នេះខ្មែរខ្មែរខ្មែរ

១ ខូតានខុត

និយមន័យ ១. ដេរីវេនៃអនុគមន៍ $\mathbf{y} = \mathbf{f}(\mathbf{x})$ ត្រង់ \mathbf{x}_0 កំណត់ដោយ

$$\frac{\mathrm{d}y}{\mathrm{d}x} = y' = f'(x_0) = \lim_{\Delta x \to 0} \frac{\Delta y}{\Delta x} = \lim_{x \to x_0} \frac{f(x) - f(x_0)}{x - x_0} = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

សំនាល់ ១. គេអាចសរសេរដៅវីវេដោយ y' , f'(x) ឬ $\frac{dy}{dx}$ ។

- អនុគមន៍ f មានដេរីវេត្រង់ \mathbf{x}_0 នោះ f ជាប់ត្រង់ \mathbf{x}_0 ។
- អនុគមន៍ f ជាប់ត្រង់ \mathbf{x}_0 នោះ f អាចមានដេរីវេត្រង់ \mathbf{x}_0 ឬ គ្មានដេរីវេត្រង់ \mathbf{x}_0 ។

😊 ភាពមានដេរីទេ

និយមន័យ ២. អនុគមន៍ f មានដេរីវេត្រង់ \mathbf{x}_0 លុះត្រាតែ

- អនុគមន៍ f ជាប់ត្រង់ x=0 ។
- ដេរីវេឆ្វេងស្មើដេរីវេស្តាំត្រង់ចំណុច \mathbf{x}_0 គឺ $\mathbf{f}_-'(\mathbf{x}_0) = \mathbf{f}_+'(\mathbf{x}_0)$ ដែល

$$f'_{-}(x_0) = \lim_{h \to 0^{-}} \frac{f(x_0 + h) - f(x_0)}{h} \ \hat{\mathbb{S}} h \ f'_{+}(x_0) = \lim_{h \to 0^{+}} \frac{f(x_0 + h) - f(x_0)}{h} \ \mathfrak{I}$$

<u>ದ್ದಾರಿ</u> ಮಕ್ಷಣ್ಣಚಚಿಚ್ಚುಣ್ಣ

និយមន័យ ៣. អនុគមន៍ f ជាប់លើចន្លោះបើក (a,b) កាលណា f មានដេរីវេលើគ្រប់ចំណុច $x_0\in(a,b)$ ។

និយមន័យ ៤. អនុគមន៍ f មានដេរីវេលើចន្លោះបិទ [a,b] កាលណា f មានដេរីវេលើចន្លោះ (a,b) ហើយ f មានដេរីវេខាងឆ្វេងត្រង់ x=a និងខាងស្តាំត្រង់ x=b ។

ព លទ្ធសាះនៃខេត្តិទេ

ចំពោះ \mathbf{u},\mathbf{v} ជាអនុគមន៍នៃ \mathbf{x} និង \mathbf{k} ជាចំនួនថេ នោះគេបាន៖

9.
$$(ku)' = ku'$$

$$M. (u-v)' = u'-v'$$

ਫ.
$$\left(\frac{\mathbf{u}}{\mathbf{v}}\right)' = \frac{\mathbf{u}'\mathbf{v} - \mathbf{v}'\mathbf{u}}{\mathbf{v}^2}$$

$$u = u' + v$$

ઉ.
$$(uv)' = u'v + v'u$$

$$\mathfrak{d}. \left(\frac{1}{\mathbf{v}}\right)' = -\frac{\mathbf{v}'}{\mathbf{v}^2}$$

ស្សសាលមណ្ឌាអ

9. តាង f(x) = k.u(x) ដែល u = u(x) និង k ជាចំនួនថេ តាមនិយមន័យ

$$\begin{split} f'(x_0) &= \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{ku(x_0 + h) - k.u(x_0)}{h} \\ &= k. \lim_{h \to 0} \frac{u(x_0 + h) - u(x_0)}{h} \\ &= k.u'(x_0) \\ & \therefore \quad (k.u)' = k.u' \end{split}$$

២. តាង f(x) = u(x) + v(x) ដែល u = u(x) និង v = v(x) តាមនិយមន័យ

$$\begin{split} f'(x_0) &= \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{u(x_0 + h) + v(x_0 + h) - (u(x_0) + v(x_0))}{h} \\ &= \lim_{h \to 0} \frac{u(x_0 + h) - u(x_0)}{h} + \lim_{h \to 0} \frac{v(x_0 + h) - v(x_0)}{h} \\ &= u'(x_0) + v'(x_0) \\ & \therefore \quad (u + v)' = u' + v' \end{split}$$

