MOSEK Command Line Tools

Release 9.1.13

MOSEK ApS

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Contents

Chapter 1

Introduction

The **MOSEK** Optimization Suite 9.1.13 is a powerful software package capable of solving large-scale optimization problems of the following kind:

- linear,

- conic:

    - conic quadratic (also known as second-order cone),
    - involving the exponential cone,
    - involving the power cone,
    - semidefinite,

- convex quadratic and quadratically constrained,

- integer.

In order to obtain an overview of features in the **MOSEK** Optimization Suite consult the product introduction guide.

The most widespread class of optimization problems is *linear optimization problems*, where all relations are linear. The tremendous success of both applications and theory of linear optimization can be ascribed to the following factors:

- The required data are simple, i.e. just matrices and vectors.

- Convexity is guaranteed since the problem is convex by construction.

- Linear functions are trivially differentiable.

- There exist very efficient algorithms and software for solving linear problems.

- Duality properties for linear optimization are nice and simple.

Even if the linear optimization model is only an approximation to the true problem at hand, the advantages of linear optimization may outweigh the disadvantages. In some cases, however, the problem formulation is inherently nonlinear and a linear approximation is either intractable or inadequate. *Conic optimization* has proved to be a very expressive and powerful way to introduce nonlinearities, while preserving all the nice properties of linear optimization listed above.

The fundamental expression in linear optimization is a linear expression of the form

$$Ax - b \geq 0.$$

In conic optimization this is replaced with a wider class of constraints

$$Ax - b \in \mathcal{K}$$

where $\mathcal{K}$ is a *convex cone*. For example in 3 dimensions $\mathcal{K}$ may correspond to an ice cream cone. The conic optimizer in **MOSEK** supports a number of different types of cones $\mathcal{K}$, which allows a surprisingly large number of nonlinear relations to be modeled, as described in the **MOSEK** Modeling Cookbook, while preserving the nice algorithmic and theoretical properties of linear optimization.

1.1 Why the Command Line Tools?

The **MOSEK** capabilities can be accessed from the command line without the need to use any programming language. The user can input optimization problems using files in a variety of *formats*, or via the AMPL language shell.

The Command Line Tools provides access to:

- Linear Optimization (LO)

- Conic Quadratic (Second-Order Cone) Optimization (CQO, SOCO)

- Power Cone Optimization

- Conic Exponential Optimization (CEO)

- Convex Quadratic and Quadratically Constrained Optimization (QO, QCQO)

- Semidefinite Optimization (SDO)

- Mixed-Integer Optimization (MIO)

as well as to additional utilities for:

- problem analysis,

- sensitivity analysis,

- infeasibility diagnostics.

Chapter 2

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	2100 Copenhagen O	
	Denmark	

You can get in touch with **MOSEK** using popular social media as well:

Blogger	https://blog.mosek.com/
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Google+	https://plus.google.com/+Mosek/posts
Linkedin	https://www.linkedin.com/company/mosek-aps

In particular **Twitter** is used for news, updates and release announcements.

Chapter 3

License Agreement

Before using the **MOSEK** software, please read the license agreement available in the distribution at `<MSKHOME>/mosek/9.1/mosek-eula.pdf` or on the **MOSEK** website https://mosek.com/products/license-agreement.

 MOSEK uses some third-party open-source libraries. Their license details follows.

zlib

 MOSEK includes the *zlib* library obtained from the zlib website. The license agreement for *zlib* is shown in Listing 3.1.

Listing 3.1: *zlib* license.

```
zlib.h -- interface of the 'zlib' general purpose compression library
version 1.2.7, May 2nd, 2012

Copyright (C) 1995-2012 Jean-loup Gailly and Mark Adler

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Jean-loup Gailly        Mark Adler
jloup@gzip.org          madler@alumni.caltech.edu
```

fplib

 MOSEK includes the floating point formatting library developed by David M. Gay obtained from the netlib website. The license agreement for *fplib* is shown in Listing 3.2.

Listing 3.2: *fplib* license.

```
/****************************************************************
 *
```

```
 * The author of this software is David M. Gay.
 *
 * Copyright (c) 1991, 2000, 2001 by Lucent Technologies.
 *
 * Permission to use, copy, modify, and distribute this software for any
 * purpose without fee is hereby granted, provided that this entire notice
 * is included in all copies of any software which is or includes a copy
 * or modification of this software and in all copies of the supporting
 * documentation for such software.
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 * WARRANTY.  IN PARTICULAR, NEITHER THE AUTHOR NOR LUCENT MAKES ANY
 * REPRESENTATION OR WARRANTY OF ANY KIND CONCERNING THE MERCHANTABILITY
 * OF THIS SOFTWARE OR ITS FITNESS FOR ANY PARTICULAR PURPOSE.
 *
 ****************************************************************/
```

Zstandard

MOSEK includes the *Zstandard* library developed by Facebook obtained from github/zstd. The license agreement for *Zstandard* is shown in Listing 3.3.

Listing 3.3: *Zstandard* license.

```
BSD License

For Zstandard software

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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
```

Chapter 4

Installation

In this section we discuss how to install and setup the **MOSEK** Command Line Tools.

Important: Before running this **MOSEK** interface please make sure that you:

- Installed **MOSEK** correctly. Some operating systems require extra steps. See the Installation guide for instructions and common troubleshooting tips.

- Set up a license. See the Licensing guide for instructions.

Locating files in the MOSEK Optimization Suite

The relevant files of the Command Line Tools are organized as reported in Table 4.1.

Table 4.1: Relevant files for the Command Line Tools.

Relative Path	Description	Label
`<MSKHOME>/mosek/9.1/tools/platform/<PLATFORM>/bin`	Binaries	`<BINDIR>`
`<MSKHOME>/mosek/9.1/tools/platform/<PLATFORM>/bin/mosek`	Mosek executable	
`<MSKHOME>/mosek/9.1/tools/examples/data`	Examples	`<EXDIR>`

where

- `<MSKHOME>` is the folder in which the **MOSEK** Optimization Suite has been installed,

- `<PLATFORM>` is the actual platform among those supported by **MOSEK**, i.e. `win32x86`, `win64x86`, `linux64x86` or `osx64x86`.

Setting up paths

The executable file is ready for use. It may be convenient to add the directory `<BINDIR>` to the environment variable `PATH`, and then **MOSEK** can simply be used by typing

```
mosek
```

in the command line.

4.1 Testing the installation

To test that Command Line Tools has been installed correctly go to the examples directory `<EXDIR>` and run **MOSEK** on any of the input files, for example `lo1.mps`:

```
mosek lo1.mps
```

Is should produce output similar to:

```
MOSEK Version 8.0.0.53 (Build date: 2017-1-12 22:21:45)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file 'lo1.mps'
Reading started.

[....]

Optimizer started.
Interior-point optimizer started.

[....]

Interior-point solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333280e+01    nrm: 5e+01    Viol.  con: 1e-08    var: 0e+00
  Dual.    obj: 8.3333333242e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Basic solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333333e+01    nrm: 5e+01    Viol.  con: 7e-15    var: 0e+00
  Dual.    obj: 8.3333333245e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

[....]

Open file 'lo1.sol'
Start writing.
done writing. Time: 0.00

Open file 'lo1.bas'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]
```

Chapter 5

The Command Line Tool

5.1 Introduction

The **MOSEK** command line tool is used to solve optimization problems from the operating system command line. It is invoked as follows

```
mosek [options] [filename]
```

where both `[options]` and `[filename]` are optional arguments:

- `[options]` consists of command line arguments that modify the behavior of **MOSEK**. They are listed in Sec. 5.5. In particular, options can be used to set optimizer parameters.

- `[filename]` is a file describing the optimization problem. The **MOSEK** command line accepts files in any of the *supported file formats* or in the AMPL `.nl` format.

If no arguments are given, **MOSEK** will display a splash screen and exit.

```
user@host:~$ mosek/8/tools/platform/linux64x86/bin/mosek

MOSEK Version 8.0.0.32(BETA) (Build date: 2016-7-12 10:29:26)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86


*** No input file specified. No optimization is performed.

Return code - 0  [MSK_RES_OK]
```

5.2 Files

The **MOSEK** command line tool communicates with the user via files and prints some execution logs and solution summary to the terminal.

Input files

Optimization problems are read from files. See Sec. 12 for details.

File format conversion

To convert between two file formats supported by **MOSEK** use the option `-x` together with `-out` to specify the target file name. The target file type must support the problem type of the source file, otherwise the conversion will be partial. For instance in case a MPS file must be converted in a more readable OPF format, the following line can be used

```
mosek -x -out lo1.opf lo1.mps
```

With the *-x* option the solver will not actually solve the problem.

Output files

Solutions are written to files:

- `.bas` - basic solution,

- `.sol` - interior point solution,

- `.itg` - integer solution (the only available solution for mixed-integer problems).

For linear problems both the basic and interior point solution may be present. Infeasibility certificates are stored in the same files. See Sec. 12.8 for details.

5.3 Example

To solve a problem stored in file, say `lo1.mps`, write:

```
mosek lo1.mps
```

The solver will

- read `lo1.mps` from disk,

- solve the problem and display the solution log and

- store the relevant solution files if any solution exists; file content explained in Sec. 12.8.

```
MOSEK Version 8.0.0.34(BETA) (Build date: 2016-8-24 00:51:13)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86


Open file '/home/andrea/mosek/8/tools/examples/data/lo1.mps'
Reading started.
Using 'obj' as objective vector
Read 13 number of A nonzeros in 0.00 seconds.
Using 'rhs' as rhs vector
Using 'bound' as bound vector
Reading terminated. Time: 0.00

Read summary
  Type           : LO (linear optimization problem)
  Objective sense  : max
  Scalar variables : 4
  Matrix variables : 0
  Constraints      : 3
  Cones            : 0
  Time             : 0.0

Problem
  Name               : lo1
  Objective sense    : max
  Type               : LO (linear optimization problem)
  Constraints        : 3
  Cones              : 0
  Scalar variables   : 4
  Matrix variables   : 0
  Integer variables  : 0

```

```
Optimizer started.
Interior-point optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Freed constraints in eliminator : 0
Eliminator terminated.
Eliminator    - tries               : 1                time                    : 0.00
Lin. dep.     - tries               : 1                time                    : 0.00
Lin. dep.     - number              : 0
Presolve terminated. Time: 0.00
Optimizer     - threads             : 2
Optimizer     - solved problem      : the primal
Optimizer     - Constraints         : 3
Optimizer     - Cones               : 0
Optimizer     - Scalar variables    : 6                conic                   : 0
Optimizer     - Semi-definite variables: 0             scalarized              : 0
Factor        - setup time          : 0.00             dense det. time         : 0.00
Factor        - ML order time       : 0.00             GP order time           : 0.00
Factor        - nonzeros before factor : 6            after factor            : 6
Factor        - dense dim.          : 0                flops                   : 1.06e+02
ITE PFEAS    DFEAS    GFEAS    PRSTATUS   POBJ              DOBJ              MU       TIME
0   8.0e+00  3.2e+00  3.5e+00  1.00e+00   1.000000000e+01   0.000000000e+00   1.0e+00  0.01
1   4.2e+00  2.5e+00  4.7e-01  0.00e+00   3.093970927e+01   2.766058702e+01   2.6e+00  0.01
2   4.2e-01  2.5e-01  4.6e-02  -1.82e-02  6.511676243e+01   6.308843559e+01   2.6e-01  0.01
3   3.6e-02  2.1e-02  3.9e-03  5.84e-01   8.096141239e+01   8.061962333e+01   2.2e-02  0.01
4   1.5e-05  9.1e-06  1.7e-06  9.43e-01   8.333280389e+01   8.333241803e+01   9.2e-06  0.01
5   1.5e-09  9.1e-10  1.7e-10  1.00e+00   8.333333328e+01   8.333333324e+01   9.2e-10  0.01
Basis identification started.
Primal basis identification phase started.
ITER      TIME
0         0.00
Primal basis identification phase terminated. Time: 0.00
Dual basis identification phase started.
ITER      TIME
0         0.00
Dual basis identification phase terminated. Time: 0.00
Basis identification terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.01.

Optimizer terminated. Time: 0.02

Interior-point solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333280e+01   nrm: 5e+01   Viol.  con: 1e-08   var: 0e+00
  Dual.    obj: 8.3333333242e+01   nrm: 4e+00   Viol.  con: 2e-10   var: 5e-09

Basic solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333333e+01   nrm: 5e+01   Viol.  con: 7e-15   var: 0e+00
  Dual.    obj: 8.3333333245e+01   nrm: 4e+00   Viol.  con: 2e-10   var: 5e-09

Optimizer summary
  Optimizer               -                     time: 0.02
    Interior-point        - iterations : 5      time: 0.01
      Basis identification -                    time: 0.00
        Primal            - iterations : 0      time: 0.00
        Dual              - iterations : 0      time: 0.00
```

```
        Clean primal      - iterations : 0        time: 0.00
        Clean dual        - iterations : 0        time: 0.00
    Simplex               -                       time: 0.00
      Primal simplex      - iterations : 0        time: 0.00
      Dual simplex        - iterations : 0        time: 0.00
    Mixed integer         - relaxations: 0        time: 0.00


Open file '/home/andrea/mosek/8/tools/examples/data/lo1.sol'
Start writing.
done writing. Time: 0.00


Open file '/home/andrea/mosek/8/tools/examples/data/lo1.bas'
Start writing.
done writing. Time: 0.00


Return code - 0   [MSK_RES_OK]
```

5.4 Solver Parameters

MOSEK comes with a large number of parameters that allows the user to tune the behavior of the optimizer. The typical settings which can be changed with solver parameters include:

- choice of the optimizer for linear problems,
- choice of primal/dual solver,
- turning presolve on/off,
- turning heuristics in the mixed-integer optimizer on/off,
- level of multi-threading,
- feasibility tolerances,
- solver termination criteria,
- behaviour of the license manager,

and more. All parameters have default settings which will be suitable for most typical users. Each parameter is identified by a unique string name and it can accept either integers or symbolic names, floating point values or symbolic strings. Please refer to Sec. 11.2 for the complete list of available solver parameters.

5.4.1 Setting from command line

Setting solver parameters is possible using the command line option `-d`. If multiple parameters must be specified, option `-d` must be repeated for each one. For example, the next command will switch off presolve, set a feasibility tolerance and solve the problem from lo1.opf:

```
mosek -d MSK_IPAR_PRESOLVE_USE MSK_OFF -d MSK_DPAR_INTPNT_TOL_PFEAS 1.0e-8 lo1.opf
```

5.4.2 Using the Parameter File

Solver parameters can also be set using a parameter file, for example:

```
BEGIN MOSEK
% This is a comment.
% The subsequent line tells MOSEK that an optimal
% basis should be computed by the interior-point optimizer.
MSK_IPAR_PRESOLVE_USE        MSK_OFF
MSK_DPAR_INTPNT_TOL_PFEAS    1.0e-9
END MOSEK
```

The syntax of the parameter file must obey a few simple rules:

- The file must begin with `BEGIN MOSEK` and end with `END MOSEK`.

- Empty lines and lines starting from a `%` sign are ignored.

- Each line contains a valid **MOSEK** parameter name followed by its value.

The parameter file can have any name. Assuming it has been called `mosek.par`, it can be used using the *-p* option as follows:

```
mosek -p mosek.par afiro.mps
```

Command-line parameters override those from the parameter file in case of repetition. For instance

```
mosek -p mosek.par -d MSK_DPAR_INTPNT_TOL_PFEAS 1.0e-8 afiro.mps
```

will set *MSK_DPAR_INTPNT_TOL_PFEAS* to 10^{-8} using the value provided on the command line.

5.5 Command Line Arguments

The following list shows the available command-line arguments for **MOSEK**:

-anapro
> Analyze the problem data.

-anasoli <name>
> Analyze the initial solution name e.g. `-anasoli bas`.

-anasolo <name>
> Analyze the final solution name e.g. `-anasolo itg`.

-a
> **MOSEK** is started in AMPL mode.

-basi <name>
> Input basic solution file name.

-baso <name>
> Output basic solution file name.

-d <name> <value>
> Define the value `value` for the **MOSEK** parameter `name`.

-dbgmem <name>
> Name of memory debug file.

-f
> Complete license information is printed.

-h, -?
> Help.

-inti <name>
> Input integer solution file name.

-into <name>
> Output integer solution file name.

-itri <name>
> Input interior point solution file name.

-itro <name>
> Output interior point solution file name.

-info <name>
> Infeasible subproblem output file name.

-infrepo <name>
> Feasibility reparation output file.

-l,-L <dir>
> `dir` is the directory where the **MOSEK** license file `mosek.lic` is located.

-max
> The problem is maximized.

-min
> The problem is minimized.

`-n`

      Ignore errors in subsequent parameter settings.

`-out <name>`

      Write the task to a data file named `name`. See Sec. 12.

`-p <name>, -pari <name>`

      Name of the input parameter file.

`-paro <name>`

      Name of the output parameter file.

`-primalrepair`

      Repair a primal infeasible problem. See Sec. 10.2.

`-r`

      If the option is present, the program returns -1 if an error occurred, otherwise 0.

`-removeitg`

      Removes all integer constraints after reading the problem.

`-rout <name>`

      If the option is present, the program writes the return code to file `name`.

`-q <name>`

      Name of an optional log file.

`-sen <file>`

      Perform sensitivity analysis based on file.

`-silent`

      As little information as possible is send to the terminal.

`-toconic`

      Translate to conic form after reading.

`-v`

      MOSEK version is printed and no optimization is performed.

`-w`

      If this options is on, then **MOSEK** will wait for a license.

`-x`

      Do not run the optimizer. Useful for converting between file formats.

`-=`

      List all possible solver parameters with default value, lower bound and upper bound (if applicable).

5.6 The license system

MOSEK is a commercial product that **always** needs a valid license to work. **MOSEK** uses a third party license manager to implement license checking. The number of license tokens provided determines the number of optimizations that can be run simultaneously.

    By default a license token remains checked out for the whole execution of the command line tool. If the license is not unlimited, then the number of tokens determines the maximal number of processes that can run simultaneously. In this case setting the license wait flag with the parameter *MSK_IPAR_LICENSE_WAIT* will force **MOSEK** to wait until a license token becomes available instead of returning with an error.

Chapter 6

The MOSEK-bundled AMPL shell

AMPL is a modeling language for specifying linear and nonlinear optimization models in a natural way. AMPL also makes it easy to solve the problem and e.g. display the solution or part of it. We will not discuss the specifics of the AMPL language here but instead refer the reader to *[FGK03]*, http://ampl.com/BOOK/download.html and the AMPL website http://www.ampl.com.

AMPL cannot solve optimization problems by itself but requires a link to an optimizer. The **MOSEK** distribution includes:

- An AMPL link which makes it possible to use **MOSEK** as an optimizer within AMPL. The link can be used from any AMPL shell.

- The full, official AMPL shell repackaged under the name `mampl`. This is sold as a separate product, and it can be hooked to other optimizers as well.

Note:

- To use **MOSEK** from AMPL you need to set up the system path to the **MOSEK** command line tool.

- It is possible to specify problems in AMPL that cannot be solved by **MOSEK**. The optimization problem must be a smooth convex optimization problem as discussed in Sec. 8.

For the remainder of this section we refer to the **MOSEK**-bundled `mampl` as the AMPL interpreter of choice. However, the tutorial applies also to any other standard AMPL shell available to the user.

6.1 Locating the AMPL shell

If `<MSKHOME>` is the folder in which the **MOSEK** Optimization Suite has been installed then the AMPL binary is located in

`<MSKHOME>/mosek/9.1/tools/platform/<PLATFORM>/bin/mampl`

for Linux and OSX users (`PLATFORM` must be among `linux64x86`, `osx64x86`), and under

`<MSKHOME>\mosek\9.1\tools\platform\<PLATFORM>\bin\mampl`

for Windows users (`PLATFORM` must be among `win32x86`, `win64x86`).

6.2 An example

In many instances, you can successfully apply **MOSEK** simply by specifying the model and data, setting the solver option to **MOSEK**, and typing `solve`.

Consider a simple linear optimization problem formulated as an AMPL model in Listing 6.1.

Listing 6.1: An example of an optimization problem in AMPL language.

```
set NUTR ordered;
set FOOD ordered;

param cost {FOOD} >= 0;
param f_min {FOOD} >= 0, default 0;
param f_max {j in FOOD} >= f_min[j], default Infinity;

param n_min {NUTR} >= 0, default 0;
param n_max {i in NUTR} >= n_min[i], default Infinity;

param amt {NUTR,FOOD} >= 0;

# ----------------------------------------------------------

var Buy {j in FOOD} >= f_min[j], <= f_max[j];

# ----------------------------------------------------------

minimize Total_Cost:  sum {j in FOOD} cost[j] * Buy[j];

minimize Nutr_Amt {i in NUTR}: sum {j in FOOD} amt[i,j] * Buy[j];

# ----------------------------------------------------------

subject to Diet {i in NUTR}:
   n_min[i] <= sum {j in FOOD} amt[i,j] * Buy[j] <= n_max[i];
```

We can specify the input data using an input file again following the AMPL syntax, as in Listing 6.2.

Listing 6.2: An example of data for an optimization problem using AMPL language.

```
param:  FOOD:                   cost  f_min  f_max :=
  "Quarter Pounder w/ Cheese"   1.84    .      .
  "McLean Deluxe w/ Cheese"     2.19    .      .
  "Big Mac"                     1.84    .      .
  "Filet-O-Fish"                1.44    .      .
  "McGrilled Chicken"           2.29    .      .
  "Fries, small"                 .77    .      .
  "Sausage McMuffin"            1.29    .      .
  "1% Lowfat Milk"               .60    .      .
  "Orange Juice"                 .72    .      . ;

param:  NUTR:    n_min  n_max :=
        Cal       2000    .
        Carbo      350    375
        Protein     55    .
        VitA       100    .
        VitC       100    .
        Calc       100    .
        Iron       100    . ;

param amt (tr):
                              Cal  Carbo Protein  VitA  VitC  Calc  Iron :=
  "Quarter Pounder w/ Cheese" 510    34    28      15     6    30    20
  "McLean Deluxe w/ Cheese"   370    35    24      15    10    20    20
  "Big Mac"                   500    42    25       6     2    25    20
  "Filet-O-Fish"              370    38    14       2     0    15    10
  "McGrilled Chicken"         400    42    31       8    15    15     8
```

```
"Fries, small"            220    26     3     0    15     0    2
"Sausage McMuffin"        345    27    15     4     0    20   15
"1% Lowfat Milk"          110    12     9    10     4    30    0
"Orange Juice"             80    20     1     2   120     2    2 ;
```

Invoke the AMPL shell:

```
mampl
```

and type in the commands:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: solve;
```

The resulting output is:

```
MOSEK finished.
Problem status    - PRIMAL_AND_DUAL_FEASIBLE
Solution status   - OPTIMAL
Primal objective  - 14.8557377
Dual objective    - 14.8557377


Objective = Total_Cost
```

6.3 Retrieving solutions

6.3.1 Status codes

The AMPL parameter `solve_result_num` is used to indicate the outcome of the optimization process. It is used as follows

```
ampl: display solve_result_num
```

Please refer to table Table 6.1 for possible values of this parameter.

Table 6.1: Interpretation of `solve_result_num`.

Value	Message
0	the solution is optimal.
100	suboptimal primal solution.
101	superoptimal (dual feasible) solution.
150	the solution is near optimal.
200	primal infeasible problem.
300	dual infeasible problem.
400	too many iterations.
500	solution status is unknown.
501	ill-posed problem, solution status is unknown.
> 501	Mapped **MOSEK** response code. See note below.

MOSEK response codes are mapped to AMPL return codes greater than 501. In order to get the actual response code the base value `501` must be subtracted. For example: the AMPL return code 502 corresponds to **MOSEK** response code 1.

6.3.2 Which solution is returned

MOSEK can produce three types of solutions: basic, interior point and integer. The solution returned to AMPL is determined according to the following rules:

- For problems containing integer variables only the integer solution is available and it is returned.

- For nonlinear problems only the interior point solution is available and it is returned.

- For linear problems, if both basic and interior point solution are available, then the basic solution is returned. Otherwise the only available solution is returned.

6.4 Optimizer options

6.4.1 The MOSEK parameter database

The **MOSEK** optimizer can be controller using solver parameters, as described in Sec. 5.4. These parameters can be modified within AMPL as shown in the example below:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex \
ampl? msk_ipar_sim_max_iterations = 100000';
ampl: solve;
```

In the example above a string called `mosek_options` is created which contains the parameter settings. Each parameter setting has the format

```
parameter_name = value
```

where `parameter_name` is a valid **MOSEK** parameter name. See Sec. 11.2 for a description of all valid **MOSEK** parameters.

An alternative way of specifying the parameters is

```
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex'
ampl? 'msk_ipar_sim_max_iterations = 100000';
```

New parameters can also be appended to an existing option string as shown below.

```
ampl: option mosek_options $mosek_options
ampl? ' msk_ipar_sim_print_freq = 0 msk_ipar_sim_max_iterations = 1000';
```

The expression `$mosek_options` expands to the current value of the option. Line two in the example appends an additional value `msk_ipar_sim_max_iterations` to the option string.

6.4.2 Options

MOSEK recognizes the following AMPL options.

outlev

Controls the amount of printed output. 0 means no printed output and a higher value means progressively more output. An example of setting `outlev` is as follows:

```
ampl: option mosek_options 'outlev=2';
```

wantsol

Controls the solution information generated when run in standalone mode (called without the argument `-AMPL`). It should be constructed as the sum of

1	to write a `.sol` file
2	to print the primal variable values
4	to print the dual variable values
8	to suppress printing the solution message

We refer the reader to the AMPL manual *[FGK03]* for more details.

6.4.3 Passing variable names to MOSEK

AMPL assigns meaningful names to all the constraints and variables. Since **MOSEK** uses item names in error and log messages, it may be useful to pass the AMPL names to **MOSEK**. This can be achieved with the command:

```
ampl: option auxfiles rc;
ampl: solve;
```

6.5 Hot-start

Frequently, a sequence of optimization problems is solved where each problem differs only slightly from the previous problem. In that case it may be advantageous to use the previous optimal solution to warm-start the optimizer. Such a facility is available in **MOSEK** only when the simplex optimizer is used.

The warm-start facility exploits the AMPL variable suffix `sstatus` to communicate the optimal basis back to AMPL, and AMPL uses this facility to communicate an initial basis to **MOSEK**. The following example demonstrates this feature.

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex outlev=2';
ampl: solve;
ampl: display Buy.sstatus;
ampl: solve;
```

The resulting output is:

```
Accepted: msk_ipar_optimizer                = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev                    = 2


Computer    - Platform             : Linux/64-X86
Computer    - CPU type             : Intel-P4
MOSEK       - task name            :
MOSEK       - objective sense      : min
MOSEK       - problem type         : LO (linear optimization problem)
MOSEK       - constraints          : 7               variables           : 9
MOSEK       - integer variables    : 0
Optimizer started.
Simplex optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Presolve    - Stk. size (kb) : 0
Eliminator - tries               : 0               time               : 0.00
Eliminator - elim's              : 0
Lin. dep.  - tries               : 1               time               : 0.00
Lin. dep.  - number              : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.
Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer  - solved problem       : the primal
Optimizer  - constraints          : 7               variables           : 9
Optimizer  - hotstart             : no
ITER      DEGITER(%) PFEAS       DFEAS       POBJ               DOBJ                       TIME␣
↪     TOTTIME
0         0.00      1.40e+03    NA          1.2586666667e+01   NA                         0.00␣
↪     0.01
```

```
3         0.00       0.00e+00    NA         1.4855737705e+01    NA                      0.00␣
→       0.01
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0  [MSK_RES_OK]
MOSEK finished.
Problem status    : PRIMAL_AND_DUAL_FEASIBLE
Solution status   : OPTIMAL
Primal objective  : 14.8557377
Dual objective    : 14.8557377


Objective = Total_Cost
Buy.sstatus [*] :=
'Quarter Pounder w/ Cheese'  bas
'McLean Deluxe w/ Cheese'  low
'Big Mac'  low
Filet-O-Fish  low
'McGrilled Chicken'  low
'Fries, small'  bas
'Sausage McMuffin'  low
'1% Lowfat Milk'  bas
'Orange Juice'  low
;
Accepted: msk_ipar_optimizer                = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev                            = 2
Basic solution
Problem status  : UNKNOWN
Solution status : UNKNOWN
Primal - objective: 1.4855737705e+01   eq. infeas.: 3.97e+03 max bound infeas.: 2.00e+03
Dual   - objective: 0.0000000000e+00   eq. infeas.: 7.14e-01 max bound infeas.: 0.00e+00


Computer   - Platform            : Linux/64-X86
Computer   - CPU type            : Intel-P4
MOSEK      - task name           :
MOSEK      - objective sense     : min
MOSEK      - problem type        : LO (linear optimization problem)
MOSEK      - constraints         : 7                variables            : 9
MOSEK      - integer variables   : 0
Optimizer started.
Simplex optimizer started.
Presolve started.
Presolve   - Stk. size (kb) : 0
Eliminator - tries               : 0                time                 : 0.00
Eliminator - elim's              : 0
Lin. dep.  - tries               : 0                time                 : 0.00
Lin. dep.  - number              : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.
Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer  - solved problem         : the primal
Optimizer  - constraints         : 7                variables            : 9
Optimizer  - hotstart            : yes
Optimizer  - Num. basic          : 7                Basis rank           : 7
Optimizer  - Valid bas. fac.     : no
ITER      DEGITER(%)  PFEAS       DFEAS      POBJ                DOBJ                    TIME␣
→      TOTTIME
0         0.00       0.00e+00    NA         1.4855737705e+01    NA                      0.00␣
→      0.01
0         0.00       0.00e+00    NA         1.4855737705e+01    NA                      0.00␣
→      0.01
```

```
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0  [MSK_RES_OK]
MOSEK finished.
Problem status    : PRIMAL_AND_DUAL_FEASIBLE
Solution status   : OPTIMAL
Primal objective  : 14.8557377
Dual objective    : 14.8557377


Objective = Total_Cost
```

Please note that the second solve takes fewer iterations since the previous optimal basis is reused.

6.6 Infeasibility report

For linear optimization problems without any integer constrained variables **MOSEK** can generate an infeasibility report automatically. The report provides important information about the infeasibility.

The generation of the infeasibility report is turned on using the parameter setting

```
option auxfiles rc;
option mosek_options 'msk_ipar_infeas_report_auto=msk_on';
```

For further details about infeasibility report see Sec. 10.2.

6.7 Sensitivity analysis

MOSEK can calculate sensitivity information for the objective and constraints. To enable sensitivity information set the option:

```
sensitivity = 1
```

Results are returned in variable/constraint suffixes as follows:

- `.down` Smallest value of objective coefficient/right hand side before the optimal basis changes.

- `.up` Largest value of objective coefficient/right hand side before the optimal basis changes.

- `.current` Current value of objective coefficient/right hand side.

For ranged constraints sensitivity information is returned only for the lower bound.
The example below returns sensitivity information on the `diet` model.

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options 'sensitivity=1';

ampl: solve;
#display sensitivity information and current solution.
ampl: display _var.down,_var.current,_var.up,_var;
#display sensitivity information and optimal dual values.
ampl: display _con.down,_con.current,_con.up,_con;
```

The resulting output is:

```
Return code - 0  [MSK_RES_OK]
MOSEK finished.
Problem status    : PRIMAL_AND_DUAL_FEASIBLE
Solution status   : OPTIMAL
Primal objective  : 14.8557377
```

```
Dual objective    : 14.8557377


suffix up OUT;
suffix down OUT;
suffix current OUT;
Objective = Total_Cost
: _var.down _var.current      _var.up       _var       :=
1  1.37385       1.84            1.86075   4.38525
2  1.8677        2.19     Infinity         0
3  1.82085       1.84     Infinity         0
4  1.35466       1.44     Infinity         0
5  1.57633       2.29     Infinity         0
6  0.094         0.77            0.794851  6.14754
7  1.22759       1.29     Infinity         0
8  0.57559       0.6             0.910769  3.42213
9  0.657279      0.72     Infinity         0
;
ampl: display _con.down,_con.current,_con.up,_con;
:     _con.down    _con.current    _con.up      _con        :=
1  -Infinity           2000      3965.37    0
2        297.6          350       375       0.0277049
3  -Infinity             55      172.029    0
4         63.0531       100      195.388    0.0267541
5  -Infinity            100      132.213    0
6  -Infinity            100      234.221    0
7         17.6923       100      142.821    0.0248361
;
```

6.8 Using the command line version of the AMPL interface

AMPL can generate a data file containing the optimization problem and all relevant information which can then be read and solved by the **MOSEK** command line tool.

When the problem has been loaded into AMPL, the commands

```
ampl: option auxfiles rc;
ampl: write  bprob;
```

will make AMPL write the appropriate data files, i.e.

```
prob.nl
prob.col
prob.row
```

Then the problem can be solved using the command line version of **MOSEK** as follows

```
mosek prob.nl outlev=10 -a
```

The option `-a` indicates that **MOSEK** is invoked in AMPL mode. When **MOSEK** is invoked in AMPL mode the standard **MOSEK** command line options should appear *after* the `-a` option except for the file name which should be the first argument. As the above example demonstrates **MOSEK** accepts command line options following the AMPL convention. To see which command line arguments **MOSEK** accepts in AMPL mode write:

```
mosek -= -a
```

For linear, quadratic and quadratically constrained problems a text file representation of the problem can be obtained by performing one of the following conversions:

```
mosek prob.nl -a -x -out prob.mps
mosek prob.nl -a -x -out prob.opf
mosek prob.nl -a -x -out prob.lp
```

6.9 amplpy

It is possible to use the **MOSEK**-bundled AMPL from `amplpy` (https://pypi.org/project/amplpy/). In order to do this rename `mampl` to `ampl` (or create a symbolic link) and initialize the `AMPL` object using the path to the **MOSEK** binaries folder, for example:

```
ampl = AMPL(Environment('somepath/mosek/current/tools/platform/linux64x86/bin'))
ampl.setOption('solver', 'mosek')

ampl.setOption('mosek_options', 'outlev=2 msk_ipar_num_threads=2')  # Example of parameter
↪setting
```

In case of problems with initializing the environment, try setting the system environment variable `LM_LICENSE_FILE` to the **MOSEK** license file path.

Chapter 7

Debugging Tutorials

This collection of tutorials contains basic techniques for debugging optimization problems using tools available in **MOSEK**: optimizer log, solution summary, infeasibility report, command-line tools. It is intended as a first line of technical help for issues such as: Why do I get solution status *unknown* and how can I fix it? Why is my model infeasible while it shouldn't be? Should I change some parameters? Can the model solve faster? etc.

The major steps when debugging a model are always:

- Consult the log output.

- Run the optimization and analyze the log output, see Sec. 7.1. In particular:

  - check if the problem setup (number of constraints/variables etc.) matches your expectation.
  - check solution summary and solution status.

- Dump the problem to disk if necessary to continue analysis.

  - use a human-readable text format, such as `*.opf` if you want to check the problem structure by hand. Assign names to variables and constraints to make them easier to identify.
  - use the **MOSEK** native format `*.task.gz` when submitting a bug report or support question.

- Fix problem setup, improve the model, locate infeasibility or adjust parameters, depending on the diagnosis.

See the following sections for details.

7.1 Understanding optimizer log

The optimizer produces a log which splits roughly into four sections:

1. summary of the input data,

2. presolve and other pre-optimize problem setup stages,

3. actual optimizer iterations,

4. solution summary.

In this tutorial we show how to analyze the most important parts of the log when initially debugging a model: input data (1) and solution summary (4). For the iterations log (3) see Sec. 9.3.4 or Sec. 9.4.8.

7.1.1 Input data

If **MOSEK** behaves very far from expectations it may be due to errors in problem setup. The log file will begin with a summary of the structure of the problem, which looks for instance like:

```
Problem
  Name                    :
  Objective sense         : max
  Type                    : CONIC (conic optimization problem)
  Constraints             : 20413
  Cones                   : 2508
  Scalar variables        : 20414
  Matrix variables        : 0
  Integer variables       : 0
```

This can be consulted to eliminate simple errors: wrong objective sense, wrong number of variables etc. Note that Fusion, and third-party modeling tools can introduce additional variables and constraints to the model. In the remaining **MOSEK** APIs the problem dimensions should match exactly what the user specified.

If this is not sufficient a bit more information can be obtained by dumping the problem to a file (see Sec. 7) and using the `anapro` option of any of the command line tools. This will produce a longer summary similar to:

```
** Variables
scalar: 20414      integer: 0         matrix: 0
low: 2082          up: 5014           ranged: 0          free: 12892        fixed: 426


** Constraints
all: 20413
low: 10028         up: 0              ranged: 0          free: 0            fixed: 10385


** Cones
QUAD: 1            dims: 2865: 1
RQUAD: 2507        dims: 3: 2507


** Problem data (numerics)
|c|                nnz: 10028         min=2.09e-05       max=1.00e+00
|A|                nnz: 597023        min=1.17e-10       max=1.00e+00
blx                fin: 2508          min=-3.60e+09      max=2.75e+05
bux                fin: 5440          min=0.00e+00       max=2.94e+08
blc                fin: 20413         min=-7.61e+05      max=7.61e+05
buc                fin: 10385         min=-5.00e-01      max=0.00e+00
```

Again, this can be used to detect simple errors, such as:

- Wrong type of cone was used or it has wrong dimension.

- The bounds for variables or constraints are incorrect or incomplete.

- The model is otherwise incomplete.

- Suspicious values of coefficients.

- For various data sizes the model does not scale as expected.

Finally saving the problem in a human-friendly text format such as LP or OPF (see Sec. 7) and analyzing it by hand can reveal if the model is correct.

Warnings and errors

At this stage the user can encounter warnings which should not be ignored, unless they are well-understood. They can also serve as hints as to numerical issues with the problem data. A typical warning of this kind is

```
MOSEK warning 53: A numerically large upper bound value  2.9e+08 is specified for variable
↪'absh[107]' (2613).
```

Warnings do not stop the problem setup. If, on the other hand, an error occurs then the model will become invalid. The user should make sure to test for errors/exceptions from all API calls that set up the problem and validate the data.

7.1.2 Solution summary

The last item in the log is the solution summary.

Continuous problem

Optimal solution

A typical solution summary for a continuous (linear, conic, quadratic) problem looks like:

```
Problem status  : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: 8.7560516107e+01   nrm: 1e+02   Viol.  con: 3e-12   var: 0e+00   cones: 3e-11
Dual.    obj: 8.7560521345e+01   nrm: 1e+00   Viol.  con: 5e-09   var: 9e-11   cones: 0e+00
```

It contains the following elements:

- Problem and solution status.

- A summary of the primal solution: objective value, infinity norm of the solution vector **xx**, maximal violations of constraints, variable bounds and cones. The violation of a linear constraint such as $a^T x \leq b$ is $\max(a^T x - b, 0)$. The violation of a conic constraint $x \in \mathcal{K}$ is the distance $\text{dist}(x, \mathcal{K})$.

- The same for the dual solution.

The features of the solution summary which characterize a very good and accurate solution and a well-posed model are:

- **Status:** The solution status is OPTIMAL.

- **Duality gap:** The primal and dual objective values are (almost) identical, which proves the solution is (almost) optimal.

- **Norms:** Ideally the norms of the solution and the objective values should not be too large. This of course depends on the input data, but a huge solution norm can be an indicator of issues with the scaling, conditioning and/or well-posedness of the model. It may also indicate that the problem is borderline between feasibility and infeasibility and sensitive to small perturbations in this respect.

- **Violations:** The violations are close to zero, which proves the solution is (almost) feasible. Observe that due to rounding errors it can be expected that the violations are proportional to the norm (nrm:) of the solution. It is rarely the case that violations are exactly zero.

Solution status UNKNOWN

A typical example with solution status UNKNOWN due to numerical problems will look like:

```
Problem status  : UNKNOWN
Solution status : UNKNOWN
Primal.  obj: 1.3821656824e+01   nrm: 1e+01   Viol.  con: 2e-03   var: 0e+00   cones: 0e+00
Dual.    obj: 3.0119004098e-01   nrm: 5e+07   Viol.  con: 4e-16   var: 1e-01   cones: 0e+00
```

Note that:

- The primal and dual objective are very different.

- The dual solution has very large norm.

- There are considerable violations so the solution is likely far from feasible.

Follow the hints in Sec. 7.2 to resolve the issue.

Solution status UNKNOWN with a potentially useful solution

Solution status `UNKNOWN` does not necessarily mean that the solution is completely useless. It only means that the solver was unable to make any more progress due to numerical difficulties, and it was not able to reach the accuracy required by the termination criteria (see Sec. 9.3.2). Consider for instance:

```
Problem status  : UNKNOWN
Solution status : UNKNOWN
Primal.  obj: 3.4531019648e+04    nrm: 1e+05    Viol.  con: 7e-02    var: 0e+00    cones: 0e+00
Dual.    obj: 3.4529720645e+04    nrm: 8e+03    Viol.  con: 1e-04    var: 2e-04    cones: 0e+00
```

Such a solution may still be useful, and it is always up to the user to decide. It may be a good enough approximation of the optimal point. For example, the large constraint violation may be due to the fact that one constraint contained a huge coefficient.

Infeasibility certificate

A primal infeasibility certificate is stored in the dual variables:

```
Problem status  : PRIMAL_INFEASIBLE
Solution status : PRIMAL_INFEASIBLE_CER
Dual.    obj: 2.9238975853e+02    nrm: 6e+02    Viol.  con: 0e+00    var: 1e-11    cones: 0e+00
```

It is a Farkas-type certificate as described in Sec. 8.2.2. In particular, for a good certificate:

- The dual objective is positive for a minimization problem, negative for a maximization problem. Ideally it is well bounded away from zero.

- The norm is not too big and the violations are small (as for a solution).

If the model was not expected to be infeasible, the likely cause is an error in the problem formulation. Use the hints in Sec. 7.1.1 and Sec. 7.3 to locate the issue.

Just like a solution, the infeasibility certificate can be of better or worse quality. The infeasibility certificate above is very solid. However, there can be less clear-cut cases, such as for example:

```
Problem status  : PRIMAL_INFEASIBLE
Solution status : PRIMAL_INFEASIBLE_CER
Dual.    obj: 1.6378689238e-06    nrm: 6e+05    Viol.  con: 7e-03    var: 2e-04    cones: 0e+00
```

This infeasibility certificate is more dubious because the dual objective is positive, but barely so in comparison with the large violations. It also has rather large norm. This is more likely an indication that the problem is borderline between feasibility and infeasibility or simply ill-posed and sensitive to tiny variations in input data. See Sec. 7.3 and Sec. 7.2.

The same remarks apply to dual infeasibility (i.e. unboundedness) certificates. Here the primal objective should be negative a minimization problem and positive for a maximization problem.

7.1.3 Mixed-integer problem

Optimal integer solution

For a mixed-integer problem there is no dual solution and a typical optimal solution report will look as follows:

```
Problem status  : PRIMAL_FEASIBLE
Solution status : INTEGER_OPTIMAL
Primal.  obj: 6.0111122960e+06    nrm: 1e+03    Viol.  con: 2e-13    var: 2e-14    itg: 5e-15
```

The interpretation of all elements is as for a continuous problem. The additional field `itg` denotes the maximum violation of an integer variable from being an exact integer.

Feasible integer solution

If the solver found an integer solution but did not prove optimality, for instance because of a time limit, the solution status will be `PRIMAL_FEASIBLE`:

```
Problem status   : PRIMAL_FEASIBLE
Solution status : PRIMAL_FEASIBLE
Primal.  obj: 6.0114607792e+06    nrm: 1e+03    Viol.  con: 2e-13    var: 2e-13    itg: 4e-15
```

In this case it is valuable to go back to the optimizer summary to see how good the best solution is:

```
31        35        1        0        6.0114607792e+06      6.0078960892e+06      0.06        4.1

Objective of best integer solution : 6.011460779193e+06
Best objective bound             : 6.007896089225e+06
```

In this case the best integer solution found has objective value `6.011460779193e+06`, the best proved lower bound is `6.007896089225e+06` and so the solution is guaranteed to be within 0.06% from optimum. The same data can be obtained as information items through an API. See also Sec. 9.4 for more details.

Infeasible problem

If the problem is declared infeasible the summary is simply

```
Problem status   : PRIMAL_INFEASIBLE
Solution status : UNKNOWN
Primal.  obj: 0.0000000000e+00    nrm: 0e+00    Viol.  con: 0e+00    var: 0e+00    itg: 0e+00
```

If infeasibility was not expected, consult Sec. 7.3.

7.2 Addressing numerical issues

The suggestions in this section should help diagnose and solve issues with numerical instability, in particular UNKNOWN solution status or solutions with large violations. Since numerically stable models tend to solve faster, following these hints can also dramatically shorten solution times.

We always recommend that issues of this kind are addressed by reformulating or rescaling the model, since it is the modeler who has the best insight into the structure of the problem and can fix the cause of the issue.

7.2.1 Formulating problems

Scaling

Make sure that all the data in the problem are of comparable orders of magnitude. This applies especially to the linear constraint matrix. Use Sec. 7.1.1 if necessary. For example a report such as

```
|A|              nnz: 597023    min=1.17e-6    max=2.21e+5
```

means that the ratio of largest to smallest elements in `A` is 10^{11}. In this case the user should rescale or reformulate the model to avoid such spread which makes it difficult for **MOSEK** to scale the problem internally. In many cases it may be possible to change the units, i.e. express the model in terms of rescaled variables (for instance work with millions of dollars instead of dollars, etc.).

Similarly, if the objective contains very different coefficients, say

$$\text{maximize } 10^{10}x + y$$

then it is likely to lead to inaccuracies. The objective will be dominated by the contribution from x and y will become insignificant.

Removing huge bounds

Never use a very large number as replacement for ∞. Instead define the variable or constraint as unbounded from below/above. Similarly, avoid artificial huge bounds if you expect they will not become tight in the optimal solution.

Avoiding linear dependencies

As much as possible try to avoid linear dependencies and near-linear dependencies in the model. See Example 7.3.

Avoiding ill-posedness

Avoid continuous models which are ill-posed: the solution space is degenerate, for example consists of a single point (technically, the Slater condition is not satisfied). In general, this refers to problems which are borderline between feasible and infeasible. See Example 7.1.

Scaling the expected solution

Try to formulate the problem in such a way that the expected solution (both primal and dual) is not very large. Consult the solution summary Sec. 7.1.2 to check the objective values or solution norms.

7.2.2 Further suggestions

Here are other simple suggestions that can help locate the cause of the issues. They can also be used as hints for how to tune the optimizer if fixing the root causes of the issue is not possible.

- Remove the objective and solve the feasibility problem. This can reveal issues with the objective.

- Change the objective or change the objective sense from minimization to maximization (if applicable). If the two objective values are almost identical, this may indicate that the feasible set is very small, possibly degenerate.

- Perturb the data, for instance bounds, very slightly, and compare the results.

- For linear problems: solve the problem using a different optimizer by setting the parameter `MSK_IPAR_OPTIMIZER` and compare the results.

- Force the optimizer to solve the primal/dual versions of the problem by setting the parameter `MSK_IPAR_INTPNT_SOLVE_FORM` or `MSK_IPAR_SIM_SOLVE_FORM`. **MOSEK** has a heuristic to decide whether to dualize, but for some problems the guess is wrong an explicit choice may give better results.

- Solve the problem without presolve or some of its parts by setting the parameter `MSK_IPAR_PRESOLVE_USE`, see Sec. 9.1.

- Use different numbers of threads (`MSK_IPAR_NUM_THREADS`) and compare the results. Very different results indicate numerical issues resulting from round-off errors.

If the problem was dumped to a file, experimenting with various parameters is facilitated with the **MOSEK** Command Line Tool or **MOSEK** Python Console Sec. 7.4.

7.2.3 Typical pitfalls

Example 7.1 (Ill-posedness). A toy example of this situation is the feasibility problem

$$(x - 1)^2 \leq 1, \ (x + 1)^2 \leq 1$$

whose only solution is $x = 0$ and moreover replacing any 1 on the right hand side by $1 - \varepsilon$ makes the problem infeasible and replacing it by $1 + \varepsilon$ yields a problem whose solution set is an interval (fully-dimensional). This is an example of ill-posedness.

Example 7.2 (Huge solution). If the norm of the expected solution is very large it may lead to numerical issues or infeasibility. For example the problem

$$(10^{-4}, x, 10^3) \in \mathcal{Q}_r^3$$

may be declared infeasible because the expected solution must satisfy $x \geq 5 \cdot 10^9$.

Example 7.3 (Near linear dependency). Consider the following problem:

$$
\begin{array}{rrrrrrl}
\text{minimize} & & & & & & \\
\text{subject to} & x_1 & + & x_2 & & & = & 1, \\
& & & & x_3 & + & x_4 & = & 1, \\
& - & x_1 & & & - & x_3 & & = & -1 + \varepsilon, \\
& & & - & x_2 & & & - & x_4 & = & -1, \\
& & x_1, & & x_2, & & x_3, & & x_4 & \geq & 0.
\end{array}
$$

If we add the equalities together we obtain:

$$0 = \varepsilon$$

which is infeasible for any $\varepsilon \neq 0$. Here infeasibility is caused by a linear dependency in the constraint matrix coupled with a precision error represented by the ε. Indeed if a problem contains linear dependencies then the problem is either infeasible or contains redundant constraints. In the above case any of the equality constraints can be removed while not changing the set of feasible solutions. To summarize linear dependencies in the constraints can give rise to infeasible problems and therefore it is better to avoid them.

Example 7.4 (Presolving very tight bounds). Next consider the problem

$$
\begin{array}{rrll}
\text{minimize} & & & \\
\text{subject to} & x_1 - 0.01x_2 & = & 0, \\
& x_2 - 0.01x_3 & = & 0, \\
& x_3 - 0.01x_4 & = & 0, \\
& x_1 & \geq & -10^{-9}, \\
& x_1 & \leq & 10^{-9}, \\
& x_4 & \geq & 10^{-4}.
\end{array}
$$

Now the **MOSEK** presolve will, for the sake of efficiency, fix variables (and constraints) that have tight bounds where tightness is controlled by the parameter `MSK_DPAR_PRESOLVE_TOL_X`. Since the bounds

$$-10^{-9} \leq x_1 \leq 10^{-9}$$

are tight, presolve will set $x_1 = 0$. It easy to see that this implies $x_4 = 0$, which leads to the incorrect conclusion that the problem is infeasible. However a tiny change of the value 10^{-9} makes the problem feasible. In general it is recommended to avoid ill-posed problems, but if that is not possible then one solution is to reduce parameters such as `MSK_DPAR_PRESOLVE_TOL_X` to say 10^{-10}. This will at least make sure that presolve does not make the undesired reduction.

7.3 Debugging infeasibility

This section contains hints for debugging problems that are unexpectedly infeasible. It is always a good idea to remove the objective, i.e. only solve a feasibility problem when debugging such issues.

7.3.1 Numerical issues

Infeasible problem status may be just an artifact of numerical issues appearing when the problem is badly-scaled, barely feasible or otherwise ill-conditioned so that it is unstable under small perturbations of the data or round-off errors. This may be visible in the solution summary if the infeasibility certificate has poor quality. See Sec. 7.1.2 for how to diagnose that and Sec. 7.2 for possible hints. Sec. 7.2.3 contains examples of situations which may lead to infeasibility for numerical reasons.

We refer to Sec. 7.2 for further information on dealing with those sort of issues. For the rest of this section we concentrate on the case when the solution summary leaves little doubt that the problem solved by the optimizer actually is infeasible.

7.3.2 Locating primal infeasibility

As an example of a primal infeasible problem consider minimizing the cost of transportation between a number of production plants and stores: Each plant produces a fixed number of goods, and each store has a fixed demand that must be met. Supply, demand and cost of transportation per unit are given in Fig. 7.1.

Fig. 7.1: Supply, demand and cost of transportation.

The problem represented in Fig. 7.1 is infeasible, since the total demand

$$2300 = 1100 + 200 + 500 + 500$$

exceeds the total supply

$$2200 = 200 + 1000 + 1000$$

If we denote the number of transported goods from plant i to store j by x_{ij}, the problem can be formulated as the LP:

$$
\begin{array}{rlcccccccccc}
\text{minimize} & & x_{11} & + & 2x_{12} & + & 5x_{23} & + & 2x_{24} & + & x_{31} & + & 2x_{33} & + & x_{34} & & \\
\text{subject to} & s_0: & x_{11} & + & x_{12} & & & & & & & & & & & \leq & 200, \\
& s_1: & & & & & x_{23} & + & x_{24} & & & & & & & \leq & 1000, \\
& s_2: & & & & & & & & & x_{31} & + & x_{33} & + & x_{34} & \leq & 1000, \\
& d_1: & x_{11} & & & & & & & + & x_{31} & & & & & = & 1100, \\
& d_2: & & & x_{12} & & & & & & & & & & & = & 200, \\
& d_3: & & & & & x_{23} & + & & & & & x_{33} & & & = & 500, \\
& d_4: & & & & & & & x_{24} & + & & & & & x_{34} & = & 500, \\
& & & & & & & & & & & & & & x_{ij} & \geq & 0.
\end{array}
$$

(7.1)

Solving problem (7.1) using **MOSEK** will result in an infeasibility status. The infeasibility certificate is contained in the dual variables an can be accessed from an API. The variables and constraints with nonzero solution values form an infeasible subproblem, which frequently is very small. See Sec. 8.1.2 or Sec. 8.2.2 for detailed specifications of infeasibility certificates.

A short infeasibility report can also be printed to the log stream. It can be turned on by setting the parameter `MSK_IPAR_INFEAS_REPORT_AUTO` to `MSK_ON`. This causes **MOSEK** to print a report on variables and constraints which are involved in infeasibility in the above sense, i.e. have nonzero values in the certificate. The parameter `MSK_IPAR_INFEAS_REPORT_LEVEL` controls the amount of information presented in the infeasibility report. The default value is 1. For the above example the report is

```
MOSEK PRIMAL INFEASIBILITY REPORT.

Problem status: The problem is primal infeasible

The following constraints are involved in the primal infeasibility.

Index    Name     Lower bound      Upper bound      Dual lower       Dual upper
0        s0       NONE             2.000000e+002    0.000000e+000    1.000000e+000
2        s2       NONE             1.000000e+003    0.000000e+000    1.000000e+000
3        d1       1.100000e+003    1.100000e+003    1.000000e+000    0.000000e+000
4        d2       2.000000e+002    2.000000e+002    1.000000e+000    0.000000e+000

The following bound constraints are involved in the infeasibility.

Index    Name     Lower bound      Upper bound      Dual lower       Dual upper
8        x33      0.000000e+000    NONE             1.000000e+000    0.000000e+000
10       x34      0.000000e+000    NONE             1.000000e+000    0.000000e+000
```

The infeasibility report is divided into two sections corresponding to constraints and variables. It is a selection of those lines from the problem solution which are important in understanding primal infeasibility. In this case the constraints s0, s2, d1, d2 and variables x33, x34 are of importance because of nonzero dual values. The columns `Dual lower` and `Dual upper` contain the values of dual variables s_l^c, s_u^c, s_l^x and s_u^x in the primal infeasibility certificate (see Sec. 8.1.2).

In our example the certificate means that an appropriate linear combination of constraints s0, s1 with coefficient $s_u^c = 1$, constraints d1 and d2 with coefficient $s_u^c - s_l^c = 0 - 1 = -1$ and lower bounds on x33 and x34 with coefficient $-s_l^x = -1$ gives a contradiction. Indeed, the combination of the four involved constraints is $x_{33} + x_{34} \leq -100$ (as indicated in the introduction, the difference between supply and demand).

It is also possible to extract the infeasible subproblem with the command-line tool. For an infeasible problem called **infeas.lp** the command:

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON infeas.lp -info rinfeas.lp
```

will produce the file **rinfeas.bas.inf.lp** which contains the infeasible subproblem. Because of its size it may be easier to work with than the original problem file.

Returning to the transportation example, we discover that removing the fifth constraint $x_{12} = 200$ makes the problem feasible. Almost all undesired infeasibilities should be fixable at the modeling stage.

7.3.3 Locating dual infeasibility

A problem may also be *dual infeasible*. In this case the primal problem is usually unbounded, meaning that feasible solutions exists such that the objective tends towards infinity. For example, consider the problem

$$
\begin{array}{ll}
\text{maximize} & 200y_1 + 1000y_2 + 1000y_3 + 1100y_4 + 200y_5 + 500y_6 + 500y_7 \\
\text{subject to} & y_1 + y_4 \leq 1, \ y_1 + y_5 \leq 2, \ y_2 + y_6 \leq 5, \ y_2 + y_7 \leq 2, \\
& y_3 + y_4 \leq 1, \ y_3 + y_6 \leq 2, \ y_3 + y_7 \leq 1 \\
& y_1, y_2, y_3 \leq 0
\end{array}
$$

which is dual to (7.1) (and therefore is dual infeasible). The dual infeasibility report may look as follows:

```
MOSEK DUAL INFEASIBILITY REPORT.

Problem status: The problem is dual infeasible

The following constraints are involved in the infeasibility.

Index    Name           Activity          Objective        Lower bound      Upper bound
5        x33            -1.000000e+00                       NONE             2.000000e+00
6        x34            -1.000000e+00                       NONE             1.000000e+00


The following variables are involved in the infeasibility.

