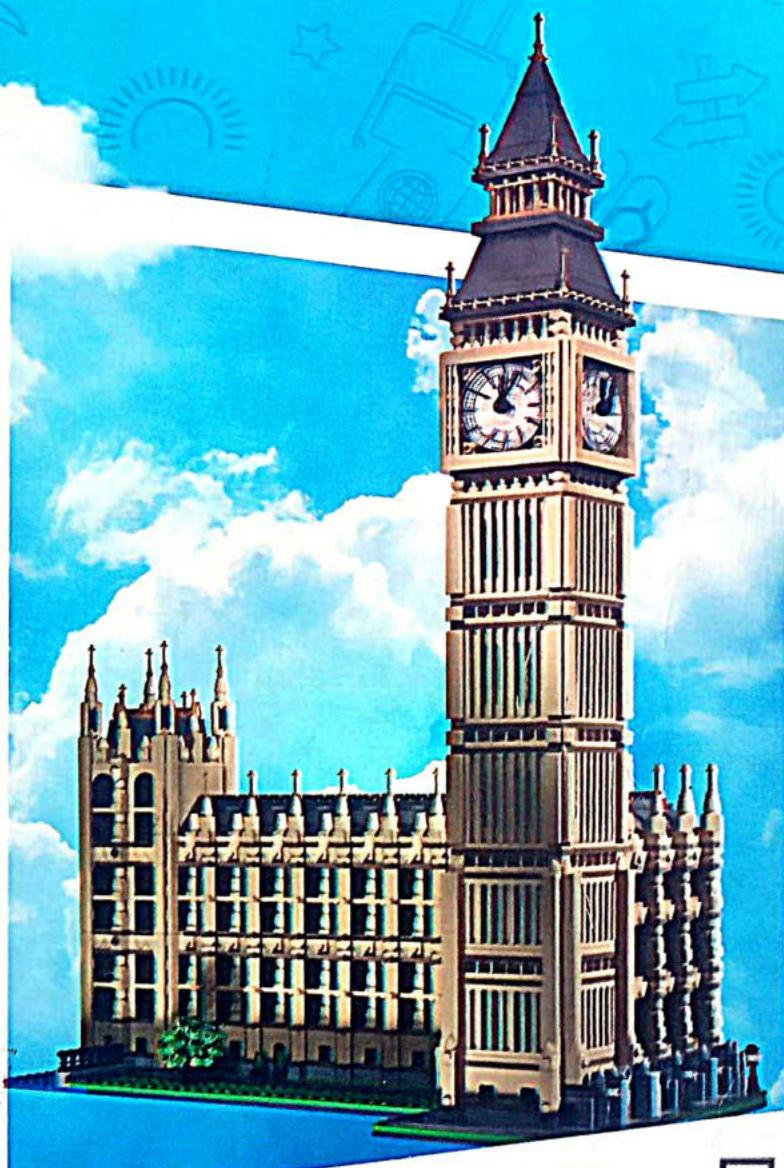




BIG BEN LONDON



#NOTEBOOKS



student exercise
notebook



"Consistency is the key to success"

| Serial No. | Date | Title | Page No. | Teacher's Sign/Remarks |
|------------|------|---|----------|------------------------|
| 1 | | Complete Java | | |
| 2 | | Complete DSA | | |
| 3 | | Live Resume Preparation | | |
| 4 | | Live Interview Preparation | | |
| 5 | | Coding Question on all important topic | | |
| | | <u>Topic</u> | | |
| | | <u>Basic</u> | | |
| 1 | | Basic of programming | | |
| 2 | | Loop function | | |
| 3 | | array | | |
| 4 | | 2D array & String | | |
| | | <u>DS A</u> | | |
| 1 | | Problem solving technique | | |
| 2 | | Object oriented programming | | |
| 3 | | Linear Data Structure | | |
| 4 | | Tree | | |
| 5 | | Advanced Data Structure | | |
| 6 | | Dynamic Programming | | |
| | | <u>Path</u> <u>Placement</u> | | |
| Step 1: | | Learn a language | | |
| Step 2: | | DSA | | |
| Step 3: | | Project, theory sub, resume, refresher, interview preparation | | |

DSA

Problem Solving technique * Recursion & Bit manipulation
* Time space Complexity

① First Month :-

- * Basic \rightarrow Java
- * Basic D.S - Array, String \rightarrow LeetCode 100%
- * Time & space Analysis, searching, sorting

② Second Month :-

- * Recursion & Advance sorting
- * Prefix sum, sliding window, Math (sieve)
- * OOPS, linked list.

③ Third Month :-

- * Stack & Queue
- * Tree
- * Hashmap & Heap (putta their implementation)

④ Fourth Month :-

- * Dynamic Programming
- * Greedy & Backtracking
- * Bit Manipulation
- * graph

Java

first program:-

```
public class JavaClass {  
    public static void main(String args[]) {
```

Y Y || boilerplate code

output in Java

```
System.out.print("Hello world"); → statement terminator  
          ↓  
        function   output
```

Example:-

```
public class JavaExample {
```

```
    public static void main(String args[]) {
```

```
        System.out.print("Hello world");
```

Y Y

Output: Red Hello World

system.out.println("Hello world");

```
system.out.println("Hello world");
```

or

```
System.out.print("Hello world") + " my name is
```

```
mohit Kumar Yadav" + " Rohit");
```

Point Pattern:-

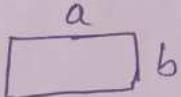
* * *

**
*

public class JavaBasic {
 public static void main (String args[]) {

 System.out.print ("*****\n" + "****\n" + "
 m| * * *\n xx | m x");

➤ Variable in Java



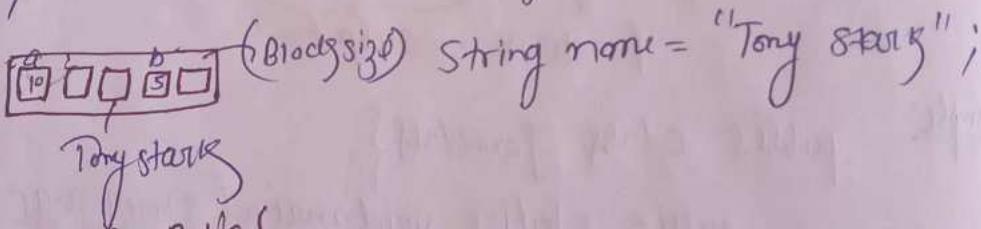
$$\text{Perimeter} = 2 * (a+b)$$

$$a = 10$$
$$b = 20$$

✓ Variable
Literal Constant

int a = 10; (a, b, c Variable) { Identifier
int b = 5;

Memory:-



* public class JavaBasic {
 public static void main (String args[]) {
 int a = 5;
 System.out.print (a);
 }

a = 5;
System.out.println (a);

} output = a

Data type in Java

Primitive (already existing) Non primitive (Create)
byte String, Array, class, object
short int, long, float interface
char double
boolean

Java → Typed language { 3.14 (float)
{ 10.5 decimal

Example:

```
public class forabasic {  
    public static void main(String Arg[]){
```

```
        byte b = 8;  
        System.out.println(b);
```

```
        char ch = 'a';
```

```
        System.out.println(ch);
```

```
        boolean var = true;
```

```
        System.out.print(var);
```

```
        float price = 10.5;
```

```
        int number = 25;
```

```
        11 long
```

```
        // double
```

```
        short n = 240;
```

Y Y

short → 2 byte

float → 4

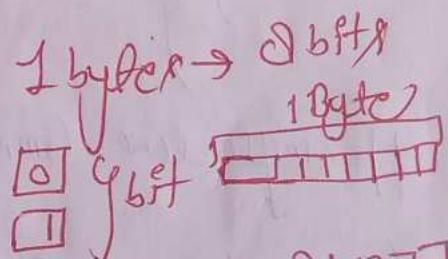
Char → 2

double → 8

boolean → 1

int → 4

long → 8



1 Byte → [128 + 127]

[Sum of a & b]

System.out.print();

int a = 10;

int b = 5;

int sum = a+b;

| a | b | Sum |
|----|---|-----|
| 10 | 5 | 15 |

System.out.print(" sum");

Comment in Java

Eg

```
public class JavaBasic{  
    public static void main(String args[]){
```

// Code to calculate sum or

int a = 10;

int b = 5;

int sum = a+b;

System.out.println(sum);

}
}

// single line Comment

/* */ multiline Comment

import java.util.*; Import in Java

public class JavaBasic{

 public static void main(String Arg[]){

 Scanner sc = new Scanner(System.in);

 String input = sc.next();

 System.out.println(input);

 }

 || string input = sc.next();

 || System.out.println(name);

 int number = sc.nextInt();

 System.out.println(name);

 or

 int number = sc.nextInt();

 System.out.println(number);

Output:
Rohit
Rohit

next
nextLine
nextInt
nextByte
nextFloat
nextDouble
nextShort
nextLong

sc.nextDouble()

Sum of a & b

int a = sc.nextInt();

int b = sc.nextInt();

int sum = a + b;

System.out.println(sum);

import java.util.*;

public class JavaBasic {

public static void main (String args[]) {

Scanner sc = new Scanner (System.in);

int a = sc.nextInt();

int b = sc.nextInt();

int sum = a+b;

System.out.println (sum);

y
y

Product of a & b

Scanner

input a . (sc.nextInt())

input b . (sc.nextInt())

int product = a * b;

sys.out.println (product)

import java.util.*;

public class JavaBasic {

public static void main (String args[]) {

Scanner sc = new Scanner (System.in);

int a = sc.nextInt();

int b = sc.nextInt();

```

int product = a * b;
System.out.println(product);
    
```

Area of Circle

②

$$\text{rad} =$$

$$\boxed{\text{area} = \pi r^2}$$

```

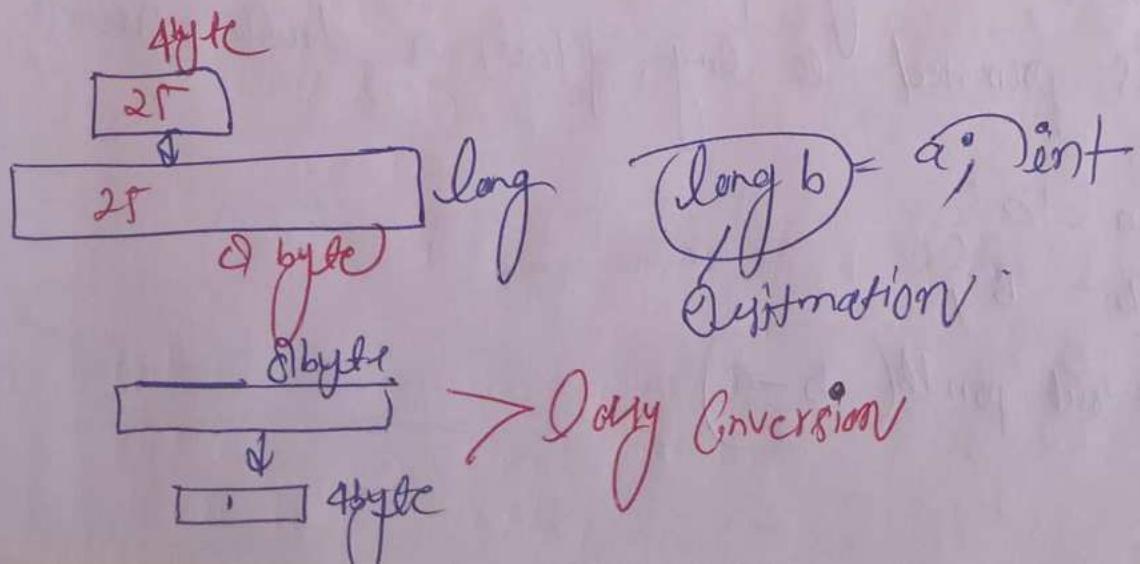
float area = 3.14f * rad * rad +
    sys.out.println(area);
    
```

Type Conversion

Conversion happen when:-

- ④ type compatible int → float int → boolean
- ⑤ destination type > source type

byte > short > int > float > long > double



Type Casting

Java not allow but casting

```
float a = 25.0;  
int b = a;
```

```
float a = 25.12f;
```

```
int b = (int)a;
```

```
int b = (int)a;
```

```
System.out.println(b);
```

Type Promotion

- Java automatically promotes code type byte, short & char operand to int when evaluating an expression.
- If one operand is long, float, or double, the whole expression is promoted to long, float, or double respectively.

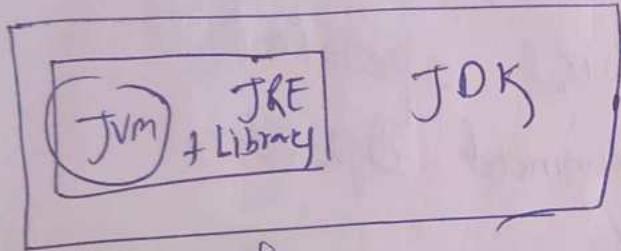
Eg

```
Char a = 'a';
```

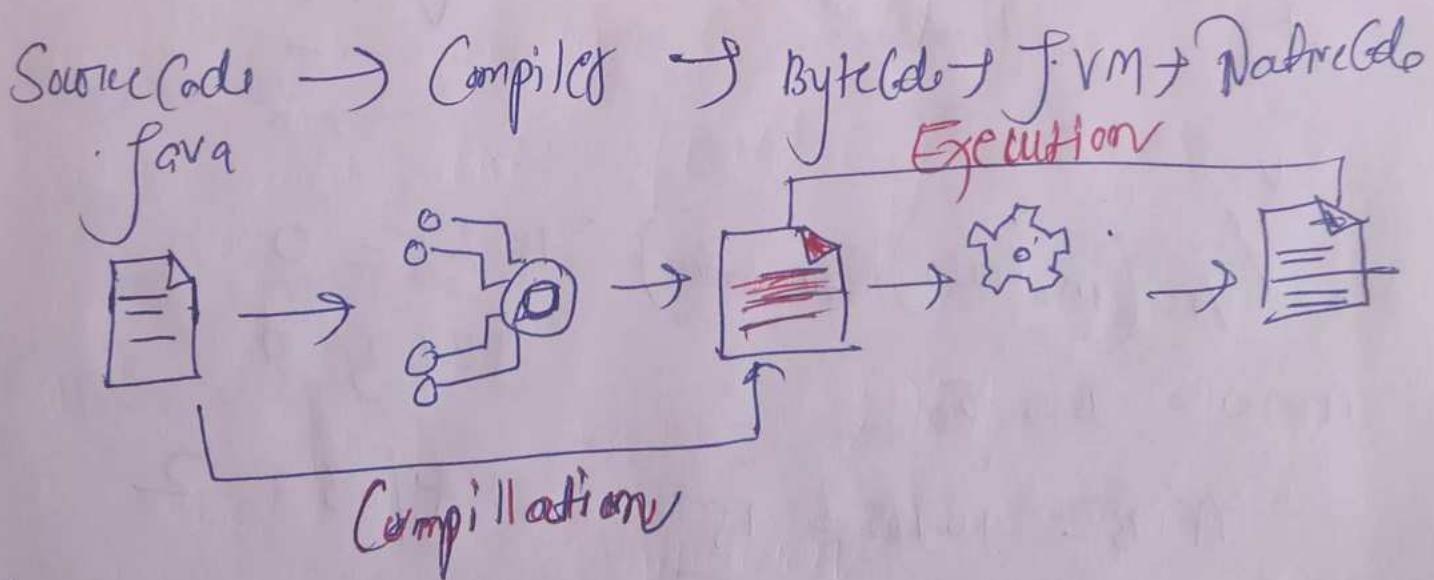
```
Char b = 'b';
```

```
System.out.println(b-a)
```

How Code is Running



Java
Runtime
Environment



G

Practice :-

Day 2 Operator in Java

4 Symbol that tells compiler to perform some operation.

$$\text{Sum} = a + b$$

operator = (+, -, *, /)

operator

operand

- ### Type of operators:-
- ① **Arithmetic operator** (Binary/Unary)
 - ② **Relational operator**
 - ③ **Logical operator**
 - ④ **Bitwise operator**
 - ⑤ **Assignment Operator**

Arithmetic Operator

Binary

+

-

*

/ % (modulo) remainder

$$A=10 \quad B=5$$

Unary

++

--

$$12 \% 3 = 0$$

$$A+B = 10+5 = 15 \quad 14 \% 3 = 2$$

$$A-B = 10-5 = 5$$

$$A*B = 10*5 = 50$$

$$A/B = 10/5 \rightarrow 2$$

Program:-

```

int A = 10;
int B = 5;
System.out.println ("Add = " + (A+B));
System.out.println ("Subtract = " + (A-B));
System.out.println ("Multiplication = " + (A*B));
System.out.println ("Divide = " + (A/B));
System.out.println ("Modulus (Remainder) = " + (A%B));
}

```

Unary operators:-

$a = a + 1 \Rightarrow a++$ or $+a$ increment
 $a = a - 1 \Rightarrow a--$, $-a$ decrement

Post increment
 $a++$ \leftarrow value of $a + 1$

- ① $\overset{++a}{\text{Value Change}}$
- ② Value ~~all~~

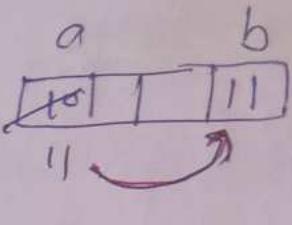
```

int a = 1;
int b = ++a;
System.out.println(a);
System.out.println(b)

```

Output:- 11

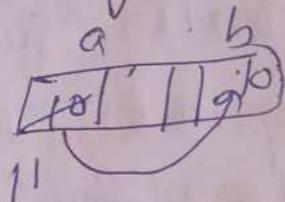
int a = 10;
int b = a++;



Post increment:

- ① Value. use
- ② Value change.

int a = 10;
int b = a++;



output: 10 11
10

post increment

4 Pre Decrement

- ① Value change
- ② Value use

int a = 10;
int b = --a;

S.O.P.L. 9

Relational operator:

$= = \rightarrow$ equal
 $\neq \rightarrow$ Not equal

$A = = B \rightarrow$ False
(10) (5)

$>$
 $<$
 \geq
 \leq

int A=5;

int B=6;

S.O.PLn((A==B));

Output \rightarrow false.

$>$
int a=5;
int b=6;

S.O.PLn((a>b));

Output \rightarrow false.

! = int A=10;

int B=10;

S.O.PLn(A!=B));

$>=$

int a=10;

int b=10;

S.O.PLn(A<=B));

\rightarrow True.

Logical operators:

8 & (Logical AND)

11 (Logical OR)

! (Logical NOT)

| | |
|--------|-------|
| 37 2 | true |
| 11 = 1 | false |
| 57 10 | false |

| Ans | Statement 1 | | S.O.PLn((3>2) & (5>0)); |
|-----|-------------|---|---------------------------|
| | T | F | |
| T | T | T | Output \rightarrow True |
| F | T | F | |
| F | F | T | (3>2) & (5>0); |
| F | F | F | <u>False</u> |

11 (Logical OR)

| Ans | S+1 | S+2 | System.out.println((372) (57)) |
|------------------------------------|-----|-----|--|
| T | T | T | |
| T | T | F | outputs - True |
| T | F | T | Yy |
| F | F | F | true \rightarrow False False \rightarrow Null |
| $(\rightarrow \text{logical Not})$ | | | |
| Ans | S+1 | S+2 | System.out.println(1075); |
| F | T | F | Yy |

Assignment Operator

= $A = B$ $A = 0$
 (10) (5)

+= $A = A + 10$ $B = B + 5$

-= $A = A - 10$ $B = B - 5$

*= $A = A * 10$

/= $A = A / 10$

int A = 20;
 B = A + 10;
 System.out.println(A);
 output \rightarrow 20.

 B = 10;
 B = B + 5;
 B = B - 5;
 print(B);

```
int B=5;  
B*=5;      B=B or B=B*5;  
prompt(B)  
output → 25
```

Condition Statement:-

if, else
else if
Ternary operator
switch

Day 3 Conditional Statement

If-else statement

```
if (condition) {  
    // code  
} else {  
    // code  
}
```

if (condition) {
 // code
} else if (condition) {
 // code
} else {
 // code
}

if (condition) {
 // code
} else if (condition) {
 // code
} else if (condition) {
 // code
} else {
 // code
}

if (condition) {
 // code
} else {
 // code
}

```
Ex int age = 22;  
if (age >= 10)  
    sys.out("Date ,drive");  
else {  
    sys.out(" not Adult");  
}
```

```
int age = 22;  
if (age >= 18) {  
    System.out.println("Adult : drive, Date");  
} else {  
    System.out.println("not Adult");  
}
```

② if ($age > 13 \& age < 10$) {
 System.out.println("Teenaged");
}

Point the Largest of 2:-

$$A = 1, B = 3$$

$A > B$ if true \rightarrow print "A"

else false \rightarrow print "B"

```
if ( $A > B$ ) {  
    System.out("A");  
}  
else {  
    System.out("B");  
}
```

```

Q) int A=1;
   int B=5;
   if(A >= B) {
       System.out.print("A is largest of 2");
   } else {
       System.out.println("B is largest of 3");
   }

```

#3 Point if a number is Even or odd:-

4 (even) → divisible of 2 or multiple of 2.

$$a \% b = 0$$

1 (odd)

$$\text{even \% 2} = 0$$

$n \% 2 == 0$ } True (Even) else print("odd")

Ques: import java.util.*;

public class JavaLab11 {

 public static void main (String args[]) {

 Scanner sc = new Scanner (System.in);

 int number = sc.nextInt();

 if (number % 2 == 0) { System.out.print("Even"); }

 else { System.out.print("odd"); }

Else if Statement:-

```

if ((Condition 1) {
    |
}
else if ( Condition 2) {
    |
}
else {
    |
}

```

Code:

```
int age = 13;
```

```
if (age == 18) {
```

```
    System.out.println("Adult");
```

```
    else if (age >= 13 & age < 18);
```

```
{ System.out.println("Teenager");}
```

```
else {
```

```
    System.out.println("Child");
```

```
}
```

Income Tax Calculator:-

① Income < 5 l
O.T. Pay

```
int income
```

```
int taxCalculator
```

② Income between 5L

20% tax

income > 5L

30% tax

if (income < 5L) {

 tax = 0;

else if (income >= 5L & income <

 tax = income * (0.2);

else

 tax = income * (0.3)

Code:-

```
Scanner sc = new Scanner(System.in);
```

```
int income = sc.nextInt();
```

```
if (income < 500000) {
```

 tax = 0;

```
else if (income >= 500000 & income < 1000000) {
```

 tax = (income * 0.2);

```
else {
```

 tax = (income * 0.3);

```
System.out.println ("your tax is: " + tax);
```

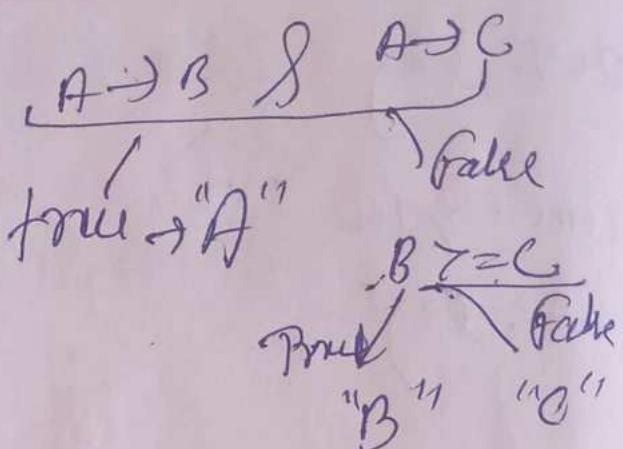
Output:-

y Point the largest of 3 numbers

$$A=1 \quad B=3 \quad C=6$$

If ($A >= B$) && ($A >= C$) {

 print("A")



y else if ($B >= C$) {

 print("B")

else print("C")

Code: int A=1, B=3, C=6;

If ($A >= B$) && ($A >= C$) {

 System.out.println("largest of A");

~~Else if~~ System.out.println(

else if ($B >= C$) {

 System.out.println("largest of B");

else { System.out.println("largest of C"); }

} }

Ternary Operator

Variable = Condition ? statement1 : statement2;
 ↓
 Check → $\begin{cases} \text{true} \\ \text{false} \end{cases}$

Ex boolean larger = (5 > 3) ? 5 : 3;
 ↓
 true → Statement1 false → Statement2

String type = (5 % 2 == 0) ? "even" : "odd";

Code:- int number = 4;
 // ternary operator

String type = ((number % 2) == 0) ? ~~odd~~ "Even" : "odd";
 System.out.println(type);

Check Student Pass or fail:

marks >= 33 : Pass

marks < 33 : fail

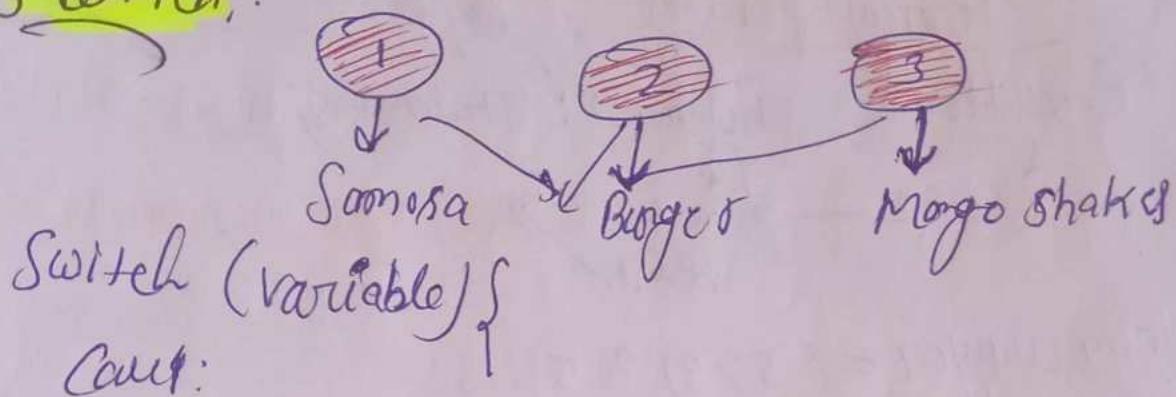
int marks

String status = marks >= 33 ? "Pass" : "Fail";
 print(status)

Ex int marks = 67;

String reportCard = marks >= 33 ? "Pass" : "Fail";
 print(reportCard);

Switch:



Case:

Case 1

Case 2

default:

}

int number=2;

switch (number){

Case 1: System.out.print("Samosa");

Case 2: " (" Burger");

Case 3: " (" mango shake");

Case default: - " (" we wake up");

}

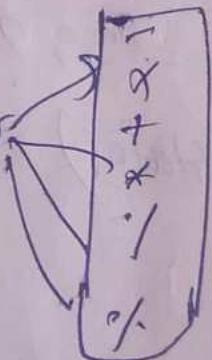
Calculator

+,-,*,,/,%

int a

int b

char → operator



Code:-

```
Scanner sc = new Scanner(System.in);
int a = sc.nextInt();
System.out.println("Enter b:");
int b = sc.nextInt();
System.out.println("Enter operator:");
char op = sc.next().charAt(0);
```

Case '+' : System.out.println(a+b);

Case '-' : break;

Case '*' : System.out.println(a*b);

Case '/' : break;

Case '%' : break;

default : ("Wrong calculator");

}

Day 4 "Loop"

↳ For repeating → Loop

Ex System.out.println("Hello Word");
 System.out.println("Hello Word");



① while loop

② for loop

③ do while loop

while loop

```
while (Condition){  
    // do something  
}
```

while (Condition) {
 System.out.println("Hello World");
}

b) int Counter = 0; ← Initialisation

```
while (Counter < 10){  
    System.out.println("Hello World");  
    Counter++;  
}
```

Counter → 0, 1, 2, 3

Hello World

Hello World

Hello World

➤ print Number 1 to 10
1 2 3 4 5 6 7 8 9 10 → while

```
int Counter = 1;  
while (Counter ≤ 10){  
    System.out.println(Counter);  
    Counter++;  
}
```

Output:-
1
2
3
4
5
6
7
8
9
10

8 > 2
5 > 3

0

Code

Output

Print

Code

Code

```

int a=1;           ↗ 1000, etc.
while(a<=10){
    System.out.print(a+" ");
    a++;
}

```

Output = 1 2 3 4 5 6 7 8 9 10 - - -

Print Number from 1 to n

```
int n= 20
```

n=7

```

int a=1;
while(a<=n) {
    System.out.print(a);
}

```

Scanner sc = new Scanner()
 or int a = sc.nextInt();
 int a = 1;
 while (counter <= a) {
 System.out.print(a+" ");
 }

Code: import java.util.*;

```
public class Java{
```

```
public static void main (String [] args){
```

```
Scanner sc = new Scanner (System.in);
```

```
int a = sc.nextInt();
```

```
int a = 1;
```

```
while (a<=n) {
```

```
System.out.print(a+" ");
a++;
}
```

Sum of first n Natural Number.

$n=5$

$$1+2+3+4+5=15$$

int $n = \text{sc. next Int();}$ int $n = 5$
 int $a = 0;$ int $\text{sum} = 0;$
 int $a = 1;$ or int $\text{sum} = 0;$
 while $(a <= n) \{$ while $(i <= n) \{$
 $a = a + 1;$ $\text{sum} = \text{sum} + i;$
 $\}$ $\}$

for loop

for (initialization; condition; update){
 counter iteration i < 10 i++ (i = i + 1)
 do something i = i + 1 i = i + 2 (i = i + 2)
 } (i = i - 1) i = i - 2 (i = i - 2)

for (int $i = 1; i < 10; i++) \{$
 say ("Hello World");
 $\}$ $\}$ $\}$

Print Square pattern:-

*** *
*** *
*** *

```
for (int i=1; i<=4; i++) {  
    cout << "*****" << endl;  
}
```

* Print Reverse of Number:-

$$n = 10899 \rightarrow 99801$$

(0) For last digit

$$\text{last digit} = n \% 10;$$

$$n = n / 10; \rightarrow \underline{1089}$$

Ex int n = 10899;

while ($n > 0$) {

 int lastDigit = n % 10;

 System.out.println(lastDigit + " ");

 n = n / 10;

 System.out.println();

numb = $\frac{132}{10}$
removing - last digit

Remove last digit = num / 10

Do-while Loop

```

do {
    // do something
} while (condition)
    do {
        cout << "Hello World";
        a++;
    } while (a <= 10);
    }
}

```

• Break Statement: to exist the loop.

```

for (int i=1; i<=5; i++) {
    if (i == 3) {
        break;
    }
    cout << i;
    system.out.print("I am out of the loop");
}

```

Q If entering number still user enters a multiple of 3

```
do {  
    int n = sc.nextInt(); if (n % 10 == 0)  
        say(n);  
} while (true);
```

Continue Statement

To skip an iteration.

1 to 5
~~i=3~~ ~~skip~~

```
for (int i=1; i<=5; i++)  
    if (i==3){  
        continue;  
        say(i);  
    }
```

Check Number prime or Not

primeNo.: 2, 3, 5, 7, 11

10. Pattern Part I

Nested loop :- if ($a > b$) {
 if ($a > c$) {
 }
 }

E for (int $i=0$; $i < n$; $i++$) {
 for (int $j=0$; $j < m$; $j++$) {

* * → 1 → 2 → 3 → 4 → 5
 * → 1 → 2 → 3 → 4
 * → 1 → 2 → 3 → 4
 * → 1 → 2 → 3 → 4
 * → 1 → 2 → 3 → 4
 * → 1 → 2 → 3 → 4 → 5

① line 4
 ② outer loop → 4 times
 Number of times
 ③ inner loop 5 times
 what print
 " * "

for (int $a=1$; $a \leq 4$; $a++$) {

for (int $y=1$; $y \leq a$; $y++$) {

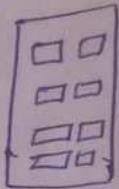
 sysy(" * ");

 y say(); next line

$a = 1$ $y = 1$

Dry Run:

Function / Method



Remote

Blocks of code:

{

y

Syntax:-

```
return Type name();
    || body
    return statement;
}
y
```

function name
 input → output
 a+b sum
 n i to m
 n n!
 class

```
public class JavaBasic {
  public static void main(String args[]) {
    || body      type
    System.out.println("Hello World");
  }
}
```

↳ Making a function:-

```
public static void printHelloWorld() {
  System.out.println("Hello World");
  // return; y
}
```

```
public static void main(String args[]) {
  printHelloWorld();
}
```

Calling →
set function

Method

function का वार्ड के साथ प्रियोग करने का Method

उदाहरण

Syntax with Parameter

return type name (type param1, type param2) {

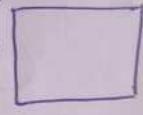
 // body

 return statement; }

}

Input

input
a,b



from
output

Code

```
import java.util Scanner;
```

```
public class JavaBasic {
```

```
    public static void calculateSum() {
```

```
        Scanner sc = new Scanner(System.in);
```

```
        int a = sc.nextInt();
```

```
        int b = sc.nextInt();
```

```
        int sum = a+b;
```

```
        System.out.println("Sum is : " + sum);
```

①

②

```
    public static main (String args) {
```

```
        calculateSum();
```

Function.

```
    public static void calculateSum (int a, int b) {
```

```
        int sum = a+b;
```

```
        return sum;
```

Parameter

Calling + ② main calculateSum (a,b) Argument

④ Parameter vs Argument

Formal param
(definition)

Actual parameter
& Call

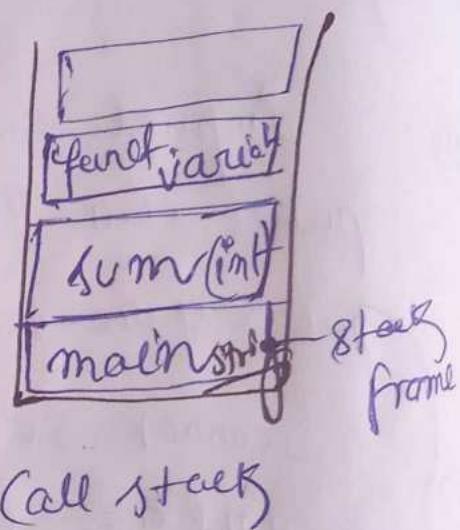
⑤ what happen in Memory

ps. void calculate (int a, int b)

{ int sum = a+b;

p. s. void main() { string age[] }

sum()



call stack

⑥ Call by Value

// swap & value exchange.

int a = 5;

int b = 10;

int c = a;

a = b;

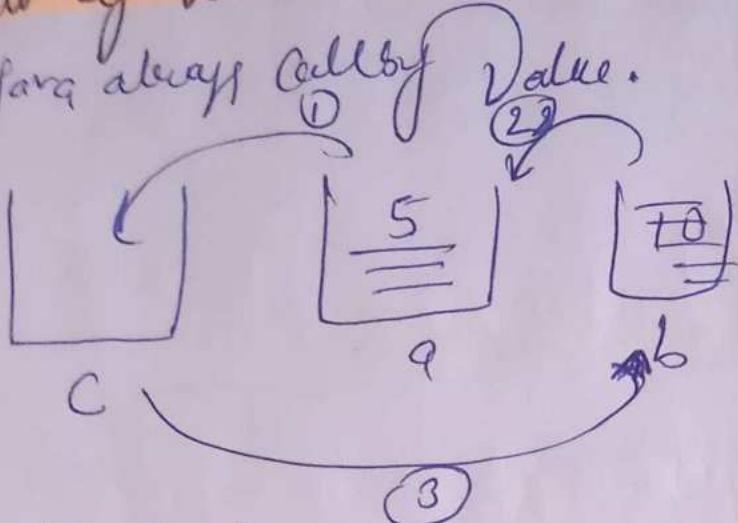
b = c;

Say ("a = " + a);
say("b = " + b); } gg

Call by Value

Call by Reference

\rightarrow Java always Call by Value.



• By function

public static void swap (int a, int b) {

// swap -

int c = a;

a = b;

b = c;

, say ("a = " + a);

, say ("b = " + b);

} public static void main (String args[]) {

int a = 5;

int b = 10;

swap (a, b);

Calling
of function

call by Value

Ex,

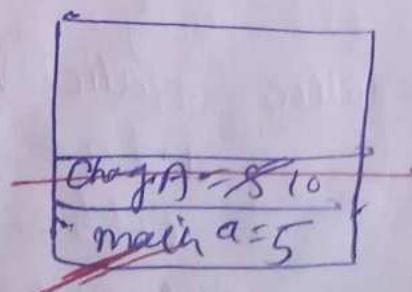
ChangeA (int a) {

a = 10;

psVm () {

int a = 5;

ChangeA (a); say (a); }



• Java always call by value.

```
Change A (int a){  
    y a=10;  
    public void m1{  
        int a=5;  
        Change A (a);  
        say (a);  
    }  
}
```

Change value outside

Find the product of a & b

• $a = 3 \quad b = 5$

```
int multiply (int a, int b){
```

```
    int product = a * b;
```

```
    return product;
```

```
int p = multiply (3, 5);
```

```
print (p);
```

Code:

```
public static void multiply (int a, int b){
```

```
    int product = a * b;
```

```
    return product;
```

```
public static void main (String args[]){
```

```
    int a = 3;
```

```
    int b = 5;
```

```
    int p = multiply (a, b);
```

```
Say ("a * b = " + p);
```

$p = \text{multiply}(10, 20);$
Soy ($a * b \leftarrow " + p$);
yy

Factorial of a Number

$$n=4 \quad n! \Rightarrow n \times (n-1) \times (n-2) \times (n-3) \dots \times 1$$

$$4! = \frac{4 \times 3 \times 2 \times 1}{24} \quad 3! = \frac{3 \times 2 \times 1}{6} \times 9 \text{ are}$$

$$n! = (n-1)! \times n = (n-2)! \times (n-1) \times n$$

$$n! = 1 \times 2 \times 3 \times 4 \times 5 \times \dots \times n$$

Code: public static int factorial (int n){

 int f = 1;
 for (int i = 1; i <= n; i++)

 f = f * i;

 return f;

yy

Explanation

$n=4$

int f = 1

for (int i = 1; i <= n; i++)

 f = f * i;

 return f; ← factorial

yy

$f = 1$ $f = 1 \times 1 = 1$
 $i = 1$ $f = 1 \times 2 = 2$
 $i = 2$ $f = 1 \times 2 \times 2 = 4$
 $i = 3$ $f = 1 \times 2 \times 3 = 6$
 $i = 4$ $f = 1 \times 2 \times 3 \times 4 = 24$

$24 = n! = \underline{\underline{4!}}$

Binomial Coefficient

$n=10 \quad r=2$

$$n(r) = \frac{n!}{r!(n-r)!}$$

factorial(r).

factorial(n) (Reusable)

int binCoeff (int n, int r){

$$n_fact = factorial(n); \quad \text{---} ①$$

$$r_fact = factorial(r); \quad \text{---} ②$$

$$n-r_fact = factorial(n-r); \quad \text{---} ③$$

$$\text{return } BC = a / (b * c);$$

Code:

```
public static int binCoeff (int n, int r){
```

$$\text{int fact_n = factorial(n);}$$

$$\text{int fact_r = factorial(r);}$$

$$\text{int fact_n_r = factorial(n-r);}$$

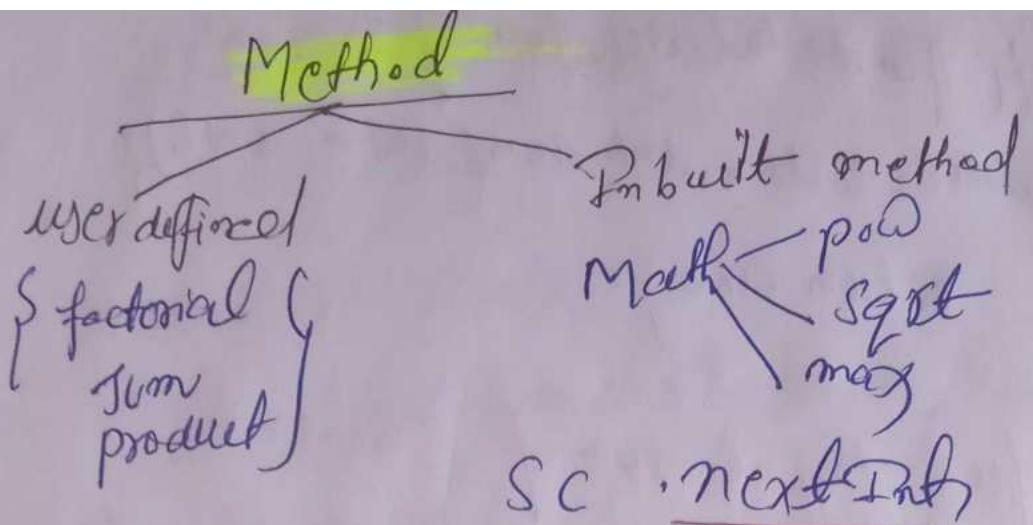
$$\text{int binCoeff = fact_n / (fact_r * fact_n_r)}$$

return binCoeff;

}

```
public static void main (String args [] )
```

$$\text{sof (binCoeff (5, 2));}$$



Function Overloading

* Multiple functions with the same name but different parameters.

Ex Calculator

multiply (int a, int b)
 multiply² (float a, float b)
 multiply³ (double a, double b)
 multiply³ (int a, int b; int c);

Function Overloading Using Parameter

f1: sum of 2 no.

int sum (int a, int b){

 return a+b;

→ only depends on parameter

f2: sum of 3 no. → int sum (int a, int b, int c){
 return a+b+c;

Coding // funct. to Cal sum of 2 num's.
public static int sum(int a, int b){
 return a+b;
}

// funct. to Cal sum of 3 num's:
public static int sum (int a, int b, int c){
 return a+b+c;
}
public static void main (String args){
 System.out.println (sum(3, 5));
 System.out.println (sum(5, 2, 1));
}

→ Function Overloading using Data type

→ f₁: add 2 int Value. int sum(int a, int b){
 return a+b;
}

f₂: add 2 float float sum (float a, float b)
 return a+b;

Code:

```
public static int sum(int a, int b){  
    return a+b;  
}
```

|| function call float:

```
public static float sum(float a, float b){  
    return a+b;  
}
```

```
public static void main(String args[]){  
    System.out.println(sum(3, 5));  
    System.out.println(sum(3.2f, 4.0f));  
}
```

Approach Check if a number is prime or not

① $n \rightarrow 1, n$

for ($\text{int } l=2 \text{ to } l=n-1$)
(n.y. $l==0$) Not prime

Fals \rightarrow Prime

Code:

```
public static boolean isPrime(int n){
```

```
    int lsPrime = true;  
    for ( $\text{int } l=2; l<n-1; l+1$ )  
        if ( $n \% l == 0$ ). Completing condition
```

Many ways

```
if prime = false;  
break;  
return if prime;  
public static main(String args){  
    System.out.println(isPrime(12));  
}
```

Optimised Method: 6

| | | |
|-----------------------------|--|---|
| for (int i=2 to i<=sqrt(n)) | 1×6 2×3 3×2 6×1 | $\theta \rightarrow 1 \times 8$ 2×4 4×2 8×1 |
|-----------------------------|--|---|

```
public static boolean isPrime (int n){  
    for (int i=2; i<=Math.sqrt(n); i++)
```

if ($n \% i == 0$)

return false;

return true;

```
public static void main(String args){
```

System.out.println(isPrime(16));

System.out.println(isPrime(17));

Print all Primes in a Range

$n = 10$

$2 \rightarrow 10$
 $\cancel{2, 3, 5, 7}$

P.S Void PrimeInRange (int n) {

for (int i = 2 to n) {

} If prime(i) = True
fall.

Code: }

public static void primeInRange (int n) {

for (int i = 2 ; i <= n ; i++) {

if (IsPrime(i)) {

Say (i + " ");

} Say ();

public static void main (String args[]) {

primeInRange (20); // 2 to 20

Convert from Binary to Decimal $n=101$

Binary Number System:-

Bit manipulation

Bit Operator

Math \rightarrow Octal

[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]

Decimal Number System

Binary \rightarrow (0, 1)

10 \rightarrow bin

'a' \rightarrow bin

$$(0)_{10} = (0)_2$$

$$(5)_{10} = (101)_2$$

$$(1)_{10} = (01)_2$$

$$(6)_{10} = (110)_2$$

$$(2)_{10} = (10)_2$$

$$(7)_{10} = (111)_2$$

$$(3)_{10} = (11)_2$$

$$(8)_{10} = (1000)_2$$

$$(4)_{10} = (100)_2$$

$$n = 10$$

$$(1000)_2 \rightarrow ()_{10}$$

$$\begin{array}{r} \downarrow \\ 2^2 \quad 2^1 \quad 2^0 \end{array}$$

$$1 \quad 0 \quad 0 \quad 1 \quad 0 \quad (5)_{10}$$

$$1 \times 10$$

$$(1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 0 \times 2^0)$$

Scope Method

① Method Scope method
 function → Var
 ↓

int sum (int a, int b){
 int s = a+b; ← (new declare & init
in parameter)
 } main() { use not var
→ f end var}

Block Scope

{ → Block of ← Block ①
 } Code.
 { } Block ②
 }

~~Ex~~ for (int i=1; i<=5; i++){
 } Block ③

Class Scope

String 1

String are type of object which can store character and elements.