- ៣. ស្រាយដូចទី២
- ៤. តាង f(x) = uv ដែល u = u(x) និង v = v(x) តាមនិយមន័យគេបាន

$$\begin{split} f'(x_0) &= \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{u(x_0 + h).v(x_0 + h) - u(x_0).v(x_0)}{h} \\ &= \lim_{h \to 0} \frac{u(x_0 + h).v(x_0 + h) - u(x_0).v(x_0 + h) + u(x_0).v(x_0 + h) + u(x_0).v(x_0)}{h} \\ &= \lim_{h \to 0} \left[\frac{u(x_0 + h).v(x_0 + h) - u(x_0).v(x_0 + h)}{h} + \frac{u(x_0).v(x_0 + h) + u(x_0).v(x_0)}{h} \right] \\ &= \lim_{h \to 0} \left[v(x_0 + h).\frac{u(x_0 + h) - u(x_0)}{h} + u(x_0).\frac{v(x_0 + h) + v(x_0)}{h} \right] \\ &= v(x_0).\frac{d}{dx}(u(x_0)) + u(x_0).\frac{d}{dx}(v(x_0)) \end{split}$$

$$\therefore (uv)' = u'v + v'u \tag{9}$$

៥. យក u=u(x) និង v=v(x) តាង $f(x)=\frac{u}{v}\Leftrightarrow f(x).v=u$ ធ្វើដេរីវេអង្គទាំងពីរធៀបនឹង x នោះគេបាន [f(x).v]'=u' ប្រើតាមសមីការ (១) គេបាន

$$f'(x).v + v'f(x) = u', f(x) = \frac{u}{v}$$

$$f'(x).v + v'.\frac{u}{v} = u'$$

$$\frac{f'(x).v^{2}}{v} + \frac{v'u}{v} = u'$$

$$f'(x).v^{2} + v'u = u'v$$

$$f'(x) = \frac{u'v - v'u}{v^{2}}$$

$$\therefore \left(\frac{\mathbf{u}}{\mathbf{v}}\right)' = \frac{\mathbf{u}'\mathbf{v} - \mathbf{v}'\mathbf{u}}{\mathbf{v}^2} \tag{0}$$

៦. យក v=v(x) តាង $f(x)=rac{1}{v}$ ប្រើសមីការ (២) គេបាន

$$f'(x) = \frac{(1)' \cdot v - v' \cdot (1)}{v^2}$$
$$= \frac{0 - v'}{v^2}$$
$$= -\frac{v'}{v^2}$$
$$\therefore \left(\frac{1}{v}\right)' = -\frac{v'}{v^2}$$

៤ ខេរីខេរិនអនុគមន៍មណ្ឌាអ

ប៊ើ
$$y=f(u)$$
 និង $u=g(x)$ នោះ $\dfrac{d}{dx}(f\circ g)=\dfrac{dy}{du}\times\dfrac{du}{dx}$ ។

ಹ್ಯಾಭಾರು ಉತ್ತುಕ್ಕ

តាង $F(x) = f \circ g = f(g(x))$ តាមនិយមន័យភាពមានដេរីវេត្រង់ $x = x_0$ នោះគេបាន

$$\begin{split} F'(x_0) &= \lim_{x \to x_0} \frac{F(x) - F(x_0)}{x - x_0} \\ &= \lim_{x \to x_0} \frac{f(g(x)) - f(g(x_0))}{x - x_0} \\ &= \lim_{x \to x_0} \left(\frac{f(g(x)) - f(g(x_0))}{g(x) - g(x_0)} \times \frac{g(x) - g(x_0)}{x - x_0} \right) \\ &= f'(g(x_0)) \times g'(x_0) \quad , u = g(x_0), y = f(x_0) \\ \therefore \quad \frac{d}{dx} (f \circ g) &= \frac{dy}{du} \times \frac{dy}{dx} \end{split}$$

ខាន្នៅ ៤.១. បើ y=c ដែល c ជាចំនួនថេរ នោះ y'=0 ។

ស្ខេតខេស្សាង

គេមាន $y=f(x_0)=c$ នោះ $f(x_0+h)=c$, $c\in\mathbb{R}$ តាមនិយមន័យគេបាន

$$\begin{split} f'(x_0) &= \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{c - c}{h} \\ &= \lim_{h \to 0} \frac{0}{h} \\ \therefore \quad \frac{d}{dx}(c) &= 0 \end{split}$$

ខ្វិតាហរណ៍ ១. គណនា y' ដែល $y = \left(\ln x. \log_a(\sqrt{3})\right)$ ។

ಜೀಣಾ:ಕ್ಷಾಟ

គេមាន
$$y = \left(\ln x. \log_a(\sqrt{3})\right) \Rightarrow y' = \left(\ln x. \log_a(\sqrt{3})\right)' = 0$$

ន្ធនាហរណ៍ ២. ស្រាយបញ្ហាក់ថា បើ $\mathbf{y}=\mathbf{x}^{\mathbf{n}}$ នោះ $\mathbf{y}'=\mathbf{n}\mathbf{x}^{\mathbf{n}-1}$ ។

គេមាន $f(x_0)=x_0^n$ នាំឲ្យ $f(x_0+h)=(x_0+h)^n$ តាមនិយមន័យ

$$\begin{split} y' &= f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{(x_0 + h)^n - x_0^n}{h} \\ &= \lim_{h \to 0} \frac{(x_0 + h - x_0)(x_0^{n-1} + x^{n-2}.x_0 + ... + x_0.x^{n-2}x_0 + x_0^{n-1})}{h} \\ &= \lim_{h \to 0} (x_0^{n-1} + x_0^{n-1} + ... + x_0^{n-1} + x_0^{n+1}) \\ &= \lim_{h \to 0} (x_0^{n-1} + x_0^{n-1} + ... + x_0^{n-1} + x_0^{n+1}) \\ &= x_0^{n-1} (\underbrace{1 + 1 + ... + 1 + 1}_{n \text{ pinor}}) \\ &= n.x_0^{n-1} \\ &\therefore \quad \frac{d}{dx}(x^n) = n.x^{n-1} \end{split}$$