Index    Name           Activity          Objective        Lower bound      Upper bound
0        y1             -1.000000e+00     2.000000e+02      NONE             0.000000e+00
2        y3             -1.000000e+00     1.000000e+03      NONE             0.000000e+00
3        y4             1.000000e+00      1.100000e+03      NONE             NONE
4        y5             1.000000e+00      2.000000e+02      NONE             NONE

Interior-point solution summary
  Problem status  : DUAL_INFEASIBLE
  Solution status : DUAL_INFEASIBLE_CER
  Primal.  obj: 1.0000000000e+02    nrm: 1e+00    Viol.  con: 0e+00    var: 0e+00
```

In the report we see that the variables y1, y3, y4, y5 and two constraints contribute to infeasibility with non-zero values in the `Activity` column. Therefore

$$(y_1, \ldots, y_7) = (-1, 0, -1, 1, 1, 0, 0)$$

is the dual infeasibility certificate as in Sec. 8.1.2. This just means, that along the ray

$$(0, 0, 0, 0, 0, 0, 0) + t(y_1, \ldots, y_7) = (-t, 0, -t, t, t, 0, 0), \ t > 0,$$

which belongs to the feasible set, the objective value $100t$ can be arbitrarily large, i.e. the problem is unbounded.

In the example problem we could

- Add a lower bound on y3. This will directly invalidate the certificate of dual infeasibility.

- Increase the objective coefficient of y3. Changing the coefficients sufficiently will invalidate the inequality $c^T y^* > 0$ and thus the certificate.

7.3.4 Suggestions

Primal infeasibility

When trying to understand what causes the unexpected primal infeasible status use the following hints:

- Remove the objective function. This does not change the infeasibility status but simplifies the problem, eliminating any possibility of issues related to the objective function.

- Remove cones, semidefinite variables and integer constraints. Solve only the linear part of the problem. Typical simple modeling errors will lead to infeasibility already at this stage.

- Consider whether your problem has some obvious necessary conditions for feasibility and examine if these are satisfied, e.g. total supply should be greater than or equal to total demand.

- Verify that coefficients and bounds are reasonably sized in your problem.

- See if there are any obvious contradictions, for instance a variable is bounded both in the variables and constraints section, and the bounds are contradictory.

- Consider replacing suspicious equality constraints by inequalities. For instance, instead of $x_{12} = 200$ see what happens for $x_{12} \geq 200$ or $x_{12} \leq 200$.

- Relax bounds of the suspicious constraints or variables.

- For integer problems, remove integrality constraints on some/all variables and see if the problem solves.

- Form an **elastic model**: allow to violate constraints at a cost. Introduce slack variables and add them to the objective as penalty. For instance, suppose we have a constraint

$$\begin{aligned} \text{minimize} \quad & c^T x, \\ \text{subject to} \quad & a^T x \leq b. \end{aligned}$$

which might be causing infeasibility. Then create a new variable y and form the problem which contains:

$$\begin{aligned} \text{minimize} \quad & c^T x + y, \\ \text{subject to} \quad & a^T x \leq b + y. \end{aligned}$$

Solving this problem will reveal by how much the constraint needs to be relaxed in order to become feasible. This is equivalent to inspecting the infeasibility certificate but may be more intuitive.

- If you think you have a feasible solution or its part, fix all or some of the variables to those values. Presolve will propagate them through the model and potentially reveal more localized sources of infeasibility.

- Dump the problem in OPF or LP format and verify that the problem that was passed to the optimizer corresponds to the problem expressed in the high-level modeling language, if any such was used.

Dual infeasibility

When trying to understand what causes the unexpected dual infeasible status use the following hints:

- Verify that the objective coefficients are reasonably sized.

- Check if no bounds and constraints are missing, for example if all variables that should be nonnegative have been declared as such etc.

- Strengthen bounds of the suspicious constraints or variables.

- Form an series of models with decreasing bounds on the objective, that is, instead of objective

$$\text{minimize } c^T x$$

solve the problem with an additional constraint such as

$$c^T x = -10^5$$

and inspect the solution to figure out the mechanism behind arbitrarily decreasing objective values. This is equivalent to inspecting the infeasibility certificate but may be more intuitive.

- Dump the problem in OPF or LP format and verify that the problem that was passed to the optimizer corresponds to the problem expressed in the high-level modeling language, if any such was used.

Please note that modifying the problem to invalidate the reported certificate does *not* imply that the problem becomes feasible — the reason for infeasibility may simply *move*, resulting a problem that is still infeasible, but for a different reason. More often, the reported certificate can be used to give a hint about errors or inconsistencies in the model that produced the problem.

7.4 Python Console

The **MOSEK** Python Console is an alternative to the **MOSEK** Command Line Tool. It can be used for interactive loading, solving and debugging optimization problems stored in files, for example **MOSEK** task files. It facilitates debugging techniques described in Sec. 7.

7.4.1 Usage

The tool requires Python 2 or 3. The **MOSEK** interface for Python must be installed following the installation instructions for Python API or Python Fusion API. In the basic case it should be sufficient to execute the script

```
python setup.py install --user
```

in the directory containing the **MOSEK** Python module.

The Python Console is contained in the file `mosekconsole.py` in the folder with **MOSEK** binaries. It can be copied to an arbitrary location. The file is also available for `download here` (`mosekconsole.py`).

To run the console in interactive mode use

```
python mosekconsole.py
```

To run the console in batch mode provide a semicolon-separated list of commands as the second argument of the script, for example:

```
python mosekconsole.py "read data.task.gz; solve form=dual; writesol data"
```

The script is written using the **MOSEK** Python API and can be extended by the user if more specific functionality is required. We refer to the documentation of the Python API.

7.4.2 Examples

To read a problem from `data.task.gz`, solve it, and write solutions to `data.sol`, `data.bas` or `data.itg`:

```
read data.task.gz; solve; writesol data
```

To convert between file formats:

```
read data.task.gz; write data.mps
```

To set a parameter before solving:

```
read data.task.gz; param INTPNT_CO_TOL_DFEAS 1e-9; solve"
```

To list parameter values related to the mixed-integer optimizer in the task file:

```
read data.task.gz; param MIO
```

To print a summary of problem structure:

```
read data.task.gz; anapro
```

To solve a problem forcing the dual and switching off presolve:

```
read data.task.gz; solve form=dual presolve=no
```

To write an infeasible subproblem to a file for debugging purposes:

```
read data.task.gz; solve; infsub; write inf.opf
```

7.4.3 Full list of commands

Below is a brief description of all the available commands. Detailed information about a specific command `cmd` and its options can be obtained with

```
help cmd
```

Table 7.1: List of commands of the MOSEK Python Console.

Command	Description
help [command]	Print list of commands or info about a specific command
log filename	Save the session to a file
intro	Print MOSEK splashscreen
testlic	Test the license system
read filename	Load problem from file
reread	Reload last problem file
solve [options]	Solve current problem
write filename	Write current problem to file
param [name [value]]	Set a parameter or get parameter values
paramdef	Set all parameters to default values
info [name]	Get an information item
anapro	Analyze problem data
hist	Plot a histogram of problem data
histsol	Plot a histogram of the solutions
spy	Plot the sparsity pattern of the A matrix
truncate epsilon	Truncate small coefficients down to 0
anasol	Analyze solutions
removeitg	Remove integrality constraints
infsub	Replace current problem with its infeasible subproblem
writesol basename	Write solution(s) to file(s) with given basename
delsol	Remove all solutions from the task
exit	Leave

Chapter 8

Problem Formulation and Solutions

In this chapter we will discuss the following issues:

- The formal, mathematical formulations of the problem types that **MOSEK** can solve and their duals.

- The solution information produced by **MOSEK**.

- The infeasibility certificate produced by **MOSEK** if the problem is infeasible.

For the underlying mathematical concepts, derivations and proofs see the Modeling Cookbook or any book on convex optimization. This chapter explains how the related data is organized specifically within the **MOSEK** API.

8.1 Linear Optimization

MOSEK accepts linear optimization problems of the form

$$
\begin{array}{lrcl}
\text{minimize} & & c^T x + c^f & \\
\text{subject to} & l^c \leq & Ax & \leq u^c, \\
& l^x \leq & x & \leq u^x,
\end{array}
\tag{8.1}
$$

where

- m is the number of constraints.

- n is the number of decision variables.

- $x \in \mathbb{R}^n$ is a vector of decision variables.

- $c \in \mathbb{R}^n$ is the linear part of the objective function.

- $c^f \in \mathbb{R}$ is a constant term in the objective

- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.

- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.

- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.

- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.

- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.

Lower and upper bounds can be infinite, or in other words the corresponding bound may be omitted.

A primal solution (x) is *(primal) feasible* if it satisfies all constraints in (8.1). If (8.1) has at least one primal feasible solution, then (8.1) is said to be (primal) feasible. In case (8.1) does not have a feasible solution, the problem is said to be *(primal) infeasible*

8.1.1 Duality for Linear Optimization

Corresponding to the primal problem (8.1), there is a dual problem

$$
\begin{array}{ll}
\text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\
& A^T y + s_l^x - s_u^x = c, \\
\text{subject to} & -y + s_l^c - s_u^c = 0, \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0.
\end{array}
\tag{8.2}
$$

If a bound in the primal problem is plus or minus infinity, the corresponding dual variable is fixed at 0, and we use the convention that the product of the bound value and the corresponding dual variable is 0. This is equivalent to removing variable $(s_l^x)_j$ from the dual problem. In other words:

$$
l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0 \text{ and } l_j^x \cdot (s_l^x)_j = 0.
$$

A solution

$$
(y, s_l^c, s_u^c, s_l^x, s_u^x)
$$

to the dual problem is feasible if it satisfies all the constraints in (8.2). If (8.2) has at least one feasible solution, then (8.2) is *(dual) feasible*, otherwise the problem is *(dual) infeasible*.

A solution

$$
(x^*, y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)
$$

is denoted a *primal-dual feasible solution*, if (x^*) is a solution to the primal problem (8.1) and $(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$ is a solution to the corresponding dual problem (8.2). We also define an auxiliary vector

$$
(x^c)^* := Ax^*
$$

containing the activities of linear constraints.

For a primal-dual feasible solution we define the *duality gap* as the difference between the primal and the dual objective value,

$$
\begin{aligned}
& c^T x^* + c^f - \left\{ (l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* + c^f \right\} \\
& = \sum_{i=0}^{m-1} \left[(s_l^c)_i^* ((x_i^c)^* - l_i^c) + (s_u^c)_i^* (u_i^c - (x_i^c)^*) \right] \\
& + \sum_{j=0}^{n-1} \left[(s_l^x)_j^* (x_j - l_j^x) + (s_u^x)_j^* (u_j^x - x_j^*) \right] \geq 0
\end{aligned}
\tag{8.3}
$$

where the first relation can be obtained by transposing and multiplying the dual constraints (8.2) by x^* and $(x^c)^*$ respectively, and the second relation comes from the fact that each term in each sum is nonnegative. It follows that the primal objective will always be greater than or equal to the dual objective.

It is well-known that a linear optimization problem has an optimal solution if and only if there exist feasible primal-dual solution so that the duality gap is zero, or, equivalently, that the *complementarity conditions*

$$
\begin{array}{rcll}
(s_l^c)_i^* ((x_i^c)^* - l_i^c) & = & 0, & i = 0, \ldots, m-1, \\
(s_u^c)_i^* (u_i^c - (x_i^c)^*) & = & 0, & i = 0, \ldots, m-1, \\
(s_l^x)_j^* (x_j^* - l_j^x) & = & 0, & j = 0, \ldots, n-1, \\
(s_u^x)_j^* (u_j^x - x_j^*) & = & 0, & j = 0, \ldots, n-1,
\end{array}
$$

are satisfied.

If (8.1) has an optimal solution and **MOSEK** solves the problem successfully, both the primal and dual solution are reported, including a status indicating the exact state of the solution.

8.1.2 Infeasibility for Linear Optimization

Primal Infeasible Problems

If the problem (8.1) is infeasible (has no feasible solution), **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the modified dual problem

$$
\begin{aligned}
\text{maximize} \quad & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\
\text{subject to} \quad & \\
& A^T y + s_l^x - s_u^x = 0, \\
& -y + s_l^c - s_u^c = 0, \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0,
\end{aligned} \tag{8.4}
$$

such that the objective value is strictly positive, i.e. a solution

$$
(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)
$$

to (8.4) so that

$$
(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* > 0.
$$

Such a solution implies that (8.4) is unbounded, and that (8.1) is infeasible.

Dual Infeasible Problems

If the problem (8.2) is infeasible (has no feasible solution), **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the modified primal problem

$$
\begin{aligned}
\text{minimize} \quad & c^T x \\
\text{subject to} \quad & \hat{l}^c \leq Ax \leq \hat{u}^c, \\
& \hat{l}^x \leq x \leq \hat{u}^x,
\end{aligned} \tag{8.5}
$$

where

$$
\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}
$$

and

$$
\hat{l}_j^x = \left\{ \begin{array}{ll} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_j^x := \left\{ \begin{array}{ll} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}
$$

such that

$$
c^T x < 0.
$$

Such a solution implies that (8.5) is unbounded, and that (8.2) is infeasible.

In case that both the primal problem (8.1) and the dual problem (8.2) are infeasible, **MOSEK** will report only one of the two possible certificates — which one is not defined (**MOSEK** returns the first certificate found).

8.1.3 Minimalization vs. Maximalization

When the objective sense of problem (8.1) is maximization, i.e.

$$
\begin{aligned}
\text{maximize} \quad & c^T x + c^f \\
\text{subject to} \quad l^c \leq \quad & Ax \quad \leq u^c, \\
l^x \leq \quad & x \quad \leq u^x,
\end{aligned}
$$

the objective sense of the dual problem changes to minimization, and the domain of all dual variables changes sign in comparison to (8.2). The dual problem thus takes the form

$$
\begin{aligned}
\text{minimize} \quad & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\
\text{subject to} \quad & \\
& A^T y + s_l^x - s_u^x = c, \\
& -y + s_l^c - s_u^c = 0, \\
& s_l^c, s_u^c, s_l^x, s_u^x \leq 0.
\end{aligned}
$$

This means that the duality gap, defined in (8.3) as the primal minus the dual objective value, becomes nonpositive. It follows that the dual objective will always be greater than or equal to the primal objective. The primal infeasibility certificate will be reported by **MOSEK** as a solution to the system

$$
\begin{aligned}
A^T y + s_l^x - s_u^x &= 0, \\
-y + s_l^c - s_u^c &= 0, \\
s_l^c, s_u^c, s_l^x, s_u^x &\leq 0,
\end{aligned}
\tag{8.6}
$$

such that the objective value is strictly negative

$$
(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* < 0.
$$

Similarly, the certificate of dual infeasibility is an x satisfying the requirements of (8.5) such that $c^T x > 0$.

8.2 Conic Optimization

Conic optimization is an extension of linear optimization (see Sec. 8.1) allowing conic domains to be specified for subsets of the problem variables. A conic optimization problem to be solved by **MOSEK** can be written as

$$
\begin{array}{lrcll}
\text{minimize} & & c^T x + c^f & & \\
\text{subject to} & l^c \leq & Ax & \leq & u^c, \\
& l^x \leq & x & \leq & u^x, \\
& & x \in \mathcal{K}, & &
\end{array}
\tag{8.7}
$$

where

- m is the number of constraints.

- n is the number of decision variables.

- $x \in \mathbb{R}^n$ is a vector of decision variables.

- $c \in \mathbb{R}^n$ is the linear part of the objective function.

- $c^f \in \mathbb{R}$ is a constant term in the objective

- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.

- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.

- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.

- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.

- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.

Lower and upper bounds can be infinite, or in other words the corresponding bound may be omitted.

The set $\mathcal{K}$ is a Cartesian product of convex cones, namely $\mathcal{K} = \mathcal{K}_1 \times \cdots \times \mathcal{K}_p$. Having the domain restriction $x \in \mathcal{K}$, is thus equivalent to

$$
x^t \in \mathcal{K}_t \subseteq \mathbb{R}^{n_t},
$$

where $x = (x^1, \ldots, x^p)$ is a partition of the problem variables. Please note that the n-dimensional Euclidean space $\mathbb{R}^n$ is a cone itself, so simple linear variables are still allowed. The user only needs to specify subsets of variables which belong to non-trivial cones.

In this section we discuss the formulations which apply to the following cones supported by **MOSEK**:

- The set $\mathbb{R}^n$.

- The zero cone $\{(0, \ldots, 0)\}$.

- Quadratic cone

$$\mathcal{Q}^n = \left\{ x \in \mathbb{R}^n : x_1 \geq \sqrt{\sum_{j=2}^{n} x_j^2} \right\}.$$

- Rotated quadratic cone

$$\mathcal{Q}_r^n = \left\{ x \in \mathbb{R}^n : 2x_1 x_2 \geq \sum_{j=3}^{n} x_j^2, \quad x_1 \geq 0, \quad x_2 \geq 0 \right\}.$$

- Primal exponential cone

$$K_{\exp} = \left\{ x \in \mathbb{R}^3 : x_1 \geq x_2 \exp(x_3/x_2), \quad x_1, x_2 \geq 0 \right\}$$

as well as its dual

$$K_{\exp}^* = \left\{ x \in \mathbb{R}^3 : x_1 \geq -x_3 e^{-1} \exp(x_2/x_3), \quad x_3 \leq 0, x_1 \geq 0 \right\}.$$

- Primal power cone (with parameter $0 < \alpha < 1$)

$$\mathcal{P}_n^{\alpha,1-\alpha} = \left\{ x \in \mathbb{R}^n : x_1^\alpha x_2^{1-\alpha} \geq \sqrt{\sum_{j=3}^{n} x_j^2}, \quad x_1, x_2 \geq 0 \right\}$$

as well as its dual

$$(\mathcal{P}_n^{\alpha,1-\alpha})^* = \left\{ x \in \mathbb{R}^n : \left(\frac{x_1}{\alpha}\right)^\alpha \left(\frac{x_2}{1-\alpha}\right)^{1-\alpha} \geq \sqrt{\sum_{j=3}^{n} x_j^2}, \quad x_1, x_2 \geq 0 \right\}.$$

MOSEK supports also the cone of positive semidefinite matrices. Since that is handled through a separate interface, we discuss it in Sec. 8.3.

8.2.1 Duality for Conic Optimization

Corresponding to the primal problem (8.7), there is a dual problem

$$
\begin{aligned}
\text{maximize} \quad & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\
\text{subject to} \quad & \\
& A^T y + s_l^x - s_u^x + s_n^x = c \\
& -y + s_l^c - s_u^c = 0, \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\
& s_n^x \in \mathcal{K}^*,
\end{aligned}
\tag{8.8}
$$

where the dual cone $\mathcal{K}^*$ is a Cartesian product of the cones dual to $\mathcal{K}_t$. In practice this means that s_n^x has one entry for each entry in x. Please note that the dual problem of the dual problem is identical to the original primal problem.

If a bound in the primal problem is plus or minus infinity, the corresponding dual variable is fixed at 0, and we use the convention that the product of the bound value and the corresponding dual variable is 0. This is equivalent to removing variable $(s_l^x)_j$ from the dual problem. In other words:

$$l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0 \text{ and } l_j^x \cdot (s_l^x)_j = 0.$$

A solution

$$(y, s_l^c, s_u^c, s_l^x, s_u^x, s_n^x)$$

to the dual problem is feasible if it satisfies all the constraints in (8.8). If (8.8) has at least one feasible solution, then (8.8) is *(dual) feasible*, otherwise the problem is *(dual) infeasible*.

A solution

$$(x^*, y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*, (s_n^x)^*)$$

is denoted a *primal-dual feasible solution*, if (x^*) is a solution to the primal problem (8.7) and $(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*, (s_n^x)^*)$ is a solution to the corresponding dual problem (8.8). We also define an auxiliary vector

$$(x^c)^* := Ax^*$$

containing the activities of linear constraints.

For a primal-dual feasible solution we define the *duality gap* as the difference between the primal and the dual objective value,

$$
\begin{aligned}
&c^T x^* + c^f - \left\{ (l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* + c^f \right\} \\
&= \sum_{i=0}^{m-1} \left[(s_l^c)_i^* ((x_i^c)^* - l_i^c) + (s_u^c)_i^* (u_i^c - (x_i^c)^*) \right] \\
&+ \sum_{j=0}^{n-1} \left[(s_l^x)_j^* (x_j - l_j^x) + (s_u^x)_j^* (u_j^x - x_j^*) \right] + \sum_{j=0}^{n-1} (s_n^x)_j^* x_j^* \geq 0
\end{aligned}
\tag{8.9}
$$

where the first relation can be obtained by transposing and multiplying the dual constraints (8.2) by x^* and $(x^c)^*$ respectively, and the second relation comes from the fact that each term in each sum is nonnegative. It follows that the primal objective will always be greater than or equal to the dual objective.

It is well-known that, under some non-degeneracy assumptions that exclude ill-posed cases, a conic optimization problem has an optimal solution if and only if there exist feasible primal-dual solution so that the duality gap is zero, or, equivalently, that the *complementarity conditions*

$$
\begin{aligned}
(s_l^c)_i^* ((x_i^c)^* - l_i^c) &= 0, & i &= 0, \ldots, m-1, \\
(s_u^c)_i^* (u_i^c - (x_i^c)^*) &= 0, & i &= 0, \ldots, m-1, \\
(s_l^x)_j^* (x_j^* - l_j^x) &= 0, & j &= 0, \ldots, n-1, \\
(s_u^x)_j^* (u_j^x - x_j^*) &= 0, & j &= 0, \ldots, n-1, \\
\sum_{j=0}^{n-1} (s_n^x)_j^* x_j^* &= 0.
\end{aligned}
\tag{8.10}
$$

are satisfied.

If (8.7) has an optimal solution and **MOSEK** solves the problem successfully, both the primal and dual solution are reported, including a status indicating the exact state of the solution.

8.2.2 Infeasibility for Conic Optimization

Primal Infeasible Problems

If the problem (8.7) is infeasible (has no feasible solution), **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the modified dual problem

$$
\begin{aligned}
\text{maximize} \quad & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\
\text{subject to} \quad & \\
& A^T y + s_l^x - s_u^x + s_n^x = 0, \\
& -y + s_l^c - s_u^c = 0, \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\
& s_n^x \in \mathcal{K}^*,
\end{aligned}
\tag{8.11}
$$

such that the objective value is strictly positive, i.e. a solution

$$(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*, (s_n^x)^*)$$

to (8.11) so that

$$(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* > 0.$$

Such a solution implies that (8.11) is unbounded, and that (8.7) is infeasible.

Dual Infeasible Problems

If the problem (8.8) is infeasible (has no feasible solution), **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the modified primal problem

$$
\begin{array}{rlrcl}
\text{minimize} & & c^T x & & \\
\text{subject to} & \hat{l}^c \leq & Ax & \leq & \hat{u}^c, \\
& \hat{l}^x \leq & x & \leq & \hat{u}^x, \\
& & x \in K, &
\end{array}
\tag{8.12}
$$

where

$$
\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}
\tag{8.13}
$$

and

$$
\hat{l}_j^x = \left\{ \begin{array}{ll} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_j^x := \left\{ \begin{array}{ll} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}
\tag{8.14}
$$

such that

$$
c^T x < 0.
$$

Such a solution implies that (8.12) is unbounded, and that (8.8) is infeasible.

In case that both the primal problem (8.7) and the dual problem (8.8) are infeasible, **MOSEK** will report only one of the two possible certificates — which one is not defined (**MOSEK** returns the first certificate found).

8.2.3 Minimalization vs. Maximalization

When the objective sense of problem (8.7) is maximization, i.e.

$$
\begin{array}{rlrcl}
\text{maximize} & & c^T x + c^f & & \\
\text{subject to} & l^c \leq & Ax & \leq & u^c, \\
& l^x \leq & x & \leq & u^x, \\
& & x \in \mathcal{K}, &
\end{array}
$$

the objective sense of the dual problem changes to minimization, and the domain of all dual variables changes sign in comparison to (8.2). The dual problem thus takes the form

$$
\begin{array}{rl}
\text{minimize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\
\text{subject to} & A^T y + s_l^x - s_u^x + s_n^x = c, \\
& -y + s_l^c - s_u^c = 0, \\
& s_l^c, s_u^c, s_l^x, s_u^x \leq 0, \\
& -s_n^x \in \mathcal{K}^*
\end{array}
$$

This means that the duality gap, defined in (8.9) as the primal minus the dual objective value, becomes nonpositive. It follows that the dual objective will always be greater than or equal to the primal objective. The primal infeasibility certificate will be reported by **MOSEK** as a solution to the system

$$
\begin{array}{l}
A^T y + s_l^x - s_u^x + s_n^x = 0, \\
-y + s_l^c - s_u^c = 0, \\
s_l^c, s_u^c, s_l^x, s_u^x \leq 0, \\
-s_n^x \in \mathcal{K}^*
\end{array}
\tag{8.15}
$$

such that the objective value is strictly negative

$$
(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* < 0.
$$

Similarly, the certificate of dual infeasibility is an x satisfying the requirements of (8.12) such that $c^T x > 0$.

8.3 Semidefinite Optimization

Semidefinite optimization is an extension of conic optimization (see Sec. 8.2) allowing positive semidefinite matrix variables to be used in addition to the usual scalar variables. All the other parts of the input are defined exactly as in Sec. 8.2, and the discussion from that section applies verbatim to all properties of problems with semidefinite variables. We only briefly indicate how the corresponding formulae should be modified with semidefinite terms.

A semidefinite optimization problem can be written as

$$
\begin{aligned}
\text{minimize} \quad & \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \langle \overline{C}_j, \overline{X}_j \rangle + c^f \\
\text{subject to} \quad l_i^c \leq \ & \sum_{j=0}^{n-1} a_{ij} x_j + \sum_{j=0}^{p-1} \langle \overline{A}_{ij}, \overline{X}_j \rangle \quad \leq \ u_i^c, \quad i = 0, \ldots, m-1 \\
l_j^x \leq \ & \qquad\qquad x_j \qquad\qquad\qquad \leq \ u_j^x, \quad j = 0, \ldots, n-1 \\
& x \in \mathcal{K}, \\
& \overline{X}_j \in \mathcal{S}_+^{r_j}, \qquad\qquad\qquad\qquad\qquad\quad j = 0, \ldots, p-1
\end{aligned} \tag{8.16}
$$

where the problem has p symmetric positive semidefinite variables $\overline{X}_j \in \mathcal{S}_+^{r_j}$ of dimension r_j with symmetric coefficient matrices $\overline{C}_j \in \mathcal{S}^{r_j}$ and $\overline{A}_{i,j} \in \mathcal{S}^{r_j}$. We use standard notation for the matrix inner product, i.e., for $U, V \in \mathbb{R}^{m \times n}$ we have

$$
\langle U, V \rangle := \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} U_{ij} V_{ij}.
$$

As always we write $A = (a_{i,j})$ for the linear coefficient matrix.

Duality

The definition of the dual problem (8.8) becomes:

$$
\begin{aligned}
\text{maximize} \quad & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\
\text{subject to} \quad & \\
& A^T y + s_l^x - s_u^x + s_n^x = c \\
& -y + s_l^c - s_u^c = 0, \\
& \overline{C}_j - \sum_{i=0}^{m-1} y_i \overline{A}_{ij} = \overline{S}_j, \qquad\qquad j = 0, \ldots, p-1 \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\
& s_n^x \in \mathcal{K}^*, \\
& \overline{S}_j \in \mathcal{S}_+^{r_j}, \qquad\qquad\qquad\qquad j = 0, \ldots, p-1.
\end{aligned} \tag{8.17}
$$

The duality gap (8.9) is computed as:

$$
\begin{aligned}
& c^T x^* + c^f - \left\{ (l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* + c^f \right\} \\
& = \sum_{i=0}^{m-1} \left[(s_l^c)_i^* ((x_i^c)^* - l_i^c) + (s_u^c)_i^* (u_i^c - (x_i^c)^*) \right] \\
& + \sum_{j=0}^{n-1} \left[(s_l^x)_j^* (x_j - l_j^x) + (s_u^x)_j^* (u_j^x - x_j^*) \right] + \sum_{j=0}^{n-1} (s_n^x)_j^* x_j^* + \sum_{j=0}^{p-1} \langle \overline{X}_j, \overline{S}_j \rangle \geq 0.
\end{aligned} \tag{8.18}
$$

Complementarity conditions (8.10) include the additional relation:

$$
\langle \overline{X}_j, \overline{S}_j \rangle = 0 \quad j = 0, \ldots, p-1. \tag{8.19}
$$

Infeasibility

A certificate of primal infeasibility (8.11) is now a feasible solution to:

$$
\begin{aligned}
\text{maximize} \quad & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\
\text{subject to} \quad & \\
& A^T y + s_l^x - s_u^x + s_n^x = 0, \\
& -y + s_l^c - s_u^c = 0, \\
& \sum_{i=0}^{m-1} y_i \overline{A}_{ij} + \overline{S}_j = 0, \qquad\qquad j = 0, \ldots, p-1 \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\
& s_n^x \in \mathcal{K}^*, \\
& \overline{S}_j \in \mathcal{S}_+^{r_j}, \qquad\qquad\qquad\qquad j = 0, \ldots, p-1.
\end{aligned} \tag{8.20}
$$

such that the objective value is strictly positive.

Similarly, a dual infeasibility certificate (8.12) is a feasible solution to

$$
\begin{array}{lllll}
\text{minimize} & & \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \left\langle \overline{C}_j, \overline{X}_j \right\rangle & & \\
\text{subject to} & \hat{l}_i^c \leq & \sum_{j=0}^{n-1} a_{ij} x_j + \sum_{j=0}^{p-1} \left\langle \overline{A}_{ij}, \overline{X}_j \right\rangle & \leq \hat{u}_i^c, & i = 0, \ldots, m-1 \\
& \hat{l}_j^x \leq & x_j & \leq \hat{u}_j^x, & j = 0, \ldots, n-1 \\
& & x \in \mathcal{K}, & & \\
& & \overline{X}_j \in \mathcal{S}_+^{r_j}, & & j = 0, \ldots, p-1
\end{array} \tag{8.21}
$$

where the modified bounds are as in (8.13) and (8.14) and the objective value is strictly negative.

8.4 Quadratic and Quadratically Constrained Optimization

A convex quadratic and quadratically constrained optimization problem has the form

$$
\begin{array}{llll}
\text{minimize} & & \frac{1}{2} x^T Q^o x + c^T x + c^f & \\
\text{subject to} & l_k^c \leq & \frac{1}{2} x^T Q^k x + \sum_{j=0}^{n-1} a_{kj} x_j \leq u_k^c, & k = 0, \ldots, m-1, \\
& l_j^x \leq & x_j \leq u_j^x, & j = 0, \ldots, n-1,
\end{array} \tag{8.22}
$$

where all variables and bounds have the same meaning as for linear problems (see Sec. 8.1) and Q^o and all Q^k are symmetric matrices. Moreover, for convexity, Q^o must be a positive semidefinite matrix and Q^k must satisfy

$$
\begin{array}{lll}
-\infty < l_k^c & \Rightarrow & Q^k \text{ is negative semidefinite,} \\
u_k^c < \infty & \Rightarrow & Q^k \text{ is positive semidefinite,} \\
-\infty < l_k^c \leq u_k^c < \infty & \Rightarrow & Q^k = 0.
\end{array}
$$

The convexity requirement is very important and **MOSEK** checks whether it is fulfilled.

8.4.1 A Recommendation

Any convex quadratic optimization problem can be reformulated as a conic quadratic optimization problem, see Modeling Cookbook and [And13]. In fact **MOSEK** does such conversion internally as a part of the solution process for the following reasons:

- the conic optimizer is numerically more robust than the one for quadratic problems.

- the conic optimizer is usually faster because quadratic cones are simpler than quadratic functions, even though the conic reformulation usually has more constraints and variables than the original quadratic formulation.

- it is easy to dualize the conic formulation if deemed worthwhile potentially leading to (huge) computational savings.

However, instead of relying on the automatic reformulation we recommend to formulate the problem as a conic problem from scratch because:

- it saves the computational overhead of the reformulation including the convexity check. A conic problem is convex by construction and hence no convexity check is needed for conic problems.

- usually the modeler can do a better reformulation than the automatic method because the modeler can exploit the knowledge of the problem at hand.

To summarize we recommend to formulate quadratic problems and in particular quadratically constrained problems directly in conic form.

8.4.2 Duality for Quadratic and Quadratically Constrained Optimization

The dual problem corresponding to the quadratic and quadratically constrained optimization problem (8.22) is given by

$$
\begin{aligned}
\text{maximize} \quad & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + \tfrac{1}{2} x^T \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x + c^f \\
\text{subject to} \quad & A^T y + s_l^x - s_u^x + \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x = c, \\
& -y + s_l^c - s_u^c = 0, \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0.
\end{aligned}
\tag{8.23}
$$

The dual problem is related to the dual problem for linear optimization (see Sec. 8.1.1), but depends on the variable x which in general can not be eliminated. In the solutions reported by **MOSEK**, the value of x is the same for the primal problem (8.22) and the dual problem (8.23).

8.4.3 Infeasibility for Quadratic Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. We write them out explicitly for quadratic problems, that is when $Q^k = 0$ for all k and quadratic terms appear only in the objective Q^o. In this case the constraints both in the primal and dual problem are linear, and **MOSEK** produces for them the same infeasibility certificate as for linear problems.

The certificate of primal infeasibility is a solution to the problem (8.4) such that the objective value is strictly positive.

The certificate of dual infeasibility is a solution to the problem (8.5) together with an additional constraint

$$
Q^o x = 0
$$

such that the objective value is strictly negative.

Chapter 9

Optimizers

The most essential part of **MOSEK** are the optimizers:

- *primal simplex* (linear problems),

- *dual simplex* (linear problems),

- *interior-point* (linear, quadratic and conic problems),

- *mixed-integer* (problems with integer variables).

The structure of a successful optimization process is roughly:

- **Presolve**

  1. *Elimination*: Reduce the size of the problem.
  2. *Dualizer*: Choose whether to solve the primal or the dual form of the problem.
  3. *Scaling*: Scale the problem for better numerical stability.

- **Optimization**

  1. *Optimize*: Solve the problem using selected method.
  2. *Terminate*: Stop the optimization when specific termination criteria have been met.
  3. *Report*: Return the solution or an infeasibility certificate.

The preprocessing stage is transparent to the user, but useful to know about for tuning purposes. The purpose of the preprocessing steps is to make the actual optimization more efficient and robust. We discuss the details of the above steps in the following sections.

9.1 Presolve

Before an optimizer actually performs the optimization the problem is preprocessed using the so-called presolve. The purpose of the presolve is to

1. remove redundant constraints,

2. eliminate fixed variables,

3. remove linear dependencies,

4. substitute out (implied) free variables, and

5. reduce the size of the optimization problem in general.

After the presolved problem has been optimized the solution is automatically postsolved so that the returned solution is valid for the original problem. Hence, the presolve is completely transparent. For further details about the presolve phase, please see *[AA95]* and *[AGMX96]*.

It is possible to fine-tune the behavior of the presolve or to turn it off entirely. If presolve consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This is done by setting the parameter *MSK_IPAR_PRESOLVE_USE* to *MSK_PRESOLVE_MODE_OFF*. The two most time-consuming steps of the presolve are

- the eliminator, and

- the linear dependency check.

Therefore, in some cases it is worthwhile to disable one or both of these.

Numerical issues in the presolve

During the presolve the problem is reformulated so that it hopefully solves faster. However, in rare cases the presolved problem may be harder to solve then the original problem. The presolve may also be infeasible although the original problem is not. If it is suspected that presolved problem is much harder to solve than the original, we suggest to first turn the eliminator off by setting the parameter `MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES` to 0. If that does not help, then trying to turn entire presolve off may help.

Since all computations are done in finite precision, the presolve employs some tolerances when concluding a variable is fixed or a constraint is redundant. If it happens that **MOSEK** incorrectly concludes a problem is primal or dual infeasible, then it is worthwhile to try to reduce the parameters `MSK_DPAR_PRESOLVE_TOL_X` and `MSK_DPAR_PRESOLVE_TOL_S`. However, if reducing the parameters actually helps then this should be taken as an indication that the problem is badly formulated.

Eliminator

The purpose of the eliminator is to eliminate free and implied free variables from the problem using substitution. For instance, given the constraints

$$
\begin{aligned}
y &= \sum_j x_j, \\
y, x &\geq 0,
\end{aligned}
$$

y is an implied free variable that can be substituted out of the problem, if deemed worthwhile. If the eliminator consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This can be done by setting the parameter `MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES` to 0. In rare cases the eliminator may cause that the problem becomes much hard to solve.

Linear dependency checker

The purpose of the linear dependency check is to remove linear dependencies among the linear equalities. For instance, the three linear equalities

$$
\begin{aligned}
x_1 + x_2 + x_3 &= 1, \\
x_1 + 0.5x_2 &= 0.5, \\
0.5x_2 + x_3 &= 0.5.
\end{aligned}
$$

contain exactly one linear dependency. This implies that one of the constraints can be dropped without changing the set of feasible solutions. Removing linear dependencies is in general a good idea since it reduces the size of the problem. Moreover, the linear dependencies are likely to introduce numerical problems in the optimization phase. It is best practice to build models without linear dependencies, but that is not always easy for the user to control. If the linear dependencies are removed at the modeling stage, the linear dependency check can safely be disabled by setting the parameter `MSK_IPAR_PRESOLVE_LINDEP_USE` to `MSK_OFF`.

Dualizer

All linear, conic, and convex optimization problems have an equivalent dual problem associated with them. **MOSEK** has built-in heuristics to determine if it is more efficient to solve the primal or dual problem. The form (primal or dual) is displayed in the **MOSEK** log and available as an information item from the solver. Should the internal heuristics not choose the most efficient form of the problem it may be worthwhile to set the dualizer manually by setting the parameters:

- `MSK_IPAR_INTPNT_SOLVE_FORM`: In case of the interior-point optimizer.

- `MSK_IPAR_SIM_SOLVE_FORM`: In case of the simplex optimizer.

Note that currently only linear and conic (but not semidefinite) problems may be automatically dualized.

Scaling

Problems containing data with large and/or small coefficients, say $1.0e + 9$ or $1.0e - 7$, are often hard to solve. Significant digits may be truncated in calculations with finite precision, which can result in the optimizer relying on inaccurate data. Since computers work in finite precision, extreme coefficients should be avoided. In general, data around the same *order of magnitude* is preferred, and we will refer to a problem, satisfying this loose property, as being *well-scaled*. If the problem is not well scaled, **MOSEK** will try to scale (multiply) constraints and variables by suitable constants. **MOSEK** solves the scaled problem to improve the numerical properties.

The scaling process is transparent, i.e. the solution to the original problem is reported. It is important to be aware that the optimizer terminates when the termination criterion is met on the scaled problem, therefore significant primal or dual infeasibilities may occur after unscaling for badly scaled problems. The best solution of this issue is to reformulate the problem, making it better scaled.

By default **MOSEK** heuristically chooses a suitable scaling. The scaling for interior-point and simplex optimizers can be controlled with the parameters `MSK_IPAR_INTPNT_SCALING` and `MSK_IPAR_SIM_SCALING` respectively.

9.2 Linear Optimization

9.2.1 Optimizer Selection

Two different types of optimizers are available for linear problems: The default is an interior-point method, and the alternative is the simplex method (primal or dual). The optimizer can be selected using the parameter `MSK_IPAR_OPTIMIZER`.

The Interior-point or the Simplex Optimizer?

Given a linear optimization problem, which optimizer is the best: the simplex or the interior-point optimizer? It is impossible to provide a general answer to this question. However, the interior-point optimizer behaves more predictably: it tends to use between 20 and 100 iterations, almost independently of problem size, but cannot perform warm-start. On the other hand the simplex method can take advantage of an initial solution, but is less predictable from cold-start. The interior-point optimizer is used by default.

The Primal or the Dual Simplex Variant?

MOSEK provides both a primal and a dual simplex optimizer. Predicting which simplex optimizer is faster is impossible, however, in recent years the dual optimizer has seen several algorithmic and computational improvements, which, in our experience, make it faster on average than the primal version. Still, it depends much on the problem structure and size. Setting the `MSK_IPAR_OPTIMIZER` parameter to `MSK_OPTIMIZER_FREE_SIMPLEX` instructs **MOSEK** to choose one of the simplex variants automatically.

To summarize, if you want to know which optimizer is faster for a given problem type, it is best to try all the options.

9.2.2 The Interior-point Optimizer

The purpose of this section is to provide information about the algorithm employed in the **MOSEK** interior-point optimizer for linear problems and about its termination criteria.

The homogeneous primal-dual problem

In order to keep the discussion simple it is assumed that **MOSEK** solves linear optimization problems of standard form

$$
\begin{array}{lll}
\text{minimize} & c^T x \\
\text{subject to} & Ax & = & b, \\
& x \geq 0.
\end{array}
\tag{9.1}
$$

This is in fact what happens inside **MOSEK**; for efficiency reasons **MOSEK** converts the problem to standard form before solving, then converts it back to the input form when reporting the solution.

Since it is not known beforehand whether problem (9.1) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason why **MOSEK** solves the so-called homogeneous model

$$
\begin{array}{rcl}
Ax - b\tau & = & 0, \\
A^T y + s - c\tau & = & 0, \\
-c^T x + b^T y - \kappa & = & 0, \\
x, s, \tau, \kappa & \geq & 0,
\end{array}
$$

(9.2)

where y and s correspond to the dual variables in (9.1), and τ and κ are two additional scalar variables. Note that the homogeneous model (9.2) always has solution since

$$
(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)
$$

is a solution, although not a very interesting one. Any solution

$$
(x^*, y^*, s^*, \tau^*, \kappa^*)
$$

to the homogeneous model (9.2) satisfies

$$
x_j^* s_j^* = 0 \text{ and } \tau^* \kappa^* = 0.
$$

Moreover, there is always a solution that has the property $\tau^* + \kappa^* > 0$.

First, assume that $\tau^* > 0$. It follows that

$$
\begin{array}{rcl}
A \frac{x^*}{\tau^*} & = & b, \\
A^T \frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} & = & c, \\
-c^T \frac{x^*}{\tau^*} + b^T \frac{y^*}{\tau^*} & = & 0, \\
x^*, s^*, \tau^*, \kappa^* & \geq & 0.
\end{array}
$$

This shows that $\frac{x^*}{\tau^*}$ is a primal optimal solution and $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau^*})$ is a dual optimal solution; this is reported as the optimal interior-point solution since

$$
(x, y, s) = \left\{ \frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*} \right\}
$$

is a primal-dual optimal solution (see Sec. 8.1 for the mathematical background on duality and optimality).

On other hand, if $\kappa^* > 0$ then

$$
\begin{array}{rcl}
Ax^* & = & 0, \\
A^T y^* + s^* & = & 0, \\
-c^T x^* + b^T y^* & = & \kappa^*, \\
x^*, s^*, \tau^*, \kappa^* & \geq & 0.
\end{array}
$$

This implies that at least one of

$$
c^T x^* < 0
$$

(9.3)

or

$$
b^T y^* > 0
$$

(9.4)

is satisfied. If (9.3) is satisfied then x^* is a certificate of dual infeasibility, whereas if (9.4) is satisfied then y^* is a certificate of primal infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm [And09].

Interior-point Termination Criterion

For efficiency reasons it is not practical to solve the homogeneous model exactly. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In the k-th iteration of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to homogeneous model is generated, where

$$x^k, s^k, \tau^k, \kappa^k > 0.$$

Optimal case

Whenever the trial solution satisfies the criterion

$$
\begin{aligned}
\left\| A \frac{x^k}{\tau^k} - b \right\|_\infty &\leq \epsilon_p (1 + \|b\|_\infty), \\
\left\| A^T \frac{y^k}{\tau^k} + \frac{s^k}{\tau^k} - c \right\|_\infty &\leq \epsilon_d (1 + \|c\|_\infty), \text{ and} \\
\min \left(\frac{(x^k)^T s^k}{(\tau^k)^2}, \left| \frac{c^T x^k}{\tau^k} - \frac{b^T y^k}{\tau^k} \right| \right) &\leq \epsilon_g \max \left(1, \frac{\min(|c^T x^k|, |b^T y^k|)}{\tau^k} \right),
\end{aligned}
\tag{9.5}
$$

the interior-point optimizer is terminated and

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is reported as the primal-dual optimal solution. The interpretation of (9.5) is that the optimizer is terminated if

- $\frac{x^k}{\tau^k}$ is approximately primal feasible,

- $\left\{ \frac{y^k}{\tau^k}, \frac{s^k}{\tau^k} \right\}$ is approximately dual feasible, and

- the duality gap is almost zero.

Dual infeasibility certificate

On the other hand, if the trial solution satisfies

$$-\epsilon_i c^T x^k > \frac{\|c\|_\infty}{\max(1, \|b\|_\infty)} \left\| A x^k \right\|_\infty$$

then the problem is declared dual infeasible and x^k is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows: First assume that $\left\| A x^k \right\|_\infty = 0$; then x^k is an exact certificate of dual infeasibility. Next assume that this is not the case, i.e.

$$\left\| A x^k \right\|_\infty > 0,$$

and define

$$\bar{x} := \epsilon_i \frac{\max(1, \|b\|_\infty)}{\left\| A x^k \right\|_\infty \|c\|_\infty} x^k.$$

It is easy to verify that

$$\|A \bar{x}\|_\infty = \epsilon_i \frac{\max(1, \|b\|_\infty)}{\|c\|_\infty} \text{ and } -c^T \bar{x} > 1,$$

which shows $\bar{x}$ is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation. A smaller value means a better approximation.

Primal infeasibility certificate

Finally, if

$$\epsilon_i b^T y^k > \frac{\|b\|_\infty}{\max\left(1, \|c\|_\infty\right)} \left\|A^T y^k + s^k\right\|_\infty$$

then y^k is reported as a certificate of primal infeasibility.

Adjusting optimality criteria

It is possible to adjust the tolerances ε_p, ε_d, ε_g and ε_i using parameters; see table for details.

Table 9.1: Parameters employed in termination criterion

ToleranceParameter	name
ε_p	`MSK_DPAR_INTPNT_TOL_PFEAS`
ε_d	`MSK_DPAR_INTPNT_TOL_DFEAS`
ε_g	`MSK_DPAR_INTPNT_TOL_REL_GAP`
ε_i	`MSK_DPAR_INTPNT_TOL_INFEAS`

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (9.5) reveals that the quality of the solution depends on $\|b\|_\infty$ and $\|c\|_\infty$; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate *[And09]*. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances, ε_p, ε_d, ε_g and ε_i, have to be relaxed together to achieve an effect.

If the optimizer terminates without locating a solution that satisfies the termination criteria, for example because of a stall or other numerical issues, then it will check if the solution found up to that point satisfies the same criteria with all tolerances multiplied by the value of `MSK_DPAR_INTPNT_CO_TOL_NEAR_REL`. If this is the case, the solution is still declared as optimal.

The basis identification discussed in Sec. 9.2.2 requires an optimal solution to work well; hence basis identification should be turned off if the termination criterion is relaxed.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

Basis Identification

An interior-point optimizer does not return an optimal basic solution unless the problem has a unique primal and dual optimal solution. Therefore, the interior-point optimizer has an optional post-processing step that computes an optimal basic solution starting from the optimal interior-point solution. More information about the basis identification procedure may be found in *[AY96]*. In the following we provide an overall idea of the procedure.

There are some cases in which a basic solution could be more valuable:

- a basic solution is often more accurate than an interior-point solution,

- a basic solution can be used to warm-start the simplex algorithm in case of reoptimization,

- a basic solution is in general more sparse, i.e. more variables are fixed to zero. This is particularly appealing when solving continuous relaxations of mixed integer problems, as well as in all applications in which sparser solutions are preferred.

To illustrate how the basis identification routine works, we use the following trivial example:

$$
\begin{array}{lll}
\text{minimize} & x + y \\
\text{subject to} & x + y & = & 1, \\
& x, y \geq 0.
\end{array}
$$

It is easy to see that all feasible solutions are also optimal. In particular, there are two basic solutions, namely

$$
\begin{array}{lll}
(x_1^*, y_1^*) & = & (1, 0), \\
(x_2^*, y_2^*) & = & (0, 1).
\end{array}
$$

The interior point algorithm will actually converge to the center of the optimal set, i.e. to $(x^*, y^*) = (1/2, 1/2)$ (to see this in **MOSEK** deactivate *Presolve*).

In practice, when the algorithm gets close to the optimal solution, it is possible to construct in polynomial time an initial basis for the simplex algorithm from the current interior point solution. This basis is used to warm-start the simplex algorithm that will provide the optimal basic solution. In most cases the constructed basis is optimal, or very few iterations are required by the simplex algorithm to make it optimal and hence the final *clean-up* phase be short. However, for some cases of ill-conditioned problems the additional simplex clean up phase may take of lot a time.

By default **MOSEK** performs a basis identification. However, if a basic solution is not needed, the basis identification procedure can be turned off. The parameters

- *MSK_IPAR_INTPNT_BASIS*,

- *MSK_IPAR_BI_IGNORE_MAX_ITER*, and

- *MSK_IPAR_BI_IGNORE_NUM_ERROR*

control when basis identification is performed.

The type of simplex algorithm to be used (primal/dual) can be tuned with the parameter *MSK_IPAR_BI_CLEAN_OPTIMIZER*, and the maximum number of iterations can be set with *MSK_IPAR_BI_MAX_ITERATIONS*.

Finally, it should be mentioned that there is no guarantee on which basic solution will be returned.

The Interior-point Log

Below is a typical log output from the interior-point optimizer:

```
Optimizer   - threads              : 1
Optimizer   - solved problem       : the dual
Optimizer   - Constraints          : 2
Optimizer   - Cones                : 0
Optimizer   - Scalar variables     : 6              conic            : 0
Optimizer   - Semi-definite variables: 0            scalarized       : 0
Factor      - setup time           : 0.00           dense det. time  : 0.00
Factor      - ML order time        : 0.00           GP order time    : 0.00
Factor      - nonzeros before factor : 3            after factor     : 3
Factor      - dense dim.           : 0              flops            : 7.00e+001
ITE PFEAS    DFEAS    GFEAS    PRSTATUS  POBJ              DOBJ              MU       TIME
0   1.0e+000 8.6e+000 6.1e+000 1.00e+000 0.000000000e+000  -2.208000000e+003 1.0e+000 0.00
1   1.1e+000 2.5e+000 1.6e-001 0.00e+000 -7.901380925e+003 -7.394611417e+003 2.5e+000 0.00
2   1.4e-001 3.4e-001 2.1e-002 8.36e-001 -8.113031650e+003 -8.055866001e+003 3.3e-001 0.00
3   2.4e-002 5.8e-002 3.6e-003 1.27e+000 -7.777530698e+003 -7.766471080e+003 5.7e-002 0.01
4   1.3e-004 3.2e-004 2.0e-005 1.08e+000 -7.668323435e+003 -7.668207177e+003 3.2e-004 0.01
5   1.3e-008 3.2e-008 2.0e-009 1.00e+000 -7.668000027e+003 -7.668000015e+003 3.2e-008 0.01
6   1.3e-012 3.2e-012 2.0e-013 1.00e+000 -7.667999994e+003 -7.667999994e+003 3.2e-012 0.01
```

The first line displays the number of threads used by the optimizer and the second line indicates if the optimizer chose to solve the primal or dual problem (see *MSK_IPAR_INTPNT_SOLVE_FORM*). The next lines display the problem dimensions as seen by the optimizer, and the `Factor...` lines show various statistics. This is followed by the iteration log.

Using the same notation as in Sec. 9.2.2 the columns of the iteration log have the following meaning:

- `ITE`: Iteration index k.

- `PFEAS`: $\left\|Ax^k - b\tau^k\right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.

- `DFEAS`: $\left\|A^T y^k + s^k - c\tau^k\right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.

- `GFEAS`: $\left|-c^T x^k + b^T y^k - \kappa^k\right|$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.

- `PRSTATUS`: This number converges to 1 if the problem has an optimal solution whereas it converges to -1 if that is not the case.

- POBJ: $c^T x^k / \tau^k$. An estimate for the primal objective value.

- DOBJ: $b^T y^k / \tau^k$. An estimate for the dual objective value.

- MU: $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$. The numbers in this column should always converge to zero.

- TIME: Time spent since the optimization started.

9.2.3 The Simplex Optimizer

An alternative to the interior-point optimizer is the simplex optimizer. The simplex optimizer uses a different method that allows exploiting an initial guess for the optimal solution to reduce the solution time. Depending on the problem it may be faster or slower to use an initial guess; see Sec. 9.2.1 for a discussion. **MOSEK** provides both a primal and a dual variant of the simplex optimizer.

Simplex Termination Criterion

The simplex optimizer terminates when it finds an optimal basic solution or an infeasibility certificate. A basic solution is optimal when it is primal and dual feasible; see Sec. 8.1 for a definition of the primal and dual problem. Due to the fact that computations are performed in finite precision **MOSEK** allows violations of primal and dual feasibility within certain tolerances. The user can control the allowed primal and dual tolerances with the parameters *MSK_DPAR_BASIS_TOL_X* and *MSK_DPAR_BASIS_TOL_S* .

Setting the parameter *MSK_IPAR_OPTIMIZER* to *MSK_OPTIMIZER_FREE_SIMPLEX* instructs **MOSEK** to select automatically between the primal and the dual simplex optimizers. Hence, **MOSEK** tries to choose the best optimizer for the given problem and the available solution. The same parameter can also be used to force one of the variants.

Starting From an Existing Solution

When using the simplex optimizer it may be possible to reuse an existing solution and thereby reduce the solution time significantly. When a simplex optimizer starts from an existing solution it is said to perform a *warm-start*. If the user is solving a sequence of optimization problems by solving the problem, making modifications, and solving again, **MOSEK** will warm-start automatically.

By default **MOSEK** uses presolve when performing a warm-start. If the optimizer only needs very few iterations to find the optimal solution it may be better to turn off the presolve.

Numerical Difficulties in the Simplex Optimizers

Though **MOSEK** is designed to minimize numerical instability, completely avoiding it is impossible when working in finite precision. **MOSEK** treats a "numerically unexpected behavior" event inside the optimizer as a *set-back*. The user can define how many set-backs the optimizer accepts; if that number is exceeded, the optimization will be aborted. Set-backs are a way to escape long sequences where the optimizer tries to recover from an unstable situation.

Examples of set-backs are: repeated singularities when factorizing the basis matrix, repeated loss of feasibility, degeneracy problems (no progress in objective) and other events indicating numerical difficulties. If the simplex optimizer encounters a lot of set-backs the problem is usually badly scaled; in such a situation try to reformulate it into a better scaled problem. Then, if a lot of set-backs still occur, trying one or more of the following suggestions may be worthwhile:

- Raise tolerances for allowed primal or dual feasibility: increase the value of

  - *MSK_DPAR_BASIS_TOL_X* , and
  - *MSK_DPAR_BASIS_TOL_S* .

- Raise or lower pivot tolerance: Change the *MSK_DPAR_SIMPLEX_ABS_TOL_PIV* parameter.

- Switch optimizer: Try another optimizer.

- Switch off crash: Set both *MSK_IPAR_SIM_PRIMAL_CRASH* and *MSK_IPAR_SIM_DUAL_CRASH* to 0.

- Experiment with other pricing strategies: Try different values for the parameters

- – `MSK_IPAR_SIM_PRIMAL_SELECTION` and
- – `MSK_IPAR_SIM_DUAL_SELECTION` .

- If you are using warm-starts, in rare cases switching off this feature may improve stability. This is controlled by the `MSK_IPAR_SIM_HOTSTART` parameter.

- Increase maximum number of set-backs allowed controlled by `MSK_IPAR_SIM_MAX_NUM_SETBACKS` .

- If the problem repeatedly becomes infeasible try switching off the special degeneracy handling. See the parameter `MSK_IPAR_SIM_DEGEN` for details.

The Simplex Log

Below is a typical log output from the simplex optimizer:

```
Optimizer  - solved problem         : the primal
Optimizer  - Constraints            : 667
Optimizer  - Scalar variables       : 1424              conic                    : 0
Optimizer  - hotstart               : no
ITER      DEGITER(%) PFEAS       DFEAS      POBJ                 DOBJ                    TIME␣
↪     TOTTIME
0         0.00       1.43e+05    NA         6.5584140832e+03     NA                      0.00␣
↪     0.02
1000      1.10       0.00e+00    NA         1.4588289726e+04     NA                      0.13␣
↪     0.14
2000      0.75       0.00e+00    NA         7.3705564855e+03     NA                      0.21␣
↪     0.22
3000      0.67       0.00e+00    NA         6.0509727712e+03     NA                      0.29␣
↪     0.31
4000      0.52       0.00e+00    NA         5.5771203906e+03     NA                      0.38␣
↪     0.39
4533      0.49       0.00e+00    NA         5.5018458883e+03     NA                      0.42␣
↪     0.44
```

The first lines summarize the problem the optimizer is solving. This is followed by the iteration log, with the following meaning:

- `ITER`: Number of iterations.

- `DEGITER(%)`: Ratio of degenerate iterations.

- `PFEAS`: Primal feasibility measure reported by the simplex optimizer. The numbers should be 0 if the problem is primal feasible (when the primal variant is used).

- `DFEAS`: Dual feasibility measure reported by the simplex optimizer. The number should be 0 if the problem is dual feasible (when the dual variant is used).

- `POBJ`: An estimate for the primal objective value (when the primal variant is used).

- `DOBJ`: An estimate for the dual objective value (when the dual variant is used).

- `TIME`: Time spent since this instance of the simplex optimizer was invoked (in seconds).

- `TOTTIME`: Time spent since optimization started (in seconds).

9.3 Conic Optimization - Interior-point optimizer

For conic optimization problems only an interior-point type optimizer is available.

9.3.1 The homogeneous primal-dual problem

The interior-point optimizer is an implementation of the so-called homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see *[ART03]*. In order to keep our discussion simple we will assume that **MOSEK** solves a conic optimization problem of the form:

$$
\begin{array}{lll}
\text{minimize} & c^T x & \\
\text{subject to} & Ax & = \quad b, \\
& x \in \mathcal{K} &
\end{array}
\tag{9.6}
$$

where K is a convex cone. The corresponding dual problem is

$$
\begin{array}{lll}
\text{maximize} & b^T y & \\
\text{subject to} & A^T y + s & = \quad c, \\
& s \in \mathcal{K}^* &
\end{array}
\tag{9.7}
$$

where $\mathcal{K}^*$ is the dual cone of $\mathcal{K}$. See Sec. 8.2 for definitions.

Since it is not known beforehand whether problem (9.6) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason that **MOSEK** solves the so-called homogeneous model

$$
\begin{array}{rcl}
Ax - b\tau & = & 0, \\
A^T y + s - c\tau & = & 0, \\
-c^T x + b^T y - \kappa & = & 0, \\
x & \in & \mathcal{K}, \\
s & \in & \mathcal{K}^*, \\
\tau, \kappa & \geq & 0,
\end{array}
\tag{9.8}
$$

where y and s correspond to the dual variables in (9.6), and τ and κ are two additional scalar variables. Note that the homogeneous model (9.8) always has a solution since

$$
(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)
$$

is a solution, although not a very interesting one. Any solution

$$
(x^*, y^*, s^*, \tau^*, \kappa^*)
$$

to the homogeneous model (9.8) satisfies

$$
(x^*)^T s^* + \tau^* \kappa^* = 0
$$

i.e. complementarity. Observe that $x^* \in \mathcal{K}$ and $s^* \in \mathcal{K}^*$ implies

$$
(x^*)^T s^* \geq 0
$$

and therefore

$$
\tau^* \kappa^* = 0.
$$

since $\tau^*, \kappa^* \geq 0$. Hence, at least one of τ^* and κ^* is zero.

First, assume that $\tau^* > 0$ and hence $\kappa^* = 0$. It follows that

$$
\begin{array}{rcl}
A \frac{x^*}{\tau^*} & = & b, \\
A^T \frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} & = & c, \\
-c^T \frac{x^*}{\tau^*} + b^T \frac{y^*}{\tau^*} & = & 0, \\
x^*/\tau^* & \in & \mathcal{K}, \\
s^*/\tau^* & \in & \mathcal{K}^*.
\end{array}
$$

This shows that $\frac{x^*}{\tau^*}$ is a primal optimal solution and $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau^*})$ is a dual optimal solution; this is reported as the optimal interior-point solution since

$$
(x, y, s) = \left(\frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*} \right)
$$

is a primal-dual optimal solution.

On other hand, if $\kappa^* > 0$ then

$$
\begin{aligned}
Ax^* &= 0, \\
A^T y^* + s^* &= 0, \\
-c^T x^* + b^T y^* &= \kappa^*, \\
x^* &\in \mathcal{K}, \\
s^* &\in \mathcal{K}^*.
\end{aligned}
$$

This implies that at least one of

$$c^T x^* < 0 \tag{9.9}$$

or

$$b^T y^* > 0 \tag{9.10}$$

holds. If (9.9) is satisfied, then x^* is a certificate of dual infeasibility, whereas if (9.10) holds then y^* is a certificate of primal infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm *[And09]*.

9.3.2 Interior-point Termination Criterion

Since computations are performed in finite precision, and for efficiency reasons, it is not possible to solve the homogeneous model exactly in general. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In every iteration k of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to the homogeneous model is generated, where

$$x^k \in \mathcal{K}, s^k \in \mathcal{K}^*, \tau^k, \kappa^k > 0.$$

Therefore, it is possible to compute the values:

$$
\begin{aligned}
\rho_p^k &= \arg\min_\rho \left\{ \rho \mid \left\| A\frac{x^k}{\tau^k} - b \right\|_\infty \le \rho\varepsilon_p(1 + \|b\|_\infty) \right\}, \\
\rho_d^k &= \arg\min_\rho \left\{ \rho \mid \left\| A^T\frac{y^k}{\tau^k} + \frac{s^k}{\tau^k} - c \right\|_\infty \le \rho\varepsilon_d(1 + \|c\|_\infty) \right\}, \\
\rho_g^k &= \arg\min_\rho \left\{ \rho \mid \left(\frac{(x^k)^T s^k}{(\tau^k)^2}, \left| \frac{c^T x^k}{\tau^k} - \frac{b^T y^k}{\tau^k} \right| \right) \le \rho\varepsilon_g \max\left(1, \frac{\min(|c^T x^k|, |b^T y^k|)}{\tau^k}\right) \right\}, \\
\rho_{pi}^k &= \arg\min_\rho \left\{ \rho \mid \left\| A^T y^k + s^k \right\|_\infty \le \rho\varepsilon_i b^T y^k, \ b^T y^k > 0 \right\} \text{ and} \\
\rho_{di}^k &= \arg\min_\rho \left\{ \rho \mid \left\| Ax^k \right\|_\infty \le -\rho\varepsilon_i c^T x^k, \ c^T x^k < 0 \right\}.
\end{aligned}
$$

Note $\varepsilon_p, \varepsilon_d, \varepsilon_g$ and ε_i are nonnegative user specified tolerances.

Optimal Case

Observe ρ_p^k measures how far x^k/τ^k is from being a good approximate primal feasible solution. Indeed if $\rho_p^k \le 1$, then

$$\left\| A\frac{x^k}{\tau^k} - b \right\|_\infty \le \varepsilon_p(1 + \|b\|_\infty). \tag{9.11}$$

This shows the violations in the primal equality constraints for the solution x^k/τ^k is small compared to the size of b given ε_p is small.

Similarly, if $\rho_d^k \le 1$, then $(y^k, s^k)/\tau^k$ is an approximate dual feasible solution. If in addition $\rho_g \le 1$, then the solution $(x^k, y^k, s^k)/\tau^k$ is approximate optimal because the associated primal and dual objective values are almost identical.

In other words if $\max(\rho_p^k, \rho_d^k, \rho_g^k) \leq 1$, then

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is an approximate optimal solution.

Dual Infeasibility Certificate

Next assume that $\rho_{di}^k \leq 1$ and hence

$$\left\|Ax^k\right\|_\infty \leq -\varepsilon_i c^T x^k \text{ and } -c^T x^k > 0$$

holds. Now in this case the problem is declared dual infeasible and x^k is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows. Let

$$\bar{x} := \frac{x^k}{-c^T x^k}$$

and it is easy to verify that

$$\|A\bar{x}\|_\infty \leq \varepsilon_i \text{ and } c^T \bar{x} = -1$$

which shows $\bar{x}$ is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation.

Primal Infeasiblity Certificate

Next assume that $\rho_{pi}^k \leq 1$ and hence

$$\left\|A^T y^k + s^k\right\|_\infty \leq \varepsilon_i b^T y^k \text{ and } b^T y^k > 0$$

holds. Now in this case the problem is declared primal infeasible and (y^k, s^k) is reported as a certificate of primal infeasibility. The motivation for this stopping criterion is as follows. Let

$$\bar{y} := \frac{y^k}{b^T y^k} \text{ and } \bar{s} := \frac{s^k}{b^T y^k}$$

and it is easy to verify that

$$\left\|A^T \bar{y} + \bar{s}\right\|_\infty \leq \varepsilon_i \text{ and } b^T \bar{y} = 1$$

which shows (y^k, s^k) is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation.

9.3.3 Adjusting optimality criteria

It is possible to adjust the tolerances ε_p, ε_d, ε_g and ε_i using parameters; see table for details.

Table 9.2: Parameters employed in termination criterion

ToleranceParameter	name
ε_p	`MSK_DPAR_INTPNT_CO_TOL_PFEAS`
ε_d	`MSK_DPAR_INTPNT_CO_TOL_DFEAS`
ε_g	`MSK_DPAR_INTPNT_CO_TOL_REL_GAP`
ε_i	`MSK_DPAR_INTPNT_CO_TOL_INFEAS`

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (9.11) reveals that the quality of the solution depends on $\|b\|_\infty$ and $\|c\|_\infty$; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate *[And09]*. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances, ε_p, ε_d, ε_g and ε_i, have to be relaxed together to achieve an effect.

If the optimizer terminates without locating a solution that satisfies the termination criteria, for example because of a stall or other numerical issues, then it will check if the solution found up to that point satisfies the same criteria with all tolerances multiplied by the value of *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*. If this is the case, the solution is still declared as optimal.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

9.3.4 The Interior-point Log

Below is a typical log output from the interior-point optimizer:

