

[6180]-141

**T.E. (Information Technology)****DESIGN & ANALYSIS OF ALGORITHMS****(2019 Pattern) (Semester - I) (314445A) (Elective - I)***Time : 2½ Hours]**[Max. Marks : 70**Instructions to the candidates:*

- 1) Answer Q1 or Q2, Q3 or Q4, Q5 or Q6, Q7 or Q8.
- 2) Neat diagrams must be drawn wherever necessary.
- 3) Figures to the right side indicate full marks.
- 4) Assume suitable data, if necessary.

**Q1)** a) Discuss the dynamic programming approach to solving the coin change-making problem. Explain how the problem can be formulated as a dynamic programming task and provide a step-by-step explanation of the algorithm. [10]

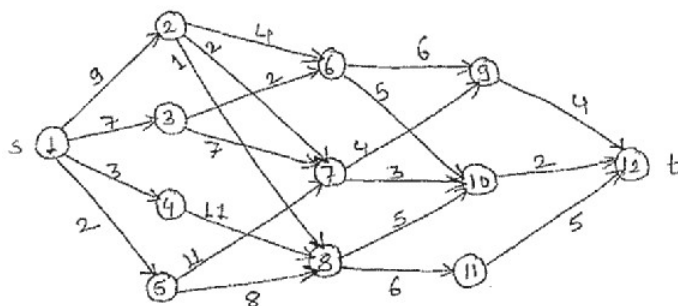
- b) Explain the Bellman-Ford algorithm for finding the shortest paths in a weighted directed graph. Discuss the problem it solves, its applications, and its time complexity. [8]

OR

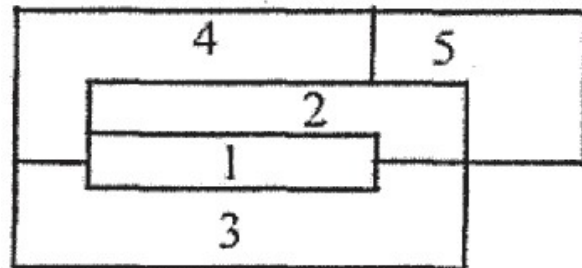
**Q2)** a) Solve the TSP problem using Dynamic Programming. [10]

$$\begin{bmatrix} 0 & 10 & 15 & 20 \\ 5 & 0 & 9 & 10 \\ 6 & 13 & 0 & 12 \\ 8 & 8 & 9 & 0 \end{bmatrix}$$

- b) Find the minimum cost path from source s to sink t of the following multistage graph. [8]



- Q3)** a) Write recursive and iterative algorithm for backtracking method. [8]
- b) Construct planar graph for following map. Explain how to find m - colouring of this planar graph by using m-colouring Backtracking algorithm. [9]



OR

- Q4)** a) Define the n-Queen problem and its objective. Explain the rules and constraints associated with placing n queens on an  $n \times n$  chessboard without attacking each other. [8]
- b) Discuss how the backtracking algorithm can be applied to solve the sum of subsets problem. Explain the decision space exploration process with some examples. [9]
- Q5)** Construct the solution of following Travelling Salesperson problem using Branch and Bound. [18]

|          |          |          |          |          |
|----------|----------|----------|----------|----------|
| $\infty$ | 20       | 30       | 10       | 11       |
| 15       | $\infty$ | 16       | 4        | 2        |
| 3        | 5        | $\infty$ | 2        | 4        |
| 19       | 6        | 18       | $\infty$ | 3        |
| 16       | 4        | 7        | 16       | $\infty$ |

OR

- Q6)** a) Write an algorithm for FIFO branch and bound. [9]
- b) Explain FIFO branch and bound method of problem solving. Explain its advantages and limitations. [9]

- Q7)** a) Prove that Satisfiability problem is NP complete. [8]
- b) Discuss the proof for the NP-completeness of the Vertex Cover problem. [9]

OR

- Q8)** a) Define the complexity classes P, NP, NP-complete, and NP-hard. Explain the relationships between these classes and their significance in computational complexity theory. [9]
- b) Prove that clique problem is NP complete. [8]