ខ្នុតាចារណ៍ ៣. គណនា f'(x)

9.
$$f(x) = x^3$$

$$varphi$$
. $f(x) = \sqrt{x}$

$$f(x) = \sqrt[3]{x^2}$$

ಕ್ಷೀಬ್ಯಾಕಿಲಡಾ

9.
$$f(x) = x^3 \Rightarrow f'(x) = (x^3)' = 3x^{3-1} = 3x^2$$

$$\text{ b. } f(x) = \sqrt{x} \Rightarrow f'(x) = (\sqrt{x})' = (x^{\frac{1}{2}})' = \frac{1}{2}x^{\frac{1}{2}-1} = \frac{1}{2}x^{-\frac{1}{2}} = \frac{1}{2\sqrt{x}}$$

$$\text{M. } f(x) = \sqrt[3]{x^2} \Rightarrow f'(x) = (\sqrt[3]{x^2})' = (x^{\frac{2}{3}})' = \frac{2}{3}x^{\frac{2}{3}-1} = \frac{2}{3}x^{-\frac{1}{3}} = \frac{2}{3\sqrt[3]{x}}$$

ខាន្នៅ ៤.២. បើ $y=u^n$ ដែល u ជាអនុគមន៍នៃ x នោះ $y'=nu'u^{n-1}$ ។

ಕಾಡಿ ಕಾರ್ಣಿಕ

គេមាន
$$y=u^n$$
 គេបាន $y'=\dfrac{dy}{dx}=\dfrac{dy}{du}\times\dfrac{du}{dx}=\dfrac{d}{du}(u^n)\times u'=nu'u^{n-1}$

<mark>ខ្វទាបារណ៍ ៤</mark>. គណនា y'

9.
$$y = (2x + \ln 2)^4$$

២. $y = \sqrt{u}$ ដែល u ជាអនុគមន៍នៃ x ។

ដំណោះស្រាយ

9.
$$y = (2x + \ln 2)^4 \Rightarrow y' = 4(2x + \ln 2)'(2x + \ln 2)^{4-1} = 4(2+0)(2x + \ln 2)^3 = 8(2x + \ln 2)^3$$

២.
$$y = \sqrt{u} = u^{\frac{1}{x}}$$
 ទាំឲ្យ $y' = (u^{\frac{1}{2}})' = \frac{1}{2}u'u^{\frac{1}{2}-1} = \frac{1}{2}u'u^{-\frac{1}{2}} = \frac{u'}{2\sqrt{u}}$ ។

🟅 នើទៃនៃអនុឝមន៍គ្រីអោលទេគ្រ

9. បើ
$$y = \sin x$$
 នោះ $y' = \cos x$

២. បើ
$$y = \cos x$$
 នោះ $y' = -\sin x$

$$\mathbb{M}$$
. បើ $y = \tan x$ នោះ $y' = \frac{1}{\cos^2 x} = 1 + \tan^2 x$

ថ. បើ
$$y = \cot x$$
 នោះ $y' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$

ಖಾತು ಮಟ್ಟು

9. គេមាន $y=f(x_0)=\sin x_0$ នោះ $f(x_0+h)=\sin(x_0+h)$ តាមនិយមន័យ

$$\begin{split} y' &= f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{\sin(x_0 + h) - \sin x_0}{h} \\ &= \lim_{h \to 0} \frac{\sin x_0 \cos h + \sin h \cdot \cos x_0 - \sin x_0}{h} \\ &= \lim_{h \to 0} \left(\cos x_0 \cdot \frac{\sin h}{h} - \sin x_0 \cdot \frac{1 - \cos h}{h}\right) \\ &= \cos x_0 \quad , \lim_{h \to 0} \frac{\sin h}{h} = 1, \lim_{h \to 0} \frac{1 - \cos h}{h} = 0 \\ & \therefore \quad \frac{d}{dx} (\sin x) = \cos x \end{split}$$

២. គេមាន $y=f(x_0)=\cos x_0$ នោះ $f(x_0+h)=\cos(x_0+h)$ តាមនិយមន័យ

$$\begin{split} y' &= f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{\cos(x_0 + h) - \cos x_0}{h} \\ &= \lim_{h \to 0} \frac{\cos x_0 \cdot \cos h - \sin x_0 \cdot \sin h - \cos x_0}{h} \\ &= \lim_{h \to 0} \left(-\frac{\sin h}{h} \cdot \sin x_0 - \cos x_0 \cdot \frac{1 - \cos h}{h} \right) \\ &= -\sin x_0 \quad , \lim_{h \to 0} \frac{1 - \cos h}{h} = 0, \lim_{h \to 0} \frac{\sin h}{h} = 1 \\ &\therefore \quad \frac{d}{dx} (\cos x) = -\sin x \end{split}$$