```
Optimizer  - threads                : 20
Optimizer  - solved problem         : the primal
Optimizer  - Constraints            : 1
Optimizer  - Cones                  : 2
Optimizer  - Scalar variables       : 6              conic            : 6
Optimizer  - Semi-definite variables: 0              scalarized       : 0
Factor     - setup time             : 0.00           dense det. time  : 0.00
Factor     - ML order time          : 0.00           GP order time    : 0.00
Factor     - nonzeros before factor : 1              after factor     : 1
Factor     - dense dim.             : 0              flops            : 1.70e+01
ITE PFEAS    DFEAS    GFEAS    PRSTATUS   POBJ                DOBJ                MU       TIME
0   1.0e+00  2.9e-01  3.4e+00  0.00e+00   2.414213562e+00     0.000000000e+00     1.0e+00  0.01
1   2.7e-01  7.9e-02  2.2e+00  8.83e-01   6.969257574e-01     -9.685901771e-03    2.7e-01  0.01
2   6.5e-02  1.9e-02  1.2e+00  1.16e+00   7.606090061e-01     6.046141322e-01     6.5e-02  0.01
3   1.7e-03  5.0e-04  2.2e-01  1.12e+00   7.084385672e-01     7.045122560e-01     1.7e-03  0.01
4   1.4e-08  4.2e-09  4.9e-08  1.00e+00   7.071067941e-01     7.071067599e-01     1.4e-08  0.01
```

The first line displays the number of threads used by the optimizer and the second line indicates if the optimizer chose to solve the primal or dual problem (see *MSK_IPAR_INTPNT_SOLVE_FORM*). The next lines display the problem dimensions as seen by the optimizer, and the `Factor...` lines show various statistics. This is followed by the iteration log.

Using the same notation as in Sec. 9.3.1 the columns of the iteration log have the following meaning:

- `ITE`: Iteration index k.

- `PFEAS`: $\left\| Ax^k - b\tau^k \right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.

- `DFEAS`: $\left\| A^T y^k + s^k - c\tau^k \right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.

- `GFEAS`: $\left| -c^T x^k + b^T y^k - \kappa^k \right|$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.

- `PRSTATUS`: This number converges to 1 if the problem has an optimal solution whereas it converges to -1 if that is not the case.

- `POBJ`: $c^T x^k / \tau^k$. An estimate for the primal objective value.

- `DOBJ`: $b^T y^k / \tau^k$. An estimate for the dual objective value.

- `MU`: $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$. The numbers in this column should always converge to zero.

- `TIME`: Time spent since the optimization started (in seconds).

9.4 The Optimizer for Mixed-integer Problems

A problem is a mixed-integer optimization problem when one or more of the variables are constrained to be integer valued. Readers unfamiliar with integer optimization are recommended to consult some relevant literature, e.g. the book *[Wol98]* by Wolsey.

9.4.1 The Mixed-integer Optimizer Overview

MOSEK can solve mixed-integer

- linear,

- quadratic and quadratically constrained, and

- conic

problems, except for mixed-integer semidefinite problems. The mixed-integer optimizer is specialized for solving linear and conic optimization problems. Pure quadratic and quadratically constrained problems are automatically converted to conic form.

By default the mixed-integer optimizer is run-to-run deterministic. This means that if a problem is solved twice on the same computer with identical parameter settings and no time limit then the obtained solutions will be identical. If a time limit is set then this may not be case since the time taken to solve a problem is not deterministic. The mixed-integer optimizer is parallelized i.e. it can exploit multiple cores during the optimization.

The solution process can be split into these phases:

1. **Presolve:** See Sec. 9.1.

2. **Cut generation:** Valid inequalities (cuts) are added to improve the lower bound.

3. **Heuristic:** Using heuristics the optimizer tries to guess a good feasible solution. Heuristics can be controlled by the parameter `MSK_IPAR_MIO_HEURISTIC_LEVEL`.

4. **Search:** The optimal solution is located by branching on integer variables.

9.4.2 Relaxations and bounds

It is important to understand that, in a worst-case scenario, the time required to solve integer optimization problems grows exponentially with the size of the problem (solving mixed-integer problems is NP-hard). For instance, a problem with n binary variables, may require time proportional to 2^n. The value of 2^n is huge even for moderate values of n.

In practice this implies that the focus should be on computing a near-optimal solution quickly rather than on locating an optimal solution. Even if the problem is only solved approximately, it is important to know how far the approximate solution is from an optimal one. In order to say something about the quality of an approximate solution the concept of *relaxation* is important.

Consider for example a mixed-integer optimization problem

$$
\begin{aligned}
z^* \quad = \quad &\text{minimize} & c^T x \\
&\text{subject to} & Ax &= b, \\
& & x &\geq 0 \\
& & x_j &\in \mathbb{Z}, & \forall j \in \mathcal{J}.
\end{aligned}
\tag{9.12}
$$

It has the continuous relaxation

$$
\begin{aligned}
\underline{z} \quad = \quad &\text{minimize} & c^T x \\
&\text{subject to} & Ax &= b, \\
& & x &\geq 0
\end{aligned}
\tag{9.13}
$$

obtained simply by ignoring the integrality restrictions. The relaxation is a continuous problem, and therefore much faster to solve to optimality with a linear (or, in the general case, conic) optimizer. We call the optimal value $\underline{z}$ the *objective bound*. The objective bound $\underline{z}$ normally increases during the solution search process when the continuous relaxation is gradually refined.

Moreover, if $\hat{x}$ is any feasible solution to (9.12) and

$$\bar{z} := c^T \hat{x}$$

then

$$\underline{z} \leq z^* \leq \bar{z}.$$

These two inequalities allow us to estimate the quality of the integer solution: it is no further away from the optimum than $\bar{z} - \underline{z}$ in terms of the objective value. Whenever a mixed-integer problem is solved **MOSEK** reports this lower bound so that the quality of the reported solution can be evaluated.

9.4.3 Outer approximation for mixed-integer conic problems

The relaxations of mixed integer conic problems can be solved either as a nonlinear problem with the interior point algorithm (default) or with a linear outer approximation algorithm. The type of relaxation used can be set with `MSK_IPAR_MIO_CONIC_OUTER_APPROXIMATION`. The best value for this option is highly problem dependent.

9.4.4 Randomization

A number of internal algorithms of the mixed-integer solver are dependend on random tie-breaking. The random tie-breaking can have a significant impact on the path taken by the algorithm and the optimal solution returned. The random seed can be set with the parameter `MSK_IPAR_MIO_SEED`.

9.4.5 Termination Criterion

In general, it is time consuming to find an exact feasible and optimal solution to an integer optimization problem, though in many practical cases it may be possible to find a sufficiently good solution. The issue of terminating the mixed-integer optimizer is rather delicate and the user has numerous possibilities of influencing it with various parameters. The mixed-integer optimizer employs a relaxed feasibility and optimality criterion to determine when a satisfactory solution is located.

A candidate solution that is feasible for the continuous relaxation is said to be an *integer feasible solution* if the criterion

$$\min(x_j - \lfloor x_j \rfloor, \lceil x_j \rceil - x_j) \leq \delta_1 \quad \forall j \in \mathcal{J}$$

is satisfied, meaning that x_j is at most δ_1 from the nearest integer.

Whenever the integer optimizer locates an integer feasible solution it will check if the criterion

$$\bar{z} - \underline{z} \leq \max(\delta_2, \delta_3 \max(\delta_4, |\bar{z}|))$$

is satisfied. If this is the case, the integer optimizer terminates and reports the integer feasible solution as an optimal solution.

All the δ tolerances discussed above can be adjusted using suitable parameters — see Table 9.3.

Table 9.3: Tolerances for the mixed-integer optimizer.

Tolerance	Parameter name
δ_1	`MSK_DPAR_MIO_TOL_ABS_RELAX_INT`
δ_2	`MSK_DPAR_MIO_TOL_ABS_GAP`
δ_3	`MSK_DPAR_MIO_TOL_REL_GAP`
δ_4	`MSK_DPAR_MIO_REL_GAP_CONST`

In Table 9.4 some other common parameters affecting the integer optimizer termination criterion are shown.

Table 9.4: Other parameters affecting the integer optimizer termination criterion.

Parameter name	Explanation
`MSK_IPAR_MIO_MAX_NUM_BRANCHES`	Maximum number of branches allowed.
`MSK_IPAR_MIO_MAX_NUM_RELAXS`	Maximum number of relaxations allowed.
`MSK_IPAR_MIO_MAX_NUM_SOLUTIONS`	Maximum number of feasible integer solutions allowed.

9.4.6 Speeding Up the Solution Process

As mentioned previously, in many cases it is not possible to find an optimal solution to an integer optimization problem in a reasonable amount of time. Some suggestions to reduce the solution time are:

- Relax the termination criterion: In case the run time is not acceptable, the first thing to do is to relax the termination criterion — see Sec. 9.4.5 for details.

- Specify a good initial solution: In many cases a good feasible solution is either known or easily computed using problem-specific knowledge. If a good feasible solution is known, it is usually worthwhile to use this as a starting point for the integer optimizer.

- Improve the formulation: A mixed-integer optimization problem may be impossible to solve in one form and quite easy in another form. However, it is beyond the scope of this manual to discuss good formulations for mixed-integer problems. For discussions on this topic see for example *[Wol98]*.

9.4.7 Understanding Solution Quality

To determine the quality of the solution one should check the following:

- The problem status and solution status returned by **MOSEK**, as well as constraint violations in case of suboptimal solutions.

- The *optimality gap* defined as

$$\epsilon = |(\text{objective value of feasible solution}) - (\text{objective bound})| = |\bar{z} - \underline{z}|.$$

which measures how much the located solution can deviate from the optimal solution to the problem. The optimality gap can be retrieved through the information item `MSK_DINF_MIO_OBJ_ABS_GAP`. Often it is more meaningful to look at the relative optimality gap normalized against the magnitude of the solution.

$$\epsilon_{\text{rel}} = \frac{|\bar{z} - \underline{z}|}{\max(\delta_4, |\bar{z}|)}.$$

The relative optimality gap is available in the information item `MSK_DINF_MIO_OBJ_REL_GAP`.

9.4.8 The Mixed-integer Log

Below is a typical log output from the mixed-integer optimizer:

```
Presolved problem: 6573 variables, 35728 constraints, 101258 non-zeros
Presolved problem: 0 general integer, 4294 binary, 2279 continuous
Clique table size: 1636
BRANCHES RELAXS   ACT_NDS DEPTH    BEST_INT_OBJ           BEST_RELAX_OBJ         REL_GAP(%)  TIME
0        1        0       0        NA                     1.8218819866e+07       NA          1.6
0        1        0       0        1.8331557950e+07       1.8218819866e+07       0.61        3.5
0        1        0       0        1.8300507546e+07       1.8218819866e+07       0.45        4.3
Cut generation started.
0        2        0       0        1.8300507546e+07       1.8218819866e+07       0.45        5.3
Cut generation terminated. Time = 1.43
0        3        0       0        1.8286893047e+07       1.8231580587e+07       0.30        7.5
15       18       1       0        1.8286893047e+07       1.8231580587e+07       0.30        10.5
31       34       1       0        1.8286893047e+07       1.8231580587e+07       0.30        11.1
51       54       1       0        1.8286893047e+07       1.8231580587e+07       0.30        11.6
91       94       1       0        1.8286893047e+07       1.8231580587e+07       0.30        12.4
171      174      1       0        1.8286893047e+07       1.8231580587e+07       0.30        14.3
331      334      1       0        1.8286893047e+07       1.8231580587e+07       0.30        17.9


[ ... ]


Objective of best integer solution : 1.825846762609e+07
Best objective bound               : 1.823311032986e+07
Construct solution objective       : Not employed
Construct solution # roundings     : 0
User objective cut value           : 0
Number of cuts generated           : 117
  Number of Gomory cuts            : 108
  Number of CMIR cuts              : 9
```

```
Number of branches             : 4425
Number of relaxations solved   : 4410
Number of interior point iterations: 25
Number of simplex iterations   : 221131
```

The first lines contain a summary of the problem as seen by the optimizer. This is followed by the iteration log. The columns have the following meaning:

- `BRANCHES`: Number of branches generated.

- `RELAXS`: Number of relaxations solved.

- `ACT_NDS`: Number of active branch bound nodes.

- `DEPTH`: Depth of the recently solved node.

- `BEST_INT_OBJ`: The best integer objective value, $\bar{z}$.

- `BEST_RELAX_OBJ`: The best objective bound, $\underline{z}$.

- `REL_GAP(%)`: Relative optimality gap, $100\% \cdot \epsilon_{\mathrm{rel}}$

- `TIME`: Time (in seconds) from the start of optimization.

Following that a summary of the optimization process is printed.

Chapter 10

Additional features

In this section we describe additional features and tools which enable more detailed analysis of optimization problems with **MOSEK**.

10.1 Problem Analyzer

The problem analyzer prints a survey of the structure of the problem, with information about linear constraints and objective, quadratic constraints, conic constraints and variables.

In the initial stages of model formulation the problem analyzer may be used as a quick way of verifying that the model has been built or imported correctly. In later stages it can help revealing special structures within the model that may be used to tune the optimizer's performance or to identify the causes of numerical difficulties.

The problem analyzer is run from the command line using the *-anapro* argument and produces output similar to the following (this is the problem analyzer's survey of the `aflow30a` problem from the MIPLIB 2003 collection.)

```
                    Analyzing the problem

*** Structural report
            Dimensions
            Constraints    Variables     Matrix var.    Cones
            479            842           0              0

            Constraint and bound types
            Free           Lower         Upper          Ranged         Fixed
 Constraints:  0           0             421            0              58
   Variables:  0           0             0              842            0

            Integer constraint types
            Binary         General
            421            0

*** Data report
            Nonzeros       Min           Max
      |cj|:  421           1.1e+01       5.0e+02
     |Aij|:  2091          1.0e+00       1.0e+02

            # finite       Min           Max
     |blci|: 58            1.0e+00       1.0e+01
     |buci|: 479           0.0e+00       1.0e+01
     |blxj|: 842           0.0e+00       0.0e+00
     |buxj|: 842           1.0e+00       1.0e+02

*** Done analyzing the problem
```

The survey is divided into a structural and numerical report. The content should be self-explanatory.

10.2 Automatic Repair of Infeasible Problems

MOSEK provides an automatic repair tool for infeasible linear problems which we cover in this section. Note that most infeasible models are so due to bugs which can (and should) be more reliably fixed manually, using the knowledge of the model structure. We discuss this approach in Sec. 7.3.

10.2.1 Automatic repair

The main idea can be described as follows. Consider the linear optimization problem with m constraints and n variables

$$
\begin{array}{lrcl}
\text{minimize} & c^T x + c^f \\
\text{subject to} & l^c \leq & Ax & \leq u^c, \\
& l^x \leq & x & \leq u^x,
\end{array}
$$

which is assumed to be infeasible.

One way of making the problem feasible is to reduce the lower bounds and increase the upper bounds. If the change is sufficiently large the problem becomes feasible. Now an obvious idea is to compute the optimal relaxation by solving an optimization problem. The problem

$$
\begin{array}{lrcll}
\text{minimize} & p(v_l^c, v_u^c, v_l^x, v_u^x) \\
\text{subject to} & l^c \leq & Ax + v_l^c - v_u^c & \leq & u^c, \\
& l^x \leq & x + v_l^x - v_u^x & \leq & u^x, \\
& v_l^c, v_u^c, v_l^x, v_u^x \geq 0
\end{array} \tag{10.1}
$$

does exactly that. The additional variables $(v_l^c)_i$, $(v_u^c)_i$, $(v_l^x)_j$ and $(v_u^c)_j$ are *elasticity* variables because they allow a constraint to be violated and hence add some elasticity to the problem. For instance, the elasticity variable $(v_l^c)_i$ controls how much the lower bound $(l^c)_i$ should be relaxed to make the problem feasible. Finally, the so-called penalty function

$$
p(v_l^c, v_u^c, v_l^x, v_u^x)
$$

is chosen so it penalizes changes to bounds. Given the weights

- $w_l^c \in \mathbb{R}^m$ (associated with l^c),

- $w_u^c \in \mathbb{R}^m$ (associated with u^c),

- $w_l^x \in \mathbb{R}^n$ (associated with l^x),

- $w_u^x \in \mathbb{R}^n$ (associated with u^x),

a natural choice is

$$
p(v_l^c, v_u^c, v_l^x, v_u^x) = (w_l^c)^T v_l^c + (w_u^c)^T v_u^c + (w_l^x)^T v_l^x + (w_u^x)^T v_u^x.
$$

Hence, the penalty function $p()$ is a weighted sum of the elasticity variables and therefore the problem (10.1) keeps the amount of relaxation at a minimum. Please observe that

- the problem (10.1) is always feasible.

- a negative weight implies problem (10.1) is unbounded. For this reason if the value of a weight is negative **MOSEK** fixes the associated elasticity variable to zero. Clearly, if one or more of the weights are negative, it may imply that it is not possible to repair the problem.

A simple choice of weights is to set them all to 1, but of course that does not take into account that constraints may have different importance.

Caveats

Observe if the infeasible problem

$$
\begin{array}{rrcl}
\text{minimize} & x + z & & \\
\text{subject to} & x & = & -1, \\
& x & \geq & 0
\end{array}
$$

is repaired then it will become unbounded. Hence, a repaired problem may not have an optimal solution.

Another and more important caveat is that only a minimal repair is performed i.e. the repair that barely makes the problem feasible. Hence, the repaired problem is barely feasible and that sometimes makes the repaired problem hard to solve.

Using the automatic repair tool

In this subsection we consider an infeasible linear optimization example:

$$
\begin{array}{rrcrcl}
\text{minimize} & -10x_1 & & -9x_2, & & \\
\text{subject to} & 7/10x_1 & + & 1x_2 & \leq & 630, \\
& 1/2x_1 & + & 5/6x_2 & \leq & 600, \\
& 1x_1 & + & 2/3x_2 & \leq & 708, \\
& 1/10x_1 & + & 1/4x_2 & \leq & 135, \\
& x_1, & & x_2 & \geq & 0, \\
& & & x_2 & \geq & 650.
\end{array}
\tag{10.2}
$$

The problem (10.2) is contained in a file:

Listing 10.1: Problem (10.2) in LP format.

```
minimize
 obj: - 10 x1 - 9 x2
st
 c1: + 7e-01 x1 + x2 <= 630
 c2: + 5e-01 x1 + 8.333333333e-01 x2 <= 600
 c3: + x1 + 6.6666667e-01 x2 <= 708
 c4: + 1e-01 x1 + 2.5e-01 x2 <= 135
bounds
x2 >= 650
end
```

Given the assumption that all weights are 1 the command

```
mosek -primalrepair -d MSK_IPAR_LOG_FEAS_REPAIR 3 feasrepair.lp
```

will form the repaired problem and solve it. The parameter *MSK_IPAR_LOG_FEAS_REPAIR* controls the amount of log output from the repair. A value of 2 causes the optimal repair to printed out. The output from running the above command is:

```
MOSEK Version 9.0.0.25(ALPHA) (Build date: 2017-11-7 16:11:50)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file 'feasrepair.lp'
Reading started.
Reading terminated. Time: 0.00

Read summary
  Type             : LO (linear optimization problem)
  Objective sense  : min
  Scalar variables : 2
  Matrix variables : 0
  Constraints      : 4
  Cones            : 0
```

```
   Time              : 0.0

Problem
  Name                   :
  Objective sense        : min
  Type                   : LO (linear optimization problem)
  Constraints            : 4
  Cones                  : 0
  Scalar variables       : 2
  Matrix variables       : 0
  Integer variables      : 0

Primal feasibility repair started.
Optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Freed constraints in eliminator : 2
Eliminator terminated.
Eliminator - tries               : 1                  time                    : 0.00
Lin. dep.  - tries               : 1                  time                    : 0.00
Lin. dep.  - number              : 0
Presolve terminated. Time: 0.00
Problem
  Name                   :
  Objective sense        : min
  Type                   : LO (linear optimization problem)
  Constraints            : 8
  Cones                  : 0
  Scalar variables       : 14
  Matrix variables       : 0
  Integer variables      : 0

Optimizer  - threads              : 20
Optimizer  - solved problem       : the primal
Optimizer  - Constraints          : 2
Optimizer  - Cones                : 0
Optimizer  - Scalar variables     : 5                  conic                   : 0
Optimizer  - Semi-definite variables: 0                scalarized              : 0
Factor     - setup time           : 0.00               dense det. time         : 0.00
Factor     - ML order time        : 0.00               GP order time           : 0.00
Factor     - nonzeros before factor : 3                after factor            : 3
Factor     - dense dim.           : 0                  flops                   : 5.00e+01
ITE PFEAS    DFEAS    GFEAS    PRSTATUS   POBJ               DOBJ                MU       TIME
0   2.7e+01  1.0e+00  4.0e+00  1.00e+00   3.000000000e+00    0.000000000e+00    1.0e+00  0.00
1   2.5e+01  9.1e-01  1.4e+00  0.00e+00   8.711262850e+00    1.115287830e+01    2.4e+00  0.00
2   2.4e+00  8.8e-02  1.4e-01  -7.33e-01  4.062505701e+01    4.422203730e+01    2.3e-01  0.00
3   9.4e-02  3.4e-03  5.5e-03  1.33e+00   4.250700434e+01    4.258548510e+01    9.1e-03  0.00
4   2.0e-05  7.2e-07  1.1e-06  1.02e+00   4.249996599e+01    4.249998669e+01    1.9e-06  0.00
5   2.0e-09  7.2e-11  1.1e-10  1.00e+00   4.250000000e+01    4.250000000e+01    1.9e-10  0.00
Basis identification started.
Basis identification terminated. Time: 0.00
Optimizer terminated. Time: 0.01


Basic solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 4.2500000000e+01   nrm: 6e+02   Viol.  con: 1e-13   var: 0e+00
  Dual.    obj: 4.2499999999e+01   nrm: 2e+00   Viol.  con: 0e+00   var: 9e-11
Optimal objective value of the penalty problem: 4.250000000000e+01
```

```
Repairing bounds.
Increasing the upper bound 1.35e+02 on constraint 'c4' (3) with 2.25e+01.
Decreasing the lower bound 6.50e+02 on variable 'x2' (4) with 2.00e+01.
Primal feasibility repair terminated.
Optimizer started.
Optimizer terminated. Time: 0.00


Interior-point solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: -5.6700000000e+03   nrm: 6e+02   Viol.  con: 0e+00   var: 0e+00
  Dual.    obj: -5.6700000000e+03   nrm: 1e+01   Viol.  con: 0e+00   var: 0e+00

Basic solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: -5.6700000000e+03   nrm: 6e+02   Viol.  con: 0e+00   var: 0e+00
  Dual.    obj: -5.6700000000e+03   nrm: 1e+01   Viol.  con: 0e+00   var: 0e+00

Optimizer summary
  Optimizer               -                        time: 0.00
    Interior-point        - iterations : 0         time: 0.00
      Basis identification -                       time: 0.00
        Primal            - iterations : 0         time: 0.00
        Dual              - iterations : 0         time: 0.00
        Clean primal      - iterations : 0         time: 0.00
        Clean dual        - iterations : 0         time: 0.00
    Simplex               -                        time: 0.00
      Primal simplex      - iterations : 0         time: 0.00
      Dual simplex        - iterations : 0         time: 0.00
    Mixed integer         - relaxations: 0         time: 0.00
```

In this case the optimal repair it is to increase the upper bound on constraint c4 by 22.5 and decrease the lower bound on variable x2 by 20.

10.3 Sensitivity Analysis

Given an optimization problem it is often useful to obtain information about how the optimal objective value changes when the problem parameters are perturbed. E.g, assume that a bound represents the capacity of a machine. Now, it may be possible to expand the capacity for a certain cost and hence it is worthwhile knowing what the value of additional capacity is. This is precisely the type of questions the sensitivity analysis deals with.

Analyzing how the optimal objective value changes when the problem data is changed is called *sensitivity analysis*.

References

The book *[Chv83]* discusses the classical sensitivity analysis in Chapter 10 whereas the book *[RTV97]* presents a modern introduction to sensitivity analysis. Finally, it is recommended to read the short paper *[Wal00]* to avoid some of the pitfalls associated with sensitivity analysis.

> **Warning:** Currently, sensitivity analysis is only available for continuous linear optimization problems. Moreover, **MOSEK** can only deal with perturbations of bounds and objective function coefficients.

10.3.1 Sensitivity Analysis for Linear Problems

The Optimal Objective Value Function

Assume that we are given the problem

$$
\begin{array}{rlrcccl}
z(l^c, u^c, l^x, u^x, c) & = & \text{minimize} & & c^T x & & \\
& & \text{subject to} & l^c \leq & Ax & \leq u^c, & \\
& & & l^x \leq & x & \leq u^x, &
\end{array}
\tag{10.3}
$$

and we want to know how the optimal objective value changes as l_i^c is perturbed. To answer this question we define the perturbed problem for l_i^c as follows

$$
\begin{array}{rlrccl}
f_{l_i^c}(\beta) & = & \text{minimize} & & c^T x & \\
& & \text{subject to} & l^c + \beta e_i \leq & Ax & \leq u^c, \\
& & & l^x \leq & x \leq & u^x,
\end{array}
$$

where e_i is the i-th column of the identity matrix. The function

$$
f_{l_i^c}(\beta)
\tag{10.4}
$$

shows the optimal objective value as a function of β. Please note that a change in β corresponds to a perturbation in l_i^c and hence (10.4) shows the optimal objective value as a function of varying l_i^c with the other bounds fixed.

It is possible to prove that the function (10.4) is a piecewise linear and convex function, i.e. its graph may look like in Fig. 10.1 and Fig. 10.2.

Fig. 10.1: $\beta = 0$ is in the interior of linearity interval.

Clearly, if the function $f_{l_i^c}(\beta)$ does not change much when β is changed, then we can conclude that the optimal objective value is insensitive to changes in l_i^c. Therefore, we are interested in the rate of change in $f_{l_i^c}(\beta)$ for small changes in β — specifically the gradient

$$
f'_{l_i^c}(0),
$$

which is called the *shadow price* related to l_i^c. The shadow price specifies how the objective value changes for small changes of β around zero. Moreover, we are interested in the *linearity interval*

$$
\beta \in [\beta_1, \beta_2]
$$

Fig. 10.2: $\beta = 0$ is a breakpoint.

for which

$$f'_{l^c_i}(\beta) = f'_{l^c_i}(0).$$

Since $f_{l^c_i}$ is not a smooth function $f'_{l^c_i}$ may not be defined at 0, as illustrated in Fig. 10.2. In this case we can define a left and a right shadow price and a left and a right linearity interval.

The function $f_{l^c_i}$ considered only changes in l^c_i. We can define similar functions for the remaining parameters of the z defined in (10.3) as well:

$$
\begin{array}{rcll}
f_{l^c_i}(\beta) & = & z(l^c + \beta e_i, u^c, l^x, u^x, c), & i = 1, \ldots, m, \\
f_{u^c_i}(\beta) & = & z(l^c, u^c + \beta e_i, l^x, u^x, c), & i = 1, \ldots, m, \\
f_{l^x_j}(\beta) & = & z(l^c, u^c, l^x + \beta e_j, u^x, c), & j = 1, \ldots, n, \\
f_{u^x_j}(\beta) & = & z(l^c, u^c, l^x, u^x + \beta e_j, c), & j = 1, \ldots, n, \\
f_{c_j}(\beta) & = & z(l^c, u^c, l^x, u^x, c + \beta e_j), & j = 1, \ldots, n.
\end{array}
$$

Given these definitions it should be clear how linearity intervals and shadow prices are defined for the parameters u^c_i etc.

Equality Constraints

In **MOSEK** a constraint can be specified as either an equality constraint or a ranged constraint. If some constraint e^c_i is an equality constraint, we define the optimal value function for this constraint as

$$f_{e^c_i}(\beta) = z(l^c + \beta e_i, u^c + \beta e_i, l^x, u^x, c)$$

Thus for an equality constraint the upper and the lower bounds (which are equal) are perturbed simultaneously. Therefore, **MOSEK** will handle sensitivity analysis differently for a ranged constraint with $l^c_i = u^c_i$ and for an equality constraint.

The Basis Type Sensitivity Analysis

The classical sensitivity analysis discussed in most textbooks about linear optimization, e.g. *[Chv83]*, is based on an optimal basis. This method may produce misleading results *[RTV97]* but is computationally cheap. This is the type of sensitivity analysis implemented in **MOSEK**.

We will now briefly discuss the basis type sensitivity analysis. Given an optimal basic solution which provides a partition of variables into basic and non-basic variables, the basis type sensitivity analysis

computes the linearity interval $[\beta_1, \beta_2]$ so that the basis remains optimal for the perturbed problem. A shadow price associated with the linearity interval is also computed. However, it is well-known that an optimal basic solution may not be unique and therefore the result depends on the optimal basic solution employed in the sensitivity analysis. If the optimal objective value function has a breakpoint for $\beta = 0$ then the basis type sensitivity method will only provide a subset of either the left or the right linearity interval.

In summary, the basis type sensitivity analysis is computationally cheap but does not provide complete information. Hence, the results of the basis type sensitivity analysis should be used with care.

Example: Sensitivity Analysis

As an example we will use the following transportation problem. Consider the problem of minimizing the transportation cost between a number of production plants and stores. Each plant supplies a number of goods and each store has a given demand that must be met. Supply, demand and cost of transportation per unit are shown in Fig. 10.3.

Fig. 10.3: Supply, demand and cost of transportation.

If we denote the number of transported goods from location i to location j by x_{ij}, problem can be formulated as the linear optimization problem of minimizing

$$1x_{11} \quad + \quad 2x_{12} \quad + \quad 5x_{23} \quad + \quad 2x_{24} \quad + \quad 1x_{31} \quad + \quad 2x_{33} \quad + \quad 1x_{34}$$

subject to

$$
\begin{array}{rcl}
x_{11} + x_{12} & \leq & 400, \\
x_{23} + x_{24} & \leq & 1200, \\
x_{31} + x_{33} + x_{34} & \leq & 1000, \\
x_{11} + x_{31} & = & 800, \\
x_{12} & = & 100, \\
x_{23} + x_{33} & = & 500, \\
x_{24} + x_{34} & = & 500, \\
x_{11}, \quad x_{12}, \quad x_{23}, \quad x_{24}, \quad x_{31}, \quad x_{33}, \quad x_{34} & \geq & 0.
\end{array}
\tag{10.5}
$$

The sensitivity parameters are shown in Table 10.1 and Table 10.2.

Table 10.1: Ranges and shadow prices related to bounds on constraints and variables.

Con.	β_1	β_2	σ_1	σ_2
1	-300.00	0.00	3.00	3.00
2	-700.00	$+\infty$	0.00	0.00
3	-500.00	0.00	3.00	3.00
4	-0.00	500.00	4.00	4.00
5	-0.00	300.00	5.00	5.00
6	-0.00	700.00	5.00	5.00
7	-500.00	700.00	2.00	2.00
Var.	β_1	β_2	σ_1	σ_2
x_{11}	$-\infty$	300.00	0.00	0.00
x_{12}	$-\infty$	100.00	0.00	0.00
x_{23}	$-\infty$	0.00	0.00	0.00
x_{24}	$-\infty$	500.00	0.00	0.00
x_{31}	$-\infty$	500.00	0.00	0.00
x_{33}	$-\infty$	500.00	0.00	0.00
x_{34}	-0.000000	500.00	2.00	2.00

Table 10.2: Ranges and shadow prices related to the objective coefficients.

Var.	β_1	β_2	σ_1	σ_2
c_1	$-\infty$	3.00	300.00	300.00
c_2	$-\infty$	∞	100.00	100.00
c_3	-2.00	∞	0.00	0.00
c_4	$-\infty$	2.00	500.00	500.00
c_5	-3.00	∞	500.00	500.00
c_6	$-\infty$	2.00	500.00	500.00
c_7	-2.00	∞	0.00	0.00

Examining the results from the sensitivity analysis we see that for constraint number 1 we have $\sigma_1 = 3$ and $\beta_1 = -300, \ \beta_2 = 0$.

If the upper bound on constraint 1 is decreased by

$$\beta \in [0, 300]$$

then the optimal objective value will increase by the value

$$\sigma_1 \beta = 3\beta.$$

10.3.2 Sensitivity Analysis with MOSEK

A sensitivity analysis can be performed with the **MOSEK** command line tool specifying the option *-sen*, e.g.

```
mosek myproblem.mps -sen sensitivity.ssp
```

where `sensitivity.ssp` is a file in the format described in the next section. The `ssp` file describes which parts of the problem the sensitivity analysis should be performed on, see Sec. 10.3.2.

By default results are written to a file named `myproblem.sen`. If necessary, this file name can be changed by setting the *MSK_SPAR_SENSITIVITY_RES_FILE_NAME* parameter.

Sensitivity Analysis Specification File

MOSEK employs an MPS-like file format to specify on which model parameters the sensitivity analysis should be performed. The format of the sensitivity specification file is shown in Listing 10.2, where capitalized names are keywords, and names in brackets are names of the constraints and variables to be included in the analysis.

Listing 10.2: Sensitivity analysis file specification.

```
BOUNDS CONSTRAINTS
U|L|LU [cname1]
U|L|LU [cname2]-[cname3]
BOUNDS VARIABLES
U|L|LU [vname1]
U|L|LU [vname2]-[vname3]
OBJECTIVE VARIABLES
[vname1]
[vname2]-[vname3]
```

The sensitivity specification file has three sections, i.e.

- `BOUNDS CONSTRAINTS`: Specifies on which bounds on constraints the sensitivity analysis should be performed.

- `BOUNDS VARIABLES`: Specifies on which bounds on variables the sensitivity analysis should be performed.

- `OBJECTIVE VARIABLES`: Specifies on which objective coefficients the sensitivity analysis should be performed.

A line in the body of a section must begin with a whitespace. In the `BOUNDS` sections one of the keys `L`, `U`, and `LU` must appear next. These keys specify whether the sensitivity analysis is performed on the lower bound, on the upper bound, or on both the lower and the upper bound respectively. Next, a single constraint (variable) or range of constraints (variables) is specified.

Recall from Sec. 10.3.1 that equality constraints are handled in a special way. Sensitivity analysis of an equality constraint can be specified with either `L`, `U`, or `LU`, all indicating the same, namely that upper and lower bounds (which are equal) are perturbed simultaneously.

As an example consider

```
BOUNDS CONSTRAINTS
L   "cons1"
U   "cons2"
LU "cons3"-"cons6"
```

which requests that sensitivity analysis is performed on the lower bound of the constraint named `cons1`, on the upper bound of the constraint named `cons2`, and on both lower and upper bound on the constraints named `cons3` to `cons6`.

It is allowed to use indexes instead of names, for instance

```
BOUNDS CONSTRAINTS
L   "cons1"
U   2
LU 3 - 6
```

The character `*` indicates that the line contains a comment and is ignored.

Example: Sensitivity Analysis from Command Line

As an example consider problem (10.5): the sensitivity file shown below (included in the distribution among the examples).

```
* Comment 1

BOUNDS CONSTRAINTS
 U "c1"          * Analyze upper bound for constraints named c1
 U 2             * Analyze upper bound for constraints with index 2
 U 3-5           * Analyze upper bound for constraint with index in interval [3:5]

VARIABLES CONSTRAINTS
 L 2-4           * This section specifies which bounds on variables should be analyzed.
 L "x11"
OBJECTIVE CONSTRAINTS
 "x11"           * This section specifies which objective coeficients should be analysed.
 2
```

The command

```
mosek transport.lp -sen sensitivity.ssp
```

produces the output file as follow

Listing 10.4: Results of sensitivity analysis

```
BOUNDS CONSTRAINTS
INDEX    NAME            BOUND    LEFTRANGE       RIGHTRANGE      LEFTPRICE        ␣
↪RIGHTPRICE
0        c1              UP       -6.574875e-18   5.000000e+02    1.000000e+00     1.
↪000000e+00
2        c3              UP       -6.574875e-18   5.000000e+02    1.000000e+00     1.
↪000000e+00
3        c4              FIX      -5.000000e+02   6.574875e-18    2.000000e+00     2.
↪000000e+00
4        c5              FIX      -1.000000e+02   6.574875e-18    3.000000e+00     3.
↪000000e+00
5        c6              FIX      -5.000000e+02   6.574875e-18    3.000000e+00     3.
↪000000e+00

BOUNDS VARIABLES
INDEX    NAME            BOUND    LEFTRANGE       RIGHTRANGE      LEFTPRICE        ␣
↪RIGHTPRICE
2        x23             LO       -6.574875e-18   5.000000e+02    2.000000e+00     2.
↪000000e+00
3        x24             LO       -inf            5.000000e+02    0.000000e+00     0.
↪000000e+00
4        x31             LO       -inf            5.000000e+02    0.000000e+00     0.
↪000000e+00
0        x11             LO       -inf            3.000000e+02    0.000000e+00     0.
↪000000e+00