Char [] = { 'a' 'b' 'c' 'd' };

String str = "abcd"

Code:

```
public class Strings {
    public static void main( String args[] ) {
        Char Arr[ ] = { 'a' , 'b' , 'c' , 'd' };
        String str = "abcd";
        String str2 = new String("xyz");
        // String are Immutable Not Change.
    }
}
```

2. Input & output

Scanner sc = new Scanner(System.in);

```
String name;
name = sc.next();
```

System.out.println(name);

}
g

3. String length

String full name = "Denny Starks";

System.out.println(full name.length());

}
g

Output : 10

4. Concatenate

// Concatenation e.g. Add first + last

```

String first name = "Rohit";
String last name = "Yadav";
String name = first name + " " + last name;
System.out.println(name);           Output RohitYadav
    
```

5. String CharAt

```

String first name = "Rohit";
String last name = "Yadav";
String full name = first name + " " + last name;
System.out.println(full name.charAt(0));           Output R
    
```

```
public class String{
```

```
    public static void printLetter(String str){
```

```
        for (int i=0; i<=str.length(); i++)
```

```
            System.out.print(str.charAt(i) + " ");
```

```
    }
```

```
    System.out.println();
```

```
    System.out.println("Full Name = " + str);
```

```
    System.out.println("Length = " + str.length());
```

```
    System.out.println("First Letter = " + str.charAt(0));
```

```
    System.out.println("Last Letter = " + str.charAt(str.length() - 1));
```

```
    System.out.println("Middle Letter = " + str.charAt(str.length() / 2));
```

```
}
```

```
}
```

Ques:-

C. Check the palindrome

"Racecar" "noon" "Madam"
(दोनों देख से Some अलग पाईज़) → Palindrome

for (int i=0; i < length) Racecar

str(i) == str(n-i-1)
0 1 2 3 4 5 6
↓
(n-1-1)

public static boolean isPalindrome (String str){

for (int i=0; i < str.length() / 2; i++) {

int n = str.length();

if (str.charAt(i) != str.charAt(n-1-i)) {

return false;

return true;

public static void main (String args []){

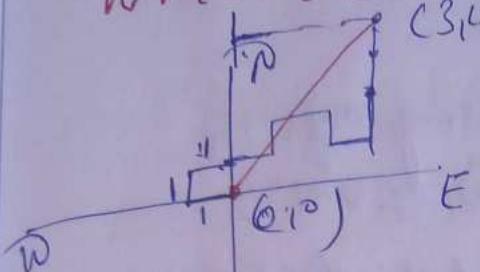
String str = "noon";

System.out.println (isPalindrome (str));

} }

Question given a route containing 4 directions (E, S, N, W)
find the shortest path to reach destination.

"WNENESENNA"



$$x=0$$

$$y=0$$

$$N = y+1$$

$$S = y-1$$

$$W = x-1$$

$$E = x+1$$

Code:

```

if (dir == 'S') {
    y--;
}
else if (dir == 'N') {
    y++;
}
else if (dir == 'W') {
    x--;
}
else if (dir == 'E') {
    x++;
}
    
```

$$\text{displacement} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

| | |
|-------------|---------------|
| $x_2 - x_1$ | $\sqrt{9+16}$ |
| $y_2 - y_1$ | 5 |

public class Route {
 public static int getShortestPath(~~float~~ s, e) {
 int x = 0, y = 0;

for (int i = 0; i < path.length(); i++) {
 char dir = path.charAt(i); // South.
 if (dir == 'S') {
 y--;

$\text{int } X^2 = x * x;$
 $\text{int } Y^2 = y * y;$
return Math.sqrt($X^2 + Y^2$);

(float) // type casting

```
public static void main(String args[])
{
    String path = "WEEENESENNN";
    System.out.println(getShortestPath(path));
}
```

Output 5.0

Q: String function

String s1 = "Tommy";

String s2 = "Tomy";

String s3 = new String("Tomy");

If ($s1 == s2$)

System.out.println("string are equal");

} else

say ("string are not equal");

If ($s1.equals(s3)$)

say ("string are equal");

else { say ("string are not equal") }

9 Substring

"Hello World"
SubString

Substring
 $s_i \rightarrow c_i$
 excluded

$[3, 5] \rightarrow "o w"$
Index SubString

```
> public class Substring {
    public static Substring(string str, int si, int ei) {
        for (int i = si; i < ei; i++) {
            substr += str.charAt(i);
        }
        return substr;
    }
}
```

```
public static void main(String args[]) {
    // SubString
    String str = "Hello World";
    System.out.println(str.substring(0, 5));
}
```

```
Say (str.substring(0, 5));
```

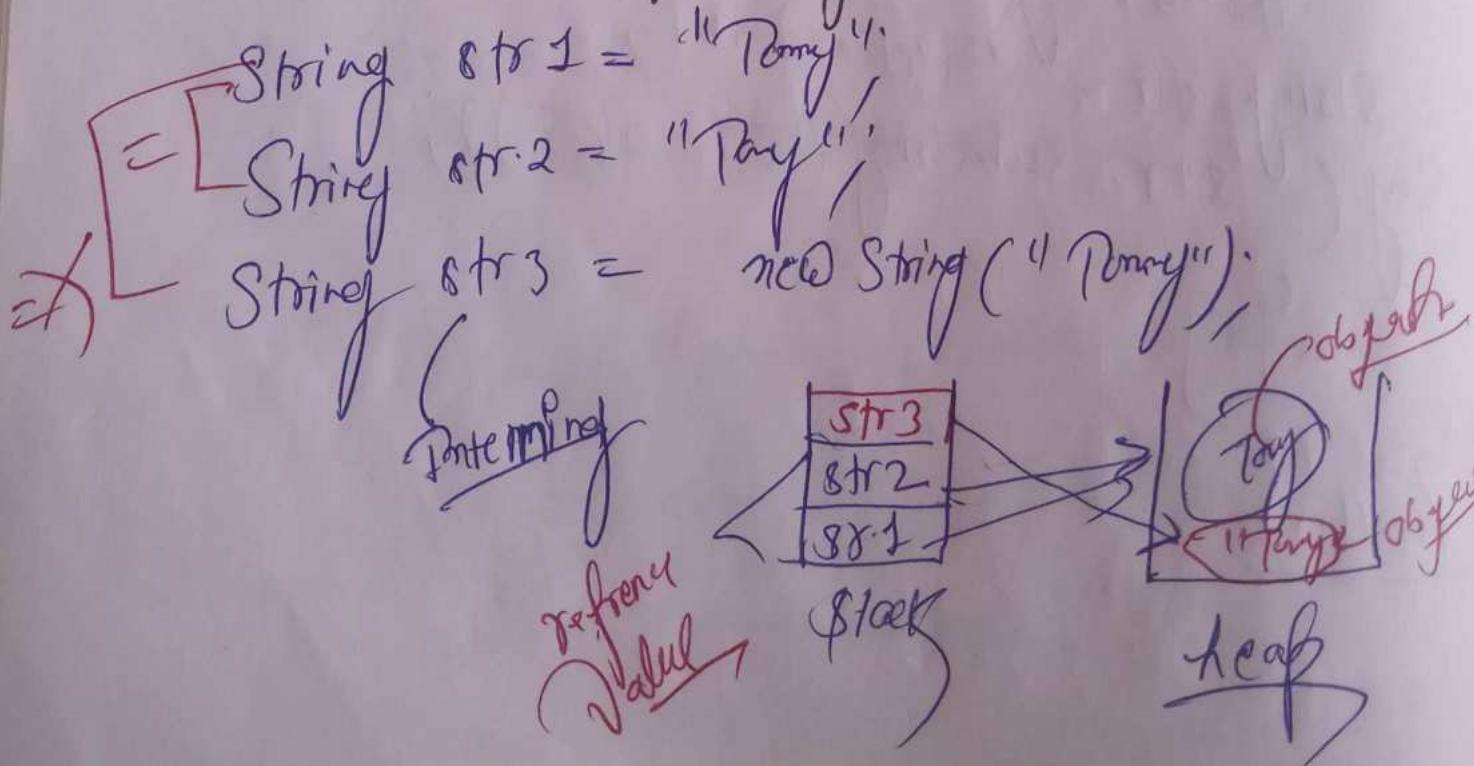
y y

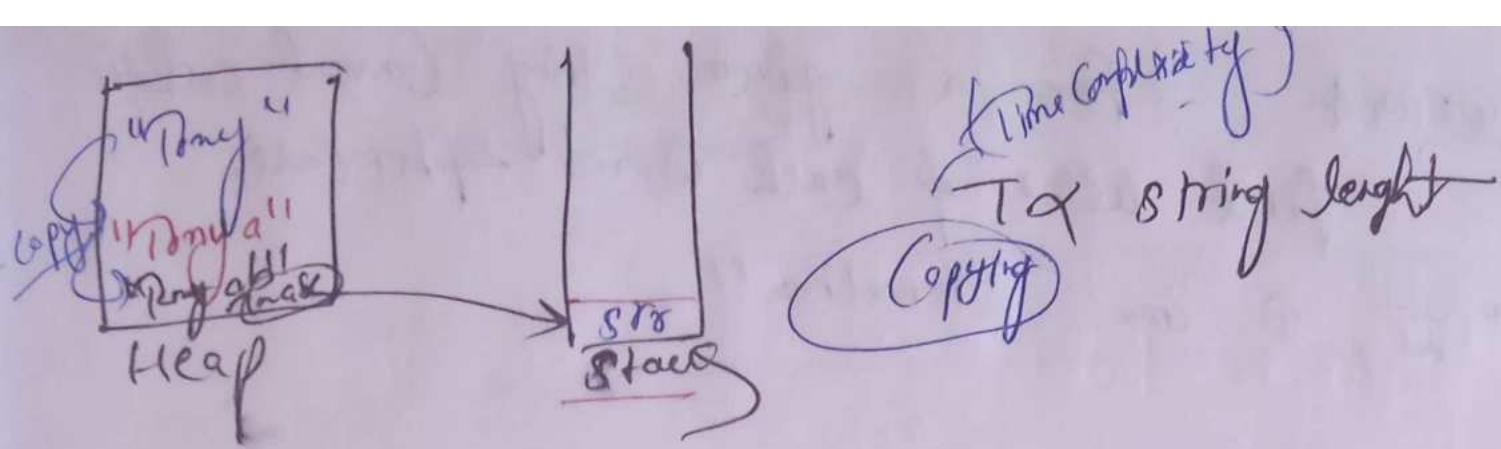
Output
Hello

Q For a given set of strings, print the longest string.

"Apple", "mango", "banana".

II. Why String are Immutable





String str = "Pony"

for (char ch = 'a' to 'z') {
 str += ch
 }
 (Time Complexity)

Pony a

Pony ab

Pony abc

man

dog

(Time Complexity)

StringBuilder

StringBuilder sb = new StringBuilder("Hello");
 sb.toString()

Char ch = 'g'
 ch.toString() X

X int a = 10;
 a.toString()()
 only object change

Code: public static void main(String args[]){
 String build sb = new StringBuilder("");
 for (char ch = 'a'; ch <= 'z'; ch++) {
 sb.append(ch);
 }
 System.out.println(sb.length());
 99

Question 4 for a given String Convert each first letter of each word upper case.

"Hi, I am Shradha"

Imp

- ① say(str.length());
- ② say(str.charAt(0));
- ③ say(str.toUpperCase());
- ④ say(str.toLowerCase());
- ⑤ say(str.substring(0, 0));

String Compression

"aaabbcccd" → "a3b2c3d2"

"aaabbbdd" → "a3b2d2"

"abc" → "abc"

'a'

0

long

(+)

• Create

• Append

• Delete

• Update

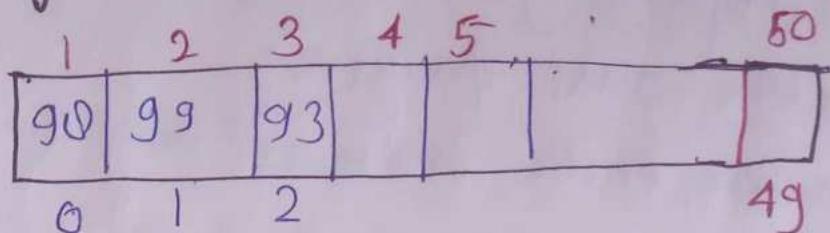
③

Arrays (DATA Structure)

int Phy = 90

int Chem = 99

int math = 93



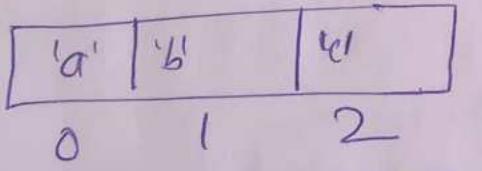
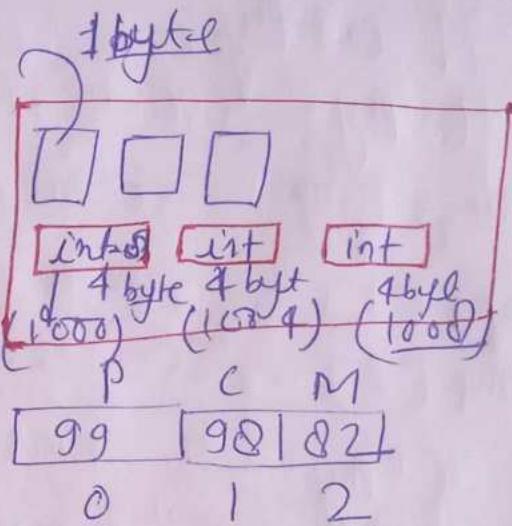
* List of elements of the same type placed in a Contiguous memory location :-

1, 2, 3, 4 → Int

a, b, c, d → Char

1.2, 3.4, 4.0 → float

"Apple" "Banana" → String



1000 1001 1002

(f1)

Operations On Arrays

- Create
- Input
- Output
- updation

① Creating An Array:-

datatype arrayName[] = new datatype [size];

Ex int marks[] = new int[50];

int number[] = { 1, 2, 3 } ; (3)

int morenumber[] = { 4, 5, 6 } ; (3)

String fruits[] = { "Apple", "Mango", "Orange" };

3

3. Input, Output - Update

```

import java.util.*;
public class Arraysc {
    public static void main(String args[]) {
        int marks[] = new int [100];
        Scanner sc = new Scanner (System.in);
        // int phy;
        phy = sc.nextInt();
        marks[0] = sc.nextInt(); // phy
        marks[1] = sc.nextInt(); // chem
        marks[2] = sc.nextInt(); // math
        System.out.println("phy : " + marks[0]);
        System.out.println("chem : " + marks[1]);
        System.out.println("math : " + marks[2]);
        // update
        marks[2] = 100;
        System.out.println("math : " + marks[2]);
    }
}

```

Ex

```

import java.util.Arrays; * Accessing Array
int arr = {1, 3, 4, 5, 6};
System.out.println(Arrays.toString(arr));

```

int [] arr = new int[4]; array length = 4
arr [0] = '1';
arr [1] = '2';
arr [2] = '3';
arr [3] = '4';
say (Arrays. toString (arr));
y y

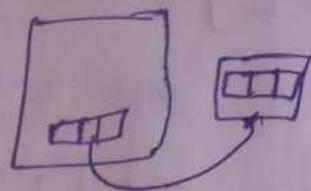
String str = "Hello world";
for (int i=0; i < str.length(); i++) {
if (str.charAt(i) == 'o') {
S.out (i);

Output: (5, 7)

import.util.Array;
int [] arr = new int[10];
for (int i=0; i < arr.length; i++) {
arr[i] = obj.nextInt();
S.out (Arrays. toString (arr));

4 Passing arrays as Argument

Pass by value
Pass by reference



```
import java.util.*;
```

```
public class Array {
```

```
    public static void update(int marks[]){}
```

```
        for (int i=0; i<marks.length; i++)
```

```
            marks[i] = marks[i]+1;
```

```
        }
```

```
    public static void main (String args[]){}
```

```
        int marks[] = {97, 10, 99};
```

```
        update(marks);
```

```
        // print our marks:
```

```
        for (int i=0; i<marks.length; i++)
```

```
            System.out.println(marks[i] + " ")
```

```
        }
```

```
    }
```

```
    }
```

5. Space And Time Complexity

Scenario:- Imagine you give 100 Rupees to one of your friend. Having them all together, you would like your pen back.

Space Complexity: Space Complexity is represented as a function portrays the amount of space necessary for an algorithm to run until complete.

⇒ In our scenario we are looking at you are thinking of space complexity as the number of room you need to find out who has pen. In Computer means how much memory does the process and data structure in our code base / function take up to achieve their goal.

Time Complexity

Time Complexity is represented as a function that portrays the amount of time necessary for an algorithm to run until complete.

Linear Search

- find the index of element in a given array..

| | | | | | |
|-------|---|---|---|----|---|
| 2 | 4 | 8 | 8 | 10 | 0 |
| index | 0 | 1 | 2 | 3 | 4 |

key = 10 return 4

int number [];

import java.util.*;

Code:- public class ArraySearch { int numbers[], int key;

public static int linearSearch (int numbers[], int key) {
for (int i = 0; i < numbers.length; i++) {
if (numbers[i] == key)
return i;
}
return -1;

public static void main (String args[]) {

int numbers [] = { 2, 4, 8, 10, 12, 14, 16 };

int key = 10;

int index = linearSearch (numbers, key);

if (index == -1) {

System.out.println ("Not found");
else {

System.out.println ("Key is at index : " + index);

Time Complexity → loop & constant time.

for ($i = 0$ to n)
 \curvearrowleft length of Array
 \curvearrowleft $O(n)$ m(operation).
 \curvearrowleft (biggin) \curvearrowleft $T C \times \text{loop}(n)$

Largest Number

Find the largest number in given array:-

| | | | | |
|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 |
| 0 | 1 | 2 | 3 | 4 |

$$\text{largest} = -\infty, +\infty$$

$-\infty = \text{integer. MIN_VALUE}$

$+\infty = \text{integer. MAX_VALUE}$

Code: import java.util.*;

```
public class Arrays {  
    public static int getLargest(int[] numbers) {  
        int largest = Integer.MIN_VALUE; // initially  
        for (int i=0; i < numbers.length; i++) {  
            if (largest < numbers[i]) {  
                largest = numbers[i];  
            }  
        }  
        return largest;  
    }
```

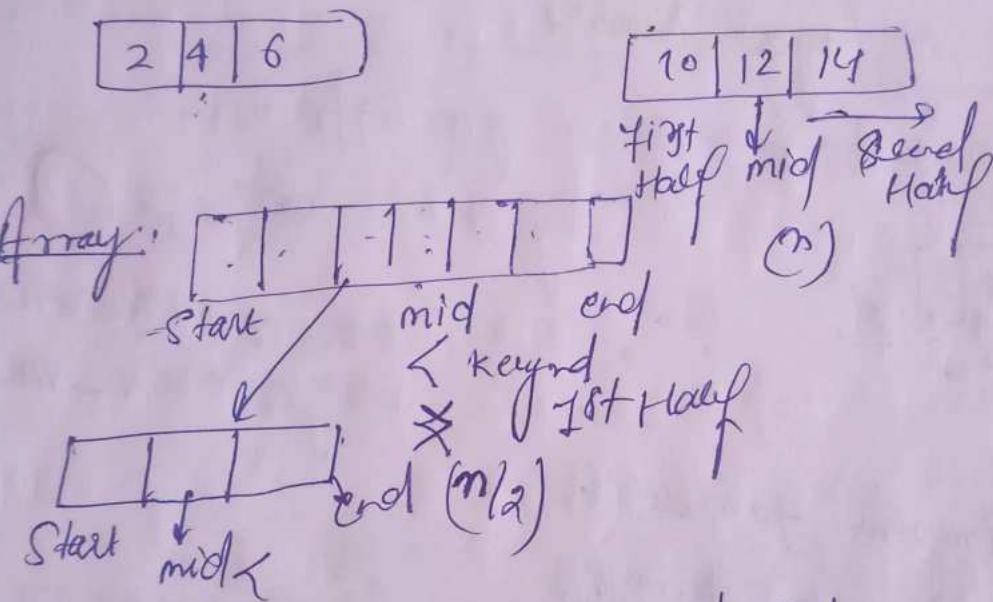
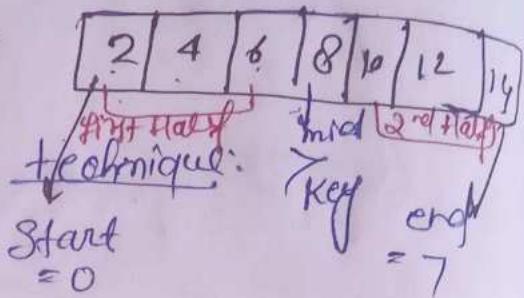
```
    public static void main(String args[]) {  
        int[] numbers = {1, 2, 6, 3, 5};  
        System.out.println("Largest value is: " + getLargest(numbers));  
    }  
}
```

Binary Search

Key = 10

Prerequisite - Sorted arrays

Dictionary \rightarrow Sorted



Pseudo Gde:-

```

start = 0 , end = n-1
while (start <= end)
    find mid
  
```

Compare mid & key

mid == key Found

mid > key Left

mid < key Right

Binary Search Code.

```
Code: Import java.util.*;  
public class Array {  
    public static int binarySearch (int numbers[], int key){  
        int start = 0, end = numbers.length - 1;  
  
        while (start <= end) {  
            int mid = (start + end) / 2;  
            // Comparison;  
            if (numbers[mid] == key) {  
                return mid;  
            } else if (numbers[mid] < key) {  
                start = mid + 1;  
            } else {  
                end = mid - 1;  
            }  
        }  
        return -1;  
    }  
}  
public static void main (String args[]) {  
    int numbers[] = {2, 4, 6, 8, 10, 12, 14};  
    int key = 10;  
    System.out.println ("index for key is : " + binarySearch (numbers));  
}
```

Time Complexity:

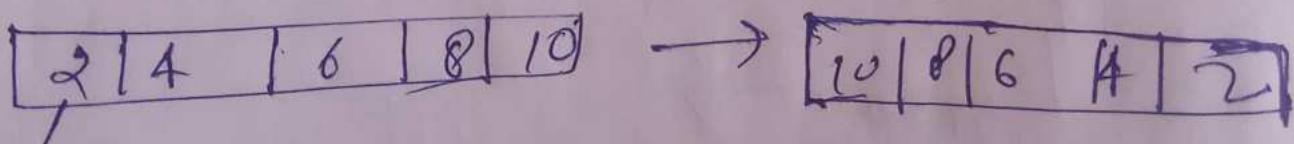
$$\begin{aligned}
 \text{Iterations} &\rightarrow n \quad \left(\frac{n}{2}^0 \right) \\
 \text{Iteration 2} &\rightarrow \frac{n}{2} \quad \left(\frac{n}{2}^1 \right) \text{ formula: } \\
 \text{Iterations} &\rightarrow \frac{n}{4} \quad \left(\frac{n}{2}^2 \right) \\
 \text{Iteration 4} &\rightarrow \frac{n}{8} \quad \left(\frac{n}{2}^3 \right) \quad (5+1)^{\text{th}} \\
 &\vdots \quad \left(\frac{n}{2}^k \right) \quad \text{Iteration} \\
 &\vdots \quad \left(\frac{n}{2}^k \right) \\
 T_C &\propto \log_2 n \quad \left(\frac{n}{2}^k \right) \quad n = 2^k \\
 &\quad \quad \quad \boxed{k = \log_2 n}
 \end{aligned}$$

$\mathcal{O}(\log n)$
 $n > \log_2 n$
 Linear search
 Binary search

Linear search
 Size = $n = 8$
 $\mathcal{O}(n)$

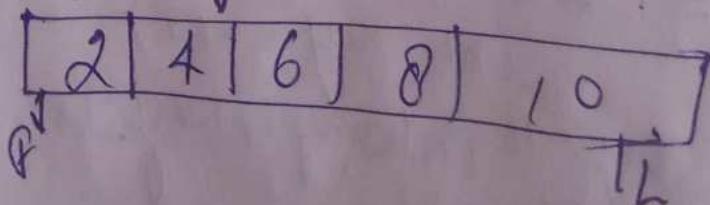
Binary Search
 $\mathcal{O}(1)$
 8 → 4 → 2 → 1 →

Reverse in Array



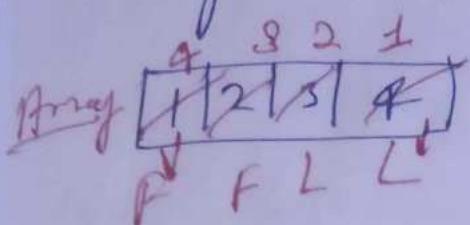
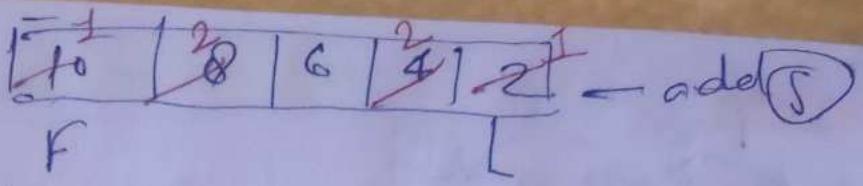
Space $\mathcal{O}(n)$
 Time Complexity $\mathcal{O}(n)$

Space Complexity $\mathcal{O}(3)$



Swap

reversed
Array



4 3 2 1 ← Reversed Array

$$\boxed{O(2) = O(1)}$$

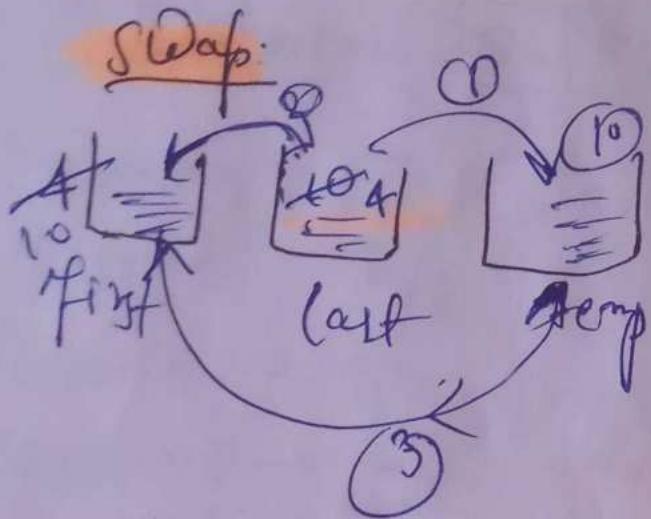
SC \rightarrow $O(1)$
 $O(n/2)$
 $O(n)$

Code: import java.util.*;

```
public class Arrays {  
    public static void reverse(int numbers[]){  
        int first=0; last=numbers.length-1;  
        while (first < last){
```

II Way

```
        int temp= numbers[last];  
        numbers[last]= numbers[first];  
        numbers[first]= temp;  
        first++;  
        last--;
```



4 10

10 4

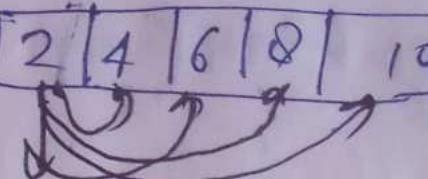
```

public static void main (String Arg[])
{
    int numbers[] = {2, 4, 6, 0, 10};
    reverse (numbers);
    for (int i=0; i<numbers.length; i++)
    {
        System.out.print (numbers[i] + " ");
    }
}

```

Output: 10 0 6 2

Pairs in An Array

(2,4) (2,6) (2,8) (2,10) \rightarrow 4 [2 | 4 | 6 | 8 | 10]


(4,6) (4,8) (4,10) \rightarrow ?

(6,8) (6,10) \rightarrow 2

(8,10) \rightarrow 1

Nested loop

"2" \rightarrow (2,4) (2,6) (2,8); (2,10)

"4" \rightarrow (4,6), (4,8), (4,10)

for (int $i=0$ to n) 2, 4, 6, 10

current

for (int $j=i+1$ to n) [2, 6, 8, 10]

\Rightarrow pairs

import. java.util.*; [4, 8, 10]

public class Arrayf {

public static void printpairs(int numbers[]){

for (int $i=0$; $i < \text{numbers.length}$; $i++$) {

int curr = numbers[i];

for (int $j=i+1$; $j < \text{numbers.length}$; $j++$) {

say("(" + curr + ", " + numbers[j] + ")");

}

say();

public static void main(String args[]){}

$i=n-1$

int numbers[] = {2, 4, 6, 8, 10};
 printPairs(numbers);
 ↴
 ↴

Sub =
 Array
 ↴
 ↴

n element

$$\boxed{Tp = \frac{n(n-1)}{2}} \rightarrow \text{formula}$$

Total pair

Time Complexity =

$O(n^2)$

$\boxed{n + (n-1) + (n-2) + (n-3) \dots O(n^2)}$

12. Print Sub Array

A Continuous part of Array :-

$\boxed{2 \boxed{4} \boxed{6} \boxed{8} \boxed{10}}$

$\boxed{\boxed{2} \boxed{4} \boxed{6}}$

Sub Array

①

2, 4, 6, 8, 10

2, 4, 6, 8, 10

$\boxed{2}$ $\boxed{2 \boxed{4}}$ $\boxed{2 \boxed{4} \boxed{6}}$

4 $\boxed{4 \boxed{6}}$ $\boxed{4 \boxed{6} \boxed{8}}$

6 $\boxed{6 \boxed{8}}$ $\boxed{6 \boxed{8} \boxed{10}}$

8 $\boxed{8 \boxed{10}}$

4, 6, 8, 10 - ④

③

②

①

$$\text{Sub} = \frac{n(n+1)}{2} = \text{formula}$$

array
Logic

start for (int i=0 to n) → L1
 for (int j=i+1 to n) → L2
 for (start to end) → L3
 } y sub Array

| | | | | |
|---|---|---|---|----|
| 2 | 4 | 6 | 8 | 10 |
|---|---|---|---|----|

start = 2

end = 4, 6, 8, 10 }

| | | | |
|-------|---------|-----------|--------------|
| [2 4] | [2 4,6] | [2,4,6 8] | [2,4,6,8 10] |
|-------|---------|-----------|--------------|

Code:

```

import java.util.*;
public class Array {
    public static void printSubarray(int[] numbers) {
        for (int i = 0; i < numbers.length; i++) {
            int start = i;
            for (int j = i; j < numbers.length; j++) {
                int end = j;
                for (int k = start; k = end; k++) {
                    System.out.print(numbers[k] + " ");
                }
                System.out.println();
            }
        }
    }
}
  
```

```

for (int k = start; k = end; k++) {
    System.out.print(numbers[k] + " ");
}
System.out.println();
for (int k = start; k = end; k++) {
    System.out.print(numbers[k] + " ");
}
System.out.println();
  
```

```

    Y      test;
    Y      soy(' ');
    Y      soy("totalSubarray = " + t);
    Y      public static void main (String args) {
        int numbers [] = {2, 4, 6, 8, 10};
        printSubarray (numbers);
    }
}

```

$$\boxed{\begin{array}{l} \text{Total} \\ \text{SubArray} \end{array} \quad \frac{n(n+1)}{2}}$$

R. Max SubArray Sum

1 1 -2 6 -1 3

(1) (1, -2) (1, -2, 6) (-1, -2, 6, -1) (1, -2, 6, -1, 3)

1 -1 5 4 7

-2
0
-1
3

1 1 -3 1 2

Maximum sum = ~~∞~~

Current sum

CS = 1

→ -1

CS = 2

```
import java.util.*;  
public static void printSumSubArry(int arr[]){  
    int currSum=0;  
    int maxSum=Integer.MIN_VALUE;  
    for (int i=0; i<arr.length; i++){  
        int start=i;  
        for (int j=i; j<arr.length; j++){  
            int end=j;  
            currSum=0;  
            for (int k=start; k<=end; k++){  
                currSum+=arr[k];  
            }  
            if (maxSum < currSum){  
                maxSum=currSum;  
            }  
        }  
    }  
    System.out.println("max sum = "+maxSum);  
}  
public class Main{  
    public static void main(String args){  
        int numbers[]={9, 4, 6, 8, 10};  
        maxSubarraySum(numbers);  
    }  
}
```

Output:- max sum = 30

II. Max SubArray Sum

Brute Force Array:

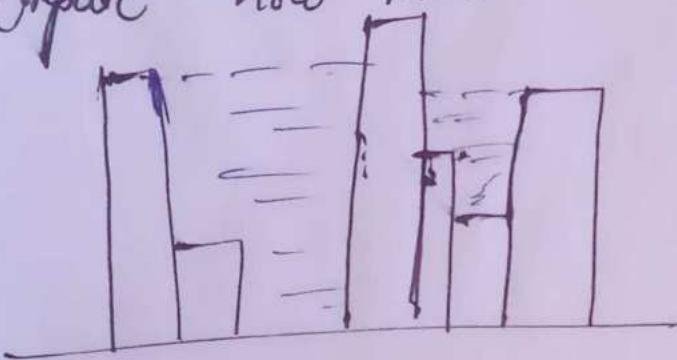
| | | | | |
|---|----|---|---|---|
| 1 | -1 | 5 | 4 | 7 |
| 0 | 1 | 2 | 3 | 4 |

III. Max SubArray Sum

Trapping Rain Water

Given a non-negative integer representing an elevation map where the width of each bar is 1. Compute how much water it can trap after raining.

$$\text{height} = [4, 2, 0, 6, 3, 2]$$



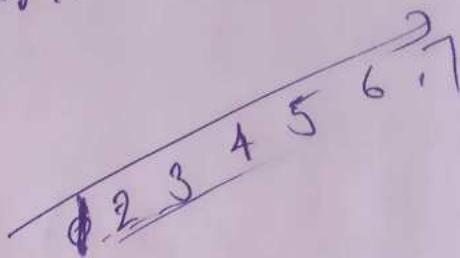
13.1Q Best time to buy stocks

You are given an array prices where prices[i] is the price of a given stock on the ith day. You want to maximize your profit by choosing a single day to buy one stock and choosing a different day in the future to sell that stock. Return the maximum profit you can achieve from this transaction. If you cannot achieve any profit, return 0;

Basic of Sorting

Arrange in an order:

- Bubble Sort
- Selection Sort
- Insertion Sort
- Counting Sort (advance)



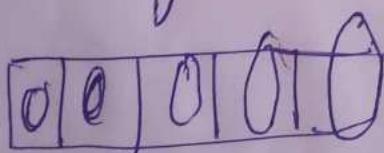
Bubble Sort

{ 5, 4, 1, 3, 2 } unsorted Array

{ 1, 2, 3, 4, 5 } increasing order

{ 5, 4, 3, 2, 1 } decreasing order.

Idea: large element come to the end of array
by swapping with adjacent element.



→ increasing
(0 to n-2)

Bubble sort n=5

5, 4, 1, 3, 2

4, 5, 1, 3, 2

4, 1, 5, 3, 2

4, 1, 3, 5, 2

4, 1, 3, 2, 5

4, 1, 3, 2, 5 → 2

bubble
sort

~~1 4 1 3 2 5~~
 1 4 3 2 5
 1 3 4 2 5
~~1 3 2 4 5~~
 2nd 1 2 3 4 5

3rd 1 2, 3, 4, 5
 1 2 3 4 5

$$\boxed{\begin{aligned} \text{sum} &= n-1 \\ j &= 1 \quad \underline{j+1} \end{aligned}}$$

for (sum = 0 to n-2)

for (int j = 0 to n-2 - sum)

sum 0
 $j = 0 \text{ to } (5-2-0) \Rightarrow 3$

Code: import java.util.*;

public class BasicSorting {

 public static void bubble(int arr[]){}

 for (int sum = 0; sum < arr.length - 1; sum++)

 for (int j = 0; j < arr.length - 1 - sum; j++)

 if (arr[j] > arr[j + 1]) {

 // swap

 int temp = arr[j + 1];

 arr[j + 1] = ~~arr~~ temp;

 y y y public static void printArr(ArrayList)

bubble sort

```

for (int i=0; i<arr.length; i++) {
    System.out.print(" " );
}
System.out();
public static void main(String args[]) {
    int arr[] = {5, 4, 1, 3, 2};
    bubbleSort(arr);
    printArr(arr);
}

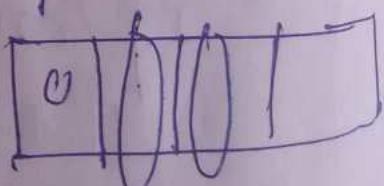
```

$O/P \quad 1, 2, 3, 4, 5$

Time Complexity $\Theta(n^2)$ Best

Selection Sort

Idea: picks the smallest (from unsorted)
put it at the begining.



5, 4, 1, 3, 2

1 S 4 3 ②

1 2 5 4 ③

1 2 3 5 ④

for (int i = 0 to m-2) → Smallest = Max
 for (j = i+1 to n-1)
 unsorted arr → start

Code: public static void selectionSort(int arr[])

for (int i = 0; i < arr.length - 1; i++)

 int minPos = i;

 for (int j = i+1; j < arr.length; j++) {

 if (arr[minPos] > arr[j]) {

 minPos = j;

(सेट की Change हो जाएगी)

y_y

||| swap

 int temp = arr[minPos];

 arr[minPos] = arr[i];

 arr[i] = temp;

y_y

public static void main(String args[]) {

 int arr[] = {8, 4, 3, 2, 1};

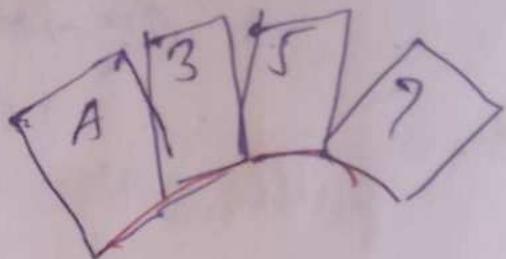
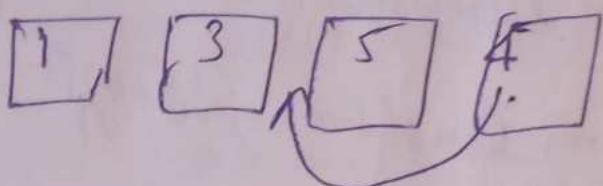
~~solution~~ bubbleSort(arr);

y_y print(arr);

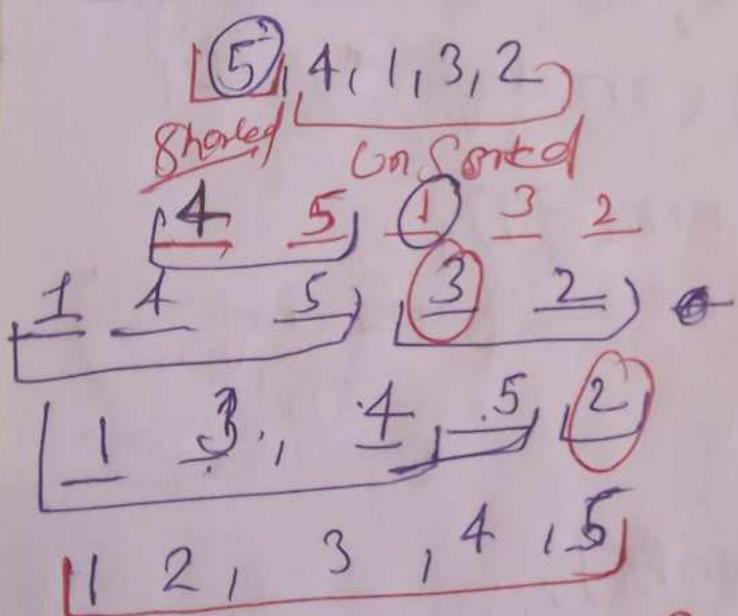
O(p > 1, 2, 3, 4, 5)

Insertion Sort

Polea: Pick an element (from unsorted part) & place in the right pos in sorted part



Insertion Sort. n=5



Code

```
import java.util.*;
public static void insertionSort(int arr[]){
    for (int i = 1; i < arr.length; i++) {
        int curr = arr[i];
        int prev = i - 1;
        while (prev >= 0 && arr[prev] > arr[curr]) {
            arr[prev + 1] = arr[prev];
            prev--;
        }
        arr[prev + 1] = curr;
    }
}
```

// insertion

```
arr[prev+1] = arr[curof];
```

```
gg public static void main(String args[]) {  
    int arr[] = {5, 4, 1, 3, 2};  
    insertionSort(arr);  
    printArr(arr);
```

Prebuilt Sort

```
import java.util.Arrays;
```

```
Arrays.sort(arr)
```

```
O(n log n)
```

```
Arrays.sort(arr, s, e)
```

```
import java.util.*;
```

```
public static void main(String args[]) {
```

```
int arr[] = {5, 4, 1, 3, 2};
```

```
// insertion sort only
```

```
Arrays.sort(arr);
```

```
printArr(arr);
```

gg

B

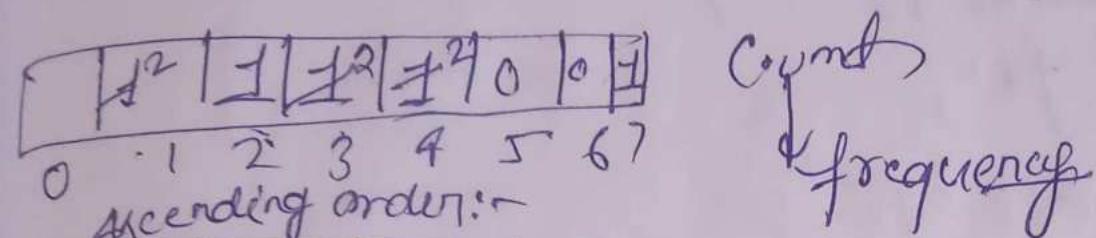
```
import java.util.*;  
public static void main(String args[]){  
    int arr[] = {5, 4, 1, 3, 2};  
    // insertion sort;  
    Arrays.sort(arr, 0, 3);  
    printArr(arr);  
}
```

O/P : {3 4, 5, 2}

Counting Sort → (1, 4, 1, 3, 2, 4, 3, 7)

Marked Min → max fve no.
 $\frac{n \log n}{\approx n}$

min → 1 range → 7
 max → 7



① for (int i=0 to n)
 freq.
 ② for (int i=0 to max. (range))

$$[T \propto O(n + \text{range})]$$

Code: public static CountingSort (int arr[]){}

```

    int minLargest = Integer. MIN_VALUE;
    for (int i=0; i<arr.length; i++)
        largest = Math.max(largest, arr[i]);
    }

    int count[] = new int [largest+1];
    for (int i=0; i<arr.length; i++)
        count [arr[i]]++;
    }

    for (int i=0; i<count.length; i++)
        arr[i] = count[i];
    }
}

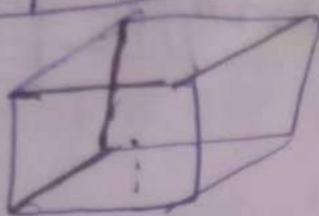
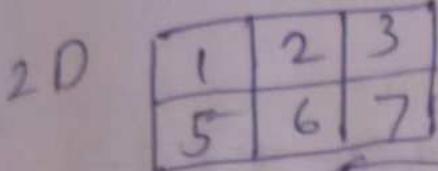
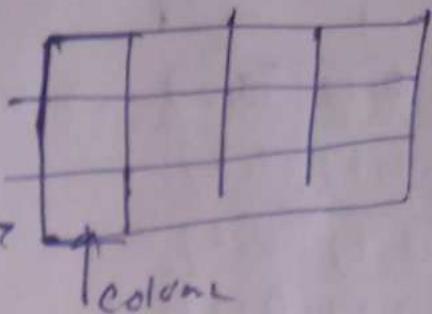
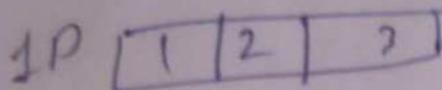
```

II sorting:

```
int j=0;
for (int i=0; i< count.length; i++) {
    while (count[i]>0) {
        arr[j] = i;
        j++;
        count[i]--;
    }
}
public static void main(String args[]) {
    int arr[] = {5, 4, 1, 3, 2};
    CountingSort(arr);
    printArr(arr);
}
```

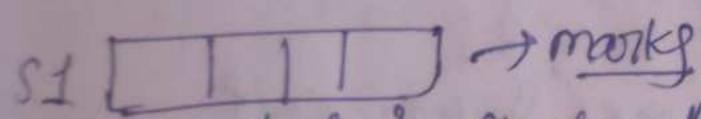
2D Array

Matrix (Rows And Columns)

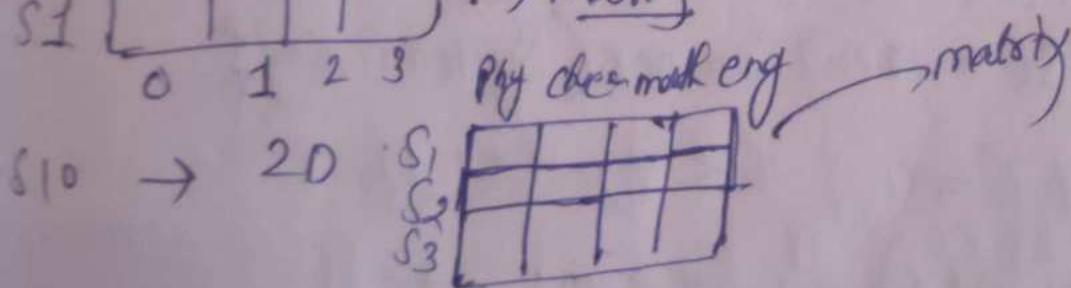


m-D Array

Real life Example



Play chess marking



RGB matrix

| | | | |
|------|-------|------|-------|
| Red | Green | Blue | |
| (255 | 255 | 255) | white |

| | | | |
|---|---|------|-------|
| 0 | 0 | 0 | black |
| 0 | 0 | 225) | blue |



pixel

Representation of 2D Array

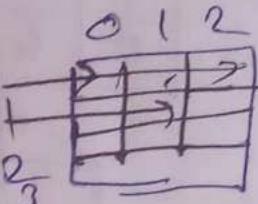
| | 0 | 1 | 2 |
|---|-------|-------|-------|
| 0 | (0,0) | (0,1) | (0,2) |
| 1 | (1,0) | (1,1) | (1,2) |
| 2 | (2,0) | (2,1) | (2,2) |
| 3 | (3,0) | (3,1) | (3,2) |

(n x m)

Rows = 4

Column = 3

Create 2D Array



Code: import java.util.*;

public class Matrix {

public static void main(String[] args) {

int matrix[][] = new int[3][3];
int n=3, m=3;

Scanner sc = new Scanner(System.in);

for (int i=0; i<m; i++) {

for (int j=0; j<m; j++) {

matrix[i][j] = sc.nextInt();

} }

// output

for (int i=0; i<m; i++) {

for (int j=0; j<m; j++) {

System.out.print(matrix[i][j] + " ")

say();

yy

output

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

you can also search in Matrix.

public class matrices {

public static boolean search (int matrix[3][3], int key){
for (int i=0; i<matrix.length; i++) {
for (int j=0; j<matrix[i].length; j++) {

if (matrix [i][j] == key) {

say ("found at cell("+i+", "+j+");
return true;

yy

yy

say ("key not found");

return false;

public static void main (String args[]){
int matrix [3][3]= new int [3][3];

```
int n = matrix.length, m = matrix[0].length;
```

```
Scanner sc = new Scanner(System.in);
```

```
for (int i=0; i<n; i++) {
```

```
    for (int j=0; j<m; j++) {
```

```
        matrix[i][j] = sc.next();
```

```
}
```

Output

```
for (int i=0; i<n; i++) {
```

```
    for (int j=0; j<m; j++) {
```

```
        System.out.print(matrix[i][j] + " ");
```

```
    System.out.println();
```

```
key
```

```
search(matrix, 5);
```

```
Y
```

Output

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

found at cell (1,1)

20 Array in Memory

→ Row major

| | | |
|---|---|---|
| 0 | 1 | 2 |
| 3 | 4 | 5 |
| 6 | 7 | 8 |

| | | |
|---|---|---|
| 0 | 1 | 2 |
| 3 | 4 | 5 |

R_1 R_2

| | | |
|---|---|---|
| 0 | 1 | 2 |
| 3 | 4 | 5 |

| | | |
|---|---|---|
| 6 | 7 | 8 |
|---|---|---|

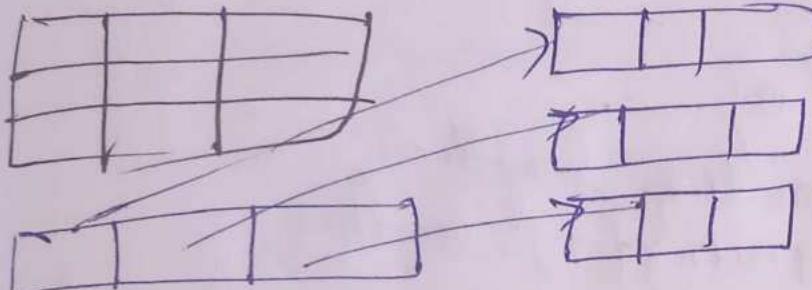
R_3

→ Column Major

| | | |
|---|---|---|
| 0 | 3 | 6 |
| 1 | 4 | 7 |

| | | |
|---|---|---|
| 1 | 4 | 7 |
| 2 | 5 | 8 |

| | | |
|---|---|---|
| 2 | 5 | 8 |
| 3 | 6 | 9 |



Spiral Matrix

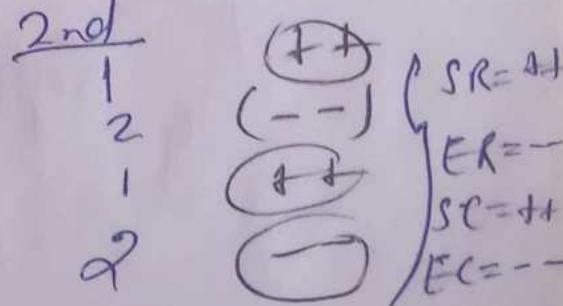
(Google, Oracle, Amazon)

| | | | |
|----|----|----|----|
| 1 | 2 | 3 | 4 |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |

Output: 1, 2, 3, 4, 8, 12, 16, 15, 14, 13, 9, 5, 6, 7, 11, 10

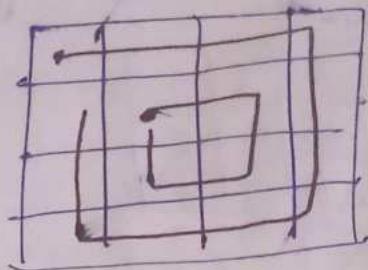
Approach: Border \rightarrow 2 calc
 2 rows
(loop)

- Starting row = 0
- ending row = $n-1$
- start Col. = 0
- Challenging Col. = $n-1$



while(=)

- { ① top
- ② right
- ③ bottom
- ④ left.