៣. តាង $y = \tan x = \frac{\sin x}{\cos x}$ តាមសមីការ (២) គេបាន

$$y' = \left(\frac{\sin x}{\cos x}\right)' = \frac{(\sin x)' \cos x - (\cos x)' \cdot \sin x}{(\cos x)^2}$$

$$= \frac{\cos x \cdot \cos x - (-\sin x) \cdot \sin x}{\cos^2 x}$$

$$= \frac{\cos^2 x + \sin^2 x}{\cos^2 x}$$

$$= 1 + \tan^2 x$$

$$= \frac{1}{\cos^2 x}, \sin^2 x + \cos^2 x = 1$$

$$\therefore (\tan x)' = \frac{1}{\cos^2} = 1 + \tan^2 x$$

៤. តាង $y = \cot x = \frac{\cos x}{\sin x}$ តាមសមីការ (២) គេបាន

$$y' = \left(\frac{\cos x}{\sin x}\right)' = \frac{(\cos x)' \cdot \sin x - (\sin x)' \cdot \cos x}{(\sin^2 x)^2}$$

$$= \frac{-\sin x \cdot \sin x - \cos x \cdot \cos x}{\sin^2 x}$$

$$= \frac{-\sin^2 x - \cos^2 x}{\sin^2 x}$$

$$= -\frac{\sin^2 x + \cos^2 x}{\sin^2 x}, \sin^2 x + \cos^2 x = 1$$

$$\therefore (\cot x)' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$$

ខាន្តនៅ ៥.១. បើ ${\bf u}$ ជាអនុគមន៍នៃ ${\bf x}$ គេបាន

- ១. បើ $y = \sin u$ នោះ $y' = u' \cos u$
- ២. បើ $y = \cos u$ នោះ $y' = -u' \sin u$
- ៤. បើ $y = \cot u$ នោះ $y' = -\frac{u'}{\sin^2 u} = -u'(1 + \cot^2 u)$

೫೬೩೩೩೩೩

9. បើ u ជាអនុគមន៍នៃ x នោះ y = sin u គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\sin u) \times \frac{du}{dx} = \cos u \times u' = u' \cos u$$

$$\therefore \frac{d}{dx}(\sin u) = u' \cos u$$

២. បើ u ជាអនុគមន៍នៃ x នោះ y = $\cos u$ គេបាន

$$\begin{split} \frac{\mathrm{d}y}{\mathrm{d}x} &= \frac{\mathrm{d}y}{\mathrm{d}u} \times \frac{\mathrm{d}u}{\mathrm{d}x} = \frac{\mathrm{d}}{\mathrm{d}u} (\cos u) \times \frac{\mathrm{d}u}{\mathrm{d}x} = -\sin u \times u' = -u' \sin u \\ & \div \quad \frac{\mathrm{d}}{\mathrm{d}x} (\cos u) = -u' \sin u \end{split}$$

៣. បើ u ជាអនុគមន៍នៃ x នោះ y = tan u គេបាន

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{d}y}{\mathrm{d}u} \times \frac{\mathrm{d}u}{\mathrm{d}x} = \frac{\mathrm{d}}{\mathrm{d}u}(\tan u) \times \frac{\mathrm{d}u}{\mathrm{d}x} = \frac{1}{\cos^2 u} \times u' = (1 + \tan^2 u) \times u'$$

$$\therefore (\tan u)' = \frac{u'}{\cos^2 u} = u'(1 + \tan^2 u)$$

៤. បើ u ជាអនុគមន៍នៃ x នោះ y = cot u គេបាន

$$\begin{split} \frac{\mathrm{d} y}{\mathrm{d} x} &= \frac{\mathrm{d} y}{\mathrm{d} u} \times \frac{\mathrm{d} u}{\mathrm{d} x} = \frac{\mathrm{d}}{\mathrm{d} u} (\cot u) \times \frac{\mathrm{d} u}{\mathrm{d} x} = -\frac{1}{\sin^2 u} \times u' = -(1 + \cot^2 u) \times u' \\ & \div (\cot u)' = -\frac{u'}{\sin^2 u} = -u'(1 + \cot^2 u) \end{split}$$

ន្ធទាហរណ៍ ៥. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$y = \sin(2x + 1)$$

$$M. y = \tan(2x + 1)$$

$$v = cos(2x + 1)$$

6.
$$y = \cot(2x + 1)$$
 9

ಜೀನಾ:;ಕಾಆ

9.
$$y = \sin(2x + 1) \Rightarrow y' = (2x + 1)'\cos(2x + 1) = 2\cos(2x + 1)$$

$$\texttt{ "b. } y = \cos(2x+1) \Rightarrow y' = -(2x+1)' \sin(2x+1) = -2\sin(2x+1)$$

$$\text{M. } y = \tan(2x+1) \Rightarrow y' = \frac{(2x+1)'}{\cos^2(2x+1)} = \frac{2}{\cos^2(2x+1)} = 2[1 + \tan^2(2x+1)]$$

$$\text{M. } y = \tan(2x+1) \Rightarrow y' = \frac{(2x+1)'}{\cos^2(2x+1)} = \frac{2}{\cos^2(2x+1)} = 2[1 + \tan^2(2x+1)]$$

$$\text{G. } y = \cot(2x+1) \Rightarrow y' = -\frac{(2x+1)'}{\sin^2(2x+1)} = -\frac{2}{\sin^2(2x+1)} = -2[1 + \cot^2(2x+1)] \text{ 1}$$