OBJECTIVE VARIABLES
INDEX    NAME                     LEFTRANGE       RIGHTRANGE      LEFTPRICE        ␣
↪RIGHTPRICE
0        x11                      -inf            1.000000e+00    3.000000e+02     3.
↪000000e+02
2        x23                      -2.000000e+00   +inf            0.000000e+00     0.
↪000000e+00
```

Controlling Log Output

Setting the parameter *MSK_IPAR_LOG_SENSITIVITY* to 1 or 0 (default) controls whether or not the results from sensitivity calculations are printed to the message stream.

The parameter *MSK_IPAR_LOG_SENSITIVITY_OPT* controls the amount of debug information on internal calculations from the sensitivity analysis.

Chapter 11

API Reference

- **Optimizer parameters:**
  - *Double*, *Integer*, *String*
  - *Full list*
  - *Browse by topic*

- *Optimizer response codes*

- *Constants*

11.1 Parameters grouped by topic

Analysis

- `MSK_DPAR_ANA_SOL_INFEAS_TOL`

- `MSK_IPAR_ANA_SOL_BASIS`

- `MSK_IPAR_ANA_SOL_PRINT_VIOLATED`

- `MSK_IPAR_LOG_ANA_PRO`

Basis identification

- `MSK_DPAR_SIM_LU_TOL_REL_PIV`

- `MSK_IPAR_BI_CLEAN_OPTIMIZER`

- `MSK_IPAR_BI_IGNORE_MAX_ITER`

- `MSK_IPAR_BI_IGNORE_NUM_ERROR`

- `MSK_IPAR_BI_MAX_ITERATIONS`

- `MSK_IPAR_INTPNT_BASIS`

- `MSK_IPAR_LOG_BI`

- `MSK_IPAR_LOG_BI_FREQ`

Conic interior-point method

- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*

Data check

- *MSK_DPAR_DATA_SYM_MAT_TOL*
- *MSK_DPAR_DATA_SYM_MAT_TOL_HUGE*
- *MSK_DPAR_DATA_SYM_MAT_TOL_LARGE*
- *MSK_DPAR_DATA_TOL_AIJ_HUGE*
- *MSK_DPAR_DATA_TOL_AIJ_LARGE*
- *MSK_DPAR_DATA_TOL_BOUND_INF*
- *MSK_DPAR_DATA_TOL_BOUND_WRN*
- *MSK_DPAR_DATA_TOL_C_HUGE*
- *MSK_DPAR_DATA_TOL_CJ_LARGE*
- *MSK_DPAR_DATA_TOL_QIJ*
- *MSK_DPAR_DATA_TOL_X*
- *MSK_DPAR_SEMIDEFINITE_TOL_APPROX*
- *MSK_IPAR_CHECK_CONVEXITY*
- *MSK_IPAR_LOG_CHECK_CONVEXITY*

Data input/output

- *MSK_IPAR_INFEAS_REPORT_AUTO*
- *MSK_IPAR_LOG_FILE*
- *MSK_IPAR_OPF_WRITE_HEADER*
- *MSK_IPAR_OPF_WRITE_HINTS*
- *MSK_IPAR_OPF_WRITE_LINE_LENGTH*
- *MSK_IPAR_OPF_WRITE_PARAMETERS*
- *MSK_IPAR_OPF_WRITE_PROBLEM*
- *MSK_IPAR_OPF_WRITE_SOL_BAS*
- *MSK_IPAR_OPF_WRITE_SOL_ITG*
- *MSK_IPAR_OPF_WRITE_SOL_ITR*
- *MSK_IPAR_OPF_WRITE_SOLUTIONS*

- *MSK_IPAR_PARAM_READ_CASE_NAME*
- *MSK_IPAR_PARAM_READ_IGN_ERROR*
- *MSK_IPAR_PTF_WRITE_TRANSFORM*
- *MSK_IPAR_READ_DEBUG*
- *MSK_IPAR_READ_KEEP_FREE_CON*
- *MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU*
- *MSK_IPAR_READ_LP_QUOTED_NAMES*
- *MSK_IPAR_READ_MPS_FORMAT*
- *MSK_IPAR_READ_MPS_WIDTH*
- *MSK_IPAR_READ_TASK_IGNORE_PARAM*
- *MSK_IPAR_SOL_READ_NAME_WIDTH*
- *MSK_IPAR_SOL_READ_WIDTH*
- *MSK_IPAR_WRITE_BAS_CONSTRAINTS*
- *MSK_IPAR_WRITE_BAS_HEAD*
- *MSK_IPAR_WRITE_BAS_VARIABLES*
- *MSK_IPAR_WRITE_COMPRESSION*
- *MSK_IPAR_WRITE_DATA_PARAM*
- *MSK_IPAR_WRITE_FREE_CON*
- *MSK_IPAR_WRITE_GENERIC_NAMES*
- *MSK_IPAR_WRITE_GENERIC_NAMES_IO*
- *MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS*
- *MSK_IPAR_WRITE_INT_CONSTRAINTS*
- *MSK_IPAR_WRITE_INT_HEAD*
- *MSK_IPAR_WRITE_INT_VARIABLES*
- *MSK_IPAR_WRITE_LP_FULL_OBJ*
- *MSK_IPAR_WRITE_LP_LINE_WIDTH*
- *MSK_IPAR_WRITE_LP_QUOTED_NAMES*
- *MSK_IPAR_WRITE_LP_STRICT_FORMAT*
- *MSK_IPAR_WRITE_LP_TERMS_PER_LINE*
- *MSK_IPAR_WRITE_MPS_FORMAT*
- *MSK_IPAR_WRITE_MPS_INT*
- *MSK_IPAR_WRITE_PRECISION*
- *MSK_IPAR_WRITE_SOL_BARVARIABLES*
- *MSK_IPAR_WRITE_SOL_CONSTRAINTS*
- *MSK_IPAR_WRITE_SOL_HEAD*
- *MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES*

- *MSK_IPAR_WRITE_SOL_VARIABLES*

- *MSK_IPAR_WRITE_TASK_INC_SOL*

- *MSK_IPAR_WRITE_XML_MODE*

- *MSK_SPAR_BAS_SOL_FILE_NAME*

- *MSK_SPAR_DATA_FILE_NAME*

- *MSK_SPAR_DEBUG_FILE_NAME*

- *MSK_SPAR_INT_SOL_FILE_NAME*

- *MSK_SPAR_ITR_SOL_FILE_NAME*

- *MSK_SPAR_MIO_DEBUG_STRING*

- *MSK_SPAR_PARAM_COMMENT_SIGN*

- *MSK_SPAR_PARAM_READ_FILE_NAME*

- *MSK_SPAR_PARAM_WRITE_FILE_NAME*

- *MSK_SPAR_READ_MPS_BOU_NAME*

- *MSK_SPAR_READ_MPS_OBJ_NAME*

- *MSK_SPAR_READ_MPS_RAN_NAME*

- *MSK_SPAR_READ_MPS_RHS_NAME*

- *MSK_SPAR_SENSITIVITY_FILE_NAME*

- *MSK_SPAR_SENSITIVITY_RES_FILE_NAME*

- *MSK_SPAR_SOL_FILTER_XC_LOW*

- *MSK_SPAR_SOL_FILTER_XC_UPR*

- *MSK_SPAR_SOL_FILTER_XX_LOW*

- *MSK_SPAR_SOL_FILTER_XX_UPR*

- *MSK_SPAR_STAT_FILE_NAME*

- *MSK_SPAR_STAT_KEY*

- *MSK_SPAR_STAT_NAME*

- *MSK_SPAR_WRITE_LP_GEN_VAR_NAME*

Debugging

- *MSK_IPAR_AUTO_SORT_A_BEFORE_OPT*

Dual simplex

- *MSK_IPAR_SIM_DUAL_CRASH*

- *MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION*

- *MSK_IPAR_SIM_DUAL_SELECTION*

Infeasibility report

- *MSK_IPAR_INFEAS_GENERIC_NAMES*
- *MSK_IPAR_INFEAS_REPORT_LEVEL*
- *MSK_IPAR_LOG_INFEAS_ANA*

Interior-point method

- *MSK_DPAR_CHECK_CONVEXITY_REL_TOL*
- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_DFEAS*
- *MSK_DPAR_INTPNT_TOL_DSAFE*
- *MSK_DPAR_INTPNT_TOL_INFEAS*
- *MSK_DPAR_INTPNT_TOL_MU_RED*
- *MSK_DPAR_INTPNT_TOL_PATH*
- *MSK_DPAR_INTPNT_TOL_PFEAS*
- *MSK_DPAR_INTPNT_TOL_PSAFE*
- *MSK_DPAR_INTPNT_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_REL_STEP*
- *MSK_DPAR_INTPNT_TOL_STEP_SIZE*
- *MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL*
- *MSK_IPAR_BI_IGNORE_MAX_ITER*
- *MSK_IPAR_BI_IGNORE_NUM_ERROR*
- *MSK_IPAR_INTPNT_BASIS*
- *MSK_IPAR_INTPNT_DIFF_STEP*
- *MSK_IPAR_INTPNT_HOTSTART*
- *MSK_IPAR_INTPNT_MAX_ITERATIONS*

- *MSK_IPAR_INTPNT_MAX_NUM_COR*

- *MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS*

- *MSK_IPAR_INTPNT_OFF_COL_TRH*

- *MSK_IPAR_INTPNT_ORDER_GP_NUM_SEEDS*

- *MSK_IPAR_INTPNT_ORDER_METHOD*

- *MSK_IPAR_INTPNT_PURIFY*

- *MSK_IPAR_INTPNT_REGULARIZATION_USE*

- *MSK_IPAR_INTPNT_SCALING*

- *MSK_IPAR_INTPNT_SOLVE_FORM*

- *MSK_IPAR_INTPNT_STARTING_POINT*

- *MSK_IPAR_LOG_INTPNT*

License manager

- *MSK_IPAR_CACHE_LICENSE*

- *MSK_IPAR_LICENSE_DEBUG*

- *MSK_IPAR_LICENSE_PAUSE_TIME*

- *MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS*

- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*

- *MSK_IPAR_LICENSE_WAIT*

Logging

- *MSK_IPAR_LOG*

- *MSK_IPAR_LOG_ANA_PRO*

- *MSK_IPAR_LOG_BI*

- *MSK_IPAR_LOG_BI_FREQ*

- *MSK_IPAR_LOG_CUT_SECOND_OPT*

- *MSK_IPAR_LOG_EXPAND*

- *MSK_IPAR_LOG_FEAS_REPAIR*

- *MSK_IPAR_LOG_FILE*

- *MSK_IPAR_LOG_INCLUDE_SUMMARY*

- *MSK_IPAR_LOG_INFEAS_ANA*

- *MSK_IPAR_LOG_INTPNT*

- *MSK_IPAR_LOG_LOCAL_INFO*

- *MSK_IPAR_LOG_MIO*

- *MSK_IPAR_LOG_MIO_FREQ*

- *MSK_IPAR_LOG_ORDER*

- *MSK_IPAR_LOG_PRESOLVE*

- *MSK_IPAR_LOG_RESPONSE*

- *MSK_IPAR_LOG_SENSITIVITY*

- *MSK_IPAR_LOG_SENSITIVITY_OPT*

- *MSK_IPAR_LOG_SIM*

- *MSK_IPAR_LOG_SIM_FREQ*

- *MSK_IPAR_LOG_STORAGE*

Mixed-integer optimization

- *MSK_DPAR_MIO_MAX_TIME*

- *MSK_DPAR_MIO_REL_GAP_CONST*

- *MSK_DPAR_MIO_TOL_ABS_GAP*

- *MSK_DPAR_MIO_TOL_ABS_RELAX_INT*

- *MSK_DPAR_MIO_TOL_FEAS*

- *MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT*

- *MSK_DPAR_MIO_TOL_REL_GAP*

- *MSK_IPAR_LOG_MIO*

- *MSK_IPAR_LOG_MIO_FREQ*

- *MSK_IPAR_MIO_BRANCH_DIR*

- *MSK_IPAR_MIO_CONIC_OUTER_APPROXIMATION*

- *MSK_IPAR_MIO_CUT_CLIQUE*

- *MSK_IPAR_MIO_CUT_CMIR*

- *MSK_IPAR_MIO_CUT_GMI*

- *MSK_IPAR_MIO_CUT_IMPLIED_BOUND*

- *MSK_IPAR_MIO_CUT_KNAPSACK_COVER*

- *MSK_IPAR_MIO_CUT_SELECTION_LEVEL*

- *MSK_IPAR_MIO_FEASPUMP_LEVEL*

- *MSK_IPAR_MIO_HEURISTIC_LEVEL*

- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*

- *MSK_IPAR_MIO_MAX_NUM_RELAXS*

- *MSK_IPAR_MIO_MAX_NUM_ROOT_CUT_ROUNDS*

- *MSK_IPAR_MIO_MAX_NUM_SOLUTIONS*

- *MSK_IPAR_MIO_NODE_OPTIMIZER*

- *MSK_IPAR_MIO_NODE_SELECTION*

- *MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE*

- *MSK_IPAR_MIO_PROBING_LEVEL*

- *MSK_IPAR_MIO_PROPAGATE_OBJECTIVE_CONSTRAINT*

- *MSK_IPAR_MIO_RINS_MAX_NODES*

- *MSK_IPAR_MIO_ROOT_OPTIMIZER*

- *MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL*

- *MSK_IPAR_MIO_SEED*

- *MSK_IPAR_MIO_VB_DETECTION_LEVEL*

Output information

- *MSK_IPAR_INFEAS_REPORT_LEVEL*

- *MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS*

- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*

- *MSK_IPAR_LOG*

- *MSK_IPAR_LOG_BI*

- *MSK_IPAR_LOG_BI_FREQ*

- *MSK_IPAR_LOG_CUT_SECOND_OPT*

- *MSK_IPAR_LOG_EXPAND*

- *MSK_IPAR_LOG_FEAS_REPAIR*

- *MSK_IPAR_LOG_FILE*

- *MSK_IPAR_LOG_INCLUDE_SUMMARY*

- *MSK_IPAR_LOG_INFEAS_ANA*

- *MSK_IPAR_LOG_INTPNT*

- *MSK_IPAR_LOG_LOCAL_INFO*

- *MSK_IPAR_LOG_MIO*

- *MSK_IPAR_LOG_MIO_FREQ*

- *MSK_IPAR_LOG_ORDER*

- *MSK_IPAR_LOG_RESPONSE*

- *MSK_IPAR_LOG_SENSITIVITY*

- *MSK_IPAR_LOG_SENSITIVITY_OPT*

- *MSK_IPAR_LOG_SIM*

- *MSK_IPAR_LOG_SIM_FREQ*

- *MSK_IPAR_LOG_SIM_MINOR*

- *MSK_IPAR_LOG_STORAGE*

- *MSK_IPAR_MAX_NUM_WARNINGS*

Overall solver

- *MSK_IPAR_BI_CLEAN_OPTIMIZER*

- *MSK_IPAR_INFEAS_PREFER_PRIMAL*

- *MSK_IPAR_LICENSE_WAIT*

- *MSK_IPAR_MIO_MODE*

- *MSK_IPAR_OPTIMIZER*

- *MSK_IPAR_PRESOLVE_LEVEL*

- *MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS*

- *MSK_IPAR_PRESOLVE_USE*

- *MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER*

- *MSK_IPAR_SENSITIVITY_ALL*

- *MSK_IPAR_SENSITIVITY_OPTIMIZER*

- *MSK_IPAR_SENSITIVITY_TYPE*

- *MSK_IPAR_SOLUTION_CALLBACK*

Overall system

- *MSK_IPAR_AUTO_UPDATE_SOL_INFO*

- *MSK_IPAR_INTPNT_MULTI_THREAD*

- *MSK_IPAR_LICENSE_WAIT*

- *MSK_IPAR_LOG_STORAGE*

- *MSK_IPAR_MT_SPINCOUNT*

- *MSK_IPAR_NUM_THREADS*

- *MSK_IPAR_REMOVE_UNUSED_SOLUTIONS*

- *MSK_IPAR_TIMING_LEVEL*

- *MSK_SPAR_REMOTE_ACCESS_TOKEN*

Presolve

- *MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP*

- *MSK_DPAR_PRESOLVE_TOL_AIJ*

- *MSK_DPAR_PRESOLVE_TOL_REL_LINDEP*

- *MSK_DPAR_PRESOLVE_TOL_S*

- *MSK_DPAR_PRESOLVE_TOL_X*

- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL*

- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES*

- *MSK_IPAR_PRESOLVE_LEVEL*

- *MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH*

- *MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH*

- *MSK_IPAR_PRESOLVE_LINDEP_USE*

- *MSK_IPAR_PRESOLVE_MAX_NUM_PASS*

- *MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS*

- *MSK_IPAR_PRESOLVE_USE*

Primal simplex

- *MSK_IPAR_SIM_PRIMAL_CRASH*

- *MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION*

- *MSK_IPAR_SIM_PRIMAL_SELECTION*

Progress callback

- *MSK_IPAR_SOLUTION_CALLBACK*

Simplex optimizer

- *MSK_DPAR_BASIS_REL_TOL_S*

- *MSK_DPAR_BASIS_TOL_S*

- *MSK_DPAR_BASIS_TOL_X*

- *MSK_DPAR_SIM_LU_TOL_REL_PIV*

- *MSK_DPAR_SIMPLEX_ABS_TOL_PIV*

- *MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE*

- *MSK_IPAR_LOG_SIM*

- *MSK_IPAR_LOG_SIM_FREQ*

- *MSK_IPAR_LOG_SIM_MINOR*

- *MSK_IPAR_SENSITIVITY_OPTIMIZER*

- *MSK_IPAR_SIM_BASIS_FACTOR_USE*

- *MSK_IPAR_SIM_DEGEN*

- *MSK_IPAR_SIM_DUAL_PHASEONE_METHOD*

- *MSK_IPAR_SIM_EXPLOIT_DUPVEC*

- *MSK_IPAR_SIM_HOTSTART*

- *MSK_IPAR_SIM_HOTSTART_LU*

- *MSK_IPAR_SIM_MAX_ITERATIONS*

- *MSK_IPAR_SIM_MAX_NUM_SETBACKS*

- *MSK_IPAR_SIM_NON_SINGULAR*

- *MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD*

- *MSK_IPAR_SIM_REFACTOR_FREQ*

- *MSK_IPAR_SIM_REFORMULATION*

- *MSK_IPAR_SIM_SAVE_LU*

- *MSK_IPAR_SIM_SCALING*

- *MSK_IPAR_SIM_SCALING_METHOD*

- *MSK_IPAR_SIM_SEED*

- *MSK_IPAR_SIM_SOLVE_FORM*

- *MSK_IPAR_SIM_STABILITY_PRIORITY*

- *MSK_IPAR_SIM_SWITCH_OPTIMIZER*

Solution input/output

- *MSK_IPAR_INFEAS_REPORT_AUTO*

- *MSK_IPAR_SOL_FILTER_KEEP_BASIC*

- *MSK_IPAR_SOL_FILTER_KEEP_RANGED*

- *MSK_IPAR_SOL_READ_NAME_WIDTH*

- *MSK_IPAR_SOL_READ_WIDTH*

- *MSK_IPAR_WRITE_BAS_CONSTRAINTS*

- *MSK_IPAR_WRITE_BAS_HEAD*

- *MSK_IPAR_WRITE_BAS_VARIABLES*

- *MSK_IPAR_WRITE_INT_CONSTRAINTS*

- *MSK_IPAR_WRITE_INT_HEAD*

- *MSK_IPAR_WRITE_INT_VARIABLES*

- *MSK_IPAR_WRITE_SOL_BARVARIABLES*

- *MSK_IPAR_WRITE_SOL_CONSTRAINTS*

- *MSK_IPAR_WRITE_SOL_HEAD*

- *MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES*

- *MSK_IPAR_WRITE_SOL_VARIABLES*

- *MSK_SPAR_BAS_SOL_FILE_NAME*

- *MSK_SPAR_INT_SOL_FILE_NAME*

- *MSK_SPAR_ITR_SOL_FILE_NAME*

- *MSK_SPAR_SOL_FILTER_XC_LOW*

- *MSK_SPAR_SOL_FILTER_XC_UPR*

- *MSK_SPAR_SOL_FILTER_XX_LOW*

- *MSK_SPAR_SOL_FILTER_XX_UPR*

Termination criteria

- *MSK_DPAR_BASIS_REL_TOL_S*

- *MSK_DPAR_BASIS_TOL_S*

- *MSK_DPAR_BASIS_TOL_X*

- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*

- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*

- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*

- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*

- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*

- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*

- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*

- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*

- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*

- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*

- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*

- *MSK_DPAR_INTPNT_TOL_DFEAS*

- *MSK_DPAR_INTPNT_TOL_INFEAS*

- *MSK_DPAR_INTPNT_TOL_MU_RED*

- *MSK_DPAR_INTPNT_TOL_PFEAS*

- *MSK_DPAR_INTPNT_TOL_REL_GAP*

- *MSK_DPAR_LOWER_OBJ_CUT*

- *MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH*

- *MSK_DPAR_MIO_MAX_TIME*

- *MSK_DPAR_MIO_REL_GAP_CONST*

- *MSK_DPAR_MIO_TOL_REL_GAP*

- *MSK_DPAR_OPTIMIZER_MAX_TIME*

- *MSK_DPAR_UPPER_OBJ_CUT*

- *MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH*

- *MSK_IPAR_BI_MAX_ITERATIONS*

- *MSK_IPAR_INTPNT_MAX_ITERATIONS*

- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*

- *MSK_IPAR_MIO_MAX_NUM_ROOT_CUT_ROUNDS*

- *MSK_IPAR_MIO_MAX_NUM_SOLUTIONS*

- *MSK_IPAR_SIM_MAX_ITERATIONS*

Other

- *MSK_IPAR_COMPRESS_STATFILE*

11.2 Parameters (alphabetical list sorted by type)

- *Double parameters*
- *Integer parameters*
- *String parameters*

11.2.1 Double parameters

MSK_DPAR_ANA_SOL_INFEAS_TOL
> If a constraint violates its bound with an amount larger than this value, the constraint name, index and violation will be printed by the solution analyzer.
>
>> **Default** 1e-6
>> **Accepted** [0.0; +inf]
>> **Example** mosek -d MSK_DPAR_ANA_SOL_INFEAS_TOL 1e-6 file
>> **Groups** *Analysis*

MSK_DPAR_BASIS_REL_TOL_S
> Maximum relative dual bound violation allowed in an optimal basic solution.
>
>> **Default** 1.0e-12
>> **Accepted** [0.0; +inf]
>> **Example** mosek -d MSK_DPAR_BASIS_REL_TOL_S 1.0e-12 file
>> **Groups** *Simplex optimizer*, *Termination criteria*

MSK_DPAR_BASIS_TOL_S
> Maximum absolute dual bound violation in an optimal basic solution.
>
>> **Default** 1.0e-6
>> **Accepted** [1.0e-9; +inf]
>> **Example** mosek -d MSK_DPAR_BASIS_TOL_S 1.0e-6 file
>> **Groups** *Simplex optimizer*, *Termination criteria*

MSK_DPAR_BASIS_TOL_X
> Maximum absolute primal bound violation allowed in an optimal basic solution.
>
>> **Default** 1.0e-6
>> **Accepted** [1.0e-9; +inf]
>> **Example** mosek -d MSK_DPAR_BASIS_TOL_X 1.0e-6 file
>> **Groups** *Simplex optimizer*, *Termination criteria*

MSK_DPAR_CHECK_CONVEXITY_REL_TOL
> This parameter controls when the full convexity check declares a problem to be non-convex. Increasing this tolerance relaxes the criteria for declaring the problem non-convex.
>
> A problem is declared non-convex if negative (positive) pivot elements are detected in the Cholesky factor of a matrix which is required to be PSD (NSD). This parameter controls how much this non-negativity requirement may be violated.
>
> If d_i is the pivot element for column i, then the matrix Q is considered to not be PSD if:
>
> $$d_i \leq -|Q_{ii}|\texttt{check\_convexity\_rel\_tol}$$
>
>> **Default** 1e-10

Accepted [0; +inf]

Example `mosek -d MSK_DPAR_CHECK_CONVEXITY_REL_TOL 1e-10 file`

Groups *Interior-point method*

`MSK_DPAR_DATA_SYM_MAT_TOL`

Absolute zero tolerance for elements in in symmetric matrices. If any value in a symmetric matrix is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Default 1.0e-12

Accepted [1.0e-16; 1.0e-6]

Example `mosek -d MSK_DPAR_DATA_SYM_MAT_TOL 1.0e-12 file`

Groups *Data check*

`MSK_DPAR_DATA_SYM_MAT_TOL_HUGE`

An element in a symmetric matrix which is larger than this value in absolute size causes an error.

Default 1.0e20

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_SYM_MAT_TOL_HUGE 1.0e20 file`

Groups *Data check*

`MSK_DPAR_DATA_SYM_MAT_TOL_LARGE`

An element in a symmetric matrix which is larger than this value in absolute size causes a warning message to be printed.

Default 1.0e10

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_SYM_MAT_TOL_LARGE 1.0e10 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_AIJ_HUGE`

An element in A which is larger than this value in absolute size causes an error.

Default 1.0e20

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_AIJ_HUGE 1.0e20 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_AIJ_LARGE`

An element in A which is larger than this value in absolute size causes a warning message to be printed.

Default 1.0e10

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_AIJ_LARGE 1.0e10 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_BOUND_INF`

Any bound which in absolute value is greater than this parameter is considered infinite.

Default 1.0e16

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_BOUND_INF 1.0e16 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_BOUND_WRN`

If a bound value is larger than this value in absolute size, then a warning message is issued.

Default 1.0e8

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_BOUND_WRN 1.0e8 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_C_HUGE`

An element in c which is larger than the value of this parameter in absolute terms is considered to be huge and generates an error.

Default 1.0e16

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_C_HUGE 1.0e16 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_CJ_LARGE`

An element in c which is larger than this value in absolute terms causes a warning message to be printed.

Default 1.0e8

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_CJ_LARGE 1.0e8 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_QIJ`

Absolute zero tolerance for elements in Q matrices.

Default 1.0e-16

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_QIJ 1.0e-16 file`

Groups *Data check*

`MSK_DPAR_DATA_TOL_X`

Zero tolerance for constraints and variables i.e. if the distance between the lower and upper bound is less than this value, then the lower and upper bound is considered identical.

Default 1.0e-8

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_DATA_TOL_X 1.0e-8 file`

Groups *Data check*

`MSK_DPAR_INTPNT_CO_TOL_DFEAS`

Dual feasibility tolerance used by the interior-point optimizer for conic problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_CO_TOL_DFEAS 1.0e-8 file`

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

`MSK_DPAR_INTPNT_CO_TOL_INFEAS`

Infeasibility tolerance used by the interior-point optimizer for conic problems. Controls when the interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-12

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_CO_TOL_INFEAS 1.0e-12 file`

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

`MSK_DPAR_INTPNT_CO_TOL_MU_RED`

Relative complementarity gap tolerance used by the interior-point optimizer for conic problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_CO_TOL_MU_RED 1.0e-8 file`

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

MSK_DPAR_INTPNT_CO_TOL_NEAR_REL
Optimality tolerance used by the interior-point optimizer for conic problems. If **MOSEK** cannot compute a solution that has the prescribed accuracy then it will check if the solution found satisfies the termination criteria with all tolerances multiplied by the value of this parameter. If yes, then the solution is also declared optimal.

Default 1000

Accepted [1.0; +inf]

Example `mosek -d MSK_DPAR_INTPNT_CO_TOL_NEAR_REL 1000 file`

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

MSK_DPAR_INTPNT_CO_TOL_PFEAS
Primal feasibility tolerance used by the interior-point optimizer for conic problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_CO_TOL_PFEAS 1.0e-8 file`

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

MSK_DPAR_INTPNT_CO_TOL_REL_GAP
Relative gap termination tolerance used by the interior-point optimizer for conic problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_CO_TOL_REL_GAP 1.0e-8 file`

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

MSK_DPAR_INTPNT_QO_TOL_DFEAS
Dual feasibility tolerance used by the interior-point optimizer for quadratic problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_QO_TOL_DFEAS 1.0e-8 file`

See also *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*

Groups *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_INFEAS
Infeasibility tolerance used by the interior-point optimizer for quadratic problems. Controls when the interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-12

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_QO_TOL_INFEAS 1.0e-12 file`

Groups *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_MU_RED
Relative complementarity gap tolerance used by the interior-point optimizer for quadratic problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_INTPNT_QO_TOL_MU_RED 1.0e-8 file`

Groups *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_NEAR_REL

Optimality tolerance used by the interior-point optimizer for quadratic problems. If **MOSEK** cannot compute a solution that has the prescribed accuracy then it will check if the solution found satisfies the termination criteria with all tolerances multiplied by the value of this parameter. If yes, then the solution is also declared optimal.

> **Default** 1000
> **Accepted** [1.0; +inf]
> **Example** mosek -d MSK_DPAR_INTPNT_QO_TOL_NEAR_REL 1000 file
> **Groups** *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_PFEAS

Primal feasibility tolerance used by the interior-point optimizer for quadratic problems.

> **Default** 1.0e-8
> **Accepted** [0.0; 1.0]
> **Example** mosek -d MSK_DPAR_INTPNT_QO_TOL_PFEAS 1.0e-8 file
> **See also** *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
> **Groups** *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_REL_GAP

Relative gap termination tolerance used by the interior-point optimizer for quadratic problems.

> **Default** 1.0e-8
> **Accepted** [0.0; 1.0]
> **Example** mosek -d MSK_DPAR_INTPNT_QO_TOL_REL_GAP 1.0e-8 file
> **See also** *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
> **Groups** *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_TOL_DFEAS

Dual feasibility tolerance used by the interior-point optimizer for linear problems.

> **Default** 1.0e-8
> **Accepted** [0.0; 1.0]
> **Example** mosek -d MSK_DPAR_INTPNT_TOL_DFEAS 1.0e-8 file
> **Groups** *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_TOL_DSAFE

Controls the initial dual starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it might be worthwhile to increase this value.

> **Default** 1.0
> **Accepted** [1.0e-4; +inf]
> **Example** mosek -d MSK_DPAR_INTPNT_TOL_DSAFE 1.0 file
> **Groups** *Interior-point method*

MSK_DPAR_INTPNT_TOL_INFEAS

Infeasibility tolerance used by the interior-point optimizer for linear problems. Controls when the interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

> **Default** 1.0e-10
> **Accepted** [0.0; 1.0]
> **Example** mosek -d MSK_DPAR_INTPNT_TOL_INFEAS 1.0e-10 file
> **Groups** *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_TOL_MU_RED
   Relative complementarity gap tolerance used by the interior-point optimizer for linear problems.

   > **Default** 1.0e-16
   > **Accepted** [0.0; 1.0]
   > **Example** mosek -d MSK_DPAR_INTPNT_TOL_MU_RED 1.0e-16 file
   > **Groups** *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_TOL_PATH
   Controls how close the interior-point optimizer follows the central path. A large value of this parameter means the central path is followed very closely. On numerically unstable problems it may be worthwhile to increase this parameter.

   > **Default** 1.0e-8
   > **Accepted** [0.0; 0.9999]
   > **Example** mosek -d MSK_DPAR_INTPNT_TOL_PATH 1.0e-8 file
   > **Groups** *Interior-point method*

MSK_DPAR_INTPNT_TOL_PFEAS
   Primal feasibility tolerance used by the interior-point optimizer for linear problems.

   > **Default** 1.0e-8
   > **Accepted** [0.0; 1.0]
   > **Example** mosek -d MSK_DPAR_INTPNT_TOL_PFEAS 1.0e-8 file
   > **Groups** *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_TOL_PSAFE
   Controls the initial primal starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it may be worthwhile to increase this value.

   > **Default** 1.0
   > **Accepted** [1.0e-4; +inf]
   > **Example** mosek -d MSK_DPAR_INTPNT_TOL_PSAFE 1.0 file
   > **Groups** *Interior-point method*

MSK_DPAR_INTPNT_TOL_REL_GAP
   Relative gap termination tolerance used by the interior-point optimizer for linear problems.

   > **Default** 1.0e-8
   > **Accepted** [1.0e-14; +inf]
   > **Example** mosek -d MSK_DPAR_INTPNT_TOL_REL_GAP 1.0e-8 file
   > **Groups** *Termination criteria*, *Interior-point method*

MSK_DPAR_INTPNT_TOL_REL_STEP
   Relative step size to the boundary for linear and quadratic optimization problems.

   > **Default** 0.9999
   > **Accepted** [1.0e-4; 0.999999]
   > **Example** mosek -d MSK_DPAR_INTPNT_TOL_REL_STEP 0.9999 file
   > **Groups** *Interior-point method*

MSK_DPAR_INTPNT_TOL_STEP_SIZE
   Minimal step size tolerance. If the step size falls below the value of this parameter, then the interior-point optimizer assumes that it is stalled. In other words the interior-point optimizer does not make any progress and therefore it is better to stop.

   > **Default** 1.0e-6
   > **Accepted** [0.0; 1.0]
   > **Example** mosek -d MSK_DPAR_INTPNT_TOL_STEP_SIZE 1.0e-6 file

Groups *Interior-point method*

MSK_DPAR_LOWER_OBJ_CUT
    If either a primal or dual feasible solution is found proving that the optimal objective value is
    outside the interval [*MSK_DPAR_LOWER_OBJ_CUT* , *MSK_DPAR_UPPER_OBJ_CUT*], then **MOSEK** is
    terminated.

    Default -1.0e30
    Accepted [-inf; +inf]
    Example mosek -d MSK_DPAR_LOWER_OBJ_CUT -1.0e30 file
    See also *MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH*
    Groups *Termination criteria*

MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH
    If the lower objective cut is less than the value of this parameter value, then the lower objective
    cut i.e. *MSK_DPAR_LOWER_OBJ_CUT* is treated as $-\infty$.

    Default -0.5e30
    Accepted [-inf; +inf]
    Example mosek -d MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH -0.5e30 file
    Groups *Termination criteria*

MSK_DPAR_MIO_MAX_TIME
    This parameter limits the maximum time spent by the mixed-integer optimizer. A negative number
    means infinity.

    Default -1.0
    Accepted [-inf; +inf]
    Example mosek -d MSK_DPAR_MIO_MAX_TIME -1.0 file
    Groups *Mixed-integer optimization*, *Termination criteria*

MSK_DPAR_MIO_REL_GAP_CONST
    This value is used to compute the relative gap for the solution to an integer optimization problem.

    Default 1.0e-10
    Accepted [1.0e-15; +inf]
    Example mosek -d MSK_DPAR_MIO_REL_GAP_CONST 1.0e-10 file
    Groups *Mixed-integer optimization*, *Termination criteria*

MSK_DPAR_MIO_TOL_ABS_GAP
    Absolute optimality tolerance employed by the mixed-integer optimizer.

    Default 0.0
    Accepted [0.0; +inf]
    Example mosek -d MSK_DPAR_MIO_TOL_ABS_GAP 0.0 file
    Groups *Mixed-integer optimization*

MSK_DPAR_MIO_TOL_ABS_RELAX_INT
    Absolute integer feasibility tolerance. If the distance to the nearest integer is less than this tolerance
    then an integer constraint is assumed to be satisfied.

    Default 1.0e-5
    Accepted [1e-9; +inf]
    Example mosek -d MSK_DPAR_MIO_TOL_ABS_RELAX_INT 1.0e-5 file
    Groups *Mixed-integer optimization*

MSK_DPAR_MIO_TOL_FEAS
    Feasibility tolerance for mixed integer solver.

    Default 1.0e-6

Accepted [1e-9; 1e-3]

Example `mosek -d MSK_DPAR_MIO_TOL_FEAS 1.0e-6 file`

Groups *Mixed-integer optimization*

`MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT`

If the relative improvement of the dual bound is smaller than this value, the solver will terminate the root cut generation. A value of 0.0 means that the value is selected automatically.

Default 0.0

Accepted [0.0; 1.0]

Example `mosek -d MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT 0.0 file`

Groups *Mixed-integer optimization*

`MSK_DPAR_MIO_TOL_REL_GAP`

Relative optimality tolerance employed by the mixed-integer optimizer.

Default 1.0e-4

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_MIO_TOL_REL_GAP 1.0e-4 file`

Groups *Mixed-integer optimization*, *Termination criteria*

`MSK_DPAR_OPTIMIZER_MAX_TIME`

Maximum amount of time the optimizer is allowed to spent on the optimization. A negative number means infinity.

Default -1.0

Accepted [-inf; +inf]

Example `mosek -d MSK_DPAR_OPTIMIZER_MAX_TIME -1.0 file`

Groups *Termination criteria*

`MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP`

Absolute tolerance employed by the linear dependency checker.

Default 1.0e-6

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP 1.0e-6 file`

Groups *Presolve*

`MSK_DPAR_PRESOLVE_TOL_AIJ`

Absolute zero tolerance employed for a_{ij} in the presolve.

Default 1.0e-12

Accepted [1.0e-15; +inf]

Example `mosek -d MSK_DPAR_PRESOLVE_TOL_AIJ 1.0e-12 file`

Groups *Presolve*

`MSK_DPAR_PRESOLVE_TOL_REL_LINDEP`

Relative tolerance employed by the linear dependency checker.

Default 1.0e-10

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_PRESOLVE_TOL_REL_LINDEP 1.0e-10 file`

Groups *Presolve*

`MSK_DPAR_PRESOLVE_TOL_S`

Absolute zero tolerance employed for s_i in the presolve.

Default 1.0e-8

Accepted [0.0; +inf]

Example `mosek -d MSK_DPAR_PRESOLVE_TOL_S 1.0e-8 file`

Groups *Presolve*

MSK_DPAR_PRESOLVE_TOL_X
> Absolute zero tolerance employed for x_j in the presolve.

> > **Default** 1.0e-8
> > **Accepted** [0.0; +inf]
> > **Example** mosek -d MSK_DPAR_PRESOLVE_TOL_X 1.0e-8 file
> > **Groups** *Presolve*

MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL
> This parameter determines when columns are dropped in incomplete Cholesky factorization during reformulation of quadratic problems.

> > **Default** 1e-15
> > **Accepted** [0; +inf]
> > **Example** mosek -d MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL 1e-15 file
> > **Groups** *Interior-point method*

MSK_DPAR_SEMIDEFINITE_TOL_APPROX
> Tolerance to define a matrix to be positive semidefinite.

> > **Default** 1.0e-10
> > **Accepted** [1.0e-15; +inf]
> > **Example** mosek -d MSK_DPAR_SEMIDEFINITE_TOL_APPROX 1.0e-10 file
> > **Groups** *Data check*

MSK_DPAR_SIM_LU_TOL_REL_PIV
> Relative pivot tolerance employed when computing the LU factorization of the basis in the simplex optimizers and in the basis identification procedure. A value closer to 1.0 generally improves numerical stability but typically also implies an increase in the computational work.

> > **Default** 0.01
> > **Accepted** [1.0e-6; 0.999999]
> > **Example** mosek -d MSK_DPAR_SIM_LU_TOL_REL_PIV 0.01 file
> > **Groups** *Basis identification*, *Simplex optimizer*

MSK_DPAR_SIMPLEX_ABS_TOL_PIV
> Absolute pivot tolerance employed by the simplex optimizers.

> > **Default** 1.0e-7
> > **Accepted** [1.0e-12; +inf]
> > **Example** mosek -d MSK_DPAR_SIMPLEX_ABS_TOL_PIV 1.0e-7 file
> > **Groups** *Simplex optimizer*

MSK_DPAR_UPPER_OBJ_CUT
> If either a primal or dual feasible solution is found proving that the optimal objective value is outside the interval [*MSK_DPAR_LOWER_OBJ_CUT*, *MSK_DPAR_UPPER_OBJ_CUT*], then **MOSEK** is terminated.

> > **Default** 1.0e30
> > **Accepted** [-inf; +inf]
> > **Example** mosek -d MSK_DPAR_UPPER_OBJ_CUT 1.0e30 file
> > **See also** *MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH*
> > **Groups** *Termination criteria*

MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH
> If the upper objective cut is greater than the value of this parameter, then the upper objective cut *MSK_DPAR_UPPER_OBJ_CUT* is treated as ∞.

Default 0.5e30

Accepted [-inf; +inf]

Example mosek -d MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH 0.5e30 file

Groups *Termination criteria*

11.2.2 Integer parameters

MSK_IPAR_ANA_SOL_BASIS

Controls whether the basis matrix is analyzed in solution analyzer.

Default *ON*

Accepted *ON*, *OFF*

Example mosek -d MSK_IPAR_ANA_SOL_BASIS MSK_ON file

Groups *Analysis*

MSK_IPAR_ANA_SOL_PRINT_VIOLATED

A parameter of the problem analyzer. Controls whether a list of violated constraints is printed. All constraints violated by more than the value set by the parameter *MSK_DPAR_ANA_SOL_INFEAS_TOL* will be printed.

Default *OFF*

Accepted *ON*, *OFF*

Example mosek -d MSK_IPAR_ANA_SOL_PRINT_VIOLATED MSK_OFF file

Groups *Analysis*

MSK_IPAR_AUTO_SORT_A_BEFORE_OPT

Controls whether the elements in each column of A are sorted before an optimization is performed. This is not required but makes the optimization more deterministic.

Default *OFF*

Accepted *ON*, *OFF*

Example mosek -d MSK_IPAR_AUTO_SORT_A_BEFORE_OPT MSK_OFF file

Groups *Debugging*

MSK_IPAR_AUTO_UPDATE_SOL_INFO

Controls whether the solution information items are automatically updated after an optimization is performed.

Default *OFF*

Accepted *ON*, *OFF*

Example mosek -d MSK_IPAR_AUTO_UPDATE_SOL_INFO MSK_OFF file

Groups *Overall system*

MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE

If a slack variable is in the basis, then the corresponding column in the basis is a unit vector with -1 in the right position. However, if this parameter is set to *MSK_ON*, -1 is replaced by 1.

Default *OFF*

Accepted *ON*, *OFF*

Example mosek -d MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE MSK_OFF file

Groups *Simplex optimizer*

MSK_IPAR_BI_CLEAN_OPTIMIZER

Controls which simplex optimizer is used in the clean-up phase. Anything else than *MSK_OPTIMIZER_PRIMAL_SIMPLEX* or *MSK_OPTIMIZER_DUAL_SIMPLEX* is equivalent to *MSK_OPTIMIZER_FREE_SIMPLEX*.

Default *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Example `mosek -d MSK_IPAR_BI_CLEAN_OPTIMIZER MSK_OPTIMIZER_FREE file`

Groups *Basis identification*, *Overall solver*

`MSK_IPAR_BI_IGNORE_MAX_ITER`

If the parameter `MSK_IPAR_INTPNT_BASIS` has the value `MSK_BI_NO_ERROR` and the interior-point optimizer has terminated due to maximum number of iterations, then basis identification is performed if this parameter has the value `MSK_ON`.

Default `OFF`

Accepted `ON`, `OFF`

Example `mosek -d MSK_IPAR_BI_IGNORE_MAX_ITER MSK_OFF file`

Groups *Interior-point method*, *Basis identification*

`MSK_IPAR_BI_IGNORE_NUM_ERROR`

If the parameter `MSK_IPAR_INTPNT_BASIS` has the value `MSK_BI_NO_ERROR` and the interior-point optimizer has terminated due to a numerical problem, then basis identification is performed if this parameter has the value `MSK_ON`.

Default `OFF`

Accepted `ON`, `OFF`

Example `mosek -d MSK_IPAR_BI_IGNORE_NUM_ERROR MSK_OFF file`

Groups *Interior-point method*, *Basis identification*

`MSK_IPAR_BI_MAX_ITERATIONS`

Controls the maximum number of simplex iterations allowed to optimize a basis after the basis identification.

Default 1000000

Accepted $[0; +\mathrm{inf}]$

Example `mosek -d MSK_IPAR_BI_MAX_ITERATIONS 1000000 file`

Groups *Basis identification*, *Termination criteria*

`MSK_IPAR_CACHE_LICENSE`

Specifies if the license is kept checked out for the lifetime of the **MOSEK** environment/model/process (`MSK_ON`) or returned to the server immediately after the optimization (`MSK_OFF`).

Check-in and check-out of licenses have an overhead. Frequent communication with the license server should be avoided.

Default `ON`

Accepted `ON`, `OFF`

Example `mosek -d MSK_IPAR_CACHE_LICENSE MSK_ON file`

Groups *License manager*

`MSK_IPAR_CHECK_CONVEXITY`

Specify the level of convexity check on quadratic problems.

Default `FULL`

Accepted `NONE`, `SIMPLE`, `FULL`

Example `mosek -d MSK_IPAR_CHECK_CONVEXITY MSK_CHECK_CONVEXITY_FULL file`

Groups *Data check*

`MSK_IPAR_COMPRESS_STATFILE`

Control compression of stat files.

Default `ON`

Accepted `ON`, `OFF`

Example `mosek -d MSK_IPAR_COMPRESS_STATFILE MSK_ON file`

`MSK_IPAR_INFEAS_GENERIC_NAMES`

    Controls whether generic names are used when an infeasible subproblem is created.

        Default *OFF*

        Accepted *ON*, *OFF*

        Example `mosek -d MSK_IPAR_INFEAS_GENERIC_NAMES MSK_OFF file`

        Groups *Infeasibility report*

`MSK_IPAR_INFEAS_PREFER_PRIMAL`

    If both certificates of primal and dual infeasibility are supplied then only the primal is used when this option is turned on.

        Default *ON*

        Accepted *ON*, *OFF*

        Example `mosek -d MSK_IPAR_INFEAS_PREFER_PRIMAL MSK_ON file`

        Groups *Overall solver*

`MSK_IPAR_INFEAS_REPORT_AUTO`

    Controls whether an infeasibility report is automatically produced after the optimization if the problem is primal or dual infeasible.

        Default *OFF*

        Accepted *ON*, *OFF*

        Example `mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_OFF file`

        Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_INFEAS_REPORT_LEVEL`

    Controls the amount of information presented in an infeasibility report. Higher values imply more information.

        Default 1

        Accepted [0; +inf]

        Example `mosek -d MSK_IPAR_INFEAS_REPORT_LEVEL 1 file`

        Groups *Infeasibility report*, *Output information*

`MSK_IPAR_INTPNT_BASIS`

    Controls whether the interior-point optimizer also computes an optimal basis.

        Default *ALWAYS*

        Accepted *NEVER*, *ALWAYS*, *NO_ERROR*, *IF_FEASIBLE*, *RESERVERED*

        Example `mosek -d MSK_IPAR_INTPNT_BASIS MSK_BI_ALWAYS file`

        See also *MSK_IPAR_BI_IGNORE_MAX_ITER*, *MSK_IPAR_BI_IGNORE_NUM_ERROR*, *MSK_IPAR_BI_MAX_ITERATIONS*, *MSK_IPAR_BI_CLEAN_OPTIMIZER*

        Groups *Interior-point method*, *Basis identification*

`MSK_IPAR_INTPNT_DIFF_STEP`

    Controls whether different step sizes are allowed in the primal and dual space.

        Default *ON*

        Accepted

            • *ON*: Different step sizes are allowed.

            • *OFF*: Different step sizes are not allowed.

        Example `mosek -d MSK_IPAR_INTPNT_DIFF_STEP MSK_ON file`

        Groups *Interior-point method*

`MSK_IPAR_INTPNT_HOTSTART`

    Currently not in use.

        Default *NONE*

>   **Accepted** *NONE*, *PRIMAL*, *DUAL*, *PRIMAL_DUAL*
>
>   **Example** mosek -d MSK_IPAR_INTPNT_HOTSTART MSK_INTPNT_HOTSTART_NONE file
>
>   **Groups** *Interior-point method*

MSK_IPAR_INTPNT_MAX_ITERATIONS
>   Controls the maximum number of iterations allowed in the interior-point optimizer.
>
>   **Default** 400
>
>   **Accepted** [0; +inf]
>
>   **Example** mosek -d MSK_IPAR_INTPNT_MAX_ITERATIONS 400 file
>
>   **Groups** *Interior-point method*, *Termination criteria*

MSK_IPAR_INTPNT_MAX_NUM_COR
>   Controls the maximum number of correctors allowed by the multiple corrector procedure. A negative value means that **MOSEK** is making the choice.
>
>   **Default** -1
>
>   **Accepted** [-1; +inf]
>
>   **Example** mosek -d MSK_IPAR_INTPNT_MAX_NUM_COR -1 file
>
>   **Groups** *Interior-point method*

MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS
>   Maximum number of steps to be used by the iterative refinement of the search direction. A negative value implies that the optimizer chooses the maximum number of iterative refinement steps.
>
>   **Default** -1
>
>   **Accepted** [-inf; +inf]
>
>   **Example** mosek -d MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS -1 file
>
>   **Groups** *Interior-point method*

MSK_IPAR_INTPNT_MULTI_THREAD
>   Controls whether the interior-point optimizers are allowed to employ multiple threads if more threads is available.
>
>   **Default** *ON*
>
>   **Accepted** *ON*, *OFF*
>
>   **Example** mosek -d MSK_IPAR_INTPNT_MULTI_THREAD MSK_ON file
>
>   **Groups** *Overall system*

MSK_IPAR_INTPNT_OFF_COL_TRH
>   Controls how many offending columns are detected in the Jacobian of the constraint matrix.

0	no detection
1	aggressive detection
> 1	higher values mean less aggressive detection

>   **Default** 40
>
>   **Accepted** [0; +inf]
>
>   **Example** mosek -d MSK_IPAR_INTPNT_OFF_COL_TRH 40 file
>
>   **Groups** *Interior-point method*

MSK_IPAR_INTPNT_ORDER_GP_NUM_SEEDS
>   The GP ordering is dependent on a random seed. Therefore, trying several random seeds may lead to a better ordering. This parameter controls the number of random seeds tried.
>
>   A value of 0 means that MOSEK makes the choice.
>
>   **Default** 0
>
>   **Accepted** [0; +inf]
>
>   **Example** mosek -d MSK_IPAR_INTPNT_ORDER_GP_NUM_SEEDS 0 file

Groups *Interior-point method*

MSK_IPAR_INTPNT_ORDER_METHOD
Controls the ordering strategy used by the interior-point optimizer when factorizing the Newton equation system.

> **Default** *FREE*
>
> **Accepted** *FREE*, *APPMINLOC*, *EXPERIMENTAL*, *TRY_GRAPHPAR*, *FORCE_GRAPHPAR*, *NONE*
>
> **Example** mosek -d MSK_IPAR_INTPNT_ORDER_METHOD MSK_ORDER_METHOD_FREE
>   file
>
> **Groups** *Interior-point method*

MSK_IPAR_INTPNT_PURIFY
Currently not in use.

> **Default** *NONE*
>
> **Accepted** *NONE*, *PRIMAL*, *DUAL*, *PRIMAL_DUAL*, *AUTO*
>
> **Example** mosek -d MSK_IPAR_INTPNT_PURIFY MSK_PURIFY_NONE file
>
> **Groups** *Interior-point method*

MSK_IPAR_INTPNT_REGULARIZATION_USE
Controls whether regularization is allowed.

> **Default** *ON*
>
> **Accepted** *ON*, *OFF*
>
> **Example** mosek -d MSK_IPAR_INTPNT_REGULARIZATION_USE MSK_ON file
>
> **Groups** *Interior-point method*

MSK_IPAR_INTPNT_SCALING
Controls how the problem is scaled before the interior-point optimizer is used.

> **Default** *FREE*
>
> **Accepted** *FREE*, *NONE*, *MODERATE*, *AGGRESSIVE*
>
> **Example** mosek -d MSK_IPAR_INTPNT_SCALING MSK_SCALING_FREE file
>
> **Groups** *Interior-point method*

MSK_IPAR_INTPNT_SOLVE_FORM
Controls whether the primal or the dual problem is solved.

> **Default** *FREE*
>
> **Accepted** *FREE*, *PRIMAL*, *DUAL*
>
> **Example** mosek -d MSK_IPAR_INTPNT_SOLVE_FORM MSK_SOLVE_FREE file
>
> **Groups** *Interior-point method*

MSK_IPAR_INTPNT_STARTING_POINT
Starting point used by the interior-point optimizer.

> **Default** *FREE*
>
> **Accepted** *FREE*, *GUESS*, *CONSTANT*, *SATISFY_BOUNDS*
>
> **Example** mosek -d MSK_IPAR_INTPNT_STARTING_POINT MSK_STARTING_POINT_FREE
>   file
>
> **Groups** *Interior-point method*

MSK_IPAR_LICENSE_DEBUG
This option is used to turn on debugging of the license manager.

> **Default** *OFF*
>
> **Accepted** *ON*, *OFF*
>
> **Example** mosek -d MSK_IPAR_LICENSE_DEBUG MSK_OFF file
>
> **Groups** *License manager*

MSK_IPAR_LICENSE_PAUSE_TIME

If *MSK_IPAR_LICENSE_WAIT* is *MSK_ON* and no license is available, then **MOSEK** sleeps a number of milliseconds between each check of whether a license has become free.

> **Default** 100
>
> **Accepted** [0; 1000000]
>
> **Example** mosek -d MSK_IPAR_LICENSE_PAUSE_TIME 100 file
>
> **Groups** *License manager*

MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS

Controls whether license features expire warnings are suppressed.

> **Default** *OFF*
>
> **Accepted** *ON*, *OFF*
>
> **Example** mosek -d MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS MSK_OFF file
>
> **Groups** *License manager*, *Output information*

MSK_IPAR_LICENSE_TRH_EXPIRY_WRN

If a license feature expires in a numbers of days less than the value of this parameter then a warning will be issued.

> **Default** 7
>
> **Accepted** [0; +inf]
>
> **Example** mosek -d MSK_IPAR_LICENSE_TRH_EXPIRY_WRN 7 file
>
> **Groups** *License manager*, *Output information*

MSK_IPAR_LICENSE_WAIT

If all licenses are in use **MOSEK** returns with an error code. However, by turning on this parameter **MOSEK** will wait for an available license.

> **Default** *OFF*
>
> **Accepted** *ON*, *OFF*
>
> **Example** mosek -d MSK_IPAR_LICENSE_WAIT MSK_OFF file
>
> **Groups** *Overall solver*, *Overall system*, *License manager*

MSK_IPAR_LOG

Controls the amount of log information. The value 0 implies that all log information is suppressed. A higher level implies that more information is logged.

Please note that if a task is employed to solve a sequence of optimization problems the value of this parameter is reduced by the value of *MSK_IPAR_LOG_CUT_SECOND_OPT* for the second and any subsequent optimizations.

> **Default** 10
>
> **Accepted** [0; +inf]
>
> **Example** mosek -d MSK_IPAR_LOG 10 file
>
> **See also** *MSK_IPAR_LOG_CUT_SECOND_OPT*
>
> **Groups** *Output information*, *Logging*

MSK_IPAR_LOG_ANA_PRO

Controls amount of output from the problem analyzer.

> **Default** 1
>
> **Accepted** [0; +inf]
>
> **Example** mosek -d MSK_IPAR_LOG_ANA_PRO 1 file
>
> **Groups** *Analysis*, *Logging*

MSK_IPAR_LOG_BI

Controls the amount of output printed by the basis identification procedure. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_BI 1 file

Groups *Basis identification*, *Output information*, *Logging*

MSK_IPAR_LOG_BI_FREQ

Controls how frequently the optimizer outputs information about the basis identification and how frequent the user-defined callback function is called.

Default 2500

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_BI_FREQ 2500 file

Groups *Basis identification*, *Output information*, *Logging*

MSK_IPAR_LOG_CHECK_CONVEXITY

Controls logging in convexity check on quadratic problems. Set to a positive value to turn logging on. If a quadratic coefficient matrix is found to violate the requirement of PSD (NSD) then a list of negative (positive) pivot elements is printed. The absolute value of the pivot elements is also shown.

Default 0

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_CHECK_CONVEXITY 0 file

Groups *Data check*

MSK_IPAR_LOG_CUT_SECOND_OPT

If a task is employed to solve a sequence of optimization problems, then the value of the log levels is reduced by the value of this parameter. E.g *MSK_IPAR_LOG* and *MSK_IPAR_LOG_SIM* are reduced by the value of this parameter for the second and any subsequent optimizations.

Default 1

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_CUT_SECOND_OPT 1 file

See also *MSK_IPAR_LOG*, *MSK_IPAR_LOG_INTPNT*, *MSK_IPAR_LOG_MIO*, *MSK_IPAR_LOG_SIM*

Groups *Output information*, *Logging*

MSK_IPAR_LOG_EXPAND

Controls the amount of logging when a data item such as the maximum number constrains is expanded.

Default 0

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_EXPAND 0 file

Groups *Output information*, *Logging*

MSK_IPAR_LOG_FEAS_REPAIR

Controls the amount of output printed when performing feasibility repair. A value higher than one means extensive logging.

Default 1

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_FEAS_REPAIR 1 file

Groups *Output information*, *Logging*

MSK_IPAR_LOG_FILE

If turned on, then some log info is printed when a file is written or read.

Default 1

Accepted [0; +inf]

Example `mosek -d MSK_IPAR_LOG_FILE 1 file`

Groups *Data input/output*, *Output information*, *Logging*

`MSK_IPAR_LOG_INCLUDE_SUMMARY`
Not relevant for this API.

Default *OFF*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_LOG_INCLUDE_SUMMARY MSK_OFF file`

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_INFEAS_ANA`
Controls amount of output printed by the infeasibility analyzer procedures. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Example `mosek -d MSK_IPAR_LOG_INFEAS_ANA 1 file`

Groups *Infeasibility report*, *Output information*, *Logging*

`MSK_IPAR_LOG_INTPNT`
Controls amount of output printed by the interior-point optimizer. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Example `mosek -d MSK_IPAR_LOG_INTPNT 1 file`

Groups *Interior-point method*, *Output information*, *Logging*

`MSK_IPAR_LOG_LOCAL_INFO`
Controls whether local identifying information like environment variables, filenames, IP addresses etc. are printed to the log.

Note that this will only affect some functions. Some functions that specifically emit system information will not be affected.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_LOG_LOCAL_INFO MSK_ON file`

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_MIO`
Controls the log level for the mixed-integer optimizer. A higher level implies that more information is logged.

Default 4

Accepted [0; +inf]

Example `mosek -d MSK_IPAR_LOG_MIO 4 file`

Groups *Mixed-integer optimization*, *Output information*, *Logging*

`MSK_IPAR_LOG_MIO_FREQ`
Controls how frequent the mixed-integer optimizer prints the log line. It will print line every time *MSK_IPAR_LOG_MIO_FREQ* relaxations have been solved.

Default 10

Accepted [-inf; +inf]

Example `mosek -d MSK_IPAR_LOG_MIO_FREQ 10 file`

Groups *Mixed-integer optimization*, *Output information*, *Logging*

`MSK_IPAR_LOG_ORDER`
    If turned on, then factor lines are added to the log.

> **Default** 1
> **Accepted** [0; +inf]
> **Example** `mosek -d MSK_IPAR_LOG_ORDER 1 file`
> **Groups** *Output information*, *Logging*

`MSK_IPAR_LOG_PRESOLVE`
    Controls amount of output printed by the presolve procedure. A higher level implies that more information is logged.

> **Default** 1
> **Accepted** [0; +inf]
> **Example** `mosek -d MSK_IPAR_LOG_PRESOLVE 1 file`
> **Groups** *Logging*

`MSK_IPAR_LOG_RESPONSE`
    Controls amount of output printed when response codes are reported. A higher level implies that more information is logged.

> **Default** 0
> **Accepted** [0; +inf]
> **Example** `mosek -d MSK_IPAR_LOG_RESPONSE 0 file`
> **Groups** *Output information*, *Logging*

`MSK_IPAR_LOG_SENSITIVITY`
    Controls the amount of logging during the sensitivity analysis.

- 0. Means no logging information is produced.
- 1. Timing information is printed.
- 2. Sensitivity results are printed.

> **Default** 1
> **Accepted** [0; +inf]
> **Example** `mosek -d MSK_IPAR_LOG_SENSITIVITY 1 file`
> **Groups** *Output information*, *Logging*

`MSK_IPAR_LOG_SENSITIVITY_OPT`
    Controls the amount of logging from the optimizers employed during the sensitivity analysis. 0 means no logging information is produced.

> **Default** 0
> **Accepted** [0; +inf]
> **Example** `mosek -d MSK_IPAR_LOG_SENSITIVITY_OPT 0 file`
> **Groups** *Output information*, *Logging*

`MSK_IPAR_LOG_SIM`
    Controls amount of output printed by the simplex optimizer. A higher level implies that more information is logged.

> **Default** 4
> **Accepted** [0; +inf]
> **Example** `mosek -d MSK_IPAR_LOG_SIM 4 file`
> **Groups** *Simplex optimizer*, *Output information*, *Logging*

`MSK_IPAR_LOG_SIM_FREQ`
    Controls how frequent the simplex optimizer outputs information about the optimization and how frequent the user-defined callback function is called.

Default 1000

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_SIM_FREQ 1000 file

Groups *Simplex optimizer*, *Output information*, *Logging*

MSK_IPAR_LOG_SIM_MINOR

Currently not in use.

Default 1

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_SIM_MINOR 1 file

Groups *Simplex optimizer*, *Output information*

MSK_IPAR_LOG_STORAGE

When turned on, **MOSEK** prints messages regarding the storage usage and allocation.

Default 0

Accepted [0; +inf]

Example mosek -d MSK_IPAR_LOG_STORAGE 0 file

Groups *Output information*, *Overall system*, *Logging*

MSK_IPAR_MAX_NUM_WARNINGS

Each warning is shown a limited number of times controlled by this parameter. A negative value is identical to infinite number of times.

Default 10

Accepted [-inf; +inf]

Example mosek -d MSK_IPAR_MAX_NUM_WARNINGS 10 file

Groups *Output information*

MSK_IPAR_MIO_BRANCH_DIR

Controls whether the mixed-integer optimizer is branching up or down by default.

Default *FREE*

Accepted *FREE*, *UP*, *DOWN*, *NEAR*, *FAR*, *ROOT_LP*, *GUIDED*, *PSEUDOCOST*

Example mosek -d MSK_IPAR_MIO_BRANCH_DIR MSK_BRANCH_DIR_FREE file

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CONIC_OUTER_APPROXIMATION

If this option is turned on outer approximation is used when solving relaxations of conic problems; otherwise interior point is used.

Default *OFF*

Accepted *ON*, *OFF*

Example mosek -d MSK_IPAR_MIO_CONIC_OUTER_APPROXIMATION MSK_OFF file

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_CLIQUE

Controls whether clique cuts should be generated.

Default *ON*

Accepted *ON*, *OFF*

Example mosek -d MSK_IPAR_MIO_CUT_CLIQUE MSK_ON file

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_CMIR

Controls whether mixed integer rounding cuts should be generated.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_MIO_CUT_CMIR MSK_ON file`

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_GMI`

Controls whether GMI cuts should be generated.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_MIO_CUT_GMI MSK_ON file`

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_IMPLIED_BOUND`

Controls whether implied bound cuts should be generated.

Default *OFF*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_MIO_CUT_IMPLIED_BOUND MSK_OFF file`

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_KNAPSACK_COVER`

Controls whether knapsack cover cuts should be generated.

Default *OFF*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_MIO_CUT_KNAPSACK_COVER MSK_OFF file`

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_SELECTION_LEVEL`

Controls how aggressively generated cuts are selected to be included in the relaxation.

- -1. The optimizer chooses the level of cut selection
- 0. Generated cuts less likely to be added to the relaxation
- 1. Cuts are more aggressively selected to be included in the relaxation

Default -1

Accepted [-1; +1]

Example `mosek -d MSK_IPAR_MIO_CUT_SELECTION_LEVEL -1 file`

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_FEASPUMP_LEVEL`

Controls the way the Feasibility Pump heuristic is employed by the mixed-integer optimizer.

- -1. The optimizer chooses how the Feasibility Pump is used
- 0. The Feasibility Pump is disabled
- 1. The Feasibility Pump is enabled with an effort to improve solution quality
- 2. The Feasibility Pump is enabled with an effort to reach feasibility early

Default -1

Accepted [-1; 2]

Example `mosek -d MSK_IPAR_MIO_FEASPUMP_LEVEL -1 file`

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_HEURISTIC_LEVEL`

Controls the heuristic employed by the mixed-integer optimizer to locate an initial good integer feasible solution. A value of zero means the heuristic is not used at all. A larger value than 0 means that a gradually more sophisticated heuristic is used which is computationally more expensive. A negative value implies that the optimizer chooses the heuristic. Normally a value around 3 to 5 should be optimal.

Default -1

Accepted [-inf; +inf]

Example mosek -d MSK_IPAR_MIO_HEURISTIC_LEVEL -1 file

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_MAX_NUM_BRANCHES

Maximum number of branches allowed during the branch and bound search. A negative value means infinite.

Default -1

Accepted [-inf; +inf]

Example mosek -d MSK_IPAR_MIO_MAX_NUM_BRANCHES -1 file

Groups *Mixed-integer optimization*, *Termination criteria*

MSK_IPAR_MIO_MAX_NUM_RELAXS

Maximum number of relaxations allowed during the branch and bound search. A negative value means infinite.

Default -1

Accepted [-inf; +inf]

Example mosek -d MSK_IPAR_MIO_MAX_NUM_RELAXS -1 file

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_MAX_NUM_ROOT_CUT_ROUNDS

Maximum number of cut separation rounds at the root node.

Default 100

Accepted [0; +inf]

Example mosek -d MSK_IPAR_MIO_MAX_NUM_ROOT_CUT_ROUNDS 100 file

Groups *Mixed-integer optimization*, *Termination criteria*

MSK_IPAR_MIO_MAX_NUM_SOLUTIONS

The mixed-integer optimizer can be terminated after a certain number of different feasible solutions has been located. If this parameter has the value $n > 0$, then the mixed-integer optimizer will be terminated when n feasible solutions have been located.

Default -1

Accepted [-inf; +inf]

Example mosek -d MSK_IPAR_MIO_MAX_NUM_SOLUTIONS -1 file

Groups *Mixed-integer optimization*, *Termination criteria*

MSK_IPAR_MIO_MODE

Controls whether the optimizer includes the integer restrictions when solving a (mixed) integer optimization problem.

Default *SATISFIED*

Accepted *IGNORED*, *SATISFIED*

Example mosek -d MSK_IPAR_MIO_MODE MSK_MIO_MODE_SATISFIED file

Groups *Overall solver*

MSK_IPAR_MIO_NODE_OPTIMIZER

Controls which optimizer is employed at the non-root nodes in the mixed-integer optimizer.

Default *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Example mosek -d MSK_IPAR_MIO_NODE_OPTIMIZER MSK_OPTIMIZER_FREE file

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_NODE_SELECTION`
> Controls the node selection strategy employed by the mixed-integer optimizer.
>
>> **Default** *FREE*
>> **Accepted** *FREE*, *FIRST*, *BEST*, *PSEUDO*
>> **Example** `mosek -d MSK_IPAR_MIO_NODE_SELECTION MSK_MIO_NODE_SELECTION_FREE file`
>> **Groups** *Mixed-integer optimization*

`MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE`
> Enables or disables perspective reformulation in presolve.
>
>> **Default** *ON*
>> **Accepted** *ON*, *OFF*
>> **Example** `mosek -d MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE MSK_ON file`
>> **Groups** *Mixed-integer optimization*

`MSK_IPAR_MIO_PROBING_LEVEL`
> Controls the amount of probing employed by the mixed-integer optimizer in presolve.
>
> - −1. The optimizer chooses the level of probing employed
> - 0. Probing is disabled
> - 1. A low amount of probing is employed
> - 2. A medium amount of probing is employed
> - 3. A high amount of probing is employed
>
>> **Default** -1
>> **Accepted** [-1; 3]
>> **Example** `mosek -d MSK_IPAR_MIO_PROBING_LEVEL -1 file`
>> **Groups** *Mixed-integer optimization*

`MSK_IPAR_MIO_PROPAGATE_OBJECTIVE_CONSTRAINT`
> Use objective domain propagation.
>
>> **Default** *OFF*
>> **Accepted** *ON*, *OFF*
>> **Example** `mosek -d MSK_IPAR_MIO_PROPAGATE_OBJECTIVE_CONSTRAINT MSK_OFF file`
>> **Groups** *Mixed-integer optimization*

`MSK_IPAR_MIO_RINS_MAX_NODES`
> Controls the maximum number of nodes allowed in each call to the RINS heuristic. The default value of -1 means that the value is determined automatically. A value of zero turns off the heuristic.
>
>> **Default** -1
>> **Accepted** [-1; +inf]
>> **Example** `mosek -d MSK_IPAR_MIO_RINS_MAX_NODES -1 file`
>> **Groups** *Mixed-integer optimization*

`MSK_IPAR_MIO_ROOT_OPTIMIZER`
> Controls which optimizer is employed at the root node in the mixed-integer optimizer.
>
>> **Default** *FREE*
>> **Accepted** *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*
>> **Example** `mosek -d MSK_IPAR_MIO_ROOT_OPTIMIZER MSK_OPTIMIZER_FREE file`
>> **Groups** *Mixed-integer optimization*

MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL
　　Controls whether presolve can be repeated at root node.

- −1. The optimizer chooses whether presolve is repeated
- 0. Never repeat presolve
- 1. Always repeat presolve

　　Default -1
　　Accepted [-1; 1]
　　Example mosek -d MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL -1 file
　　Groups *Mixed-integer optimization*

MSK_IPAR_MIO_SEED
　　Sets the random seed used for randomization in the mixed integer optimizer. Selecting a different seed can change the path the optimizer takes to the optimal solution.

　　Default 42
　　Accepted [0; +inf]
　　Example mosek -d MSK_IPAR_MIO_SEED 42 file
　　Groups *Mixed-integer optimization*

MSK_IPAR_MIO_VB_DETECTION_LEVEL
　　Controls how much effort is put into detecting variable bounds.

- −1. The optimizer chooses
- 0. No variable bounds are detected
- 1. Only detect variable bounds that are directly represented in the problem
- 2. Detect variable bounds in probing

　　Default -1
　　Accepted [-1; +2]
　　Example mosek -d MSK_IPAR_MIO_VB_DETECTION_LEVEL -1 file
　　Groups *Mixed-integer optimization*

MSK_IPAR_MT_SPINCOUNT
　　Set the number of iterations to spin before sleeping.

　　Default 0
　　Accepted [0; 1000000000]
　　Example mosek -d MSK_IPAR_MT_SPINCOUNT 0 file
　　Groups *Overall system*

MSK_IPAR_NUM_THREADS
　　Controls the number of threads employed by the optimizer. If set to 0 the number of threads used will be equal to the number of cores detected on the machine.

　　If using the conic optimizer, the value of this parameter set at first optimization remains constant through the lifetime of the process. **MOSEK** will allocate a thread pool of given size, and changing the parameter value later will have no effect. It will, however, remain possible to demand single-threaded execution by setting *MSK_IPAR_INTPNT_MULTI_THREAD* .

　　For the mixed-integer optimizer and interior-point linear optimizer there is no such restriction.

　　Default 0
　　Accepted [0; +inf]
　　Example mosek -d MSK_IPAR_NUM_THREADS 0 file
　　Groups *Overall system*

MSK_IPAR_OPF_WRITE_HEADER
　　Write a text header with date and **MOSEK** version in an OPF file.

> **Default** *ON*
>
> **Accepted** *ON*, *OFF*
>
> **Example** `mosek -d MSK_IPAR_OPF_WRITE_HEADER MSK_ON file`
>
> **Groups** *Data input/output*

MSK_IPAR_OPF_WRITE_HINTS
> Write a hint section with problem dimensions in the beginning of an OPF file.
>
> > **Default** *ON*
> >
> > **Accepted** *ON*, *OFF*
> >
> > **Example** `mosek -d MSK_IPAR_OPF_WRITE_HINTS MSK_ON file`
> >
> > **Groups** *Data input/output*

MSK_IPAR_OPF_WRITE_LINE_LENGTH
> Aim to keep lines in OPF files not much longer than this.
>
> > **Default** 80
> >
> > **Accepted** [0; +inf]
> >
> > **Example** `mosek -d MSK_IPAR_OPF_WRITE_LINE_LENGTH 80 file`
> >
> > **Groups** *Data input/output*

MSK_IPAR_OPF_WRITE_PARAMETERS
> Write a parameter section in an OPF file.
>
> > **Default** *OFF*
> >
> > **Accepted** *ON*, *OFF*
> >
> > **Example** `mosek -d MSK_IPAR_OPF_WRITE_PARAMETERS MSK_OFF file`
> >
> > **Groups** *Data input/output*

MSK_IPAR_OPF_WRITE_PROBLEM
> Write objective, constraints, bounds etc. to an OPF file.
>
> > **Default** *ON*
> >
> > **Accepted** *ON*, *OFF*
> >
> > **Example** `mosek -d MSK_IPAR_OPF_WRITE_PROBLEM MSK_ON file`
> >
> > **Groups** *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_BAS
> If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and a basic solution is defined, include the basic solution in OPF files.
>
> > **Default** *ON*
> >
> > **Accepted** *ON*, *OFF*
> >
> > **Example** `mosek -d MSK_IPAR_OPF_WRITE_SOL_BAS MSK_ON file`
> >
> > **Groups** *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_ITG
> If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and an integer solution is defined, write the integer solution in OPF files.
>
> > **Default** *ON*
> >
> > **Accepted** *ON*, *OFF*
> >
> > **Example** `mosek -d MSK_IPAR_OPF_WRITE_SOL_ITG MSK_ON file`
> >
> > **Groups** *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_ITR
> If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and an interior solution is defined, write the interior solution in OPF files.
>
> > **Default** *ON*

Accepted *ON* , *OFF*

Example `mosek -d MSK_IPAR_OPF_WRITE_SOL_ITR MSK_ON file`

Groups *Data input/output*

`MSK_IPAR_OPF_WRITE_SOLUTIONS`
    Enable inclusion of solutions in the OPF files.

Default *OFF*

Accepted *ON* , *OFF*

Example `mosek -d MSK_IPAR_OPF_WRITE_SOLUTIONS MSK_OFF file`

Groups *Data input/output*

`MSK_IPAR_OPTIMIZER`
    The parameter controls which optimizer is used to optimize the task.

Default *FREE*

Accepted *FREE* , *INTPNT* , *CONIC* , *PRIMAL_SIMPLEX* , *DUAL_SIMPLEX* , *FREE_SIMPLEX* , *MIXED_INT*

Example `mosek -d MSK_IPAR_OPTIMIZER MSK_OPTIMIZER_FREE file`

Groups *Overall solver*

`MSK_IPAR_PARAM_READ_CASE_NAME`
    If turned on, then names in the parameter file are case sensitive.

Default *ON*

Accepted *ON* , *OFF*

Example `mosek -d MSK_IPAR_PARAM_READ_CASE_NAME MSK_ON file`

Groups *Data input/output*

`MSK_IPAR_PARAM_READ_IGN_ERROR`
    If turned on, then errors in parameter settings is ignored.

Default *OFF*

Accepted *ON* , *OFF*

Example `mosek -d MSK_IPAR_PARAM_READ_IGN_ERROR MSK_OFF file`

Groups *Data input/output*

`MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL`
    Controls the maximum amount of fill-in that can be created by one pivot in the elimination phase of the presolve. A negative value means the parameter value is selected automatically.

Default -1

Accepted [-inf; +inf]

Example `mosek -d MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL -1 file`

Groups *Presolve*

`MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES`
    Control the maximum number of times the eliminator is tried. A negative value implies **MOSEK** decides.

Default -1

Accepted [-inf; +inf]

Example `mosek -d MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES -1 file`

Groups *Presolve*

`MSK_IPAR_PRESOLVE_LEVEL`
    Currently not used.

Default -1

Accepted [-inf; +inf]

Example `mosek -d MSK_IPAR_PRESOLVE_LEVEL -1 file`

Groups *Overall solver*, *Presolve*

`MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH`

Controls linear dependency check in presolve. The linear dependency check is potentially computationally expensive.

> **Default** 100
>
> **Accepted** [-inf; +inf]
>
> **Example** `mosek -d MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH 100 file`
>
> **Groups** *Presolve*

`MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH`

Controls linear dependency check in presolve. The linear dependency check is potentially computationally expensive.

> **Default** 100
>
> **Accepted** [-inf; +inf]
>
> **Example** `mosek -d MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH 100 file`
>
> **Groups** *Presolve*

`MSK_IPAR_PRESOLVE_LINDEP_USE`

Controls whether the linear constraints are checked for linear dependencies.

> **Default** *ON*
>
> **Accepted** *ON*, *OFF*
>
> **Example** `mosek -d MSK_IPAR_PRESOLVE_LINDEP_USE MSK_ON file`
>
> **Groups** *Presolve*

`MSK_IPAR_PRESOLVE_MAX_NUM_PASS`

Control the maximum number of times presolve passes over the problem. A negative value implies **MOSEK** decides.

> **Default** -1
>
> **Accepted** [-inf; +inf]
>
> **Example** `mosek -d MSK_IPAR_PRESOLVE_MAX_NUM_PASS -1 file`
>
> **Groups** *Presolve*

`MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS`

Controls the maximum number of reductions performed by the presolve. The value of the parameter is normally only changed in connection with debugging. A negative value implies that an infinite number of reductions are allowed.

> **Default** -1
>
> **Accepted** [-inf; +inf]
>
> **Example** `mosek -d MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS -1 file`
>
> **Groups** *Overall solver*, *Presolve*

`MSK_IPAR_PRESOLVE_USE`

Controls whether the presolve is applied to a problem before it is optimized.

> **Default** *FREE*
>
> **Accepted** *OFF*, *ON*, *FREE*
>
> **Example** `mosek -d MSK_IPAR_PRESOLVE_USE MSK_PRESOLVE_MODE_FREE file`
>
> **Groups** *Overall solver*, *Presolve*

`MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER`

Controls which optimizer that is used to find the optimal repair.

> **Default** *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Example `mosek -d MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER MSK_OPTIMIZER_FREE file`

Groups *Overall solver*

MSK_IPAR_PTF_WRITE_TRANSFORM

If *MSK_IPAR_PTF_WRITE_TRANSFORM* is *MSK_ON*, constraint blocks with identifiable conic slacks are transformed into conic constraints and the slacks are eliminated.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_PTF_WRITE_TRANSFORM MSK_ON file`

Groups *Data input/output*

MSK_IPAR_READ_DEBUG

Turns on additional debugging information when reading files.

Default *OFF*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_READ_DEBUG MSK_OFF file`

Groups *Data input/output*

MSK_IPAR_READ_KEEP_FREE_CON

Controls whether the free constraints are included in the problem.

Default *OFF*

Accepted

- *ON*: The free constraints are kept.
- *OFF*: The free constraints are discarded.

Example `mosek -d MSK_IPAR_READ_KEEP_FREE_CON MSK_OFF file`

Groups *Data input/output*

MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU

If this option is turned on, **MOSEK** will drop variables that are defined for the first time in the bounds section.

Default *OFF*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU MSK_OFF file`

Groups *Data input/output*

MSK_IPAR_READ_LP_QUOTED_NAMES

If a name is in quotes when reading an LP file, the quotes will be removed.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_READ_LP_QUOTED_NAMES MSK_ON file`

Groups *Data input/output*

MSK_IPAR_READ_MPS_FORMAT

Controls how strictly the MPS file reader interprets the MPS format.

Default *FREE*

Accepted *STRICT*, *RELAXED*, *FREE*, *CPLEX*

Example `mosek -d MSK_IPAR_READ_MPS_FORMAT MSK_MPS_FORMAT_FREE file`

Groups *Data input/output*

`MSK_IPAR_READ_MPS_WIDTH`
    Controls the maximal number of characters allowed in one line of the MPS file.

        Default 1024
        Accepted [80; +inf]
        Example `mosek -d MSK_IPAR_READ_MPS_WIDTH 1024 file`
        Groups *Data input/output*

`MSK_IPAR_READ_TASK_IGNORE_PARAM`
    Controls whether **MOSEK** should ignore the parameter setting defined in the task file and use the default parameter setting instead.

        Default *OFF*
        Accepted *ON*, *OFF*
        Example `mosek -d MSK_IPAR_READ_TASK_IGNORE_PARAM MSK_OFF file`
        Groups *Data input/output*

`MSK_IPAR_REMOVE_UNUSED_SOLUTIONS`
    Removes unused solutions before the optimization is performed.

        Default *OFF*
        Accepted *ON*, *OFF*
        Example `mosek -d MSK_IPAR_REMOVE_UNUSED_SOLUTIONS MSK_OFF file`
        Groups *Overall system*

`MSK_IPAR_SENSITIVITY_ALL`
    Not applicable.

        Default *OFF*
        Accepted *ON*, *OFF*
        Example `mosek -d MSK_IPAR_SENSITIVITY_ALL MSK_OFF file`
        Groups *Overall solver*

`MSK_IPAR_SENSITIVITY_OPTIMIZER`
    Controls which optimizer is used for optimal partition sensitivity analysis.

        Default *FREE_SIMPLEX*
        Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*
        Example `mosek -d MSK_IPAR_SENSITIVITY_OPTIMIZER MSK_OPTIMIZER_FREE_SIMPLEX file`
        Groups *Overall solver*, *Simplex optimizer*

`MSK_IPAR_SENSITIVITY_TYPE`
    Controls which type of sensitivity analysis is to be performed.

        Default *BASIS*
        Accepted *BASIS*
        Example `mosek -d MSK_IPAR_SENSITIVITY_TYPE MSK_SENSITIVITY_TYPE_BASIS file`
        Groups *Overall solver*

`MSK_IPAR_SIM_BASIS_FACTOR_USE`
    Controls whether an LU factorization of the basis is used in a hot-start. Forcing a refactorization sometimes improves the stability of the simplex optimizers, but in most cases there is a performance penalty.

        Default *ON*
        Accepted *ON*, *OFF*
        Example `mosek -d MSK_IPAR_SIM_BASIS_FACTOR_USE MSK_ON file`

Groups *Simplex optimizer*

`MSK_IPAR_SIM_DEGEN`
    Controls how aggressively degeneration is handled.

        Default *FREE*
        Accepted *NONE*, *FREE*, *AGGRESSIVE*, *MODERATE*, *MINIMUM*
        Example `mosek -d MSK_IPAR_SIM_DEGEN MSK_SIM_DEGEN_FREE file`
        Groups *Simplex optimizer*

`MSK_IPAR_SIM_DUAL_CRASH`
    Controls whether crashing is performed in the dual simplex optimizer. If this parameter is set to x, then a crash will be performed if a basis consists of more than $(100 - x) \mod f_v$ entries, where f_v is the number of fixed variables.

        Default 90
        Accepted $[0; +\inf]$
        Example `mosek -d MSK_IPAR_SIM_DUAL_CRASH 90 file`
        Groups *Dual simplex*

`MSK_IPAR_SIM_DUAL_PHASEONE_METHOD`
    An experimental feature.

        Default 0
        Accepted $[0; 10]$
        Example `mosek -d MSK_IPAR_SIM_DUAL_PHASEONE_METHOD 0 file`
        Groups *Simplex optimizer*

`MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION`
    The dual simplex optimizer can use a so-called restricted selection/pricing strategy to choose the outgoing variable. Hence, if restricted selection is applied, then the dual simplex optimizer first choose a subset of all the potential outgoing variables. Next, for some time it will choose the outgoing variable only among the subset. From time to time the subset is redefined. A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

        Default 50
        Accepted $[0; 100]$
        Example `mosek -d MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION 50 file`
        Groups *Dual simplex*

`MSK_IPAR_SIM_DUAL_SELECTION`
    Controls the choice of the incoming variable, known as the selection strategy, in the dual simplex optimizer.

        Default *FREE*
        Accepted *FREE*, *FULL*, *ASE*, *DEVEX*, *SE*, *PARTIAL*
        Example `mosek -d MSK_IPAR_SIM_DUAL_SELECTION MSK_SIM_SELECTION_FREE file`
        Groups *Dual simplex*

`MSK_IPAR_SIM_EXPLOIT_DUPVEC`
    Controls if the simplex optimizers are allowed to exploit duplicated columns.

        Default *OFF*
        Accepted *ON*, *OFF*, *FREE*
        Example `mosek -d MSK_IPAR_SIM_EXPLOIT_DUPVEC MSK_SIM_EXPLOIT_DUPVEC_OFF file`
        Groups *Simplex optimizer*

`MSK_IPAR_SIM_HOTSTART`

Controls the type of hot-start that the simplex optimizer perform.

>**Default** *FREE*
>**Accepted** *NONE*, *FREE*, *STATUS_KEYS*
>**Example** `mosek -d MSK_IPAR_SIM_HOTSTART MSK_SIM_HOTSTART_FREE file`
>**Groups** *Simplex optimizer*

`MSK_IPAR_SIM_HOTSTART_LU`

Determines if the simplex optimizer should exploit the initial factorization.

>**Default** *ON*
>**Accepted**
>
>>- *ON*: Factorization is reused if possible.
>>- *OFF*: Factorization is recomputed.
>
>**Example** `mosek -d MSK_IPAR_SIM_HOTSTART_LU MSK_ON file`
>**Groups** *Simplex optimizer*

`MSK_IPAR_SIM_MAX_ITERATIONS`

Maximum number of iterations that can be used by a simplex optimizer.

>**Default** 10000000
>**Accepted** [0; +inf]
>**Example** `mosek -d MSK_IPAR_SIM_MAX_ITERATIONS 10000000 file`
>**Groups** *Simplex optimizer*, *Termination criteria*

`MSK_IPAR_SIM_MAX_NUM_SETBACKS`

Controls how many set-backs are allowed within a simplex optimizer. A set-back is an event where the optimizer moves in the wrong direction. This is impossible in theory but may happen due to numerical problems.

>**Default** 250
>**Accepted** [0; +inf]
>**Example** `mosek -d MSK_IPAR_SIM_MAX_NUM_SETBACKS 250 file`
>**Groups** *Simplex optimizer*

`MSK_IPAR_SIM_NON_SINGULAR`

Controls if the simplex optimizer ensures a non-singular basis, if possible.

>**Default** *ON*
>**Accepted** *ON*, *OFF*
>**Example** `mosek -d MSK_IPAR_SIM_NON_SINGULAR MSK_ON file`
>**Groups** *Simplex optimizer*

`MSK_IPAR_SIM_PRIMAL_CRASH`

Controls whether crashing is performed in the primal simplex optimizer. In general, if a basis consists of more than (100-this parameter value)% fixed variables, then a crash will be performed.

>**Default** 90
>**Accepted** [0; +inf]
>**Example** `mosek -d MSK_IPAR_SIM_PRIMAL_CRASH 90 file`
>**Groups** *Primal simplex*

`MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD`

An experimental feature.

>**Default** 0
>**Accepted** [0; 10]
>**Example** `mosek -d MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD 0 file`

MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION

The primal simplex optimizer can use a so-called restricted selection/pricing strategy to choose the outgoing variable. Hence, if restricted selection is applied, then the primal simplex optimizer first choose a subset of all the potential incoming variables. Next, for some time it will choose the incoming variable only among the subset. From time to time the subset is redefined. A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

> **Default** 50
>
> **Accepted** [0; 100]
>
> **Example** mosek -d MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION 50 file
>
> **Groups** *Primal simplex*

MSK_IPAR_SIM_PRIMAL_SELECTION

Controls the choice of the incoming variable, known as the selection strategy, in the primal simplex optimizer.

> **Default** *FREE*
>
> **Accepted** *FREE*, *FULL*, *ASE*, *DEVEX*, *SE*, *PARTIAL*
>
> **Example** mosek -d MSK_IPAR_SIM_PRIMAL_SELECTION MSK_SIM_SELECTION_FREE file
>
> **Groups** *Primal simplex*

MSK_IPAR_SIM_REFACTOR_FREQ

Controls how frequent the basis is refactorized. The value 0 means that the optimizer determines the best point of refactorization. It is strongly recommended NOT to change this parameter.

> **Default** 0
>
> **Accepted** [0; +inf]
>
> **Example** mosek -d MSK_IPAR_SIM_REFACTOR_FREQ 0 file
>
> **Groups** *Simplex optimizer*

MSK_IPAR_SIM_REFORMULATION

Controls if the simplex optimizers are allowed to reformulate the problem.

> **Default** *OFF*
>
> **Accepted** *ON*, *OFF*, *FREE*, *AGGRESSIVE*
>
> **Example** mosek -d MSK_IPAR_SIM_REFORMULATION MSK_SIM_REFORMULATION_OFF file
>
> **Groups** *Simplex optimizer*

MSK_IPAR_SIM_SAVE_LU

Controls if the LU factorization stored should be replaced with the LU factorization corresponding to the initial basis.

> **Default** *OFF*
>
> **Accepted** *ON*, *OFF*
>
> **Example** mosek -d MSK_IPAR_SIM_SAVE_LU MSK_OFF file
>
> **Groups** *Simplex optimizer*

MSK_IPAR_SIM_SCALING

Controls how much effort is used in scaling the problem before a simplex optimizer is used.

> **Default** *FREE*
>
> **Accepted** *FREE*, *NONE*, *MODERATE*, *AGGRESSIVE*
>
> **Example** mosek -d MSK_IPAR_SIM_SCALING MSK_SCALING_FREE file
>
> **Groups** *Simplex optimizer*

MSK_IPAR_SIM_SCALING_METHOD
   Controls how the problem is scaled before a simplex optimizer is used.

   > **Default** *POW2*
   > **Accepted** *POW2*, *FREE*
   > **Example** mosek -d MSK_IPAR_SIM_SCALING_METHOD MSK_SCALING_METHOD_POW2
   >   file
   > **Groups** *Simplex optimizer*

MSK_IPAR_SIM_SEED
   Sets the random seed used for randomization in the simplex optimizers.

   > **Default** 23456
   > **Accepted** [0; 32749]
   > **Example** mosek -d MSK_IPAR_SIM_SEED 23456 file
   > **Groups** *Simplex optimizer*

MSK_IPAR_SIM_SOLVE_FORM
   Controls whether the primal or the dual problem is solved by the primal-/dual-simplex optimizer.

   > **Default** *FREE*
   > **Accepted** *FREE*, *PRIMAL*, *DUAL*
   > **Example** mosek -d MSK_IPAR_SIM_SOLVE_FORM MSK_SOLVE_FREE file
   > **Groups** *Simplex optimizer*

MSK_IPAR_SIM_STABILITY_PRIORITY
   Controls how high priority the numerical stability should be given.

   > **Default** 50
   > **Accepted** [0; 100]
   > **Example** mosek -d MSK_IPAR_SIM_STABILITY_PRIORITY 50 file
   > **Groups** *Simplex optimizer*

MSK_IPAR_SIM_SWITCH_OPTIMIZER
   The simplex optimizer sometimes chooses to solve the dual problem instead of the primal problem. This implies that if you have chosen to use the dual simplex optimizer and the problem is dualized, then it actually makes sense to use the primal simplex optimizer instead. If this parameter is on and the problem is dualized and furthermore the simplex optimizer is chosen to be the primal (dual) one, then it is switched to the dual (primal).

   > **Default** *OFF*
   > **Accepted** *ON*, *OFF*
   > **Example** mosek -d MSK_IPAR_SIM_SWITCH_OPTIMIZER MSK_OFF file
   > **Groups** *Simplex optimizer*

MSK_IPAR_SOL_FILTER_KEEP_BASIC
   If turned on, then basic and super basic constraints and variables are written to the solution file independent of the filter setting.

   > **Default** *OFF*
   > **Accepted** *ON*, *OFF*
   > **Example** mosek -d MSK_IPAR_SOL_FILTER_KEEP_BASIC MSK_OFF file
   > **Groups** *Solution input/output*

MSK_IPAR_SOL_FILTER_KEEP_RANGED
   If turned on, then ranged constraints and variables are written to the solution file independent of the filter setting.

   > **Default** *OFF*
   > **Accepted** *ON*, *OFF*

Example `mosek -d MSK_IPAR_SOL_FILTER_KEEP_RANGED MSK_OFF file`

Groups *Solution input/output*

MSK_IPAR_SOL_READ_NAME_WIDTH

When a solution is read by **MOSEK** and some constraint, variable or cone names contain blanks, then a maximum name width much be specified. A negative value implies that no name contain blanks.

Default -1

Accepted [-inf; +inf]

Example `mosek -d MSK_IPAR_SOL_READ_NAME_WIDTH -1 file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_SOL_READ_WIDTH

Controls the maximal acceptable width of line in the solutions when read by **MOSEK**.

Default 1024

Accepted [80; +inf]

Example `mosek -d MSK_IPAR_SOL_READ_WIDTH 1024 file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_SOLUTION_CALLBACK

Indicates whether solution callbacks will be performed during the optimization.

Default *OFF*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_SOLUTION_CALLBACK MSK_OFF file`

Groups *Progress callback*, *Overall solver*

MSK_IPAR_TIMING_LEVEL

Controls the amount of timing performed inside **MOSEK**.

Default 1

Accepted [0; +inf]

Example `mosek -d MSK_IPAR_TIMING_LEVEL 1 file`

Groups *Overall system*

MSK_IPAR_WRITE_BAS_CONSTRAINTS

Controls whether the constraint section is written to the basic solution file.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_BAS_CONSTRAINTS MSK_ON file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_WRITE_BAS_HEAD

Controls whether the header section is written to the basic solution file.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_BAS_HEAD MSK_ON file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_WRITE_BAS_VARIABLES

Controls whether the variables section is written to the basic solution file.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_BAS_VARIABLES MSK_ON file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_WRITE_COMPRESSION

Controls whether the data file is compressed while it is written. 0 means no compression while higher values mean more compression.

> **Default** 9
>
> **Accepted** [0; +inf]
>
> **Example** `mosek -d MSK_IPAR_WRITE_COMPRESSION 9 file`
>
> **Groups** *Data input/output*

MSK_IPAR_WRITE_DATA_PARAM

If this option is turned on the parameter settings are written to the data file as parameters.

> **Default** *OFF*
>
> **Accepted** *ON*, *OFF*
>
> **Example** `mosek -d MSK_IPAR_WRITE_DATA_PARAM MSK_OFF file`
>
> **Groups** *Data input/output*

MSK_IPAR_WRITE_FREE_CON

Controls whether the free constraints are written to the data file.

> **Default** *ON*
>
> **Accepted** *ON*, *OFF*
>
> **Example** `mosek -d MSK_IPAR_WRITE_FREE_CON MSK_ON file`
>
> **Groups** *Data input/output*

MSK_IPAR_WRITE_GENERIC_NAMES

Controls whether generic names should be used instead of user-defined names when writing to the data file.

> **Default** *OFF*
>
> **Accepted** *ON*, *OFF*
>
> **Example** `mosek -d MSK_IPAR_WRITE_GENERIC_NAMES MSK_OFF file`
>
> **Groups** *Data input/output*

MSK_IPAR_WRITE_GENERIC_NAMES_IO

Index origin used in generic names.

> **Default** 1
>
> **Accepted** [0; +inf]
>
> **Example** `mosek -d MSK_IPAR_WRITE_GENERIC_NAMES_IO 1 file`
>
> **Groups** *Data input/output*

MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS

Controls if the writer ignores incompatible problem items when writing files.

> **Default** *OFF*
>
> **Accepted**
>
> - *ON*: Ignore items that cannot be written to the current output file format.
> - *OFF*: Produce an error if the problem contains items that cannot the written to the current output file format.
>
> **Example** `mosek -d MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS MSK_OFF file`
>
> **Groups** *Data input/output*

MSK_IPAR_WRITE_INT_CONSTRAINTS

Controls whether the constraint section is written to the integer solution file.

> **Default** *ON*
>
> **Accepted** *ON*, *OFF*
>
> **Example** `mosek -d MSK_IPAR_WRITE_INT_CONSTRAINTS MSK_ON file`

`MSK_IPAR_WRITE_INT_HEAD`

Controls whether the header section is written to the integer solution file.

> **Default** *ON*
> **Accepted** *ON*, *OFF*
> **Example** `mosek -d MSK_IPAR_WRITE_INT_HEAD MSK_ON file`
> **Groups** *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_INT_VARIABLES`

Controls whether the variables section is written to the integer solution file.

> **Default** *ON*
> **Accepted** *ON*, *OFF*
> **Example** `mosek -d MSK_IPAR_WRITE_INT_VARIABLES MSK_ON file`
> **Groups** *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_LP_FULL_OBJ`

Write all variables, including the ones with 0-coefficients, in the objective.

> **Default** *ON*
> **Accepted** *ON*, *OFF*
> **Example** `mosek -d MSK_IPAR_WRITE_LP_FULL_OBJ MSK_ON file`
> **Groups** *Data input/output*

`MSK_IPAR_WRITE_LP_LINE_WIDTH`

Maximum width of line in an LP file written by **MOSEK**.

> **Default** 80
> **Accepted** [40; +inf]
> **Example** `mosek -d MSK_IPAR_WRITE_LP_LINE_WIDTH 80 file`
> **Groups** *Data input/output*

`MSK_IPAR_WRITE_LP_QUOTED_NAMES`

If this option is turned on, then **MOSEK** will quote invalid LP names when writing an LP file.

> **Default** *ON*
> **Accepted** *ON*, *OFF*
> **Example** `mosek -d MSK_IPAR_WRITE_LP_QUOTED_NAMES MSK_ON file`
> **Groups** *Data input/output*

`MSK_IPAR_WRITE_LP_STRICT_FORMAT`

Controls whether LP output files satisfy the LP format strictly.

> **Default** *OFF*
> **Accepted** *ON*, *OFF*
> **Example** `mosek -d MSK_IPAR_WRITE_LP_STRICT_FORMAT MSK_OFF file`
> **Groups** *Data input/output*

`MSK_IPAR_WRITE_LP_TERMS_PER_LINE`

Maximum number of terms on a single line in an LP file written by **MOSEK**. 0 means unlimited.

> **Default** 10
> **Accepted** [0; +inf]
> **Example** `mosek -d MSK_IPAR_WRITE_LP_TERMS_PER_LINE 10 file`
> **Groups** *Data input/output*

`MSK_IPAR_WRITE_MPS_FORMAT`

Controls in which format the MPS is written.

Default *FREE*

Accepted *STRICT*, *RELAXED*, *FREE*, *CPLEX*

Example `mosek -d MSK_IPAR_WRITE_MPS_FORMAT MSK_MPS_FORMAT_FREE file`

Groups *Data input/output*

MSK_IPAR_WRITE_MPS_INT

Controls if marker records are written to the MPS file to indicate whether variables are integer restricted.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_MPS_INT MSK_ON file`

Groups *Data input/output*

MSK_IPAR_WRITE_PRECISION

Controls the precision with which `double` numbers are printed in the MPS data file. In general it is not worthwhile to use a value higher than 15.

Default 15

Accepted [0; +inf]

Example `mosek -d MSK_IPAR_WRITE_PRECISION 15 file`

Groups *Data input/output*

MSK_IPAR_WRITE_SOL_BARVARIABLES

Controls whether the symmetric matrix variables section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_SOL_BARVARIABLES MSK_ON file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_WRITE_SOL_CONSTRAINTS

Controls whether the constraint section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_SOL_CONSTRAINTS MSK_ON file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_WRITE_SOL_HEAD

Controls whether the header section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_SOL_HEAD MSK_ON file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES

Even if the names are invalid MPS names, then they are employed when writing the solution file.

Default *OFF*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES MSK_OFF file`

Groups *Data input/output*, *Solution input/output*

MSK_IPAR_WRITE_SOL_VARIABLES

Controls whether the variables section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Example `mosek -d MSK_IPAR_WRITE_SOL_VARIABLES MSK_ON file`

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_TASK_INC_SOL`
Controls whether the solutions are stored in the task file too.

> **Default** *ON*
> **Accepted** *ON*, *OFF*
> **Example** `mosek -d MSK_IPAR_WRITE_TASK_INC_SOL MSK_ON file`
> **Groups** *Data input/output*

`MSK_IPAR_WRITE_XML_MODE`
Controls if linear coefficients should be written by row or column when writing in the XML file format.

> **Default** *ROW*
> **Accepted** *ROW*, *COL*
> **Example** `mosek -d MSK_IPAR_WRITE_XML_MODE MSK_WRITE_XML_MODE_ROW file`
> **Groups** *Data input/output*

11.2.3 String parameters

`MSK_SPAR_BAS_SOL_FILE_NAME`
Name of the `bas` solution file.

> **Accepted** Any valid file name.
> **Example** `mosek -d MSK_SPAR_BAS_SOL_FILE_NAME somevalue file`
> **Groups** *Data input/output*, *Solution input/output*

`MSK_SPAR_DATA_FILE_NAME`
Data are read and written to this file.

> **Accepted** Any valid file name.
> **Example** `mosek -d MSK_SPAR_DATA_FILE_NAME somevalue file`
> **Groups** *Data input/output*

`MSK_SPAR_DEBUG_FILE_NAME`
MOSEK debug file.

> **Accepted** Any valid file name.
> **Example** `mosek -d MSK_SPAR_DEBUG_FILE_NAME somevalue file`
> **Groups** *Data input/output*

`MSK_SPAR_INT_SOL_FILE_NAME`
Name of the `int` solution file.

> **Accepted** Any valid file name.
> **Example** `mosek -d MSK_SPAR_INT_SOL_FILE_NAME somevalue file`
> **Groups** *Data input/output*, *Solution input/output*

`MSK_SPAR_ITR_SOL_FILE_NAME`
Name of the `itr` solution file.

> **Accepted** Any valid file name.
> **Example** `mosek -d MSK_SPAR_ITR_SOL_FILE_NAME somevalue file`
> **Groups** *Data input/output*, *Solution input/output*

`MSK_SPAR_MIO_DEBUG_STRING`
For internal debugging purposes.

> **Accepted** Any valid string.

Example `mosek -d MSK_SPAR_MIO_DEBUG_STRING somevalue file`

Groups *Data input/output*

`MSK_SPAR_PARAM_COMMENT_SIGN`

Only the first character in this string is used. It is considered as a start of comment sign in the **MOSEK** parameter file. Spaces are ignored in the string.

Default
%%

Accepted Any valid string.

Example `mosek -d MSK_SPAR_PARAM_COMMENT_SIGN %% file`

Groups *Data input/output*

`MSK_SPAR_PARAM_READ_FILE_NAME`

Modifications to the parameter database is read from this file.

Accepted Any valid file name.

Example `mosek -d MSK_SPAR_PARAM_READ_FILE_NAME somevalue file`

Groups *Data input/output*

`MSK_SPAR_PARAM_WRITE_FILE_NAME`

The parameter database is written to this file.

Accepted Any valid file name.

Example `mosek -d MSK_SPAR_PARAM_WRITE_FILE_NAME somevalue file`

Groups *Data input/output*

`MSK_SPAR_READ_MPS_BOU_NAME`

Name of the BOUNDS vector used. An empty name means that the first BOUNDS vector is used.

Accepted Any valid MPS name.

Example `mosek -d MSK_SPAR_READ_MPS_BOU_NAME somevalue file`

Groups *Data input/output*

`MSK_SPAR_READ_MPS_OBJ_NAME`

Name of the free constraint used as objective function. An empty name means that the first constraint is used as objective function.

Accepted Any valid MPS name.

Example `mosek -d MSK_SPAR_READ_MPS_OBJ_NAME somevalue file`

Groups *Data input/output*

`MSK_SPAR_READ_MPS_RAN_NAME`

Name of the RANGE vector used. An empty name means that the first RANGE vector is used.

Accepted Any valid MPS name.

Example `mosek -d MSK_SPAR_READ_MPS_RAN_NAME somevalue file`

Groups *Data input/output*

`MSK_SPAR_READ_MPS_RHS_NAME`

Name of the RHS used. An empty name means that the first RHS vector is used.

Accepted Any valid MPS name.

Example `mosek -d MSK_SPAR_READ_MPS_RHS_NAME somevalue file`

Groups *Data input/output*

`MSK_SPAR_REMOTE_ACCESS_TOKEN`

An access token used to submit tasks to a remote **MOSEK** server. An access token is a random 32-byte string encoded in base64, i.e. it is a 44 character ASCII string.

Accepted Any valid string.

Example `mosek -d MSK_SPAR_REMOTE_ACCESS_TOKEN somevalue file`

Groups *Overall system*

MSK_SPAR_SENSITIVITY_FILE_NAME
Not applicable.

> **Accepted** Any valid string.
>
> **Example** `mosek -d MSK_SPAR_SENSITIVITY_FILE_NAME somevalue file`
>
> **Groups** *Data input/output*

MSK_SPAR_SENSITIVITY_RES_FILE_NAME
Not applicable.

> **Accepted** Any valid string.
>
> **Example** `mosek -d MSK_SPAR_SENSITIVITY_RES_FILE_NAME somevalue file`
>
> **Groups** *Data input/output*

MSK_SPAR_SOL_FILTER_XC_LOW
A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having `xc[i]>0.5` should be listed, whereas +0.5 means that all constraints having `xc[i]>=blc[i]+0.5` should be listed. An empty filter means that no filter is applied.

> **Accepted** Any valid filter.
>
> **Example** `mosek -d MSK_SPAR_SOL_FILTER_XC_LOW somevalue file`
>
> **Groups** *Data input/output*, *Solution input/output*

MSK_SPAR_SOL_FILTER_XC_UPR
A filter used to determine which constraints should be listed in the solution file. A value of `0.5` means that all constraints having `xc[i]<0.5` should be listed, whereas `-0.5` means all constraints having `xc[i]<=buc[i]-0.5` should be listed. An empty filter means that no filter is applied.

> **Accepted** Any valid filter.
>
> **Example** `mosek -d MSK_SPAR_SOL_FILTER_XC_UPR somevalue file`
>
> **Groups** *Data input/output*, *Solution input/output*

MSK_SPAR_SOL_FILTER_XX_LOW
A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having `xx[j]>=0.5` should be listed, whereas "+0.5" means that all constraints having `xx[j]>=blx[j]+0.5` should be listed. An empty filter means no filter is applied.

> **Accepted** Any valid filter.
>
> **Example** `mosek -d MSK_SPAR_SOL_FILTER_XX_LOW somevalue file`
>
> **Groups** *Data input/output*, *Solution input/output*

MSK_SPAR_SOL_FILTER_XX_UPR
A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having `xx[j]<0.5` should be printed, whereas "-0.5" means all constraints having `xx[j]<=bux[j]-0.5` should be listed. An empty filter means no filter is applied.

> **Accepted** Any valid file name.
>
> **Example** `mosek -d MSK_SPAR_SOL_FILTER_XX_UPR somevalue file`
>
> **Groups** *Data input/output*, *Solution input/output*

MSK_SPAR_STAT_FILE_NAME
Statistics file name.

> **Accepted** Any valid file name.
>
> **Example** `mosek -d MSK_SPAR_STAT_FILE_NAME somevalue file`
>
> **Groups** *Data input/output*