Spiral matrix Code

```
public static void printSpiral(int matrix[][])
```

```
int startRow = 0;
```

```
int startCol = 0;
```

```
int endRow = matrix.length - 1;
```

```
int endCol = matrix[0].length - 1;
```

```
while( startRow <= endRow && startCol <= endCol)
```

```
// top  
for( int j = startCol; j <= endCol; j++)
```

```
System.out.println(matrix[startRow][j] + " ");
```

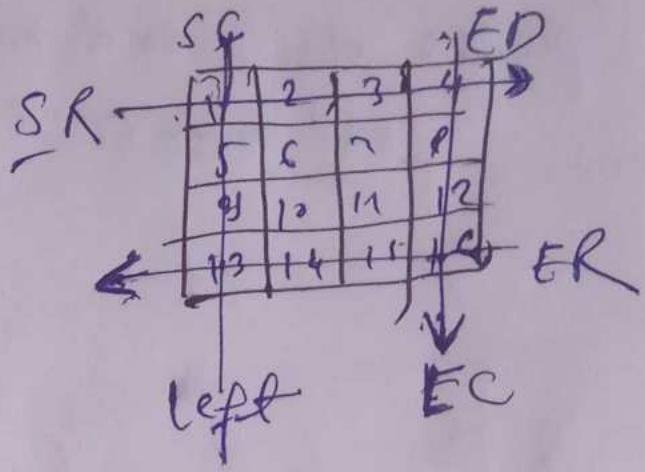
// right

```
for( int i = startRow + 1; i <= endRow; i++)
```

```
System.out.println(matrix[i][endCol] + " ");
```

// bottom

SR } Top
 $SC \rightarrow EC$
 $SR+1 \rightarrow ER$ } Right
 $EC-1 \rightarrow SC$ } Bottom
~~ER fixed~~



Left } SC
 || bottom } (ER-1 → SR+1)

```

for (int j = endCol - 1; j >= startCol; j--) {
  soy(matrix[endRow][j] + " ");
}
  
```

|| left }
 for (int i = endRow - 1; i >= startRow + 1; i--) {
 soy(matrix[i][startCol] + " ");
 }

startCol++;
 StartRow++;
 endRow--;
 startRow++;

soy();

public static void main (String args []) {

int matrix [] [] = { { 1, 2, 3, 4, 9 },

{ 5, 6, 7, 8, 9 },

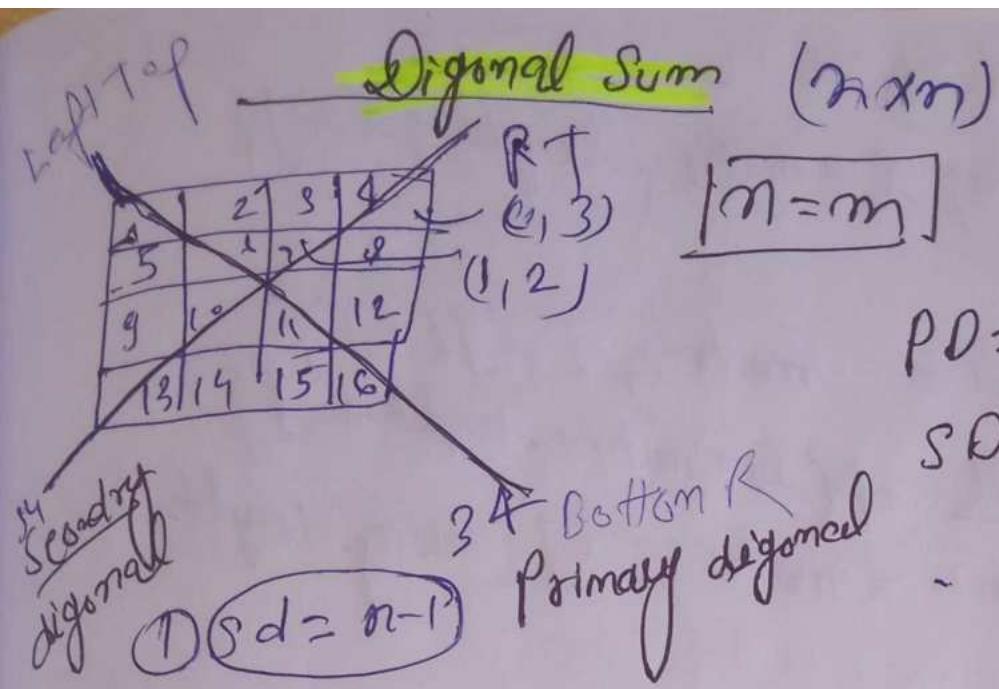
{ 9, 10, 11, 12, 9 },

{ 13, 14, 15, 16, 9 } },

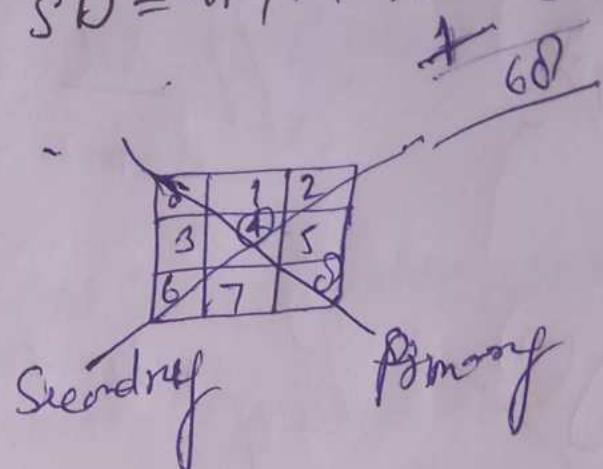
printspiral (matrix);

output: 12 34 8 12 16 15 14 13 9 5 6 7 11 10

Di



P.D = $1+6+11+16 = 34$
 S.D = $4+7+10+13 = 34$
~~68~~



Code:

```

public static digital sum {
    int matrix[ ][ ];
    int sum = 0;
    for (int i = 0; i < matrix[0].length; i++) {
        for (int j = 0; j < matrix[0].length; j++) {
            if (i == j) {
                sum = matrix[i][j];
            } else if (i + j == matrix.length - 1) {
                sum = matrix[i][j];
            }
        }
    }
    return sum;
}
    
```

$O(n^2)$

for (int i=0; i < matrix.length; i++) {
 // pd
 sum = matrix[i][i];
 // sd if (i == matrix.length - 1) {
 sum = matrix[i][matrix.length - 1];
 }
 return sum;
}

$\mathcal{O}(n)$

Search in Sorted Matrix

Search for a key in row wise & col. wise sorted matrix.

| | | | | |
|----|----|----|----|-----------------------------|
| 10 | 20 | 30 | 40 | Key = 33 |
| 15 | 25 | 35 | 45 | Approach |
| 21 | 29 | 37 | 48 | $n^2 = 16$ elements |
| 27 | 33 | 39 | 50 | ① Brut force. Row wise |
| 32 | | | | ② Row wise Col wise |

Staircase Search

$(0, m-1)$

• key < cell value
LEFT

key = 33

$O(n \log n)$

key > cell value

RIGHT

$(n \log n)$

(Binary Search)

④ Cell → {
 key < cell value
 Left
 key ≥ cell value
 Bottom

③ (n-1; 0) → {
 key < cell value
 Top
 key ≥ cell value
 Right

③ Staircase Search

Code: public static boolean staircaseSearch(int matrix[][], int key){
 int row = 0; col = matrix[0].length - 1;
 while (row < matrix.length && col >= 0) {
 if (matrix[row][col] == key) {
 System.out.println("found key at (" + row + ", " + col + ")");
 return true;
 } else if (key < matrix[row][col]) {
 col--;
 } else {
 row++;
 }
 }
 System.out.println("key not found!");
 return false;

```

public static void main(String arg[])
{
    int matrix[][]
        = { { 10, 20, 30, 40 },
            { 11, 21, 31, 41 },
            { 27, 29, 37, 48 },
            { 32, 33, 39, 50 } };
    int key = 33;
}

```

```

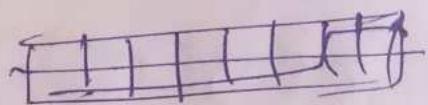
static void Search (matrix, key);
}

```

Time Complexity :-

$O(n+m)$

$O(n) \quad n > m$



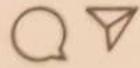
$O(m)$

Complexity done



N. Nature™
YOUR CHILD IS OUR PRIORITY

BIG BEN L O N D O N



#NOTEBOOKS



A4

student exercise
Notebook



INDEX

Name: Rohit Kumar Yadav

Class:

Subject: D

Roll No.:

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| | | Divide and Conqueror | | |
| | | Back tracking | | |
| | | Array list | | |
| | | Unit 2 * Linked list | | |
| Unit 3 | | * Stack * Queue | | |
| | | Greedy | | |
| Unit 4 | | * Binary Tree Binary Search tree (BST) Heap Hash Priority Queue Graph | | |
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| | | <u>Rule:</u> | | |

Total day = 100 day = 3 month 10 day.

Chapter = 50

Day 1 = Lecture

Day 2 = Practice Break.

Sep 3 25

Oct 3 30

Nov. 3 15

70

Sep

- 6 → Recursion lecture []
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- 26 → Binary tree 1 []
- 27 → Practice []
- 28 → Binary tree 2 []
- 29 → Practice []
- 30 → K th level []

Oct

- 1 → BST []
- 2 → Practice []
- 3 → BST - 2 []
- 4 → Practice []
- 5 → Heap []
- 6 → Practice []
- 7 → Hashing []
- 8 → Priority []
- 9 → Tree []
- 10 → Practice []
- 11 → Graph []
- 12 → Practice []
- 13 → DFS graph - 2 []
- 14 → Practice []
- 15 → BFS []
- 16 → Practice []
- 17 → Dictionaries []
- 18 → Practice []
- 19 → Good find algorithm []
- 20 → Graph []
- 21 → Practice []
- 22 → DP Part 1 []
- 23 → Practice []
- 24 → DP 2 []
- 25 → Practice []
- 26 → DP 3 []
- 27 → Practice []
- 28 → DP 4 []
- 29 → Practice []
- 30 → DP 5 []
- 31 → Practice []

Nov.

- 1. DP 6 []
- 2. Practice []
- 3. segment tree []
- 4. Practice []

Complete

Lect Cal

9 AM

HackerRank

Recursion

- Iteration
- function

→ what is recursion:-

using Math: $f(0) = x^2$

$$f(f(x)) = (x^2)^2$$

$$x = 2$$

$$f(x) = 4 = 2 \underset{2}{\cancel{)} \underset{16}{\cancel{)}}$$

$$f(5) = 5 \times f(4) = 6 \leftarrow 6$$

\downarrow

$$= 5 \times 4 \times f(3) = 6 \leftarrow 2$$

\downarrow

$$= 5 \times 4 \times 3 \times f(2) = 6 \leftarrow 2$$

\downarrow

$$= 5 \times 4 \times 3 \times 2 \times f(1) = 6 \leftarrow 2$$

\downarrow

$$= 5 \times 4 \times 3 \times 2 \times 1 \times f(0) = 6 \leftarrow 1$$

factorial =

$$n = n \times (n-1) \times (n-2) \dots$$

$$5! = 5 \times 4 \times 3 \times 2 \times 1$$

$$4! = 4 \times 3 \times 2 \times 1$$

$$0! = 1$$

$$f(n) = n \times f^{(n-1)}$$

\downarrow

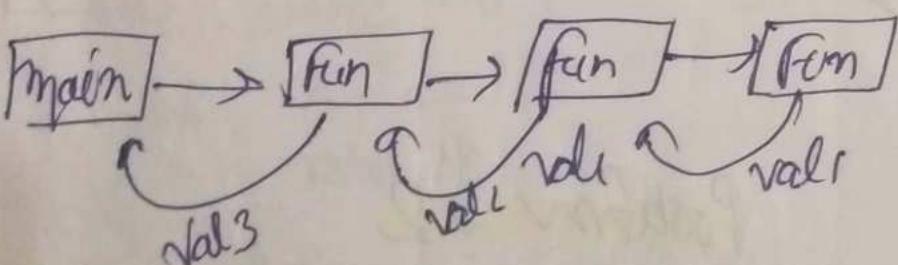
$$(n-1) \times f^{(n-2)}$$

\downarrow

Base Case: $\begin{cases} 1 \times f(0) \\ \dots \end{cases}$

Recursion: Recursion is a method of solving a computational problem where the solution depend on solution to smaller instance of the same problem.

Base Case: where recursion stop (end).



① Base Case

② Recursion ($f(n) \rightarrow n \times f(n-1)$)

③ Call inner function

Tree graph } Mainly used.
DP

PMI

Principal of mathematical induction

Problem 1

Print number from n to 1 (Decreasing order)

$$n=10$$

10 9 8 7 6 5 4 3 2 1

```
for( int i=10; i>=1; i-- )  
    print(i);
```

$$f(n) = n + f(n-1)$$

$$9 + f(8)$$

$$8 + f(7)$$

$$7 + f(6)$$

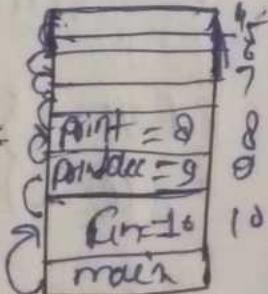
```
funct(int n)  
print(n);  
fun(n-1);
```

Codes:

```
public static void printDec(  
    if (n==1){  
        say(n)  
        return;  
    } say(n);  
    printDec(n-1);  
}
```

Call stack

Decreasing order-



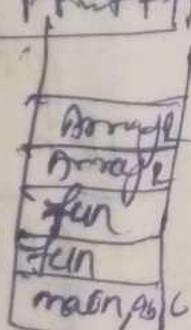
>

① Parameter :

② too many call → **Stack overflow**.

Base Case X

Stack overflow Front = front + 1



Problem 2

Print number from n to 1. (Increasing order)

$n=5$

1 2 3 4 5

$$f(0) = f(\boxed{n-1}) + n$$

$f(n-1)$
 $f(n-2) + (n-1)$
 $m = -1$
print return
 $fun(\text{int } n)$
 $fun(n-1)$
 $print(n).$

$$\boxed{f(32)} \quad 3^y \quad 5$$

public static void print(
 \times int n)
 if ($n == -1$) {
 say(\pm);
 return;
 }
 g printLine($n-1$);
 say(n);
}

0! = 1

Problem 3

Print factorial of a number n :

$$n! = n \times (n-1)! \rightarrow f(n) = n \times f(n-1)$$

$$f_{n-1} = fact(n-1);$$

$$f_n = n \times f_{n-1};$$

if ($n == 0$)

 return ± 1 ;

else: public static int fact($\text{int } n$) {

 if ($n == 0$) {

 return \pm ;

 int $f_{n-1} = fact(n-1)$;

 int $f_n = n \times fact(n-1)$;

 return f_n ;

 }

 p.s.r.m (.)
 int $n = 5$; say(fact(0));

Stack Analysis

```

    f(m=2)
    f(m=3)
    f(n=4)
    f(n=5)
    main()
  
```

$n = -0 \rightarrow$ return 1
 $f_{n-1} \rightarrow 1$
 $f(n) = n \times f_{n-1}$
return f_n .

Problem 4

Print sum of N natural nos. $m = 5$

$$f(n) = n + f(n-1)$$

$$f(5) = 5 + f(4)$$

15
if $f(3) = 6$

$$\text{sum}(\text{int } n) \rightarrow \text{if } (n=1) \text{ return 1;}$$

$$S_N = n + S_{N-1}$$

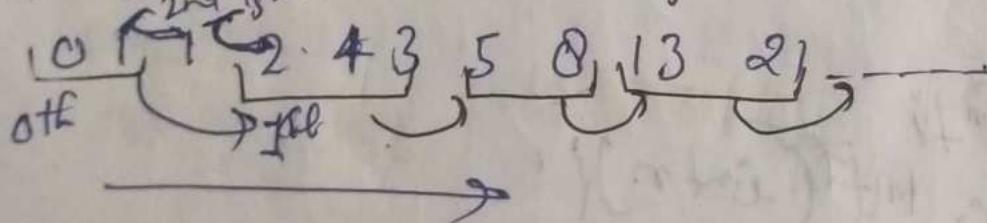
return S_N

$$3 + f(2) = 3$$

2 + f(1) = 1

Problem

Print N th Fibonacci Series:-



$$fib_n + fib_{n+1} = fib_{n+2}$$

$$fib_n = fib_{n-1} + fib_{n-2}$$

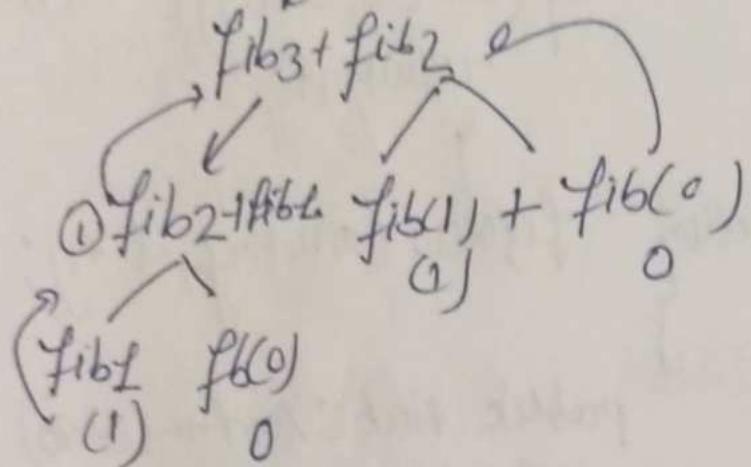
$$fib_5 = fib_4 + fib_3$$

Base case:

$$fib_3 + fib_2 \rightarrow$$

$$fib_2 + fib_1$$

$$\text{fib}_5 = \text{fib}_4 + \text{fib}_3$$



$\text{fib}(\text{int } n)$

if ($n = 0 \rightarrow 0$)
 $n = 1 \rightarrow 1$)
 else

$$\text{fib}_{n-1} = \text{fib}(n-1)$$

$$\text{fib}_{n-2} = \text{fib}(n-2)$$

$$\text{fib}_n = \text{fib}_{n-1} + \text{fib}_{n-2}$$

return fib_n ;

Problem 6 Check array are sorted or not

[1 2] [3 4] 5

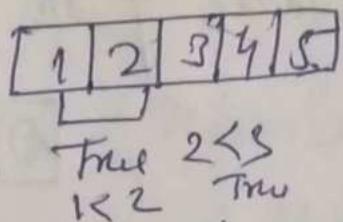
Loop $i=0$ to $n-1$

$$arr[i] \leq arr[i+1]$$

$$\{ \text{sorted}[n] = [0] \leq [1] \leq \dots \leq [n-1]$$

+ 8 sorted[n-1]

0, l+1



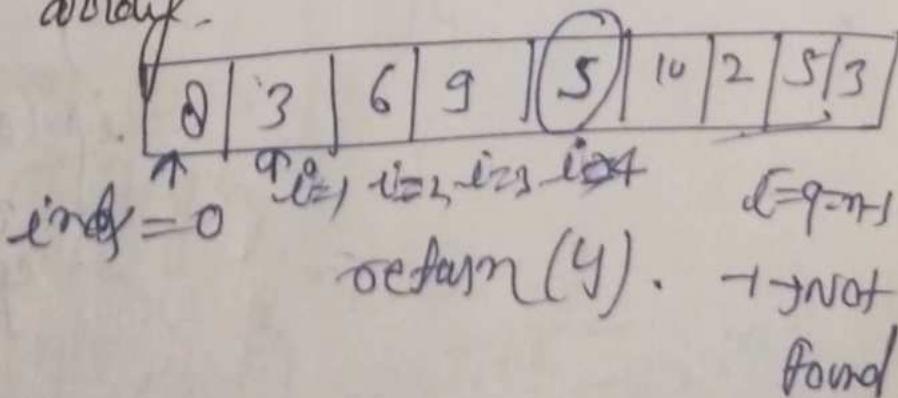
if sorted(arr[0], int l)
 $arr[i] \leq arr[i+1] \rightarrow$ Base case $l = \text{arr.length}$
 if sorted(arr, l+1);

Problem 7 WAF to find occurrence of an element
 in an array.

key = 5

ordkey = 4 ✓

ordarr = 7



indx = 0

return (4). → not found

first occur(arr, key)

$a[i] == \text{key}$

return i;

return follow(arr, key+1);

Code public static int firstOcc(int arr[],
key)
 if (arr[i] == key) {
 return i;
}
 return follow(arr, key+1);

public static void main(String args[]){
 int arr[] = {1, 2, 3, 4, 5};
 System.out.println(firstOcc(arr, 5));
}

last occurrence

WAP to find last occurrence of an element in an array

key=5

Compare with self.

Look forward

↓
Look forward

Compare with self

| | | | | | | | | |
|---|---|---|---|---|----|---|---|---|
| 8 | 3 | 6 | 9 | 5 | 10 | 2 | 1 | 3 |
|---|---|---|---|---|----|---|---|---|

i=4 l=7

int l=found = lastOcc(arr, key, l+1);
 if (l=found == -1) {
}

return l; }
}

if (arr[i] == key) {
 return i;
}

Problem

Print x^n . $x=2$ $x^n = x \times x^{n-1}$

$2^P \rightarrow 1024$ $n=10$

$$\begin{matrix} & n \\ n & \times x^{n-2} \\ & \downarrow \\ x & \times x^{n-3} \end{matrix}$$

$$\text{pow}(x, n) = x \times \text{pow}(x, n-1)$$

$n=1$

$$x^1 = x$$

$$\text{pow}(x, N)$$

$$\text{return } \text{pow}(x, n-1)$$

Code:
public static int power(int x, int n){

if (n == 1){

return 1;

y

int $x^{n-1} = \text{power}(x, n-1);$

int $x^n = x * x^{n-1};$

return $x^n;$

y return $x * \text{power}(x, n-1);$

g public static void main(String[] args){

int x = 5, y = 5, z = 5;

say(digitSum(5, 0));

say(power(2, 10));

y y

Problem 10

Print x^n in $O(\log n)$

$$x^n (2^{10}) = x^{n/2} \times x^{n/2}$$

$$\eta = \text{even} \quad (2^5) \times (2^5) = 2^{5+5} = 2^{10}$$

$$2^{10} \rightarrow 2^8 \times 2^5$$

$$2 \times 2 \times 2 \times 2$$

$$2 \times 2 \quad 2 \times 2$$

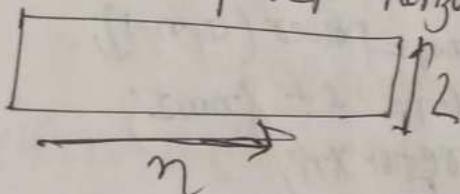
$O(\log n)$

$$\frac{n}{2^l} \Rightarrow l \Rightarrow n=2^l$$

$$\boxed{\log_2 n = l}$$

Problem 11

Tiling problem: given a ' $2 \times n$ ' board and tiles of size (2×1)
 count the number of ways to tile the given
 board using the 2×1 tiles. A tile can either
 be placed horizontally or vertically



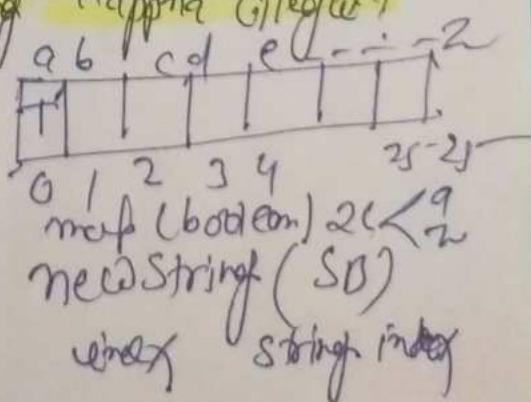
Code:

```
public static int fillingBottom(int n) is 112xm (floors)
    if (n == 0 || n == 1)
        return 1
    int verticalFile = fillingProblem(n-1);
    // horizontal choice
    int fm1 = fillingProblem(n-2);
    int toways = fm1 + fm2;
    return toways;
```

Problem No. 12

remove Duplicate in a string "apple Gilege"

pppxx
apple Gilege
"apnle Gileg"
"unique"



① bye $\text{idx} = \text{ato}$

② from $\text{char} \rightarrow \text{present in map} \rightarrow \text{new str} \times$

③ $\text{idx} = \text{idx} + 1 \rightarrow \text{new str}$

friend

or given

up

com

n =

n =

n

④

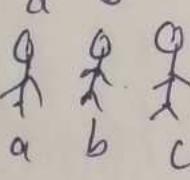
Problem 13

Friend pairing problem

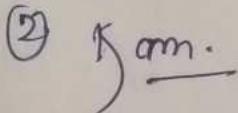
- Given n friend, each one can remain single or can paired up with some other friend. Each friend can be paired only once. Find out total ways in which friend can remain single or can paired up.

$n=1$  (single) (a)

$n=2$  (a,b)

$n=3$ 
 a b c a,b,c way = 4
 (a,b,c)
 $(a,b).c, (b,c).a, (a,c)b,$

(1) Berge Case $n=1$ way = 1 $n=1 \parallel n=2$
 $n=2$ way = 2 $n=1 \parallel n=2$ way = n

(2) 

Binary String Problem

Print all binary strings of size n without consecutive ones.

010101 ✓ $n=6$ Base Case:

01101001 X

n -size

Binary string (0,1)

0 0
0 1
1 0

$n=0$ " "

$n=1$ " 1 ", " 0 "

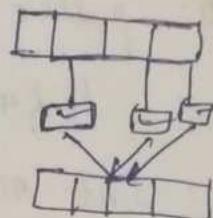
$n=2$ 0 0
 0 1
 1 0

① Base: $n=0$ 1 X
empty

② From

Divide And Conqueror

Convert into small problem



Merge Sort

Unsorted Array: [6 | 3 | 9 | 5 | 2 | 8]

Sorted Array: [2 | 3 | 5 | 6 | 8 | 9]

Approach:

(1) To Divide
6 mid

s_i = starting index
 e_i = ending index.

$$mid = \frac{(s_i + e_i)}{2}$$

$$\boxed{s_i + (e_i - s_i)/2}$$

Step 1 mergeSort(left)
mergeSort(right)

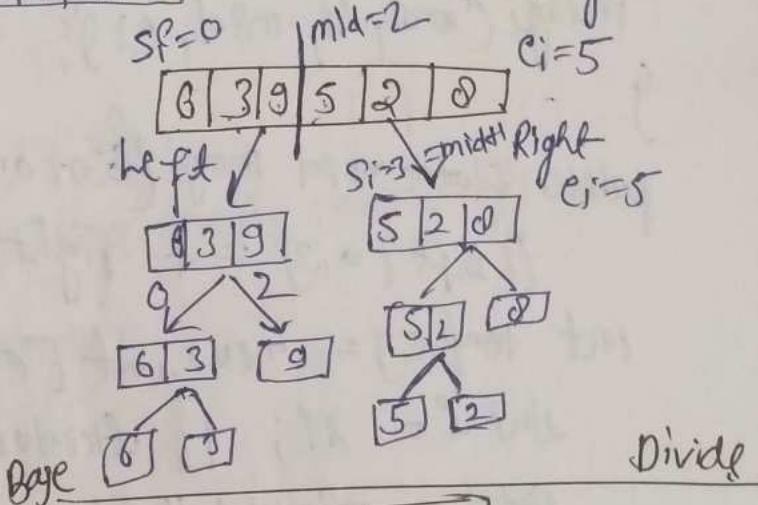
Steps merge

① Base $\rightarrow s_i > e_i$

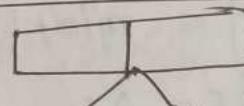
② $s_i = e_i$

13 am divide

mergeSort(left)
right
merge



Divide



left Right

[6 | 3 | 9 | 5 | 2 | 8] m.

[6 | 3 | 9]

[5 | 2 | 8]

m.

mergeSort

3 6 9 2 5 8

temp: [2 | 3 | 5 | 6 | 8 | 9 |]
0 1 2 3 4 5 6
Left Right
de.

mergeSort(left)
right
merge

Code: public static void mergesort(int arr[], int si, int ei){
 if(si >= ei)
 return;

int mid = (si + ei) / 2;

mergesort(arr, si, mid);

mergesort(arr, mid + 1, ei);

merge(arr, si, mid, ei);

}
public static void merge(int arr[], int si, mid, int ei){

if(left(0, 3) = 4 right(4, 6) = 3 $\rightarrow c - o = 6$

int temp[] = new int [ei - si + 1];

int i = si; // Iterator for left part

int j = mid + 1; // Iterator for right part

int k = 0; // Iterator for temp arr.

while (i <= mid && j <= ei){

if (arr[i] < arr[j]) {

temp[k] = arr[i];

i++;

k++;

} else { temp[k] = arr[j];

j++;

k++;

4 → 5 → 6 → 7 → 8

// left part

while ($i \leq mid$) {

 temp [$k++$] = arr [$e+i$];

}

while ($j \leq e_i$) {

 temp [$k++$] = arr [$j++$];

}

// copy temp to original arr.

for ($k=0$; $k=e_i$; $k < \text{temp.length}$; $k++$, $e++$) {

 arr [e] = temp [k];

}

public static void main(String args) {

 int arr [] = {6, 3, 9, 5, 2, 8, 4};

 mergeSort (arr, 0, arr.length - 1);

}

Quick Sort → average $O(n \log n)$
 worst $O(n^2)$
 space $O(1)$.

Pivot & Partition

① Pivot:
 random
 median
 first
 last

② partition (part)
 left element

③ Quicksort (left)
 (right)

$s_i = 0$ $c_i = 5$

$\frac{3-2}{\text{quicksort}} < 5 < \frac{6-9}{\text{quicksort}}$

base

single sorted

$\boxed{3 \ 6 \ | \ | \ | \ |}$
 0 1 2 3 4 5

~~$\boxed{3 \ 2 \ 5 \ 4 \ 9}$~~ ~~(3) (13) (9) (2) (5)~~

$i++$

loop

$int temp = arr[j];$

$arr[j] = arr[i];$

$arr[i] = temp;$

Code: public static void quickSort(int arr[], int si, int ei)
 || last element if ($s_i >= e_i$)
 return;

int pivot = partition (arr[si], ei);

quicksort (arr, si, pivot - 1)

quicksort (arr, pivot + 1, ei)

public static int partition (int arr[], int si, int ei)

int pivot = arr[ei];

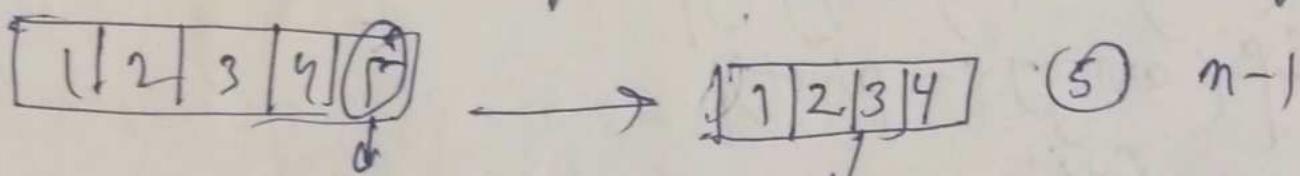
```

int & = arr[i];
for (int j = 0; j < i; j++)
    if (arr[j] <= pivot)
        arr[i] = arr[j];
        swap(i, j);
int temp = arr[i];
arr[i] = arr[x];
arr[x] = temp;
return i;
}

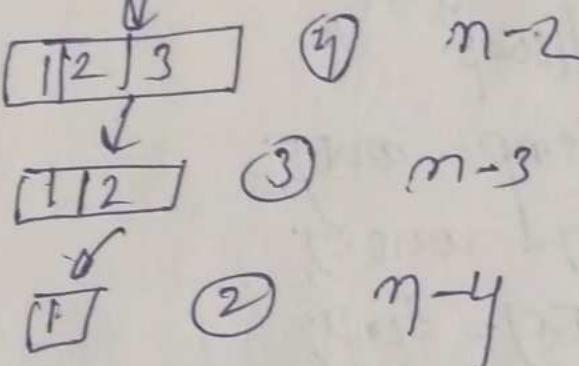
public static void main(String args[])
{
    int arr[] = {6, 3, 9, 8, 2, 5};
    quickSort(arr, 0, arr.length - 1);
    printArr(arr);
}

```

Worst Case: worst case occurs when pivot is always the smallest or the largest element.



last element → largest



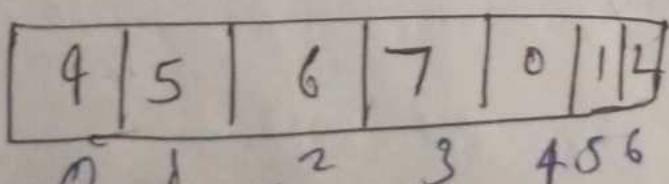
loop → n times.

$$\frac{n(n+1)}{2} \rightarrow \frac{n^2+n}{2}$$

worst case $\Theta(n^2)$

Search in Rotated sorted Array

Input: sorted, rotated array with distinct numbers (in increasing order). It is rotated at pivot point. Find the index of given element.



target = 0

$$0 \xrightarrow{\text{out}} 4$$

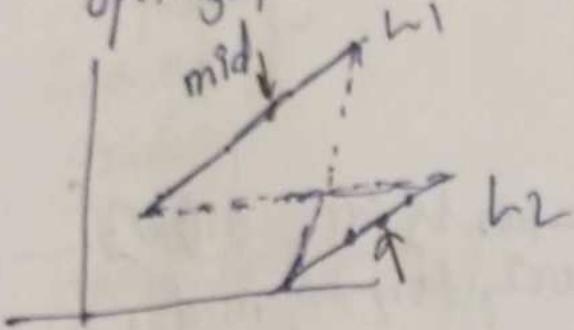
Ex rotate:-
1 2 3 4 5

0 1 2 4 5 6 7

4 5 1 2 3

Linear Search: $T.C \rightarrow O(n)$

optimized: $T.C \rightarrow O(n \log n)$



Modified binary search

$$\text{mid} = (s_i + e_i) / 2$$

$\text{arr}[mid]$

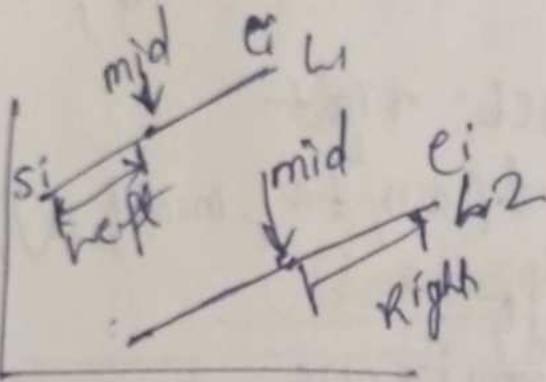
$L_1 \quad L_2 \quad (\text{mid} < \text{tar} \Rightarrow e_i)$

$(s_i \leq \text{tar} \leq \text{mid})$

left

Right
(false)

right left



Case 1 mid on L_1 $\star \text{arr}[mid] \leq \text{mid}$

Case a; $L_1 \text{ left}$ ($s_i \leq \text{tar} \leq \text{mid}$)

Case b; $L_1 \text{ right}$ else

Case 2 mid on L_2 $\text{arr}[mid] \leq \text{arr}[e_i]$

Case c = $L_1 \text{ right}$ ($\text{mid} < \text{tar} \leq e_i$)

case d = mid left else.

Code: public class divider {

public static int search(int arr[], int tar, int s, int e)

// kaam if ($s > e$) { return -1; }

int mid = $s + (e - s) / 2$; // $(s + e) / 2$

// Case found

if (arr[mid] == tar) {

return mid;

} if mid on L1

if (arr[ei] <= arr[mid]) {

 || Case: left if (arr[ei] <= tar & tar <= arr[mid]) {

 return search(arr, tar, si, mid);

 } else {

 || Case: right

 return search(arr, tar, mid+1, ei);

 } if (arr[mid] <= tar & tar <= arr[ei]) {

 return search(arr, tar, mid+1, ei);

 } else {

 || Case: left

 return search(arr, tar, si, mid-1);

public static void main(String args[]) {

 int arr[] = {4, 5, 6, 7, 0, 1, 2};

 int target = 0; // output → 4;

 int tarIdx = search(arr, target, 0, arr.length - 1);

 System.out.println(tarIdx);

(प्रैग प्रैग गेट) Back

n-queen } ,

Sudoku } ,

gridway

Type of Backtracking

Back

| | | | |
|-----|-----|-----|-----|
| 1 | 2 | 3 | 4 |
| i=0 | i=1 | i=2 | i=3 |
| -1 | 0 | 1 | 2 |

Code: public class

public

// base

// recu

arr

change

a

(पीएमर्गेंट) Backtracking

→ Back

→ Divide And Conquer.