៦ នេះខែអនុឝនន៍អិចស្ប៉ូណខ់ស្យែល

ស្រាយថាបើ $y = a^x$ នោះ $y' = a^x . \ln a$

ទេស ខេស្សាន្ត

គេមាន $y=a^x$ តាមនិយមន័យ គេបាន

$$\begin{split} y' &= f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{a^{x_0 + h} - a^{x_0}}{h} \\ &= \lim_{h \to 0} \frac{a^{x_0} (a^h - 1)}{h} \\ &= a^{x_0} \lim_{h \to 0} \frac{a^h - 1}{h} \text{ im w } \lim_{x \to 0} \frac{a^x - 1}{x} = \ln a \\ &= a^{x_0} \cdot \ln a \\ \\ & \ \therefore \quad (a^x)' = a^x \cdot \ln a \end{split}$$

ខាន្នៅ ៦.១. បើ u ជាអនុគមន៍នៃ x នោះ $(a^u)' = u'a^u . \ln a$ ។

ស្ថែខាតាសំឃង្

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(a^{u}) \times \frac{du}{dx} = a^{u} \cdot \ln a \times u'$$

$$\therefore (a^{u})' = u' \cdot a^{u} \cdot \ln a)$$

ខ្វិតាហរណ៍ ៦. គណនា \mathbf{y}' ចំពោះ \mathbf{u} ជាអនុគមន៍នៃ \mathbf{x} នៃអនុគមន៍ខាងក្រោម៖

9.
$$y = e^x$$

$$v = a^{x^2-1}$$

$$M. y = e^{u}$$

ដំណោះស្រាយ

9.
$$y=e^x$$
 នោះ $y'=(e^x)'=e^x.\ln e=e^x$, $\ln e=1$

២.
$$y = a^{x^2-1}$$
 នោះ $y' = (x^{x^2-1})'a^{x^2-1} \ln a = 2x.a^{x^2-1} \ln a$

M.
$$y=e^u$$
 is: $y'=(e^u)'=u'e^u.\ln e=u'e^u$, $\ln e=1$

៧ ខេរីទេខែអនុគមន៍អោភាអ៊

ស្រាយបញ្ហាក់ថា បើ $y = \log_a x$, a > 0 , $a \neq 1$ នោះ $y' = \frac{1}{x \ln a}$ ។

អសិខាតាតយ៉ាង

គេមាន $y = \log_a x$ តាមនិយមន័យ គេបាន

$$y' = f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{\log_a(x_0 + h) - \log_a(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{1}{h} \log_a \left(\frac{x_0 + h}{x_0}\right)$$

$$= \lim_{h \to 0} \log_a \left(1 + \frac{h}{x_0}\right)^{\frac{1}{h}}$$

$$= \log_a \left(\lim_{h \to 0} \ln\left(1 + \frac{h}{x_0}\right)^{\frac{1}{h}}\right)^{\frac{1}{x_0}}$$

$$= \log_a e^{\frac{1}{x_0}} = \frac{1}{x_0} \frac{\ln e}{\ln a}$$

$$\therefore (\log_a x)' = \frac{1}{x \ln a}, a > 0, a \neq 1$$

ខាន្នៅ ៧.១. បើ u ជាអនុគមន៍នៃ x នោះ $(\log_a u)' = \frac{u'}{u \ln a}$, a>0, $a\neq 1$ ។

ಘತಿಕಾಣಕಯೆು

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\begin{split} \frac{\mathrm{d} y}{\mathrm{d} x} &= \frac{\mathrm{d} y}{\mathrm{d} u} \times \frac{\mathrm{d} u}{\mathrm{d} x} = \frac{\mathrm{d}}{\mathrm{d} u} (\log_\mathrm{a} u) \times \frac{\mathrm{d} u}{\mathrm{d} x} = \frac{1}{u \ln a} \times u' \\ & \therefore \quad (\log_\mathrm{a} u)' = \frac{u'}{u \ln a} \; , \mathrm{a} > 0, \mathrm{a} \neq 1 \end{split}$$

៤ ខេរ្តិខេរ្តិមមនុខ្លួនស្វារម្នៃខេត្ត

ស្រាយបញ្ជាក់ថា បើ $y = \ln x$ នោះ $y' = \frac{1}{x}$ ។

ಹುಳುಣಣಮೆ,

គេមាន $y = \ln x$ តាមនិយមន័យ គេបាន

$$\begin{split} y' &= f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{\ln(x_0 + h) - \ln(x_0)}{h} \\ &= \lim_{h \to 0} \frac{\ln\left(\frac{x_0 + h}{x_0}\right)}{h} \\ &= \lim_{h \to 0} \frac{1}{h} \ln\left(1 + \frac{h}{x_0}\right) \\ &= \lim_{h \to 0} \ln\left(1 + \frac{1}{x_0}\right)^{\frac{1}{h}} \\ &= \ln\left[\lim_{h \to 0} \left(1 + \frac{1}{\frac{x_0}{h}}\right)^{\frac{x_0}{h} \times \frac{1}{x_0}}\right], \lim_{h \to 0} \left(1 + \frac{1}{\frac{x_0}{h}}\right)^{\frac{x_0}{h}} = e \\ &= \ln e^{\frac{1}{x_0}}, \ln e = 1 \\ &\therefore \quad (\ln x)' = \frac{1}{x} \end{split}$$

ខ្វិតាហរណ៍ ៧. រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x^2 \cdot \log_a x$$
, $a > 0$, $a \neq 1$