```
MSK_SPAR_STAT_KEY
```
Key used when writing the summary file.

> **Accepted** Any valid string.
>
> **Example** `mosek -d MSK_SPAR_STAT_KEY somevalue file`
>
> **Groups** *Data input/output*

```
MSK_SPAR_STAT_NAME
```
Name used when writing the statistics file.

> **Accepted** Any valid XML string.
>
> **Example** `mosek -d MSK_SPAR_STAT_NAME somevalue file`
>
> **Groups** *Data input/output*

```
MSK_SPAR_WRITE_LP_GEN_VAR_NAME
```
Sometimes when an LP file is written additional variables must be inserted. They will have the prefix denoted by this parameter.

> **Default** xmskgen
>
> **Accepted** Any valid string.
>
> **Example** `mosek -d MSK_SPAR_WRITE_LP_GEN_VAR_NAME xmskgen file`
>
> **Groups** *Data input/output*

11.3 Response codes

Response codes include:

- *Termination codes*

- *Warnings*

- *Errors*

The numerical code (in brackets) identifies the response in error messages and in the log output.

11.3.1 Termination

```
MSK_RES_OK (0)
```
No error occurred.
```
MSK_RES_TRM_MAX_ITERATIONS (10000)
```
The optimizer terminated at the maximum number of iterations.
```
MSK_RES_TRM_MAX_TIME (10001)
```
The optimizer terminated at the maximum amount of time.
```
MSK_RES_TRM_OBJECTIVE_RANGE (10002)
```
The optimizer terminated with an objective value outside the objective range.
```
MSK_RES_TRM_MIO_NUM_RELAXS (10008)
```
The mixed-integer optimizer terminated as the maximum number of relaxations was reached.
```
MSK_RES_TRM_MIO_NUM_BRANCHES (10009)
```
The mixed-integer optimizer terminated as the maximum number of branches was reached.
```
MSK_RES_TRM_NUM_MAX_NUM_INT_SOLUTIONS (10015)
```
The mixed-integer optimizer terminated as the maximum number of feasible solutions was reached.
```
MSK_RES_TRM_STALL (10006)
```
The optimizer is terminated due to slow progress.

Stalling means that numerical problems prevent the optimizer from making reasonable progress and that it makes no sense to continue. In many cases this happens if the problem is badly scaled or otherwise ill-conditioned. There is no guarantee that the solution will be feasible or optimal. However, often stalling happens near the optimum, and the returned solution may be of good quality. Therefore, it is recommended to check the status of the solution. If the solution status is optimal the solution is most likely good enough for most practical purposes.

Please note that if a linear optimization problem is solved using the interior-point optimizer with basis identification turned on, the returned basic solution likely to have high accuracy, even though the optimizer stalled.

Some common causes of stalling are a) badly scaled models, b) near feasible or near infeasible problems.

MSK_RES_TRM_USER_CALLBACK (10007)
    The optimizer terminated due to the return of the user-defined callback function.

MSK_RES_TRM_MAX_NUM_SETBACKS (10020)
    The optimizer terminated as the maximum number of set-backs was reached. This indicates serious numerical problems and a possibly badly formulated problem.

MSK_RES_TRM_NUMERICAL_PROBLEM (10025)
    The optimizer terminated due to numerical problems.

MSK_RES_TRM_INTERNAL (10030)
    The optimizer terminated due to some internal reason. Please contact **MOSEK** support.

MSK_RES_TRM_INTERNAL_STOP (10031)
    The optimizer terminated for internal reasons. Please contact **MOSEK** support.

11.3.2 Warnings

MSK_RES_WRN_OPEN_PARAM_FILE (50)
    The parameter file could not be opened.

MSK_RES_WRN_LARGE_BOUND (51)
    A numerically large bound value is specified.

MSK_RES_WRN_LARGE_LO_BOUND (52)
    A numerically large lower bound value is specified.

MSK_RES_WRN_LARGE_UP_BOUND (53)
    A numerically large upper bound value is specified.

MSK_RES_WRN_LARGE_CON_FX (54)
    An equality constraint is fixed to a numerically large value. This can cause numerical problems.

MSK_RES_WRN_LARGE_CJ (57)
    A numerically large value is specified for one c_j.

MSK_RES_WRN_LARGE_AIJ (62)
    A numerically large value is specified for an $a_{i,j}$ element in A. The parameter *MSK_DPAR_DATA_TOL_AIJ_LARGE* controls when an $a_{i,j}$ is considered large.

MSK_RES_WRN_ZERO_AIJ (63)
    One or more zero elements are specified in A.

MSK_RES_WRN_NAME_MAX_LEN (65)
    A name is longer than the buffer that is supposed to hold it.

MSK_RES_WRN_SPAR_MAX_LEN (66)
    A value for a string parameter is longer than the buffer that is supposed to hold it.

MSK_RES_WRN_MPS_SPLIT_RHS_VECTOR (70)
    An RHS vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_MPS_SPLIT_RAN_VECTOR (71)
    A RANGE vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_MPS_SPLIT_BOU_VECTOR (72)
    A BOUNDS vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_LP_OLD_QUAD_FORMAT (80)
    Missing '/2' after quadratic expressions in bound or objective.

MSK_RES_WRN_LP_DROP_VARIABLE (85)
    Ignored a variable because the variable was not previously defined. Usually this implies that a variable appears in the bound section but not in the objective or the constraints.

MSK_RES_WRN_NZ_IN_UPR_TRI (200)
    Non-zero elements specified in the upper triangle of a matrix were ignored.

MSK_RES_WRN_DROPPED_NZ_QOBJ (201)
    One or more non-zero elements were dropped in the Q matrix in the objective.

MSK_RES_WRN_IGNORE_INTEGER (250)
    Ignored integer constraints.

MSK_RES_WRN_NO_GLOBAL_OPTIMIZER (251)
        No global optimizer is available.
MSK_RES_WRN_MIO_INFEASIBLE_FINAL (270)
        The final mixed-integer problem with all the integer variables fixed at their optimal values is
        infeasible.
MSK_RES_WRN_SOL_FILTER (300)
        Invalid solution filter is specified.
MSK_RES_WRN_UNDEF_SOL_FILE_NAME (350)
        Undefined name occurred in a solution.
MSK_RES_WRN_SOL_FILE_IGNORED_CON (351)
        One or more lines in the constraint section were ignored when reading a solution file.
MSK_RES_WRN_SOL_FILE_IGNORED_VAR (352)
        One or more lines in the variable section were ignored when reading a solution file.
MSK_RES_WRN_TOO_FEW_BASIS_VARS (400)
        An incomplete basis has been specified. Too few basis variables are specified.
MSK_RES_WRN_TOO_MANY_BASIS_VARS (405)
        A basis with too many variables has been specified.
MSK_RES_WRN_LICENSE_EXPIRE (500)
        The license expires.
MSK_RES_WRN_LICENSE_SERVER (501)
        The license server is not responding.
MSK_RES_WRN_EMPTY_NAME (502)
        A variable or constraint name is empty. The output file may be invalid.
MSK_RES_WRN_USING_GENERIC_NAMES (503)
        Generic names are used because a name is not valid. For instance when writing an LP file the
        names must not contain blanks or start with a digit.
MSK_RES_WRN_LICENSE_FEATURE_EXPIRE (505)
        The license expires.
MSK_RES_WRN_PARAM_NAME_DOU (510)
        The parameter name is not recognized as a double parameter.
MSK_RES_WRN_PARAM_NAME_INT (511)
        The parameter name is not recognized as a integer parameter.
MSK_RES_WRN_PARAM_NAME_STR (512)
        The parameter name is not recognized as a string parameter.
MSK_RES_WRN_PARAM_STR_VALUE (515)
        The string is not recognized as a symbolic value for the parameter.
MSK_RES_WRN_PARAM_IGNORED_CMIO (516)
        A parameter was ignored by the conic mixed integer optimizer.
MSK_RES_WRN_ZEROS_IN_SPARSE_ROW (705)
        One or more (near) zero elements are specified in a sparse row of a matrix. Since, it is redundant
        to specify zero elements then it may indicate an error.
MSK_RES_WRN_ZEROS_IN_SPARSE_COL (710)
        One or more (near) zero elements are specified in a sparse column of a matrix. It is redundant to
        specify zero elements. Hence, it may indicate an error.
MSK_RES_WRN_INCOMPLETE_LINEAR_DEPENDENCY_CHECK (800)
        The linear dependency check(s) is incomplete. Normally this is not an important warning unless
        the optimization problem has been formulated with linear dependencies. Linear dependencies may
        prevent **MOSEK** from solving the problem.
MSK_RES_WRN_ELIMINATOR_SPACE (801)
        The eliminator is skipped at least once due to lack of space.
MSK_RES_WRN_PRESOLVE_OUTOFSPACE (802)
        The presolve is incomplete due to lack of space.
MSK_RES_WRN_WRITE_CHANGED_NAMES (803)
        Some names were changed because they were invalid for the output file format.
MSK_RES_WRN_WRITE_DISCARDED_CFIX (804)
        The fixed objective term could not be converted to a variable and was discarded in the output file.
MSK_RES_WRN_DUPLICATE_CONSTRAINT_NAMES (850)
        Two constraint names are identical.

`MSK_RES_WRN_DUPLICATE_VARIABLE_NAMES (851)`
> Two variable names are identical.

`MSK_RES_WRN_DUPLICATE_BARVARIABLE_NAMES (852)`
> Two barvariable names are identical.

`MSK_RES_WRN_DUPLICATE_CONE_NAMES (853)`
> Two cone names are identical.

`MSK_RES_WRN_ANA_LARGE_BOUNDS (900)`
> This warning is issued by the problem analyzer, if one or more constraint or variable bounds are very large. One should consider omitting these bounds entirely by setting them to +inf or -inf.

`MSK_RES_WRN_ANA_C_ZERO (901)`
> This warning is issued by the problem analyzer, if the coefficients in the linear part of the objective are all zero.

`MSK_RES_WRN_ANA_EMPTY_COLS (902)`
> This warning is issued by the problem analyzer, if columns, in which all coefficients are zero, are found.

`MSK_RES_WRN_ANA_CLOSE_BOUNDS (903)`
> This warning is issued by problem analyzer, if ranged constraints or variables with very close upper and lower bounds are detected. One should consider treating such constraints as equalities and such variables as constants.

`MSK_RES_WRN_ANA_ALMOST_INT_BOUNDS (904)`
> This warning is issued by the problem analyzer if a constraint is bound nearly integral.

`MSK_RES_WRN_QUAD_CONES_WITH_ROOT_FIXED_AT_ZERO (930)`
> For at least one quadratic cone the root is fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problem, or to fix all the variables in the cone to 0.

`MSK_RES_WRN_RQUAD_CONES_WITH_ROOT_FIXED_AT_ZERO (931)`
> For at least one rotated quadratic cone at least one of the root variables are fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problem, or to fix all the variables in the cone to 0.

`MSK_RES_WRN_EXP_CONES_WITH_VARIABLES_FIXED_AT_ZERO (932)`
> For at least one exponential cone $x \geq y \exp(z/y)$ either the variable x or y is fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problem, or to fix all the variables in the cone to 0.

`MSK_RES_WRN_POW_CONES_WITH_ROOT_FIXED_AT_ZERO (933)`
> For at least one power cone at least one of the root variables are fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problem, or to fix all the variables in the cone to 0.

`MSK_RES_WRN_NO_DUALIZER (950)`
> No automatic dualizer is available for the specified problem. The primal problem is solved.

`MSK_RES_WRN_SYM_MAT_LARGE (960)`
> A numerically large value is specified for an $e_{i,j}$ element in E. The parameter `MSK_DPAR_DATA_SYM_MAT_TOL_LARGE` controls when an $e_{i,j}$ is considered large.

11.3.3 Errors

`MSK_RES_ERR_LICENSE (1000)`
> Invalid license.

`MSK_RES_ERR_LICENSE_EXPIRED (1001)`
> The license has expired.

`MSK_RES_ERR_LICENSE_VERSION (1002)`
> The license is valid for another version of **MOSEK**.

`MSK_RES_ERR_SIZE_LICENSE (1005)`
> The problem is bigger than the license.

`MSK_RES_ERR_PROB_LICENSE (1006)`
> The software is not licensed to solve the problem.

`MSK_RES_ERR_FILE_LICENSE (1007)`
> Invalid license file.

`MSK_RES_ERR_MISSING_LICENSE_FILE (1008)`

   MOSEK cannot find license file or a token server. See the **MOSEK** licensing manual for details.

`MSK_RES_ERR_SIZE_LICENSE_CON (1010)`

   The problem has too many constraints to be solved with the available license.

`MSK_RES_ERR_SIZE_LICENSE_VAR (1011)`

   The problem has too many variables to be solved with the available license.

`MSK_RES_ERR_SIZE_LICENSE_INTVAR (1012)`

   The problem contains too many integer variables to be solved with the available license.

`MSK_RES_ERR_OPTIMIZER_LICENSE (1013)`

   The optimizer required is not licensed.

`MSK_RES_ERR_FLEXLM (1014)`

   The FLEXlm license manager reported an error.

`MSK_RES_ERR_LICENSE_SERVER (1015)`

   The license server is not responding.

`MSK_RES_ERR_LICENSE_MAX (1016)`

   Maximum number of licenses is reached.

`MSK_RES_ERR_LICENSE_MOSEKLM_DAEMON (1017)`

   The MOSEKLM license manager daemon is not up and running.

`MSK_RES_ERR_LICENSE_FEATURE (1018)`

   A requested feature is not available in the license file(s). Most likely due to an incorrect license system setup.

`MSK_RES_ERR_PLATFORM_NOT_LICENSED (1019)`

   A requested license feature is not available for the required platform.

`MSK_RES_ERR_LICENSE_CANNOT_ALLOCATE (1020)`

   The license system cannot allocate the memory required.

`MSK_RES_ERR_LICENSE_CANNOT_CONNECT (1021)`

   MOSEK cannot connect to the license server. Most likely the license server is not up and running.

`MSK_RES_ERR_LICENSE_INVALID_HOSTID (1025)`

   The host ID specified in the license file does not match the host ID of the computer.

`MSK_RES_ERR_LICENSE_SERVER_VERSION (1026)`

   The version specified in the checkout request is greater than the highest version number the daemon supports.

`MSK_RES_ERR_LICENSE_NO_SERVER_SUPPORT (1027)`

   The license server does not support the requested feature. Possible reasons for this error include:

   - The feature has expired.

   - The feature's start date is later than today's date.

   - The version requested is higher than feature's the highest supported version.

   - A corrupted license file.

   Try restarting the license and inspect the license server debug file, usually called `lmgrd.log`.

`MSK_RES_ERR_LICENSE_NO_SERVER_LINE (1028)`

   There is no `SERVER` line in the license file. All non-zero license count features need at least one `SERVER` line.

`MSK_RES_ERR_OLDER_DLL (1035)`

   The dynamic link library is older than the specified version.

`MSK_RES_ERR_NEWER_DLL (1036)`

   The dynamic link library is newer than the specified version.

`MSK_RES_ERR_LINK_FILE_DLL (1040)`

   A file cannot be linked to a stream in the DLL version.

`MSK_RES_ERR_THREAD_MUTEX_INIT (1045)`

   Could not initialize a mutex.

`MSK_RES_ERR_THREAD_MUTEX_LOCK (1046)`

   Could not lock a mutex.

`MSK_RES_ERR_THREAD_MUTEX_UNLOCK (1047)`

   Could not unlock a mutex.

`MSK_RES_ERR_THREAD_CREATE (1048)`
> Could not create a thread. This error may occur if a large number of environments are created and not deleted again. In any case it is a good practice to minimize the number of environments created.

`MSK_RES_ERR_THREAD_COND_INIT (1049)`
> Could not initialize a condition.

`MSK_RES_ERR_UNKNOWN (1050)`
> Unknown error.

`MSK_RES_ERR_SPACE (1051)`
> Out of space.

`MSK_RES_ERR_FILE_OPEN (1052)`
> Error while opening a file.

`MSK_RES_ERR_FILE_READ (1053)`
> File read error.

`MSK_RES_ERR_FILE_WRITE (1054)`
> File write error.

`MSK_RES_ERR_DATA_FILE_EXT (1055)`
> The data file format cannot be determined from the file name.

`MSK_RES_ERR_INVALID_FILE_NAME (1056)`
> An invalid file name has been specified.

`MSK_RES_ERR_INVALID_SOL_FILE_NAME (1057)`
> An invalid file name has been specified.

`MSK_RES_ERR_END_OF_FILE (1059)`
> End of file reached.

`MSK_RES_ERR_NULL_ENV (1060)`
> `env` is a NULL pointer.

`MSK_RES_ERR_NULL_TASK (1061)`
> `task` is a NULL pointer.

`MSK_RES_ERR_INVALID_STREAM (1062)`
> An invalid stream is referenced.

`MSK_RES_ERR_NO_INIT_ENV (1063)`
> `env` is not initialized.

`MSK_RES_ERR_INVALID_TASK (1064)`
> The `task` is invalid.

`MSK_RES_ERR_NULL_POINTER (1065)`
> An argument to a function is unexpectedly a NULL pointer.

`MSK_RES_ERR_LIVING_TASKS (1066)`
> All tasks associated with an enviroment must be deleted before the environment is deleted. There are still some undeleted tasks.

`MSK_RES_ERR_BLANK_NAME (1070)`
> An all blank name has been specified.

`MSK_RES_ERR_DUP_NAME (1071)`
> The same name was used multiple times for the same problem item type.

`MSK_RES_ERR_FORMAT_STRING (1072)`
> The name format string is invalid.

`MSK_RES_ERR_INVALID_OBJ_NAME (1075)`
> An invalid objective name is specified.

`MSK_RES_ERR_INVALID_CON_NAME (1076)`
> An invalid constraint name is used.

`MSK_RES_ERR_INVALID_VAR_NAME (1077)`
> An invalid variable name is used.

`MSK_RES_ERR_INVALID_CONE_NAME (1078)`
> An invalid cone name is used.

`MSK_RES_ERR_INVALID_BARVAR_NAME (1079)`
> An invalid symmetric matrix variable name is used.

`MSK_RES_ERR_SPACE_LEAKING (1080)`
> **MOSEK** is leaking memory. This can be due to either an incorrect use of **MOSEK** or a bug.

```
MSK_RES_ERR_SPACE_NO_INFO (1081)
```
No available information about the space usage.
```
MSK_RES_ERR_READ_FORMAT (1090)
```
The specified format cannot be read.
```
MSK_RES_ERR_MPS_FILE (1100)
```
An error occurred while reading an MPS file.
```
MSK_RES_ERR_MPS_INV_FIELD (1101)
```
A field in the MPS file is invalid. Probably it is too wide.
```
MSK_RES_ERR_MPS_INV_MARKER (1102)
```
An invalid marker has been specified in the MPS file.
```
MSK_RES_ERR_MPS_NULL_CON_NAME (1103)
```
An empty constraint name is used in an MPS file.
```
MSK_RES_ERR_MPS_NULL_VAR_NAME (1104)
```
An empty variable name is used in an MPS file.
```
MSK_RES_ERR_MPS_UNDEF_CON_NAME (1105)
```
An undefined constraint name occurred in an MPS file.
```
MSK_RES_ERR_MPS_UNDEF_VAR_NAME (1106)
```
An undefined variable name occurred in an MPS file.
```
MSK_RES_ERR_MPS_INV_CON_KEY (1107)
```
An invalid constraint key occurred in an MPS file.
```
MSK_RES_ERR_MPS_INV_BOUND_KEY (1108)
```
An invalid bound key occurred in an MPS file.
```
MSK_RES_ERR_MPS_INV_SEC_NAME (1109)
```
An invalid section name occurred in an MPS file.
```
MSK_RES_ERR_MPS_NO_OBJECTIVE (1110)
```
No objective is defined in an MPS file.
```
MSK_RES_ERR_MPS_SPLITTED_VAR (1111)
```
All elements in a column of the A matrix must be specified consecutively. Hence, it is illegal to specify non-zero elements in A for variable 1, then for variable 2 and then variable 1 again.
```
MSK_RES_ERR_MPS_MUL_CON_NAME (1112)
```
A constraint name was specified multiple times in the `ROWS` section.
```
MSK_RES_ERR_MPS_MUL_QSEC (1113)
```
Multiple `QSECTION`s are specified for a constraint in the MPS data file.
```
MSK_RES_ERR_MPS_MUL_QOBJ (1114)
```
The Q term in the objective is specified multiple times in the MPS data file.
```
MSK_RES_ERR_MPS_INV_SEC_ORDER (1115)
```
The sections in the MPS data file are not in the correct order.
```
MSK_RES_ERR_MPS_MUL_CSEC (1116)
```
Multiple `CSECTION`s are given the same name.
```
MSK_RES_ERR_MPS_CONE_TYPE (1117)
```
Invalid cone type specified in a `CSECTION`.
```
MSK_RES_ERR_MPS_CONE_OVERLAP (1118)
```
A variable is specified to be a member of several cones.
```
MSK_RES_ERR_MPS_CONE_REPEAT (1119)
```
A variable is repeated within the `CSECTION`.
```
MSK_RES_ERR_MPS_NON_SYMMETRIC_Q (1120)
```
A non symmetric matrix has been speciefied.
```
MSK_RES_ERR_MPS_DUPLICATE_Q_ELEMENT (1121)
```
Duplicate elements is specfied in a Q matrix.
```
MSK_RES_ERR_MPS_INVALID_OBJSENSE (1122)
```
An invalid objective sense is specified.
```
MSK_RES_ERR_MPS_TAB_IN_FIELD2 (1125)
```
A tab char occurred in field 2.
```
MSK_RES_ERR_MPS_TAB_IN_FIELD3 (1126)
```
A tab char occurred in field 3.
```
MSK_RES_ERR_MPS_TAB_IN_FIELD5 (1127)
```
A tab char occurred in field 5.

MSK_RES_ERR_MPS_INVALID_OBJ_NAME (1128)
An invalid objective name is specified.
MSK_RES_ERR_LP_INCOMPATIBLE (1150)
The problem cannot be written to an LP formatted file.
MSK_RES_ERR_LP_EMPTY (1151)
The problem cannot be written to an LP formatted file.
MSK_RES_ERR_LP_DUP_SLACK_NAME (1152)
The name of the slack variable added to a ranged constraint already exists.
MSK_RES_ERR_WRITE_MPS_INVALID_NAME (1153)
An invalid name is created while writing an MPS file. Usually this will make the MPS file unreadable.
MSK_RES_ERR_LP_INVALID_VAR_NAME (1154)
A variable name is invalid when used in an LP formatted file.
MSK_RES_ERR_LP_FREE_CONSTRAINT (1155)
Free constraints cannot be written in LP file format.
MSK_RES_ERR_WRITE_OPF_INVALID_VAR_NAME (1156)
Empty variable names cannot be written to OPF files.
MSK_RES_ERR_LP_FILE_FORMAT (1157)
Syntax error in an LP file.
MSK_RES_ERR_WRITE_LP_FORMAT (1158)
Problem cannot be written as an LP file.
MSK_RES_ERR_READ_LP_MISSING_END_TAG (1159)
Syntax error in LP file. Possibly missing End tag.
MSK_RES_ERR_LP_FORMAT (1160)
Syntax error in an LP file.
MSK_RES_ERR_WRITE_LP_NON_UNIQUE_NAME (1161)
An auto-generated name is not unique.
MSK_RES_ERR_READ_LP_NONEXISTING_NAME (1162)
A variable never occurred in objective or constraints.
MSK_RES_ERR_LP_WRITE_CONIC_PROBLEM (1163)
The problem contains cones that cannot be written to an LP formatted file.
MSK_RES_ERR_LP_WRITE_GECO_PROBLEM (1164)
The problem contains general convex terms that cannot be written to an LP formatted file.
MSK_RES_ERR_WRITING_FILE (1166)
An error occurred while writing file
MSK_RES_ERR_PTF_FORMAT (1167)
Syntax error in an PTF file
MSK_RES_ERR_OPF_FORMAT (1168)
Syntax error in an OPF file
MSK_RES_ERR_OPF_NEW_VARIABLE (1169)
Introducing new variables is now allowed. When a `[variables]` section is present, it is not allowed to introduce new variables later in the problem.
MSK_RES_ERR_INVALID_NAME_IN_SOL_FILE (1170)
An invalid name occurred in a solution file.
MSK_RES_ERR_LP_INVALID_CON_NAME (1171)
A constraint name is invalid when used in an LP formatted file.
MSK_RES_ERR_OPF_PREMATURE_EOF (1172)
Premature end of file in an OPF file.
MSK_RES_ERR_JSON_SYNTAX (1175)
Syntax error in an JSON data
MSK_RES_ERR_JSON_STRING (1176)
Error in JSON string.
MSK_RES_ERR_JSON_NUMBER_OVERFLOW (1177)
Invalid number entry - wrong type or value overflow.
MSK_RES_ERR_JSON_FORMAT (1178)
Error in an JSON Task file
MSK_RES_ERR_JSON_DATA (1179)
Inconsistent data in JSON Task file

MSK_RES_ERR_JSON_MISSING_DATA (1180)
  Missing data section in JSON task file.
MSK_RES_ERR_ARGUMENT_LENNEQ (1197)
  Incorrect length of arguments.
MSK_RES_ERR_ARGUMENT_TYPE (1198)
  Incorrect argument type.
MSK_RES_ERR_NUM_ARGUMENTS (1199)
  Incorrect number of function arguments.
MSK_RES_ERR_IN_ARGUMENT (1200)
  A function argument is incorrect.
MSK_RES_ERR_ARGUMENT_DIMENSION (1201)
  A function argument is of incorrect dimension.
MSK_RES_ERR_SHAPE_IS_TOO_LARGE (1202)
  The size of the n-dimensional shape is too large.
MSK_RES_ERR_INDEX_IS_TOO_SMALL (1203)
  An index in an argument is too small.
MSK_RES_ERR_INDEX_IS_TOO_LARGE (1204)
  An index in an argument is too large.
MSK_RES_ERR_PARAM_NAME (1205)
  The parameter name is not correct.
MSK_RES_ERR_PARAM_NAME_DOU (1206)
  The parameter name is not correct for a double parameter.
MSK_RES_ERR_PARAM_NAME_INT (1207)
  The parameter name is not correct for an integer parameter.
MSK_RES_ERR_PARAM_NAME_STR (1208)
  The parameter name is not correct for a string parameter.
MSK_RES_ERR_PARAM_INDEX (1210)
  Parameter index is out of range.
MSK_RES_ERR_PARAM_IS_TOO_LARGE (1215)
  The parameter value is too large.
MSK_RES_ERR_PARAM_IS_TOO_SMALL (1216)
  The parameter value is too small.
MSK_RES_ERR_PARAM_VALUE_STR (1217)
  The parameter value string is incorrect.
MSK_RES_ERR_PARAM_TYPE (1218)
  The parameter type is invalid.
MSK_RES_ERR_INF_DOU_INDEX (1219)
  A double information index is out of range for the specified type.
MSK_RES_ERR_INF_INT_INDEX (1220)
  An integer information index is out of range for the specified type.
MSK_RES_ERR_INDEX_ARR_IS_TOO_SMALL (1221)
  An index in an array argument is too small.
MSK_RES_ERR_INDEX_ARR_IS_TOO_LARGE (1222)
  An index in an array argument is too large.
MSK_RES_ERR_INF_LINT_INDEX (1225)
  A long integer information index is out of range for the specified type.
MSK_RES_ERR_ARG_IS_TOO_SMALL (1226)
  The value of a argument is too small.
MSK_RES_ERR_ARG_IS_TOO_LARGE (1227)
  The value of a argument is too large.
MSK_RES_ERR_INVALID_WHICHSOL (1228)
  `whichsol` is invalid.
MSK_RES_ERR_INF_DOU_NAME (1230)
  A double information name is invalid.
MSK_RES_ERR_INF_INT_NAME (1231)
  An integer information name is invalid.
MSK_RES_ERR_INF_TYPE (1232)
  The information type is invalid.

MSK_RES_ERR_INF_LINT_NAME (1234)

A long integer information name is invalid.

MSK_RES_ERR_INDEX (1235)

An index is out of range.

MSK_RES_ERR_WHICHSOL (1236)

The solution defined by `whichsol` does not exists.

MSK_RES_ERR_SOLITEM (1237)

The solution item number `solitem` is invalid. Please note that *MSK_SOL_ITEM_SNX* is invalid for the basic solution.

MSK_RES_ERR_WHICHITEM_NOT_ALLOWED (1238)

`whichitem` is unacceptable.

MSK_RES_ERR_MAXNUMCON (1240)

The maximum number of constraints specified is smaller than the number of constraints in the task.

MSK_RES_ERR_MAXNUMVAR (1241)

The maximum number of variables specified is smaller than the number of variables in the task.

MSK_RES_ERR_MAXNUMBARVAR (1242)

The maximum number of semidefinite variables specified is smaller than the number of semidefinite variables in the task.

MSK_RES_ERR_MAXNUMQNZ (1243)

The maximum number of non-zeros specified for the Q matrices is smaller than the number of non-zeros in the current Q matrices.

MSK_RES_ERR_TOO_SMALL_MAX_NUM_NZ (1245)

The maximum number of non-zeros specified is too small.

MSK_RES_ERR_INVALID_IDX (1246)

A specified index is invalid.

MSK_RES_ERR_INVALID_MAX_NUM (1247)

A specified index is invalid.

MSK_RES_ERR_NUMCONLIM (1250)

Maximum number of constraints limit is exceeded.

MSK_RES_ERR_NUMVARLIM (1251)

Maximum number of variables limit is exceeded.

MSK_RES_ERR_TOO_SMALL_MAXNUMANZ (1252)

The maximum number of non-zeros specified for A is smaller than the number of non-zeros in the current A.

MSK_RES_ERR_INV_APTRE (1253)

`aptre[j]` is strictly smaller than `aptrb[j]` for some j.

MSK_RES_ERR_MUL_A_ELEMENT (1254)

An element in A is defined multiple times.

MSK_RES_ERR_INV_BK (1255)

Invalid bound key.

MSK_RES_ERR_INV_BKC (1256)

Invalid bound key is specified for a constraint.

MSK_RES_ERR_INV_BKX (1257)

An invalid bound key is specified for a variable.

MSK_RES_ERR_INV_VAR_TYPE (1258)

An invalid variable type is specified for a variable.

MSK_RES_ERR_SOLVER_PROBTYPE (1259)

Problem type does not match the chosen optimizer.

MSK_RES_ERR_OBJECTIVE_RANGE (1260)

Empty objective range.

MSK_RES_ERR_UNDEF_SOLUTION (1265)

MOSEK has the following solution types:

- an interior-point solution,

- a basic solution,

- and an integer solution.

Each optimizer may set one or more of these solutions; e.g by default a successful optimization with the interior-point optimizer defines the interior-point solution and, for linear problems, also the basic solution. This error occurs when asking for a solution or for information about a solution that is not defined.

`MSK_RES_ERR_BASIS` (1266)

An invalid basis is specified. Either too many or too few basis variables are specified.

`MSK_RES_ERR_INV_SKC` (1267)

Invalid value in `skc`.

`MSK_RES_ERR_INV_SKX` (1268)

Invalid value in `skx`.

`MSK_RES_ERR_INV_SKN` (1274)

Invalid value in `skn`.

`MSK_RES_ERR_INV_SK_STR` (1269)

Invalid status key string encountered.

`MSK_RES_ERR_INV_SK` (1270)

Invalid status key code.

`MSK_RES_ERR_INV_CONE_TYPE_STR` (1271)

Invalid cone type string encountered.

`MSK_RES_ERR_INV_CONE_TYPE` (1272)

Invalid cone type code is encountered.

`MSK_RES_ERR_INVALID_SURPLUS` (1275)

Invalid surplus.

`MSK_RES_ERR_INV_NAME_ITEM` (1280)

An invalid name item code is used.

`MSK_RES_ERR_PRO_ITEM` (1281)

An invalid problem is used.

`MSK_RES_ERR_INVALID_FORMAT_TYPE` (1283)

Invalid format type.

`MSK_RES_ERR_FIRSTI` (1285)

Invalid `firsti`.

`MSK_RES_ERR_LASTI` (1286)

Invalid `lasti`.

`MSK_RES_ERR_FIRSTJ` (1287)

Invalid `firstj`.

`MSK_RES_ERR_LASTJ` (1288)

Invalid `lastj`.

`MSK_RES_ERR_MAX_LEN_IS_TOO_SMALL` (1289)

A maximum length that is too small has been specified.

`MSK_RES_ERR_NONLINEAR_EQUALITY` (1290)

The model contains a nonlinear equality which defines a nonconvex set.

`MSK_RES_ERR_NONCONVEX` (1291)

The optimization problem is nonconvex.

`MSK_RES_ERR_NONLINEAR_RANGED` (1292)

Nonlinear constraints with finite lower and upper bound always define a nonconvex feasible set.

`MSK_RES_ERR_CON_Q_NOT_PSD` (1293)

The quadratic constraint matrix is not positive semidefinite as expected for a constraint with finite upper bound. This results in a nonconvex problem. The parameter `MSK_DPAR_CHECK_CONVEXITY_REL_TOL` can be used to relax the convexity check.

`MSK_RES_ERR_CON_Q_NOT_NSD` (1294)

The quadratic constraint matrix is not negative semidefinite as expected for a constraint with finite lower bound. This results in a nonconvex problem. The parameter `MSK_DPAR_CHECK_CONVEXITY_REL_TOL` can be used to relax the convexity check.

`MSK_RES_ERR_OBJ_Q_NOT_PSD` (1295)

The quadratic coefficient matrix in the objective is not positive semidefinite as expected for a minimization problem. The parameter `MSK_DPAR_CHECK_CONVEXITY_REL_TOL` can be used to relax the convexity check.

`MSK_RES_ERR_OBJ_Q_NOT_NSD` (1296)

The quadratic coefficient matrix in the objective is not negative semidefinite as expected for a

maximization problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

MSK_RES_ERR_ARGUMENT_PERM_ARRAY (1299)

An invalid permutation array is specified.

MSK_RES_ERR_CONE_INDEX (1300)

An index of a non-existing cone has been specified.

MSK_RES_ERR_CONE_SIZE (1301)

A cone with incorrect number of members is specified.

MSK_RES_ERR_CONE_OVERLAP (1302)

One or more of the variables in the cone to be added is already member of another cone. Now assume the variable is x_j then add a new variable say x_k and the constraint

$$x_j = x_k$$

and then let x_k be member of the cone to be appended.

MSK_RES_ERR_CONE_REP_VAR (1303)

A variable is included multiple times in the cone.

MSK_RES_ERR_MAXNUMCONE (1304)

The value specified for `maxnumcone` is too small.

MSK_RES_ERR_CONE_TYPE (1305)

Invalid cone type specified.

MSK_RES_ERR_CONE_TYPE_STR (1306)

Invalid cone type specified.

MSK_RES_ERR_CONE_OVERLAP_APPEND (1307)

The cone to be appended has one variable which is already member of another cone.

MSK_RES_ERR_REMOVE_CONE_VARIABLE (1310)

A variable cannot be removed because it will make a cone invalid.

MSK_RES_ERR_APPENDING_TOO_BIG_CONE (1311)

Trying to append a too big cone.

MSK_RES_ERR_CONE_PARAMETER (1320)

An invalid cone parameter.

MSK_RES_ERR_SOL_FILE_INVALID_NUMBER (1350)

An invalid number is specified in a solution file.

MSK_RES_ERR_HUGE_C (1375)

A huge value in absolute size is specified for one c_j.

MSK_RES_ERR_HUGE_AIJ (1380)

A numerically huge value is specified for an $a_{i,j}$ element in A. The parameter *MSK_DPAR_DATA_TOL_AIJ_HUGE* controls when an $a_{i,j}$ is considered huge.

MSK_RES_ERR_DUPLICATE_AIJ (1385)

An element in the A matrix is specified twice.

MSK_RES_ERR_LOWER_BOUND_IS_A_NAN (1390)

The lower bound specified is not a number (nan).

MSK_RES_ERR_UPPER_BOUND_IS_A_NAN (1391)

The upper bound specified is not a number (nan).

MSK_RES_ERR_INFINITE_BOUND (1400)

A numerically huge bound value is specified.

MSK_RES_ERR_INV_QOBJ_SUBI (1401)

Invalid value in qosubi.

MSK_RES_ERR_INV_QOBJ_SUBJ (1402)

Invalid value in qosubj.

MSK_RES_ERR_INV_QOBJ_VAL (1403)

Invalid value in qoval.

MSK_RES_ERR_INV_QCON_SUBK (1404)

Invalid value in qcsubk.

MSK_RES_ERR_INV_QCON_SUBI (1405)

Invalid value in qcsubi.

MSK_RES_ERR_INV_QCON_SUBJ (1406)

Invalid value in qcsubj.

MSK_RES_ERR_INV_QCON_VAL (1407)

Invalid value in qcval.

MSK_RES_ERR_QCON_SUBI_TOO_SMALL (1408)

Invalid value in qcsubi.

MSK_RES_ERR_QCON_SUBI_TOO_LARGE (1409)

Invalid value in qcsubi.

MSK_RES_ERR_QOBJ_UPPER_TRIANGLE (1415)

An element in the upper triangle of Q^o is specified. Only elements in the lower triangle should be specified.

MSK_RES_ERR_QCON_UPPER_TRIANGLE (1417)

An element in the upper triangle of a Q^k is specified. Only elements in the lower triangle should be specified.

MSK_RES_ERR_FIXED_BOUND_VALUES (1420)

A fixed constraint/variable has been specified using the bound keys but the numerical value of the lower and upper bound is different.

MSK_RES_ERR_TOO_SMALL_A_TRUNCATION_VALUE (1421)

A too small value for the A trucation value is specified.

MSK_RES_ERR_INVALID_OBJECTIVE_SENSE (1445)

An invalid objective sense is specified.

MSK_RES_ERR_UNDEFINED_OBJECTIVE_SENSE (1446)

The objective sense has not been specified before the optimization.

MSK_RES_ERR_Y_IS_UNDEFINED (1449)

The solution item y is undefined.

MSK_RES_ERR_NAN_IN_DOUBLE_DATA (1450)

An invalid floating point value was used in some double data.

MSK_RES_ERR_NAN_IN_BLC (1461)

l^c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BUC (1462)

u^c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_C (1470)

c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BLX (1471)

l^x contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BUX (1472)

u^x contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_INVALID_AIJ (1473)

$a_{i,j}$ contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK_RES_ERR_SYM_MAT_INVALID (1480)

A symmetric matrix contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK_RES_ERR_SYM_MAT_HUGE (1482)

A symmetric matrix contains a huge value in absolute size. The parameter *MSK_DPAR_DATA_SYM_MAT_TOL_HUGE* controls when an $e_{i,j}$ is considered huge.

MSK_RES_ERR_INV_PROBLEM (1500)

Invalid problem type. Probably a nonconvex problem has been specified.

MSK_RES_ERR_MIXED_CONIC_AND_NL (1501)

The problem contains nonlinear terms conic constraints. The requested operation cannot be applied to this type of problem.

MSK_RES_ERR_GLOBAL_INV_CONIC_PROBLEM (1503)

The global optimizer can only be applied to problems without semidefinite variables.

MSK_RES_ERR_INV_OPTIMIZER (1550)

An invalid optimizer has been chosen for the problem.

MSK_RES_ERR_MIO_NO_OPTIMIZER (1551)

No optimizer is available for the current class of integer optimization problems.

MSK_RES_ERR_NO_OPTIMIZER_VAR_TYPE (1552)

No optimizer is available for this class of optimization problems.

MSK_RES_ERR_FINAL_SOLUTION (1560)

An error occurred during the solution finalization.

`MSK_RES_ERR_FIRST (1570)`

Invalid `first`.

`MSK_RES_ERR_LAST (1571)`

Invalid index `last`. A given index was out of expected range.

`MSK_RES_ERR_SLICE_SIZE (1572)`

Invalid slice size specified.

`MSK_RES_ERR_NEGATIVE_SURPLUS (1573)`

Negative surplus.

`MSK_RES_ERR_NEGATIVE_APPEND (1578)`

Cannot append a negative number.

`MSK_RES_ERR_POSTSOLVE (1580)`

An error occurred during the postsolve. Please contact **MOSEK** support.

`MSK_RES_ERR_OVERFLOW (1590)`

A computation produced an overflow i.e. a very large number.

`MSK_RES_ERR_NO_BASIS_SOL (1600)`

No basic solution is defined.

`MSK_RES_ERR_BASIS_FACTOR (1610)`

The factorization of the basis is invalid.

`MSK_RES_ERR_BASIS_SINGULAR (1615)`

The basis is singular and hence cannot be factored.

`MSK_RES_ERR_FACTOR (1650)`

An error occurred while factorizing a matrix.

`MSK_RES_ERR_FEASREPAIR_CANNOT_RELAX (1700)`

An optimization problem cannot be relaxed.

`MSK_RES_ERR_FEASREPAIR_SOLVING_RELAXED (1701)`

The relaxed problem could not be solved to optimality. Please consult the log file for further details.

`MSK_RES_ERR_FEASREPAIR_INCONSISTENT_BOUND (1702)`

The upper bound is less than the lower bound for a variable or a constraint. Please correct this before running the feasibility repair.

`MSK_RES_ERR_REPAIR_INVALID_PROBLEM (1710)`

The feasibility repair does not support the specified problem type.

`MSK_RES_ERR_REPAIR_OPTIMIZATION_FAILED (1711)`

Computation the optimal relaxation failed. The cause may have been numerical problems.

`MSK_RES_ERR_NAME_MAX_LEN (1750)`

A name is longer than the buffer that is supposed to hold it.

`MSK_RES_ERR_NAME_IS_NULL (1760)`

The name buffer is a NULL pointer.

`MSK_RES_ERR_INVALID_COMPRESSION (1800)`

Invalid compression type.

`MSK_RES_ERR_INVALID_IOMODE (1801)`

Invalid io mode.

`MSK_RES_ERR_NO_PRIMAL_INFEAS_CER (2000)`

A certificate of primal infeasibility is not available.

`MSK_RES_ERR_NO_DUAL_INFEAS_CER (2001)`

A certificate of infeasibility is not available.

`MSK_RES_ERR_NO_SOLUTION_IN_CALLBACK (2500)`

The required solution is not available.

`MSK_RES_ERR_INV_MARKI (2501)`

Invalid value in marki.

`MSK_RES_ERR_INV_MARKJ (2502)`

Invalid value in markj.

`MSK_RES_ERR_INV_NUMI (2503)`

Invalid numi.

`MSK_RES_ERR_INV_NUMJ (2504)`

Invalid numj.

`MSK_RES_ERR_TASK_INCOMPATIBLE (2560)`

The Task file is incompatible with this platform. This results from reading a file on a 32 bit platform generated on a 64 bit platform.

MSK_RES_ERR_TASK_INVALID (2561)
    The Task file is invalid.
MSK_RES_ERR_TASK_WRITE (2562)
    Failed to write the task file.
MSK_RES_ERR_LU_MAX_NUM_TRIES (2800)
    Could not compute the LU factors of the matrix within the maximum number of allowed tries.
MSK_RES_ERR_INVALID_UTF8 (2900)
    An invalid UTF8 string is encountered.
MSK_RES_ERR_INVALID_WCHAR (2901)
    An invalid wchar string is encountered.
MSK_RES_ERR_NO_DUAL_FOR_ITG_SOL (2950)
    No dual information is available for the integer solution.
MSK_RES_ERR_NO_SNX_FOR_BAS_SOL (2953)
    s_n^x is not available for the basis solution.
MSK_RES_ERR_INTERNAL (3000)
    An internal error occurred. Please report this problem.
MSK_RES_ERR_API_ARRAY_TOO_SMALL (3001)
    An input array was too short.
MSK_RES_ERR_API_CB_CONNECT (3002)
    Failed to connect a callback object.
MSK_RES_ERR_API_FATAL_ERROR (3005)
    An internal error occurred in the API. Please report this problem.
MSK_RES_ERR_API_INTERNAL (3999)
    An internal fatal error occurred in an interface function.
MSK_RES_ERR_SEN_FORMAT (3050)
    Syntax error in sensitivity analysis file.
MSK_RES_ERR_SEN_UNDEF_NAME (3051)
    An undefined name was encountered in the sensitivity analysis file.
MSK_RES_ERR_SEN_INDEX_RANGE (3052)
    Index out of range in the sensitivity analysis file.
MSK_RES_ERR_SEN_BOUND_INVALID_UP (3053)
    Analysis of upper bound requested for an index, where no upper bound exists.
MSK_RES_ERR_SEN_BOUND_INVALID_LO (3054)
    Analysis of lower bound requested for an index, where no lower bound exists.
MSK_RES_ERR_SEN_INDEX_INVALID (3055)
    Invalid range given in the sensitivity file.
MSK_RES_ERR_SEN_INVALID_REGEXP (3056)
    Syntax error in regexp or regexp longer than 1024.
MSK_RES_ERR_SEN_SOLUTION_STATUS (3057)
    No optimal solution found to the original problem given for sensitivity analysis.
MSK_RES_ERR_SEN_NUMERICAL (3058)
    Numerical difficulties encountered performing the sensitivity analysis.
MSK_RES_ERR_SEN_UNHANDLED_PROBLEM_TYPE (3080)
    Sensitivity analysis cannot be performed for the specified problem. Sensitivity analysis is only possible for linear problems.
MSK_RES_ERR_UNB_STEP_SIZE (3100)
    A step size in an optimizer was unexpectedly unbounded. For instance, if the step-size becomes unbounded in phase 1 of the simplex algorithm then an error occurs. Normally this will happen only if the problem is badly formulated. Please contact **MOSEK** support if this error occurs.
MSK_RES_ERR_IDENTICAL_TASKS (3101)
    Some tasks related to this function call were identical. Unique tasks were expected.
MSK_RES_ERR_AD_INVALID_CODELIST (3102)
    The code list data was invalid.
MSK_RES_ERR_INTERNAL_TEST_FAILED (3500)
    An internal unit test function failed.
MSK_RES_ERR_XML_INVALID_PROBLEM_TYPE (3600)
    The problem type is not supported by the XML format.

MSK_RES_ERR_INVALID_AMPL_STUB (3700)
Invalid AMPL stub.

MSK_RES_ERR_INT64_TO_INT32_CAST (3800)
A 64 bit integer could not be cast to a 32 bit integer.

MSK_RES_ERR_SIZE_LICENSE_NUMCORES (3900)
The computer contains more cpu cores than the license allows for.

MSK_RES_ERR_INFEAS_UNDEFINED (3910)
The requested value is not defined for this solution type.

MSK_RES_ERR_NO_BARX_FOR_SOLUTION (3915)
There is no $\overline{X}$ available for the solution specified. In particular note there are no $\overline{X}$ defined for the basic and integer solutions.

MSK_RES_ERR_NO_BARS_FOR_SOLUTION (3916)
There is no $\bar{s}$ available for the solution specified. In particular note there are no $\bar{s}$ defined for the basic and integer solutions.

MSK_RES_ERR_BAR_VAR_DIM (3920)
The dimension of a symmetric matrix variable has to be greater than 0.

MSK_RES_ERR_SYM_MAT_INVALID_ROW_INDEX (3940)
A row index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_INVALID_COL_INDEX (3941)
A column index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_NOT_LOWER_TRINGULAR (3942)
Only the lower triangular part of sparse symmetric matrix should be specified.

MSK_RES_ERR_SYM_MAT_INVALID_VALUE (3943)
The numerical value specified in a sparse symmetric matrix is not a floating point value.

MSK_RES_ERR_SYM_MAT_DUPLICATE (3944)
A value in a symmetric matric as been specified more than once.

MSK_RES_ERR_INVALID_SYM_MAT_DIM (3950)
A sparse symmetric matrix of invalid dimension is specified.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_SYM_MAT (4000)
The file format does not support a problem with symmetric matrix variables.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_CFIX (4001)
The file format does not support a problem with nonzero fixed term in c.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_RANGED_CONSTRAINTS (4002)
The file format does not support a problem with ranged constraints.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_FREE_CONSTRAINTS (4003)
The file format does not support a problem with free constraints.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_CONES (4005)
The file format does not support a problem with conic constraints.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_NONLINEAR (4010)
The file format does not support a problem with nonlinear terms.

MSK_RES_ERR_DUPLICATE_CONSTRAINT_NAMES (4500)
Two constraint names are identical.

MSK_RES_ERR_DUPLICATE_VARIABLE_NAMES (4501)
Two variable names are identical.

MSK_RES_ERR_DUPLICATE_BARVARIABLE_NAMES (4502)
Two barvariable names are identical.

MSK_RES_ERR_DUPLICATE_CONE_NAMES (4503)
Two cone names are identical.

MSK_RES_ERR_NON_UNIQUE_ARRAY (5000)
An array does not contain unique elements.

MSK_RES_ERR_ARGUMENT_IS_TOO_LARGE (5005)
The value of a function argument is too large.

MSK_RES_ERR_MIO_INTERNAL (5010)
A fatal error occurred in the mixed integer optimizer. Please contact **MOSEK** support.

MSK_RES_ERR_INVALID_PROBLEM_TYPE (6000)
An invalid problem type.

MSK_RES_ERR_UNHANDLED_SOLUTION_STATUS (6010)
Unhandled solution status.

`MSK_RES_ERR_UPPER_TRIANGLE (6020)`

An element in the upper triangle of a lower triangular matrix is specified.

`MSK_RES_ERR_LAU_SINGULAR_MATRIX (7000)`

A matrix is singular.

`MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE (7001)`

A matrix is not positive definite.

`MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX (7002)`

An invalid lower triangular matrix.

`MSK_RES_ERR_LAU_UNKNOWN (7005)`

An unknown error.

`MSK_RES_ERR_LAU_ARG_M (7010)`

Invalid argument m.

`MSK_RES_ERR_LAU_ARG_N (7011)`

Invalid argument n.

`MSK_RES_ERR_LAU_ARG_K (7012)`

Invalid argument k.

`MSK_RES_ERR_LAU_ARG_TRANSA (7015)`

Invalid argument transa.

`MSK_RES_ERR_LAU_ARG_TRANSB (7016)`

Invalid argument transb.

`MSK_RES_ERR_LAU_ARG_UPLO (7017)`

Invalid argument uplo.

`MSK_RES_ERR_LAU_ARG_TRANS (7018)`

Invalid argument trans.

`MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX (7019)`

An invalid sparse symmetric matrix is specfified. Note only the lower triangular part with no duplicates is specifed.

`MSK_RES_ERR_CBF_PARSE (7100)`

An error occurred while parsing an CBF file.

`MSK_RES_ERR_CBF_OBJ_SENSE (7101)`

An invalid objective sense is specified.

`MSK_RES_ERR_CBF_NO_VARIABLES (7102)`

No variables are specified.

`MSK_RES_ERR_CBF_TOO_MANY_CONSTRAINTS (7103)`

Too many constraints specified.

`MSK_RES_ERR_CBF_TOO_MANY_VARIABLES (7104)`

Too many variables specified.

`MSK_RES_ERR_CBF_NO_VERSION_SPECIFIED (7105)`

No version specified.

`MSK_RES_ERR_CBF_SYNTAX (7106)`

Invalid syntax.

`MSK_RES_ERR_CBF_DUPLICATE_OBJ (7107)`

Duplicate OBJ keyword.

`MSK_RES_ERR_CBF_DUPLICATE_CON (7108)`

Duplicate CON keyword.

`MSK_RES_ERR_CBF_DUPLICATE_VAR (7109)`

Duplicate VAR keyword.

`MSK_RES_ERR_CBF_DUPLICATE_INT (7110)`

Duplicate INT keyword.

`MSK_RES_ERR_CBF_INVALID_VAR_TYPE (7111)`

Invalid variable type.

`MSK_RES_ERR_CBF_INVALID_CON_TYPE (7112)`

Invalid constraint type.

`MSK_RES_ERR_CBF_INVALID_DOMAIN_DIMENSION (7113)`

Invalid domain dimension.

`MSK_RES_ERR_CBF_DUPLICATE_OBJACOORD (7114)`

Duplicate index in OBJCOORD.

MSK_RES_ERR_CBF_DUPLICATE_BCOORD (7115)
    Duplicate index in BCOORD.
MSK_RES_ERR_CBF_DUPLICATE_ACOORD (7116)
    Duplicate index in ACOORD.
MSK_RES_ERR_CBF_TOO_FEW_VARIABLES (7117)
    Too few variables defined.
MSK_RES_ERR_CBF_TOO_FEW_CONSTRAINTS (7118)
    Too few constraints defined.
MSK_RES_ERR_CBF_TOO_FEW_INTS (7119)
    Too few ints are specified.
MSK_RES_ERR_CBF_TOO_MANY_INTS (7120)
    Too many ints are specified.
MSK_RES_ERR_CBF_INVALID_INT_INDEX (7121)
    Invalid INT index.
MSK_RES_ERR_CBF_UNSUPPORTED (7122)
    Unsupported feature is present.
MSK_RES_ERR_CBF_DUPLICATE_PSDVAR (7123)
    Duplicate PSDVAR keyword.
MSK_RES_ERR_CBF_INVALID_PSDVAR_DIMENSION (7124)
    Invalid PSDVAR dimension.
MSK_RES_ERR_CBF_TOO_FEW_PSDVAR (7125)
    Too few variables defined.
MSK_RES_ERR_CBF_INVALID_EXP_DIMENSION (7126)
    Invalid dimension of a exponential cone.
MSK_RES_ERR_CBF_DUPLICATE_POW_CONES (7130)
    Multiple POWCONES specified.
MSK_RES_ERR_CBF_DUPLICATE_POW_STAR_CONES (7131)
    Multiple POW*CONES specified.
MSK_RES_ERR_CBF_INVALID_POWER (7132)
    Invalid power specified.
MSK_RES_ERR_CBF_POWER_CONE_IS_TOO_LONG (7133)
    Power cone is too long.
MSK_RES_ERR_CBF_INVALID_POWER_CONE_INDEX (7134)
    Invalid power cone index.
MSK_RES_ERR_CBF_INVALID_POWER_STAR_CONE_INDEX (7135)
    Invalid power star cone index.
MSK_RES_ERR_CBF_UNHANDLED_POWER_CONE_TYPE (7136)
    An unhandled power cone type.
MSK_RES_ERR_CBF_UNHANDLED_POWER_STAR_CONE_TYPE (7137)
    An unhandled power star cone type.
MSK_RES_ERR_CBF_POWER_CONE_MISMATCH (7138)
    The power cone does not match with it definition.
MSK_RES_ERR_CBF_POWER_STAR_CONE_MISMATCH (7139)
    The power star cone does not match with it definition.
MSK_RES_ERR_CBF_INVALID_NUMBER_OF_CONES (7740)
    Invalid number of cones.
MSK_RES_ERR_CBF_INVALID_DIMENSION_OF_CONES (7741)
    Invalid dimension of cones.
MSK_RES_ERR_MIO_INVALID_ROOT_OPTIMIZER (7700)
    An invalid root optimizer was selected for the problem type.
MSK_RES_ERR_MIO_INVALID_NODE_OPTIMIZER (7701)
    An invalid node optimizer was selected for the problem type.
MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD (7800)
    The matrix defining the quadratric part of constraint is not positive semidefinite.
MSK_RES_ERR_TOCONIC_CONSTRAINT_FX (7801)
    The quadratic constraint is an equality, thus not convex.
MSK_RES_ERR_TOCONIC_CONSTRAINT_RA (7802)
    The quadratic constraint has finite lower and upper bound, and therefore it is not convex.

`MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC (7803)`
    The constraint is not conic representable.
`MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD (7804)`
    The matrix defining the quadratric part of the objective function is not positive semidefinite.
`MSK_RES_ERR_SERVER_CONNECT (8000)`
    Failed to connect to remote solver server. The server string or the port string were invalid, or the server did not accept connection.
`MSK_RES_ERR_SERVER_PROTOCOL (8001)`
    Unexpected message or data from solver server.
`MSK_RES_ERR_SERVER_STATUS (8002)`
    Server returned non-ok HTTP status code
`MSK_RES_ERR_SERVER_TOKEN (8003)`
    The job ID specified is incorrect or invalid

11.4 Constants

11.4.1 Basis identification

`MSK_BI_NEVER`
    Never do basis identification.
`MSK_BI_ALWAYS`
    Basis identification is always performed even if the interior-point optimizer terminates abnormally.
`MSK_BI_NO_ERROR`
    Basis identification is performed if the interior-point optimizer terminates without an error.
`MSK_BI_IF_FEASIBLE`
    Basis identification is not performed if the interior-point optimizer terminates with a problem status saying that the problem is primal or dual infeasible.
`MSK_BI_RESERVERED`
    Not currently in use.

11.4.2 Bound keys

`MSK_BK_LO`
    The constraint or variable has a finite lower bound and an infinite upper bound.
`MSK_BK_UP`
    The constraint or variable has an infinite lower bound and an finite upper bound.
`MSK_BK_FX`
    The constraint or variable is fixed.
`MSK_BK_FR`
    The constraint or variable is free.
`MSK_BK_RA`
    The constraint or variable is ranged.

11.4.3 Mark

`MSK_MARK_LO`
    The lower bound is selected for sensitivity analysis.
`MSK_MARK_UP`
    The upper bound is selected for sensitivity analysis.

11.4.4 Degeneracy strategies

`MSK_SIM_DEGEN_NONE`
    The simplex optimizer should use no degeneration strategy.
`MSK_SIM_DEGEN_FREE`
    The simplex optimizer chooses the degeneration strategy.
`MSK_SIM_DEGEN_AGGRESSIVE`
    The simplex optimizer should use an aggressive degeneration strategy.