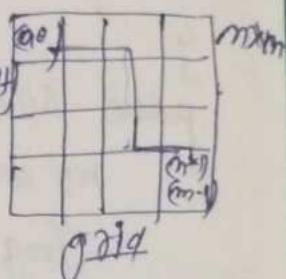
n-queens
Sudoku
gridway

Type of Backtracking:-

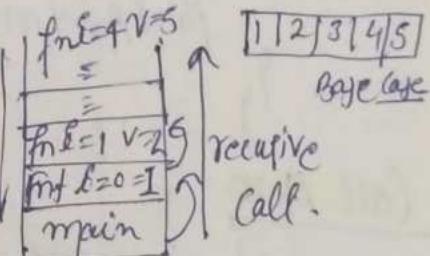
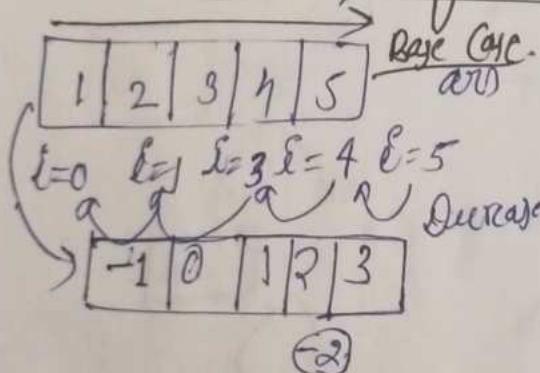
① Decision

② Optimization (shortcut)

③ Enumeration
(region)



Backtracking on Array



Code: public class class name

public static void changeArr(int arr[], int l, int val){

// base case

if ($l == arr.length$) {
printArr(arr);
return;

// recursion

arr[l] = val;

changeArr(arr, l+1, val+1)

arr[l] = arr[l] - 2;

}

```

public static void printArr(int arr[]){
    for(int i=0; i<arr.length; i++){
        System.out.print(arr[i] + " ");
    }
    System.out.println();
}

```

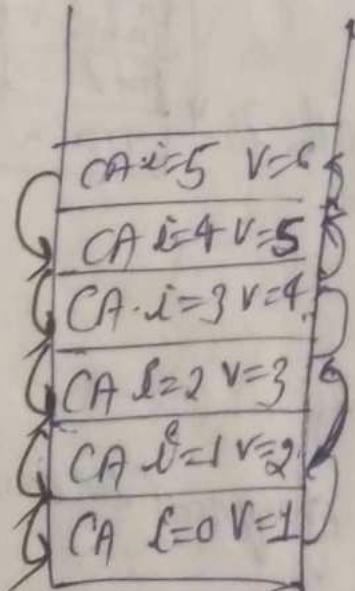
```

public static void main(String args[]){
    int arr[] = new int[5]
    changeArr(arr, 0, 1);
    printArr(arr);
}

```

Call Stack

| | | | |
|---|---|---|---|
| 2 | 3 | 4 | 5 |
| 2 | 2 | 3 | 4 |



Find Subset

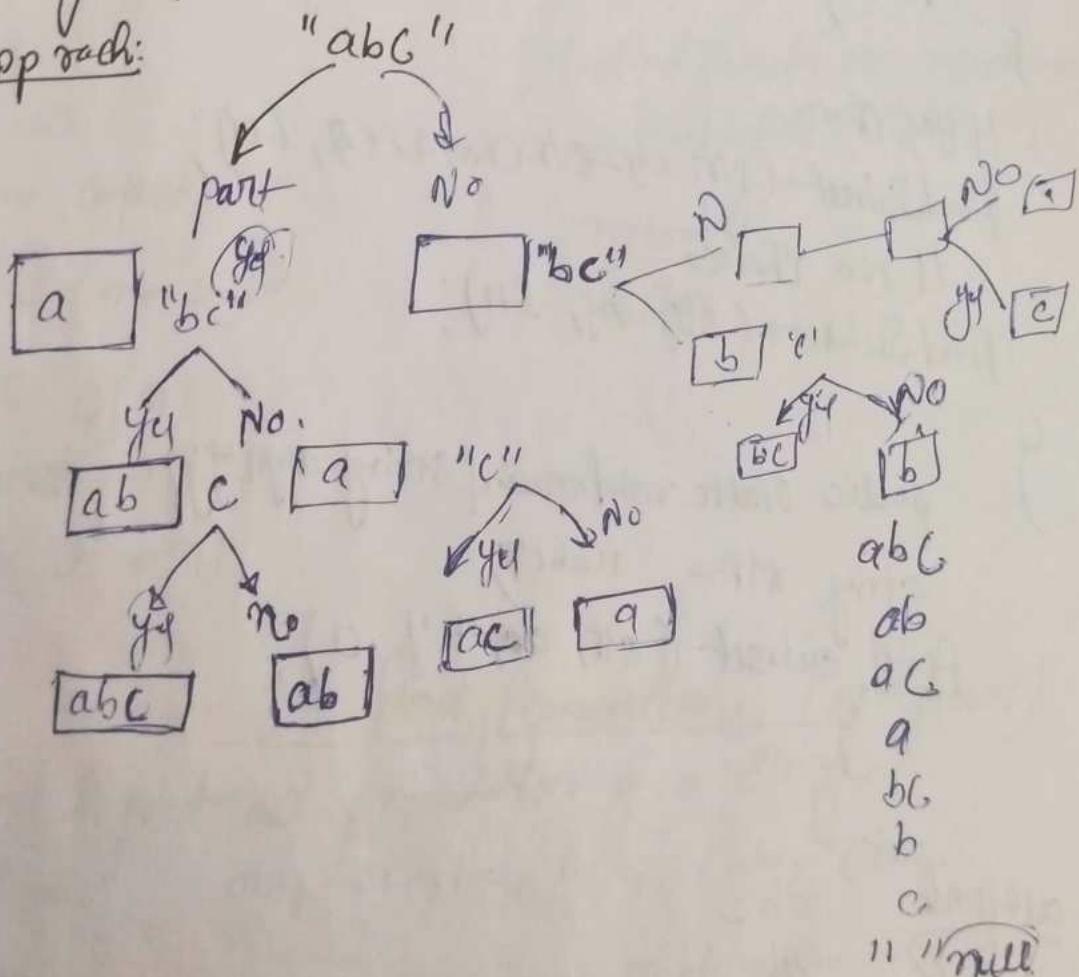
Find & print all subset of a given string

"abc" → a, b, c, ab, bc, ac, abc, " " empty (null) 2^n

Total subset: - 2^n

String length $n \rightarrow 2^n$ subset

Approach:



Coll:- public class classroom
public static void findSubset (String str, String ans, int i) {

 // base case
 if (i == str.length()) {
 System.out.println (ans);
 return;
 }

 // yes choice
 findSubset (str, ans + str.charAt(i), i+1);
 // No choice
 findSubset (str, ans, i+1);

}

public static void main (String args[]) {
 String str = "abc";
 findSubset (str, "", 0);

}
}

output:-

abc

ab

a

bc

b

c

" "

(null)

Call Stack:

| | |
|----------|-------|
| G | "abc" |
| FS · i=3 | "ab" |
| FS · L=L | "a" |
| FS · L=L | " " |
| FS · L=0 | |

```

public static void findSubset(String str, String org)
{
    if (i == str.length())
    {
        if (org.length() == 0)
            System.out.println(org);
        return;
    }
}

```

str = "abc";

org = ""

L = 0

Time Complexity

$\Theta(n \cdot 2^n)$

S.C. $O(n)$

Subset $\rightarrow 2^n$

$O(2^n \cdot n)$

$\frac{n \text{ element}}{\text{char}}$

Find Permutation (Arrangement)

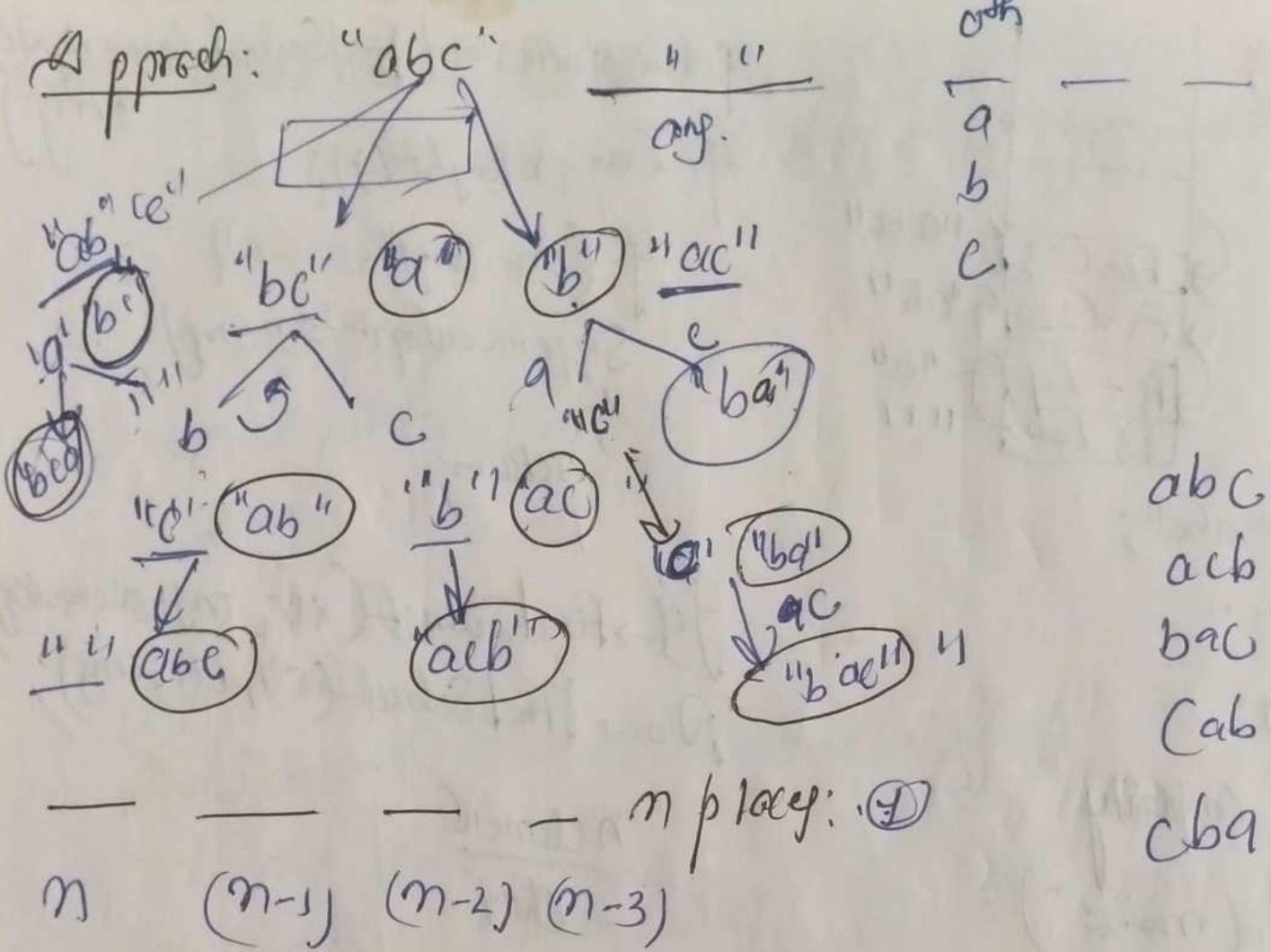
- Find & print all permutation of a string
"abc" abc, acb, bac, bca, cab, cba.

arr

$n \text{ element}$

length n $\frac{n!}{0}$ permutation.

$n!$



Time. ~~$n \times n!$~~

```
for (str str, string ans) {
```

```
    for (i=0 to str.length()) {
```

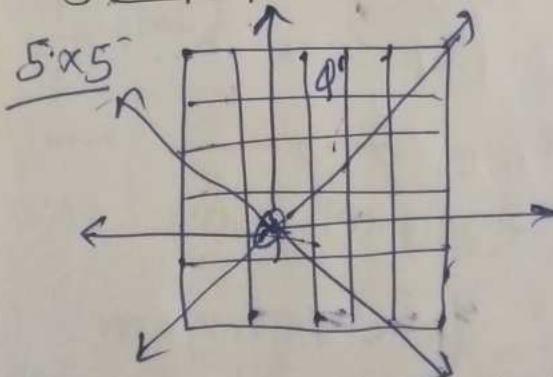
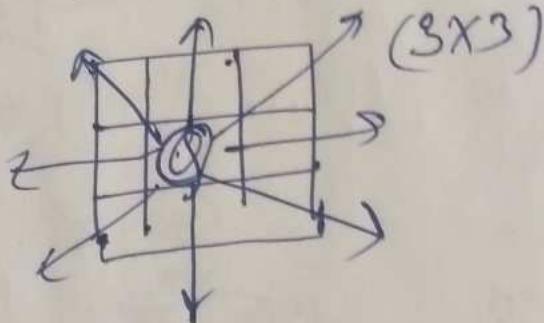
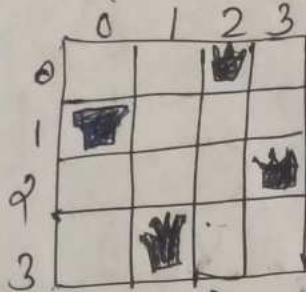
ans + str.charAt(i)

i,

Remove

N-Queens

Place N queen on an $N \times N$ chessboard such that no 2 queen attack each other $N=4$.

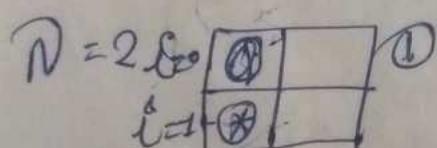
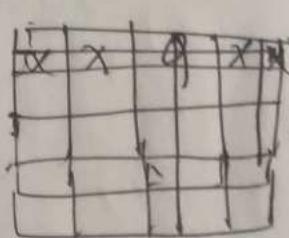


Approach:- Logic

vertical:-

horizontal:-

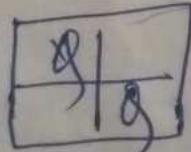
diagonal:-



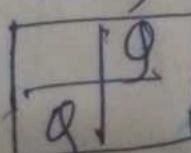
nq

nr

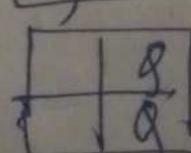
①



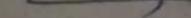
②



③



④



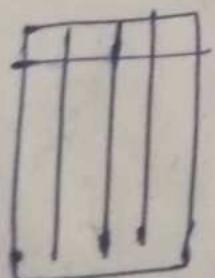
public
public
if (row == last)
printBoard();
return;
y

public class classroom

① public static void nque(char board[][], int row){
 //base case
 for (int j = 0; j < board.length; j++)
 if (row == board.length) {
 board[row][j] = 'Q';
 printBoard(board);
 return;
 }
 nqueens(board, row + 1);
 board[row][j] = '.';
 }
 //backtracking step

public static void main (String args[]){

 int n = 2;
 char board[][] = new char[n][n];
 // initialize
 for (int i = 0; i < n; i++) {
 for (int j = 0; j < n; j++) {
 board[i][j] = '-';
 }
 }
 nqueens(board, 0);
}



N Queen Time Complexity

nquey

1 2 3 ... $\frac{n}{n}$

$n \times (n-1) \times (n-2) \dots$

$\underline{\mathcal{O}(n^n)}$

$$T(n) = 1 \text{ queplace} * \overbrace{T(n-1)}^{\mathcal{O}(n)} + \text{isSafe} \downarrow$$

$\mathcal{O}(n)$.

T.C. $\mathcal{O}(n!)$

$$T(n) = n * T(n-1) + \text{isSafe}().$$

N Queen - Count ways

Count total number of ways in which we can solve N Queen problem.

∴ Base Case

$\text{row} == \text{board.length}$
→ board point
Count++;

N Queen - print ± solution ↗ Yes ↗ No.

Checks if problem can be solved & print only ± solution to N Queen problem.

isSafe(board, row, f) {

place

$f(n-1)$

→ true

→ place

→ $(n-1)q$

→ unplace

Solution Not exist

↳ return

Solution Exist

public static void nQuery (char board[8][int])

// base

if (row == board.length)

// printBoard (board),

Count ++;

return;

// column loop

for (int j=0; j < board.length; j++)

if (isSafe (board, row, j))

board [row][j] = 'Q';

nQuery (board, row+1); // function call

board [row][j] = 'X'; // backtracking step

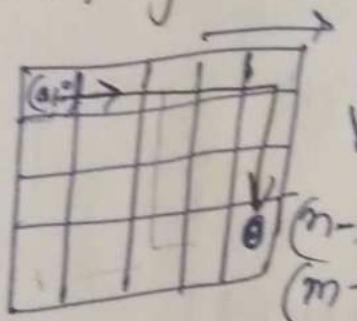
g g

public static void printBoard (char board[8][int])

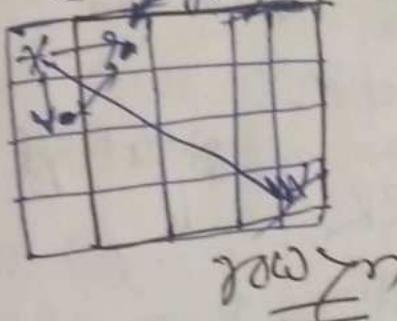
say (" — chek board — ");

Grid ways

Find number of ways to reach from $(0,0)$ to $(n-1, m-1)$ in a $n \times m$ grid. Allowed moves right or down.



w_1 w_2



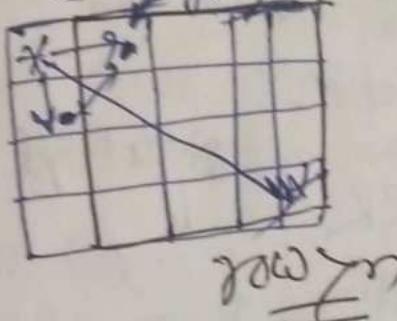
$w_1 + w_2 = \text{total way}$

$$f(x, y) = f(x+1, y) + f(x, y+1)$$

Down Right

Approach:

$(x+1, y)$



Target

source = $(n-1, m-1)$

1 way

Code:

public class classrooms

public static int gridways(int x, int y, int n, int m)

// base case

if ($x == n-1$ & $y == m-1$) { // end for last cell

else if ($x == n$ & $y == m$) return 1;

return 0;

int $w_1 = \text{gridways}(x+1, y, n, m);$

int $w_2 = \text{gridways}(x, y+1, n, m);$

return $w_1 + w_2;$

public static void main(String args[]){}

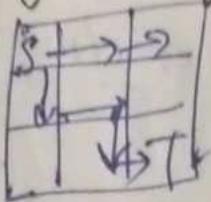
int $n = 3, m = 3;$

System.out.println(gridways(0, 0, n, m));

gridway trick

Mathtrick

Permutation-



RRDD

PRDR

way/path $(n-1)D$

$(m-1)R$ Rightpath

$\{ D D D D \} \rightarrow (n-1)$

$\{ R R R R R \} \rightarrow (m-1)$

Total character = $(n+m-1)$

Permutation

PPRR

DRDR

DRRD

Repeat $\rightarrow (n-1)D$
 $(m-1)R$

$$\frac{(n-1+m-1)!}{(n-1)! (m-1)!}$$

Total way

T.C O(n+m)

Sudoku ($n^2 \times n^2$)

Write a function to complete a Sudoku grid

| | | | | | | | | |
|-------|---|---|---|---|----|---|--|--|
| 3x3 | 2 | 8 | 3 | | 10 | | | |
| row 1 | 4 | 9 | 1 | 5 | 7 | 2 | | |
| row 2 | | 3 | | 4 | 1 | 9 | | |
| row 3 | 1 | 0 | 5 | 6 | | 2 | | |
| row 4 | 9 | 6 | 4 | 5 | 3 | | | |
| row 5 | 3 | | 7 | 2 | | 4 | | |
| row 6 | 4 | 9 | 3 | | 5 | 7 | | |
| row 7 | 8 | 2 | 7 | 9 | 1 | 3 | | |
| row 8 | | | | | | | | |

Some Row
Same Col.
Same Grid

9×9

Approach: for (int i=1; i<9) {
 if (isSafe(i)) {
 place
 cell
 }
}

Code

public class ClassRoom {
 public static boolean SudukoSolver(int Suduko[9][9], int row, int col)
 // base case
 if (row == 9 && col == 9) {
 return true;
 } else if (row == 9) {
 return false;
 }
 // recursion
 int nextRow = row, nextCol = col + 1;
 if (nextCol == 9) {
 nextRow += 1;
 nextCol = 0;
 }
 for (int digit = 1; digit <= 9; digit++) {
 if (isSafe(Suduko, nextRow, nextCol, digit)) {
 Suduko[nextRow][nextCol] = digit;
 if (SudukoSolver(Suduko, nextRow, nextCol)) {
 return true;
 }
 Suduko[nextRow][nextCol] = 0;
 }
 }
}

public static void main (String args) {

int suduko [] = {{ 0, 0, 0, 0, 0, 0, 0, 0, 0 },

{ 1, 9, 0, 1, 5, 7, 0, 9, 2 },

{ 0, 0, 3, 0, 0, 4, 1, 9, 0 },

{ 1, 8, 5, 0, 1, 6, 0, 0, 1, 6 },

{ 0, 0, 0, 0, 2, 0, 0, 6, 0 },

{ 9, 6, 0, 4, 0, 5, 3, 0, 0 },

{ 0, 3, 0, 0, 1, 7, 2, 0, 0, 5, 7 },

{ 0, 4, 9, 0, 3, 0, 0, 1, 5, 7 },

{ 0, 2, 1, 7, 0, 0, 1, 9, 0, 1, 3 }, };

if (sudoku8olver (sudoku, 0, 0)) {

System.out.println ("Solution exist");

printSudoku (sudoku);

} else {

System.out.println ("Solution does not exist");

}

}

}

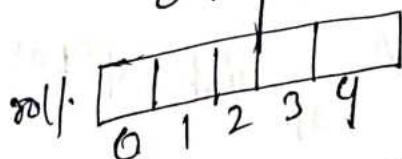
ArrayList → inbuilt linear form
Array List

Array

- fixed size
- primitive data types
- can be stored
- dynamic size
- primitive data type
- can't stored directly

int a[] = new int [5]

↑
max 5 elements
out of bound



• dynamic size

Integer → class

Code:-

```
import java.util.ArrayList;  
// import java.util.*;  
public class classroom {
```

public static void main(String args[])

// string / Books / Plant

ArrayList < Integer > list = new ArrayList<>();

ArrayList < String > list2 = new ArrayList<>();

Add element $O(1)$ operation on ArrayList
 get element $O(1)$
 Remove element $O(n)$
 Set Element at index $O(n)$
 Contains element $O(n)$

Code

```

import java.util.*;
public class ClassRooms
{
    public static void main(String[] args)
    {
        // Create new object
        ArrayList<Integer> list = new ArrayList();
        list.add(1);
        list.add(2);
        list.add(3);
        list.add(4);

        System.out.println(list);
    }
}
    
```

|| Get operation

```

int element = list.get(2);
System.out.println(element);
    
```

|| Delete

```

list.remove(2);
System.out.println(list);
    
```

|| Set

```

list.set(2, 10);
System.out.println(list);
    
```

|| Contains element $O(n)$

```

System.out.print(list.contains(1));
    
```

list.get()

Size of Array list

Code:

```

import java.util.ArrayList;
public class classroom {
    public static void main(String args[]) {
        ArrayList<Integer> list = new ArrayList<()>;
        list.add(1);
        list.add(2);
        list.add(3);
        list.add(4);
        System.out.println(list.size());
    }
}

```

Output: 5
1 2 3 4 5

// print all Arraylist
for (int i=0; i < list.size(); i++)
 System.out.println(list.get(i));
}
System.out.println()

Print Reverse of Arraylist

list = 1, 2, 3, 4, 5 → 5 4 3 2 1

Code:

```

ArrayList<Integer> list = new ArrayList<()>;
list.add(1);
list.add(2);
list.add(3);
list.add(4);
list.add(5);
for (int i = list.size() - 1; i >= 0; i--) {
    System.out.println(list.get(i));
}

```

Find Maximum Element in Arraylist

list = 2, 5, 9, 3, 6 max = ∞ (Integer.MIN_VALUE)

ArrayList<Integer> list = new ArrayList<()>;

list.add(2);

list.add(5);

list.add(9);

int max = Integer.MIN_VALUE;

for (int i=0; i < list.size(); i++) {

if (max < list.get(i)) {

max = list.get(i);

}

System.out.println("max element = " + max);

}

out → 9

Swap 2 Number

list = 2, 5, 9, 3, 6 index: index1=1, index2=3.

ArrayList<Integer> list = new ArrayList<()>;

list.add(2);

list.add(5);

list.add(9);

list.add(3);

list.add(6);

→ public void swap(ArrayList<Integer> list, int index1, int index2) {

int temp = list.get(index1); if index1 = 1 index2 = 3
swap(list, index1, index2);

list.set(index1, list.get(index2)); swap(list, index2, index1);

list.set(index2, temp);

}

original → [1 5 9 3 6]

swap. → [2 3 9 5 6]

Sorting on ArrayList

scratches

Basic
ArrayList
Inversion
Merge
Quick

optimized

Collections.sort();

✓ Collections → class

Collections.sort(list);

Collection → interface

Ascending
order

Code: //import java.util.ArrayList; or import java.util.*;

//import java.util.Collections;

public class Classroom{

public static void swap(ArrayList<Integer> list, int index1, int index2){

int temp = list.get(index1);

list.set(index1, list.get(index2));

list.set(index2, temp);

} public static void main (String args[]){

ArrayList<Integer> list = new ArrayList<()>;

list.add(2);

list.add(3);

list.add(9);

list.add(3);

list.add(6);

Say(list);

Collections.sort(list);

Say(list);

g,

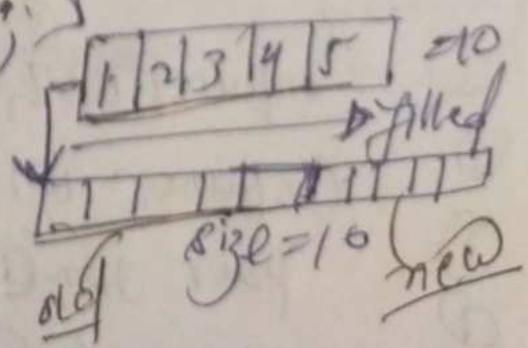
Implementation

→ yourself.

ArrayList<Integer> list = new AL<()>;

0132=5

2x



Multidimensional Array:-

list1: 1 2 3 4 5 (1 table)
 list2: 2 4 6 8 10 (2 table)
 list3: 3 6 9 12 15 (3 table)

ArrayList<ArrayList<Integer>> mainList;
 new ArrayList<>() ;
 ArrayList<int> arr = new ArrayList<()>;
 mainList.add(arr);

public static void main(String args[]){
 ArrayList<ArrayList<Integer>> mainList = new ArrayList<()>;
 ArrayList<Integer> list = new ArrayList<()>;

list.add(1); list.add(2);
 mainList.add(list);

ArrayList<Integer> list2 = new ArrayList<()>;

list2.add(3); list2.add(4);
 mainList.add(list2);

for(int i=0; i < mainList.size(); i++)

ArrayList<Integer> current = mainList.get(i);

for(int j=0; j < current.size(); j++)

System.out.println(current.get(j) + " ");

System.out.println();

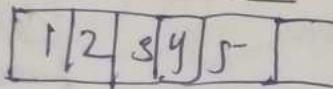
g
g
g

Question

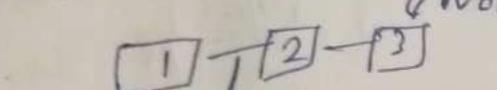
- ① Container with most water
- ② Container with max of trapping water
- ③ pour sum ①
- ④ pour sum ②

linked list

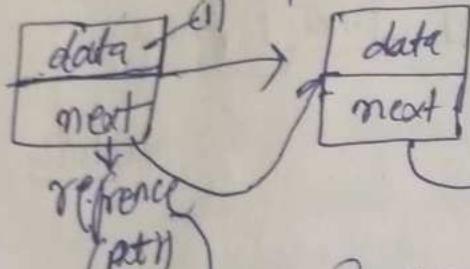
Linear list (data structure)



dynamic

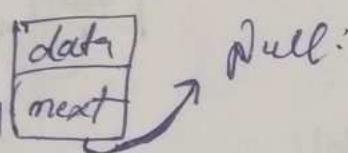


(Nodes) \rightarrow Node



reference Variable
(ptr)

Nodes



Class \rightarrow Node.

Syntax

```

class node {
    int data;
    Node next;
}

public node (int data) {
    this.data = data;
    this.next = null;
}
  
```

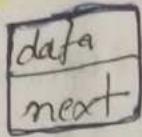
Code

```

public class linked list {
    public static class Node {
        int data;
        Node next;
    }

    public static void main (node (int data)) {
        this.data = data;
        this.next = null;
    }
}
  
```

Head node:



Class Node {

int data;

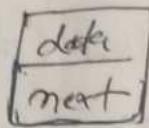
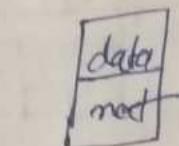
Node next;

public Node (int data) {

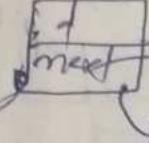
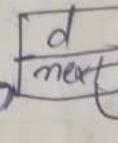
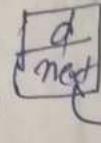
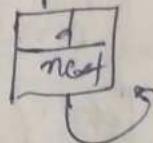
this.data = data;

this.next = null;

}



Head



Tail

Null

①
 ②
 ③
 → pu

Cook public class LinkedList {

public static class Node {

int data;

Node next;

public Node (int data) {

this.data = data;

this.next = null;

}

public static Node head;

public static Node tail;

// Method

add()

remove()

print()

search()

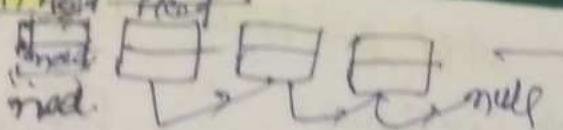
public static void main (String args[]) {

LinkedList ll = new LinkedList();

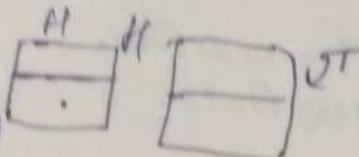
q4

Add 2 in Linked list Head

add first



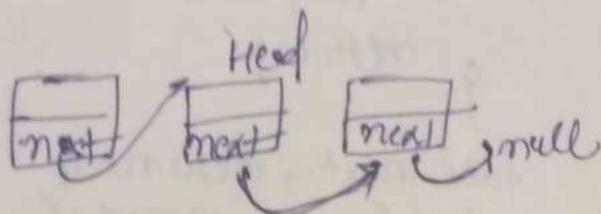
add last



- ① To create new node
- ② new node's next = Head
- ③ Head = new node

public class LinkedList {
 public static class Node {

```
        int data;  
        Node next;  
        public Node (int data){  
            this.data = data;  
            this.next = null;  
        }
```



public static Node head;

public static Node tail;

public void addFirst (int data) {

// step 1 - create new node

Node newNode = new Node (data);

if (head == null) {

head = tail = newNode;

return;

}

// step 2 - New Node next = Head

newNode.next = head; // work

// step 3 - head = new Node

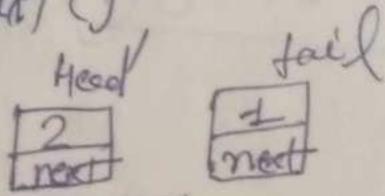
head = newNode;

public static void main (String args[]) {

LinkedList LL = new LinkedList();

LL.addFirst (1);

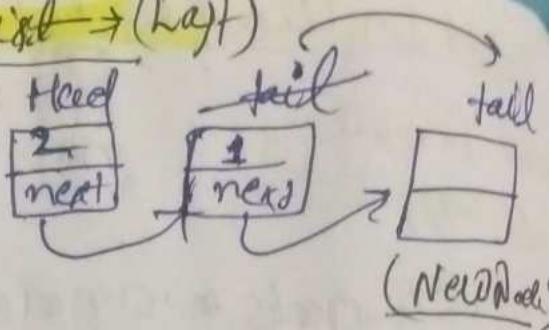
LL.addFirst (2);



T.C = O(1).

Add in linked list \rightarrow (last)

- ① Create a node (new node)
- ② tail.next = new node
- ③ tail = new Node.



public void addLast(int data){

Node newNode = new Node(data);

if (head == null) {

head = tail = newNode;

} return;

tail.next = newNode;

tail = newNode;

}

public static void main(String args[]){}

LinkedList LL = new LinkedList();

LL.addFirst(2);

LL.addFirst(1);

LL.addLast(3);

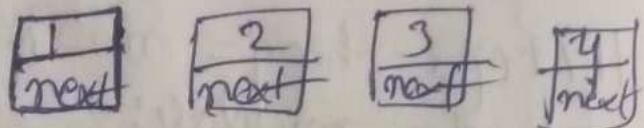
LL.addLast(4);

} }

1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow null

Head

tail



T.C = O(r)

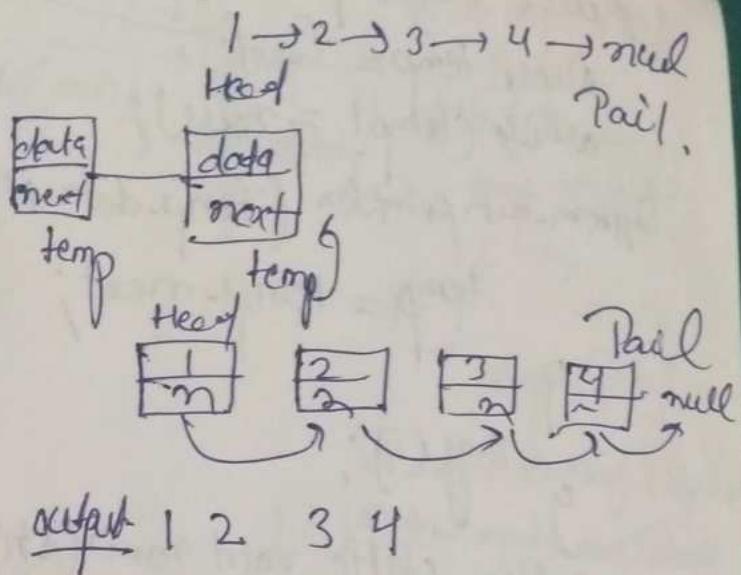
Print a linked list

```
Node temp = head;
print(temp.data);
```

```
temp = temp.next;
```

```
while (temp != null) {
```

}



Code public class Linkedlist

```
public static class Node {
```

```
    int data;
```

```
    int next;
```

```
    public Node (int data) {
```

```
        this.data = data;
```

```
        this.next = null;
```

g

```
    public static Node head;
```

```
    public static Node tail;
```

```
    public void addFirst (int data) {
```

```
        Node newNode = new Node(data);
```

```
        if (head == null) {
```

```
            head = tail = newNode;
```

return;

```
        head.next = newNode;
```

g head = newNode;

```

public void print() {
    Node temp = head;
    while (temp != null) {
        if (head == null) {
            say("LL is empty.");
            return;
        }

```

```
System.out.println(temp.data + " ");

```

```
temp = temp.next;
```

y

y say();

```
public static void main(String[] args) {

```

```
    linkedList lL = new LinkedList();

```

```
    lL.addFirst(2);

```

```
    lL.addFirst(1);

```

```
    lL.print();

```

```
    lL.addFirst(3);

```

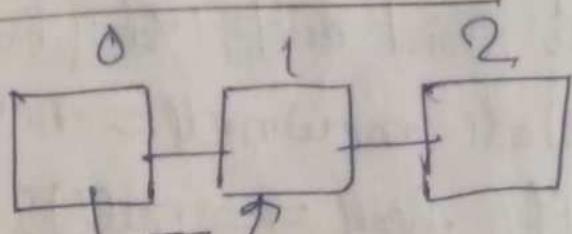
```
    lL.print();

```

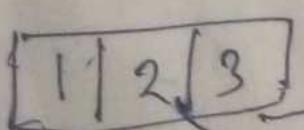
y
y

Add in the middle

add (index, data)

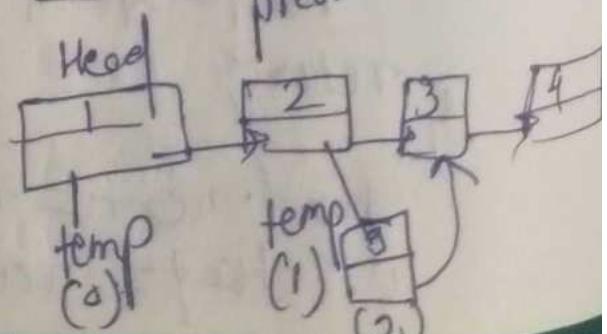
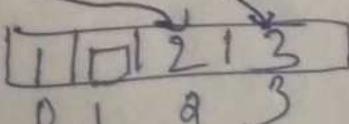


$i^{\text{th}} \text{ index} = 1$



(Array Arraylist)

data[2]
data[3]



prev.

Head
temp(0)

temp(1)
temp(2)

```
public void add(int idx, int data){
```

```
    Node newNode = New Node(data);  
    if(idx == 0){  
        Node temp = head;  
        int l = 0;
```

Node temp = head

l = 0

while (l < idx - 1)

temp → next

l++;

g

temp (prev)

- ① newNode.next = temp.next
- ② temp.next = newNode

```
    while (l < idx - 1){  
        temp = temp.next;  
        l++;  
    }
```

```
    // l = idx - 1; temp → prev
```

```
    newNode.next = temp.next;  
    temp.next = newNode;  
}
```

```
public static void main(String args[]){  
    linkedList lL = new linkedList();
```

```
    lL.addFirst(2);
```

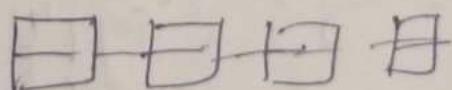
```
    lL.add(2, 9);
```

```
    lL.print();
```

Y
output:

Size of linked list

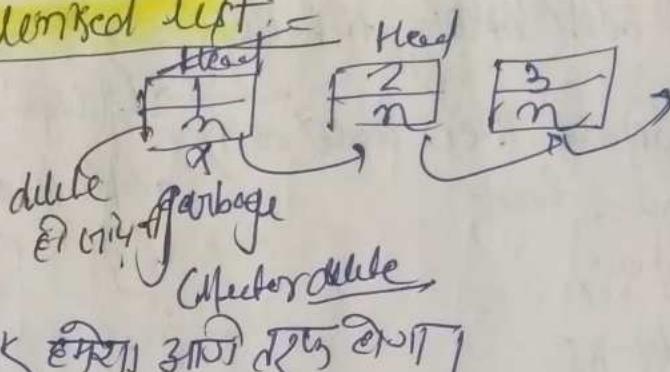
static int size = 1



et new node of size 4 at head . $\Rightarrow j = 4$

Remove in a linked list

- Remove first
- remove last



SinglyList :- Link से जुटी तरह है।

(Method)

```
public int removeFirst() {
    int val = head.data;
    head = head.next;
    return val;
}
```

```
public static void main(String[] args) {
    linkedList lL = new linkedList();
    lL.removeFirst();
    lL.print();
}
```

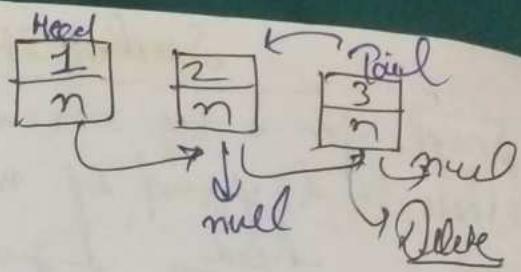
∴

Output : 2 3 4 5

Two Case :- if ($size == 0$)
 say "LL is empty";
 return Integer.MIN_VALUE;
 else if ($size == 1$)
 int val = head.data;
 head = head.next = null;
 return val;

Remove last

- ① prev.next = null
- ② tail = prev



Method public int removeLast()

if (size == 0){

say ("LL is empty");

return Integer.MIN_VALUE;

} else if (size == 1){

int val = head.data;

head = tail = null;

size = 0;

return val;

}

// prev.size = size - 1

for (int i=0; i < size-1; i++)

prev = prev.next;

int val = prev.next.data; // tail.data

prev.next = null;

tail = prev;

size--;

public static void main ()

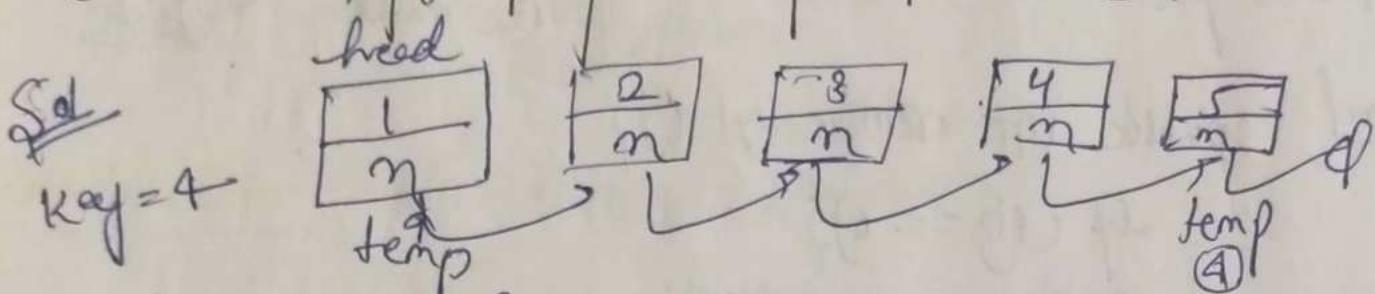
ll.removeLast();

ll.print();

qy

Search (Iterative) Linear Search

Search for a key in a linked list return the position where it is found if not found return -1.



Node temp = head;

while (temp != null){

 Check (temp.data == key)

}

public int search(int key){

 Node temp = head;

 int i = 0;

 while (temp != null){

 if (temp.data == key) { // key found

 return i;

 temp = temp.next;

 i++;

 // key not found

 return -1;

 p.s.v.m();

 linkedlist l = new SinglyList();

 l.addFirst(2);

 l.addFirst(1);

ll. add last(4);

ll. " (5);

ll. add (2,3);

ll. print(); l) 1>2>3>4>5

say(ll. isSearch(3));

say(ll. ftrSearch(10));

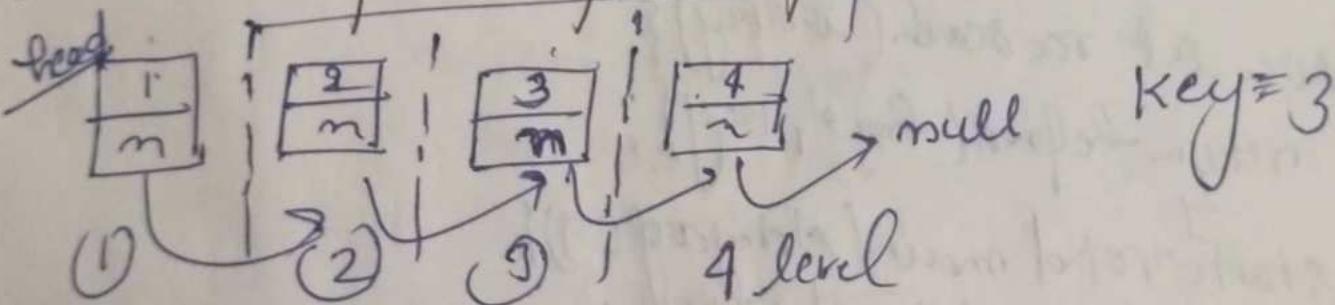
T.C = O(n)

gg

out 2
7 -1

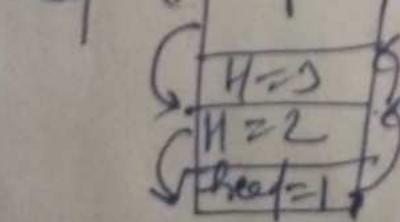
Search (Recursive)

Search for a key in a linked list. Return the position where it is found if not found return -1. Use Recursion.



Base Case: head=null → if (head.data == key)
return -1; → return 0
searched(head.next);

1 → 2 → 3 → 4 → null Key=3

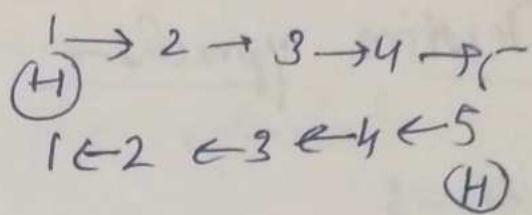
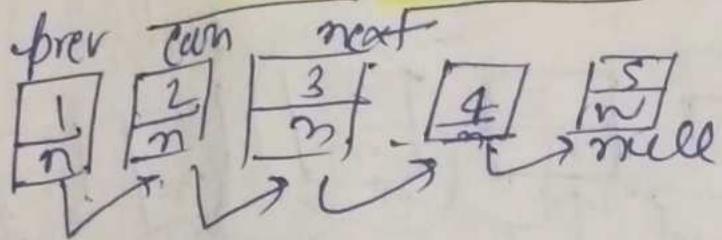


Code:

```
public int search(Node head, int key){  
    if (head == null){  
        return -1;  
    }  
    if (head.data == key){  
        return 0;  
    }  
    int idx = helper(head.next, key);  
    if (idx == -1){  
        return -1;  
    }  
    return idx+1;  
}  
public int search(int key){  
    return helper(head, key);  
}  
public static void main(String args[]){  
    linkedLL = new linkedList();  
    ll.addFirst(1);  
    ll.addFirst(2);  
    ll.add(3);  
    ll.print();  
    System.out.println(ll.search(3));  
    System.out.println(ll.search(10));  
}
```

Output: -1

Reverse a linked list



- ① $\text{next} = \text{curr}.next;$
- ② $\text{curr}.next = \text{prev};$
- ③ $\text{prev} = \text{curr};$
- ④ $\text{curr} = \text{next};$

Method public void reverse() {

```

    Node prev = null;
    Node curr = head != null;
    Node next;
    while (curr != null) {
        next = curr.next;
        curr.next = prev;
        prev = curr;
        curr = next;
    }
    head = prev;
}
  
```

public static void main(String args[]) {

LinkedLL ll = new LinkedLL();

ll.addFirst(2);

ll.addFirst(3);

ll.add(2, 7);

ll.print();

ll.reverse()

ll.print();

Output 5-74->3->2->1

Find & remove n^{th} node from End

Iterative approach

$n=3$

n^{th} end
start

$(size-n+1)^{th}$ start

Code: public void deleteNthFromEnd(int n){

// calculate size

int s3 = 0;

Node temp = head;

while (temp != null){

temp = temp.next;

s3++;

if (n == s3){

head = head.next; // remove first

return;

// s3 - 3

int s = 1;

int sToFind = s3 - n;

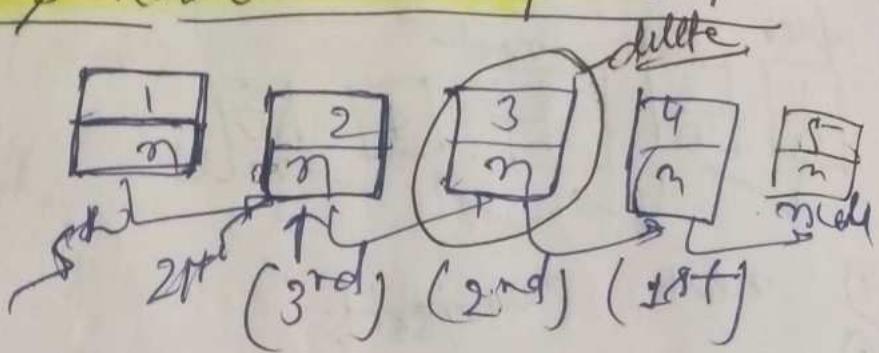
Node prev = head;

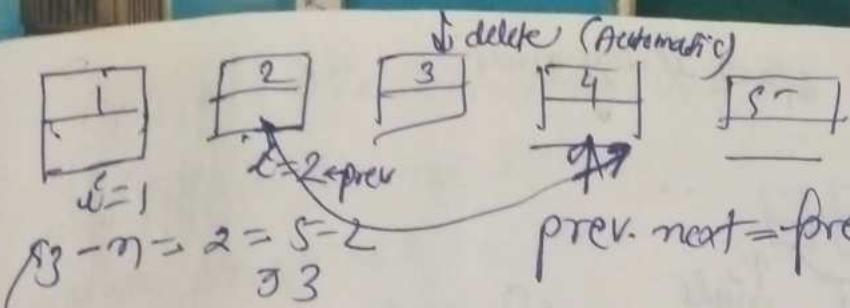
while (s < sToFind){

prev = prev.next;

s++;

prev.next = null; // delete nth from End(s)





prev. next = pre. next. next.

Check if LL is a palindrome

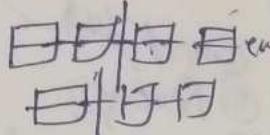
Slow fast
current
reversehalf

{1221
1441
Cac
madam
racecar}

① LL → Arraylist → O(n) → TC
array → O(n) → SC
String

Step

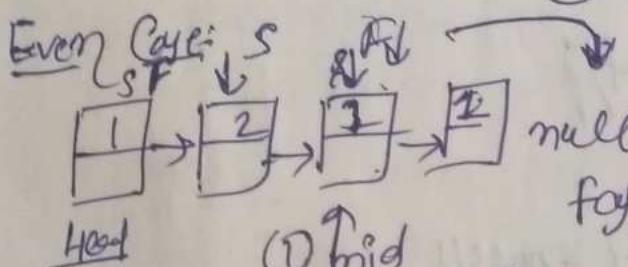
① Find mid node



② 2nd half reverse

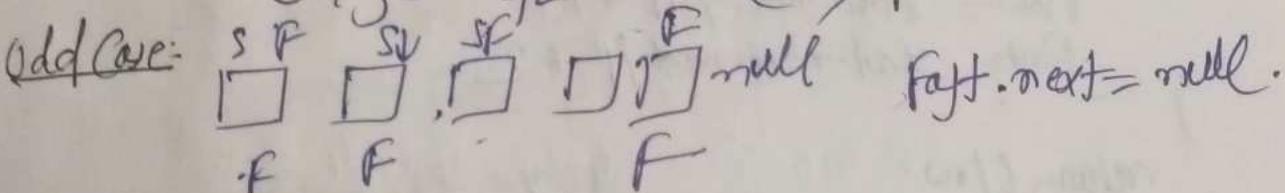
③ Checks if 1st half = 2nd half.

left = right



① Slow fast technique

(Fast) fast = head; $l/l+1$
(Slow) fast = head; $l/l+2$



① Find mid [fast = null]

fast.next = null

public Node findMid(Node head){

 Node slow = head;

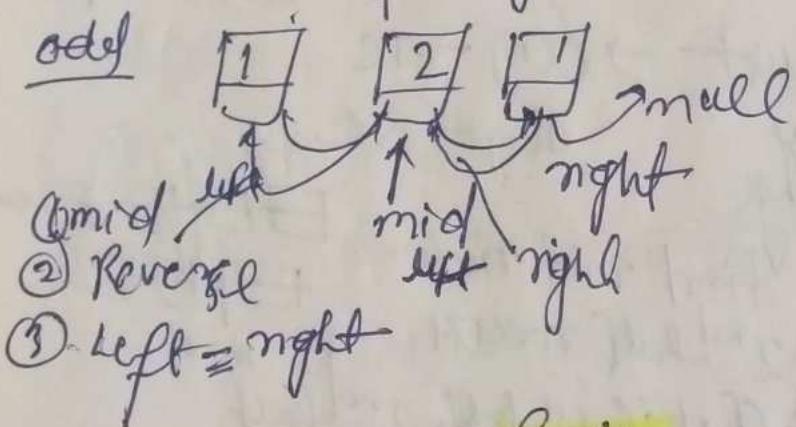
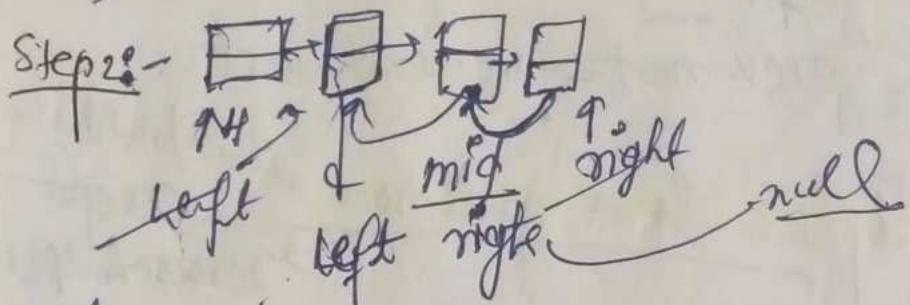
 Node fast = head;

 while (fast != null && fast.next != null)

 slow = slow.next; $l/l+1$

 fast = fast.next.next; $l/l+2$

return $\text{slow} // \text{slow is my node}$



Code

```
public Node find_mid(Node head){  
    Node slow = head;  
    Node fast = head;  
    while(fast != null & fast.next != null){  
        slow = slow.next; // +1  
        fast = fast.next.next; // +2  
    }  
    return slow;
```

public boolean check_pallidm(){

// step1 → find mid

// step2 → Reverse second half

// step3 → check left half & right half

```
if(head == null || head.next == null){  
    return true;
```

Node midNode = findMid(head);

11 step 2 → Reverse 2nd Half.