G.
$$f(x) = \log(x^2 \sqrt{x^3 - 1})$$

$$0. f(x) = \sin(2x) + \log_2(x^2 + 1)$$

ರೆ.
$$f(x) = (\sin x)^{\log x}$$

$$\text{m. } f(x) = \frac{e^{2x} + \log_3 x}{x^2}$$

$$\mathfrak{d}$$
. $f(x) = (\log_a x)^{\ln(2x)}, a > 0, a \neq 1$

೫೬೩೩೩೩೩

9.
$$f(x) = x^2 \cdot \log_a x$$
, $a > 0$, $a \neq 1 \Longrightarrow f'(x) = (x^2)' \log_a x + (\log_a x)' x^2$

$$= 2x \log_a x + \frac{1}{x \ln a} x^2$$

$$\therefore f'(x) = 2x \log_a x + \frac{x}{\ln a}, a > 0, a \neq 1$$

$$\text{ \it th}. \ \ f(x) = \sin(2x) + \log_2(x^2+1) \Longrightarrow f'(x) = -(2x)'\cos(2x) + \frac{(x^2+1)'}{(x^2+1)\ln 2}$$

$$\ \, : \quad f'(x) = -2\cos(2x) + \frac{2x}{(x^2+1)\ln 2}$$

$$\begin{split} \text{M. } f(x) &= \frac{\mathrm{e}^{2x} + \log_3 x}{x^2} \Longrightarrow f'(x) = \frac{(\mathrm{e}^{2x} + \log_3 x)'x^2 - (x^2)'(\mathrm{e}^{2x} + \log_3 x)}{x^4} \\ &= \frac{(2\mathrm{e}^{2x} + \frac{1}{x \ln 3})x^2 - 2x(\mathrm{e}^{2x} + \log_3 x)}{x^4} \\ &= \frac{2x\mathrm{e}^{2x} + \frac{1}{\ln 3} - 2\mathrm{e}^{2x} - 2\log_3 x}{x^3} \\ & \therefore \quad f'(x) &= \frac{2\mathrm{e}^{2x}(x-1) + \frac{1}{\ln 3} - \log_3 x^2}{x^3} \end{split}$$

$$\begin{aligned} \text{d. } f(x) &= \log(x^2\sqrt{x^3-1}) = \log x^2 + \log(x^3-1)^{\frac{1}{2}} = 2\log x + \frac{1}{2}\log(x^3-1) \\ & \therefore \quad f'(x) = \frac{2}{x\ln 10} + \frac{(x^3-1)'}{2(x^3-1)\ln 10} = \frac{2}{x\ln 10} + \frac{3x^2}{2(x^3-1)\ln 10} \\ \text{d. } f(x) &= (\sin x)^{\log x} \iff \ln f(x) = \ln(\sin x)^{\log x} \end{aligned}$$

$$\begin{aligned} \left(\ln f(x)\right)' &= (\log x. \ln(\sin x))' \\ \frac{f'(x)}{f(x)} &= (\log x)' \ln(\sin x) + (\ln(\sin x))' \log x \\ f'(x) &= f(x) \left(\frac{1}{x \ln 10} \ln(\sin x) + \frac{(\sin x)'}{\sin x}. \log x\right) \\ \therefore f'(x) &= (\sin x)^{\log x} \left(\frac{\ln(\sin x)}{x \ln 10} + \cot x. \log x\right) \end{aligned}$$

$$\vartheta. \ f(x) = (\log_a x)^{\ln(2x)}, a > 0, a \neq 1 \Longleftrightarrow \ln f(x) = \ln(\log_a x)^{\ln(2x)}$$

$$\begin{split} &(\ln f(x))' = \left(\ln(2x).\ln(\log_a x)\right)' \\ &\frac{f'(x)}{f(x)} = (\ln(2x))'\ln(\log_a x) + (\ln(\log_a x))'\ln(2x) \\ &f'(x) = f(x)\left(\frac{(2x)'}{2x}\ln(\log_a x) + \frac{(\log_a x)'}{\log_a x}\ln(2x)\right) \\ &\therefore \quad f'(x) = (\log_a x)^{\ln(2x)}\left(\frac{\ln(\log_a x)}{x} + \frac{\ln(2x)}{x\ln a\log_a x}\right), a > 0, a \neq 1 \end{split}$$

ខានុនៅ ៤.១. បើ
$$u$$
 ជាអនុគមន៍នៃ x នោះ $(\ln u)' = \frac{u'}{u}$ ។

ಣ ನಿಲಾಣ ಣಯು ಜ

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\begin{split} \frac{\mathrm{d} y}{\mathrm{d} x} &= \frac{\mathrm{d} y}{\mathrm{d} u} \times \frac{\mathrm{d} u}{\mathrm{d} x} = \frac{\mathrm{d}}{\mathrm{d} u} (\ln u) \times \frac{\mathrm{d} u}{\mathrm{d} x} = \frac{1}{u} \times u' \\ & \therefore \quad (\ln u)' = \frac{u'}{u} \end{split}$$