```
MSK_SIM_DEGEN_MODERATE
```
        The simplex optimizer should use a moderate degeneration strategy.
```
MSK_SIM_DEGEN_MINIMUM
```
        The simplex optimizer should use a minimum degeneration strategy.

11.4.5 Transposed matrix.

```
MSK_TRANSPOSE_NO
```
        No transpose is applied.
```
MSK_TRANSPOSE_YES
```
        A transpose is applied.

11.4.6 Triangular part of a symmetric matrix.

```
MSK_UPLO_LO
```
        Lower part.
```
MSK_UPLO_UP
```
        Upper part.

11.4.7 Problem reformulation.

```
MSK_SIM_REFORMULATION_ON
```
        Allow the simplex optimizer to reformulate the problem.
```
MSK_SIM_REFORMULATION_OFF
```
        Disallow the simplex optimizer to reformulate the problem.
```
MSK_SIM_REFORMULATION_FREE
```
        The simplex optimizer can choose freely.
```
MSK_SIM_REFORMULATION_AGGRESSIVE
```
        The simplex optimizer should use an aggressive reformulation strategy.

11.4.8 Exploit duplicate columns.

```
MSK_SIM_EXPLOIT_DUPVEC_ON
```
        Allow the simplex optimizer to exploit duplicated columns.
```
MSK_SIM_EXPLOIT_DUPVEC_OFF
```
        Disallow the simplex optimizer to exploit duplicated columns.
```
MSK_SIM_EXPLOIT_DUPVEC_FREE
```
        The simplex optimizer can choose freely.

11.4.9 Hot-start type employed by the simplex optimizer

```
MSK_SIM_HOTSTART_NONE
```
        The simplex optimizer performs a coldstart.
```
MSK_SIM_HOTSTART_FREE
```
        The simplex optimize chooses the hot-start type.
```
MSK_SIM_HOTSTART_STATUS_KEYS
```
        Only the status keys of the constraints and variables are used to choose the type of hot-start.

11.4.10 Hot-start type employed by the interior-point optimizers.

```
MSK_INTPNT_HOTSTART_NONE
```
        The interior-point optimizer performs a coldstart.
```
MSK_INTPNT_HOTSTART_PRIMAL
```
        The interior-point optimizer exploits the primal solution only.
```
MSK_INTPNT_HOTSTART_DUAL
```
        The interior-point optimizer exploits the dual solution only.
```
MSK_INTPNT_HOTSTART_PRIMAL_DUAL
```
        The interior-point optimizer exploits both the primal and dual solution.

11.4.11 Solution purification employed optimizer.

MSK_PURIFY_NONE
  The optimizer performs no solution purification.
MSK_PURIFY_PRIMAL
  The optimizer purifies the primal solution.
MSK_PURIFY_DUAL
  The optimizer purifies the dual solution.
MSK_PURIFY_PRIMAL_DUAL
  The optimizer purifies both the primal and dual solution.
MSK_PURIFY_AUTO
  TBD

11.4.12 Progress callback codes

MSK_CALLBACK_BEGIN_BI
  The basis identification procedure has been started.
MSK_CALLBACK_BEGIN_CONIC
  The callback function is called when the conic optimizer is started.
MSK_CALLBACK_BEGIN_DUAL_BI
  The callback function is called from within the basis identification procedure when the dual phase
  is started.
MSK_CALLBACK_BEGIN_DUAL_SENSITIVITY
  Dual sensitivity analysis is started.
MSK_CALLBACK_BEGIN_DUAL_SETUP_BI
  The callback function is called when the dual BI phase is started.
MSK_CALLBACK_BEGIN_DUAL_SIMPLEX
  The callback function is called when the dual simplex optimizer started.
MSK_CALLBACK_BEGIN_DUAL_SIMPLEX_BI
  The callback function is called from within the basis identification procedure when the dual simplex
  clean-up phase is started.
MSK_CALLBACK_BEGIN_FULL_CONVEXITY_CHECK
  Begin full convexity check.
MSK_CALLBACK_BEGIN_INFEAS_ANA
  The callback function is called when the infeasibility analyzer is started.
MSK_CALLBACK_BEGIN_INTPNT
  The callback function is called when the interior-point optimizer is started.
MSK_CALLBACK_BEGIN_LICENSE_WAIT
  Begin waiting for license.
MSK_CALLBACK_BEGIN_MIO
  The callback function is called when the mixed-integer optimizer is started.
MSK_CALLBACK_BEGIN_OPTIMIZER
  The callback function is called when the optimizer is started.
MSK_CALLBACK_BEGIN_PRESOLVE
  The callback function is called when the presolve is started.
MSK_CALLBACK_BEGIN_PRIMAL_BI
  The callback function is called from within the basis identification procedure when the primal phase
  is started.
MSK_CALLBACK_BEGIN_PRIMAL_REPAIR
  Begin primal feasibility repair.
MSK_CALLBACK_BEGIN_PRIMAL_SENSITIVITY
  Primal sensitivity analysis is started.
MSK_CALLBACK_BEGIN_PRIMAL_SETUP_BI
  The callback function is called when the primal BI setup is started.
MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX
  The callback function is called when the primal simplex optimizer is started.
MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX_BI
  The callback function is called from within the basis identification procedure when the primal
  simplex clean-up phase is started.

MSK_CALLBACK_BEGIN_QCQO_REFORMULATE
    Begin QCQO reformulation.
MSK_CALLBACK_BEGIN_READ
    MOSEK has started reading a problem file.
MSK_CALLBACK_BEGIN_ROOT_CUTGEN
    The callback function is called when root cut generation is started.
MSK_CALLBACK_BEGIN_SIMPLEX
    The callback function is called when the simplex optimizer is started.
MSK_CALLBACK_BEGIN_SIMPLEX_BI
    The callback function is called from within the basis identification procedure when the simplex clean-up phase is started.
MSK_CALLBACK_BEGIN_TO_CONIC
    Begin conic reformulation.
MSK_CALLBACK_BEGIN_WRITE
    MOSEK has started writing a problem file.
MSK_CALLBACK_CONIC
    The callback function is called from within the conic optimizer after the information database has been updated.
MSK_CALLBACK_DUAL_SIMPLEX
    The callback function is called from within the dual simplex optimizer.
MSK_CALLBACK_END_BI
    The callback function is called when the basis identification procedure is terminated.
MSK_CALLBACK_END_CONIC
    The callback function is called when the conic optimizer is terminated.
MSK_CALLBACK_END_DUAL_BI
    The callback function is called from within the basis identification procedure when the dual phase is terminated.
MSK_CALLBACK_END_DUAL_SENSITIVITY
    Dual sensitivity analysis is terminated.
MSK_CALLBACK_END_DUAL_SETUP_BI
    The callback function is called when the dual BI phase is terminated.
MSK_CALLBACK_END_DUAL_SIMPLEX
    The callback function is called when the dual simplex optimizer is terminated.
MSK_CALLBACK_END_DUAL_SIMPLEX_BI
    The callback function is called from within the basis identification procedure when the dual clean-up phase is terminated.
MSK_CALLBACK_END_FULL_CONVEXITY_CHECK
    End full convexity check.
MSK_CALLBACK_END_INFEAS_ANA
    The callback function is called when the infeasibility analyzer is terminated.
MSK_CALLBACK_END_INTPNT
    The callback function is called when the interior-point optimizer is terminated.
MSK_CALLBACK_END_LICENSE_WAIT
    End waiting for license.
MSK_CALLBACK_END_MIO
    The callback function is called when the mixed-integer optimizer is terminated.
MSK_CALLBACK_END_OPTIMIZER
    The callback function is called when the optimizer is terminated.
MSK_CALLBACK_END_PRESOLVE
    The callback function is called when the presolve is completed.
MSK_CALLBACK_END_PRIMAL_BI
    The callback function is called from within the basis identification procedure when the primal phase is terminated.
MSK_CALLBACK_END_PRIMAL_REPAIR
    End primal feasibility repair.
MSK_CALLBACK_END_PRIMAL_SENSITIVITY
    Primal sensitivity analysis is terminated.

`MSK_CALLBACK_END_PRIMAL_SETUP_BI`
> The callback function is called when the primal BI setup is terminated.

`MSK_CALLBACK_END_PRIMAL_SIMPLEX`
> The callback function is called when the primal simplex optimizer is terminated.

`MSK_CALLBACK_END_PRIMAL_SIMPLEX_BI`
> The callback function is called from within the basis identification procedure when the primal clean-up phase is terminated.

`MSK_CALLBACK_END_QCQO_REFORMULATE`
> End QCQO reformulation.

`MSK_CALLBACK_END_READ`
> **MOSEK** has finished reading a problem file.

`MSK_CALLBACK_END_ROOT_CUTGEN`
> The callback function is called when root cut generation is terminated.

`MSK_CALLBACK_END_SIMPLEX`
> The callback function is called when the simplex optimizer is terminated.

`MSK_CALLBACK_END_SIMPLEX_BI`
> The callback function is called from within the basis identification procedure when the simplex clean-up phase is terminated.

`MSK_CALLBACK_END_TO_CONIC`
> End conic reformulation.

`MSK_CALLBACK_END_WRITE`
> **MOSEK** has finished writing a problem file.

`MSK_CALLBACK_IM_BI`
> The callback function is called from within the basis identification procedure at an intermediate point.

`MSK_CALLBACK_IM_CONIC`
> The callback function is called at an intermediate stage within the conic optimizer where the information database has not been updated.

`MSK_CALLBACK_IM_DUAL_BI`
> The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

`MSK_CALLBACK_IM_DUAL_SENSIVITY`
> The callback function is called at an intermediate stage of the dual sensitivity analysis.

`MSK_CALLBACK_IM_DUAL_SIMPLEX`
> The callback function is called at an intermediate point in the dual simplex optimizer.

`MSK_CALLBACK_IM_FULL_CONVEXITY_CHECK`
> The callback function is called at an intermediate stage of the full convexity check.

`MSK_CALLBACK_IM_INTPNT`
> The callback function is called at an intermediate stage within the interior-point optimizer where the information database has not been updated.

`MSK_CALLBACK_IM_LICENSE_WAIT`
> **MOSEK** is waiting for a license.

`MSK_CALLBACK_IM_LU`
> The callback function is called from within the LU factorization procedure at an intermediate point.

`MSK_CALLBACK_IM_MIO`
> The callback function is called at an intermediate point in the mixed-integer optimizer.

`MSK_CALLBACK_IM_MIO_DUAL_SIMPLEX`
> The callback function is called at an intermediate point in the mixed-integer optimizer while running the dual simplex optimizer.

`MSK_CALLBACK_IM_MIO_INTPNT`
> The callback function is called at an intermediate point in the mixed-integer optimizer while running the interior-point optimizer.

`MSK_CALLBACK_IM_MIO_PRIMAL_SIMPLEX`
> The callback function is called at an intermediate point in the mixed-integer optimizer while running the primal simplex optimizer.

`MSK_CALLBACK_IM_ORDER`
> The callback function is called from within the matrix ordering procedure at an intermediate point.

`MSK_CALLBACK_IM_PRESOLVE`
>   The callback function is called from within the presolve procedure at an intermediate stage.

`MSK_CALLBACK_IM_PRIMAL_BI`
>   The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

`MSK_CALLBACK_IM_PRIMAL_SENSIVITY`
>   The callback function is called at an intermediate stage of the primal sensitivity analysis.

`MSK_CALLBACK_IM_PRIMAL_SIMPLEX`
>   The callback function is called at an intermediate point in the primal simplex optimizer.

`MSK_CALLBACK_IM_QO_REFORMULATE`
>   The callback function is called at an intermediate stage of the conic quadratic reformulation.

`MSK_CALLBACK_IM_READ`
>   Intermediate stage in reading.

`MSK_CALLBACK_IM_ROOT_CUTGEN`
>   The callback is called from within root cut generation at an intermediate stage.

`MSK_CALLBACK_IM_SIMPLEX`
>   The callback function is called from within the simplex optimizer at an intermediate point.

`MSK_CALLBACK_IM_SIMPLEX_BI`
>   The callback function is called from within the basis identification procedure at an intermediate point in the simplex clean-up phase. The frequency of the callbacks is controlled by the `MSK_IPAR_LOG_SIM_FREQ` parameter.

`MSK_CALLBACK_INTPNT`
>   The callback function is called from within the interior-point optimizer after the information database has been updated.

`MSK_CALLBACK_NEW_INT_MIO`
>   The callback function is called after a new integer solution has been located by the mixed-integer optimizer.

`MSK_CALLBACK_PRIMAL_SIMPLEX`
>   The callback function is called from within the primal simplex optimizer.

`MSK_CALLBACK_READ_OPF`
>   The callback function is called from the OPF reader.

`MSK_CALLBACK_READ_OPF_SECTION`
>   A chunk of Q non-zeros has been read from a problem file.

`MSK_CALLBACK_SOLVING_REMOTE`
>   The callback function is called while the task is being solved on a remote server.

`MSK_CALLBACK_UPDATE_DUAL_BI`
>   The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

`MSK_CALLBACK_UPDATE_DUAL_SIMPLEX`
>   The callback function is called in the dual simplex optimizer.

`MSK_CALLBACK_UPDATE_DUAL_SIMPLEX_BI`
>   The callback function is called from within the basis identification procedure at an intermediate point in the dual simplex clean-up phase. The frequency of the callbacks is controlled by the `MSK_IPAR_LOG_SIM_FREQ` parameter.

`MSK_CALLBACK_UPDATE_PRESOLVE`
>   The callback function is called from within the presolve procedure.

`MSK_CALLBACK_UPDATE_PRIMAL_BI`
>   The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

`MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX`
>   The callback function is called in the primal simplex optimizer.

`MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX_BI`
>   The callback function is called from within the basis identification procedure at an intermediate point in the primal simplex clean-up phase. The frequency of the callbacks is controlled by the `MSK_IPAR_LOG_SIM_FREQ` parameter.

`MSK_CALLBACK_WRITE_OPF`
>   The callback function is called from the OPF writer.

11.4.13 Types of convexity checks.

`MSK_CHECK_CONVEXITY_NONE`
 No convexity check.
`MSK_CHECK_CONVEXITY_SIMPLE`
 Perform simple and fast convexity check.
`MSK_CHECK_CONVEXITY_FULL`
 Perform a full convexity check.

11.4.14 Compression types

`MSK_COMPRESS_NONE`
 No compression is used.
`MSK_COMPRESS_FREE`
 The type of compression used is chosen automatically.
`MSK_COMPRESS_GZIP`
 The type of compression used is gzip compatible.
`MSK_COMPRESS_ZSTD`
 The type of compression used is zstd compatible.

11.4.15 Cone types

`MSK_CT_QUAD`
 The cone is a quadratic cone.
`MSK_CT_RQUAD`
 The cone is a rotated quadratic cone.
`MSK_CT_PEXP`
 A primal exponential cone.
`MSK_CT_DEXP`
 A dual exponential cone.
`MSK_CT_PPOW`
 A primal power cone.
`MSK_CT_DPOW`
 A dual power cone.
`MSK_CT_ZERO`
 The zero cone.

11.4.16 Name types

`MSK_NAME_TYPE_GEN`
 General names. However, no duplicate and blank names are allowed.
`MSK_NAME_TYPE_MPS`
 MPS type names.
`MSK_NAME_TYPE_LP`
 LP type names.

11.4.17 SCopt operator types

`MSK_OPR_ENT`
 Entropy
`MSK_OPR_EXP`
 Exponential
`MSK_OPR_LOG`
 Logarithm
`MSK_OPR_POW`
 Power
`MSK_OPR_SQRT`
 Square root

11.4.18 Cone types

MSK_SYMMAT_TYPE_SPARSE
> Sparse symmetric matrix.

11.4.19 Data format types

MSK_DATA_FORMAT_EXTENSION
> The file extension is used to determine the data file format.

MSK_DATA_FORMAT_MPS
> The data file is MPS formatted.

MSK_DATA_FORMAT_LP
> The data file is LP formatted.

MSK_DATA_FORMAT_OP
> The data file is an optimization problem formatted file.

MSK_DATA_FORMAT_FREE_MPS
> The data a free MPS formatted file.

MSK_DATA_FORMAT_TASK
> Generic task dump file.

MSK_DATA_FORMAT_PTF
> (P)retty (T)ext (F)format.

MSK_DATA_FORMAT_CB
> Conic benchmark format,

MSK_DATA_FORMAT_JSON_TASK
> JSON based task format.

11.4.20 Double information items

MSK_DINF_BI_CLEAN_DUAL_TIME
> Time spent within the dual clean-up optimizer of the basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_PRIMAL_TIME
> Time spent within the primal clean-up optimizer of the basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_TIME
> Time spent within the clean-up phase of the basis identification procedure since its invocation.

MSK_DINF_BI_DUAL_TIME
> Time spent within the dual phase basis identification procedure since its invocation.

MSK_DINF_BI_PRIMAL_TIME
> Time spent within the primal phase of the basis identification procedure since its invocation.

MSK_DINF_BI_TIME
> Time spent within the basis identification procedure since its invocation.

MSK_DINF_INTPNT_DUAL_FEAS
> Dual feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure is not directly related to the original problem because a homogeneous model is employed.)

MSK_DINF_INTPNT_DUAL_OBJ
> Dual objective value reported by the interior-point optimizer.

MSK_DINF_INTPNT_FACTOR_NUM_FLOPS
> An estimate of the number of flops used in the factorization.

MSK_DINF_INTPNT_OPT_STATUS
> A measure of optimality of the solution. It should converge to $+1$ if the problem has a primal-dual optimal solution, and converge to -1 if the problem is (strictly) primal or dual infeasible. If the measure converges to another constant, or fails to settle, the problem is usually ill-posed.

MSK_DINF_INTPNT_ORDER_TIME
> Order time (in seconds).

MSK_DINF_INTPNT_PRIMAL_FEAS

Primal feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure is not directly related to the original problem because a homogeneous model is employed).

MSK_DINF_INTPNT_PRIMAL_OBJ

Primal objective value reported by the interior-point optimizer.

MSK_DINF_INTPNT_TIME

Time spent within the interior-point optimizer since its invocation.

MSK_DINF_MIO_CLIQUE_SEPARATION_TIME

Separation time for clique cuts.

MSK_DINF_MIO_CMIR_SEPARATION_TIME

Separation time for CMIR cuts.

MSK_DINF_MIO_CONSTRUCT_SOLUTION_OBJ

If **MOSEK** has successfully constructed an integer feasible solution, then this item contains the optimal objective value corresponding to the feasible solution.

MSK_DINF_MIO_DUAL_BOUND_AFTER_PRESOLVE

Value of the dual bound after presolve but before cut generation.

MSK_DINF_MIO_GMI_SEPARATION_TIME

Separation time for GMI cuts.

MSK_DINF_MIO_IMPLIED_BOUND_TIME

Separation time for implied bound cuts.

MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME

Separation time for knapsack cover.

MSK_DINF_MIO_OBJ_ABS_GAP

Given the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the absolute gap defined by

$$|(\text{objective value of feasible solution}) - (\text{objective bound})|.$$

Otherwise it has the value -1.0.

MSK_DINF_MIO_OBJ_BOUND

The best known bound on the objective function. This value is undefined until at least one relaxation has been solved: To see if this is the case check that *MSK_IINF_MIO_NUM_RELAX* is strictly positive.

MSK_DINF_MIO_OBJ_INT

The primal objective value corresponding to the best integer feasible solution. Please note that at least one integer feasible solution must have been located i.e. check *MSK_IINF_MIO_NUM_INT_SOLUTIONS*.

MSK_DINF_MIO_OBJ_REL_GAP

Given that the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the relative gap defined by

$$\frac{|(\text{objective value of feasible solution}) - (\text{objective bound})|}{\max(\delta, |(\text{objective value of feasible solution})|)}.$$

where δ is given by the parameter *MSK_DPAR_MIO_REL_GAP_CONST*. Otherwise it has the value -1.0.

MSK_DINF_MIO_PROBING_TIME

Total time for probing.

MSK_DINF_MIO_ROOT_CUTGEN_TIME

Total time for cut generation.

MSK_DINF_MIO_ROOT_OPTIMIZER_TIME

Time spent in the optimizer while solving the root node relaxation

MSK_DINF_MIO_ROOT_PRESOLVE_TIME

Time spent presolving the problem at the root node.

MSK_DINF_MIO_TIME

Time spent in the mixed-integer optimizer.

MSK_DINF_MIO_USER_OBJ_CUT

If the objective cut is used, then this information item has the value of the cut.

MSK_DINF_OPTIMIZER_TIME
    Total time spent in the optimizer since it was invoked.
MSK_DINF_PRESOLVE_ELI_TIME
    Total time spent in the eliminator since the presolve was invoked.
MSK_DINF_PRESOLVE_LINDEP_TIME
    Total time spent in the linear dependency checker since the presolve was invoked.
MSK_DINF_PRESOLVE_TIME
    Total time (in seconds) spent in the presolve since it was invoked.
MSK_DINF_PRIMAL_REPAIR_PENALTY_OBJ
    The optimal objective value of the penalty function.
MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION
    Maximum absolute diagonal perturbation occurring during the QCQO reformulation.
MSK_DINF_QCQO_REFORMULATE_TIME
    Time spent with conic quadratic reformulation.
MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING
    Worst Cholesky column scaling.
MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING
    Worst Cholesky diagonal scaling.
MSK_DINF_RD_TIME
    Time spent reading the data file.
MSK_DINF_SIM_DUAL_TIME
    Time spent in the dual simplex optimizer since invoking it.
MSK_DINF_SIM_FEAS
    Feasibility measure reported by the simplex optimizer.
MSK_DINF_SIM_OBJ
    Objective value reported by the simplex optimizer.
MSK_DINF_SIM_PRIMAL_TIME
    Time spent in the primal simplex optimizer since invoking it.
MSK_DINF_SIM_TIME
    Time spent in the simplex optimizer since invoking it.
MSK_DINF_SOL_BAS_DUAL_OBJ
    Dual objective value of the basic solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .
MSK_DINF_SOL_BAS_DVIOLCON
    Maximal dual bound violation for x^c in the basic solution. Updated if
    MSK_IPAR_AUTO_UPDATE_SOL_INFO is set .
MSK_DINF_SOL_BAS_DVIOLVAR
    Maximal dual bound violation for x^x in the basic solution. Updated if
    MSK_IPAR_AUTO_UPDATE_SOL_INFO is set .
MSK_DINF_SOL_BAS_NRM_BARX
    Infinity norm of $\overline{X}$ in the basic solution.
MSK_DINF_SOL_BAS_NRM_SLC
    Infinity norm of s_l^c in the basic solution.
MSK_DINF_SOL_BAS_NRM_SLX
    Infinity norm of s_l^x in the basic solution.
MSK_DINF_SOL_BAS_NRM_SUC
    Infinity norm of s_u^c in the basic solution.
MSK_DINF_SOL_BAS_NRM_SUX
    Infinity norm of s_u^X in the basic solution.
MSK_DINF_SOL_BAS_NRM_XC
    Infinity norm of x^c in the basic solution.
MSK_DINF_SOL_BAS_NRM_XX
    Infinity norm of x^x in the basic solution.
MSK_DINF_SOL_BAS_NRM_Y
    Infinity norm of y in the basic solution.
MSK_DINF_SOL_BAS_PRIMAL_OBJ
    Primal objective value of the basic solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set
    .

MSK_DINF_SOL_BAS_PVIOLCON
Maximal primal bound violation for x^c in the basic solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_BAS_PVIOLVAR
Maximal primal bound violation for x^x in the basic solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITG_NRM_BARX
Infinity norm of $\overline{X}$ in the integer solution.

MSK_DINF_SOL_ITG_NRM_XC
Infinity norm of x^c in the integer solution.

MSK_DINF_SOL_ITG_NRM_XX
Infinity norm of x^x in the integer solution.

MSK_DINF_SOL_ITG_PRIMAL_OBJ
Primal objective value of the integer solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITG_PVIOLBARVAR
Maximal primal bound violation for $\overline{X}$ in the integer solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITG_PVIOLCON
Maximal primal bound violation for x^c in the integer solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITG_PVIOLCONES
Maximal primal violation for primal conic constraints in the integer solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITG_PVIOLITG
Maximal violation for the integer constraints in the integer solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITG_PVIOLVAR
Maximal primal bound violation for x^x in the integer solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITR_DUAL_OBJ
Dual objective value of the interior-point solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITR_DVIOLBARVAR
Maximal dual bound violation for $\overline{X}$ in the interior-point solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITR_DVIOLCON
Maximal dual bound violation for x^c in the interior-point solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITR_DVIOLCONES
Maximal dual violation for dual conic constraints in the interior-point solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITR_DVIOLVAR
Maximal dual bound violation for x^x in the interior-point solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO* is set .

MSK_DINF_SOL_ITR_NRM_BARS
Infinity norm of $\overline{S}$ in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_BARX
Infinity norm of $\overline{X}$ in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SLC
Infinity norm of s_l^c in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SLX
Infinity norm of s_l^x in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SNX
Infinity norm of s_n^x in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SUC
Infinity norm of s_u^c in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SUX
    Infinity norm of s_u^X in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_XC
    Infinity norm of x^c in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_XX
    Infinity norm of x^x in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_Y
    Infinity norm of y in the interior-point solution.
MSK_DINF_SOL_ITR_PRIMAL_OBJ
    Primal objective value of the interior-point solution. Updated if *MSK_IPAR_AUTO_UPDATE_SOL_INFO*
    is set .
MSK_DINF_SOL_ITR_PVIOLBARVAR
    Maximal primal bound violation for $\overline{X}$ in the interior-point solution. Updated if
    MSK_IPAR_AUTO_UPDATE_SOL_INFO is set .
MSK_DINF_SOL_ITR_PVIOLCON
    Maximal primal bound violation for x^c in the interior-point solution. Updated if
    MSK_IPAR_AUTO_UPDATE_SOL_INFO is set .
MSK_DINF_SOL_ITR_PVIOLCONES
    Maximal primal violation for primal conic constraints in the interior-point solution. Updated if
    MSK_IPAR_AUTO_UPDATE_SOL_INFO is set .
MSK_DINF_SOL_ITR_PVIOLVAR
    Maximal primal bound violation for x^x in the interior-point solution. Updated if
    MSK_IPAR_AUTO_UPDATE_SOL_INFO is set .
MSK_DINF_TO_CONIC_TIME
    Time spent in the last to conic reformulation.

11.4.21 License feature

MSK_FEATURE_PTS
    Base system.
MSK_FEATURE_PTON
    Conic extension.

11.4.22 Long integer information items.

MSK_LIINF_BI_CLEAN_DUAL_DEG_ITER
    Number of dual degenerate clean iterations performed in the basis identification.
MSK_LIINF_BI_CLEAN_DUAL_ITER
    Number of dual clean iterations performed in the basis identification.
MSK_LIINF_BI_CLEAN_PRIMAL_DEG_ITER
    Number of primal degenerate clean iterations performed in the basis identification.
MSK_LIINF_BI_CLEAN_PRIMAL_ITER
    Number of primal clean iterations performed in the basis identification.
MSK_LIINF_BI_DUAL_ITER
    Number of dual pivots performed in the basis identification.
MSK_LIINF_BI_PRIMAL_ITER
    Number of primal pivots performed in the basis identification.
MSK_LIINF_INTPNT_FACTOR_NUM_NZ
    Number of non-zeros in factorization.
MSK_LIINF_MIO_ANZ
    Number of non-zero entries in the constraint matrix of the probelm to be solved by the mixed-
    integer optimizer.
MSK_LIINF_MIO_INTPNT_ITER
    Number of interior-point iterations performed by the mixed-integer optimizer.
MSK_LIINF_MIO_PRESOLVED_ANZ
    Number of non-zero entries in the constraint matrix of the problem after the mixed-integer opti-
    mizer's presolve.

`MSK_LIINF_MIO_SIMPLEX_ITER`
> Number of simplex iterations performed by the mixed-integer optimizer.

`MSK_LIINF_RD_NUMANZ`
> Number of non-zeros in A that is read.

`MSK_LIINF_RD_NUMQNZ`
> Number of Q non-zeros.

11.4.23 Integer information items.

`MSK_IINF_ANA_PRO_NUM_CON`
> Number of constraints in the problem.

`MSK_IINF_ANA_PRO_NUM_CON_EQ`
> Number of equality constraints.

`MSK_IINF_ANA_PRO_NUM_CON_FR`
> Number of unbounded constraints.

`MSK_IINF_ANA_PRO_NUM_CON_LO`
> Number of constraints with a lower bound and an infinite upper bound.

`MSK_IINF_ANA_PRO_NUM_CON_RA`
> Number of constraints with finite lower and upper bounds.

`MSK_IINF_ANA_PRO_NUM_CON_UP`
> Number of constraints with an upper bound and an infinite lower bound.

`MSK_IINF_ANA_PRO_NUM_VAR`
> Number of variables in the problem.

`MSK_IINF_ANA_PRO_NUM_VAR_BIN`
> Number of binary (0-1) variables.

`MSK_IINF_ANA_PRO_NUM_VAR_CONT`
> Number of continuous variables.

`MSK_IINF_ANA_PRO_NUM_VAR_EQ`
> Number of fixed variables.

`MSK_IINF_ANA_PRO_NUM_VAR_FR`
> Number of free variables.

`MSK_IINF_ANA_PRO_NUM_VAR_INT`
> Number of general integer variables.

`MSK_IINF_ANA_PRO_NUM_VAR_LO`
> Number of variables with a lower bound and an infinite upper bound.

`MSK_IINF_ANA_PRO_NUM_VAR_RA`
> Number of variables with finite lower and upper bounds.

`MSK_IINF_ANA_PRO_NUM_VAR_UP`
> Number of variables with an upper bound and an infinite lower bound.

`MSK_IINF_INTPNT_FACTOR_DIM_DENSE`
> Dimension of the dense sub system in factorization.

`MSK_IINF_INTPNT_ITER`
> Number of interior-point iterations since invoking the interior-point optimizer.

`MSK_IINF_INTPNT_NUM_THREADS`
> Number of threads that the interior-point optimizer is using.

`MSK_IINF_INTPNT_SOLVE_DUAL`
> Non-zero if the interior-point optimizer is solving the dual problem.

`MSK_IINF_MIO_ABSGAP_SATISFIED`
> Non-zero if absolute gap is within tolerances.

`MSK_IINF_MIO_CLIQUE_TABLE_SIZE`
> Size of the clique table.

`MSK_IINF_MIO_CONSTRUCT_SOLUTION`
> This item informs if **MOSEK** constructed an initial integer feasible solution.
>
> - -1: tried, but failed,
>
> - 0: no partial solution supplied by the user,
>
> - 1: constructed feasible solution.

`MSK_IINF_MIO_NODE_DEPTH`
    Depth of the last node solved.
`MSK_IINF_MIO_NUM_ACTIVE_NODES`
    Number of active branch and bound nodes.
`MSK_IINF_MIO_NUM_BRANCH`
    Number of branches performed during the optimization.
`MSK_IINF_MIO_NUM_CLIQUE_CUTS`
    Number of clique cuts.
`MSK_IINF_MIO_NUM_CMIR_CUTS`
    Number of Complemented Mixed Integer Rounding (CMIR) cuts.
`MSK_IINF_MIO_NUM_GOMORY_CUTS`
    Number of Gomory cuts.
`MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS`
    Number of implied bound cuts.
`MSK_IINF_MIO_NUM_INT_SOLUTIONS`
    Number of integer feasible solutions that have been found.
`MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS`
    Number of clique cuts.
`MSK_IINF_MIO_NUM_RELAX`
    Number of relaxations solved during the optimization.
`MSK_IINF_MIO_NUM_REPEATED_PRESOLVE`
    Number of times presolve was repeated at root.
`MSK_IINF_MIO_NUMBIN`
    Number of binary variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMBINCONEVAR`
    Number of binary cone variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMCON`
    Number of constraints in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMCONE`
    Number of cones in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMCONEVAR`
    Number of cone variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMCONT`
    Number of continuous variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMCONTCONEVAR`
    Number of continuous cone variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMDEXPCONES`
    Number of dual exponential cones in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMDPOWCONES`
    Number of dual power cones in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMINT`
    Number of integer variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMINTCONEVAR`
    Number of integer cone variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMPEXPCONES`
    Number of primal exponential cones in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMPPOWCONES`
    Number of primal power cones in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMQCONES`
    Number of quadratic cones in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMRQCONES`
    Number of rotated quadratic cones in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_NUMVAR`
    Number of variables in the problem to be solved by the mixed-integer optimizer.
`MSK_IINF_MIO_OBJ_BOUND_DEFINED`
    Non-zero if a valid objective bound has been found, otherwise zero.
`MSK_IINF_MIO_PRESOLVED_NUMBIN`
    Number of binary variables in the problem after the mixed-integer optimizer's presolve.

MSK_IINF_MIO_PRESOLVED_NUMBINCONEVAR
Number of binary cone variables in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMCON
Number of constraints in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMCONE
Number of cones in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMCONEVAR
Number of cone variables in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMCONT
Number of continuous variables in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMCONTCONEVAR
Number of continuous cone variables in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMDEXPCONES
Number of dual exponential cones in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMDPOWCONES
Number of dual power cones in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMINT
Number of integer variables in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMINTCONEVAR
Number of integer cone variables in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMPEXPCONES
Number of primal exponential cones in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMPPOWCONES
Number of primal power cones in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMQCONES
Number of quadratic cones in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMRQCONES
Number of rotated quadratic cones in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_PRESOLVED_NUMVAR
Number of variables in the problem after the mixed-integer optimizer's presolve.
MSK_IINF_MIO_RELGAP_SATISFIED
Non-zero if relative gap is within tolerances.
MSK_IINF_MIO_TOTAL_NUM_CUTS
Total number of cuts generated by the mixed-integer optimizer.
MSK_IINF_MIO_USER_OBJ_CUT
If it is non-zero, then the objective cut is used.
MSK_IINF_OPT_NUMCON
Number of constraints in the problem solved when the optimizer is called.
MSK_IINF_OPT_NUMVAR
Number of variables in the problem solved when the optimizer is called
MSK_IINF_OPTIMIZE_RESPONSE
The response code returned by optimize.
MSK_IINF_PURIFY_DUAL_SUCCESS
Is nonzero if the dual solution is purified.
MSK_IINF_PURIFY_PRIMAL_SUCCESS
Is nonzero if the primal solution is purified.
MSK_IINF_RD_NUMBARVAR
Number of symmetric variables read.
MSK_IINF_RD_NUMCON
Number of constraints read.
MSK_IINF_RD_NUMCONE
Number of conic constraints read.
MSK_IINF_RD_NUMINTVAR
Number of integer-constrained variables read.
MSK_IINF_RD_NUMQ
Number of nonempty Q matrices read.
MSK_IINF_RD_NUMVAR
Number of variables read.

`MSK_IINF_RD_PROTYPE`
    Problem type.
`MSK_IINF_SIM_DUAL_DEG_ITER`
    The number of dual degenerate iterations.
`MSK_IINF_SIM_DUAL_HOTSTART`
    If 1 then the dual simplex algorithm is solving from an advanced basis.
`MSK_IINF_SIM_DUAL_HOTSTART_LU`
    If 1 then a valid basis factorization of full rank was located and used by the dual simplex algorithm.
`MSK_IINF_SIM_DUAL_INF_ITER`
    The number of iterations taken with dual infeasibility.
`MSK_IINF_SIM_DUAL_ITER`
    Number of dual simplex iterations during the last optimization.
`MSK_IINF_SIM_NUMCON`
    Number of constraints in the problem solved by the simplex optimizer.
`MSK_IINF_SIM_NUMVAR`
    Number of variables in the problem solved by the simplex optimizer.
`MSK_IINF_SIM_PRIMAL_DEG_ITER`
    The number of primal degenerate iterations.
`MSK_IINF_SIM_PRIMAL_HOTSTART`
    If 1 then the primal simplex algorithm is solving from an advanced basis.
`MSK_IINF_SIM_PRIMAL_HOTSTART_LU`
    If 1 then a valid basis factorization of full rank was located and used by the primal simplex algorithm.
`MSK_IINF_SIM_PRIMAL_INF_ITER`
    The number of iterations taken with primal infeasibility.
`MSK_IINF_SIM_PRIMAL_ITER`
    Number of primal simplex iterations during the last optimization.
`MSK_IINF_SIM_SOLVE_DUAL`
    Is non-zero if dual problem is solved.
`MSK_IINF_SOL_BAS_PROSTA`
    Problem status of the basic solution. Updated after each optimization.
`MSK_IINF_SOL_BAS_SOLSTA`
    Solution status of the basic solution. Updated after each optimization.
`MSK_IINF_SOL_ITG_PROSTA`
    Problem status of the integer solution. Updated after each optimization.
`MSK_IINF_SOL_ITG_SOLSTA`
    Solution status of the integer solution. Updated after each optimization.
`MSK_IINF_SOL_ITR_PROSTA`
    Problem status of the interior-point solution. Updated after each optimization.
`MSK_IINF_SOL_ITR_SOLSTA`
    Solution status of the interior-point solution. Updated after each optimization.
`MSK_IINF_STO_NUM_A_REALLOC`
    Number of times the storage for storing A has been changed. A large value may indicates that memory fragmentation may occur.

11.4.24 Information item types

`MSK_INF_DOU_TYPE`
    Is a double information type.
`MSK_INF_INT_TYPE`
    Is an integer.
`MSK_INF_LINT_TYPE`
    Is a long integer.

11.4.25 Input/output modes

`MSK_IOMODE_READ`
    The file is read-only.

MSK_IOMODE_WRITE
    The file is write-only. If the file exists then it is truncated when it is opened. Otherwise it is created
    when it is opened.
MSK_IOMODE_READWRITE
    The file is to read and write.

11.4.26 Specifies the branching direction.

MSK_BRANCH_DIR_FREE
    The mixed-integer optimizer decides which branch to choose.
MSK_BRANCH_DIR_UP
    The mixed-integer optimizer always chooses the up branch first.
MSK_BRANCH_DIR_DOWN
    The mixed-integer optimizer always chooses the down branch first.
MSK_BRANCH_DIR_NEAR
    Branch in direction nearest to selected fractional variable.
MSK_BRANCH_DIR_FAR
    Branch in direction farthest from selected fractional variable.
MSK_BRANCH_DIR_ROOT_LP
    Chose direction based on root lp value of selected variable.
MSK_BRANCH_DIR_GUIDED
    Branch in direction of current incumbent.
MSK_BRANCH_DIR_PSEUDOCOST
    Branch based on the pseudocost of the variable.

11.4.27 Continuous mixed-integer solution type

MSK_MIO_CONT_SOL_NONE
    No interior-point or basic solution are reported when the mixed-integer optimizer is used.
MSK_MIO_CONT_SOL_ROOT
    The reported interior-point and basic solutions are a solution to the root node problem when
    mixed-integer optimizer is used.
MSK_MIO_CONT_SOL_ITG
    The reported interior-point and basic solutions are a solution to the problem with all integer
    variables fixed at the value they have in the integer solution. A solution is only reported in case
    the problem has a primal feasible solution.
MSK_MIO_CONT_SOL_ITG_REL
    In case the problem is primal feasible then the reported interior-point and basic solutions are a
    solution to the problem with all integer variables fixed at the value they have in the integer solution.
    If the problem is primal infeasible, then the solution to the root node problem is reported.

11.4.28 Integer restrictions

MSK_MIO_MODE_IGNORED
    The integer constraints are ignored and the problem is solved as a continuous problem.
MSK_MIO_MODE_SATISFIED
    Integer restrictions should be satisfied.

11.4.29 Mixed-integer node selection types

MSK_MIO_NODE_SELECTION_FREE
    The optimizer decides the node selection strategy.
MSK_MIO_NODE_SELECTION_FIRST
    The optimizer employs a depth first node selection strategy.
MSK_MIO_NODE_SELECTION_BEST
    The optimizer employs a best bound node selection strategy.
MSK_MIO_NODE_SELECTION_PSEUDO
    The optimizer employs selects the node based on a pseudo cost estimate.

11.4.30 MPS file format type

MSK_MPS_FORMAT_STRICT
> It is assumed that the input file satisfies the MPS format strictly.

MSK_MPS_FORMAT_RELAXED
> It is assumed that the input file satisfies a slightly relaxed version of the MPS format.

MSK_MPS_FORMAT_FREE
> It is assumed that the input file satisfies the free MPS format. This implies that spaces are not allowed in names. Otherwise the format is free.

MSK_MPS_FORMAT_CPLEX
> The CPLEX compatible version of the MPS format is employed.

11.4.31 Objective sense types

MSK_OBJECTIVE_SENSE_MINIMIZE
> The problem should be minimized.

MSK_OBJECTIVE_SENSE_MAXIMIZE
> The problem should be maximized.

11.4.32 On/off

MSK_ON
> Switch the option on.

MSK_OFF
> Switch the option off.

11.4.33 Optimizer types

MSK_OPTIMIZER_CONIC
> The optimizer for problems having conic constraints.

MSK_OPTIMIZER_DUAL_SIMPLEX
> The dual simplex optimizer is used.

MSK_OPTIMIZER_FREE
> The optimizer is chosen automatically.

MSK_OPTIMIZER_FREE_SIMPLEX
> One of the simplex optimizers is used.

MSK_OPTIMIZER_INTPNT
> The interior-point optimizer is used.

MSK_OPTIMIZER_MIXED_INT
> The mixed-integer optimizer.

MSK_OPTIMIZER_PRIMAL_SIMPLEX
> The primal simplex optimizer is used.

11.4.34 Ordering strategies

MSK_ORDER_METHOD_FREE
> The ordering method is chosen automatically.

MSK_ORDER_METHOD_APPMINLOC
> Approximate minimum local fill-in ordering is employed.

MSK_ORDER_METHOD_EXPERIMENTAL
> This option should not be used.

MSK_ORDER_METHOD_TRY_GRAPHPAR
> Always try the graph partitioning based ordering.

MSK_ORDER_METHOD_FORCE_GRAPHPAR
> Always use the graph partitioning based ordering even if it is worse than the approximate minimum local fill ordering.

MSK_ORDER_METHOD_NONE
> No ordering is used.

11.4.35 Presolve method.

MSK_PRESOLVE_MODE_OFF
> The problem is not presolved before it is optimized.

MSK_PRESOLVE_MODE_ON
> The problem is presolved before it is optimized.

MSK_PRESOLVE_MODE_FREE
> It is decided automatically whether to presolve before the problem is optimized.

11.4.36 Parameter type

MSK_PAR_INVALID_TYPE
> Not a valid parameter.

MSK_PAR_DOU_TYPE
> Is a double parameter.

MSK_PAR_INT_TYPE
> Is an integer parameter.

MSK_PAR_STR_TYPE
> Is a string parameter.

11.4.37 Problem data items

MSK_PI_VAR
> Item is a variable.

MSK_PI_CON
> Item is a constraint.

MSK_PI_CONE
> Item is a cone.

11.4.38 Problem types

MSK_PROBTYPE_LO
> The problem is a linear optimization problem.

MSK_PROBTYPE_QO
> The problem is a quadratic optimization problem.

MSK_PROBTYPE_QCQO
> The problem is a quadratically constrained optimization problem.

MSK_PROBTYPE_CONIC
> A conic optimization.

MSK_PROBTYPE_MIXED
> General nonlinear constraints and conic constraints. This combination can not be solved by **MOSEK**.

11.4.39 Problem status keys

MSK_PRO_STA_UNKNOWN
> Unknown problem status.

MSK_PRO_STA_PRIM_AND_DUAL_FEAS
> The problem is primal and dual feasible.

MSK_PRO_STA_PRIM_FEAS
> The problem is primal feasible.

MSK_PRO_STA_DUAL_FEAS
> The problem is dual feasible.

MSK_PRO_STA_PRIM_INFEAS
> The problem is primal infeasible.

MSK_PRO_STA_DUAL_INFEAS
> The problem is dual infeasible.

MSK_PRO_STA_PRIM_AND_DUAL_INFEAS
> The problem is primal and dual infeasible.

MSK_PRO_STA_ILL_POSED
    The problem is ill-posed. For example, it may be primal and dual feasible but have a positive
    duality gap.
MSK_PRO_STA_PRIM_INFEAS_OR_UNBOUNDED
    The problem is either primal infeasible or unbounded. This may occur for mixed-integer problems.

11.4.40 XML writer output mode

MSK_WRITE_XML_MODE_ROW
    Write in row order.
MSK_WRITE_XML_MODE_COL
    Write in column order.

11.4.41 Response code type

MSK_RESPONSE_OK
    The response code is OK.
MSK_RESPONSE_WRN
    The response code is a warning.
MSK_RESPONSE_TRM
    The response code is an optimizer termination status.
MSK_RESPONSE_ERR
    The response code is an error.
MSK_RESPONSE_UNK
    The response code does not belong to any class.

11.4.42 Scaling type

MSK_SCALING_FREE
    The optimizer chooses the scaling heuristic.
MSK_SCALING_NONE
    No scaling is performed.
MSK_SCALING_MODERATE
    A conservative scaling is performed.
MSK_SCALING_AGGRESSIVE
    A very aggressive scaling is performed.

11.4.43 Scaling method

MSK_SCALING_METHOD_POW2
    Scales only with power of 2 leaving the mantissa untouched.
MSK_SCALING_METHOD_FREE
    The optimizer chooses the scaling heuristic.

11.4.44 Sensitivity types

MSK_SENSITIVITY_TYPE_BASIS
    Basis sensitivity analysis is performed.

11.4.45 Simplex selection strategy

MSK_SIM_SELECTION_FREE
    The optimizer chooses the pricing strategy.
MSK_SIM_SELECTION_FULL
    The optimizer uses full pricing.
MSK_SIM_SELECTION_ASE
    The optimizer uses approximate steepest-edge pricing.