Node prev = null;

Node curr = midNode;

Node next;

while (curr != null) {

next = curr.next;

curr.next = prev;

prev = curr;

} curr = next;

Node right = prev; // right half head

Node left = head;

11 step 3 check left and right half

while (right != null) {

if (left.data != right.data))

return false;

} left = left.next;

} right = right.next;

} return true;

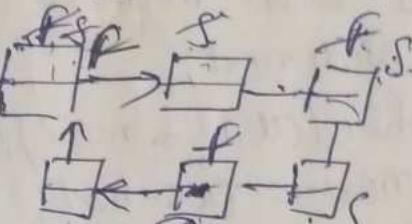
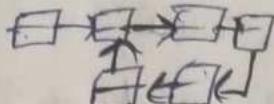
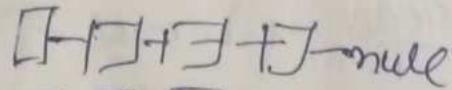
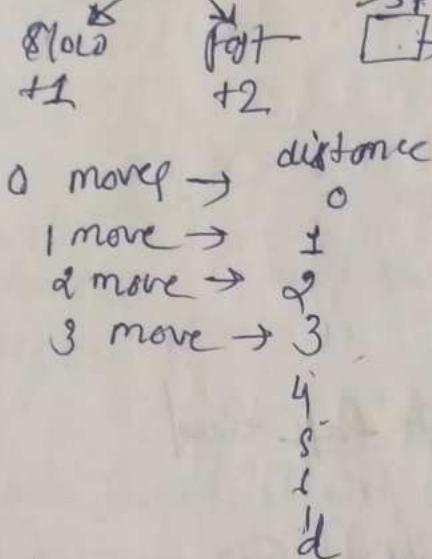
ll.print(); // 1 > 2 > 2 > 1

say (ll.checkPalindrome());

linked list - 2

Detect a loop/cycle in LL :-

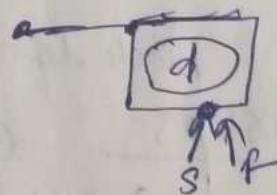
Floyd's cycle finding algorithm:-



रेखा की लिंगमें

Cycle exist or
not

slow = fast
cycle → true.
false



Logic
slow = head
fast = head

while (fast != null && fast.next != null) {

slow → +1

fast → +2

(slow == fast) || cycle

} return true;

public boolean isCycle() {

Node slow = head;

Node fast = head;

while (fast != null && fast.next != null) {

slow = slow.next; // +1

fast = fast.next.next; // +2

if (slow == fast) {

Apro

return true; // Cycle exist

y

return false; // Cycle does not exist

y

public static void main(String args[]){

head = new Node(1);

head.next = new Node(2);

head.next.next = new Node(3);

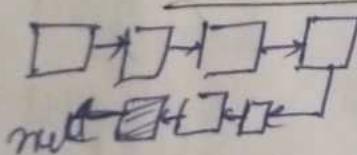
head.next.next.next = head;

// 1->2->3->1

System.out.println("Cycle");

y

Remove a loop / cycle in a linked list



~~Approach~~ ①

Find last node

②

last node.next = null.

Approach: ① detect Cycle

② slow = head

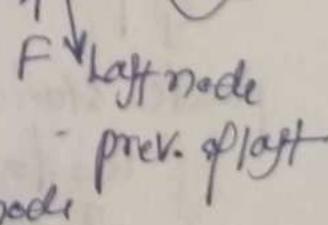
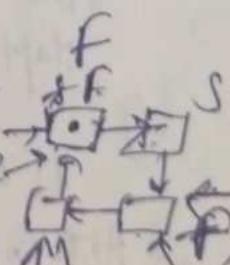
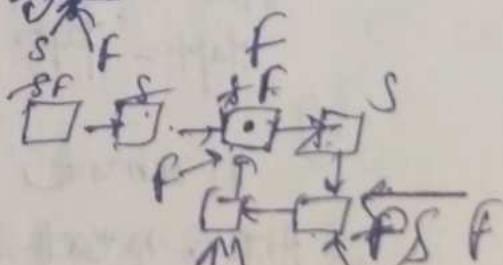
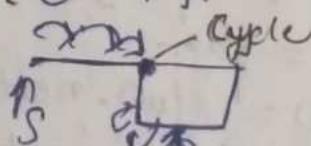
③ slow → +1

fast → +2
prev = null;

④ while (slow == fast) {

slow → +1
fast → +2
prev = fast

prev.next = null // last node



public static void removeCycle(){
 Step
 Node slow = head; **slow =**
 Node fast = head; **fast =** boolean cycle = false;
 if (fast == null || fast.next == null)
 return;

while (fast != null && fast.next != null){

slow = slow.next;

fast = fast.next.next;

if (fast == slow){

cycle = true;

break;

}

if (cycle == false){

return;

// Find meeting point

slow = head;

 Node prev = null;

while (slow != fast){

prev = fast;

slow = slow.next;

fast = fast.next;

}

// remove cycle > fast.next = null

prev.next = null;

public static void main(String[]){

head = new Node(1);

head.next = new Node(2);

head.next.next = new Node(3);

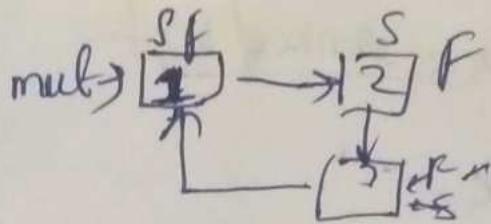
head.next.next.next = head;

- ① Detect Cycle
- ② Find meeting point
- ③ Remove cycle
 $fast.next = null$

```

    || 1->2->3->1
    say( iscycle() );
    removeCycle();
    say( iscycle() );
}

```



Java Collection Framework

ArrayList → import java.util.ArrayList
import java.util.LinkedList;

J.CF :
 ArrayList
 linkedlist
 stack
 Queue
 HashSet
 HashMap

↳ L.L in Java Collection framework:-

```

import java.util.LinkedList;
public class classroom {
    public static void main(String args[]) {
        // Create
        LinkedList< Integer > LL = new LinkedList< >();
        // add
        LL.addLast(1);
        LL.addLast(2);
        LL.addFirst(0);
        // 0->1->2
    }
}

```

```

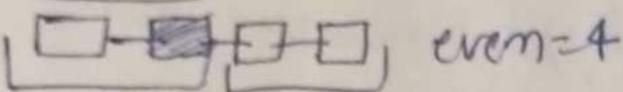
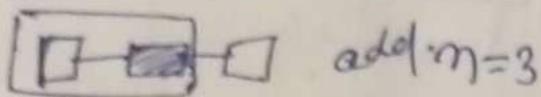
    say(LL);
    // remove
    LL.removeLast();
    LL.removeFirst();
}

```

Merge Sort on a linked list

Steps:-

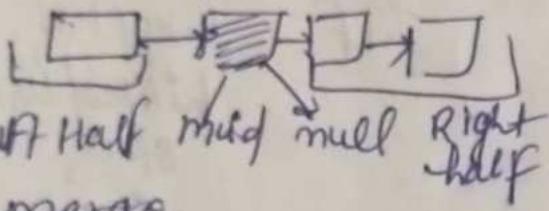
① LL → middle



② ① left half → MS

② Right Half → MS

mid.next=null



③ merge

Mid

slow = head

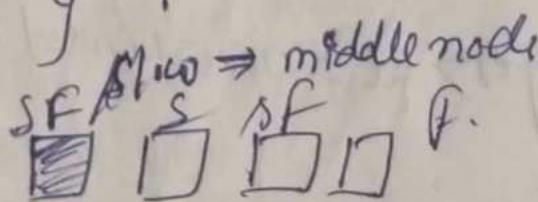
fast = head.next

while(fast != null & fast.next != null) {

slow → +1

fast → +2

y



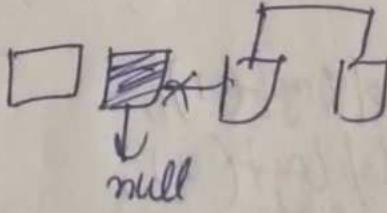
right half

② righthead = mid.next

mid.next = null

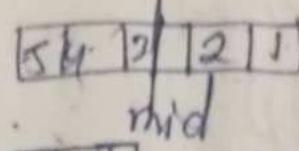
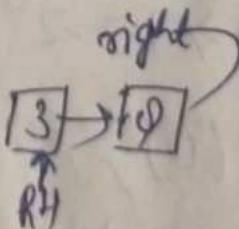
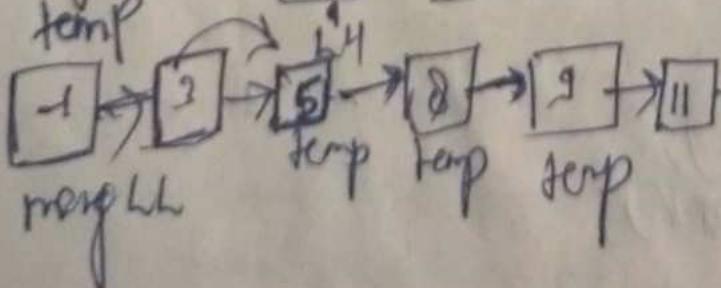
MS (head) || left half

MS (right) || right half

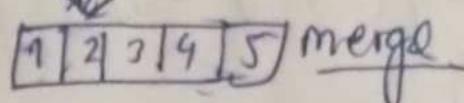
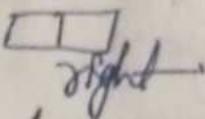
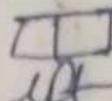


③ merge

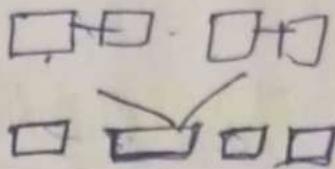
temp



mid



merge



Code:

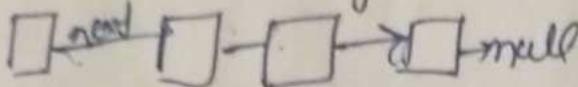
public Node mergeSort (Node head) {

Zig-Zag linked list

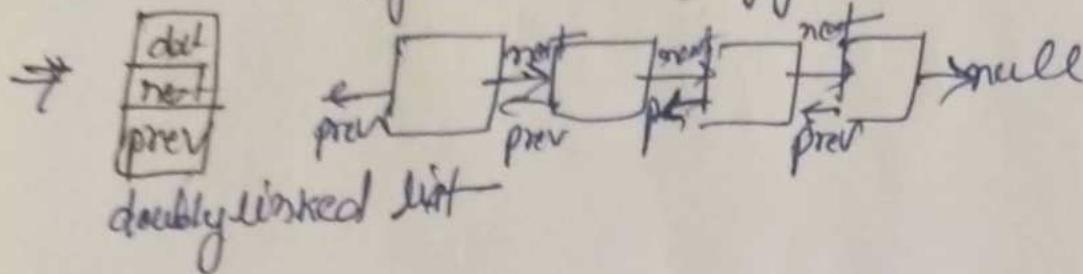
for a linked list of the form : $L(1) \rightarrow L(2) \rightarrow L(3) \rightarrow L(4) \rightarrow \dots \rightarrow L(n-1) \rightarrow L(n)$.
Convert it into a zig-zag form i.e. $L(1) \rightarrow L(3) \rightarrow L(2) \rightarrow L(n-1) \rightarrow L(n)$.

Doubly linked list

Approach:



single direction. (Singly linked list)



Nodes

int data;

Node next;

Node prev;

g

public class DoublyLL {

public class Node {

int data;

Node next;

Node prev;

public Node (int data) {

this.data = data;

this.next = null;

this.prev = null;

public static Node head;

public static Node tail;

public static int size;

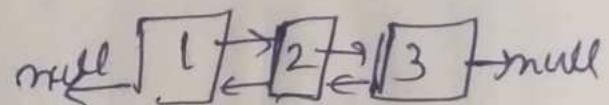
// add

public void addFirst (int data) {

Node newNode = new Node (data);

if (head == null) {

head = tail = newNode;



① Create node

② newNode.next = head

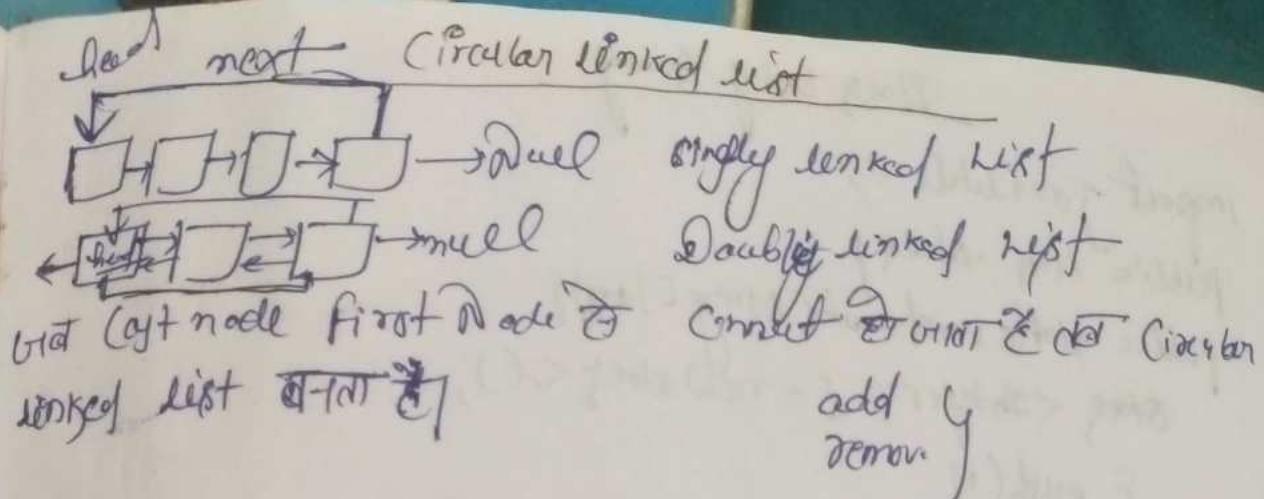
head.prev = newNode

head = newNode.

```
return;
}
newNode.next = head;
head.prev = newNode;
head = newNode;
}

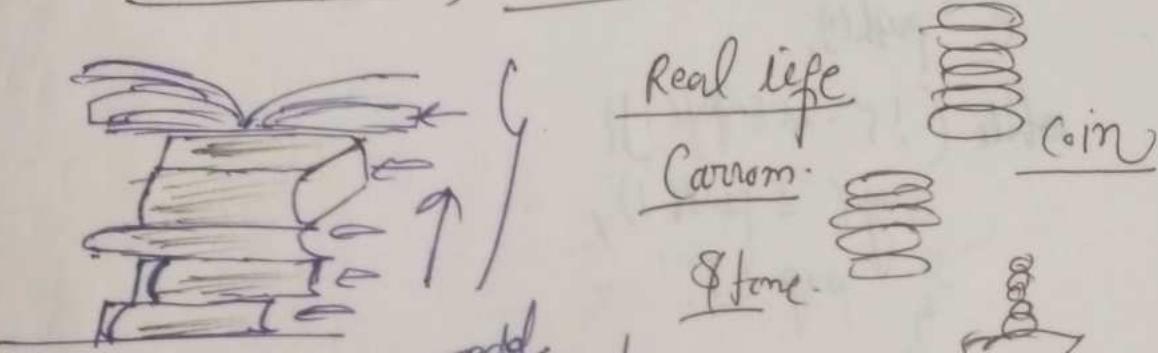
// print
public void print(){
    Node temp = head;
    while( temp != null){
        System.out.println(temp.data + " <-> ");
        temp = temp.next;
    }
}

public static void main( String args[] ){
    DoubleLL dll = new DoubleLL();
    dll.addFirst(3);
    dll.addFirst(2);
    dll.addFirst(1);
    dll.print();
    System.out.println( dll.size );
}
}
```



Stacks Data Structure

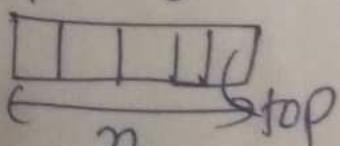
STACK



- Operations:
- ① push O(1) add
 - ② pop O(1) remove
 - ③ peek O(1)
- LIFO (Last in first out.)

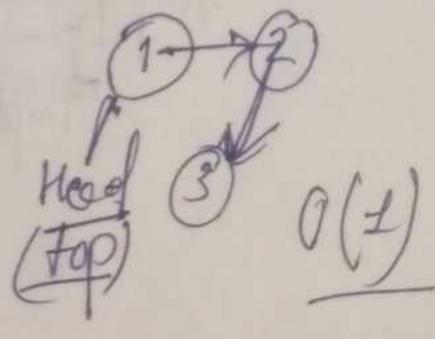
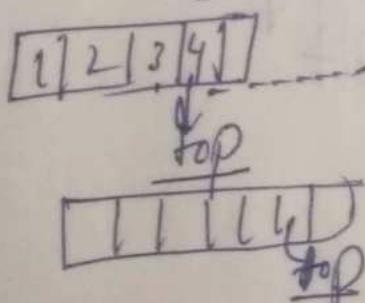
stack with
variable size

Array
fixed size



Stack == Full

ArrayList
variable size



Stack Using Array

```
import java.util.*;  
public class Stack {  
    public static void main(String[] args) {  
        Stack < Integer > S = new Stack < Integer >;
```

S. push(1);

S. push(2);

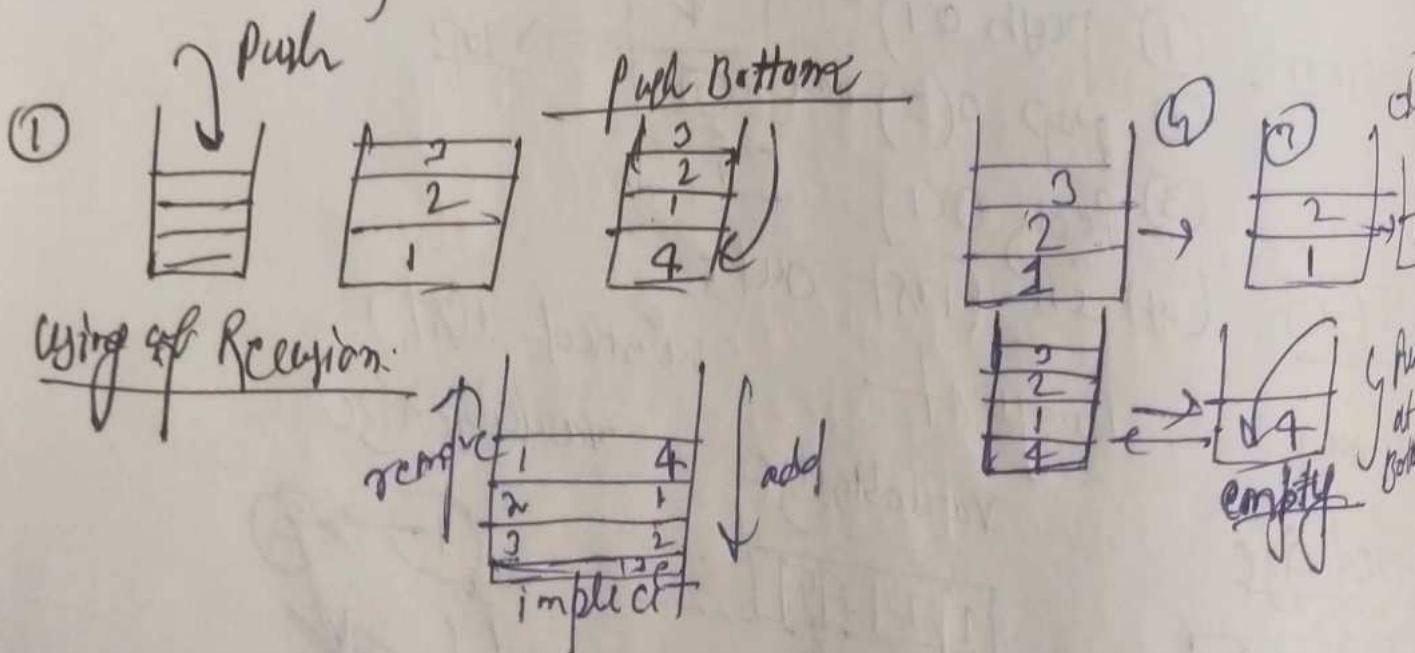
S. push(3);

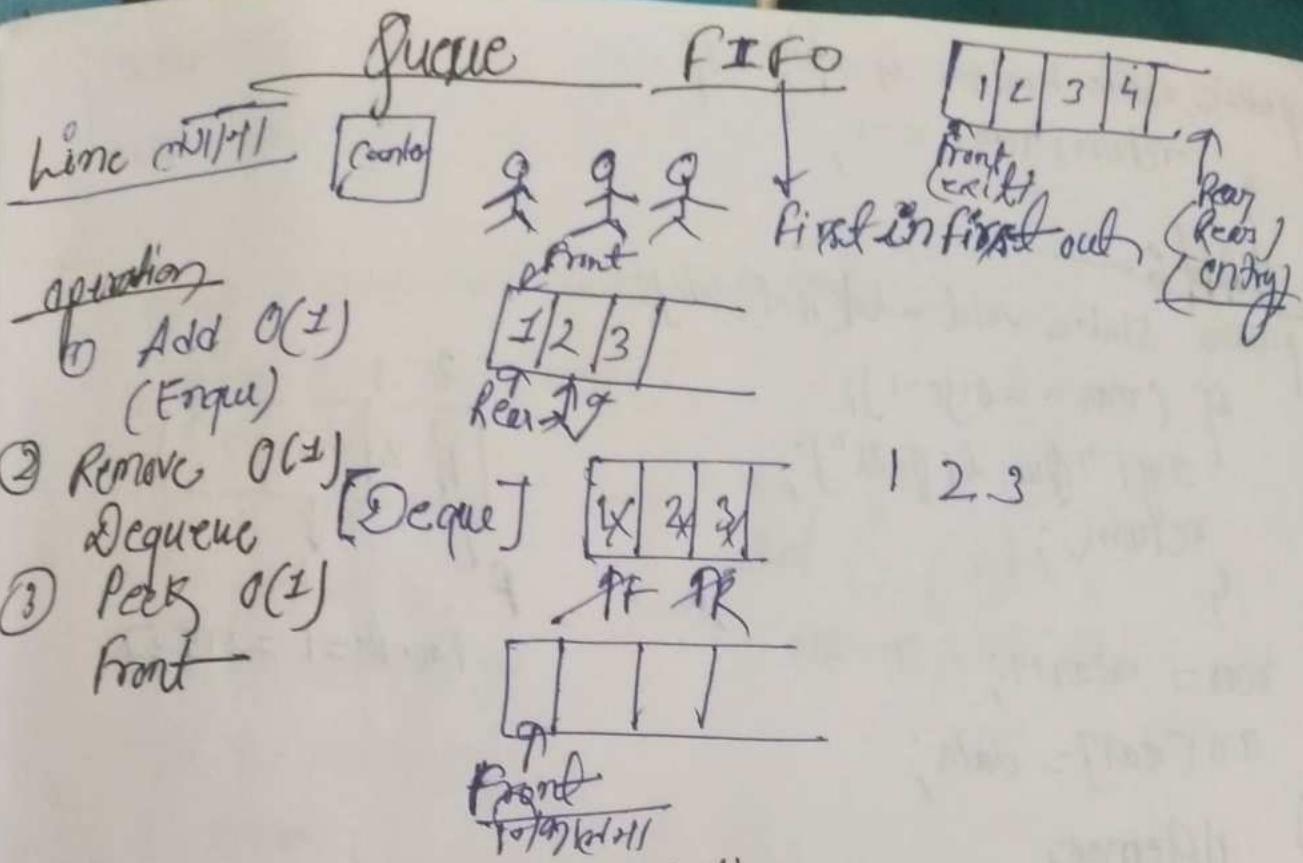
while (!S.isEmpty()) {

S. System.out.println(S.pop());

S. pop();

} } }





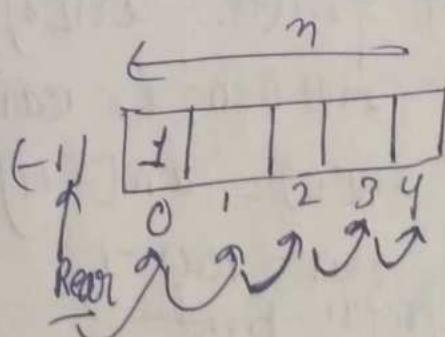
→ fixed size
 $n \times n$
 ④ Remove $O(n)$

Circular Queue

```

Code: public class Queue {
    static class Queue {
        static int arr[];
        static int front;
        static int rear;
        Queue (int n) {
            arr = new int [n];
            arr[0] = -1;
            size = n;
            rear = -1;
        }
    }
}

```



```
public static boolean isEmpty() {  
    return rear == -1;  
}
```

// Add :-

```
public static void add(int data) {
```

```
    if (rear == size - 1) {  
        System.out.println("Queue is full");  
        return;  
    }
```

```
    rear = rear + 1;
```

```
    arr[rear] = data;
```

// Remove

```
public static int remove() {
```

```
    if (!isEmpty()) {
```

```
        System.out.println("empty queue");  
        return -1;  
    }
```

```
    int front = arr[0];
```

```
    for (int i=0; i < rear; i++) {
```

```
        arr[i] = arr[i+1];
```

```
    }
```

```
    rear = rear - 1;
```

```
    return front;
```

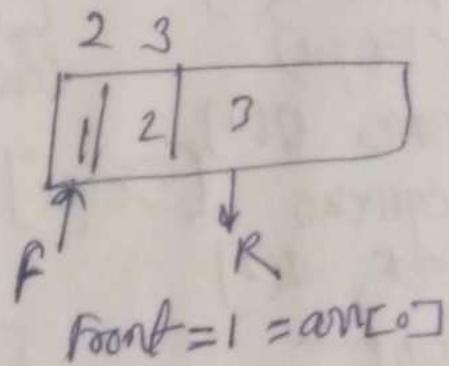
```
}
```

// peek

```
public static int peek() {
```

```
    if (!isEmpty()) {
```

```
        System.out.println("empty queue");  
    }
```



```

    g return -1;
    g return arr[i];
}
g
public static void main(String args[]) {
    Queue q = new Queue(5);
    q.add(1);
    q.add(2);
    q.add(3);
    while (!q.isEmpty()) {
        System.out.println(q.peek());
        q.remove();
    }
    g
    g
    g
}

```

$\text{add } O(1)$
 $\text{remove } O(n)$

Circular Queue

Static class Queue
 static int arr[];
 static int size;
 static int rear;
 static int front;

Queue (int n) {

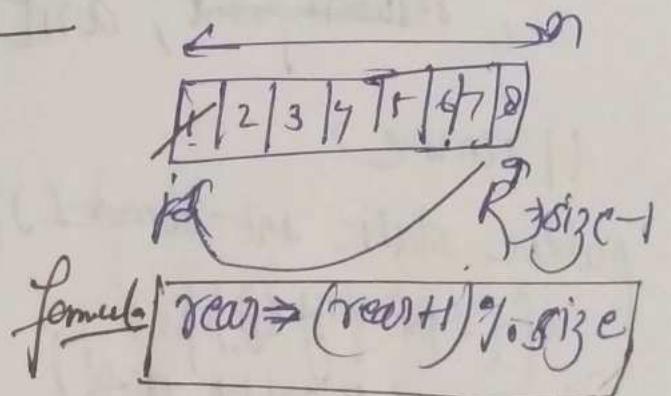
Queue arr = new int[n];

size = n;

rear = -1;

front = -1;

public static boolean isEmpty() {



$$\text{size} = 8$$

$$\text{rear} = (7 + 1) \% 8$$

$$\not\rightarrow 0$$

$$\text{front} = (\text{front} + 1) \% \text{size}$$

return rear == -1 && front == -1;

|| peek
public static boolean isfull() {
 return (rear + 1) % size == front;

|| add
public static void add(int data) {

if (isfull()) {

Say ("queue is full");

return;

if (front == -1) {

front = 0;

rear = rear + 1; size;

~~return front; arr[rear] = data;~~

|| remove

public static int remove() {

if (isEmpty()) {

Say ("empty que");

return -1;

int result = arr[front];

if (rear == front) {

rear = front = -1;

} else

front = (front + 1) % size;

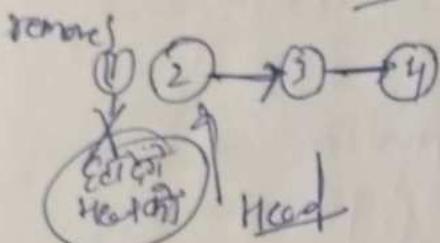
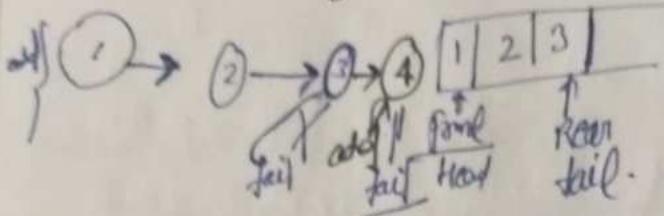
front = (front + 1) % size;

~~return result;~~

~~return result;~~

```
11 peek  
public static int peek(){  
    if (isEmtpy())  
        System.out.println("empty queue");  
    return -1;  
}  
9  
return arr[front];  
9  
public static void main (String args[]){  
    Queue q = new Queue(3);  
    q.add(1);  
    q.add(2);  
    q.add(3);  
    System.out.println(q.remove());  
    q.add(4);  
    System.out.println(q.remove());  
    q.add(5);  
    // 123  
    while (!q.isEmpty())  
        System.out.println(q.peek());  
        q.remove();  
    }  
9
```

Question Queue using linked list



Code:

```
public class Queue {
    static class Node {
```

```
        int data;
        Node next;
        Node (int data) {
            this.data = data;
            this.next = null;
        }
```

```
    static class Queue {
```

```
        static Node head = null;
```

```
        static Node tail = null;
```

```
        public static boolean isEmpty() {
```

```
            return head == null & tail == null;
        }
```

// add

```
        public static void add (int data) {
```

```
            Node newNode = new Node (data);
```

```
            if (head == null) {
```

```
                head = tail = newNode;
```

```
            return;
```

```
tail.next = newNode;  
tail = newNode;
```

y
|| remove
public static int remove(){

```
if (isEmpty())  
    say( "empty queue");  
return -1;
```

y int front = head.data;
return if (~~rear~~ == front)
tail = head = null;

y else {

```
head = head.next;
```

y return front;

y || peek public static int peek(){

```
if (isEmpty())  
    say( "empty queue")
```

return -1;

y return head.data;

y public static void main(String args[]){

```
Queue q = new Queue(3);
```

q.add(1);

q.add(2);

q.add(3);

while(!q.isEmpty()){

```
say( q.peek());
```

q.remove();

};

Java Collection framework

Import java.util.*;

public class QueueS

public static void main (String args[]){

// Queue q = new Queue();

Queue<Integer> q = new LinkedList<Integer>(); // Array Impl.

q.add(1);

q.add(2);

q.add(3);

while (!q.isEmpty()) {

System.out.println(q.peek());

q.remove();

q
q
q

Output:
1.
2.
3.

Queue using 2 stacks (LIFO)

Push O(n) or
add
remove

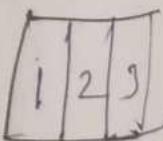
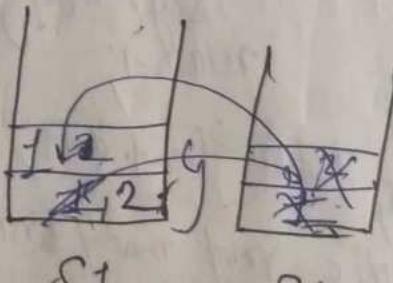
Pop O(1)
remove

peek
add O(1)

① Add

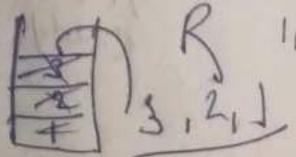
S1 → S2
S1 push

② S2 → S1



3, 2, 1

Add 1, 2, 3



1, 2

R 1, 2

3, 2, 1

⑥ remove

$s1 \rightarrow pop$

Code: import java.util.*;
public class QueueB{
static Stack<Integer> s1 = new Stack<>();
static Stack<Integer> s2 = new Stack<>();
public static boolean isEmpty(){
return s1.isEmpty();
}
}

// add

public static void add(int data){
while (!s1.isEmpty()) {
s2.push(s1.pop());
}

s1.push(data);
while (!s2.isEmpty()) {
s1.push(s2.pop());
}

public static int remove(){
if (isEmpty()) {
System.out.println("queue is empty");
return -1;
}
return s1.pop();
}

public static int peek(){

1, 2, 3

1, 2

```

if (q.isEmpty()){
    System.out.println("que is Empty");
}
return -1;
}
return sl.pop();
}

public static void main(String args[])
{
Queue q = new Queue();
q.add(1);
q.add(2);
q.add(3);
while (!q.isEmpty()){
    System.out.println(q.pop());
    q.remove();
}
}

```

Output

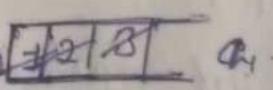
1
2
3

Question 3

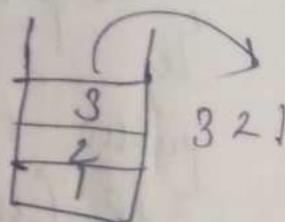
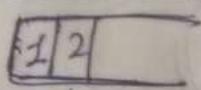
Stacks using 2 Queues:

push $O(n)$
add - $O(1)$

pop $O(n)$



Q_1
top = 5
top = 4
top = 3
top = 2
top = 1



Code: `import java.util.*;`
`public class Queue{`
 `public class Stack{`
 `static Queue<Integer> Q1 = new LinkedQueue<>();`
 `static Queue<Integer> Q2 = new LinkedQueue<>();`
 `public static boolean isEmpty(){`
 `return Q1.isEmpty() && Q2.isEmpty();`
 `}`
 `public static void push(int data){`
 `if (!Q1.isEmpty())`
 `Q2.add(data);`
 `else`
 `Q1.add(data);`
 `}`
 `public static int pop(){`
 `if (isEmpty())`
 `System.out.println("empty stack");`
 `return -1;`
 `else`
 `int top = -1;`
 `while (!Q1.isEmpty())`
 `top = Q1.remove();`
 `if (Q1.isEmpty())`
 `break;`

```

q2.add(top);
if else if care
while (!q1.isEmpty())
    top = q1.remove();
    if (q2.isEmpty())
        break;
    q2.add(top);
}
return top;
public static int peek(){
if (!q1.isEmpty())
    System.out.println("Empty stack");
return -1;
int top = -1;
}

```

else if care

```

if (!q1.isEmpty())
    while (!q1.isEmpty())
        top = q1.remove();
        q2.add(top);
}

```

else if care

```

while (!q2.isEmpty())
    top = q2.remove();
    q1.add(top);
}

```

```

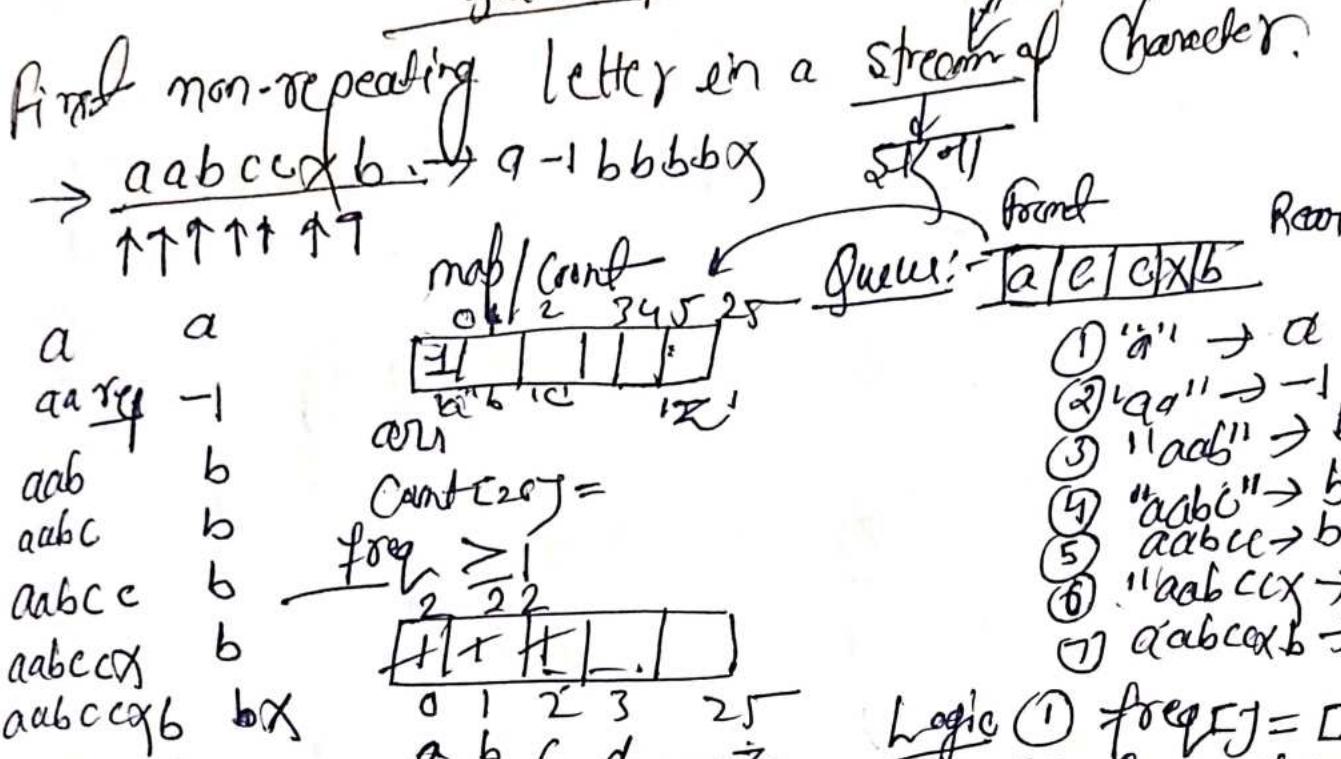
→ return top;
public static void main()
{
    Stack S = new Stack();
    S.push(1);
    S.push(2);
    S.push(3);
    while (!S.isEmpty())
        System.out.println(S.pop());
}

```

Output

3
3
1

Question 4



- ① 'a' → a
- ② 'aa' → -1
- ③ 'aab' → b
- ④ 'aabC' → b
- ⑤ 'aabcc' → b
- ⑥ 'aabccx' → b
- ⑦ 'aabccxb' → x

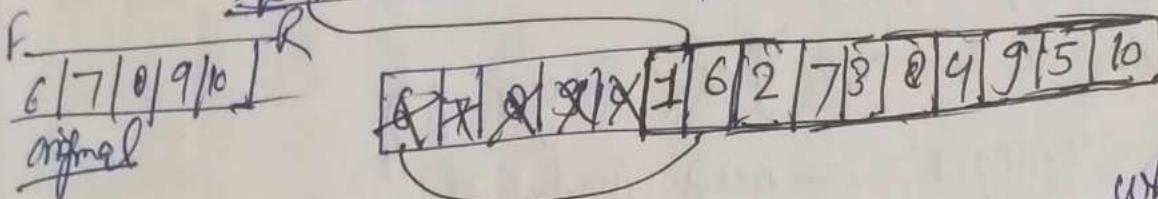
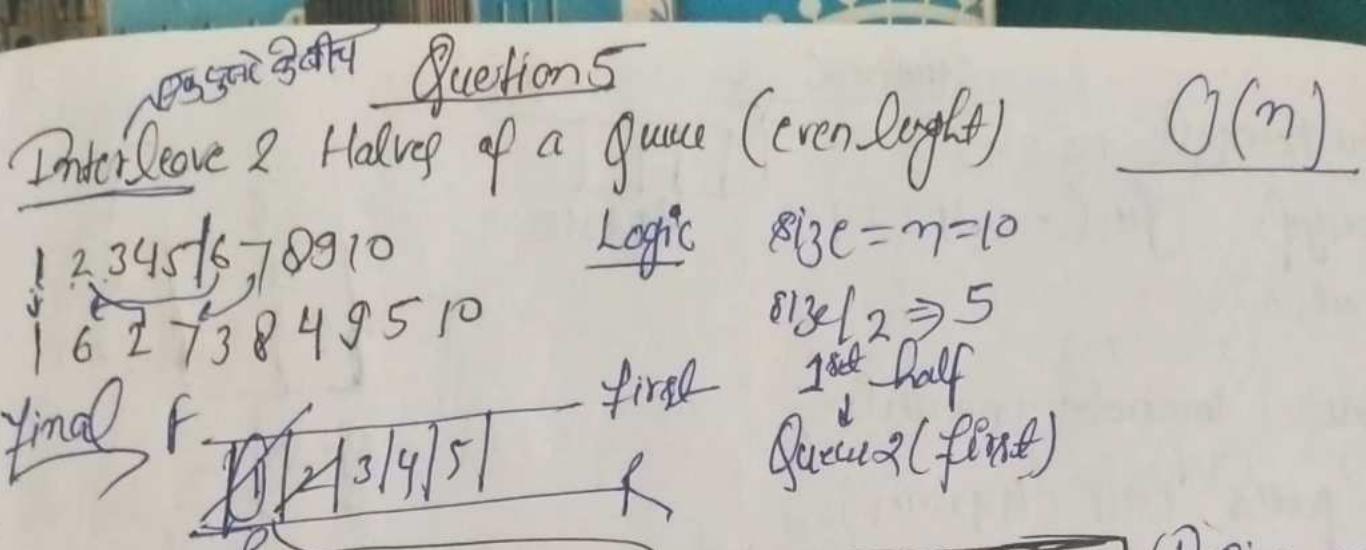
Logic

- ① freq[25] = a-z
- ② Queue<Character>

```
for (int i=0; str.length(); i++) {
    ch = str.charAt(i);
    q.add(ch);
    freq[ch - 'a']++;
}
q.remove();
if (q.isEmpty()) → -1
freq[q.peek()] = 1;
```

```
if (q.isEmpty())
    System.out.println(-1);
else
    System.out.println(q);
```

```
public static void main() {
    String str = "geeksforgeeks";
}
```



$$\text{① } \text{size} = q.size()$$

queue first $\rightarrow \text{size}/2$

while (first != empty())

q.add(first.remove())

q.add(q.remove())

Import java.util.*;

public class classrooms

public static void interleave(Queue<Integer> q){}

Queue<Integer> firstHalf = new linkedList<>();

int size = q.size();

for (int i=0; i<size/2; i++)

firstHalf.add(q.remove());

// point Q

while (!q.isEmpty())

System.out.println(q.remove());

System.out.println();

while (!firstHalf.isEmpty())

q.add(firstHalf.remove());

q.add(q.remove());

}

public static void main (String args[]){}

Queue<Integer> q = new linkedList<>();

q.add(1);

q.add(0);

interleave(q);

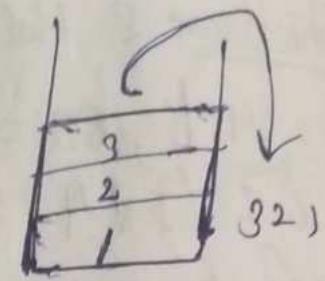
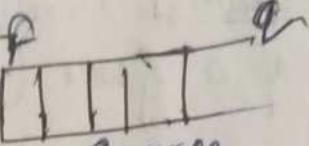
Output

16273049510

Que Reverse: 1 2 3 4 5

Property of: final = 5.4.3.2.1

Stack:



Code: import java.util.*;

public class classroom{

 public static void reverse(Queue<Integer> q){}

 Stack<Integer> s = new Stack<()>;

 while (!q.isEmpty())

 s.push(q.remove());

 g

 while (!s.isEmpty())

 q.add(s.pop());

 g

 public static void main (String args[]){}

 Queue< Integer > q = new LinkedList< ()>;

 q.add(1);

 q.add(5);

 reverse(q);

 // print q

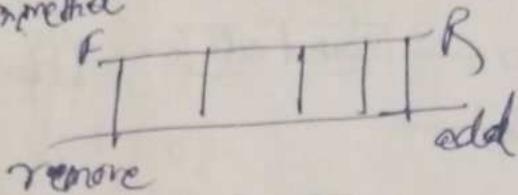
 while (!q.isEmpty()) {

 System.out.print(q.remove());

 System.out.print(" ");

 System.out.println();

~~Dequeue->ext
action method~~



Deque (Double ended queue)

addFirst()
addLast()
removeFirst()
removeLast()
getFirst() -> peek()
getLast()

```
import java.util.*;  
public class deque {
```

```
    public static void main(String args[]){
```

```
        Deque < Integer > deque = new LinkedList < >();
```

```
        deque.addFirst(1);    // 1
```

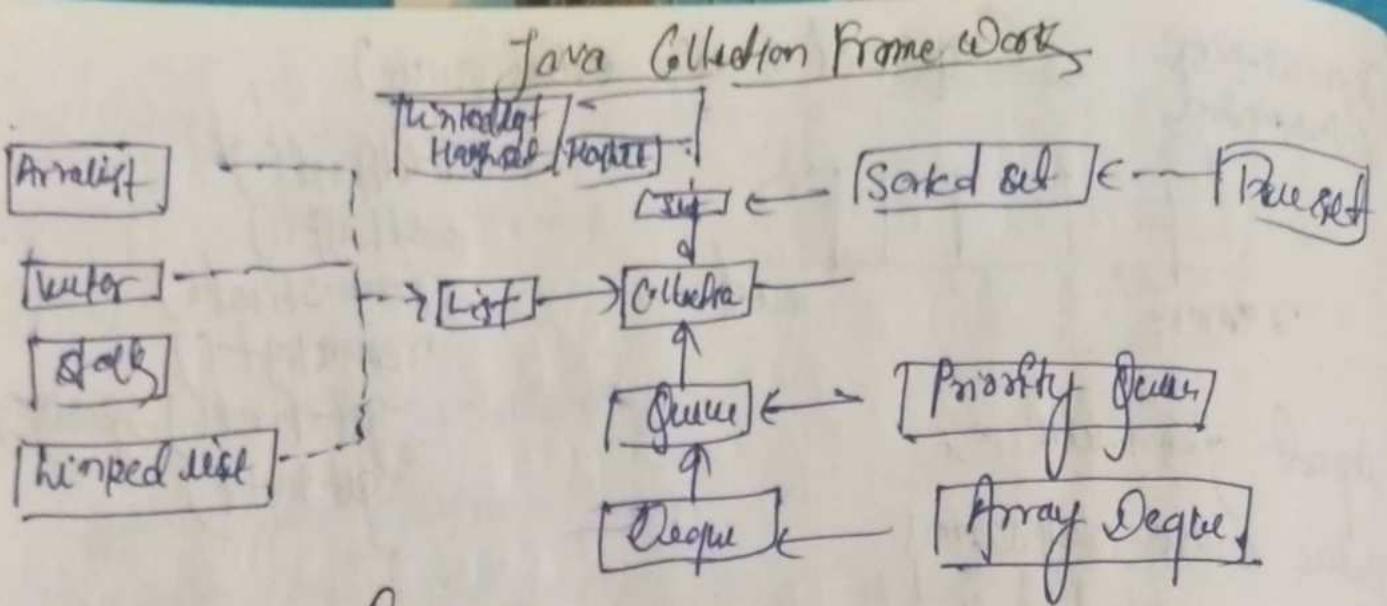
```
        deque.addFirst(2);    // 2 — 1
```

```
        System.out.println(deque);
```

```
        deque.removeFirst();
```

```
        System.out.println(deque);
```

Y



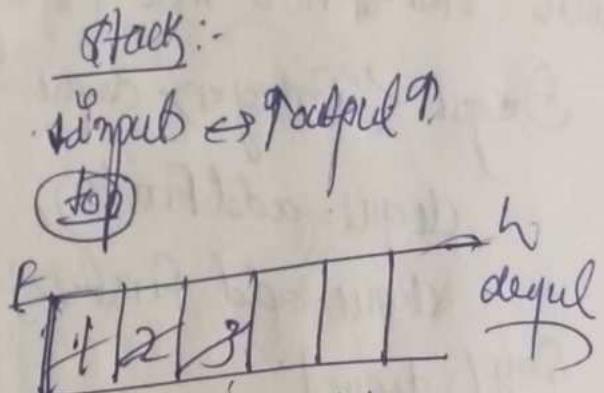
Question 7

Stack & Queue using Deque.

| | | |
|-------------|---------------|--------------------|
| → push O(1) | → add | Stack :- |
| → pop O(1) | → remove O(1) | → input → output ↑ |
| → peek O(1) | → peek | (top) |

Remove → 3, 2, 1 push → addLast() ✓
last pop → removeLast() ✓
 peek → getLast().

