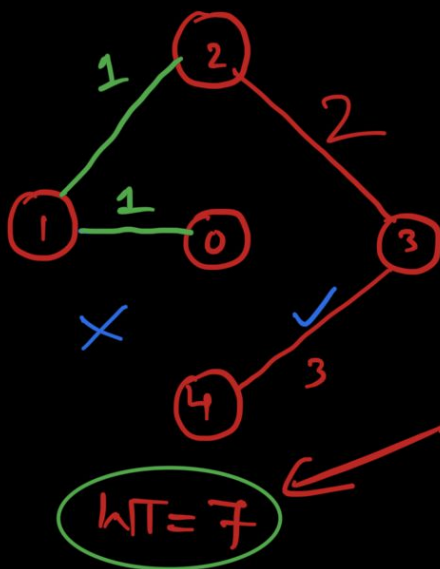
Example :-  $n = 5$

$edges = [\{0, 1, 1\}, \{1, 2, 1\}, \{2, 3, 2\}, \{0, 3, 2\}, \{0, 4, 3\}, \{3, 4, 3\}, \{1, 4, 6\}]$

CE  $\{1, 0\}$  PC  $\{2, 3, 4, 5\}$

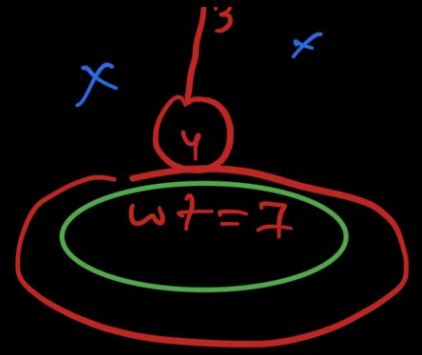
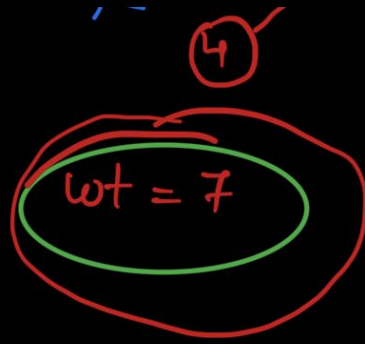


$wT = 21$   
 $V = 5$





Ad



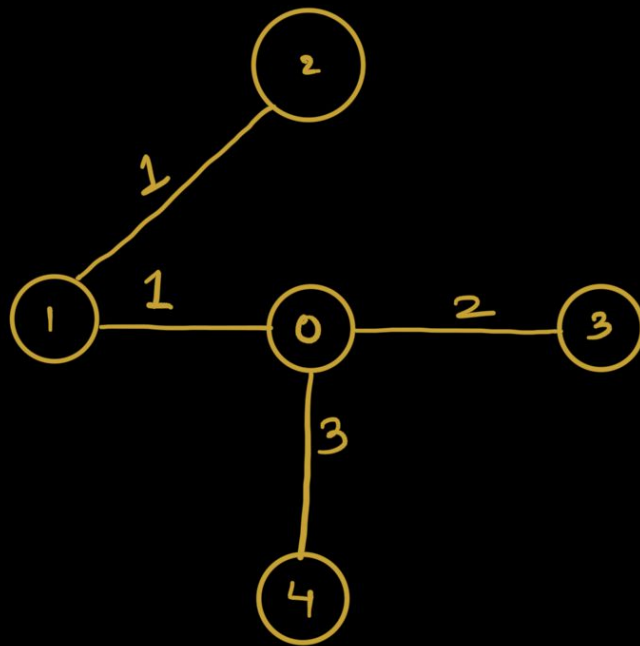
# Quick Recap of

## Kruskal's :-

Sort

Sorted (wt.) & we added index.

<sup>0</sup>  
 $\{0, 1, 1, 0\}$ ,  $\{1, 2, 1, 1\}$ ,  $\{0, 3, 2, 3\}$ ,  $\{2, 3, 2, 2\}$ ,  
 $\{0, 4, 3, 4\}$ ,  $\{3, 4, 3, 5\}$ ,  $\{1, 4, 6, 6\}$



MST-WEIGHT  
= 7

## Steps :-

- ① Push original index also ✓
- ② Sort based on weight ✓
- ③ Find MST-WEIGHT → Kruskal's Algo ✓
- ④ Check each edge →
  - ① skip (Krusk).
  - ② Add (Krusk).