```
MSK_SIM_SELECTION_DEVEX
```
The optimizer uses devex steepest-edge pricing (or if it is not available an approximate steep-edge selection).
```
MSK_SIM_SELECTION_SE
```
The optimizer uses steepest-edge selection (or if it is not available an approximate steep-edge selection).
```
MSK_SIM_SELECTION_PARTIAL
```
The optimizer uses a partial selection approach. The approach is usually beneficial if the number of variables is much larger than the number of constraints.

11.4.46 Solution items

```
MSK_SOL_ITEM_XC
```
Solution for the constraints.
```
MSK_SOL_ITEM_XX
```
Variable solution.
```
MSK_SOL_ITEM_Y
```
Lagrange multipliers for equations.
```
MSK_SOL_ITEM_SLC
```
Lagrange multipliers for lower bounds on the constraints.
```
MSK_SOL_ITEM_SUC
```
Lagrange multipliers for upper bounds on the constraints.
```
MSK_SOL_ITEM_SLX
```
Lagrange multipliers for lower bounds on the variables.
```
MSK_SOL_ITEM_SUX
```
Lagrange multipliers for upper bounds on the variables.
```
MSK_SOL_ITEM_SNX
```
Lagrange multipliers corresponding to the conic constraints on the variables.

11.4.47 Solution status keys

```
MSK_SOL_STA_UNKNOWN
```
Status of the solution is unknown.
```
MSK_SOL_STA_OPTIMAL
```
The solution is optimal.
```
MSK_SOL_STA_PRIM_FEAS
```
The solution is primal feasible.
```
MSK_SOL_STA_DUAL_FEAS
```
The solution is dual feasible.
```
MSK_SOL_STA_PRIM_AND_DUAL_FEAS
```
The solution is both primal and dual feasible.
```
MSK_SOL_STA_PRIM_INFEAS_CER
```
The solution is a certificate of primal infeasibility.
```
MSK_SOL_STA_DUAL_INFEAS_CER
```
The solution is a certificate of dual infeasibility.
```
MSK_SOL_STA_PRIM_ILLPOSED_CER
```
The solution is a certificate that the primal problem is illposed.
```
MSK_SOL_STA_DUAL_ILLPOSED_CER
```
The solution is a certificate that the dual problem is illposed.
```
MSK_SOL_STA_INTEGER_OPTIMAL
```
The primal solution is integer optimal.

11.4.48 Solution types

```
MSK_SOL_BAS
```
The basic solution.
```
MSK_SOL_ITR
```
The interior solution.

```
MSK_SOL_ITG
```
The integer solution.

11.4.49 Solve primal or dual form

```
MSK_SOLVE_FREE
```
The optimizer is free to solve either the primal or the dual problem.
```
MSK_SOLVE_PRIMAL
```
The optimizer should solve the primal problem.
```
MSK_SOLVE_DUAL
```
The optimizer should solve the dual problem.

11.4.50 Status keys

```
MSK_SK_UNK
```
The status for the constraint or variable is unknown.
```
MSK_SK_BAS
```
The constraint or variable is in the basis.
```
MSK_SK_SUPBAS
```
The constraint or variable is super basic.
```
MSK_SK_LOW
```
The constraint or variable is at its lower bound.
```
MSK_SK_UPR
```
The constraint or variable is at its upper bound.
```
MSK_SK_FIX
```
The constraint or variable is fixed.
```
MSK_SK_INF
```
The constraint or variable is infeasible in the bounds.

11.4.51 Starting point types

```
MSK_STARTING_POINT_FREE
```
The starting point is chosen automatically.
```
MSK_STARTING_POINT_GUESS
```
The optimizer guesses a starting point.
```
MSK_STARTING_POINT_CONSTANT
```
The optimizer constructs a starting point by assigning a constant value to all primal and dual variables. This starting point is normally robust.
```
MSK_STARTING_POINT_SATISFY_BOUNDS
```
The starting point is chosen to satisfy all the simple bounds on nonlinear variables. If this starting point is employed, then more care than usual should employed when choosing the bounds on the nonlinear variables. In particular very tight bounds should be avoided.

11.4.52 Stream types

```
MSK_STREAM_LOG
```
Log stream. Contains the aggregated contents of all other streams. This means that a message written to any other stream will also be written to this stream.
```
MSK_STREAM_MSG
```
Message stream. Log information relating to performance and progress of the optimization is written to this stream.
```
MSK_STREAM_ERR
```
Error stream. Error messages are written to this stream.
```
MSK_STREAM_WRN
```
Warning stream. Warning messages are written to this stream.

11.4.53 Integer values

`MSK_MAX_STR_LEN`
    Maximum string length allowed in **MOSEK**.
`MSK_LICENSE_BUFFER_LENGTH`
    The length of a license key buffer.

11.4.54 Variable types

`MSK_VAR_TYPE_CONT`
    Is a continuous variable.
`MSK_VAR_TYPE_INT`
    Is an integer variable.

Chapter 12

Supported File Formats

MOSEK supports a range of problem and solution formats listed in Table 12.1 and Table 12.2. The **Task format** is **MOSEK**'s native binary format and it supports all features that **MOSEK** supports. The **OPF format** is **MOSEK**'s human-readable alternative that supports nearly all features (everything except semidefinite problems). In general, text formats are significantly slower to read, but can be examined and edited directly in any text editor.

Problem formats

Table 12.1: List of supported file formats for optimization problems. The column *Conic* refers to conic problems involving the quadratic, rotated quadratic, power or exponential cone. The last two columns indicate if the format supports solutions and optimizer parameters.

Format Type	Ext.	Binary/Text	LP	QO	Conic	SDP	Sol	Param
LP	lp	plain text	X	X				
MPS	mps	plain text	X	X	X			
OPF	opf	plain text	X	X	X		X	X
PTF	ptf	plain text	X	X	X	X	X	
CBF	cbf	plain text	X		X	X		
Task format	task	binary	X	X	X	X	X	X
Jtask format	jtask	text	X	X	X	X	X	X

Solution formats

Table 12.2: List of supported solution formats.

Format Type	Ext.	Binary/Text	Description
SOL	sol	plain text	Interior Solution
	bas	plain text	Basic Solution
	int	plain text	Integer
Jsol format	jsol	text	Solution

Compression

MOSEK supports GZIP and Zstandard compression. Problem files with extension `.gz` (for GZIP) and `.zst` (for Zstandard) are assumed to be compressed when read, and are automatically compressed when written. For example, a file called

```
problem.mps.gz
```

will be considered as a GZIP compressed MPS file.

12.1 The LP File Format

MOSEK supports the LP file format with some extensions. The LP format is not a completely well-defined standard and hence different optimization packages may interpret the same LP file in slightly different ways. **MOSEK** tries to emulate as closely as possible CPLEX's behavior, but tries to stay backward compatible.

The LP file format can specify problems of the form

$$
\begin{array}{llrcl}
\text{minimize/maximize} & & c^T x + \frac{1}{2} q^o(x) & & \\
\text{subject to} & l^c \leq & Ax + \frac{1}{2} q(x) & \leq & u^c, \\
& l^x \leq & x & \leq & u^x, \\
& & x_{\mathcal{J}} \text{ integer,} & &
\end{array}
$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.

- $c \in \mathbb{R}^n$ is the linear term in the objective.

- $q^o :\in \mathbb{R}^n \to \mathbb{R}$ is the quadratic term in the objective where

$$q^o(x) = x^T Q^o x$$

and it is assumed that

$$Q^o = (Q^o)^T.$$

- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.

- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.

- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.

- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.

- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.

- $q : \mathbb{R}^n \to \mathbb{R}$ is a vector of quadratic functions. Hence,

$$q_i(x) = x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

- $\mathcal{J} \subseteq \{1, 2, \ldots, n\}$ is an index set of the integer constrained variables.

12.1.1 File Sections

An LP formatted file contains a number of sections specifying the objective, constraints, variable bounds, and variable types. The section keywords may be any mix of upper and lower case letters.

Objective Function

The first section beginning with one of the keywords

```
max
maximum
maximize
min
minimum
minimize
```

defines the objective sense and the objective function, i.e.

$$c^T x + \frac{1}{2} x^T Q^o x.$$

The objective may be given a name by writing

```
myname:
```

before the expressions. If no name is given, then the objective is named `obj`.

The objective function contains linear and quadratic terms. The linear terms are written as

```
4 x1 + x2 - 0.1 x3
```

and so forth. The quadratic terms are written in square brackets (`[ ]/2`) and are either squared or multiplied as in the examples

```
x1^2
```

and

```
x1 * x2
```

There may be zero or more pairs of brackets containing quadratic expressions.

An example of an objective section is

```
minimize
myobj: 4 x1 + x2 - 0.1 x3 + [ x1^2 + 2.1 x1 * x2 ]/2
```

Please note that the quadratic expressions are multiplied with $\frac{1}{2}$, so that the above expression means

$$\text{minimize} \quad 4x_1 + x_2 - 0.1 \cdot x_3 + \tfrac{1}{2}(x_1^2 + 2.1 \cdot x_1 \cdot x_2)$$

If the same variable occurs more than once in the linear part, the coefficients are added, so that `4 x1 + 2 x1` is equivalent to `6 x1`. In the quadratic expressions `x1 * x2` is equivalent to `x2 * x1` and, as in the linear part, if the same variables multiplied or squared occur several times their coefficients are added.

Constraints

The second section beginning with one of the keywords

```
subj to
subject to
s.t.
st
```

defines the linear constraint matrix A and the quadratic matrices Q^i.

A constraint contains a name (optional), expressions adhering to the same rules as in the objective and a bound:

```
subject to
con1: x1 + x2 + [ x3^2 ]/2 <= 5.1
```

The bound type (here `<=`) may be any of `<, <=, =, >, >=` (`<` and `<=` mean the same), and the bound may be any number.

In the standard LP format it is not possible to define more than one bound per line, but **MOSEK** supports defining ranged constraints by using double-colon (`::`) instead of a single-colon (`:`) after the constraint name, i.e.

$$-5 \le x_1 + x_2 \le 5 \tag{12.1}$$

may be written as

```
con:: -5 < x_1 + x_2 < 5
```

By default **MOSEK** writes ranged constraints this way.

If the files must adhere to the LP standard, ranged constraints must either be split into upper bounded and lower bounded constraints or be written as an equality with a slack variable. For example the expression (12.1) may be written as

$$x_1 + x_2 - sl_1 = 0, \ -5 \le sl_1 \le 5.$$

Bounds

Bounds on the variables can be specified in the bound section beginning with one of the keywords

```
bound
bounds
```

The bounds section is optional but should, if present, follow the `subject to` section. All variables listed in the bounds section must occur in either the objective or a constraint.

The default lower and upper bounds are 0 and $+\infty$. A variable may be declared free with the keyword `free`, which means that the lower bound is $-\infty$ and the upper bound is $+\infty$. Furthermore it may be assigned a finite lower and upper bound. The bound definitions for a given variable may be written in one or two lines, and bounds can be any number or $\pm\infty$ (written as `+inf`/`-inf`/`+infinity`/`-infinity`) as in the example

```
bounds
x1 free
x2 <= 5
0.1 <= x2
x3 = 42
2 <= x4 < +inf
```

Variable Types

The final two sections are optional and must begin with one of the keywords

```
bin
binaries
binary
```

and

```
gen
general
```

Under `general` all integer variables are listed, and under `binary` all binary (integer variables with bounds 0 and 1) are listed:

```
general
x1 x2
binary
x3 x4
```

Again, all variables listed in the binary or general sections must occur in either the objective or a constraint.

Terminating Section

Finally, an LP formatted file must be terminated with the keyword

```
end
```

12.1.2 LP File Examples

Linear example `lo1.lp`

```
\ File: lo1.lp
maximize
obj: 3 x1 + x2 + 5 x3 + x4
subject to
c1:  3 x1 + x2 + 2 x3 = 30
c2:  2 x1 + x2 + 3 x3 + x4 >= 15
c3:  2 x2 + 3 x4 <= 25
bounds
 0 <= x1 <= +infinity
 0 <= x2 <= 10
 0 <= x3 <= +infinity
 0 <= x4 <= +infinity
end
```

Mixed integer example `milo1.lp`

```
maximize
obj: x1 + 6.4e-01 x2
subject to
c1:  5e+01 x1 + 3.1e+01 x2 <= 2.5e+02
c2:  3e+00 x1 - 2e+00 x2 >= -4e+00
bounds
 0 <= x1 <= +infinity
 0 <= x2 <= +infinity
general
 x1 x2
end
```

12.1.3 LP Format peculiarities

Comments

Anything on a line after a \ is ignored and is treated as a comment.

Names

A name for an objective, a constraint or a variable may contain the letters `a-z`, `A-Z`, the digits `0-9` and the characters

```
!"#$%&()/,.;?@_'`|~
```

The first character in a name must not be a number, a period or the letter `e` or `E`. Keywords must not be used as names.

MOSEK accepts any character as valid for names, except `\0`. A name that is not allowed in LP file will be changed and a warning will be issued.

The algorithm for making names LP valid works as follows: The name is interpreted as an `utf-8` string. For a Unicode character `c`:

- If `c==_` (underscore), the output is `__` (two underscores).

- If `c` is a valid LP name character, the output is just `c`.

- If `c` is another character in the ASCII range, the output is `_XX`, where `XX` is the hexadecimal code for the character.

- If `c` is a character in the range *127-65535*, the output is `_uXXXX`, where `XXXX` is the hexadecimal code for the character.

- If `c` is a character above 65535, the output is `_UXXXXXXXX`, where `XXXXXXXX` is the hexadecimal code for the character.

Invalid `utf-8` substrings are escaped as `_XX'`, and if a name starts with a period, `e` or `E`, that character is escaped as `_XX`.

Variable Bounds

Specifying several upper or lower bounds on one variable is possible but **MOSEK** uses only the tightest bounds. If a variable is fixed (with `=`), then it is considered the tightest bound.

MOSEK Extensions to the LP Format

Some optimization software packages employ a more strict definition of the LP format than the one used by **MOSEK**. The limitations imposed by the strict LP format are the following:

- Quadratic terms in the constraints are not allowed.

- Names can be only 16 characters long.

- Lines must not exceed 255 characters in length.

To get around some of the inconveniences converting from other problem formats, **MOSEK** allows lines to contain 1024 characters and names may have any length (shorter than the 1024 characters).

If an LP formatted file created by **MOSEK** should satisfy the strict definition, then the parameter `MSK_IPAR_WRITE_LP_STRICT_FORMAT` should be set; note, however, that some problems cannot be written correctly as a strict LP formatted file. For instance, all names are truncated to 16 characters and hence they may lose their uniqueness and change the problem.

Internally in **MOSEK** names may contain any (printable) character, many of which cannot be used in LP names. Setting the parameters `MSK_IPAR_READ_LP_QUOTED_NAMES` and `MSK_IPAR_WRITE_LP_QUOTED_NAMES` allows **MOSEK** to use quoted names. The first parameter tells **MOSEK** to remove quotes from quoted names e.g, `"x1"`, when reading LP formatted files. The second parameter tells **MOSEK** to put quotes around any semi-illegal name (names beginning with a number or a period) and fully illegal name (containing illegal characters). As double quote is a legal character in the LP format, quoting semi-illegal names makes them legal in the pure LP format as long as they are still shorter than 16 characters. Fully illegal names are still illegal in a pure LP file.

The strict LP format

The LP format is not a formal standard and different vendors have slightly different interpretations of the LP format. To make **MOSEK**'s definition of the LP format more compatible with the definitions of other vendors set the parameter `MSK_IPAR_WRITE_LP_STRICT_FORMAT` to `MSK_ON`.

This setting may lead to truncation of some names and hence to an invalid LP file. The simple solution to this problem is to set the parameter `MSK_IPAR_WRITE_GENERIC_NAMES` to `MSK_ON` which will cause all names to be renamed systematically in the output file.

Formatting of an LP File

A few parameters control the visual formatting of LP files written by **MOSEK** in order to make it easier to read the files. These parameters are

- `MSK_IPAR_WRITE_LP_LINE_WIDTH` sets the maximum number of characters on a single line. The default value is 80 corresponding roughly to the width of a standard text document.

- `MSK_IPAR_WRITE_LP_TERMS_PER_LINE` sets the maximum number of terms per line; a term means a sign, a coefficient, and a name (for example `+ 42 elephants`). The default value is 0, meaning that there is no maximum.

Unnamed Constraints

Reading and writing an LP file with **MOSEK** may change it superficially. If an LP file contains unnamed constraints or objective these are given their generic names when the file is read (however unnamed constraints in **MOSEK** are written without names).

12.2 The MPS File Format

MOSEK supports the standard MPS format with some extensions. For a detailed description of the MPS format see the book by Nazareth [Naz87].

12.2.1 MPS File Structure

The version of the MPS format supported by **MOSEK** allows specification of an optimization problem of the form

$$
\begin{array}{rcccl}
\text{maximize/minimize} & & c^T x + q_0(x) & & \\
l^c & \leq & Ax + q(x) & \leq & u^c, \\
l^x & \leq & x & \leq & u^x, \\
& & x \in \mathcal{K}, & & \\
& & x_{\mathcal{J}} \quad \text{integer}, & &
\end{array} \tag{12.2}
$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.

- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.

- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.

- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.

- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.

- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.

- $q : \mathbb{R}^n \to \mathbb{R}$ is a vector of quadratic functions. Hence,

$$
q_i(x) = \frac{1}{2} x^T Q^i x
$$

  where it is assumed that $Q^i = (Q^i)^T$. Please note the explicit $\frac{1}{2}$ in the quadratic term and that Q^i is required to be symmetric. The same applies to q_0.

- $\mathcal{K}$ is a convex cone.

- $\mathcal{J} \subseteq \{1, 2, \ldots, n\}$ is an index set of the integer-constrained variables.

- c is the vector of objective coefficients.

An MPS file with one row and one column can be illustrated like this:

```
*         1         2         3         4         5         6
*234567890123456789012345678901234567890123456789012345678901234567890
NAME          [name]
OBJSENSE
    [objsense]
OBJNAME       [objname]
ROWS
 ?  [cname1]
COLUMNS
    [vname1]  [cname1]  [value1]      [cname2]  [value2]
RHS
    [name]    [cname1]  [value1]      [cname2]  [value2]
RANGES
    [name]    [cname1]  [value1]      [cname2]  [value2]
QSECTION      [cname1]
    [vname1]  [vname2]  [value1]      [vname3]  [value2]
QMATRIX
    [vname1]  [vname2]  [value1]
```

```
QUADOBJ
    [vname1]    [vname2]    [value1]
QCMATRIX        [cname1]
    [vname1]    [vname2]    [value1]
BOUNDS
 ?? [name]      [vname1]    [value1]
CSECTION        [kname1]    [value1]            [ktype]
    [vname1]
ENDATA
```

Here the names in capitals are keywords of the MPS format and names in brackets are custom defined names or values. A couple of notes on the structure:

- Fields: All items surrounded by brackets appear in *fields*. The fields named "valueN" are numerical values. Hence, they must have the format

```
[+|-]XXXXXXX.XXXXXX[[e|E][+|-]XXX]
```

where

```
X = [0|1|2|3|4|5|6|7|8|9].
```

- Sections: The MPS file consists of several sections where the names in capitals indicate the beginning of a new section. For example, COLUMNS denotes the beginning of the columns section.

- Comments: Lines starting with an * are comment lines and are ignored by **MOSEK**.

- Keys: The question marks represent keys to be specified later.

- Extensions: The sections QSECTION and CSECTION are specific **MOSEK** extensions of the MPS format. The sections QMATRIX, QUADOBJ and QCMATRIX are included for sake of compatibility with other vendors extensions to the MPS format.

- The standard MPS format is a fixed format, i.e. everything in the MPS file must be within certain fixed positions. **MOSEK** also supports a *free format*. See Sec. 12.2.5 for details.

Linear example `lo1.mps`

A concrete example of a MPS file is presented below:

```
* File: lo1.mps
NAME            lo1
OBJSENSE
    MAX
ROWS
 N  obj
 E  c1
 G  c2
 L  c3
COLUMNS
    x1          obj         3
    x1          c1          3
    x1          c2          2
    x2          obj         1
    x2          c1          1
    x2          c2          1
    x2          c3          2
    x3          obj         5
    x3          c1          2
    x3          c2          3
    x4          obj         1
    x4          c2          1
```

```
     x4          c3          3
RHS
     rhs         c1          30
     rhs         c2          15
     rhs         c3          25
RANGES
BOUNDS
 UP bound        x2          10
ENDATA
```

Subsequently each individual section in the MPS format is discussed.

NAME (optional)

In this section a name (`[name]`) is assigned to the problem.

OBJSENSE (optional)

This is an optional section that can be used to specify the sense of the objective function. The `OBJSENSE` section contains one line at most which can be one of the following:

```
MIN
MINIMIZE
MAX
MAXIMIZE
```

It should be obvious what the implication is of each of these four lines.

OBJNAME (optional)

This is an optional section that can be used to specify the name of the row that is used as objective function. `objname` should be a valid row name.

ROWS

A record in the `ROWS` section has the form

```
?   [cname1]
```

where the requirements for the fields are as follows:

Field	Starting Position	Max Width	required	Description
?	2	1	Yes	Constraint key
[cname1]	5	8	Yes	Constraint name

Hence, in this section each constraint is assigned a unique name denoted by `[cname1]`. Please note that `[cname1]` starts in position 5 and the field can be at most 8 characters wide. An initial key `?` must be present to specify the type of the constraint. The key can have values `E`, `G`, `L`, or `N` with the following interpretation:

Constraint type	l_i^c	u_i^c
E (equal)	finite	$= l_i^c$
G (greater)	finite	∞
L (lower)	$-\infty$	finite
N (none)	$-\infty$	∞

In the MPS format the objective vector is not specified explicitly, but one of the constraints having the key `N` will be used as the objective vector c. In general, if multiple `N` type constraints are specified, then the first will be used as the objective vector c, unless something else was specified in the section `OBJNAME`.

In this section the elements of A are specified using one or more records having the form:

```
[vname1]   [cname1]    [value1]      [cname2]   [value2]
```

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

Hence, a record specifies one or two elements a_{ij} of A using the principle that [vname1] and [cname1] determines j and i respectively. Please note that [cname1] must be a constraint name specified in the ROWS section. Finally, [value1] denotes the numerical value of a_{ij}. Another optional element is specified by [cname2], and [value2] for the variable specified by [vname1]. Some important comments are:

- All elements belonging to one variable must be grouped together.

- Zero elements of A should not be specified.

- At least one element for each variable should be specified.

RHS (optional)

A record in this section has the format

```
[name]     [cname1]    [value1]      [cname2]   [value2]
```

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RHS vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The interpretation of a record is that [name] is the name of the RHS vector to be specified. In general, several vectors can be specified. [cname1] denotes a constraint name previously specified in the ROWS section. Now, assume that this name has been assigned to the i -h constraint and v_1 denotes the value specified by [value1], then the interpretation of v_1 is:

Constraint	l_i^c	u_i^c
E	v_1	v_1
G	v_1	
L		v_1
N		

An optional second element is specified by [cname2] and [value2] and is interpreted in the same way. Please note that it is not necessary to specify zero elements, because elements are assumed to be zero.

RANGES (optional)

A record in this section has the form

```
[name]     [cname1]    [value1]      [cname2]   [value2]
```

where the requirements for each fields are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RANGE vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The records in this section are used to modify the bound vectors for the constraints, i.e. the values in l^c and u^c. A record has the following interpretation: [name] is the name of the RANGE vector and [cname1] is a valid constraint name. Assume that [cname1] is assigned to the i-th constraint and let v_1 be the value specified by [value1], then a record has the interpretation:

Constraint type	Sign of v_1	l_i^c	u_i^c
E	$-$	$u_i^c + v_1$	
E	$+$		$l_i^c + v_1$
G	$-$ or $+$		$l_i^c + |v_1|$
L	$-$ or $+$	$u_i^c - |v_1|$	
N			

Another constraint bound can optionally be modified using [cname2] and [value2] the same way.

QSECTION (optional)

Within the QSECTION the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic terms belong. A record in the QSECTION has the form

```
[vname1]   [vname2]      [value1]       [vname3]   [value2]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value
[vname3]	40	8	No	Variable name
[value2]	50	12	No	Numerical value

A record specifies one or two elements in the lower triangular part of the Q^i matrix where [cname1] specifies the i. Hence, if the names [vname1] and [vname2] have been assigned to the k-th and j-th variable, then Q_{kj}^i is assigned the value given by [value1] An optional second element is specified in the same way by the fields [vname1], [vname3], and [value2].

The example

$$\begin{array}{ll}
\text{minimize} & -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) \\
\text{subject to} & x_1 + x_2 + x_3 \quad \geq \quad 1, \\
& x \geq 0
\end{array}$$

has the following MPS file representation

```
* File: qo1.mps
NAME            qo1
ROWS
 N  obj
 G  c1
COLUMNS
    x1        c1        1.0
    x2        obj       -1.0
    x2        c1        1.0
```

```
    x3          c1          1.0
RHS
    rhs         c1          1.0
QSECTION        obj
    x1          x1          2.0
    x1          x3          -1.0
    x2          x2          0.2
    x3          x3          2.0
ENDATA
```

Regarding the `QSECTION`s please note that:

- Only one `QSECTION` is allowed for each constraint.

- The `QSECTION`s can appear in an arbitrary order after the `COLUMNS` section.

- All variable names occurring in the `QSECTION` must already be specified in the `COLUMNS` section.

- All entries specified in a `QSECTION` are assumed to belong to the lower triangular part of the quadratic term of Q .

QMATRIX/QUADOBJ (optional)

The `QMATRIX` and `QUADOBJ` sections allow to define the quadratic term of the objective function. They differ in how the quadratic term of the objective function is stored:

- `QMATRIX` stores all the nonzeros coefficients, without taking advantage of the symmetry of the Q matrix.

- `QUADOBJ` stores the upper diagonal nonzero elements of the Q matrix.

A record in both sections has the form:

```
[vname1]    [vname2]      [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies one elements of the Q matrix in the objective function . Hence, if the names [vname1] and [vname2] have been assigned to the k-th and j-th variable, then Q_{kj} is assigned the value given by [value1]. Note that a line must appear for each off-diagonal coefficient if using a `QMATRIX` section, while only one entry is required in a `QUADOBJ` section. The quadratic part of the objective function will be evaluated as $1/2x^T Q x$.

The example

$$
\begin{aligned}
\text{minimize} \quad & -x_2 + \tfrac{1}{2}(2x_1^2 - 2x_1 x_3 + 0.2x_2^2 + 2x_3^2) \\
\text{subject to} \quad & x_1 + x_2 + x_3 \geq 1, \\
& x \geq 0
\end{aligned}
$$

has the following MPS file representation using `QMATRIX`

```
* File: qo1_matrix.mps
NAME            qo1_qmatrix
ROWS
 N  obj
 G  c1
COLUMNS
    x1          c1          1.0
    x2          obj         -1.0
```

```
    x2          c1          1.0
    x3          c1          1.0
RHS
    rhs         c1          1.0
QMATRIX
    x1          x1          2.0
    x1          x3         -1.0
    x3          x1         -1.0
    x2          x2          0.2
    x3          x3          2.0
ENDATA
```

or the following using `QUADOBJ`

```
* File: qo1_quadobj.mps
NAME            qo1_quadobj
ROWS
 N  obj
 G  c1
COLUMNS
    x1          c1          1.0
    x2          obj        -1.0
    x2          c1          1.0
    x3          c1          1.0
RHS
    rhs         c1          1.0
QUADOBJ
    x1          x1          2.0
    x1          x3         -1.0
    x2          x2          0.2
    x3          x3          2.0
ENDATA
```

Please also note that:

- A `QMATRIX`/`QUADOBJ` section can appear in an arbitrary order after the `COLUMNS` section.

- All variable names occurring in the `QMATRIX`/`QUADOBJ` section must already be specified in the `COLUMNS` section.

QCMATRIX (optional)

A `QCMATRIX` section allows to specify the quadratic part of a given constraint. Within the `QCMATRIX` the label [cname1] must be a constraint name previously specified in the `ROWS` section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the `QSECTION` has the form

```
[vname1]    [vname2]        [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies an entry of the Q^i matrix where [cname1] specifies the i. Hence, if the names [vname1] and [vname2] have been assigned to the k-th and j-th variable, then Q^i_{kj} is assigned the value given by [value1]. Moreover, the quadratic term is represented as $1/2 x^T Q x$.

The example

$$
\begin{array}{rccl}
\text{minimize} & x_2 & & \\
\text{subject to} & x_1 + x_2 + x_3 & \geq & 1, \\
& \frac{1}{2}(-2x_1 x_3 + 0.2x_2^2 + 2x_3^2) & \leq & 10, \\
& x \geq 0 &
\end{array}
$$

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has the following MPS file representation

```
* File: qo1.mps
NAME            qo1
ROWS
 N  obj
 G  c1
 L  q1
COLUMNS
    x1          c1          1.0
    x2          obj         -1.0
    x2          c1          1.0
    x3          c1          1.0
RHS
    rhs         c1          1.0
    rhs         q1          10.0
QCMATRIX        q1
    x1          x1          2.0
    x1          x3          -1.0
    x3          x1          -1.0
    x2          x2          0.2
    x3          x3          2.0
ENDATA
```

Regarding the QCMATRIXs please note that:

- Only one QCMATRIX is allowed for each constraint.

- The QCMATRIXs can appear in an arbitrary order after the COLUMNS section.

- All variable names occurring in the QSECTION must already be specified in the COLUMNS section.

- QCMATRIX does not exploit the symmetry of Q: an off-diagonal entry (i, j) should appear twice.

BOUNDS (optional)

In the BOUNDS section changes to the default bounds vectors l^x and u^x are specified. The default bounds vectors are $l^x = 0$ and $u^x = \infty$. Moreover, it is possible to specify several sets of bound vectors. A record in this section has the form

```
?? [name]     [vname1]     [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	Required	Description
??	2	2	Yes	Bound key
[name]	5	8	Yes	Name of the BOUNDS vector
[vname1]	15	8	Yes	Variable name
[value1]	25	12	No	Numerical value

Hence, a record in the BOUNDS section has the following interpretation:[name] is the name of the bound vector and [vname1] is the name of the variable for which the bounds are modified by the record. ?? and [value1] are used to modify the bound vectors according to the following table:

??	l_j^x	u_j^x	Made integer (added to $\mathcal{J}$)
FR	$-\infty$	∞	No
FX	v_1	v_1	No
LO	v_1	unchanged	No
MI	$-\infty$	unchanged	No
PL	unchanged	∞	No
UP	unchanged	v_1	No
BV	0	1	Yes
LI	$\lceil v_1 \rceil$	unchanged	Yes
UI	unchanged	$\lfloor v_1 \rfloor$	Yes

Here v_1 is the value specified by [value1].

The purpose of the CSECTION is to specify the conic constraint

$$x \in \mathcal{K}$$

in (12.2). It is assumed that $\mathcal{K}$ satisfies the following requirements. Let

$$x^t \in \mathbb{R}^{n^t}, \quad t = 1, \ldots, k$$

be vectors comprised of parts of the decision variables x so that each decision variable is a member of exactly **one** vector x^t, for example

$$x^1 = \begin{bmatrix} x_1 \\ x_4 \\ x_7 \end{bmatrix} \quad \text{and} \quad x^2 = \begin{bmatrix} x_6 \\ x_5 \\ x_3 \\ x_2 \end{bmatrix}.$$

Next define

$$\mathcal{K} := \left\{ x \in \mathbb{R}^n : \quad x^t \in \mathcal{K}_t, \quad t = 1, \ldots, k \right\}$$

where $\mathcal{K}_t$ must have one of the following forms:

- $\mathbb{R}$ set:

$$\mathcal{K}_t = \mathbb{R}^{n^t}.$$

- Zero cone:

$$\mathcal{K}_t = \{0\} \subseteq \mathbb{R}^{n^t}. \tag{12.3}$$

- Quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : x_1 \geq \sqrt{\sum_{j=2}^{n^t} x_j^2} \right\}. \tag{12.4}$$

- Rotated quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : 2x_1 x_2 \geq \sum_{j=3}^{n^t} x_j^2, \quad x_1, x_2 \geq 0 \right\}. \tag{12.5}$$

- Primal exponential cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^3 : x_1 \geq x_2 \exp(x_3/x_2), \quad x_1, x_2 \geq 0 \right\}. \tag{12.6}$$

- Primal power cone (with parameter $0 < \alpha < 1$):

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : x_1^\alpha x_2^{1-\alpha} \geq \sqrt{\sum_{j=3}^{n^t} x_j^2}, \quad x_1, x_2 \geq 0 \right\}. \tag{12.7}$$

- Dual exponential cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^3 : x_1 \geq -x_3 e^{-1} \exp(x_2/x_3), \quad x_3 \leq 0, x_1 \geq 0 \right\}. \tag{12.8}$$

- Dual power cone (with parameter $0 < \alpha < 1$):

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : \left(\frac{x_1}{\alpha}\right)^\alpha \left(\frac{x_2}{1-\alpha}\right)^{1-\alpha} \geq \sqrt{\sum_{j=3}^{n^t} x_j^2}, \quad x_1, x_2 \geq 0 \right\}. \tag{12.9}$$

In general, membership in the $\mathbb{R}$ set is not specified. If a variable is not a member of any other cone then it is assumed to be a member of the $\mathbb{R}$ cone.

Next, let us study an example. Assume that the power cone

$$x_4^{1/3} x_5^{2/3} \geq |x_8|$$

and the rotated quadratic cone

$$2x_3 x_7 \geq x_1^2 + x_0^2, \quad x_3, x_7 \geq 0,$$

should be specified in the MPS file. One `CSECTION` is required for each cone and they are specified as follows:

```
*        1         2         3         4         5         6
*234567890123456789012345678901234567890123456789012345678901234567890
CSECTION      konea     3e-1           PPOW
x4
x5
x8
CSECTION      koneb     0.0            RQUAD
x7
x3
x1
x0
```

In general, a `CSECTION` header has the format

```
CSECTION      [kname1]    [value1]     [ktype]
```

where the requirements for each field are as follows:

Field	Starting Position	Max Width	Required	Description
[kname1]	15	8	Yes	Name of the cone
[value1]	25	12	No	Cone parameter
[ktype]	40		Yes	Type of the cone.

The possible cone type keys are:

[ktype]	Members	[value1]	Interpretation.
ZERO	≥ 0	unused	Zero cone (12.3).
QUAD	≥ 1	unused	Quadratic cone (12.4).
RQUAD	≥ 2	unused	Rotated quadratic cone (12.5).
PEXP	3	unused	Primal exponential cone (12.6).
PPOW	≥ 2	α	Primal power cone (12.7).
DEXP	3	unused	Dual exponential cone (12.8).
DPOW	≥ 2	α	Dual power cone (12.9).

A record in the `CSECTION` has the format

```
[vname1]
```

where the requirements for each field are

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	A valid variable name

A variable must occur in at most one `CSECTION`.

```
ENDATA
```

This keyword denotes the end of the MPS file.

12.2.2 Integer Variables

Using special bound keys in the `BOUNDS` section it is possible to specify that some or all of the variables should be integer-constrained i.e. be members of $\mathcal{J}$. However, an alternative method is available. This method is available only for backward compatibility and we recommend that it is not used. This method requires that markers are placed in the `COLUMNS` section as in the example:

```
COLUMNS
x1          obj          -10.0          c1          0.7
x1          c2           0.5            c3          1.0
x1          c4           0.1
* Start of integer-constrained variables.
MARK000     'MARKER'                    'INTORG'
x2          obj          -9.0           c1          1.0
x2          c2           0.8333333333   c3          0.66666667
x2          c4           0.25
x3          obj          1.0            c6          2.0
MARK001     'MARKER'                    'INTEND'
* End of integer-constrained variables.
```

Please note that special marker lines are used to indicate the start and the end of the integer variables. Furthermore be aware of the following

- All variables between the markers are assigned a default lower bound of 0 and a default upper bound of 1. **This may not be what is intended.** If it is not intended, the correct bounds should be defined in the `BOUNDS` section of the MPS formatted file.

- **MOSEK** ignores field 1, i.e. `MARK0001` and `MARK001`, however, other optimization systems require them.

- Field 2, i.e. `MARKER`, must be specified including the single quotes. This implies that no row can be assigned the name `MARKER`.

- Field 3 is ignored and should be left blank.

- Field 4, i.e. `INTORG` and `INTEND`, must be specified.

- It is possible to specify several such integer marker sections within the `COLUMNS` section.

12.2.3 General Limitations

- An MPS file should be an ASCII file.

12.2.4 Interpretation of the MPS Format

Several issues related to the MPS format are not well-defined by the industry standard. However, **MOSEK** uses the following interpretation:

- If a matrix element in the `COLUMNS` section is specified multiple times, then the multiple entries are added together.

- If a matrix element in a `QSECTION` section is specified multiple times, then the multiple entries are added together.

12.2.5 The Free MPS Format

MOSEK supports a free format variation of the MPS format. The free format is similar to the MPS file format but less restrictive, e.g. it allows longer names. However, a name must not contain any blanks.

Moreover, by default a line in the MPS file must not contain more than 1024 characters. By modifying the parameter *MSK_IPAR_READ_MPS_WIDTH* an arbitrary large line width will be accepted.

The free MPS format is default. To change to the strict and other formats use the parameter *MSK_IPAR_READ_MPS_FORMAT*.

12.3 The OPF Format

The *Optimization Problem Format (OPF)* is an alternative to LP and MPS files for specifying optimization problems. It is row-oriented, inspired by the CPLEX LP format.

Apart from containing objective, constraints, bounds etc. it may contain complete or partial solutions, comments and extra information relevant for solving the problem. It is designed to be easily read and modified by hand and to be forward compatible with possible future extensions.

Intended use

The OPF file format is meant to replace several other files:

- The LP file format: Any problem that can be written as an LP file can be written as an OPF file too; furthermore it naturally accommodates ranged constraints and variables as well as arbitrary characters in names, fixed expressions in the objective, empty constraints, and conic constraints.

- Parameter files: It is possible to specify integer, double and string parameters along with the problem (or in a separate OPF file).

- Solution files: It is possible to store a full or a partial solution in an OPF file and later reload it.

12.3.1 The File Format

The format uses tags to structure data. A simple example with the basic sections may look like this:

```
[comment]
This is a comment. You may write almost anything here...
[/comment]

# This is a single-line comment.

[objective min 'myobj']
x + 3 y + x^2 + 3 y^2 + z + 1
[/objective]

[constraints]
[con 'con01'] 4 <= x + y  [/con]
[/constraints]

[bounds]
[b] -10 <= x,y <= 10  [/b]

[cone quad] x,y,z [/cone]
[/bounds]
```

A scope is opened by a tag of the form `[tag]` and closed by a tag of the form `[/tag]`. An opening tag may accept a list of unnamed and named arguments, for examples:

```
[tag value] tag with one unnamed argument [/tag]
[tag arg=value] tag with one named argument [/tag]
```

Unnamed arguments are identified by their order, while named arguments may appear in any order, but never before an unnamed argument. The `value` can be a quoted, single-quoted or double-quoted text string, i.e.

```
[tag 'value']     single-quoted value [/tag]
[tag arg='value'] single-quoted value [/tag]
[tag "value"]     double-quoted value [/tag]
[tag arg="value"] double-quoted value [/tag]
```

12.3.2 Sections

The recognized tags are

[comment]

A comment section. This can contain *almost* any text: Between single quotes (') or double quotes (")
any text may appear. Outside quotes the markup characters ([and]) must be prefixed by backslashes.
Both single and double quotes may appear alone or inside a pair of quotes if it is prefixed by a backslash.

[objective]

The objective function: This accepts one or two parameters, where the first one (in the above example
min) is either min or max (regardless of case) and defines the objective sense, and the second one (above
myobj), if present, is the objective name. The section may contain linear and quadratic expressions.
    If several objectives are specified, all but the last are ignored.

[constraints]

This does not directly contain any data, but may contain subsections con defining a linear constraint.

[con]

Defines a single constraint; if an argument is present ([con NAME]) this is used as the name of the
constraint, otherwise it is given a null-name. The section contains a constraint definition written as
linear and quadratic expressions with a lower bound, an upper bound, with both or with an equality.
Examples:

```
[constraints]
[con 'con1'] 0 <= x + y        [/con]
[con 'con2'] 0 >= x + y        [/con]
[con 'con3'] 0 <= x + y <= 10 [/con]
[con 'con4']     x + y  = 10 [/con]
[/constraints]
```

Constraint names are unique. If a constraint is specified which has the same name as a previously
defined constraint, the new constraint replaces the existing one.

[bounds]

This does not directly contain any data, but may contain subsections b (linear bounds on variables)
and cone (cones).

[b]

Bound definition on one or several variables separated by comma (,). An upper or lower bound on a
variable replaces any earlier defined bound on that variable. If only one bound (upper or lower) is given
only this bound is replaced. This means that upper and lower bounds can be specified separately. So
the OPF bound definition:

```
[b]  x,y >= -10  [/b]
[b]  x,y <= 10   [/b]
```

results in the bound $-10 \le x, y \le 10$.

Specifies a cone. A cone is defined as a sequence of variables which belong to a single unique cone. The supported cone types are:

- quad: a quadratic cone of n variables $x_1, \ldots, x_n$ defines a constraint of the form

$$x_1^2 \geq \sum_{i=2}^{n} x_i^2, \quad x_1 \geq 0.$$

- rquad: a rotated quadratic cone of n variables $x_1, \ldots, x_n$ defines a constraint of the form

$$2x_1 x_2 \geq \sum_{i=3}^{n} x_i^2, \quad x_1, x_2 \geq 0.$$

- pexp: primal exponential cone of 3 variables x_1, x_2, x_3 defines a constraint of the form

$$x_1 \geq x_2 \exp(x_3/x_2), \quad x_1, x_2 \geq 0.$$

- ppow with parameter $0 < \alpha < 1$: primal power cone of n variables $x_1, \ldots, x_n$ defines a constraint of the form

$$x_1^{\alpha} x_2^{1-\alpha} \geq \sqrt{\sum_{j=3}^{n} x_j^2}, \quad x_1, x_2 \geq 0.$$

- dexp: dual exponential cone of 3 variables x_1, x_2, x_3 defines a constraint of the form

$$x_1 \geq -x_3 e^{-1} \exp(x_2/x_3), \quad x_3 \leq 0, x_1 \geq 0.$$

- dpow with parameter $0 < \alpha < 1$: dual power cone of n variables $x_1, \ldots, x_n$ defines a constraint of the form

$$\left(\frac{x_1}{\alpha}\right)^{\alpha} \left(\frac{x_2}{1-\alpha}\right)^{1-\alpha} \geq \sqrt{\sum_{j=3}^{n^t} x_j^2}, \quad x_1, x_2 \geq 0.$$

- zero: zero cone of n variables $x_1, \ldots, x_n$ defines a constraint of the form

$$x_1 = \cdots = x_n = 0$$

A [bounds]-section example:

```
[bounds]
[b]  0 <= x,y <= 10  [/b] # ranged bound
[b] 10 >= x,y >=  0  [/b] # ranged bound
[b]  0 <= x,y <= inf [/b] # using inf
[b]       x,y free   [/b] # free variables
# Let (x,y,z,w) belong to the cone K
[cone rquad] x,y,z,w  [/cone] # rotated quadratic cone
[cone ppow '3e-01' 'a'] x1, x2, x3 [/cone] # power cone with alpha=1/3 and name 'a'
[/bounds]
```

By default all variables are free.

[variables]

This defines an ordering of variables as they should appear in the problem. This is simply a space-separated list of variable names.

[integer]

This contains a space-separated list of variables and defines the constraint that the listed variables must be integer-valued.

[hints]

This may contain only non-essential data; for example estimates of the number of variables, constraints and non-zeros. Placed before all other sections containing data this may reduce the time spent reading the file.

In the `hints` section, any subsection which is not recognized by **MOSEK** is simply ignored. In this section a hint is defined as follows:

```
[hint ITEM] value [/hint]
```

The hints recognized by **MOSEK** are:

- `numvar` (number of variables),

- `numcon` (number of linear/quadratic constraints),

- `numanz` (number of linear non-zeros in constraints),

- `numqnz` (number of quadratic non-zeros in constraints).

[solutions]

This section can contain a set of full or partial solutions to a problem. Each solution must be specified using a `[solution]`-section, i.e.

```
[solutions]
[solution]...[/solution] #solution 1
[solution]...[/solution] #solution 2
#other solutions....
[solution]...[/solution] #solution n
[/solutions]
```

The syntax of a `[solution]`-section is the following:

```
[solution SOLTYPE status=STATUS]...[/solution]
```

where **SOLTYPE** is one of the strings

- `interior`, a non-basic solution,

- `basic`, a basic solution,

- `integer`, an integer solution,

and **STATUS** is one of the strings

- `UNKNOWN`,

- `OPTIMAL`,

- `INTEGER_OPTIMAL`,

- `PRIM_FEAS`,

- `DUAL_FEAS`,

- `PRIM_AND_DUAL_FEAS`,

- `NEAR_OPTIMAL`,

- `NEAR_PRIM_FEAS`,

- `NEAR_DUAL_FEAS`,

- `NEAR_PRIM_AND_DUAL_FEAS`,

- `PRIM_INFEAS_CER`,

- `DUAL_INFEAS_CER`,

- `NEAR_PRIM_INFEAS_CER`,

- `NEAR_DUAL_INFEAS_CER`,

- `NEAR_INTEGER_OPTIMAL`.

Most of these values are irrelevant for input solutions; when constructing a solution for simplex hot-start or an initial solution for a mixed integer problem the safe setting is `UNKNOWN`.

A `[solution]`-section contains `[con]` and `[var]` sections. Each `[con]` and `[var]` section defines solution information for a single variable or constraint, specified as list of KEYWORD/`value` pairs, in any order, written as

```
KEYWORD=value
```

Allowed keywords are as follows:

- `sk`. The status of the item, where the `value` is one of the following strings:

  - `LOW`, the item is on its lower bound.
  - `UPR`, the item is on its upper bound.
  - `FIX`, it is a fixed item.
  - `BAS`, the item is in the basis.
  - `SUPBAS`, the item is super basic.
  - `UNK`, the status is unknown.
  - `INF`, the item is outside its bounds (infeasible).

- `lvl` Defines the level of the item.

- `sl` Defines the level of the dual variable associated with its lower bound.

- `su` Defines the level of the dual variable associated with its upper bound.

- `sn` Defines the level of the variable associated with its cone.

- `y` Defines the level of the corresponding dual variable (for constraints only).

A `[var]` section should always contain the items `sk`, `lvl`, `sl` and `su`. Items `sl` and `su` are not required for `integer` solutions.

A `[con]` section should always contain `sk`, `lvl`, `sl`, `su` and `y`.

An example of a solution section

```
[solution basic status=UNKNOWN]
[var x0] sk=LOW    lvl=5.0        [/var]
[var x1] sk=UPR    lvl=10.0       [/var]
[var x2] sk=SUPBAS lvl=2.0  sl=1.5 su=0.0 [/var]


[con c0] sk=LOW    lvl=3.0 y=0.0 [/con]
[con c0] sk=UPR    lvl=0.0 y=5.0 [/con]
[/solution]
```

- `[vendor]` This contains solver/vendor specific data. It accepts one argument, which is a vendor ID – for **MOSEK** the ID is simply `mosek` – and the section contains the subsection `parameters` defining solver parameters. When reading a vendor section, any unknown vendor can be safely ignored. This is described later.

Comments using the `#` may appear anywhere in the file. Between the `#` and the following line-break any text may be written, including markup characters.

12.3.3 Numbers

Numbers, when used for parameter values or coefficients, are written in the usual way by the `printf` function. That is, they may be prefixed by a sign (`+` or `-`) and may contain an integer part, decimal part and an exponent. The decimal point is always `.` (a dot). Some examples are

```
1
1.0
.0
1.
1e10
1e+10
1e-10
```

Some *invalid* examples are

```
e10   # invalid, must contain either integer or decimal part
.     # invalid
.e10  # invalid
```

More formally, the following standard regular expression describes numbers as used:

```
[+|-]?([0-9]+[.][0-9]*|[.][0-9]+)([eE][+|-]?[0-9]+)?
```

12.3.4 Names

Variable names, constraint names and objective name may contain arbitrary characters, which in some cases must be enclosed by quotes (single or double) that in turn must be preceded by a backslash. Unquoted names must begin with a letter (`a-z` or `A-Z`) and contain only the following characters: the letters `a-z` and `A-Z`, the digits `0-9`, braces (`{` and `}`) and underscore (`_`).

Some examples of legal names:

```
an_unquoted_name
another_name{123}
'single quoted name'
"double quoted name"
"name with \\"quote\\" in it"
"name with []s in it"
```

12.3.5 Parameters Section

In the `vendor` section solver parameters are defined inside the `parameters` subsection. Each parameter is written as

```
[p PARAMETER_NAME] value [/p]
```

where `PARAMETER_NAME` is replaced by a **MOSEK** parameter name, usually of the form `MSK_IPAR_...`, `MSK_DPAR_...` or `MSK_SPAR_...`, and the `value` is replaced by the value of that parameter; both integer values and named values may be used. Some simple examples are

```
[vendor mosek]
[parameters]
[p MSK_IPAR_OPF_MAX_TERMS_PER_LINE] 10      [/p]
[p MSK_IPAR_OPF_WRITE_PARAMETERS]   MSK_ON [/p]
[p MSK_DPAR_DATA_TOL_BOUND_INF]     1.0e18 [/p]
[/parameters]
[/vendor]
```

12.3.6 Writing OPF Files from MOSEK

To write an OPF file then make sure the file extension is .opf.

Then modify the following parameters to define what the file should contain:

MSK_IPAR_OPF_WRITE_SOL_BAS	Include basic solution, if defined.
MSK_IPAR_OPF_WRITE_SOL_ITG	Include integer solution, if defined.
MSK_IPAR_OPF_WRITE_SOL_ITR	Include interior solution, if defined.
MSK_IPAR_OPF_WRITE_SOLUTIONS	Include solutions if they are defined. If this is off, no solutions are included.
MSK_IPAR_OPF_WRITE_HEADER	Include a small header with comments.
MSK_IPAR_OPF_WRITE_PROBLEM	Include the problem itself — objective, constraints and bounds.
MSK_IPAR_OPF_WRITE_PARAMETERS	Include all parameter settings.
MSK_IPAR_OPF_WRITE_HINTS	Include hints about the size of the problem.

12.3.7 Examples

This section contains a set of small examples written in OPF and describing how to formulate linear, quadratic and conic problems.

Linear Example `lo1.opf`

Consider the example:

$$\begin{array}{llrrrrrrrrrr}
\text{maximize} & 3x_0 & + & 1x_1 & + & 5x_2 & + & 1x_3 & & \\
\text{subject to} & 3x_0 & + & 1x_1 & + & 2x_2 & & & = & 30, \\
& 2x_0 & + & 1x_1 & + & 3x_2 & + & 1x_3 & \geq & 15, \\
& & & 2x_1 & & & + & 3x_3 & \leq & 25,
\end{array}$$

having the bounds

$$\begin{array}{rclcl}
0 & \leq & x_0 & \leq & \infty, \\
0 & \leq & x_1 & \leq & 10, \\
0 & \leq & x_2 & \leq & \infty, \\
0 & \leq & x_3 & \leq & \infty.
\end{array}$$

In the OPF format the example is displayed as shown in Listing 12.1.

Listing 12.1: Example of an OPF file for a linear problem.

```
[comment]
  The lo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 4 [/hint]
  [hint NUMCON] 3 [/hint]
  [hint NUMANZ] 9 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4
[/variables]

[objective maximize 'obj']
   3 x1 + x2 + 5 x3 + x4
[/objective]

[constraints]
  [con 'c1'] 3 x1 +   x2 + 2 x3          = 30 [/con]
  [con 'c2'] 2 x1 +   x2 + 3 x3 +   x4 >= 15 [/con]
  [con 'c3']         2 x2       + 3 x4 <= 25 [/con]
[/constraints]

[bounds]
```

```
  [b] 0 <= * [/b]
  [b] 0 <= x2 <= 10 [/b]
[/bounds]
```

Quadratic Example `qo1.opf`

An example of a quadratic optimization problem is

$$\begin{aligned}
\text{minimize} \quad & x_1^2 + 0.1x_2^2 + x_3^2 - x_1 x_3 - x_2 \\
\text{subject to} \quad 1 \leq \ & x_1 + x_2 + x_3, \\
& x \geq 0.
\end{aligned}$$

This can be formulated in `opf` as shown below.

Listing 12.2: Example of an OPF file for a quadratic problem.

```
[comment]
  The qo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 3 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
  [hint NUMQNZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3
[/variables]

[objective minimize 'obj']
  # The quadratic terms are often written with a factor of 1/2 as here,
  # but this is not required.

   - x2 + 0.5 ( 2.0 x1 ^ 2 - 2.0 x3 * x1 + 0.2 x2 ^ 2 + 2.0 x3 ^ 2 )
[/objective]

[constraints]
  [con 'c1'] 1.0 <= x1 + x2 + x3 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]
```

Conic Quadratic Example `cqo1.opf`

Consider the example:

$$\begin{aligned}
\text{minimize} \quad & x_3 + x_4 + x_5 \\
\text{subject to} \quad & x_0 + x_1 + 2x_2 \ = \ 1, \\
& x_0, x_1, x_2 \ \geq \ 0, \\
& x_3 \geq \sqrt{x_0^2 + x_1^2}, \\
& 2x_4 x_5 \geq x_2^2.
\end{aligned}$$

Please note that the type of the cones is defined by the parameter to `[cone ...]`; the content of the `cone`-section is the names of variables that belong to the cone. The resulting OPF file is in Listing 12.3.

Listing 12.3: Example of an OPF file for a conic quadratic problem.

```
[comment]
  The cqo1 example in OPF format.
[/comment]

[hints]
  [hint NUMVAR] 6 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4 x5 x6
[/variables]

[objective minimize 'obj']
   x4 + x5 + x6
[/objective]

[constraints]
  [con 'c1']  x1 + x2 + 2e+00 x3 = 1e+00 [/con]
[/constraints]

[bounds]
  # We let all variables default to the positive orthant
  [b] 0 <= * [/b]

  # ...and change those that differ from the default
  [b] x4,x5,x6 free [/b]

  # Define quadratic cone: x4 >= sqrt( x1^2 + x2^2 )
  [cone quad 'k1'] x4, x1, x2 [/cone]

  # Define rotated quadratic cone: 2 x5 x6 >= x3^2
  [cone rquad 'k2'] x5, x6, x3 [/cone]
[/bounds]
```

Mixed Integer Example `milo1.opf`

Consider the mixed integer problem:

$$
\begin{array}{lrcl}
\text{maximize} & x_0 + 0.64x_1 & & \\
\text{subject to} & 50x_0 + 31x_1 & \leq & 250, \\
& 3x_0 - 2x_1 & \geq & -4, \\
& x_0, x_1 \geq 0 & & \text{and integer}
\end{array}
$$

This can be implemented in OPF with the file in .

Listing 12.4: Example of an OPF file for a mixed-integer linear problem.

```
[comment]
  The milo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 2 [/hint]
  [hint NUMCON] 2 [/hint]
  [hint NUMANZ] 4 [/hint]
[/hints]
```

```
[variables disallow_new_variables]
  x1 x2
[/variables]

[objective maximize 'obj']
   x1 + 6.4e-1 x2
[/objective]

[constraints]
  [con 'c1'] 5e+1 x1 + 3.1e+1 x2 <= 2.5e+2 [/con]
  [con 'c2'] -4 <= 3 x1 - 2 x2 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]

[integer]
  x1 x2
[/integer]
```

12.4 The CBF Format

This document constitutes the technical reference manual of the *Conic Benchmark Format* with file extension: `.cbf` or `.CBF`. It unifies linear, second-order cone (also known as conic quadratic) and semidefinite optimization with mixed-integer variables. The format has been designed with benchmark libraries in mind, and therefore focuses on compact and easily parsable representations. The problem structure is separated from the problem data, and the format moreover facilitates benchmarking of hotstart capability through sequences of changes.

12.4.1 How Instances Are Specified

This section defines the spectrum of conic optimization problems that can be formulated in terms of the keywords of the CBF format.

In the CBF format, conic optimization problems are considered in the following form:

$$\begin{array}{ll} \min/\max & g^{obj} \\ & g_i \in \mathcal{K}_i, \quad i \in \mathcal{I}, \\ \text{s.t.} & G_i \in \mathcal{K}_i, \quad i \in \mathcal{I}^{PSD}, \\ & x_j \in \mathcal{K}_j, \quad j \in \mathcal{J}, \\ & \overline{X}_j \in \mathcal{K}_j, \quad j \in \mathcal{J}^{PSD}. \end{array} \tag{12.10}$$

- **Variables** are either scalar variables, x_j for $j \in \mathcal{J}$, or variables, $\overline{X}_j$ for $j \in \mathcal{J}^{PSD}$. Scalar variables can also be declared as integer.

- **Constraints** are affine expressions of the variables, either scalar-valued g_i for $i \in \mathcal{I}$, or matrix-valued G_i for $i \in \mathcal{I}^{PSD}$

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i.$$

- The **objective function** is a scalar-valued affine expression of the variables, either to be minimized or maximized. We refer to this expression as g^{obj}

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj}.$$

CBF format can represent the following cones $\mathcal{K}$:

- **Free domain** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n\}, \text{ for } n \geq 1.$$

- **Positive orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \geq 0 \text{ for } j = 1, \ldots, n\}, \text{ for } n \geq 1.$$

- **Negative orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \leq 0 \text{ for } j = 1, \ldots, n\}, \text{ for } n \geq 1.$$

- **Fixpoint zero** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j = 0 \text{ for } j = 1, \ldots, n\}, \text{ for } n \geq 1.$$

- **Quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R}^{n-1}, \; p^2 \geq x^T x, \; p \geq 0 \right\}, \text{ for } n \geq 2.$$

- **Rotated quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ q \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R} \times \mathbb{R}^{n-2}, \; 2pq \geq x^T x, \; p \geq 0, \; q \geq 0 \right\}, \text{ for } n \geq 3.$$

12.4.2 The Structure of CBF Files

This section defines how information is written in the CBF format, without being specific about the type of information being communicated.

All information items belong to exactly one of the three groups of information. These information groups, and the order they must appear in, are:

1. File format.

2. Problem structure.

3. Problem data.

The first group, file format, provides information on how to interpret the file. The second group, problem structure, provides the information needed to deduce the type and size of the problem instance. Finally, the third group, problem data, specifies the coefficients and constants of the problem instance.

Information items

The format is composed as a list of information items. The first line of an information item is the `KEYWORD`, revealing the type of information provided. The second line - of some keywords only - is the `HEADER`, typically revealing the size of information that follows. The remaining lines are the `BODY` holding the actual information to be specified.