ខ្វិតាហរណ៍ ${f d}$. រក ${f f}'({f x})$ នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x \cdot \ln x$$

d.
$$f(x) = \ln(x^2 \sqrt{x^3 - 1})$$

$$0. f(x) = x^2 + \ln(x^2 + 1)$$

ය.
$$f(x) = x^x$$

$$\mathfrak{m.} \ f(x) = \frac{e^x + \ln x}{x^2}$$

$$\delta. f(x) = (\sin x)^{\cos x}$$

9.
$$f(x) = x \cdot \ln x \implies f'(x) = x' \ln x + (\ln x)' x = \ln x + \frac{1}{x} \cdot x = \ln x + 1$$

$$\mathfrak{V}. \ f(x) = x^2 + \ln(x^2 + 1) \Longrightarrow f'(x) = (x^2)' + \frac{(x^2 + 1)'}{x^2 + 1} = 2x + \frac{2x}{x^2 + 1}$$

$$\text{M. } f(x) = \frac{e^x + \ln x}{x^2} \Longrightarrow f'(x) = \frac{(e^x + \ln x)' x^2 - (x^2)' (e^x + \ln x)}{(x^2)^2}$$

$$= \frac{\left(e^{x} + \frac{1}{x}\right)x^{2} - 2x(e^{x} + \ln x)}{x^{4}}$$

$$\therefore f'(x) = \frac{xe^{x} + 1 - 2e^{x} - 2\ln x}{x^{3}}$$

$$\text{d. } f(x) = \ln(x^2 \sqrt{x^3 - 1}) = \ln x^2 + \ln \sqrt{x^3 - 1} = 2 \ln x + \ln(x^3 - 1)^{\frac{1}{2}}$$

$$f'(x) = 2(\ln x)' + \frac{1}{2}[\ln(x^3 - 1)]'$$
$$= 2 \cdot \frac{1}{x} + \frac{1}{2} \cdot \frac{(x^3 - 1)'}{x^3 - 1}$$

$$\therefore f'(x) = \frac{2}{x} + \frac{3}{2} \cdot \frac{x^2}{x^3 - 1}$$

ರೆ. $f(x) = x^x \iff \ln f(x) = \ln x^x = x \ln x$

$$(\ln f(x))' = (x \ln x)'$$

$$\frac{f'(x)}{f(x)} = x' \ln x + (\ln x)'x$$

$$f'(x) = f(x)(\ln x + \frac{1}{x}.x)$$

$$\therefore f'(x) = x^x(\ln x + 1)$$

 $\vartheta. \ f(x) = (\sin x)^{\cos x} \Longleftrightarrow \ln f(x) = \ln(\sin x)^{\cos x}$

$$\begin{aligned} \left(\ln f(x)\right)' &= (\cos x \ln \sin x)' \\ \frac{f'(x)}{f(x)} &= (\cos x)' \ln \sin x + (\ln \sin x)' \cos x \\ f'(x) &= f(x) \left(-\sin x \ln \sin x + \frac{(\sin x)'}{\sin x} \cdot \cos x\right) \\ \therefore f'(x) &= (\sin x)^{\cos x} \left(\cos x \cot x - \sin x \ln \sin x\right) \end{aligned}$$

៩ នេះីទេខែអនុឝមន៍ Arc Sine និ១ Arc Tangent

$$y = \arcsin x \iff x = \sin y \ \Re \theta - \frac{\pi}{2} \le y \le \frac{\pi}{2},$$

 $y = \arctan x \iff x = \tan y \ \Re \theta - \frac{\pi}{2} \le y \le \frac{\pi}{2},$

បើ
$$y = \arcsin x$$
 នោះ $y' = \frac{1}{\sqrt{1-x^2}}$ ។

ស្ខេតខេយាង

បើ $y = \arcsin x$ នោះ $x = \sin y$ ធ្វើដេរីវេអង្គសងខាងធៀបនឹង x គេបាន

$$(x)' = (\sin y)' \iff 1 = y' \cos y$$
$$y' = \frac{1}{\cos y}, \sin^2 y + \cos^2 y = 1 \implies \cos y = \pm \sqrt{1 - \sin^2 x}$$

ដោយ
$$-\frac{\pi}{2} \leq y \frac{\pi}{2} \Longrightarrow \cos y \geq 0 \Longrightarrow \cos y = \sqrt{1-x^2}$$

$$\therefore (\arcsin x)' = \frac{1}{\sqrt{1 - x^2}}$$

បើ $y = \arctan x$ នោះ $y' = \frac{1}{1 + x^2}$ ។

೫೬೩೩೩೩೩

បើ $y = \arctan x$ នោះ $x = \tan y$ ធ្វើដេរីវេអង្គសងខាងធៀបនឹង x គេបាន

$$(x)' = (\sin y)' \iff 1 = y'(1 + \tan^2 y)$$
$$y' = \frac{1}{1 + \tan^2 y}$$
$$\therefore (\arctan x)' = \frac{1}{1 + x^2}$$