KR  
DSU

MST-WEIGHT = 7

<sup>0</sup>  
 $\{0, 1, 1, 0\}$ ,  $\{1, 2, 1, 1\}$ ,  $\{0, 3, 2, 3\}$ ,  $\{2, 3, 2, 2\}$ ,  
<sup>i</sup>  
 $\{0, 4, 3, 4\}$ ,  $\{3, 4, 3, 5\}$ ,  $\{1, 4, 6, 6\}$

$u = 0$   
 $v = 1$   
 $wt = 1$   
 $idx = 0$   
 $skipwt = \text{Kruskal}(skip = i);$   
 $if (skipwt > MST-WEIGHT) \{$   
 $\quad \text{critical.push\_back}(idx);$   
 $\} else if$   
 $include_{add}$

$== MST\_wt$

Pseudo-Critical :-

$\text{Kruskal}(add\_edge) \{$

$wt == MST\_wt$

Pseudo-Critical :-

Kruskal (add\_edge) {

wt == MST wt.

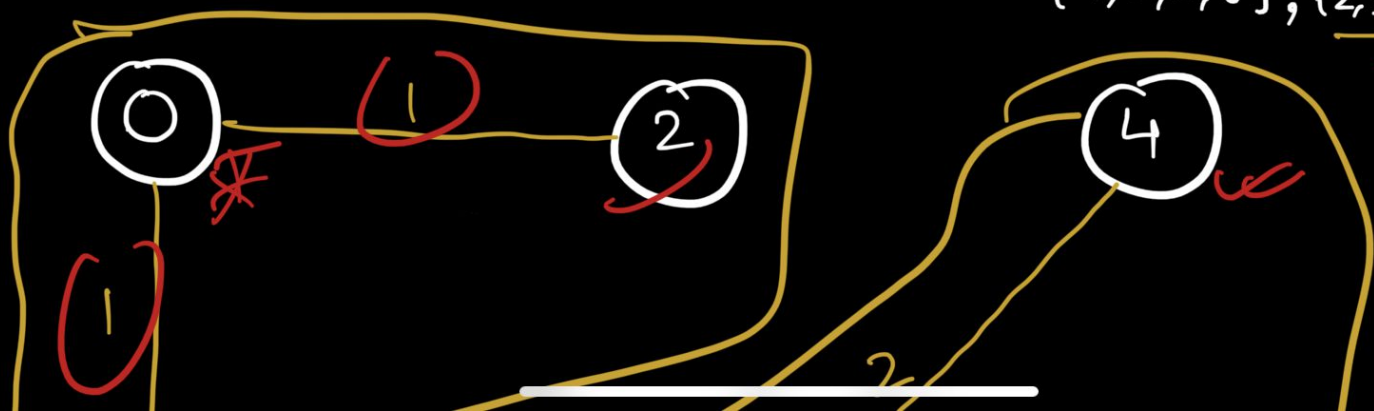
}

MST<sub>3</sub>

MST<sub>4</sub>

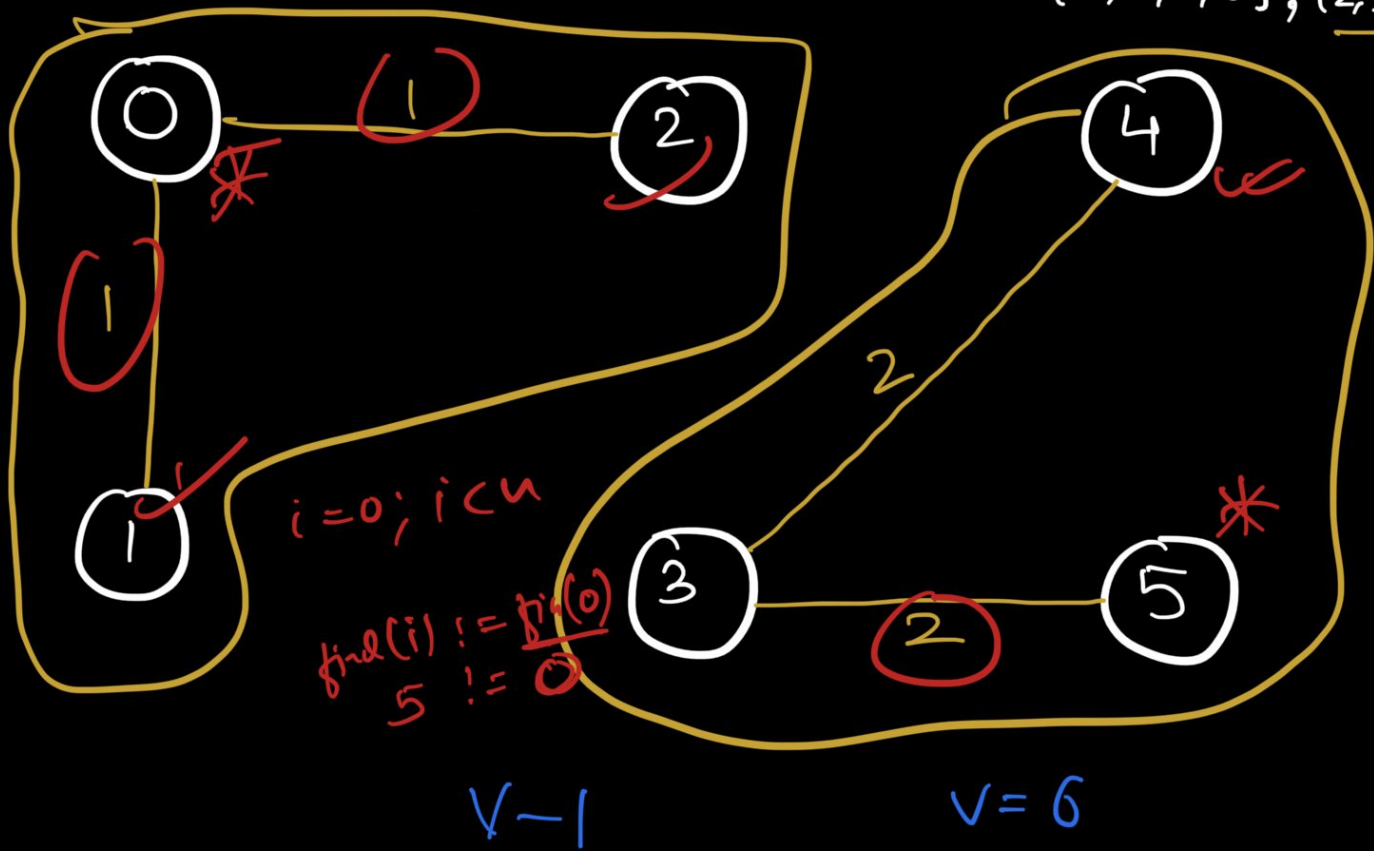
MST-WEIGHT = 10

{0, 1, 1, 0}, {0, 2, 1, 2}, {1, 2, 1, 1}, {3, 4, 2, 4}, {3, 5, 2, 5},  
{4, 5, 2, 6}, {2, 3, 4, 3} }  
skip



MST-WEIGHT = 10

{0,1,1,0}, {0,2,1,2}, {1,2,1,1}, {3,4,2,4}, {3,5,2,5},  
{4,5,2,6}, {2,3,4,3} }  
 skip



if  $(\text{Kruskal}(i, -1) > \text{MST}_e)$   
 (min)

ans: ( )