```
KEYWORD
BODY

KEYWORD
HEADER
BODY
```

The `KEYWORD` determines how each line in the `HEADER` and `BODY` is structured. Moreover, the number of lines in the `BODY` follows either from the `KEYWORD`, the `HEADER`, or from another information item required to precede it.

Embedded hotstart-sequences

A sequence of problem instances, based on the same problem structure, is within a single file. This is facilitated via the `CHANGE` within the problem data information group, as a separator between the information items of each instance. The information items following a `CHANGE` keyword are appending to, or changing (e.g., setting coefficients back to their default value of zero), the problem data of the preceding instance.

The sequence is intended for benchmarking of hotstart capability, where the solvers can reuse their internal state and solution (subject to the achieved accuracy) as warmpoint for the succeeding instance. Whenever this feature is unsupported or undesired, the keyword `CHANGE` should be interpreted as the end of file.

File encoding and line width restrictions

The format is based on the US-ASCII printable character set with two extensions as listed below. Note, by definition, that none of these extensions can be misinterpreted as printable US-ASCII characters:

- A line feed marks the end of a line, carriage returns are ignored.

- Comment-lines may contain unicode characters in UTF-8 encoding.

The line width is restricted to 512 bytes, with 3 bytes reserved for the potential carriage return, line feed and null-terminator.

Integers and floating point numbers must follow the ISO C decimal string representation in the standard C locale. The format does not impose restrictions on the magnitude of, or number of significant digits in numeric data, but the use of 64-bit integers and 64-bit IEEE 754 floating point numbers should be sufficient to avoid loss of precision.

Comment-line and whitespace rules

The format allows single-line comments respecting the following rule:

- Lines having first byte equal to '#' (US-ASCII 35) are comments, and should be ignored. Comments are only allowed between information items.

Given that a line is not a comment-line, whitespace characters should be handled according to the following rules:

- Leading and trailing whitespace characters should be ignored.

  - The seperator between multiple pieces of information on one line, is either one or more whitespace characters.

- Lines containing only whitespace characters are empty, and should be ignored. Empty lines are only allowed between information items.

12.4.3 Problem Specification

The problem structure

The problem structure defines the objective sense, whether it is minimization and maximization. It also defines the index sets, $\mathcal{J}$, $\mathcal{J}^{PSD}$, $\mathcal{I}$ and $\mathcal{I}^{PSD}$, which are all numbered from zero, $\{0, 1, \ldots\}$, and empty until explicitly constructed.

- **Scalar variables** are constructed in vectors restricted to a conic domain, such as $(x_0, x_1) \in \mathbb{R}^2_+$, $(x_2, x_3, x_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$x \in \mathcal{K}_1^{n_1} \times \mathcal{K}_2^{n_2} \times \cdots \times \mathcal{K}_k^{n_k}$$

  which in the CBF format becomes:

```
VAR
n k
K1 n1
K2 n2
...
Kk nk
```

  where $\sum_i n_i = n$ is the total number of scalar variables. The list of supported cones is found in Table 12.3. Integrality of scalar variables can be specified afterwards.

- **PSD variables** are constructed one-by-one. That is, $X_j \succeq \mathbf{0}^{n_j \times n_j}$ for $j \in \mathcal{J}^{PSD}$, constructs a matrix-valued variable of size $n_j \times n_j$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes:

```
PSDVAR
N
n1
n2
...
nN
```

  where N is the total number of PSD variables.

- **Scalar constraints** are constructed in vectors restricted to a conic domain, such as $(g_0, g_1) \in \mathbb{R}^2_+$, $(g_2, g_3, g_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$g \in \mathcal{K}_1^{m_1} \times \mathcal{K}_2^{m_2} \times \cdots \times \mathcal{K}_k^{m_k}$$

  which in the CBF format becomes:

```
CON
m k
K1 m1
K2 m2
..
Kk mk
```

  where $\sum_i m_i = m$ is the total number of scalar constraints. The list of supported cones is found in Table 12.3.

- **PSD constraints** are constructed one-by-one. That is, $G_i \succeq \mathbf{0}^{m_i \times m_i}$ for $i \in \mathcal{I}^{PSD}$, constructs a matrix-valued affine expressions of size $m_i \times m_i$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes

```
PSDCON
M
m1
m2
..
mM
```

where M is the total number of PSD constraints.

With the objective sense, variables (with integer indications) and constraints, the definitions of the many affine expressions follow in problem data.

Problem data

The problem data defines the coefficients and constants of the affine expressions of the problem instance. These are considered zero until explicitly defined, implying that instances with no keywords from this information group are, in fact, valid. Duplicating or conflicting information is a failure to comply with the standard. Consequently, two coefficients written to the same position in a matrix (or to transposed positions in a symmetric matrix) is an error.

The affine expressions of the objective, g^{obj}, of the scalar constraints, g_i, and of the PSD constraints, G_i, are defined separately. The following notation uses the standard trace inner product for matrices, $\langle X, Y \rangle = \sum_{i,j} X_{ij} Y_{ij}$.

- The affine expression of the objective is defined as

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj},$$

in terms of the symmetric matrices, F_j^{obj}, and scalars, a_j^{obj} and b^{obj}.

- The affine expressions of the scalar constraints are defined, for $i \in \mathcal{I}$, as

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

in terms of the symmetric matrices, F_{ij}, and scalars, a_{ij} and b_i.

- The affine expressions of the PSD constraints are defined, for $i \in \mathcal{I}^{PSD}$, as

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i,$$

in terms of the symmetric matrices, H_{ij} and D_i.

List of cones

The format uses an explicit syntax for symmetric positive semidefinite cones as shown above. For scalar variables and constraints, constructed in vectors, the supported conic domains and their minimum sizes are given as follows.

Table 12.3: Cones available in the CBF format

Name	CBF keyword	Cone family
Free domain	F	linear
Positive orthant	L+	linear
Negative orthant	L-	linear
Fixpoint zero	L=	linear
Quadratic cone	Q	second-order
Rotated quadratic cone	QR	second-order

12.4.4 File Format Keywords

VER

Description: The version of the Conic Benchmark Format used to write the file.
HEADER: None
BODY: One line formatted as:

```
INT
```

This is the version number.
Must appear exactly once in a file, as the first keyword.

OBJSENSE

Description: Define the objective sense.
    HEADER: None
    BODY: One line formatted as:

```
STR
```

having `MIN` indicates minimize, and `MAX` indicates maximize. Capital letters are required.
Must appear exactly once in a file.

PSDVAR

Description: Construct the PSD variables.
    HEADER: One line formatted as:

```
INT
```

This is the number of PSD variables in the problem.
    BODY: A list of lines formatted as:

```
INT
```

This indicates the number of rows (equal to the number of columns) in the matrix-valued PSD variable. The number of lines should match the number stated in the header.

VAR

Description: Construct the scalar variables.
    HEADER: One line formatted as:

```
INT INT
```

This is the number of scalar variables, followed by the number of conic domains they are restricted to.
    BODY: A list of lines formatted as:

```
STR INT
```

This indicates the cone name (see Table 12.3), and the number of scalar variables restricted to this cone. These numbers should add up to the number of scalar variables stated first in the header. The number of lines should match the second number stated in the header.

INT

Description: Declare integer requirements on a selected subset of scalar variables.
    HEADER: one line formatted as:

```
INT
```

This is the number of integer scalar variables in the problem.
    BODY: a list of lines formatted as:

```
INT
```

This indicates the scalar variable index $j \in \mathcal{J}$. The number of lines should match the number stated in the header.
Can only be used after the keyword `VAR`.

PSDCON

Description: Construct the PSD constraints.
    HEADER: One line formatted as:

```
INT
```

This is the number of PSD constraints in the problem.
    BODY: A list of lines formatted as:

```
INT
```

This indicates the number of rows (equal to the number of columns) in the matrix-valued affine expression of the PSD constraint. The number of lines should match the number stated in the header.
    Can only be used after these keywords: PSDVAR, VAR.

CON

Description: Construct the scalar constraints.
    HEADER: One line formatted as:

```
INT INT
```

This is the number of scalar constraints, followed by the number of conic domains they restrict to.
    BODY: A list of lines formatted as:

```
STR INT
```

This indicates the cone name (see Table 12.3), and the number of affine expressions restricted to this cone. These numbers should add up to the number of scalar constraints stated first in the header. The number of lines should match the second number stated in the header.
    Can only be used after these keywords: PSDVAR, VAR

OBJFCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices F_j^{obj}, as used in the objective.
    HEADER: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.
    BODY: A list of lines formatted as:

```
INT INT INT REAL
```

This indicates the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

OBJACOORD

Description: Input sparse coordinates (pairs) to define the scalars, a_j^{obj}, as used in the objective.
    HEADER: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.
    BODY: A list of lines formatted as:

```
INT REAL
```

This indicates the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

OBJBCOORD

Description: Input the scalar, b^{obj}, as used in the objective.
    HEADER: None.
    BODY: One line formatted as:

```
REAL
```

    This indicates the coefficient value.

FCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, F_{ij}, as used in the scalar constraints.
    HEADER: One line formatted as:

```
INT
```

    This is the number of coordinates to be specified.
    BODY: A list of lines formatted as:

```
INT INT INT INT REAL
```

    This indicates the scalar constraint index $i \in \mathcal{I}$, the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

ACOORD

Description: Input sparse coordinates (triplets) to define the scalars, a_{ij}, as used in the scalar constraints.
    HEADER: One line formatted as:

```
INT
```

    This is the number of coordinates to be specified.
    BODY: A list of lines formatted as:

```
INT INT REAL
```

    This indicates the scalar constraint index $i \in \mathcal{I}$, the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

BCOORD

Description: Input sparse coordinates (pairs) to define the scalars, b_i, as used in the scalar constraints.
    HEADER: One line formatted as:

```
INT
```

    This is the number of coordinates to be specified.
    BODY: A list of lines formatted as:

```
INT REAL
```

    This indicates the scalar constraint index $i \in \mathcal{I}$ and the coefficient value. The number of lines should match the number stated in the header.

HCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, H_{ij}, as used in the PSD constraints.
    HEADER: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.

BODY: A list of lines formatted as

```
INT INT INT INT REAL
```

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the scalar variable index $j \in \mathcal{J}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

DCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices, D_i, as used in the PSD constraints.

HEADER: One line formatted as

```
INT
```

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

```
INT INT INT REAL
```

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

CHANGE

Start of a new instance specification based on changes to the previous. Can be interpreted as the end of file when the hotstart-sequence is unsupported or undesired.

BODY: None

Header: None

12.4.5 CBF Format Examples

Minimal Working Example

The conic optimization problem (12.11) , has three variables in a quadratic cone - first one is integer - and an affine expression in domain 0 (equality constraint).

$$
\begin{array}{ll}
\text{minimize} & 5.1\,x_0 \\
\text{subject to} & 6.2\,x_1 + 7.3\,x_2 - 8.4 \in \{0\} \\
& x \in \mathcal{Q}^3,\ x_0 \in \mathbb{Z}.
\end{array}
\tag{12.11}
$$

Its formulation in the Conic Benchmark Format begins with the version of the CBF format used, to safeguard against later revisions.

```
VER
1
```

Next follows the problem structure, consisting of the objective sense, the number and domain of variables, the indices of integer variables, and the number and domain of scalar-valued affine expressions (i.e., the equality constraint).

```
OBJSENSE
MIN

VAR
3 1
Q 3

INT
1
0
```

```
CON
1 1
L= 1
```

Finally follows the problem data, consisting of the coefficients of the objective, the coefficients of the constraints, and the constant terms of the constraints. All data is specified on a sparse coordinate form.

```
OBJACOORD
1
0 5.1

ACOORD
2
0 1 6.2
0 2 7.3

BCOORD
1
0 -8.4
```

This concludes the example.

Mixing Linear, Second-order and Semidefinite Cones

The conic optimization problem (12.12), has a semidefinite cone, a quadratic cone over unordered subindices, and two equality constraints.

$$
\begin{aligned}
\text{minimize} \quad & \left\langle \begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}, X_1 \right\rangle + x_1 \\
\text{subject to} \quad & \left\langle \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 & = & 1.0, \\
& \left\langle \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, X_1 \right\rangle + x_0 + x_2 & = & 0.5, \\
& x_1 \geq \sqrt{x_0^2 + x_2^2}, \\
& X_1 \succeq \mathbf{0}.
\end{aligned}
\tag{12.12}
$$

The equality constraints are easily rewritten to the conic form, $(g_0, g_1) \in \{0\}^2$, by moving constants such that the right-hand-side becomes zero. The quadratic cone does not fit under the VAR keyword in this variable permutation. Instead, it takes a scalar constraint $(g_2, g_3, g_4) = (x_1, x_0, x_2) \in \mathcal{Q}^3$, with scalar variables constructed as $(x_0, x_1, x_2) \in \mathbb{R}^3$. Its formulation in the CBF format is reported in the following list

```
# File written using this version of the Conic Benchmark Format:
#     | Version 1.
VER
1

# The sense of the objective is:
#     | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#     | Three times three.
PSDVAR
1
3
```

```
# Three scalar variables in this one conic domain:
#       | Three are free.
VAR
3 1
F 3

# Five scalar constraints with affine expressions in two conic domains:
#       | Two are fixed to zero.
#       | Three are in conic quadratic domain.
CON
5 2
L= 2
Q 3

# Five coordinates in F^{obj}_j coefficients:
#       | F^{obj}[0][0,0] = 2.0
#       | F^{obj}[0][1,0] = 1.0
#       | and more...
OBJFCOORD
5
0 0 0 2.0
0 1 0 1.0
0 1 1 2.0
0 2 1 1.0
0 2 2 2.0

# One coordinate in a^{obj}_j coefficients:
#       | a^{obj}[1] = 1.0
OBJACOORD
1
1 1.0

# Nine coordinates in F_ij coefficients:
#       | F[0,0][0,0] = 1.0
#       | F[0,0][1,1] = 1.0
#       | and more...
FCOORD
9
0 0 0 0 1.0
0 0 1 1 1.0
0 0 2 2 1.0
1 0 0 0 1.0
1 0 1 0 1.0
1 0 2 0 1.0
1 0 1 1 1.0
1 0 2 1 1.0
1 0 2 2 1.0

# Six coordinates in a_ij coefficients:
#     | a[0,1] = 1.0
#     | a[1,0] = 1.0
#     | and more...
ACOORD
6
0 1 1.0
1 0 1.0
1 2 1.0
2 1 1.0
3 0 1.0
4 2 1.0
```

```
# Two coordinates in b_i coefficients:
#      | b[0] = -1.0
#      | b[1] = -0.5
BCOORD
2
0 -1.0
1 -0.5
```

Mixing Semidefinite Variables and Linear Matrix Inequalities

The standard forms in semidefinite optimization are usually based either on semidefinite variables or linear matrix inequalities. In the CBF format, both forms are supported and can even be mixed as shown in.

$$
\begin{aligned}
\text{minimize} \quad & \left\langle \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 + x_2 + 1 \\
\text{subject to} \quad & \left\langle \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, X_1 \right\rangle - x_1 - x_2 \geq 0.0, \\
& x_1 \begin{bmatrix} 0 & 1 \\ 1 & 3 \end{bmatrix} + x_2 \begin{bmatrix} 3 & 1 \\ 1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \succeq \mathbf{0}, \\
& X_1 \succeq \mathbf{0}.
\end{aligned}
\tag{12.13}
$$

Its formulation in the CBF format is written in what follows

```
# File written using this version of the Conic Benchmark Format:
#      | Version 1.
VER
1

# The sense of the objective is:
#      | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#      | Two times two.
PSDVAR
1
2

# Two scalar variables in this one conic domain:
#      | Two are free.
VAR
2 1
F 2

# One PSD constraint of this size:
#      | Two times two.
PSDCON
1
2

# One scalar constraint with an affine expression in this one conic domain:
#      | One is greater than or equal to zero.
CON
1 1
L+ 1

# Two coordinates in F^{obj}_j coefficients:
```

```
#       | F^{obj}[0][0,0] = 1.0
#       | F^{obj}[0][1,1] = 1.0
OBJFCOORD
2
0 0 0 1.0
0 1 1 1.0

# Two coordinates in a^{obj}_j coefficients:
#       | a^{obj}[0] = 1.0
#       | a^{obj}[1] = 1.0
OBJACOORD
2
0 1.0
1 1.0

# One coordinate in b^{obj} coefficient:
#       | b^{obj} = 1.0
OBJBCOORD
1.0

# One coordinate in F_ij coefficients:
#       | F[0,0][1,0] = 1.0
FCOORD
1
0 0 1 0 1.0

# Two coordinates in a_ij coefficients:
#       | a[0,0] = -1.0
#       | a[0,1] = -1.0
ACOORD
2
0 0 -1.0
0 1 -1.0

# Four coordinates in H_ij coefficients:
#       | H[0,0][1,0] = 1.0
#       | H[0,0][1,1] = 3.0
#       | and more...
HCOORD
4
0 0 1 0 1.0
0 0 1 1 3.0
0 1 0 0 3.0
0 1 1 0 1.0

# Two coordinates in D_i coefficients:
#       | D[0][0,0] = -1.0
#       | D[0][1,1] = -1.0
DCOORD
2
0 0 0 -1.0
0 1 1 -1.0
```

Optimization Over a Sequence of Objectives

The linear optimization problem (12.14), is defined for a sequence of objectives such that hotstarting from one to the next might be advantages.

$$
\begin{aligned}
\text{maximize}_k \quad & g_k^{obj} \\
\text{subject to} \quad & 50\,x_0 + 31 && \leq && 250\,, \\
& 3\,x_0 - 2x_1 && \geq && -4\,, \\
& x \in \mathbb{R}_+^2\,,
\end{aligned}
\tag{12.14}
$$

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given,

1. $g_0^{obj} = x_0 + 0.64x_1$.

2. $g_1^{obj} = 1.11x_0 + 0.76x_1$.

3. $g_2^{obj} = 1.11x_0 + 0.85x_1$.

Its formulation in the CBF format is reported in Listing 12.5.

Listing 12.5: Problem (12.14) in CBF format.

```
# File written using this version of the Conic Benchmark Format:
#       | Version 1.
VER
1

# The sense of the objective is:
#       | Maximize.
OBJSENSE
MAX

# Two scalar variables in this one conic domain:
#       | Two are nonnegative.
VAR
2 1
L+ 2

# Two scalar constraints with affine expressions in these two conic domains:
#       | One is in the nonpositive domain.
#       | One is in the nonnegative domain.
CON
2 2
L- 1
L+ 1

# Two coordinates in a^{obj}_j coefficients:
#       | a^{obj}[0] = 1.0
#       | a^{obj}[1] = 0.64
OBJACOORD
2
0 1.0
1 0.64

# Four coordinates in a_ij coefficients:
#       | a[0,0] = 50.0
#       | a[1,0] = 3.0
#       | and more...
ACOORD
4
0 0 50.0
1 0 3.0
0 1 31.0
1 1 -2.0

# Two coordinates in b_i coefficients:
#       | b[0] = -250.0
#       | b[1] = 4.0
BCOORD
2
0 -250.0
1 4.0
```

```
# New problem instance defined in terms of changes.
CHANGE

# Two coordinate changes in a^{obj}_j coefficients. Now it is:
#       | a^{obj}[0] = 1.11
#       | a^{obj}[1] = 0.76
OBJACOORD
2
0 1.11
1 0.76


# New problem instance defined in terms of changes.
CHANGE

# One coordinate change in a^{obj}_j coefficients. Now it is:
#       | a^{obj}[0] = 1.11
#       | a^{obj}[1] = 0.85
OBJACOORD
1
1 0.85
```

12.5 The PTF Format

The PTF format is a new human-readable, natural text format. Its features and structure are similar to the OPF format, with the difference that the PTF format **does** support semidefinite terms.

12.5.1 The overall format

The format is indentation based, where each section is started by a head line and followed by a section body with deeper indentation that the head line. For example:

```
Header line
   Body line 1
   Body line 1
   Body line 1
```

Section can also be nested:

```
Header line A
   Body line in A
   Header line A.1
      Body line in A.1
      Body line in A.1
   Body line in A
```

The indentation of blank lines is ignored, so a subsection can contain a blank line with no indentation. The character # defines a line comment and anything between the # character and the end of the line is ignored.

In a PTF file, the first section must be a `Task` section. The order of the remaining section is arbitrary, and sections may occur multiple times or not at all.

MOSEK will ignore any top-level section it does not recognize.

Names

In the description of the format we use following definitions for name strings:

```
NAME: PLAIN_NAME | QUOTED_NAME
PLAIN_NAME: [a-zA-Z_] [a-zA-Z0-9_-.!|]
QUOTED_NAME: "'" ( [^'\\\r\n] | "\\" ( [\\rn] | "x" [0-9a-fA-F] [0-9a-fA-F] ) )* "'"
```

Expressions

An expression is a sum of terms. A term is either a linear term (a coefficient and a variable name, where the coefficient can be left out if it is 1.0), or a matrix inner product.

An expression:

```
EXPR: EMPTY | [+-]? TERM ( [+-] TERM )*
TERM: LINEAR_TERM | MATRIX_TERM
```

A linear term

```
LINEAR_TERM: FLOAT? NAME
```

A matrix term

```
MATRIX_TERM: "<" FLOAT? NAME ( [+-] FLOAT? NAME)* ";" NAME ">"
```

Here the right-hand name is the name of a (semidefinite) matrix variable, and the left-hand side is a sum of symmetric matrixes. The actual matrixes are defined in a separate section.

Expressions can span multiple lines by giving subsequent lines a deeper indentation.

For example following two section are equivalent:

```
# Everything on one line:
x1 + x2 + x3 + x4

# Split into multiple lines:
x1
  + x2
  + x3
  + x4
```

12.5.2 `Task` section

The first section of the file must be a `Task`. The text in this section is not used and may contain comments, or meta-information from the writer or about the content.

Format:

```
Task NAME
   Anything goes here...
```

`NAME` is a the task name.

12.5.3 `Objective` section

The `Objective` section defines the objective name, sense and function. The format:

```
"Objective" NAME?
   ( "Minimize" | "Maximize" ) EXPR
```

For example:

```
Objective 'obj'
   Minimize x1 + 0.2 x2 + < M1 ; X1 >
```

12.5.4 `Constraints` section

The constraints section defines a series of constraints. A constraint defines a term $A \cdot x + b \in K$. For linear constraints `A` is just one row, while for conic constraints it can be multiple rows. If a constraint spans multiple rows these can either be written inline separated by semi-colons, or each expression in a separete sub-section.

Simple linear constraints:

```
"Constraints"
  NAME? "[" [-+] (FLOAT | "Inf") (";" [-+] (FLOAT | "Inf") )? "]" EXPR
```

If the brackets contain two values, they are used as upper and lower bounds. It they contain one value the constraint is an equality.

For example:

```
Constraints
  'c1' [0;10] x1 + x2 + x3
  [0] x1 + x2 + x3
```

Constraint blocks put the expression either in a subsection or inline. The cone type (domain) is written in the brackets, and **MOSEK** currently supports following types:

- `SOC(N)` Second order cone of dimension `N`

- `RSOC(N)` Rotated second order cone of dimension `N`

- `PSD(N)` Symmetric positive semidefinite cone of dimension `N`. This contains `N*(N+1)/2` elements.

- `PEXP` Primal exponential cone of dimension 3

- `DEXP` Dual exponential cone of dimension 3

- `PPOW(N,P)` Primal power cone of dimension `N` with parameter `P`

- `DPOW(N,P)` Dual power cone of dimension `N` with parameter `P`

- `ZERO(N)` The zero-cone of dimension `N`.

```
"Constraints"
  NAME? "[" DOMAIN "]" EXPR_LIST
```

For example:

```
Constraints
  'K1' [SOC(3)] x1 + x2 ; x2 + x3 ; x3 + x1
  'K2' [RSOC(3)]
     x1 + x2
     x2 + x3
     x3 + x1
```

12.5.5 `Variables` **section**

Any variable used in an expression must be defined in a variable section. The variable section defines each variable domain.

```
"Variables"
  NAME "[" [-+] (FLOAT | "Inf") (";" [-+] (FLOAT | "Inf") )? "]"
  NAME "[" DOMAIN "]" NAMES

  For example, a linear variable
```

```
Variables
  x1 [0;Inf]
```

As with constraints, members of a conic domain can be listed either inline or in a subsection:

```
Variables
  k1 [SOC(3)] x1 ; x2 ; x3
  k2 [RSOC(3)]
     x1
     x2
     x3
```

12.5.6 `Integer` **section**

This section contains a list of variables that are integral. For example:

```
Integer
   x1 x2 x3
```

12.5.7 `SymmetricMatrixes` **section**

This section defines the symmetric matrixes used for matrix coefficients in matrix inner product terms. The section lists named matrixes, each with a size and a number of non-zeros. Only non-zeros in the lower triangular part should be defined.

```
"SymmetricMatrixes"
   NAME "SYMMAT" "(" INT ")"  ( "(" INT "," INT "," FLOAT ")" )*
   ...
```

For example:

```
SymmetricMatrixes
   M1 SYMMAT(3) (0,0,1.0) (1,1,2.0) (2,1,0.5)
   M2 SYMMAT(3)
      (0,0,1.0)
      (1,1,2.0)
      (2,1,0.5)
```

12.5.8 `Solutions` **section**

Each subsection defines a solution. A solution defines for each constraint and for each variable exactly one primal value and either one (for conic domains) or two (for linear domains) dual values. The values follow the same logic as in the **MOSEK** C API. A primal and a dual solution status defines the meaning of the values primal and dual (solution, certificate, unknown, etc.)

The format is this:

```
"Solutions"
   "Solution" WHICHSOL
      "ProblemStatus" PROSTA PROSTA?
   "SolutionStatus" SOLSTA SOLSTA?
   "Objective" FLOAT FLOAT
   "Variables"
      # Linear variable status: level, slx, sux
      NAME "[" STATUS "]" FLOAT (FLOAT FLOAT)?
      # Conic variable status: level, snx
      NAME
         "[" STATUS "]" FLOAT FLOAT?
         ...
   "Constraints"
      # Linear variable status: level, slx, sux
      NAME "[" STATUS "]" FLOAT (FLOAT FLOAT)?
      # Conic variable status: level, snx
      NAME
         "[" STATUS "]" FLOAT FLOAT?
         ...
```

Following values for `WHICHSOL` are supported:

- `interior` Interior solution, the result of an interior-point solver.

- `basic` Basic solution, as produced by a simplex solver.

- `integer` Integer solution, the solution to a mixed-integer problem. This does not define a dual solution.

Following values for `PROSTA` are supported:

- `unknown` The problem status is unknown

- `feasible` The problem has been proven feasible

- `infeasible` The problem has been proven infeasible

- `illposed` The problem has been proved to be ill posed

- `infeasible_or_unbounded` The problem is infeasible or unbounded

Following values for `SOLSTA` are supported:

- `unknown` The solution status is unknown

- `feasible` The solution is feasible

- `optimal` The solution is optimal

- `infeas_cert` The solution is a certificate of infeasibility

- `illposed_cert` The solution is a certificate of illposedness

Following values for `STATUS` are supported:

- `unknown` The value is unknown

- `super_basic` The value is super basic

- `at_lower` The value is basic and at its lower bound

- `at_upper` The value is basic and at its upper bound

- `fixed` The value is basic fixed

- `infinite` The value is at infinity

12.6 The Task Format

The Task format is **MOSEK**'s native binary format. It contains a complete image of a **MOSEK** task, i.e.

- Problem data: Linear, conic, semidefinite and quadratic data

- Problem item names: Variable names, constraints names, cone names etc.

- Parameter settings

- Solutions

There are a few things to be aware of:

- Status of a solution read from a file will *always* be unknown.

- Parameter settings in a task file *always override* any parameters set on the command line or in a parameter file.

The format is based on the *TAR* (USTar) file format. This means that the individual pieces of data in a `.task` file can be examined by unpacking it as a *TAR* file. Please note that the inverse may not work: Creating a file using *TAR* will most probably not create a valid **MOSEK** Task file since the order of the entries is important.

12.7 The JSON Format

MOSEK provides the possibility to read/write problems in valid JSON format.

JSON (JavaScript Object Notation) is a lightweight data-interchange format. It is easy for humans to read and write. It is easy for machines to parse and generate. It is based on a subset of the JavaScript Programming Language, Standard ECMA-262 3rd Edition - December 1999. JSON is a text format that is completely language independent but uses conventions that are familiar to programmers of the C-family of languages, including C, C++, C#, Java, JavaScript, Perl, Python, and many others. These properties make JSON an ideal data-interchange language.

The official JSON website http://www.json.org provides plenty of information along with the format definition.

MOSEK defines two JSON-like formats:

- jtask

- jsol

Despite being text-based human-readable formats, *jtask* and *jsol* files will include no indentation and no new-lines, in order to keep the files as compact as possible. We therefore strongly advise to use JSON viewer tools to inspect *jtask* and *jsol* files.

12.7.1 *jtask* format

It stores a problem instance. The *jtask* format contains the same information as a *task format*. Even though a *jtask* file is human-readable, we do not recommend users to create it by hand, but to rely on **MOSEK**.

12.7.2 *jsol* format

It stores a problem solution. The *jsol* format contains all solutions and information items.

12.7.3 A *jtask* example

In Listing 12.6 we present a file in the *jtask* format that corresponds to the sample problem from `lo1.lp`. The listing has been formatted for readability.

Listing 12.6: A formatted *jtask* file for the `lo1.lp` example.

```
{
    "$schema":"http://mosek.com/json/schema#",
    "Task/INFO":{
        "taskname":"lo1",
        "numvar":4,
        "numcon":3,
        "numcone":0,
        "numbarvar":0,
        "numanz":9,
        "numsymmat":0,
        "mosekver":[
            8,
            0,
            0,
            9
        ]
    },
    "Task/data":{
        "var":{
            "name":[
                "x1",
                "x2",
                "x3",
```

```
                    "x4"
                ],
                "bk":[
                    "lo",
                    "ra",
                    "lo",
                    "lo"
                ],
                "bl":[
                    0.0,
                    0.0,
                    0.0,
                    0.0
                ],
                "bu":[
                    1e+30,
                    1e+1,
                    1e+30,
                    1e+30
                ],
                "type":[
                    "cont",
                    "cont",
                    "cont",
                    "cont"
                ]
            },
            "con":{
                "name":[
                    "c1",
                    "c2",
                    "c3"
                ],
                "bk":[
                    "fx",
                    "lo",
                    "up"
                ],
                "bl":[
                    3e+1,
                    1.5e+1,
                        -1e+30
                ],
                "bu":[
                    3e+1,
                    1e+30,
                    2.5e+1
                ]
            },
            "objective":{
                "sense":"max",
                "name":"obj",
                "c":{
                    "subj":[
                        0,
                        1,
                        2,
                        3
                    ],
                    "val":[
                        3e+0,
```

```
                        1e+0,
                        5e+0,
                        1e+0
                    ]
                },
                "cfix":0.0
            },
            "A":{
                "subi":[
                    0,
                    0,
                    0,
                    1,
                    1,
                    1,
                    1,
                    2,
                    2
                ],
                "subj":[
                    0,
                    1,
                    2,
                    0,
                    1,
                    2,
                    3,
                    1,
                    3
                ],
                "val":[
                    3e+0,
                    1e+0,
                    2e+0,
                    2e+0,
                    1e+0,
                    3e+0,
                    1e+0,
                    2e+0,
                    3e+0
                ]
            }
        },
        "Task/parameters":{
            "iparam":{
                "ANA_SOL_BASIS":"ON",
                "ANA_SOL_PRINT_VIOLATED":"OFF",
                "AUTO_SORT_A_BEFORE_OPT":"OFF",
                "AUTO_UPDATE_SOL_INFO":"OFF",
                "BASIS_SOLVE_USE_PLUS_ONE":"OFF",
                "BI_CLEAN_OPTIMIZER":"OPTIMIZER_FREE",
                "BI_IGNORE_MAX_ITER":"OFF",
                "BI_IGNORE_NUM_ERROR":"OFF",
                "BI_MAX_ITERATIONS":1000000,
                "CACHE_LICENSE":"ON",
                "CHECK_CONVEXITY":"CHECK_CONVEXITY_FULL",
                "COMPRESS_STATFILE":"ON",
                "CONCURRENT_NUM_OPTIMIZERS":2,
                "CONCURRENT_PRIORITY_DUAL_SIMPLEX":2,
                "CONCURRENT_PRIORITY_FREE_SIMPLEX":3,
                "CONCURRENT_PRIORITY_INTPNT":4,
```

```
                    "CONCURRENT_PRIORITY_PRIMAL_SIMPLEX":1,
                    "FEASREPAIR_OPTIMIZE":"FEASREPAIR_OPTIMIZE_NONE",
                    "INFEAS_GENERIC_NAMES":"OFF",
                    "INFEAS_PREFER_PRIMAL":"ON",
                    "INFEAS_REPORT_AUTO":"OFF",
                    "INFEAS_REPORT_LEVEL":1,
                    "INTPNT_BASIS":"BI_ALWAYS",
                    "INTPNT_DIFF_STEP":"ON",
                    "INTPNT_FACTOR_DEBUG_LVL":0,
                    "INTPNT_FACTOR_METHOD":0,
                    "INTPNT_HOTSTART":"INTPNT_HOTSTART_NONE",
                    "INTPNT_MAX_ITERATIONS":400,
                    "INTPNT_MAX_NUM_COR":-1,
                    "INTPNT_MAX_NUM_REFINEMENT_STEPS":-1,
                    "INTPNT_OFF_COL_TRH":40,
                    "INTPNT_ORDER_METHOD":"ORDER_METHOD_FREE",
                    "INTPNT_REGULARIZATION_USE":"ON",
                    "INTPNT_SCALING":"SCALING_FREE",
                    "INTPNT_SOLVE_FORM":"SOLVE_FREE",
                    "INTPNT_STARTING_POINT":"STARTING_POINT_FREE",
                    "LIC_TRH_EXPIRY_WRN":7,
                    "LICENSE_DEBUG":"OFF",
                    "LICENSE_PAUSE_TIME":0,
                    "LICENSE_SUPPRESS_EXPIRE_WRNS":"OFF",
                    "LICENSE_WAIT":"OFF",
                    "LOG":10,
                    "LOG_ANA_PRO":1,
                    "LOG_BI":4,
                    "LOG_BI_FREQ":2500,
                    "LOG_CHECK_CONVEXITY":0,
                    "LOG_CONCURRENT":1,
                    "LOG_CUT_SECOND_OPT":1,
                    "LOG_EXPAND":0,
                    "LOG_FACTOR":1,
                    "LOG_FEAS_REPAIR":1,
                    "LOG_FILE":1,
                    "LOG_HEAD":1,
                    "LOG_INFEAS_ANA":1,
                    "LOG_INTPNT":4,
                    "LOG_MIO":4,
                    "LOG_MIO_FREQ":1000,
                    "LOG_OPTIMIZER":1,
                    "LOG_ORDER":1,
                    "LOG_PRESOLVE":1,
                    "LOG_RESPONSE":0,
                    "LOG_SENSITIVITY":1,
                    "LOG_SENSITIVITY_OPT":0,
                    "LOG_SIM":4,
                    "LOG_SIM_FREQ":1000,
                    "LOG_SIM_MINOR":1,
                    "LOG_STORAGE":1,
                    "MAX_NUM_WARNINGS":10,
                    "MIO_BRANCH_DIR":"BRANCH_DIR_FREE",
                    "MIO_CONSTRUCT_SOL":"OFF",
                    "MIO_CUT_CLIQUE":"ON",
                    "MIO_CUT_CMIR":"ON",
                    "MIO_CUT_GMI":"ON",
                    "MIO_CUT_KNAPSACK_COVER":"OFF",
                    "MIO_HEURISTIC_LEVEL":-1,
                    "MIO_MAX_NUM_BRANCHES":-1,
                    "MIO_MAX_NUM_RELAXS":-1,
```

```
                    "MIO_MAX_NUM_SOLUTIONS":-1,
                    "MIO_MODE":"MIO_MODE_SATISFIED",
                    "MIO_MT_USER_CB":"ON",
                    "MIO_NODE_OPTIMIZER":"OPTIMIZER_FREE",
                    "MIO_NODE_SELECTION":"MIO_NODE_SELECTION_FREE",
                    "MIO_PERSPECTIVE_REFORMULATE":"ON",
                    "MIO_PROBING_LEVEL":-1,
                    "MIO_RINS_MAX_NODES":-1,
                    "MIO_ROOT_OPTIMIZER":"OPTIMIZER_FREE",
                    "MIO_ROOT_REPEAT_PRESOLVE_LEVEL":-1,
                    "MT_SPINCOUNT":0,
                    "NUM_THREADS":0,
                    "OPF_MAX_TERMS_PER_LINE":5,
                    "OPF_WRITE_HEADER":"ON",
                    "OPF_WRITE_HINTS":"ON",
                    "OPF_WRITE_PARAMETERS":"OFF",
                    "OPF_WRITE_PROBLEM":"ON",
                    "OPF_WRITE_SOL_BAS":"ON",
                    "OPF_WRITE_SOL_ITG":"ON",
                    "OPF_WRITE_SOL_ITR":"ON",
                    "OPF_WRITE_SOLUTIONS":"OFF",
                    "OPTIMIZER":"OPTIMIZER_FREE",
                    "PARAM_READ_CASE_NAME":"ON",
                    "PARAM_READ_IGN_ERROR":"OFF",
                    "PRESOLVE_ELIMINATOR_MAX_FILL":-1,
                    "PRESOLVE_ELIMINATOR_MAX_NUM_TRIES":-1,
                    "PRESOLVE_LEVEL":-1,
                    "PRESOLVE_LINDEP_ABS_WORK_TRH":100,
                    "PRESOLVE_LINDEP_REL_WORK_TRH":100,
                    "PRESOLVE_LINDEP_USE":"ON",
                    "PRESOLVE_MAX_NUM_REDUCTIONS":-1,
                    "PRESOLVE_USE":"PRESOLVE_MODE_FREE",
                    "PRIMAL_REPAIR_OPTIMIZER":"OPTIMIZER_FREE",
                    "QO_SEPARABLE_REFORMULATION":"OFF",
                    "READ_DATA_COMPRESSED":"COMPRESS_FREE",
                    "READ_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
                    "READ_DEBUG":"OFF",
                    "READ_KEEP_FREE_CON":"OFF",
                    "READ_LP_DROP_NEW_VARS_IN_BOU":"OFF",
                    "READ_LP_QUOTED_NAMES":"ON",
                    "READ_MPS_FORMAT":"MPS_FORMAT_FREE",
                    "READ_MPS_WIDTH":1024,
                    "READ_TASK_IGNORE_PARAM":"OFF",
                    "SENSITIVITY_ALL":"OFF",
                    "SENSITIVITY_OPTIMIZER":"OPTIMIZER_FREE_SIMPLEX",
                    "SENSITIVITY_TYPE":"SENSITIVITY_TYPE_BASIS",
                    "SIM_BASIS_FACTOR_USE":"ON",
                    "SIM_DEGEN":"SIM_DEGEN_FREE",
                    "SIM_DUAL_CRASH":90,
                    "SIM_DUAL_PHASEONE_METHOD":0,
                    "SIM_DUAL_RESTRICT_SELECTION":50,
                    "SIM_DUAL_SELECTION":"SIM_SELECTION_FREE",
                    "SIM_EXPLOIT_DUPVEC":"SIM_EXPLOIT_DUPVEC_OFF",
                    "SIM_HOTSTART":"SIM_HOTSTART_FREE",
                    "SIM_HOTSTART_LU":"ON",
                    "SIM_INTEGER":0,
                    "SIM_MAX_ITERATIONS":10000000,
                    "SIM_MAX_NUM_SETBACKS":250,
                    "SIM_NON_SINGULAR":"ON",
                    "SIM_PRIMAL_CRASH":90,
                    "SIM_PRIMAL_PHASEONE_METHOD":0,
```

```json
            "SIM_PRIMAL_RESTRICT_SELECTION":50,
            "SIM_PRIMAL_SELECTION":"SIM_SELECTION_FREE",
            "SIM_REFACTOR_FREQ":0,
            "SIM_REFORMULATION":"SIM_REFORMULATION_OFF",
            "SIM_SAVE_LU":"OFF",
            "SIM_SCALING":"SCALING_FREE",
            "SIM_SCALING_METHOD":"SCALING_METHOD_POW2",
            "SIM_SOLVE_FORM":"SOLVE_FREE",
            "SIM_STABILITY_PRIORITY":50,
            "SIM_SWITCH_OPTIMIZER":"OFF",
            "SOL_FILTER_KEEP_BASIC":"OFF",
            "SOL_FILTER_KEEP_RANGED":"OFF",
            "SOL_READ_NAME_WIDTH":-1,
            "SOL_READ_WIDTH":1024,
            "SOLUTION_CALLBACK":"OFF",
            "TIMING_LEVEL":1,
            "WRITE_BAS_CONSTRAINTS":"ON",
            "WRITE_BAS_HEAD":"ON",
            "WRITE_BAS_VARIABLES":"ON",
            "WRITE_DATA_COMPRESSED":0,
            "WRITE_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
            "WRITE_DATA_PARAM":"OFF",
            "WRITE_FREE_CON":"OFF",
            "WRITE_GENERIC_NAMES":"OFF",
            "WRITE_GENERIC_NAMES_IO":1,
            "WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS":"OFF",
            "WRITE_IGNORE_INCOMPATIBLE_ITEMS":"OFF",
            "WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS":"OFF",
            "WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS":"OFF",
            "WRITE_INT_CONSTRAINTS":"ON",
            "WRITE_INT_HEAD":"ON",
            "WRITE_INT_VARIABLES":"ON",
            "WRITE_LP_FULL_OBJ":"ON",
            "WRITE_LP_LINE_WIDTH":80,
            "WRITE_LP_QUOTED_NAMES":"ON",
            "WRITE_LP_STRICT_FORMAT":"OFF",
            "WRITE_LP_TERMS_PER_LINE":10,
            "WRITE_MPS_FORMAT":"MPS_FORMAT_FREE",
            "WRITE_MPS_INT":"ON",
            "WRITE_PRECISION":15,
            "WRITE_SOL_BARVARIABLES":"ON",
            "WRITE_SOL_CONSTRAINTS":"ON",
            "WRITE_SOL_HEAD":"ON",
            "WRITE_SOL_IGNORE_INVALID_NAMES":"OFF",
            "WRITE_SOL_VARIABLES":"ON",
            "WRITE_TASK_INC_SOL":"ON",
            "WRITE_XML_MODE":"WRITE_XML_MODE_ROW"
        },
        "dparam":{
            "ANA_SOL_INFEAS_TOL":1e-6,
            "BASIS_REL_TOL_S":1e-12,
            "BASIS_TOL_S":1e-6,
            "BASIS_TOL_X":1e-6,
            "CHECK_CONVEXITY_REL_TOL":1e-10,
            "DATA_TOL_AIJ":1e-12,
            "DATA_TOL_AIJ_HUGE":1e+20,
            "DATA_TOL_AIJ_LARGE":1e+10,
            "DATA_TOL_BOUND_INF":1e+16,
            "DATA_TOL_BOUND_WRN":1e+8,
            "DATA_TOL_C_HUGE":1e+16,
            "DATA_TOL_CJ_LARGE":1e+8,
```

```
                    "DATA_TOL_QIJ":1e-16,
                    "DATA_TOL_X":1e-8,
                    "FEASREPAIR_TOL":1e-10,
                    "INTPNT_CO_TOL_DFEAS":1e-8,
                    "INTPNT_CO_TOL_INFEAS":1e-10,
                    "INTPNT_CO_TOL_MU_RED":1e-8,
                    "INTPNT_CO_TOL_NEAR_REL":1e+3,
                    "INTPNT_CO_TOL_PFEAS":1e-8,
                    "INTPNT_CO_TOL_REL_GAP":1e-7,
                    "INTPNT_NL_MERIT_BAL":1e-4,
                    "INTPNT_NL_TOL_DFEAS":1e-8,
                    "INTPNT_NL_TOL_MU_RED":1e-12,
                    "INTPNT_NL_TOL_NEAR_REL":1e+3,
                    "INTPNT_NL_TOL_PFEAS":1e-8,
                    "INTPNT_NL_TOL_REL_GAP":1e-6,
                    "INTPNT_NL_TOL_REL_STEP":9.95e-1,
                    "INTPNT_QO_TOL_DFEAS":1e-8,
                    "INTPNT_QO_TOL_INFEAS":1e-10,
                    "INTPNT_QO_TOL_MU_RED":1e-8,
                    "INTPNT_QO_TOL_NEAR_REL":1e+3,
                    "INTPNT_QO_TOL_PFEAS":1e-8,
                    "INTPNT_QO_TOL_REL_GAP":1e-8,
                    "INTPNT_TOL_DFEAS":1e-8,
                    "INTPNT_TOL_DSAFE":1e+0,
                    "INTPNT_TOL_INFEAS":1e-10,
                    "INTPNT_TOL_MU_RED":1e-16,
                    "INTPNT_TOL_PATH":1e-8,
                    "INTPNT_TOL_PFEAS":1e-8,
                    "INTPNT_TOL_PSAFE":1e+0,
                    "INTPNT_TOL_REL_GAP":1e-8,
                    "INTPNT_TOL_REL_STEP":9.999e-1,
                    "INTPNT_TOL_STEP_SIZE":1e-6,
                    "LOWER_OBJ_CUT":-1e+30,
                    "LOWER_OBJ_CUT_FINITE_TRH":-5e+29,
                    "MIO_DISABLE_TERM_TIME":-1e+0,
                    "MIO_MAX_TIME":-1e+0,
                    "MIO_MAX_TIME_APRX_OPT":6e+1,
                    "MIO_NEAR_TOL_ABS_GAP":0.0,
                    "MIO_NEAR_TOL_REL_GAP":1e-3,
                    "MIO_REL_GAP_CONST":1e-10,
                    "MIO_TOL_ABS_GAP":0.0,
                    "MIO_TOL_ABS_RELAX_INT":1e-5,
                    "MIO_TOL_FEAS":1e-6,
                    "MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT":0.0,
                    "MIO_TOL_REL_GAP":1e-4,
                    "MIO_TOL_X":1e-6,
                    "OPTIMIZER_MAX_TIME":-1e+0,
                    "PRESOLVE_TOL_ABS_LINDEP":1e-6,
                    "PRESOLVE_TOL_AIJ":1e-12,
                    "PRESOLVE_TOL_REL_LINDEP":1e-10,
                    "PRESOLVE_TOL_S":1e-8,
                    "PRESOLVE_TOL_X":1e-8,
                    "QCQO_REFORMULATE_REL_DROP_TOL":1e-15,
                    "SEMIDEFINITE_TOL_APPROX":1e-10,
                    "SIM_LU_TOL_REL_PIV":1e-2,
                    "SIMPLEX_ABS_TOL_PIV":1e-7,
                    "UPPER_OBJ_CUT":1e+30,
                    "UPPER_OBJ_CUT_FINITE_TRH":5e+29
            },
            "sparam":{
                    "BAS_SOL_FILE_NAME":"",
```

```
                "DATA_FILE_NAME":"examples/tools/data/lo1.mps",
                "DEBUG_FILE_NAME":"",
                "INT_SOL_FILE_NAME":"",
                "ITR_SOL_FILE_NAME":"",
                "MIO_DEBUG_STRING":"",
                "PARAM_COMMENT_SIGN":"%%",
                "PARAM_READ_FILE_NAME":"",
                "PARAM_WRITE_FILE_NAME":"",
                "READ_MPS_BOU_NAME":"",
                "READ_MPS_OBJ_NAME":"",
                "READ_MPS_RAN_NAME":"",
                "READ_MPS_RHS_NAME":"",
                "SENSITIVITY_FILE_NAME":"",
                "SENSITIVITY_RES_FILE_NAME":"",
                "SOL_FILTER_XC_LOW":"",
                "SOL_FILTER_XC_UPR":"",
                "SOL_FILTER_XX_LOW":"",
                "SOL_FILTER_XX_UPR":"",
                "STAT_FILE_NAME":"",
                "STAT_KEY":"",
                "STAT_NAME":"",
                "WRITE_LP_GEN_VAR_NAME":"XMSKGEN"
        }
    }
}
```

12.8 The Solution File Format

MOSEK provides several solution files depending on the problem type and the optimizer used:

- *basis solution file* (extension `.bas`) if the problem is optimized using the simplex optimizer or basis identification is performed,

- *interior solution file* (extension `.sol`) if a problem is optimized using the interior-point optimizer and no basis identification is required,

- *integer solution file* (extension `.int`) if the problem contains integer constrained variables.

All solution files have the format:

```
NAME                : <problem name>
PROBLEM STATUS      : <status of the problem>
SOLUTION STATUS     : <status of the solution>
OBJECTIVE NAME      : <name of the objective function>
PRIMAL OBJECTIVE    : <primal objective value corresponding to the solution>
DUAL OBJECTIVE      : <dual objective value corresponding to the solution>
CONSTRAINTS
INDEX  NAME     AT ACTIVITY     LOWER LIMIT    UPPER LIMIT    DUAL LOWER    DUAL UPPER
?      <name>   ?? <a value>    <a value>      <a value>      <a value>     <a value>
VARIABLES
INDEX  NAME     AT ACTIVITY     LOWER LIMIT    UPPER LIMIT    DUAL LOWER    DUAL UPPER    CONIC␣
↪DUAL
?      <name>   ?? <a value>    <a value>      <a value>      <a value>     <a value>     <a value>
```

In the example the fields `?` and `<>` will be filled with problem and solution specific information. As can be observed a solution report consists of three sections, i.e.

- `HEADER` In this section, first the name of the problem is listed and afterwards the problem and solution status are shown. Next the primal and dual objective values are displayed.

- **CONSTRAINTS** For each constraint i of the form

$$l_i^c \leq \sum_{j=1}^n a_{ij}x_j \leq u_i^c, \tag{12.15}$$

  the following information is listed:

  - **INDEX**: A sequential index assigned to the constraint by **MOSEK**
  - **NAME**: The name of the constraint assigned by the user.
  - **AT**: The status of the constraint. In Table 12.4 the possible values of the status keys and their interpretation are shown.

Table 12.4: Status keys.

Status key	Interpretation
UN	Unknown status
BS	Is basic
SB	Is superbasic
LL	Is at the lower limit (bound)
UL	Is at the upper limit (bound)
EQ	Lower limit is identical to upper limit
**	Is infeasible i.e. the lower limit is greater than the upper limit.

  - **ACTIVITY**: the quantity $\sum_{j=1}^n a_{ij}x_j^*$, where x^* is the value of the primal solution.
  - **LOWER LIMIT**: the quantity l_i^c (see (12.15).)
  - **UPPER LIMIT**: the quantity u_i^c (see (12.15).)
  - **DUAL LOWER**: the dual multiplier corresponding to the lower limit on the constraint.
  - **DUAL UPPER**: the dual multiplier corresponding to the upper limit on the constraint.

- **VARIABLES** The last section of the solution report lists information about the variables. This information has a similar interpretation as for the constraints. However, the column with the header **CONIC DUAL** is included for problems having one or more conic constraints. This column shows the dual variables corresponding to the conic constraints.

Example: `lo1.sol`

In Listing 12.7 we show the solution file for the `lo1.opf` problem.

Listing 12.7: An example of `.sol` file.

```
NAME                   :
PROBLEM STATUS         : PRIMAL_AND_DUAL_FEASIBLE
SOLUTION STATUS        : OPTIMAL
OBJECTIVE NAME         : obj
PRIMAL OBJECTIVE       : 8.33333333e+01
DUAL OBJECTIVE         : 8.33333332e+01

CONSTRAINTS
INDEX       NAME         AT ACTIVITY                LOWER LIMIT        UPPER LIMIT        ␣
↪DUAL LOWER             DUAL UPPER
0           c1           EQ 3.00000000000000e+01    3.00000000e+01     3.00000000e+01     -0.
↪00000000000000e+00    -2.49999999741653e+00
1           c2           SB 5.33333333049187e+01    1.50000000e+01     NONE               2.
↪09159033069640e-10    -0.00000000000000e+00
2           c3           UL 2.49999999842049e+01    NONE               2.50000000e+01     -0.
↪00000000000000e+00    -3.33333332895108e-01

VARIABLES
INDEX       NAME         AT ACTIVITY                LOWER LIMIT        UPPER LIMIT        ␣
↪DUAL LOWER             DUAL UPPER
0           x1           LL 1.67020427038537e-09    0.00000000e+00     NONE               -4.
↪49999999528054e+00    -0.00000000000000e+00
```

1	x2	LL 2.93510446211883e-09	0.00000000e+00	1.00000000e+01	-2.
↪16666666494915e+00		6.20868657679896e-10			
2	x3	SB 1.49999999899424e+01	0.00000000e+00	NONE	-8.
↪79123177245553e-10		-0.00000000000000e+00			
3	x4	SB 8.33333332273115e+00	0.00000000e+00	NONE	-1.
↪69795978848200e-09		-0.00000000000000e+00			

Chapter 13

List of examples

List of examples shipped in the distribution of Command Line Tools:

Table 13.1: List of distributed examples

File	Description
`25fv47.mps`	A large linear problem from the Netlib library
`ampl1.res`	Interfacing **MOSEK** from AMPL
`ampl2.res`	Interfacing **MOSEK** from AMPL
`ampl3.res`	Interfacing **MOSEK** from AMPL
`cqo1.mps`	A simple conic quadratic problem
`diet.dat`	Data for the diet example `diet.mod`
`diet.mod`	A diet balancing AMPL example
`dinfeas.lp`	A simple dual infeasible linear problem
`feasrepair.lp`	An example demonstrating repair of infeasible problems
`infeas.lp`	A simple primal infeasible problem
`lo1.mps`	A simple linear problem
`qo1.mps`	A simple quadratic problem
`sensitivity.ssp`	Sensitivity analysis specification for `transport.lp`
`transport.lp`	A linear problem in the sensitivity analysis example

Additional examples can be found on the **MOSEK** website and in other **MOSEK** publications.

Chapter 14

Interface changes

The section shows interface-specific changes to the **MOSEK** Command Line Tools in version 9.1 compared to version 8. See the release notes for general changes and new features of the **MOSEK** Optimization Suite.

14.1 Backwards compatibility

- **Parameters.** Users who set parameters to tune the performance and numerical properties of the solver (termination criteria, tolerances, solving primal or dual, presolve etc.) are recommended to reevaluate such tuning. It may be that other, or default, parameter settings will be more beneficial in the current version. The hints in Sec. 7 may be useful for some cases.

- Removed all `Near` problem and solution statuses i.e. `NEAR_OPTIMAL`, `NEAR_PRIMAL_INFEASIBLE_CER`, etc. See Sec. 9.3.3.

- All programs related to the general nonlinear optimizer and Scopt (`mskexpopt`, `mskscopt`, `mskdgopt`) have been removed.

14.2 Parameters

Added

- *MSK_IPAR_INTPNT_ORDER_GP_NUM_SEEDS*

- *MSK_IPAR_INTPNT_PURIFY*

- *MSK_IPAR_LOG_INCLUDE_SUMMARY*

- *MSK_IPAR_LOG_LOCAL_INFO*

- *MSK_IPAR_MIO_CONIC_OUTER_APPROXIMATION*

- *MSK_IPAR_MIO_FEASPUMP_LEVEL*

- *MSK_IPAR_MIO_MAX_NUM_ROOT_CUT_ROUNDS*

- *MSK_IPAR_MIO_PROPAGATE_OBJECTIVE_CONSTRAINT*

- *MSK_IPAR_MIO_SEED*

- *MSK_IPAR_OPF_WRITE_LINE_LENGTH*

- *MSK_IPAR_PRESOLVE_MAX_NUM_PASS*

- *MSK_IPAR_PTF_WRITE_TRANSFORM*

- *MSK_IPAR_SIM_SEED*

- *MSK_IPAR_WRITE_COMPRESSION*

Removed

- MSK_DPAR_DATA_TOL_AIJ

- MSK_DPAR_INTPNT_NL_MERIT_BAL

- MSK_DPAR_INTPNT_NL_TOL_DFEAS

- MSK_DPAR_INTPNT_NL_TOL_MU_RED

- MSK_DPAR_INTPNT_NL_TOL_NEAR_REL

- MSK_DPAR_INTPNT_NL_TOL_PFEAS

- MSK_DPAR_INTPNT_NL_TOL_REL_GAP

- MSK_DPAR_INTPNT_NL_TOL_REL_STEP

- MSK_DPAR_MIO_DISABLE_TERM_TIME

- MSK_DPAR_MIO_NEAR_TOL_ABS_GAP

- MSK_DPAR_MIO_NEAR_TOL_REL_GAP

- MSK_IPAR_MIO_CONSTRUCT_SOL

- MSK_IPAR_MIO_MT_USER_CB

- MSK_IPAR_OPF_MAX_TERMS_PER_LINE

- MSK_IPAR_READ_DATA_COMPRESSED

- MSK_IPAR_READ_DATA_FORMAT

- MSK_IPAR_WRITE_DATA_COMPRESSED

- MSK_IPAR_WRITE_DATA_FORMAT

14.3 Constants

Added

- *MSK_COMPRESS_ZSTD*

- *MSK_CT_DEXP*

- *MSK_CT_DPOW*

- *MSK_CT_PEXP*

- *MSK_CT_PPOW*

- *MSK_CT_ZERO*

- *MSK_DATA_FORMAT_PTF*

- *MSK_IINF_MIO_NUMBIN*

- *MSK_IINF_MIO_NUMBINCONEVAR*

- *MSK_IINF_MIO_NUMCONE*

- *MSK_IINF_MIO_NUMCONEVAR*

- *MSK_IINF_MIO_NUMCONT*

- *MSK_IINF_MIO_NUMCONTCONEVAR*

- *MSK_IINF_MIO_NUMDEXPCONES*

- *MSK_IINF_MIO_NUMDPOWCONES*

- *MSK_IINF_MIO_NUMINTCONEVAR*

- *MSK_IINF_MIO_NUMPEXPCONES*

- *MSK_IINF_MIO_NUMPPOWCONES*

- *MSK_IINF_MIO_NUMQCONES*

- *MSK_IINF_MIO_NUMRQCONES*

- *MSK_IINF_MIO_PRESOLVED_NUMBINCONEVAR*

- *MSK_IINF_MIO_PRESOLVED_NUMCONE*

- *MSK_IINF_MIO_PRESOLVED_NUMCONEVAR*

- *MSK_IINF_MIO_PRESOLVED_NUMCONTCONEVAR*

- *MSK_IINF_MIO_PRESOLVED_NUMDEXPCONES*

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- *MSK_IINF_PURIFY_DUAL_SUCCESS*

- *MSK_IINF_PURIFY_PRIMAL_SUCCESS*

- *MSK_LIINF_MIO_ANZ*

Removed

- MSK_DATAFORMAT_XML

- MSK_DINFITEM_MIO_HEURISTIC_TIME

- MSK_DINFITEM_MIO_OPTIMIZER_TIME

- MSK_IINFITEM_MIO_CONSTRUCT_NUM_ROUNDINGS

- MSK_IINFITEM_MIO_INITIAL_SOLUTION

- MSK_IINFITEM_MIO_NEAR_ABSGAP_SATISFIED

- MSK_IINFITEM_MIO_NEAR_RELGAP_SATISFIED

- MSK_LIINFITEM_MIO_SIM_MAXITER_SETBACKS

- MSK_MIONODESELTYPE_HYBRID

- `MSK_MIONODESELTYPE_WORST`

- `MSK_PROBLEMTYPE_GECO`

- `MSK_PROSTA_NEAR_DUAL_FEAS`

- `MSK_PROSTA_NEAR_PRIM_AND_DUAL_FEAS`

- `MSK_PROSTA_NEAR_PRIM_FEAS`

- `MSK_SENSITIVITYTYPE_OPTIMAL_PARTITION`

- `MSK_SOLSTA_NEAR_DUAL_FEAS`

- `MSK_SOLSTA_NEAR_DUAL_INFEAS_CER`

- `MSK_SOLSTA_NEAR_INTEGER_OPTIMAL`

- `MSK_SOLSTA_NEAR_OPTIMAL`

- `MSK_SOLSTA_NEAR_PRIM_AND_DUAL_FEAS`

- `MSK_SOLSTA_NEAR_PRIM_FEAS`

- `MSK_SOLSTA_NEAR_PRIM_INFEAS_CER`

14.4 Response Codes

Added

- *MSK_RES_ERR_APPENDING_TOO_BIG_CONE*

- *MSK_RES_ERR_CBF_DUPLICATE_POW_CONES*

- *MSK_RES_ERR_CBF_DUPLICATE_POW_STAR_CONES*

- *MSK_RES_ERR_CBF_INVALID_DIMENSION_OF_CONES*

- *MSK_RES_ERR_CBF_INVALID_EXP_DIMENSION*

- *MSK_RES_ERR_CBF_INVALID_NUMBER_OF_CONES*

- *MSK_RES_ERR_CBF_INVALID_POWER*

- *MSK_RES_ERR_CBF_INVALID_POWER_CONE_INDEX*

- *MSK_RES_ERR_CBF_INVALID_POWER_STAR_CONE_INDEX*

- *MSK_RES_ERR_CBF_POWER_CONE_IS_TOO_LONG*

- *MSK_RES_ERR_CBF_POWER_CONE_MISMATCH*

- *MSK_RES_ERR_CBF_POWER_STAR_CONE_MISMATCH*

- *MSK_RES_ERR_CBF_UNHANDLED_POWER_CONE_TYPE*

- *MSK_RES_ERR_CBF_UNHANDLED_POWER_STAR_CONE_TYPE*

- *MSK_RES_ERR_CONE_PARAMETER*

- *MSK_RES_ERR_FORMAT_STRING*

- *MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_CFIX*

- *MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_FREE_CONSTRAINTS*

- *MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_NONLINEAR*

- *MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_RANGED_CONSTRAINTS*

- *MSK_RES_ERR_NUM_ARGUMENTS*

- *MSK_RES_ERR_PTF_FORMAT*

- *MSK_RES_ERR_SHAPE_IS_TOO_LARGE*

- *MSK_RES_ERR_SLICE_SIZE*

- *MSK_RES_ERR_TOO_SMALL_A_TRUNCATION_VALUE*

- *MSK_RES_WRN_EXP_CONES_WITH_VARIABLES_FIXED_AT_ZERO*

- *MSK_RES_WRN_POW_CONES_WITH_ROOT_FIXED_AT_ZERO*

Removed

- MSK_RES_ERR_CANNOT_CLONE_NL

- MSK_RES_ERR_CANNOT_HANDLE_NL

- MSK_RES_ERR_INVALID_ACCMODE

- MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_GENERAL_NL

- MSK_RES_ERR_NONLINEAR_FUNCTIONS_NOT_ALLOWED

- MSK_RES_ERR_NR_ARGUMENTS

- MSK_RES_ERR_OPEN_DL

- MSK_RES_ERR_USER_FUNC_RET

- MSK_RES_ERR_USER_FUNC_RET_DATA

- MSK_RES_ERR_USER_NLO_EVAL

- MSK_RES_ERR_USER_NLO_EVAL_HESSUBI

- MSK_RES_ERR_USER_NLO_EVAL_HESSUBJ

- MSK_RES_ERR_USER_NLO_FUNC

- MSK_RES_TRM_MIO_NEAR_ABS_GAP

- MSK_RES_TRM_MIO_NEAR_REL_GAP

- MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG

- MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG

- MSK_RES_WRN_CONSTRUCT_SOLUTION_INFEAS

- MSK_RES_WRN_NO_NONLINEAR_FUNCTION_WRITE

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