

Q-1 What is the time complexity of fun()?

```
int fun(int n)
{
    int count = 0;
    for (int i = 0; i < n; i++)
        for (int j = i; j > 0; j--)
            count = count + 1;
    return count;
}
```

- A) Theta (n)
- B) Theta ( $n^2$ )
- C) Theta ( $n \cdot \log n$ )
- D) Theta ( $n \log n \log n$ )

Ans : B) Theta ( $n^2$ )

Q-2 Let  $w(n)$  and  $A(n)$  denote respectively, the worst case and average case running time of an algorithm executed on an input of size  $n$ . which of the following is ALWAYS TRUE? (GATE CS 2012)

- (A)  $A(n) = \Omega(W(n))$
- (B)  $A(n) = \Theta(W(n))$
- (C)  $A(n) = O(W(n))$
- (D)  $A(n) = o(W(n))$

- A) A
- B) B
- C) C
- D) D

Ans : C) C

Q-3 Which of the following is not  $O(n^2)$ ?

A)  $(15^{10}) * n + 12099$

B)  $n^{1.98}$

C)  $n^3 / (\text{sqrt}(n))$

D)  $(2^{20}) * n$

Ans : C)  $n^3 / (\text{sqrt}(n))$

Q-4 Which of the given options provides the increasing order of asymptotic complexity of functions  $f_1$ ,  $f_2$ ,  $f_3$  and  $f_4$ ?

$f_1(n) = 2^n$

$f_2(n) = n^{(3/2)}$

$f_3(n) = n \log n$

$f_4(n) = n^{(\log n)}$

A)  $f_3, f_2, f_4, f_1$

B)  $f_3, f_2, f_1, f_4$

C)  $f_2, f_3, f_1, f_4$

D)  $f_2, f_3, f_4, f_1$

Ans : A)  $f_3, f_2, f_4, f_1$

Q-5 Consider the following program fragment for reversing the digits in a given integer to obtain a new integer. Let  $n = D_1D_2\ldots D_m$

```
int n, rev;
```

```

rev = 0;
while (n > 0)
{
    rev = rev*10 + n%10;
    n = n/10;
}

```

The loop invariant condition at the end of the  $i$ th iteration is:

- A)  $n = D_1D_2\dots D_{m-i}$  and  $rev = D_mD_{m-1}\dots D_{m-i+1}$
- B)  $n = D_{m-i+1}\dots D_{m-1}D_m$  and  $rev = D_{m-1}\dots D_2D_1$
- C)  $n \neq rev$
- D)  $n = D_1D_2\dots D_m$  and  $rev = D_mD_{m-1}\dots D_2D_1$

Ans : A)  $n = D_1D_2\dots D_{m-i}$  and  $rev = D_mD_{m-1}\dots D_{m-i+1}$

Q-6 Consider the following function

```

int unknown(int n)
{
    int i, j, k = 0;
    for (i = n/2; i <= n; i++)
        for (j = 2; j <= n; j = j * 2)
            k = k + n/2;
    return k;
}

```

What is the returned value of the above function? (GATE CS 2013)

- (A)  $\Theta(n^2)$
- (B)  $\Theta(n^2 \log n)$
- (C)  $\Theta(n^3)$
- (D)  $\Theta(n^3 \log n)$

Ans : (B)  $\Theta(n^2 \log n)$

Q-7 The recurrence equation

$$T(1) = 1$$

$$T(n) = 2T(n-1) + n, n \geq 2$$

evaluates to

- A)  $2^{n+1} - n - 2$
- B)  $2^n - n$
- C)  $2^{n+1} - 2n - 2$
- D)  $2^n + n$

Ans : A)  $2^{n+1} - n - 2$

Q-8 Consider the following three claims

I  $(n+k)^m = \Theta(n^m)$ , where  $k$  and  $m$  are constants

II  $2^{n+1} = O(2^n)$

III  $2^{2n+1} = O(2^n)$

Which of these claims are correct?

- A) I and II
- B) I and III
- C) II and III
- D) I, II and III

Ans : A) I and II

Q-9 Consider the following C code segment

```

int f (int x)
{
    if (x < 1) return 1;
    else return (f(x-1) + g(x))
}

int g (int x)
{
    if (x < 2) return 2;
    else return (f(x-1) + g(x/2));
}

```

Of the following, which best describes the growth of  $f(x)$  as a function of  $x$ ?

- A) Linear
- B) Exponential
- C) Quadratic
- D) Cubic

Ans : B) Exponential

Q-10 What is the time complexity of following function `fun()`? Assume that `log(x)` returns log value in base 2.

```

void fun()
{
    int i, j;
    for (i=1; i<=n; i++)
        for (j=1; j<=log(i); j++)
            printf("GeeksforGeeks");
}

```

- A)  $\Theta(n)$
- B)  $\Theta(n \log n)$

C)  $\Theta(n^2)$

D)  $\Theta(n^2(\log n))$

Ans : B)  $\Theta(n \log n)$