Diagram of a stack represented as a vertical rectangle with a horizontal line through it, labeled "stack".



Code:

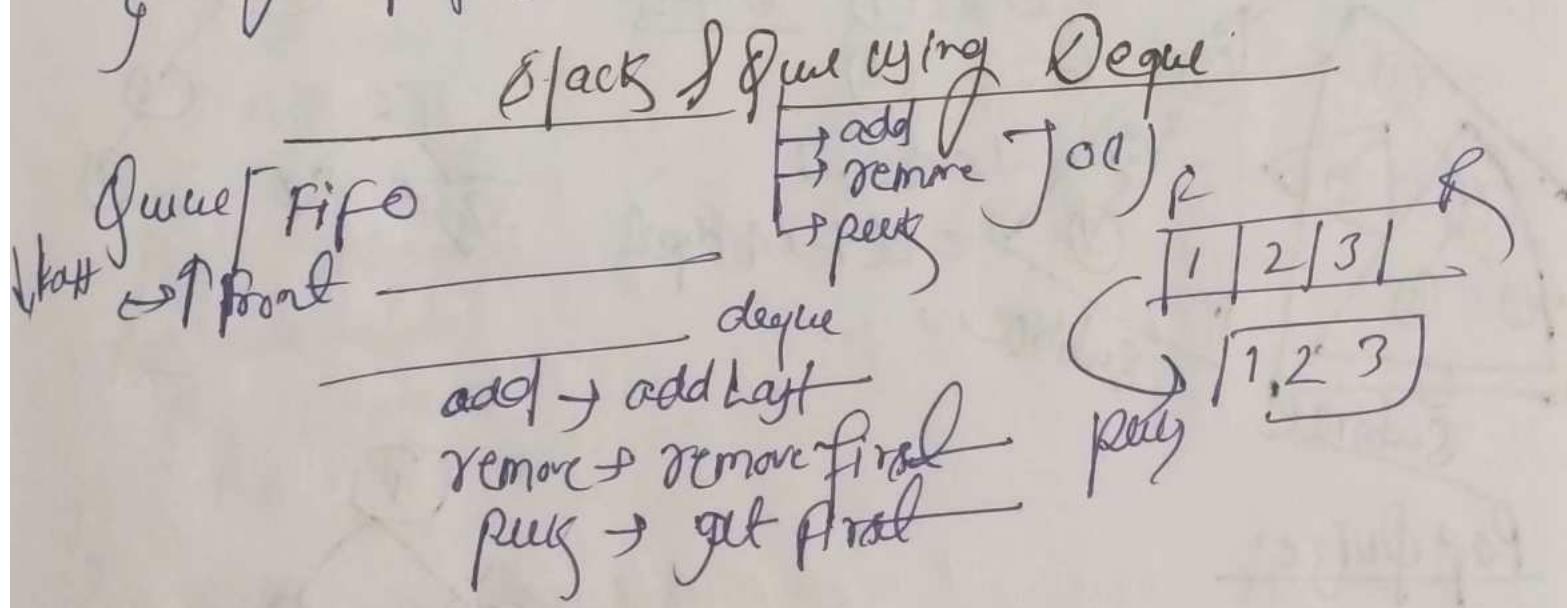
```

import java.util.*;
public class Stack {
    static class Stack {
        Deque< Integer> deque = new linkedlist();
        public void push( int data ) {
            deque.addLast( data );
        }
        public int pop() {
            return deque.removeLast();
        }
        public int peek() {
            return deque.getLast();
        }
    }
}
  
```

```

public static void main(String[] args) {
    Stack s = new Stack();
    s.push(1);
    s.push(2);
    s.push(3);
    System.out.println("pushed " + s.peek());
    System.out.println(s.pop());
    System.out.println(s.pop());
    System.out.println(s.pop());
}

```



```

static class Queue {
    Deque<Integer> deque = new LinkedList<Integer>();
    deque. public void add(int data) {
        deque.addLast(data);
    }
    public int remove() {
        return deque.removeFirst();
    }
    public int peek() {
        return deque.getFirst();
    }
}

```

```

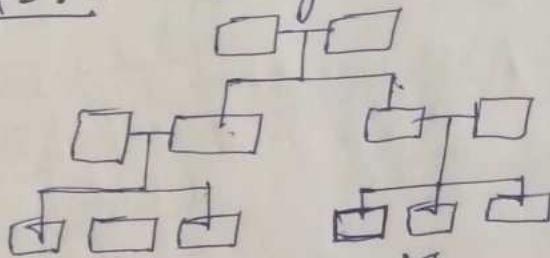
Queue q = new Queue();
q.add(1);
q.add(2);
q.add(3);
System.out.println("pushed " + q.peek());
System.out.println(q.remove());
System.out.println(q.remove());
System.out.println(q.remove());

```

Advanced Data Structure

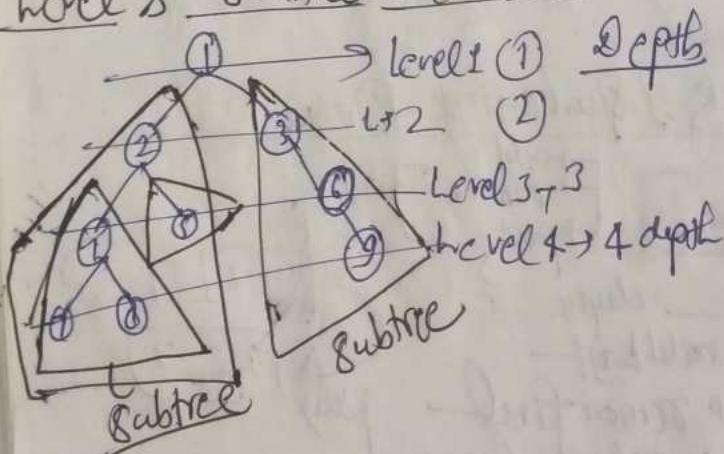
Level :-

Family Tree



Binary [at max 2 children]
tree

level & subtree in a tree



Pop Quiz:

① Children of 4: 7, 8

No. of leaves: 4

Parents of 6: 3

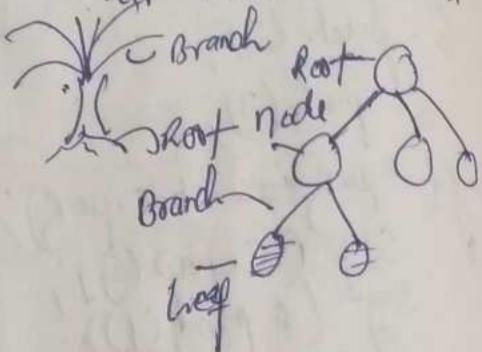
leaves of 2: 2

Subtree of 182: - (2, 4, 5, 7, 8) (3, 6, 9)

Ancestors of 8: { 4, 2, 1 }

Binary Tree

Hierarchical
Leaf Data structure



Build Tree Pre

node
left . right

Code of Bin

public class

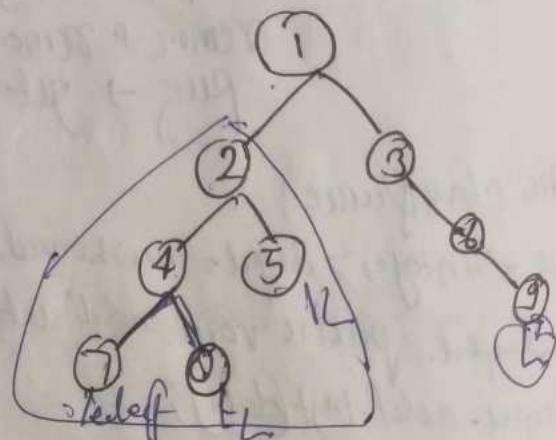
int
n
N

Node
this.
this.
this.
this.

9
y

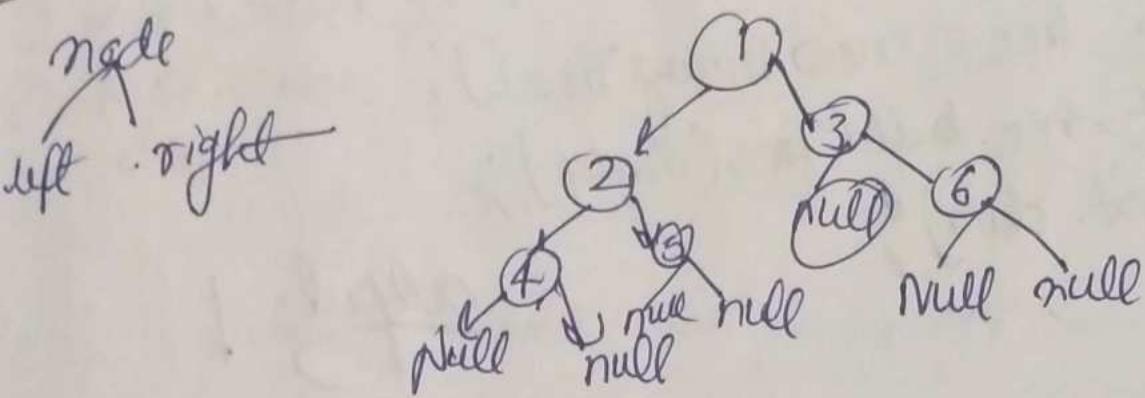
8 ta
public

if



If
pub

Build Tree Preorder - 1, 2, 4, -1, 5, -1, -1, 3, -1, 6, -1, -1



Code of Binary tree:-

```
public class BinaryTreeB {  
    static class nodes {  
        int data;  
        nodes left;  
        nodes right;  
        nodes (int data) {  
            this.data = data;  
            this.left = null;  
            this.right = null;  
        }  
    }  
}
```

```
static class Binary trees {  
    public static int idg = -1; tree (infnode, {
```

idg++;

if (nodes[idg] == -1){

return null;

}

Node newNode = new nodes (nodes[idg]);

newNode.left = buildTree (Node);

newNode.right = buildTree (node);

return newNode;

```
public static void main (String args[]) {
```

```
int node[] = {1, 2, 4, -1, -1, 5, -1, -1, 3, -1, 6, -1}
```

```
BinaryTree tree = new BinaryTree();
Node root = tree.buildTree(node);
System.out.println(root.data);
```

- ① left Subtree
- ② Right subtree
- ③ Root

output :

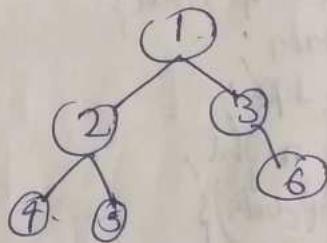
Code : public
part

T.C. O(n)

Tree Traversal

④ InOrder → In Between

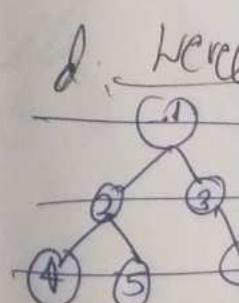
Rule :
① Left Subtree
② Root
③ Right Subtree



print: 4, 2, 5, 1, 3, 6

T.C. → O(n).

```
public static void inOrder(Node root) {
    if (root == null) return;
    inOrder(root.left);
    System.out.print(root.data + " ");
    inOrder(root.right);
}
```



public static void main(String args[]){}

```
int node[] = {1, 2, 4, -1, -1, 5, -1, -1, 3, -1, 6, -1, -1};
```

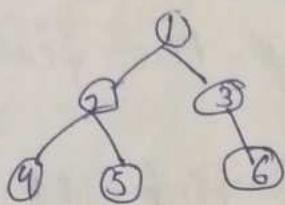
```
BinaryTree tree = new BinaryTree();
```

```
Node root = tree.buildTree(node);
```

tree.inOrder(root);

C. Postorder Reversals

- ① left Subtree
- ② Right subtree
- ③ Root



4 5 2 3 6 1
T.C $\Rightarrow O(n)$

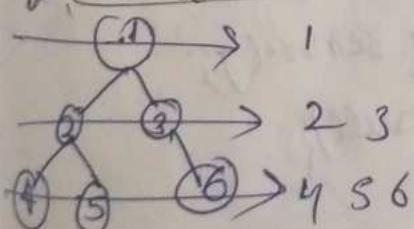
Code:

```
public static void postorder(Node root){  
    if(root == null) return;  
    postorder(root.left);  
    postorder(root.right);  
    System.out.print(root.data + " ");  
}
```

```
public static void main(String args[]){  
    int nodes[] = {1, 2, 4, -1, -1, 5, -1, -1, 3, -1, 6, -1, -1};  
    Binary Tree tree = new Binary Tree();  
    Node root = tree.buildTree(nodes);  
    tree.postorder(root);
```

Output:
4 5 2 3 6 1

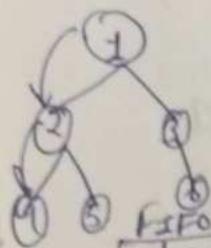
D. Level Order Reversal:-



Output:
4 5 6, 3 2, 1

Level order

DFS Depth First Search



FIFO

BFS: Breadth first search \rightarrow FIFO - Queue

1 2 3 4 5 6

1ⁿ
2 3ⁿ
4 5 6ⁿ

Time Complexity: $O(n)$.

Code:

1ⁿ
2 3ⁿ
F S 6ⁿ

// Level order Traversal
public static void levelorder (Node root){

if (root == null){
return;

Queue <Node> q = new linked list<>();
q.add(root);
q.add(null);

while (!q.isEmpty()) {

Node currNode = q.remove();

if (currNode == null){
System.out.print(" ");

if (q.isEmpty()){
break;
} else {

q.add(null);

else { System.out.print(currNode.data + " "); };

```

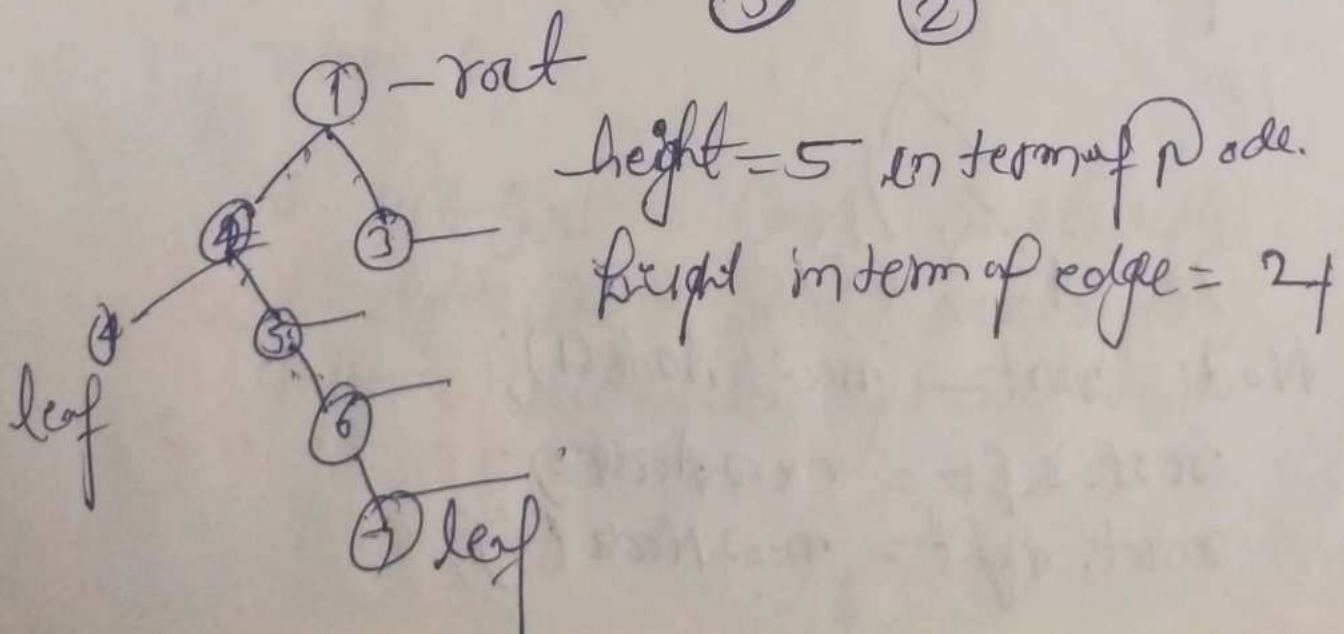
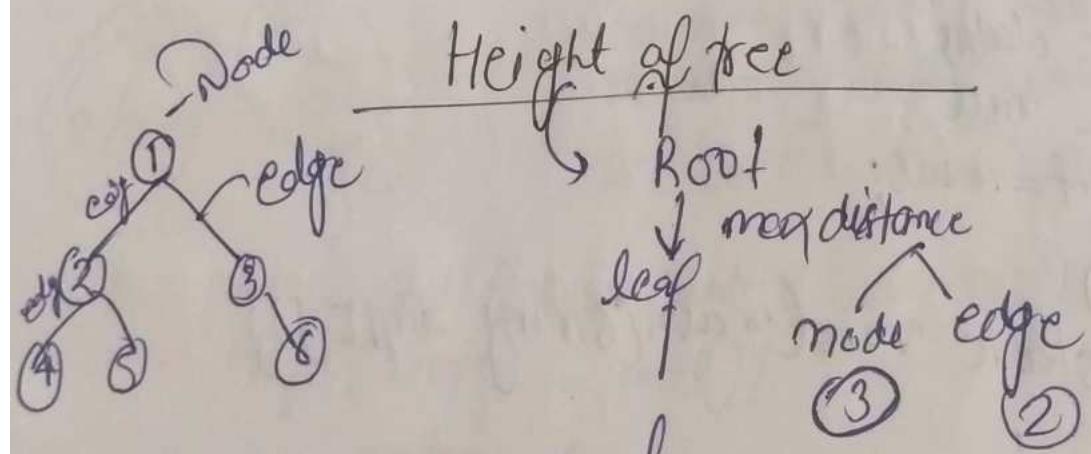
if (currNode.left != null){
    q.add(currNode.left);
}
if (currNode.right != null){
    q.add(currNode.right);
}
}

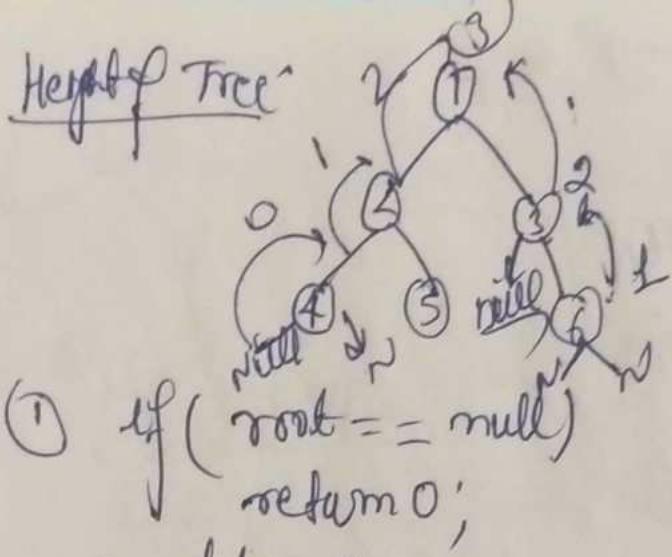
public static void main(String args[]){
    int nodes[] = {1, 2, 3, 4, -1, -1, 5, -1, -1};
    BinaryTreeNode tree = new BinaryTreeNode();
    Node root = tree.buildTree(nodes);
    tree.levelOrder(root);
}

```

Output:-

1
2 3
4 5 6





① if (
 root == null)
 return 0;

height = 3

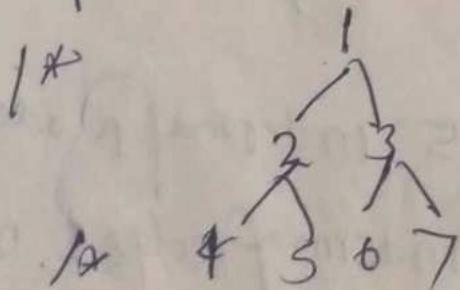
T.C = O(n)

$$\begin{aligned} \text{② } & lh = \text{height (root.left)} \\ & rh = \text{height (root.right)} \\ & \text{height} = \max + 1 \\ & \Rightarrow \max(lh, rh) + 1 \\ & \text{Height} = 3 \end{aligned}$$

```

public class classroom {
    static class node {
        int data;
        Node left, right;
    }
    public Node(int data) {
        this.data = data;
        this.left = null;
        this.right = null;
    }
}
  
```

①
public static void main(String args[]){



Node root = new Node(1);

root.left = new Node(2);

root.right = new Node(3);

```

root.left.left = new Node(4);
root.left.right = new Node(5);
root.right.left = new Node(6);
root.right.right = new Node(7);

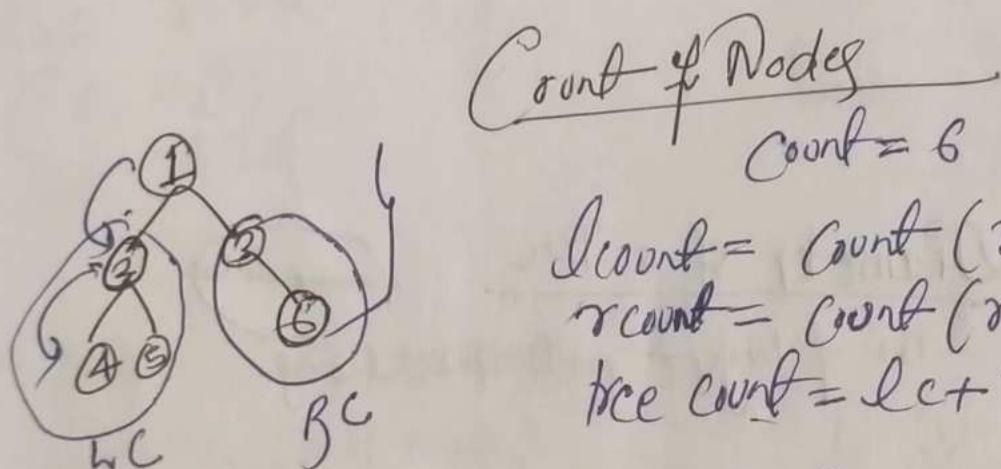
```

Q) ① public static int height (Node root) {

```

if (root == null) {
    return 0;
}
int lh = height (root.left);
int rh = height (root.right);
return Math.max (lh, rh) + 1;
}

```

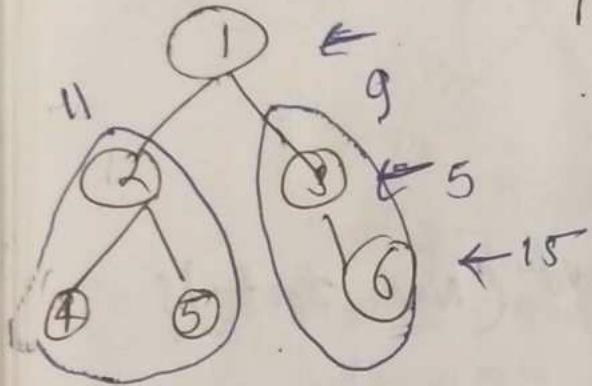


② public static int count (Node root) {

```

if (root == null) {
    return 0;
}
int leftCount = count (root.left);
int rightCount = count (root.right);
return leftCount + rightCount + 1;
}

```



Sum of Node

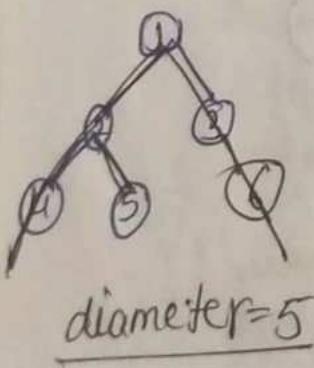
Sum of Node = 21

Recursively

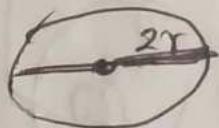
if (node == null)
return 0;

left sum = sum (root.left);
right sum = sum (root.right);

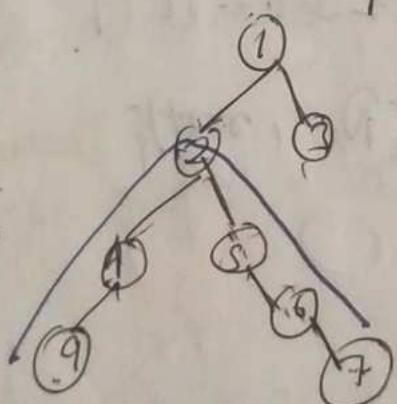
tree sum = ls + rs + root.data;



Diameter of a Tree



no. of longest path b/w 2 leaves

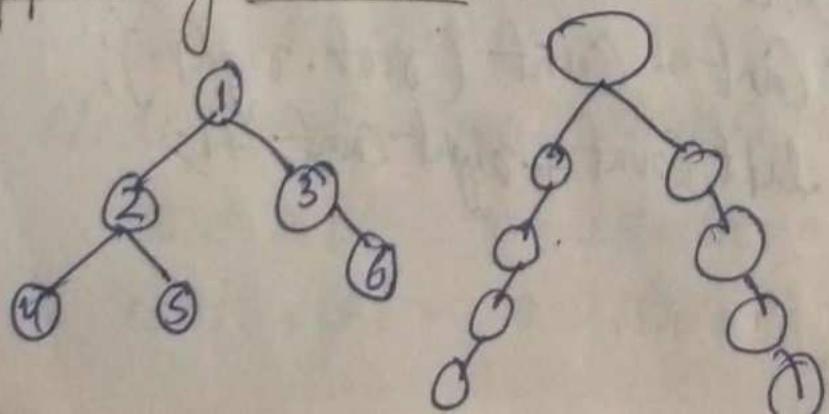


7 and 3 ≠ 6 = no. of nodes

9, 3 ≠ 5

9, 7 ≠ 6

Approach of a tree:-1:



4th 5th
left right

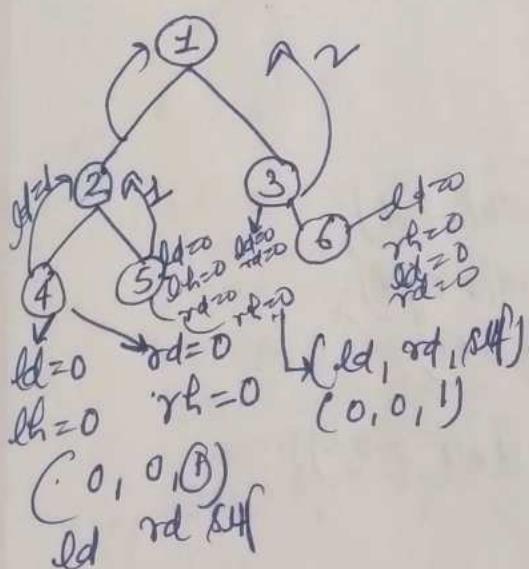
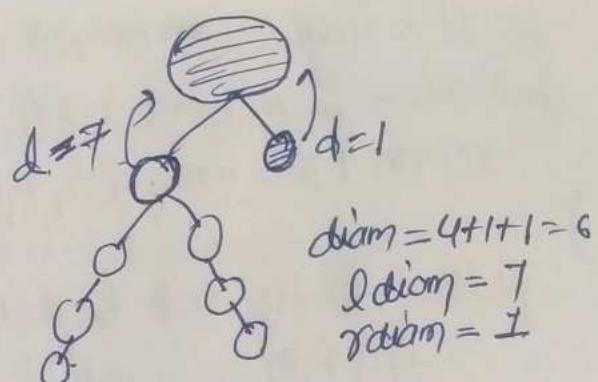
II diam pass through root

$$\text{diam} = lh + rh + 1$$

II diam does not pass

$$ldiam \checkmark$$

$$rdiam \checkmark$$



(ld rd self) ~~self = lh+rh+1~~

(0, 0, 1)

(1, 1, 3) ②. ldiam = diam(root.lf)

(0, 1, 2) ③. rdiam = diam(root.rf)

(3, 2, 5) • lh = height(root.left)

d=5 • rh = height(root.right)

① self diameter = lh + rh + 1

max(ldiam, rdiam, selfdiam)

if (root == null)
return 0;

➤ public class classroom {

 static class Node {

 int data;

 Node left, right;

 public Node (int data) {

 this.data = data;

 this.left = null;

 this.right = null;

 public static int height (Node root) {

 if (root == null) {

 return 0;

```
int lh = height(root.left);  
int rh = height(root.right);  
return Math.max(lh, rh) + 1;
```

```
}  
public static int height(Node root){  
    if (root == null){  
        return 0;  
    }
```

```
    int leftCount = count(root.left);  
    int rightCount = count(root.right);  
    return leftCount + rightCount + 1;
```

```
}  
public static int sum(Node root){  
    if (root == null){  
        return 0;  
    }
```

```
    int leftSum = sum(root.left);  
    int rightSum = sum(root.right);  
    return leftSum + rightSum + root.data;
```

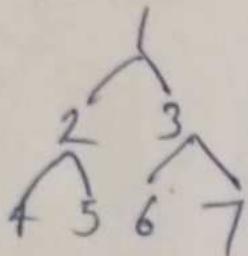
```
}  
public static int diameter(Node root){  
    if (root == null){  
        return 0;  
    }
```

```
    int leftDiam = diameter(root.left);  
    int leftHt = height(root.left);  
    int rightDiam = diameter(root.right);  
    int rightHt = height(root.right);
```

```
int selfDiam = leftHt + rightHt + 1;
```

```
Math.max(selfDiam, Math.max(leftDiam, rightDiam));
```

public static void main (String args[]){}



```

Node root = new Node(1);
root.left = new Node(2);
root.right = new Node(3);
root.left.left = new Node(4);
root.left.right = new Node(5);
root.right.left = new Node(6);
root.right.right = new Node(7);
  
```

Diameter Approach 2

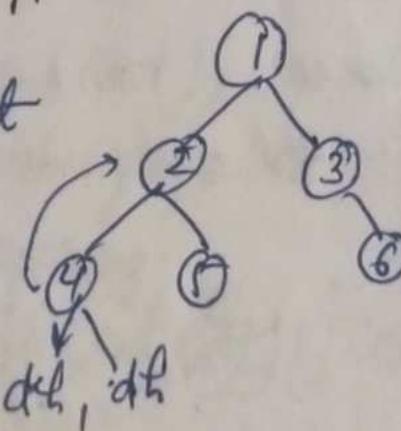
return (int) → diameter

return (Info) → diam, ht

leftD, lh

rd, rh

max (ld, rd, lh+rh+1)



height = max (lh, rh) + 1

Some functions are shared

```

class info {
    int diam
    int ht
}
  
```

Pre: (d,h) → lInfo = diam (root.left)

(d,h) & Info = diam (root.right)

Final Diam = max [lInfo.d, rInfo.d, diam]

$\text{finalHt} = \max(lh, rh) + 1$
return newInfo(Diam, ht)

Given
true
and

subm

④

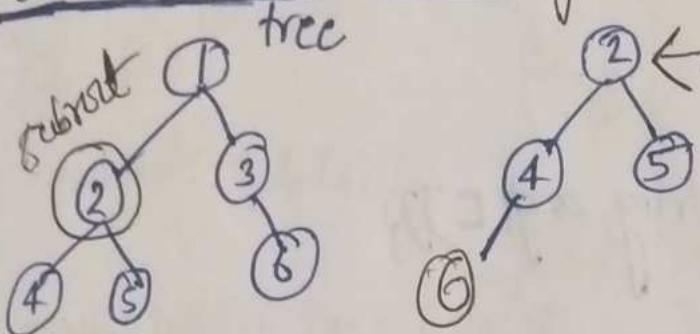
(P)

borders

b.

Subtree of another Tree

Given the root of two binary tree root and Subroot, return true, if there is a subtree of root with the same structure and node value of Subroot and false otherwise.



\Leftrightarrow subtree \rightarrow tree \rightarrow true
subtree $\not\rightarrow$ tree \rightarrow false

Q) root & 4 1 2 5 3 6 7 8 9 10
4 5 6

if (root == null){
 return false;

public static boolean isSubtree(Node root, Node subRoot){
 if (root.data == subRoot.data){
 if (isIdentical (root, subRoot))
 return true;
 }

① find Subroot in tree

② check identical

➤ traversal

root.data = subroot.data

Non Identical

① node.data = subroot.data

② node = null || subroot = null

③ left subtree \rightarrow non identical

④ right subtree \rightarrow non identical

return leftAny || rightAny;

return isSubtree (root.left, subRoot) || isSubtree (root.right, subRoot);

① public static boolean isIdentical (Node node, Node subRoot){
 if (node == null && subRoot == null){
 return true;

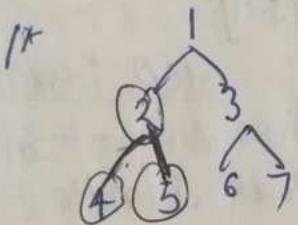
 else if (node == null || subRoot == null){
 return false;

 || node.data != subRoot.data

```
if (!isIdentical(node.left, subRoot.left)) {  
    return false;  
}
```

```
if (!isIdentical(node.right, subRoot.right)) {  
    return false;  
}  
return true;
```

```
public static void main (String args[]) {
```



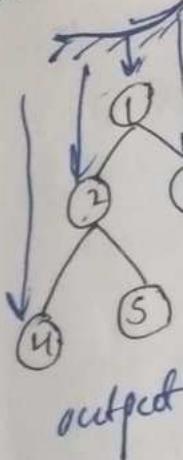
```
Node *root = new Node(1);  
root.left = new Node(2);  
root.right = new Node(3);  
root.left.left = new Node(4);  
root.left.right = new Node(5);  
root.right.left = new Node(6);  
root.right.right = new Node(7);
```



```
Node *subRoot = new Node(2);  
subRoot.left = new Node(4);  
subRoot.right = new Node(5);
```

```
So (isSubtree (root, subRoot));
```

}
g



Hash Ma

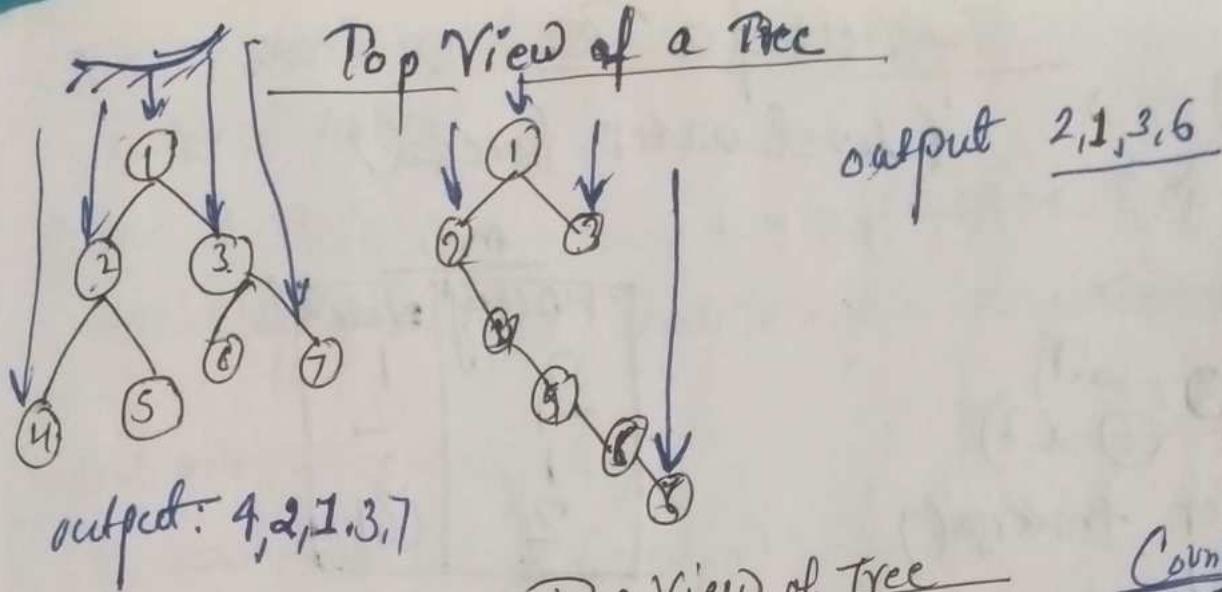
key =
value =
Syntax

① Create:
Add
remove
get

② Ad

> Hash

-- ③



Top View of Tree

HashMap in Java (Brief) map (key, value)

key = unique Value
value = Change के समी है।

| Country | Population |
|---------|------------|
| China | 125 |
| India | 100 |
| "US" | 50 |

Key

Syntax import java.util.*;

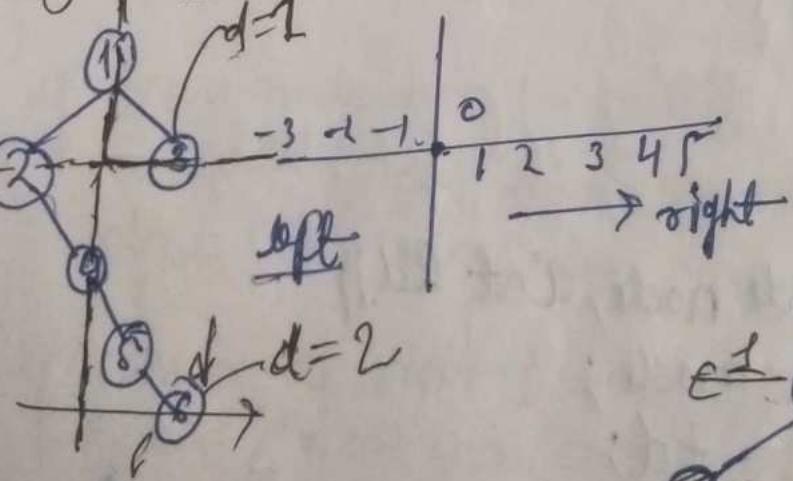
① Create: HashMap<String, Integer> map = new HashMap<>();

Add T.C O(1) { hashtable }
remove TC O(1) { hashing }
get TC O(1) { }

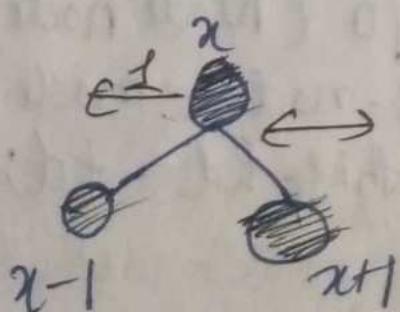
③ Get: —
map.get(key)

② Add: — (put)
map.put(key, value)
Ex map.put("India", 100)

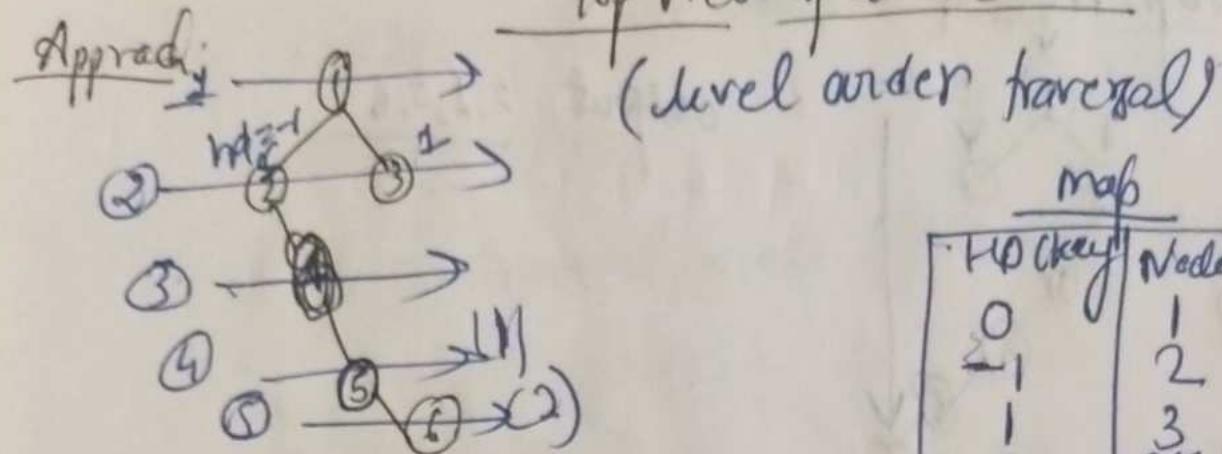
> Horizontal Distance:-



| HD | node |
|----|------|
| 0 | 1 |
| -1 | 2 |
| 1 | 3 |
| 0 | 4 |
| 2 | 6 |



$$\boxed{\text{Root HD} = 0}$$



| map | |
|----------|----------|
| Tree Key | Node Val |
| 0 | 1 |
| 1 | 2 |
| 2 | 3 |
| 3 | (6) |

① (level order traversal)

$$\min = 0 - 1$$

$$\max = 0, 1, 2 \quad \text{map.get}(0)$$

value

loop (from \min to \max) value

| | | | |
|----|---------------|-------------|---|
| -1 | \rightarrow | map.get(-1) | 2 |
| 0 | | | 1 |
| 1 | | | 3 |
| 2 | | | 6 |

