

## Agenda for today's live Session

### Application of Divide and Conquer

#### Selection Procedure

##### Problem Statement :

**Input : An array of n elements and the value of k**

**Output : To return kth smallest element**

##### Selection Procedure Algorithm :

Value of m is computed with the help of Partition algorithm that we have studied earlier in Quicksort Algorithm concept.

$m = \text{Partition}(\text{arr}, p, q) \quad O(n)$

```
SelectionProcedure(arr,p,q,k){  
    if(k == m){  
        return arr[m];           O(1)  
    }  
    else if(k < m){  
        SelectionProcedure(arr,p,m-1,k);    T(m-p)  
    }  
    else if(k > m){  
        SelectionProcedure(arr,m+1,q,k);    T(q-m)  
    }  
}
```

##### Recurrence Relation of Selection Procedure :

$$T(n) = O(n) + O(1) + T(m-p) \text{ or } T(q-m)$$

Note : Here, either we go towards left part or right side in an array and this is the reason I mentioned **or** between  $T(m-p)$  and  $T(q-m)$ .

**Best case scenario :**

$$T(n) = O(n) + T(n/2)$$

Using master's theorem

$$n^{\log_b a} = n^{\log_2 1} = n^0 = 1$$

$$f(n) = n$$

Overall time complexity =  $O(n)$

**Worst case scenario :**

$$T(n) = O(n) + T(n-1)$$

Using substitution method,

$$T(n) = O(n^2)$$