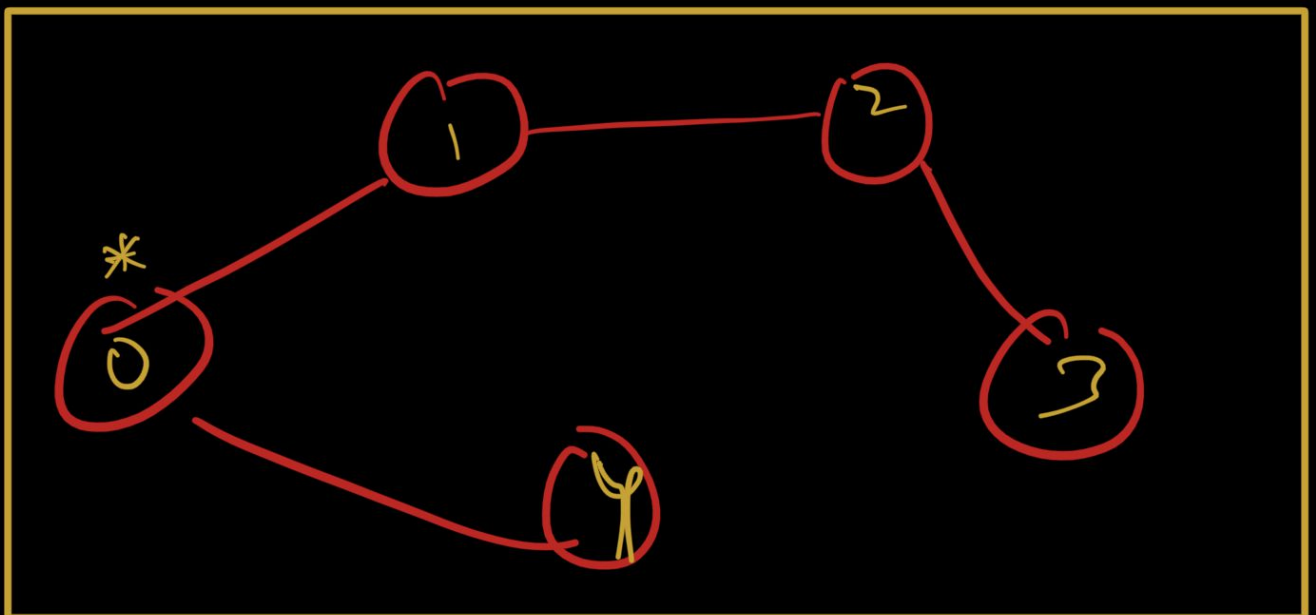
$$if \left( \overset{6}{\text{Kruskal}(i, -1)} \right) > MST_e$$

(min)

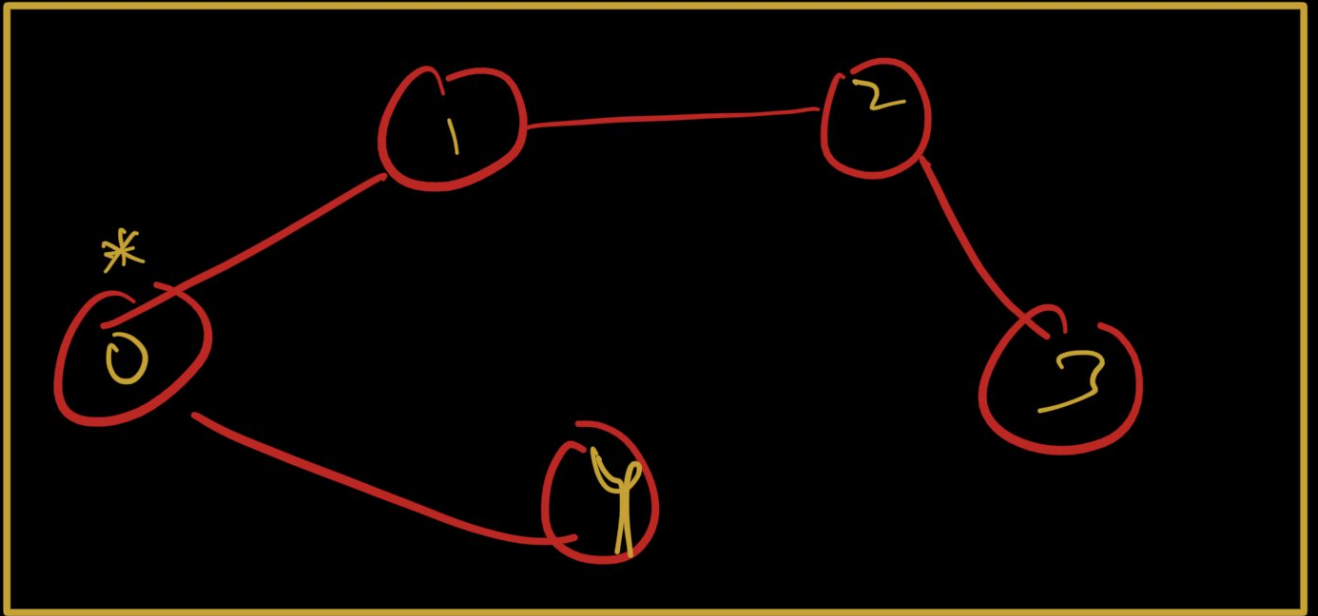
ex: ( — )

Kruskal:

MST (Connected)



# MST (Connected)



n.

```
for (i=0; i<n; i++) {  
    if ( find(i) != find(0) )  
        return ∞  
}
```