Coding

```
import java.util.*;
static class info {
    Node node;
    int hd;
}
```

```
public static void topview(Node root) {
```

```
    static class Pinfo {
        Node node;
        int hd;
    }
```

```
    public Pinfo (Node node, int hd) {
```

```
        this.node = node;
```

```
        this.hd = hd;
```

```
public static void topview(Node root){
```

```
// level order
```

```
Queue<TInfo> q = new linkedlist<T>();
```

```
HashMap<Integer, Node> map = new HashMap<>();
```

```
int min = 0, max = 0;
```

```
q.add(new TInfo(root, 0));
```

```
q.add(null);
```

```
while (!q.isEmpty()) {
```

```
TInfo cur = q.remove();
```

```
if (cur == null) {
```

```
if (q.isEmpty())
```

```
break;
```

```
else {
```

```
q.add(null);
```

```
if
```

```
(cur.hd)
```

```
if (map.containsKey(key)) { // true
```

```
// first time my hd is occurring
```

```
map.put(cur.hd, cur.node);
```

```
if
```

```
(cur.node.left != null) {
```

```
q.add(new TInfo(cur.node.left, cur.hd - 1));
```

```
min = Math.min(min, cur.hd - 1);
```

```
if (cur.node.right != null) {
```

```
q.add(new TInfo(cur.node.right, cur.hd + 1));
```

```
max = Math.max(max, cur.hd + 1);
```

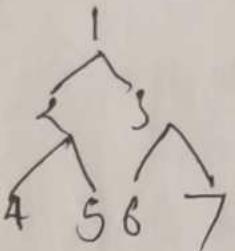
```
for (int i=min; i<=max; i++) {
```

```
    say (map.get(i).data); //
```

```
} say();
```

```
public static void main(String args) {
```

```
/*
```



```
*:.
```

```
Node root = new Node(1);
```

```
root.left = new Node(2);
```

```
root.right = new Node(3);
```

```
root.left.right = new Node(4);
```

```
root.left.left = new Node(5);
```

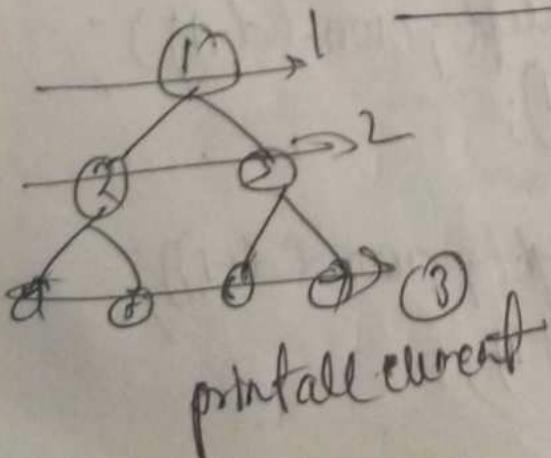
```
root.right.left = new Node(6);
```

```
root.right.right = new Node(7);
```

```
} topview(root);
```

output: 4, 2, 3, 7

Kth level of a tree



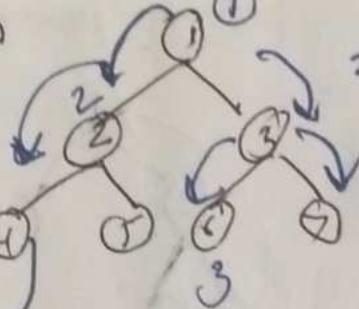
K=3
output = 4 5 6 7

print all elements

Level order Reversal

② Recursive way

Approach



Reorder

9 5 6 7

Pseudo Code

K level (root, level, K)

if (level == K){

 print (root.data)

} K level (root.left, level+1, K)

K level (root.right, level+1, K)

T.C = O(N)

Code public static void K level (Node root, int level, int K){

 if (root == null){

 return;

} if (level == K){

 System.out.print (root.data + " ");

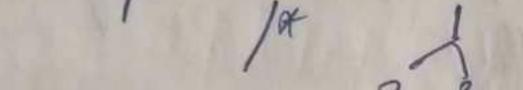
} return;

} K level (root.left, level+1, K);

} K level (root.right, level+1, K);

public static void main (String args){

/*



Node root = new Node (1);

root.left = new Node (2);

root.right = new Node (3);

root.left.left = new Node (4);

root.left.right = new Node (5);

root.right.left = new Node (6);

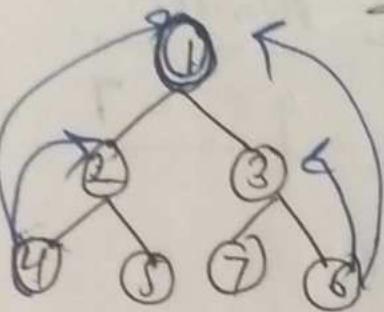
root.right.right = new Node (7);

Output - 2, 3

int i = 2

} K level (root, i, r)

Lowest Common Ancestor



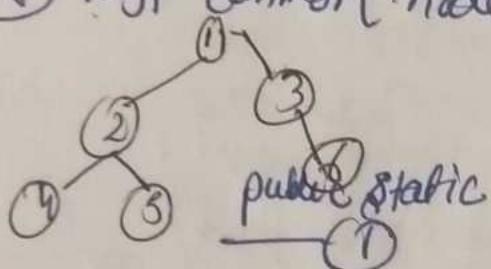
$n_1 = 4 \quad n_2 = 6$

LCA = 1

$n_1 = 4 \quad n_2 = 5$

① Root

② Last common node \rightarrow LCA



Code:

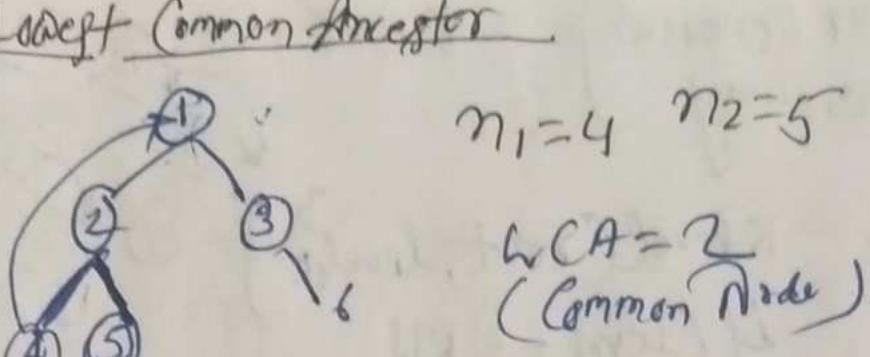
```
public static Node LCA(Node root, int n1, int n2) {
    ArrayList<Integer> path1 = new ArrayList<Integer>();
    ArrayList<Integer> path2 = new ArrayList<Integer>();
    getpath(root, n1, path1);
    getpath(root, n2, path2);
    // last common ancestor
}
```

int i=0

```
for(; i < path1.size() && path2.size(); i++)
```

```
if(path1.get(i) != path2.get(i))
    break;
```

```
// last equal node > i-1th
Node lca = path1.get(i-1);
```



$n_1 = 4 \quad n_2 = 5$

LCA = 2
(Common Node)

Approach

Path 1 (n_1) = [1 | 2 | 4]

Path 2 (n_2) = [1 | 3 | 6]

Path 1 = [1 | 2 | 4]

Path 2 = [1 | 3 | 5]

LCA = 1

LCA = 2

Step ① Root to Node

getpath(root, nodeA, path1)

[1 | 2 | 5]

② Loop ($i=0$ to path.length)

[1 | 2 | 5]

path2.length)

(last common ancestor)

ArrayList<Integer> path2 = new ArrayList<Integer>();

ArrayList<Integer> path1 = new ArrayList<Integer>();

getpath(root, n1, path1);

getpath(root, n2, path2);

if(path1.get(i) != path2.get(i))

break;

if(last equal node > i-1th)

```

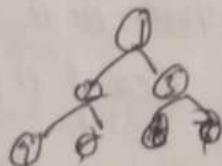
① public static boolean getPath(Node root, int n, ArrayList<Node> path)
    path.add(root);
    if (root.data == n) {
        return true;
    }
    boolean foundLeft = getPath(root.left, n, path);
    boolean foundRight = getPath(root.right, n, path);
    if (foundLeft || foundRight) {
        return true;
    }
    path.remove(path.size() - 1);
    return false;
}

```

```

public static void main(String[] args) {
}

```



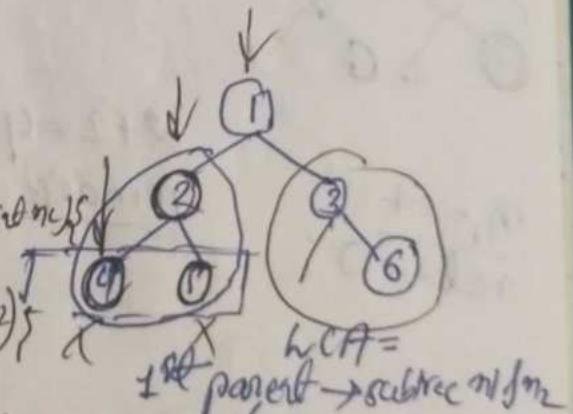
int $n_1 = 4$, $n_2 = 5$
 System.out.println(root.n1 + " " + n2 + " " + data);

How to get Ancestor & Approach 2

```

public static Node lca2(Node root, int n1, int n2) {
    if (root.data == n1 || root.data == n2) {
        return root;
    }
    Node leftLca = lca2(root.left, n1, n2).ancestor;
    Node rightLca = lca2(root.right, n1, n2).ancestor;
    if (rightLca == null) {
        return leftLca;
    }
    if (leftLca == null) {
        return rightLca;
    }
    return root;
}

```



```
public static void main (String Ar[]) {
```

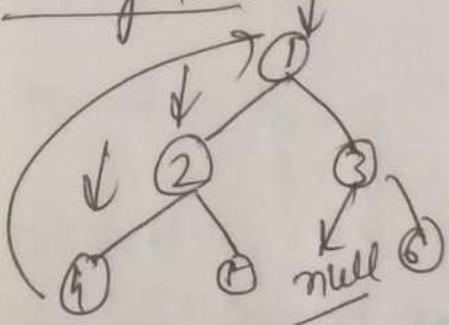
```
    int n1 = 4, n2 = 7;
```

```
    boy ( lca ( root, n1, n2 ). data );
```

```
    n1 = 4 n2 = 6
```

Condition (1) $\text{root} = \text{null}$
 $\text{root} = n_1$ $\text{root} = n_2$

Dry Run:-



left LCA
right LCA.

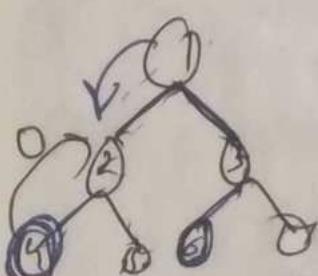
(2) right LCA = null \rightarrow left LCA

left LCA = null \rightarrow right LCA

right & left = null \rightarrow return root

Minimum Distance between Node

n_1



$n_1 = 4 \quad n_2 = 6$

$\text{dist} = 4$ (node) (edge)

LCA of n_1, n_2

Approach 1 $\text{dist} 1$ LCA to n_1

Approach 2 LCA to n_2

$\text{dist} 1 + \text{dist} 2 = \min. \text{dist}$ n_1, n_2

$n_1 = 4$
return 0;

$2+2=4$
mindist = 4

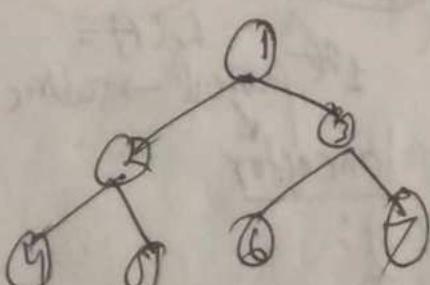
if ($\text{root}. \text{data} = n_1$)
 return 1

if ($\text{root}. \text{data} = n_2$)
 return 0.

left n search
right n search

-1, -1, \rightarrow -1

Valid (>-1) \rightarrow Valid + 1



```

public static Node Lca(Node root, int n1, int n2){
    if (root == null || root.data == n1 || root.data == n2)
        return root;
    Node leftLca = Lca(root.left, n1, n2);
    Node rightLca = Lca(root.right, n1, n2);
    if (leftLca == null)
        return rightLca;
    if (rightLca == null)
        return root;
    public static int Lcadist(Node root, int n){
        if (root == null)
            return -1;
        if (root.data == n)
            return 0;
        int leftDist = Lcadist(root.left, n);
        int rightDist = Lcadist(root.right, n);
        if (leftDist == -1 & rightDist == -1)
            return -1;
        else if (leftDist == -1)
            return rightDist + 1;
        else
            return leftDist + 1;
    }
}

```

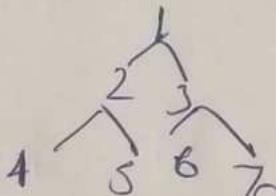
```

public static int minDist(Node root, int n1, int n2)
{
    Node lca = LCA(root, n1, n2);
    int dist1 = CA_Dist(lca, n1);
    int dist2 = lcaDist(lca, n2);
    return dist1 + dist2;
}

```

```
public static void main(String args){}
```

/*



```

Node root = new Node(1);
root.left = new Node(2);
root.right = new Node(3);
root.left.left = new Node(4);
root.left.right = new Node(5);
root.right.left = new Node(6);
root.right.right = new Node(7);
int n1 = 4, n2 = 6;

```

```

System.out.println(minDist(root, n1, n2));
}

```

node = 5 k = 2

ans = 1

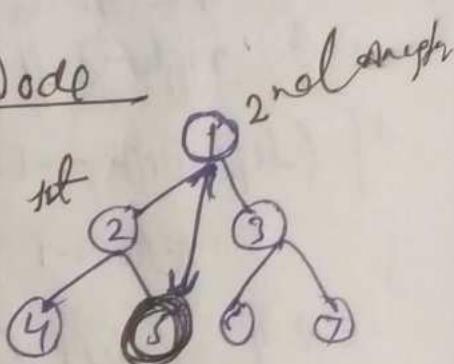
Approach:-

- ① find my node
- ② if (root.data == node)
return 0.

left Dist

right Dist

Valid Value \rightarrow $(dist + 1) == k$ print root.data



```

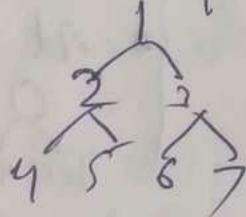
public static int kAncestor(Node root, int n, int k) {
    if (root.data == n) { → If (root == null) {
        return 0;           return -1;
    }
    int leftDist = kAncestor(root.left, n, k);
    int rightDist = kAncestor(root.right, n, k);
    if ((if leftDist == -1 && rightDist == -1) {
        return -1;
    }
    int max = Math.max(leftDist, rightDist);
    if (max + 1 == k) {
        say(root.data);
    }
    return max + 1;
}

```

```

public static void main (String args[]) {
    int

```



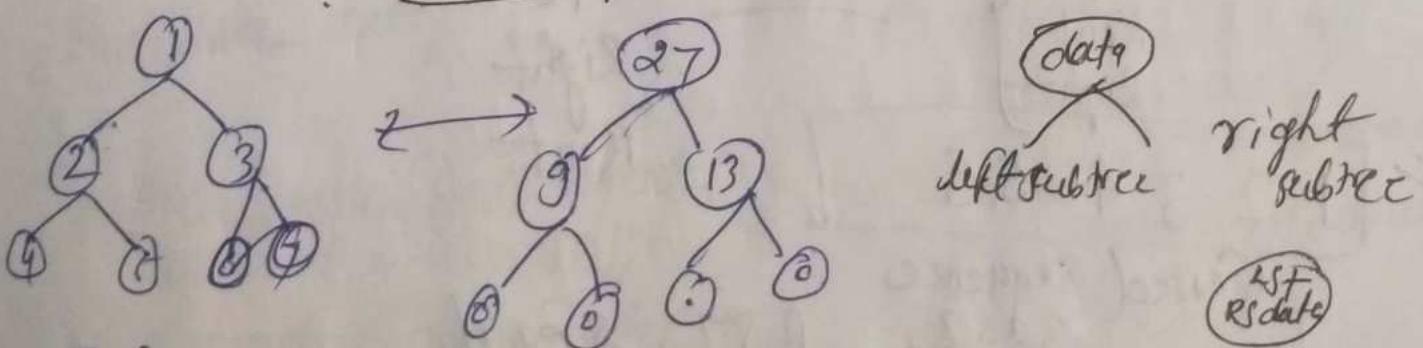
output = 2

```

    int n = 5, K = 2;
    kAncestor (root, K, n);
}

```

31.6 Transform to Sum Tree



Each node = sum of left & right subtree

Approach

left subtree sum =

right subtree sum =

data = root.data

root.data = lsum + RS

return data;

if (root == null)

return 0

leftchild = transform (root.left)

rightchild = transform (root.right)

data = root.data

root.data = root.left +
child + root.right

right child

return data;

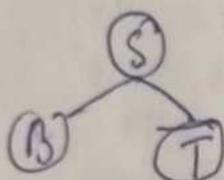
32.1

Binary Search Tree (BST)

* fast looks up.

$O(N)$ no. of nodes

$O(H)$ height

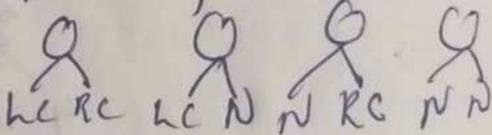


what is a BST?

- (A) left subtree Node < Root
- (B) Right Subtree Node > Root +
- (C) Left & Right Subtree are also BST with no duplicates.

Binary Tree

- At max 2 children



Preorder → Root
left
Right

* Inorder → left (Root Right)

Postorder Root

Right
Root

~~1 2 3 4 5 6~~

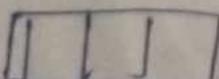
Sorted Sequence

32.2 BST

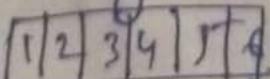
Search

key = 3

linear



Binary

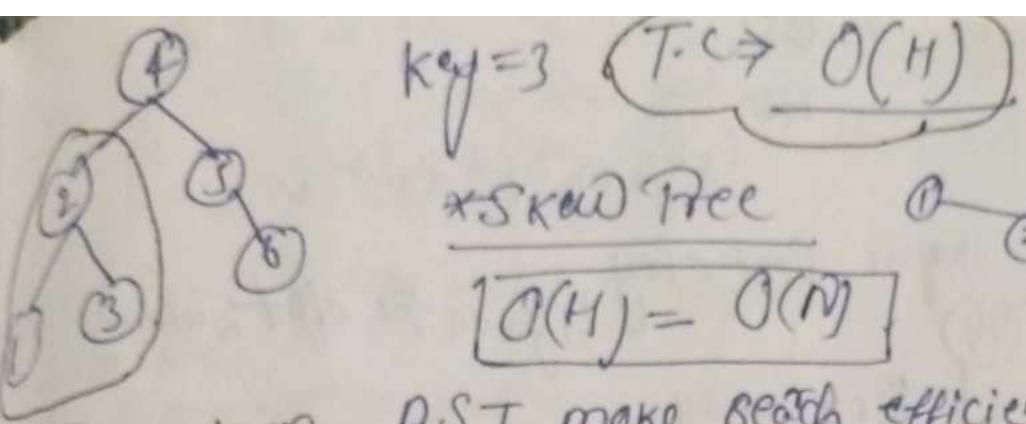


key = 6 key > data → go right

key > data → go left

key = 6 = data

return data



To remember: BST make search efficient

Strategy: Most problem will be solved using recursion i.e. by dividing into subproblem & making recursive call on subtree.

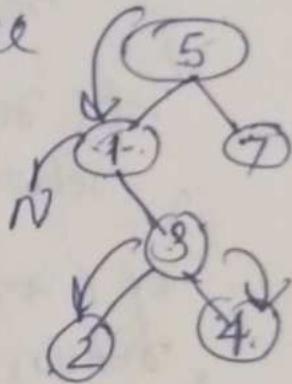
32.3 Build a BST

Value[] = {5, 1, 3, 4, 2, 7} Root = null

1 2 3 4 5 7

value [i] > root \rightarrow Right Subtree

value [i] < root \rightarrow Left Subtree



Code:

```
public class BST {
    static class node {
        int data;
        Node left;
        Node right;
        Node (int data) {
            this.data = data;
        }
    }
}
```

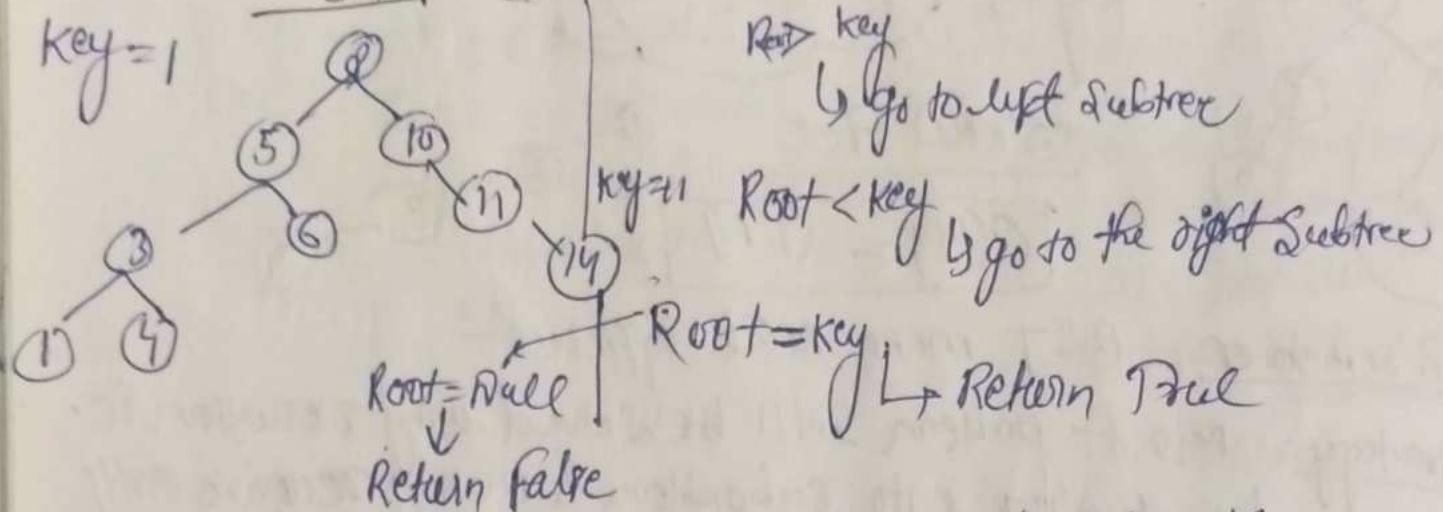
```
public static Node insert() {
    if (root == null) {
        root = new Node(val);
        return root;
    }
    if (root.data > val) {
        if (left < val)
            left = insert (root.left, val);
        else
            right = insert (root.right, val);
    }
}
```

```
else { // right subtree
    root.right = insert (root.right, val);
}
return root;
}

public static void main(String[])
{
    int value[] = {5, 1, 3, 4, 2, 7};
    Node root = null;
    for (int i=0; i<value.length; i++)
        root = insert (root, value[i]);
}
```

32.4

Search a BST



Code public static boolean search (Node root, int key) {

```
if (root == null){  
    return false;  
}  
if (root.data == key){  
    return true;  
}  
if (root.data >= key){  
    return search (root.left, key);  
}  
else {  
    return search (root.right, key);  
}
```

public static void main (String args[]){
int value [] = {5, 1, 3, 4, 2, 7};

```
Node root = null;  
for (int i = 0; i < value.length; i++){  
    root = insert (root, value [i]);  
}
```

inorder (root);
System.out.println();

```
if (search (root, 1)){  
    System.out.println ("Found");  
}  
else {  
    System.out.println ("Not Found");  
}
```

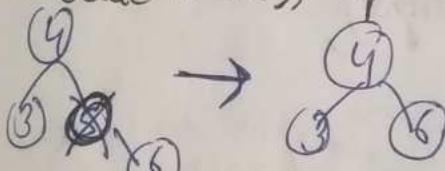
Output: Found

32.5 Delete a Node

- Case 1 No child (Leaf Node)
- ② One child (10, 11)
 - ③ Two children (3, 8, 5)

Case 2 No child (Leaf Node) Key = 4
 Delete Node
 & Return Null to parent

Case 2 One child
 Delete Node & replace with child node



Case 3 Two children
 • Replace value with inorder successor
 • Delete the node for inorder successor

Inorder successor in BST \rightarrow left most node

• In order successor always \in Right subtree
 for 1 child.

Approach ① Find in order success
 ② Node off value replace
 ③ Delete off

public static Node delete (Node root, int val){

if (root.data < val){

 root.right = delete (root.right, val);

 else if (root.data > val){

 root.left = delete (root.left, val);

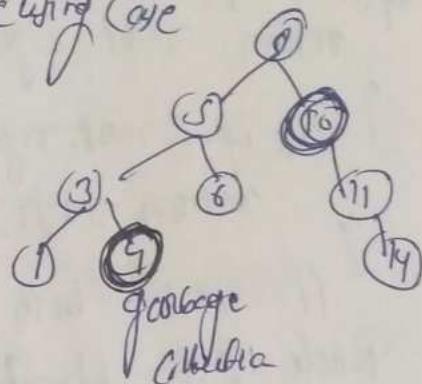
 else {
 // Voilà Case 1

 // Case 2 - Leaf node

 if (root.left == null, & if root.right == null){}

 return null;

- ① search
- ② Delete using Case



13 4 6 D

13 4 6 D -

|| Case 2 - Single Child

If (root.left == null) {
 return root.right;

} else if (root.right == null) {
 return root.left;

|| Case 3 - both children

Node DS = findInorderSuccessor(root.right);

root.data = DS.data;

root.right = delete(root.right, DS.data);

return root;

public static Node findInorderSuccessor(Node root) {

while (root.left != null)

root = root.left;

return root;

public static void main (String args[]) {

int values[] = {1, 5, 3, 4, 6, 10, 11, 14};

Node root = null;

for (int i=0; i < values.length; i++) {

root = insert(root, values[i]);

inorder(root);

System.out.println();

root = delete(root, 1);

System.out.println();

inorder(root);

} }

32.6 Point in Range

$K_1 = 5 \quad K_2 = 12$
 $5, 6, 8, 10, 11$

~~gatf~~ \leftarrow

case 1 $K_1 \leq \text{root} \leq K_2$ $C_3 \Rightarrow \text{root} < K_1$
 $\hookrightarrow \text{left search (left Subtree)}$

case 2 $\text{root} > K_2$

$\hookrightarrow \text{RS}$

$\hookrightarrow \text{LS}$



```
Code public static void pointInRange (Node root, int K1, int K2) {
    if (root.data >= K1 && root.data <= K2) {
        printInRange (root.left, K1, K2);
        say (root.data + " ");
        printInRange (root.right, K1, K2);
    } else if (root.data < K2) {
        printInRange (root.left, K1, K2);
    } else {
        printInRange (root.right, K1, K2);
    }
}
```

```
public static void main (String args[]) {
    int value [] = {8, 9, 3, 1, 4, 6, 10, 11, 14};
    Node root = null;
    for (int i=0; i<value.length; i++) {
        root = insert (root, value[i]);
    }
}
```

inorder (root);

say ();

printInRange (root, 5, 12);

ggy

output

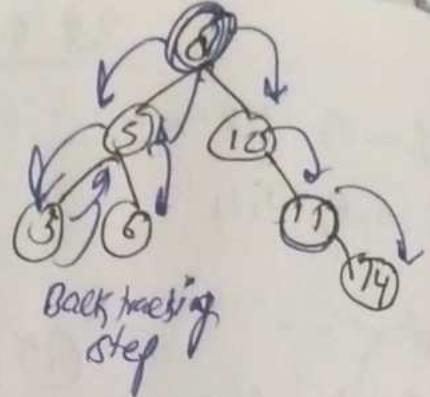
5, 6, 8, 10, 11

3d.7 Root to Leaf Path

Any left \rightarrow path

| | | | | |
|---|---|---|---|--|
| 8 | 5 | 3 | 1 | |
|---|---|---|---|--|

$$\begin{array}{l} P_1 \\ P_2 \\ P_3 \end{array} \left\{ \begin{array}{l} 8-5-2 \\ 8-5-6 \\ 8-10-11=14 \end{array} \right.$$



- ① Add (Node) to path
- ② Left Subtree
- ③ Leaf \rightarrow print path, Back Care
Right Subtree

Preorder Reversal

Code: public static void printRoot2leaf(Node root, AnyList<int> path)

```
path.add(root.data);
if (root == null)
    return;
printRoot2leaf (root.left, path);
printRoot2leaf (root.right, path);
path.remove(path.size() - 1);
```

public static void main (String args[]) {
 int values[] = {8, 5, 3, 1, 4, 6, 10, 11, 14};

Node root = null;

```
for (int i=0; i < values.length; i++) {
    root = insert (root, value(i));
}
```

inorder (root);

System.out.println();

```
printRoot2leaf (root, new AnyList<int>());
```

Approach

32.8 Validate BST

Compare with left & right

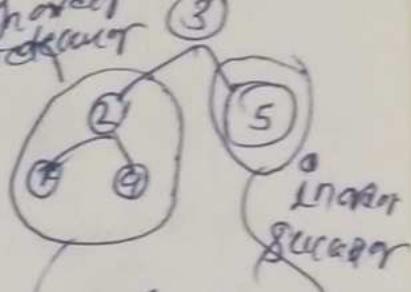


Approach Check if max value in left subtree $<$ node
and min value in right Subtree $>$ node

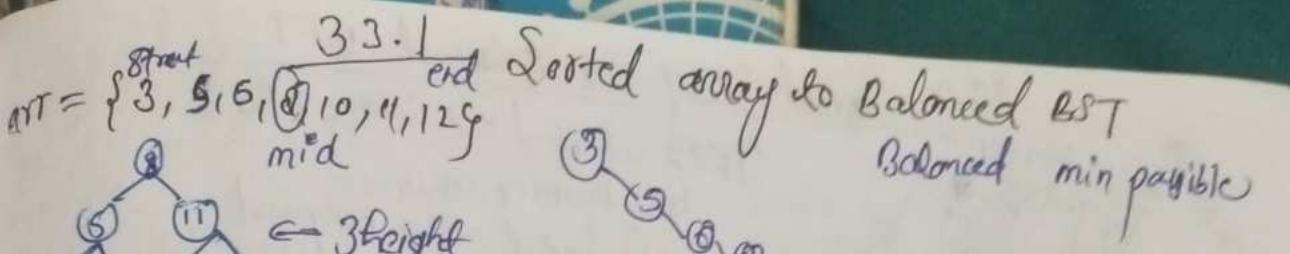
Inorder Traversal

Sorted

inorder predecessor



$[\infty < value < 5 \text{ and } 5 < value]$



Approach BST Inorder sequence

Sorted
left subtree + Current node + Right subtree

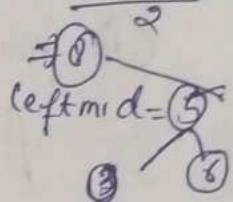
$arr = \{3, 5, 6, 8, 10, 11, 12\}$

mid = $\frac{\text{start} + \text{end}}{2}$

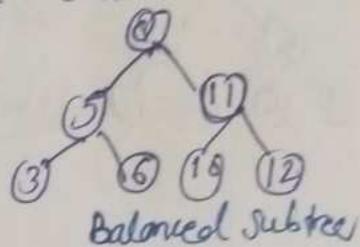
def CreateBST(arr, st, end)
if ($st > end$)
return null

if $mid = (\text{start} + \text{end})/2$

Node root = new Node(arr[mid])
root.left = CreateBST(arr, start, mid-1);
root.right = CreateBST(arr, mid+1, end);
return root;



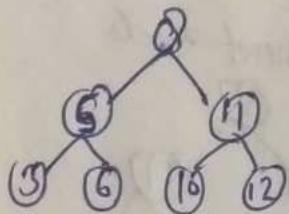
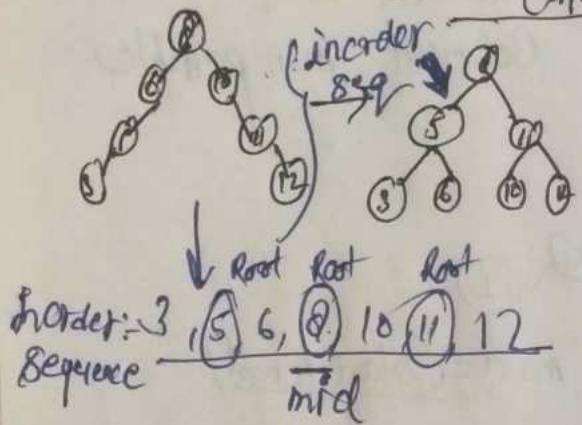
mid = $\frac{\text{start} + \text{end}}{2}$
mid = current node



$T.C = O(n)$.

Linear

33.2 Convert BST to Balanced BST



Approach Sorted \rightarrow Balanced BST

- ① Inorder sequence
- ② Sorted arr \rightarrow balanced BST

Code public static Node balanceBT(Node root,
// Inorder seq

ArrayList<Integer> inorder = new ArrayList<

getInorder(root, inorder);

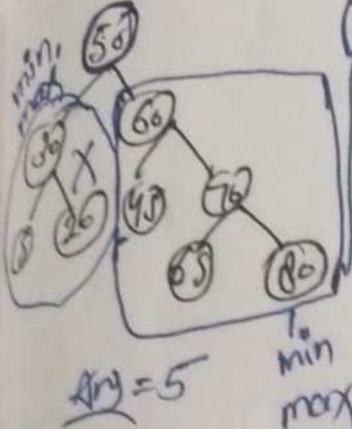
① public static void getInorder(Node root, ArrayList<Integer> inOrder){
if (root == null);
, return

getInorder(root.left, inOrder);

inOrder.add(root.data);

getInorder(root.right, inOrder);

33.3 size of largest BST in BT



Approach:

- ① is BST (bool)
- ② size
- ③ min
- ④ max

$$\min = 45$$

$$\max = 50$$

B-T if valid BST

$$\text{root} == \text{null} \rightarrow \text{True}$$

min \rightarrow min possible value

max \rightarrow max possible value

$$\text{root} < \max(\text{left}) \quad \text{if} (\text{not} > \min(\text{right}))$$

False.

$\text{root}.data > \text{left} \& \text{root}.data < \text{right}$

True {
 1. $\text{isBST} = \text{true}$
 2. $\text{size} = 0$
 3. $\min = +\infty$
 4. $\max = -\infty$

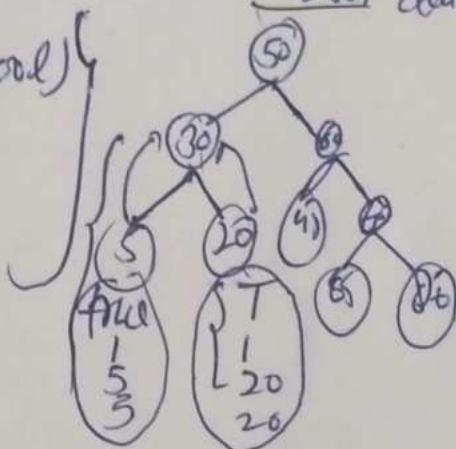
if invalid BST

$\rightarrow \text{Root} = \text{null}$

$\left\{ \begin{array}{l} \text{left max} > \text{root} \\ \text{right min} < \text{root} \end{array} \right\} \text{False} = \text{isBST}$

$$\text{size} = \text{left} + \text{right} + 1$$

$$\min = \min(\text{root}.data, \text{left min}, \text{right min})$$



left info
right info

self info
max size

Graph

- Introduction to graph
- Graph Terminology
- Graph Implementation
- Graph Traversal
- Weighted And Directed graph
- Minimum Spanning tree
- Cycle detection in graph
- Kruskal Algorithm
- Prim algorithm
- Dijkstra algorithm
- Bellman Ford Algorithm & Potof Question

- Graph
Example

Edge
①

* Q
➤ Def

Dynamic Tree

- Segment Tree
 - what are segment tree
 - Creation of segment tree
 - Solving range Query

A
Y
A
A
A

• hiyo

{ }

Graph

- Introduction to graph
- Graph Terminology
- Graph Implementation
- Graph Traversal
- Weighted And Directed graph
- Minimum Spanning tree
- Cycle detection in graph
- Kruskal Algorithm
- Prim algorithm
- Dijkstra algorithm
- Belman Ford Algorithm & Potof Question

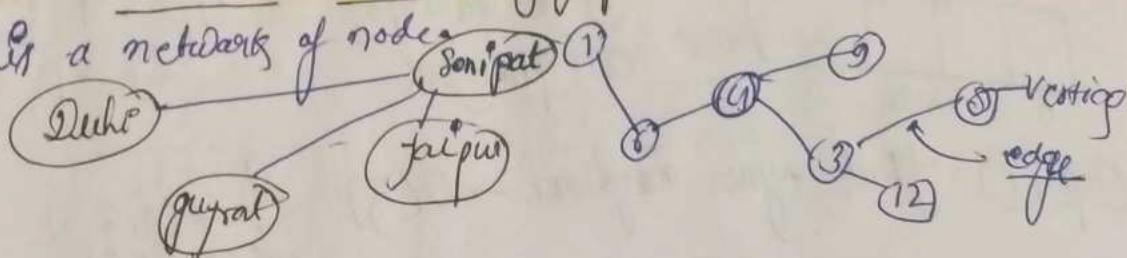
Dynamic Tree

- Segment Tree
 - what are segment tree
 - Creation of segment tree
 - Solving range query

37.1 Introduction of graph

Graph is a networks of nodes

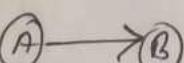
Example



37.2 Types of graph

Edge

① Uni-Directional

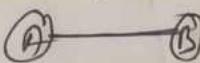


* Directed graph

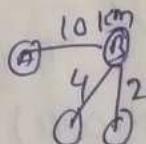
Weight: property Associate

10

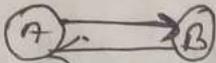
② Bi-Directional



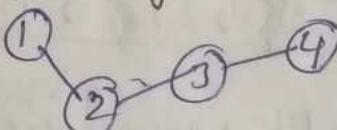
[Undirected graph]



③ Bi-directional



④ Non Weighted



37.3 Storing a Graph

→ Structure

Representation

Ex: weight

Adjacency List

Adjacency Matrix

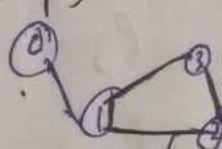
Edge List

2D matrix (Implicit graph)

Adjacency List:-

list of list

$\left\{ \begin{array}{l} \text{list } 0 \rightarrow (1) \\ \text{list } 1 \rightarrow (0, 2, 3) \\ \text{list } 2 \rightarrow (1, 3) \\ \text{list } 3 \rightarrow (1, 2) \end{array} \right.$



$V = 4$ / undirected graph

$E = 4$ / unweighted graph

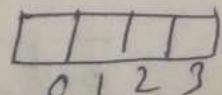
Cycle detection

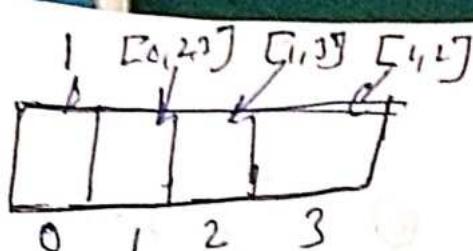
→ ArrayList < ArrayList >

ArrayList < ArrayList >

HashMaps < int, List >

vertex value
(key)





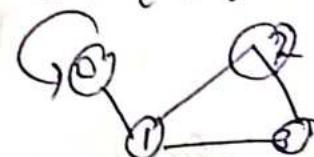
- ① extra info
- ② optimized

Vertices = 4
E = 4
undirected
unweighted

Step ① find your neighbour $\rightarrow O(5)$

Array of A maylist

$0 \rightarrow 1$
 $1 \rightarrow (0, 2, 3)$
 $2 \rightarrow (1, 3)$
 $3 \rightarrow (1, 2)$



② Adjacency matrix

| 0 | 1 | 2 | 3 | |
|---|---|---|---|---|
| 0 | 0 | 1 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 |
| 2 | 0 | 1 | 0 | 1 |
| 3 | 0 | 1 | 1 | 0 |

$V=4$
 $E=4$

$(i, j) \rightarrow$
 $i - \text{src.}$
 $j - \text{dest.}$
 $i-j \rightarrow \text{edge}$

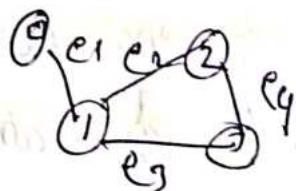
$V=4$
 $\frac{\partial V}{\partial}$

$(2-1) \rightarrow \text{edge } e_4 \Rightarrow 1$
 $(3-3) \rightarrow \text{No edge} \Rightarrow 0$

Edge List

Edge = $\{ \{0, 1\}, \{1, 2\}, \{1, 3\}, \{2, 3\} \}$

$e_1 = \{0, 1\}$
 $e_2 = \{1, 2\}$
 $e_3 = \{1, 3\}$
 $e_4 = \{2, 3\}$



{ Edge list sorting }
{ minimum spanning tree (MST) }

Implicit Graph

| | | | |
|-------|--|--|--|
| (0,0) | | | |
| | | | |
| | | | |

(i, j)
 $(i-f+1, j)$
 $(i, f+1, j)$
 $(i, j+1)$

Floyd
Floyd's
Algorithm
2D matrix

Application of graph

① Maps (shortest path)



⑥ Social Network

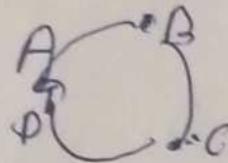
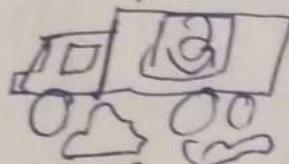
[in]

[f]

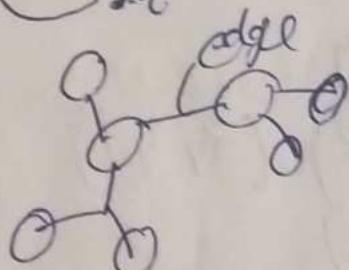
[X]

friend

② Delivery Networks (Shortest Path Route)



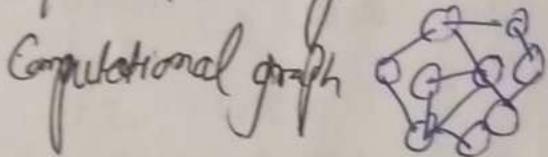
③ Physics & Chemistry



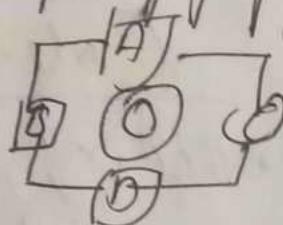
④ Routing Algorithm



⑤ Machine Learning:

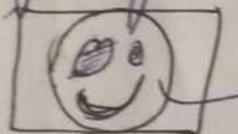


⑥ Dependency Graph



⑦ Computer Vision

• Image segmentation AI/ML

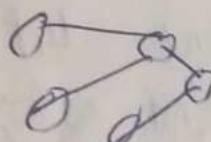


Flood fill algorithm

(called Euler tour and Color fill algorithm)

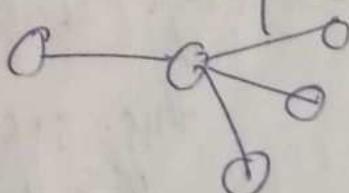
⑧ Graph Database

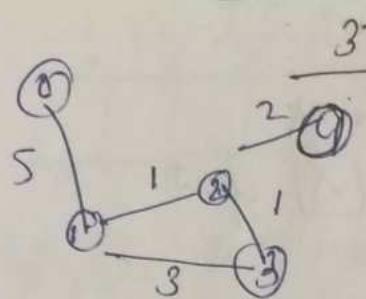
Nebula
neo4j



{ Fraud
Detection

⑨ Research:- Pearson (human)





37.5 Creating a graph (Adjacency list)

ArrayList<Edge> graph

Edge = (src, dest, weight)

(2, 4, 2)

(4, 2, 2)

0 → {2, 1, 5}

1 → {1, 0, 5}

2 → {1, 2, 1} {1, 3, 2}

2 → {2, 1, 1} {2, 4, 2} (2, 3, 1)

3 → {3, 1, 3} (3, 2, 1)

4 → {4, 1, 2}

Code.

```
import java.util.*;
```

```
public class classout {
    static class Edge {

```

```
        int src;

```

```
        int dest;

```

```
        int wt;

```

```
        public Edge (int s, int d, int w) {

```

```
            this.src = s;

```

```
            this.dest = d;

```

```
            this.wt = w;

```

g
g

```
public static void main (String args [ ] ) {  
    /* 0 (S) 1  
     * | (1) | (3)  
     * | (2) | (4) 3  
     */  
}
```

int v = 5

```
ArrayList < Edge > [ ] graph = new ArrayList [v]; // null
```

```
for (int i = 0; i < v; i++) {
```

```
    graph [i] = new ArrayList < > ();
```

// 0 - vertex

```
graph [0].add (new Edge (s: 0, d: 1, w: 5));
```

// 1 vertex

```
graph [1].add (new Edge (s: 1, d: 2, w: 2));
```

```
graph [1].add (new Edge (s: 1, d: 2, w: 1));
```

```
graph [1].add (new Edge (s: 1, d: 3, w: 3));
```

// vertex 2.

```
graph [2].add (new Edge (s: 2, d: 1, w: 1));
```

```
graph [2].add (new Edge (s: 2, d: 3, w: 1));
```

```
graph [2].add (new Edge (s: 2, d: 4, w: 1));
```

// 3 vertex

```
graph [3].add (new Edge (s: 3, d: 1, w: 3));
```

```
graph [3].add (new Edge (s: 3, d: 2, w: 1));
```

// 4 vertex

```
graph [4].add (new Edge (s: 4, d: 2, w: 4));
```

// 2's neighbour.

```
for (int i=0; i<graph[2].size(); i++) {
```

```
    Edge e = graph[2].get(i); // src, dest, wt
```

```
    System.out.println(e.dest);
```

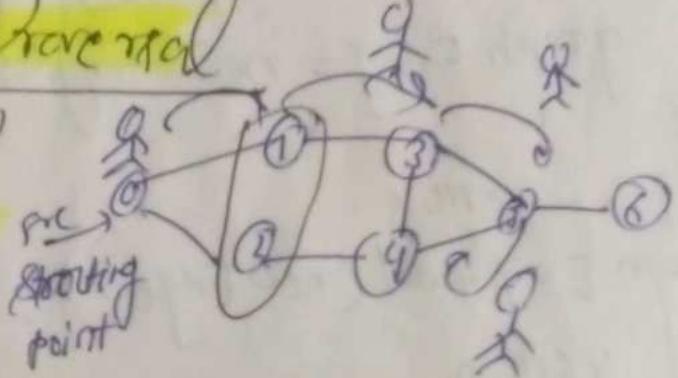
9
11

output: 1
2
4

Graph Traversal

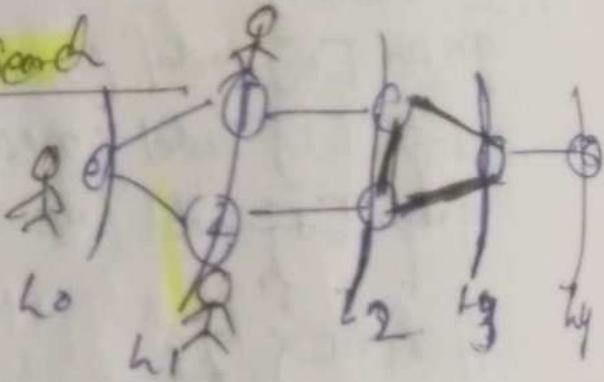
① Breadth first search (BFS)

② Depth first search (DFS)



(here it is breadth first search

* go to immediate neighbour first



Queue: [0|1|2|3|4|1|4|5|2|3|5]

FIFO F ↵

q.remove() → curr

visit[curr] + point(curr)

if (!vis[curr])

[0 1 2 3 4 5 6]

output

| | | | | | | |
|---------|---|---|---|---|---|---|
| T | T | T | T | H | T | F |
| visited | 0 | 1 | 2 | 3 | 4 | 5 |

visited → each node visit once

- ① visit[curr]
- ② print
- ③ Neighbour addly

```

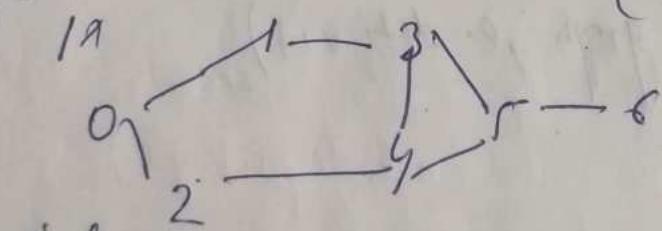
Code: public static void bfs (ArrayList<Edge> graph) {
    Queue <Integer> q = new linked list <>();
    boolean vis [] = new boolean [graph.length];
    q.add (e: 0); //q.size=0
    while (!q.isEmpty ()) {
        int cur = q.remove ();
        if (!vis [cur]) { //visit cur
            System.out.print (cur + " ");
            vis [cur] = true;
            for (int i = 0; i < graph [cur].size(); i++) {
                Edge e = graph [cur].get (i);
                q.add (e.dest);
            }
        }
    }
}

```

```

public static void main (String Arg[])
{
    int v = 7;

```



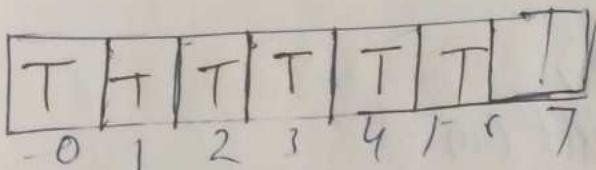
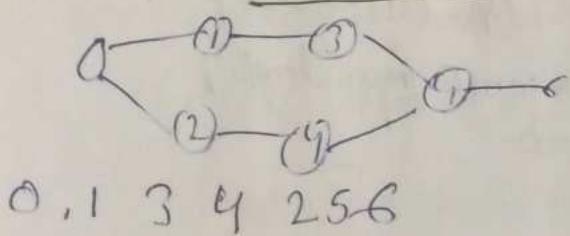
```

    ArrayList <Edge> graph [] = new ArrayList [v];
    CreateGraph (graph);
    bfs (graph);
}
}

```



DFS Depth First Search



for given out

me Recursion call stack

- ① run \rightarrow visit — print $vis[un]=T$
- ② for($i=0$ to k)
 $(!vis[adj])$
 $dfs(neighbour)$

| |
|-----|
| 6 |
| 2/5 |
| 9 |
| 3 |
| 1 |
| 0 |

Code:

```
public static void dfs(AnyList<Edge> graph, int cur, boolean vis[])
    //visit
    if (cur < 0 || cur >= graph[cur].size())
        return;
    vis[cur] = true;
```

```
for (int i = 0; i < graph[cur].size(); i++)
```

```
    Edge e = graph[cur].get(i);
```

```
    if (!vis[e.to])
```

```
        dfs(graph, e.to, vis);
```

```
}
```

```
public static void main (String args[]){}
```

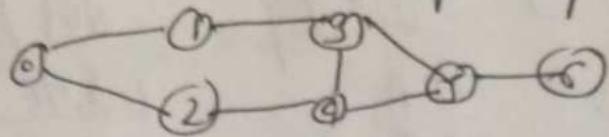
```
int v = 7
```

```
ArrayList<Edge> graph = new ArrayList[v];
CreateGraph(graph);
```

```
dfs(graph, 0, new boolean[v]);
```

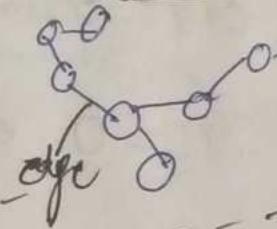
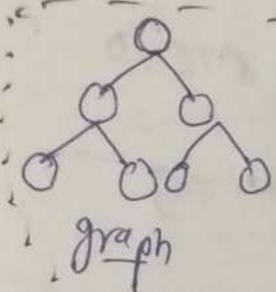
```
gg
```

Question Find Path
for given src, dest, tell if a path exist from src to
dest



$$\text{src} = 0 \quad \text{dest} = 5$$

38.1 Connected Component



o) single graph

DFS (src
BFS)

① DFS

in EJ → value
for (int i=0; i < graph.length;) {
if (vis[i] && !EJ[i]) {
dfsUtil();

FAFF

dfsUtil
DFS

} DFS (dfsUtil
helper)

g

Code-

```
public static void bfs (ArrayList<Edge> graph) {
```

```
boolean vis [] = new boolean [graph.length];
```

```
for (int i=0; i < graph.length; i++) {
```

```
Edge e = graph [i].get (i);  
visit (e.dest);
```

},

```
public static void dfs (ArrayList<Edge> graph) {
```

```
boolean vis [] = new boolean [graph.length];
```

```
for (int i=0; i < graph.length; i++) {
```

```
dfsUtil (graph, i, vis);
```

},

```
public static void dfsUtil (ArrayList<Edge> graph, int curNode,
```

```
String cur) {
```

```
vis [cur] = true;
```

```
for (int i=0; i < graph [cur].size (); i++) {
```

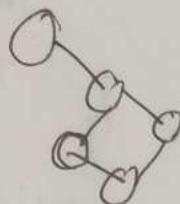
```

Edge e = graph[cam].get(i);
if (!vis[e.dst]) {
    dfsUtil(graph, e.dst, vis);
}

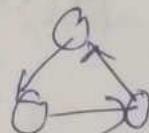
```

3.2.2 Cycle in Graph

undirected graph → DFS
 → BFS
 DSU (Disjoint Set Union)

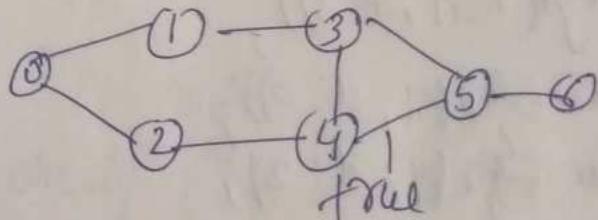


directed graph → DFS
 → BFS
 Topological sort (Kahn's algorithm)

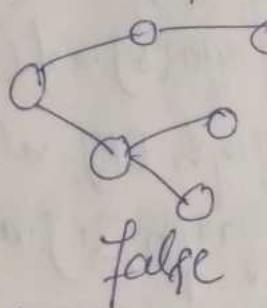


Cycle Detection

undirected graph → DFS

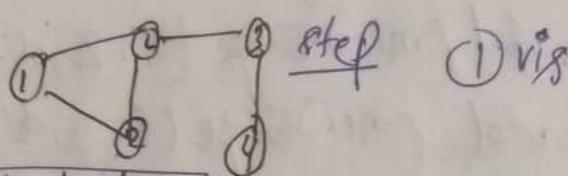


no cycle



false

Example



| | | | | | |
|------|-----|-----|-----|-----|-----|
| vis: | [] | [] | [] | [] | [] |
| | 0 | 1 | 2 | 3 | 4 |

① vis

Case 1: vis[height] → parent ✓



Case 2: vis[height] × parent ✓ case of

(cur)

Case 3: vis[height] × → normal DFS call (vis ff)

Cycle → True

{dfs
loop
dkf util
 Raum}

Code import java.util.*;
public class classrooms

static class Edge{

int src;

int dst;

public Edge (int s, int d){

this.src = s;

this.dst = d;

} }

static void createGraph (ArrayList<Edge> graph[]){

for (int e=0; e < graph.length; e++){

graph [e] = new ArrayList();

graph [0].add (new Edge(s:0, d:1));

graph [1].add (new Edge(s:0, d:2));

graph [0].add (new Edge(s:0, d:3));

graph [1].add (new Edge(s:1, d:0));

graph [1].add (new Edge(s:1, d:2));

graph [2].add (new Edge(s:2, d:0));

graph [2].add (new Edge(s:2, d:1));

graph [3].add (new Edge(s:3, d:0));

graph [3].add (new Edge(s:3, d:1));

graph [4].add (new Edge(s:4, d:3));

} }

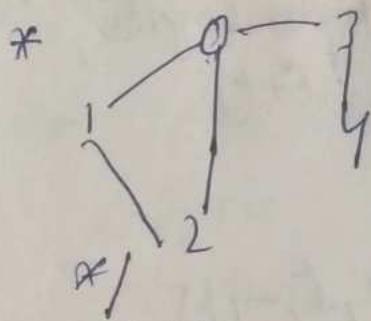
①

Code of cycle detection

```
public static boolean detectCycle (ArrayList<Edge> graph) {
    boolean vis[] = new boolean [graph.length];
    for (int i=0; i<graph.length; i++) {
        if (!vis[i]) {
            if (detectCycleUtil (graph, vis, i, -1))
                return true; // cycle exist in one part
        }
    }
    return false;
}
```

```
public static boolean detectCycleUtil (ArrayList<Edge> graph, boolean vis[], int cur) {
    vis[cur] = true;
    for (int i=0; i<graph[cur].size(); i++) {
        Edge e = graph[cur].get(i);
        if (!vis[e.dest] && detectCycleUtil (graph, vis, e.dest, cur))
            return true;
    }
    // case 1
    else if (vis[e.dest] && e.dest != par) {
        return true;
    }
    // case 2 do nothing
    else
        return false;
}
```

public static void main (String args [])



int $v = 5$;
ArrayList<Edge> graph [] = new ArrayList<v>;
Create Graph (graph);
try { detectCycle (graph); }
catch (Exception e) {

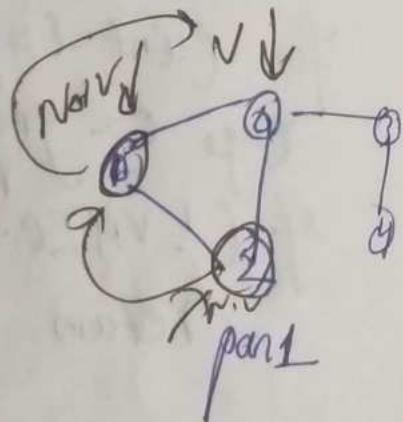
Case 1

vis [height]

pass $\rightarrow T$

Dry run

| | | | | | |
|-----|---|---|---|---|---|
| vis | [| V | V | V | |
| | 0 | 1 | 2 | 3 | 4 |



Case 2

vis [height]

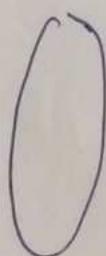
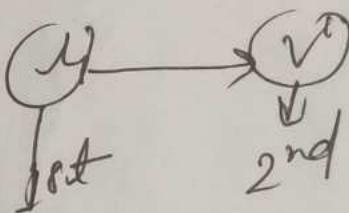
pass

Case 3

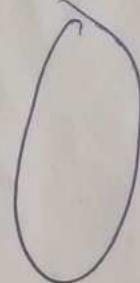
vis [height] \rightarrow normal QF
 $\text{cycle} \rightarrow T$

Bipartite graph

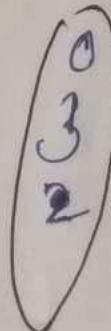
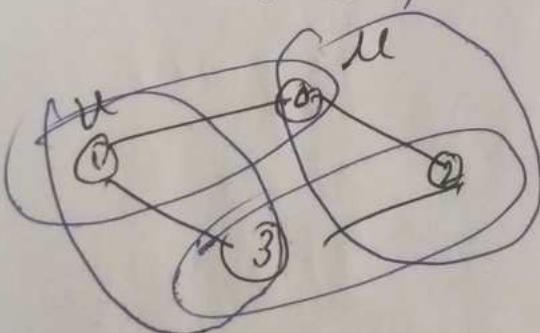
A bipartite graph is a graph where vertices can be divided into two independent sets, $U \cup V$ such that every edge (u, v) either connects a vertex from U to V or vice versa. In other words, for every edge (u, v) , either u belongs to U & v to V or u belongs to V & v to U . We can also say that there is no edge that connects vertices of same set.



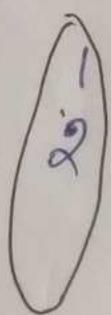
set 1 (U)



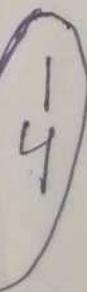
set 2 (V)



set 1 (U)

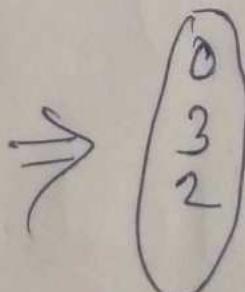


set 2 (V)

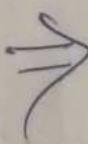
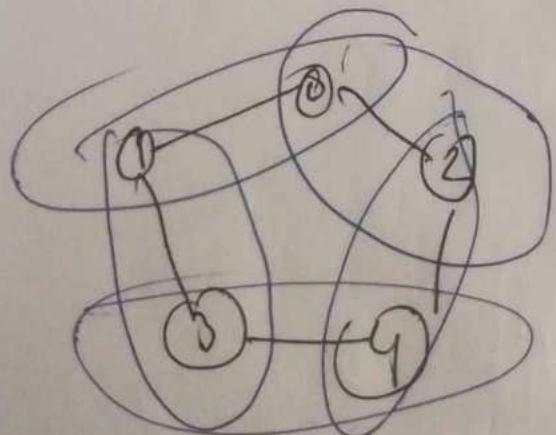


set 1 (U)

X partite

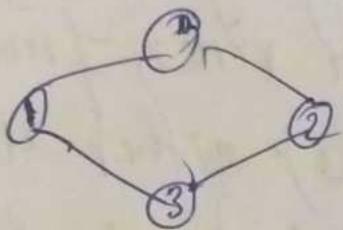


set 2 (V)



set 1 (U)

Algorithm \rightarrow Coloring

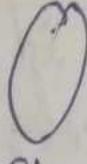


set¹



yellow
(0)

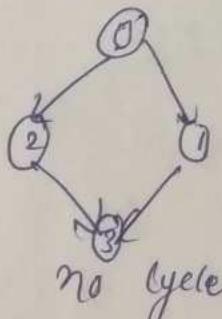
set²



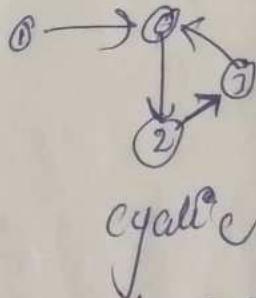
blue
(1)

Cycle Detection in Directed graph

Directed graph (DFS)

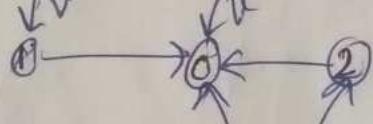


no cycle



cyclic

why undirected DFS approach fail?



Directed
no cycle

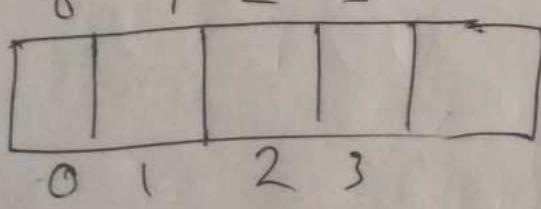
fail with DFS
+ fail

neigh \rightarrow vis \rightarrow par

Approach: DFS ✓
+

Stack \rightarrow recursion
(vis.) stack (explicit)
(boolean)

Approach Array: [] vis
[] [] [] []



Stack cell
node visit

- ① process
- ② Approach
- ③ dry run

dfs (con)

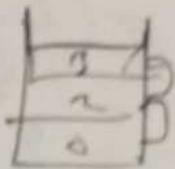
vis [con] = true

stack [con] = true;

for (all nigh.)

if (!vis [nigh]) → visit

y

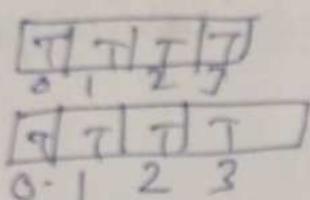
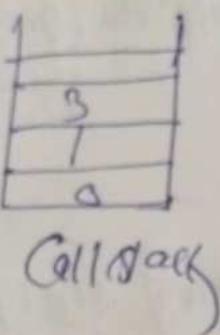


if (stack [nigh] = true)

→ cycle exist true

if (!vis [nigh])

is cycle (height) + 1
stack [con] = false



① static void CreateGraph (ArrayList<Edge> graph[])

for (int i=0; i < graph.length; i++) {

y graph [i] = new ArrayList<Edge>;

graph [i]. add (new Edge (s: 0, d: 2));

graph [0]. add (new Edge (s: 1, d: 0));

graph [2]. add (new Edge (s: 2, d: 3));

y graph [3]. add (new Edge (s: 3, d: 0));

public static boolean isCycle (ArrayList<Edge> graph) {

boolean vis [] = new boolean [graph.length];

boolean stack [] = new boolean [graph.length];

for (int i=0; i < graph.length; i++) {

y if (!vis [i]) {

```
if (isCycleUtil (graph, v, vis, stack))  
    return true;  
}  
}  
return false;
```

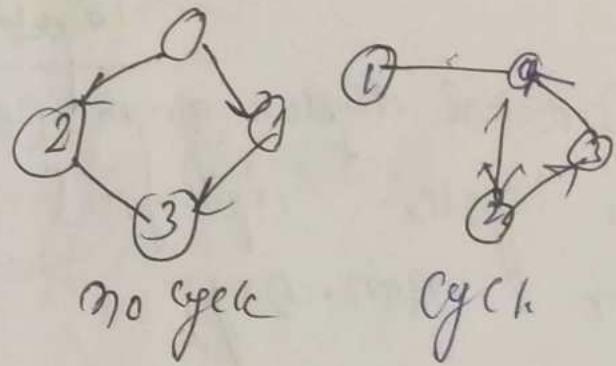
```
public static boolean isCycleUtil (ArrayList<Edge> graph, int  
vis[], Stack<int> stack, int  
v, Edge e) {
```

```
for (int i = 0; i < graph[v].size(); i++) {  
    Edge e = graph[v].get(i);  
    if (stack[e.dest])  
        return true;  
    if (!vis[e.dest] && isCycleUtil (graph, e.dest, vis, stack))  
        return true;  
}  
stack[v] = false;  
return false;
```

```
public static void main (String args[]){  
    int v = 4;  
    ArrayList<Edge> graph [] = new ArrayList[];  
    CreateGraph (graph);
```

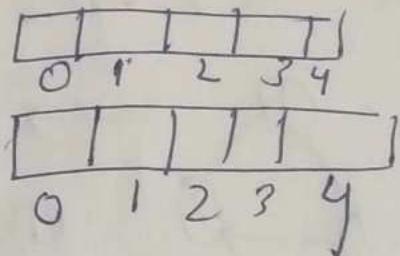
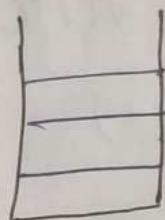
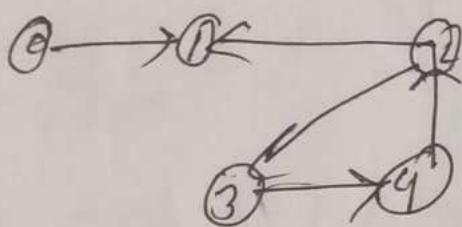
`graph (is cycle (graph));`

}
y



Cycle Detection

Qry Run.



Main Code:

`vis[can] = true;`
`stack[can] = true;`

`for (int i=0; i<graph[can].size(); i++) {`

`Edge e = graph[can].get(i);`

`if (stack[e.dest]) {`

`return true;`

}

`else if (!vis[e.dest] && Util(graph, e.dest, vis, stack)) {`

`return true;`

}

`stack[can] = false;`

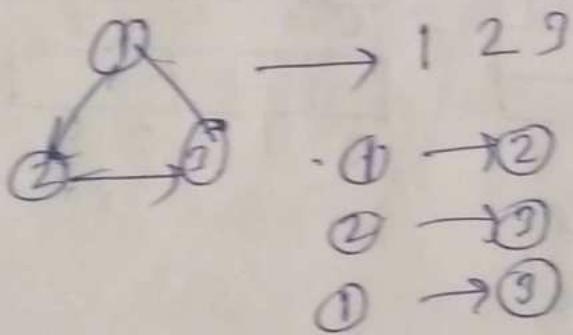
`return false;`

}

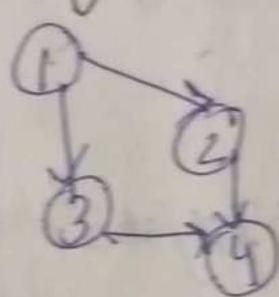
Topological Sort

Directed acyclic graph (DAG) is a directed graph with no cycle. Topological sorting is used for DAG (not for non-DAG).

- It is a linear order of vertices such that every directed edge $u \rightarrow v$, the vertex u comes before v in the order.



Dependency graph



Action 1 - boil water

Action 2 - add mealie

→ add maggi

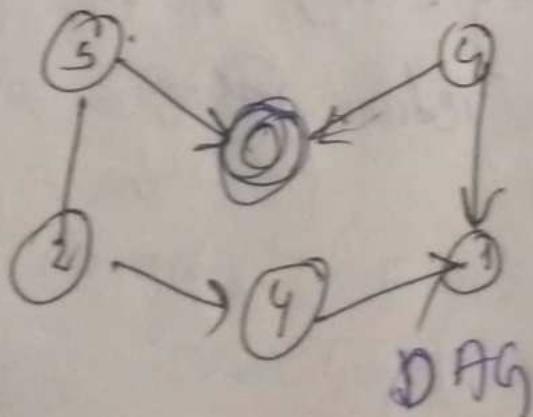
→ serve maggi

{1 2 3 4}
{1 3 2 4}

Software
OS
VS Code
extension

Cycles \Rightarrow Not dependency

using DFS



possible Ans

4 2 3 1 0

5 4 2 3 1 0

```

    4
    3
    2
    1
    0
    trace what come first
    } off
    } y
    sorting dft(graph, curr, visit, stack){  

        if(visit[curr] = true);  

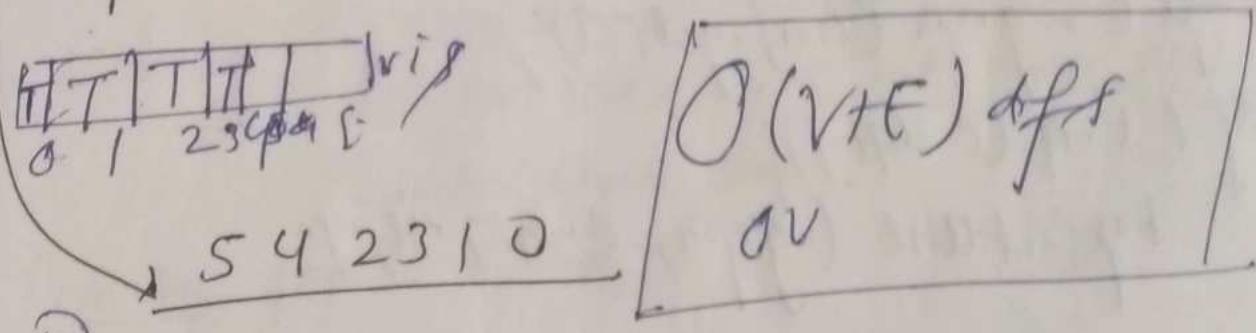
        for(int i=0; i<graph.length; i++) {  

            if(unvisited)  

                stack.add(curr);  

}

```



```

    public static void main() {
        boolean visit[] = new boolean[graph.length];
        Stack<Integer> s = new Stack<Integer>;
        for (int i=0; i<graph.length; i++) {
            if (!visit[i])
                topSortUtil(graph, i, visit, s);
        }
        while (!s.isEmpty()){
            System.out.print(s.pop() + " ");
        }
    }

```

g5

```
public static void topsortUtil(ArrayList<Edge> graph, int cur  
                                boolean vis[], Stack){  
    vis[cur] = true;  
    for(int i=0; i<graph[cur].size(); i++)  
        Edge e = graph[cur].get(i);  
        if(!vis[e.dest])  
            topsortUtil(graph, e.dest, vis, stack);  
}  
y}
```

8. push((vv));

(g6 public static void main(String Arg[]){

int v=6;

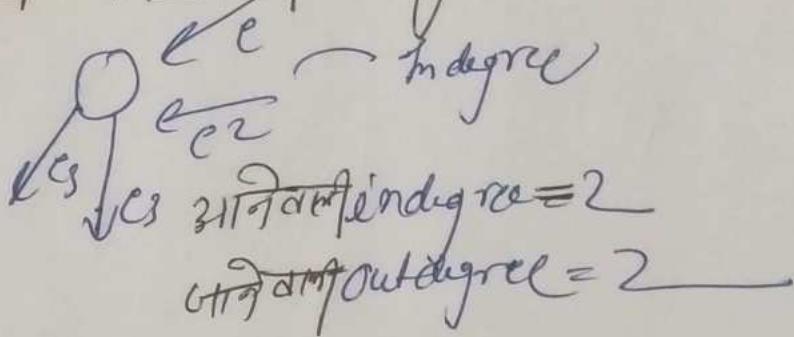
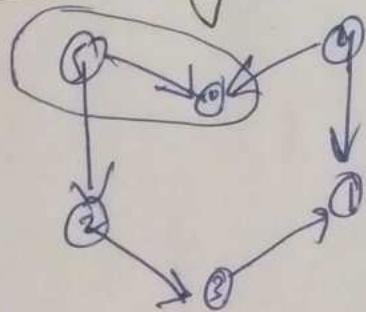
ArrayList<Edge> graph[] = new ArrayList[6];

Create Graph <graph>;

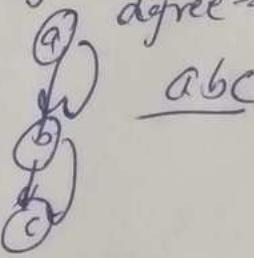
g

39.1 Topological Sort using BFS

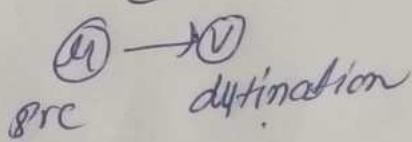
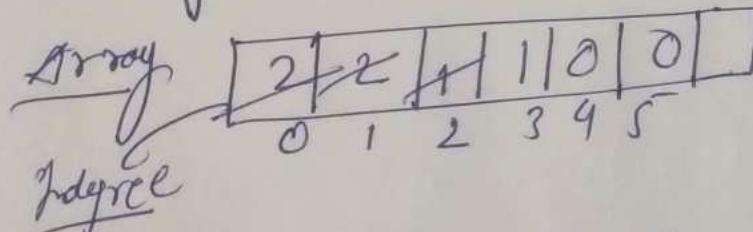
Kahn's Algorithm :-



Fact:- A DAG has at least one vertex with in degree 0 and one vertex with out degree 0.
(Directed Acyclic graph)



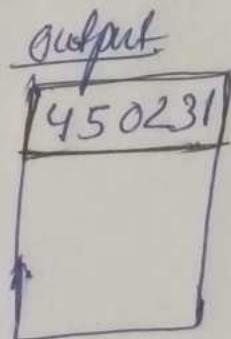
Dependency graph :-



BFS (inp on queue)

indegree $\rightarrow 0$
add in queue.

~~45101231~~
FIFO



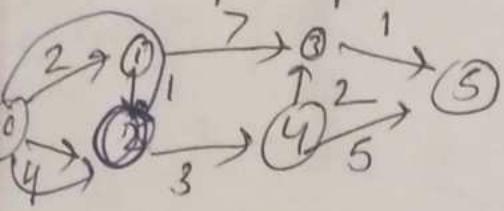
Code :-

39.2 Code -

greedy Algo

Dijkstra's algorithm $O(n \cdot log n)$

Shortest path from the source to all vertices (weighted graph)



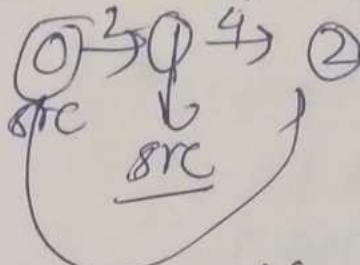
Shortest path $2+1=3$
 $0 \rightarrow 2 \Rightarrow 4$

optimization

greedy algorithm

$$\text{dist}[ij] = \text{preto}^j$$
$$\text{dist}[uj] = \text{preto}^u$$

- $\text{dist}[uj] + \text{wt}(u, uj)$
- $\text{dist}[uj] = \text{dist}[u] + \text{wt}(u, uj)$

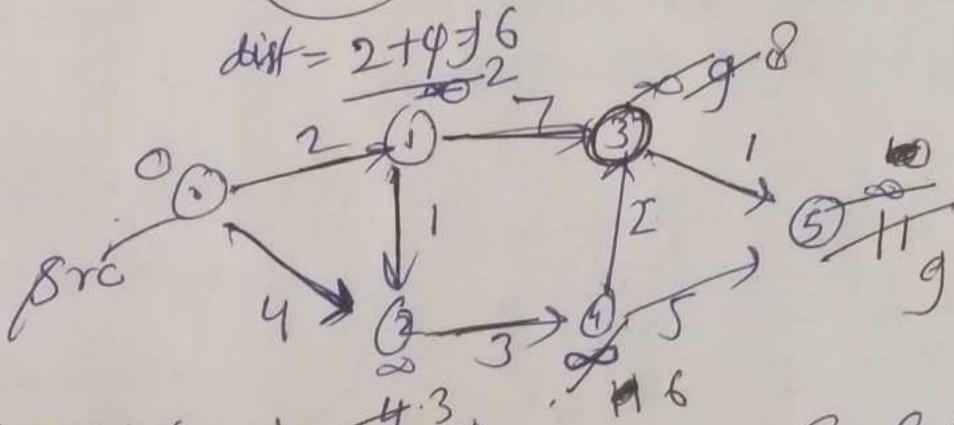


Priority Queue

$$\text{dist} = \frac{2+4+6}{2}$$

$$\text{dist}[uj] + \text{wt}(u, uj) < \text{dist}[uj]$$

$$\text{dist}[uj] = \text{dist}[u] + \text{wt}(u, uj)$$



BFS

visit X
shortest

Final Dist.

$$\begin{aligned}
 0 \rightarrow 0 &\rightarrow 0 \\
 0 \rightarrow 1 &= 2 \\
 0 \rightarrow 2 &= 3 \\
 0 \rightarrow 3 &= 8 \\
 0 \rightarrow 4 &= 6 \\
 0 \rightarrow 5 &= 9
 \end{aligned}$$

Algorithm

- ① Initialize distance
- ② Priority Queue $\langle \text{Pair} \rangle (n, \text{dist})$
- ③ while (Pa is not empty) {
 - curr \rightarrow visit

If ($\text{is}[curr] = \text{false}$) {

neighbors

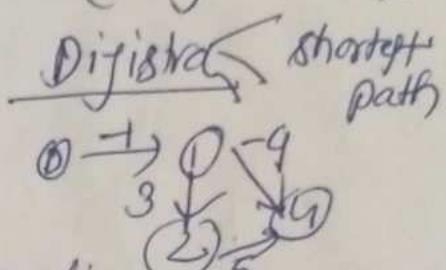
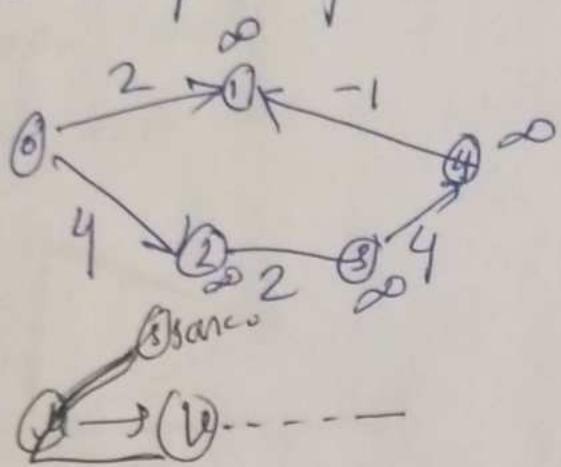
$$\text{dist}[uj] + \text{wt}(u, uj)$$

$$< \text{dist}[uj]$$

update $\text{dist}[uj]$

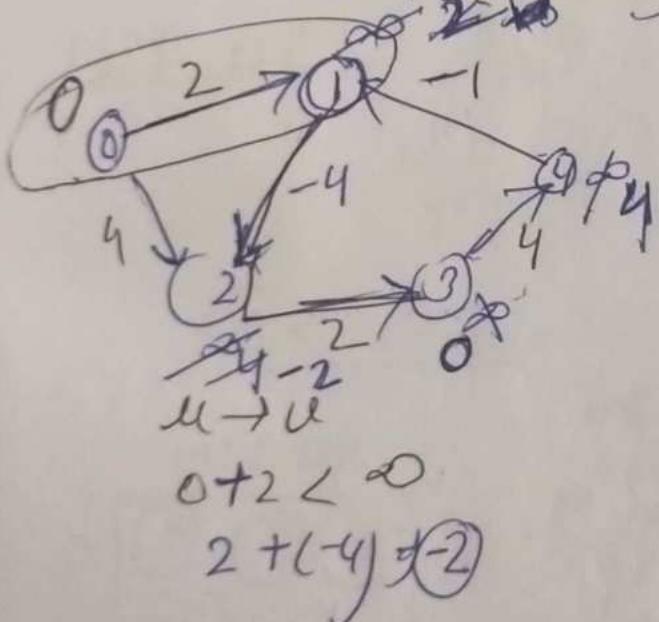
40-1

Bellman Ford Algorithm (Dynamic Programming)
Shortest path from the source to all vertices (Negative edge)



① Perform this operation $V-1$ times
for all edges (u, v)
if $dist[u] + wt(u, v) < dist[v]$
 $dist[v] = dist[u] + wt(u, v)$

logic for (int i=0 to V-1) {
edge $(u \rightarrow v)$
Relaxation}



| - | 0 | 1 | 2 | 3 | 4 |
|---|---|----------|----------|----------|---|
| 0 | 0 | ∞ | ∞ | ∞ | 0 |
| 1 | 0 | 2 | $4-2$ | 0 | 2 |
| 2 | 0 | 2 | -2 | 0 | 4 |
| 3 | 0 | 2 | -2 | 0 | 4 |
| 4 | 0 | 2 | -2 | 0 | 4 |

Code: $dist[] = \text{new int}[V]$
for (int i=0 to V-1)
edge $(u \rightarrow v)$
Relaxation

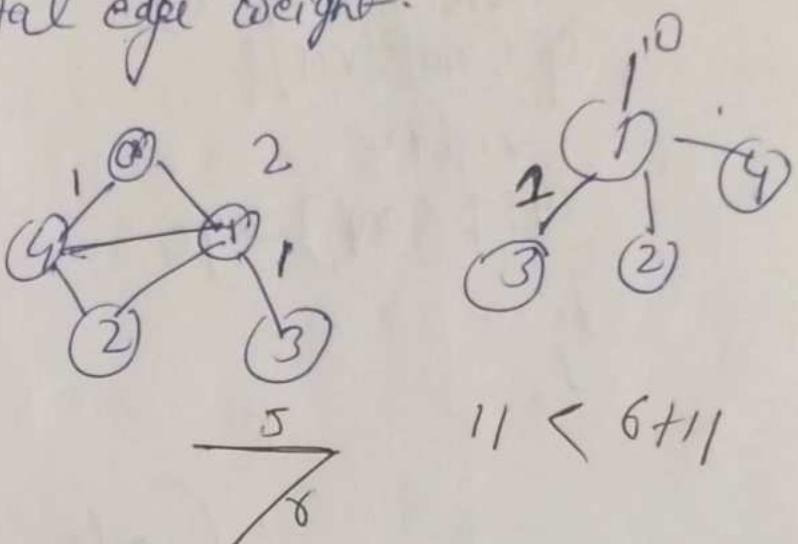
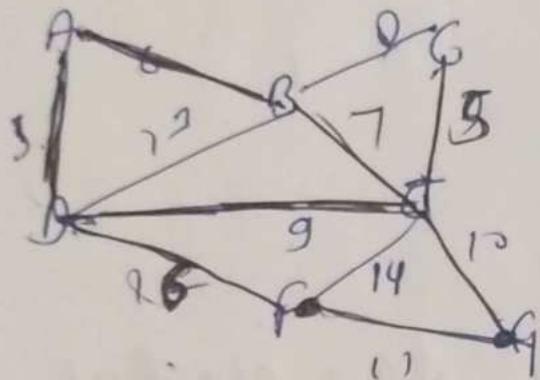
loop $\frac{u \rightarrow v}{(v=1)^{\text{th}}}$

Note Does not work for Negative weight cycle

$-4+2+4=$ 1 positive

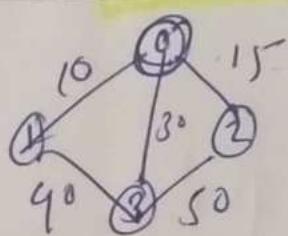
Minimum Spanning Tree (MST)

A minimum spanning tree (MST) or minimum spanning tree is a subset of the edges of a connected, edge-weighted undirected graph that connect all the vertices together, without any cycles and with minimum possible total edge weight.

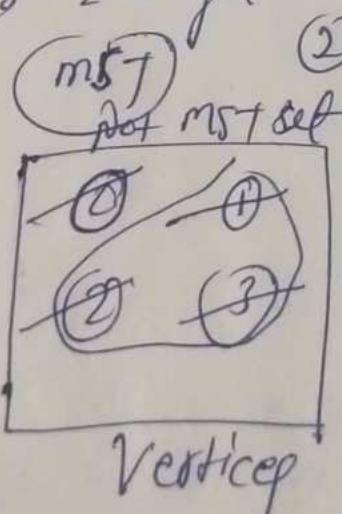
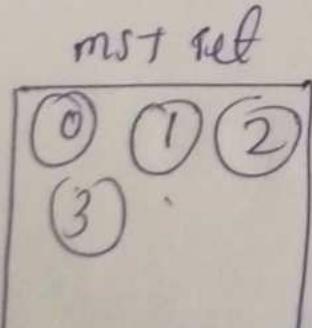


Prim's Algorithm

MST set

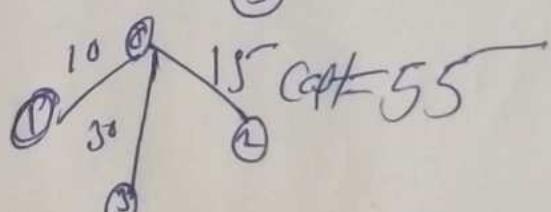
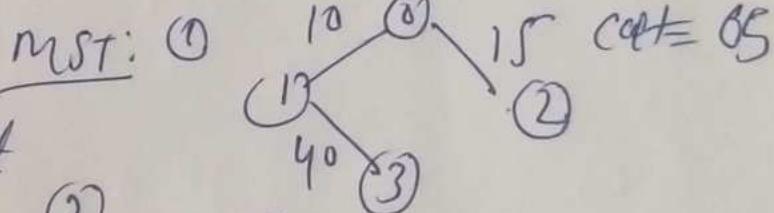


$55 < 65$ So, 2nd night

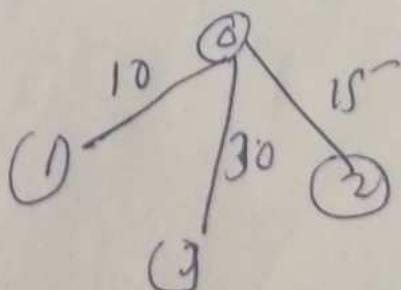


| | | | | |
|-------|---|---|---|---|
| right | T | T | T | T |
| | 0 | 1 | 2 | 3 |

• undirected + weighted
MST



{ minimum cat \Rightarrow 25 }
& 3rd node on MST }



using priority queue < v_{min} , c_{min} > \rightarrow minimum spanning tree

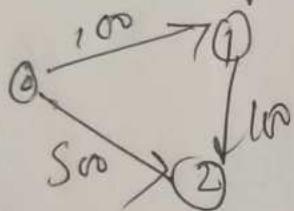
PQ $\{ (0, 0) \}$
while (PQ is not empty){
 curr $\rightarrow (v, c_{min})$
 if (not vis){
 visit v
 MST (any) edge
 }
}

Code: 40.5 Prim's Algorithm

41.1 Cheapest flight within k stop

Q There are n cities connected by some number of flight. You are given an array flight where $\text{flight}[i] = [\text{from}, \text{to}, \text{price}]$ indicate that there is a flight. You are also given three integers src , dst , k return the cheapest price from src to dst with at most k stop if there is no such route, return -1.

All values are positive.



flight = $[[0, 1, 100], [1, 2, 100], [0, 2, 500]]$
 $\text{src} = 0, \text{dst} 2, k = 1$
 $\text{ans} = 200$

41.3 Connecting cities with minimum cost

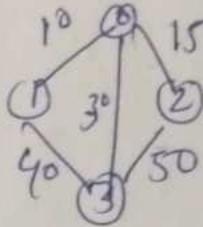
Find the minimum cost for connecting all cities on the map

$$\text{CITY}[\text{J}] = \{\{0, 1, 2, 3, 4\}, \\ \{1, 0, 5, 0, 7\}, \\ \{2, 5, 0, 6, 0\}, \\ \{3, 0, 6, 0, 0\}, \\ \{4, 7, 0, 0, 2\}\}$$

MST

g greedy

Kruskal Algorithm

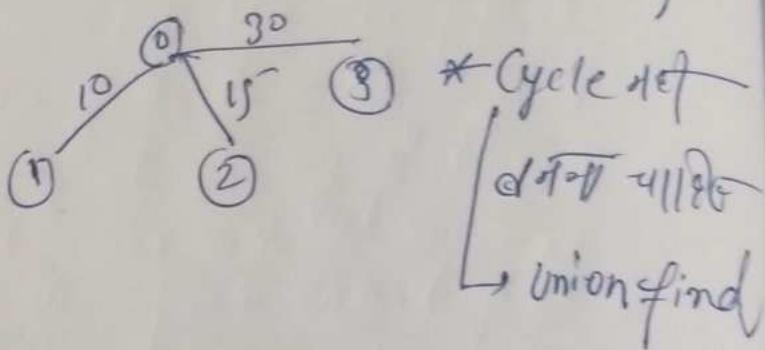


Step:-

- ① sort edge
- ② Take min. edge
→ form cycle
→ include any.

Sorted edges

| | Weight |
|-------|--------|
| (0,1) | 10 |
| (0,2) | 15 |
| (0,3) | 30 |
| (1,3) | 40 |
| (2,3) | 50 |



ArrayList <edge> → Collection.Sort()

for ($e=0$ to $v-1$)

for (count = 0 to $v-1$)

Edge e → a src
b dest

panA panB

some → x cycle

diff → union (panA, panB)

$\textcircled{0} \rightarrow \textcircled{1}$
panA & panB
same
cycle X

$O(v + e \log E)$

Code 41.6

Flood Fill Algorithm

Given a $m \times n$ integer grid Image where $\text{Image}[i][j]$ represents the pixel value of the image. You are also given three integers sr , sc , Color . You should perform a flood fill on the image starting from the pixel $\text{Image}[sr][sc]$.

To perform a flood fill, consider the starting pixel, then any pixel connected 4 directionally to the starting pixel of the same color as the starting pixel, then any pixel connected 4 directionally to those pixels (also with the same color), and so on. Replace the color of all of the aforementioned pixels with Color .

$$\text{Image} = \begin{bmatrix} [1, 1, 1] \\ [1, 1, 0] \\ [1, 0, 1] \end{bmatrix} \quad sr=1 \quad sc=1 \quad \text{Color}=2$$

$$\text{Ans} = \begin{bmatrix} [2, 2, 2] \\ [2, 2, 0] \\ [2, 0, 1] \end{bmatrix}$$

42.1 Strongly Connected Component

SCC is a component in which we can reach every vertex of the component from every vertex in that component.

42.2

Bridge in Graph

Topological Algorithm:-

- Bridge is an edge whose deletion increase the graph's number of connected component