ខាន្ទនៅ ៩.១. បើ u ជាអនុគមន៍នៃ x នោះ $(\arcsin u)' = \frac{u'}{\sqrt{1-x^2}}$

೫೬೩೩೩೩೩

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{d}y}{\mathrm{d}u} \times \frac{\mathrm{d}u}{\mathrm{d}x} = \frac{\mathrm{d}}{\mathrm{d}u}(\arcsin u) \times \frac{\mathrm{d}u}{\mathrm{d}x} = \frac{1}{\sqrt{1 - u^2}} \times u'$$

$$\therefore (\arcsin u)' = \frac{u'}{\sqrt{1 - u^2}}$$

ខាន្តនៅ ៩.២. បើ u ជាអនុគមន៍នៃ x នោះ $(\arctan u)' = \frac{u'}{1+u^2}$

ទេស ខេត្ត ខេត្

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{\mathrm{dy}}{\mathrm{dx}} = \frac{\mathrm{dy}}{\mathrm{du}} \times \frac{\mathrm{du}}{\mathrm{dx}} = \frac{\mathrm{d}}{\mathrm{du}} (\arctan u) \times \frac{\mathrm{du}}{\mathrm{dx}} = \frac{1}{1 - u^2} \times u'$$

$$\therefore (\arctan u)' = \frac{u'}{1 + u^2}$$

សំទារត់ ១. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \arcsin x \cdot \sin x$$

$$M$$
. $f(x) = \sin(\arcsin x)$

$$\mathfrak{V}$$
. $f(x) = \arctan x \cos x$

$$G$$
. $f(x) = \arctan(\tan x)$

សសៃតាតយ៉ាង

9. $f(x) = \arcsin x \cdot \sin x \implies f'(x) = (\arcsin x)' \sin x + (\sin x)' \arcsin x$

$$\therefore f'(x) = \frac{\sin x}{\sqrt{1 - x^2}} + \cos x. \arcsin x$$

 ${\mathfrak v}.\ \, f(x)=\arctan x\cos x\Longrightarrow f^{'}(x)=(\arctan x)'\cos x+(\cos x)'\arctan$

$$\therefore f'(x) = \frac{\cos x}{1 + x^2} - \sin x. \arctan x$$

 $\label{eq:final_state} \texttt{M.} \ \ f(x) = \sin(\arcsin x) \Longrightarrow f'(x) = (\arcsin x)' \cos(\arcsin x)$

$$\therefore f'(x) = \frac{\cos(\arcsin x)}{\sqrt{1 - x^2}}$$

G.
$$f(x) = \arctan(\tan x) \Longrightarrow f'(x) = \frac{(\tan x)'}{1 + (\tan x)^2} = \frac{1 + \tan^2 x}{1 + \tan^2 x}$$

$$\therefore f'(x) = 1$$

លអ្នលរះនៃខេត្តខេ

បើ f, g, y, u, v ជាអនុគមន៍នៃ x និង k ជាចំនួនថេនោះគេបាន៖

9.
$$(u \pm v)' = u' \pm v'$$

$$\mathbf{M}. \ (\mathbf{u}\mathbf{v})' = \mathbf{u}'\mathbf{v} + \mathbf{v}'\mathbf{u}$$

២.
$$(ku)' = ku'$$

$$\text{d. } \left(\frac{u}{v}\right)' = \frac{u'v - v'u}{v^2}$$

$$\mathbf{c}. \ \frac{\mathrm{dy}}{\mathrm{dx}} = \frac{\mathrm{dy}}{\mathrm{du}} \cdot \frac{\mathrm{du}}{\mathrm{dx}}$$

$$\mathfrak{d}. \left(\frac{1}{v}\right)' = -\frac{v'}{v^2}$$

រួមមន្ត្តនៃនេះទេ

បើ $\mathrm{C},\mathrm{a},\mathrm{b},\mathrm{c}$ ជាចំនួនថេ និង u ជាអនុគមន៍នៃ x ដែល $\mathrm{n}\in\mathbb{N}$ គេបាន៖

9.
$$(C)' = 0$$

$$v(x)' = 1$$

$$\mathbf{M}. \ (\mathbf{a}\mathbf{x} + \mathbf{b})' = \mathbf{a}$$

$$6. (ax^2 + bx + c)' = 2ax + b$$

៥.
$$(x^n)' = nx^{n-1}$$

່ວ.
$$(u^n)' = n.u'.u^{n-1}$$

$$\mathfrak{N}. (x)^{-n} = -\frac{n}{x^{n+1}}$$

$$G. \left(\frac{1}{x}\right)' = -\frac{1}{x^2}$$

$$\mathcal{E}. \left(\frac{1}{u}\right)' = -\frac{u}{u^2}$$

90.
$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

99.
$$(\sqrt{\mathbf{u}})' = \frac{\mathbf{u}'}{2\sqrt{\mathbf{u}}}$$

90.
$$(\sqrt[n]{x})' = \frac{1}{\sqrt[n]{x^{n-1}}}$$
90. $(\ln x)' = \frac{1}{x}$
96. $(\ln u)' = \frac{u'}{u}$

9M.
$$(\ln x)' = \frac{1}{x}$$

១៤.
$$(\ln u)' = \frac{u'}{u}$$

១៥.
$$(\log_a x)' = \frac{1}{x \ln_a}$$
, $a > 0$, $a \neq 1$

95.
$$(\log_a u)' = \frac{u'}{u \cdot \ln a}, a > 0, a \neq 1$$

91.
$$(a^x)' = a^x \ln a, a > 0, a \neq 1$$

9G.
$$(a^u)' = u'a^u \ln a, a > 0, a \neq 1$$

២០.
$$(e^u)' = u'e^u$$

២១.
$$(\sin x)' = \cos x$$

២២.
$$(\sin u)' = u' \cos u$$

$$UM. (\cos x)' = -\sin x$$

២៤.
$$(\cos u)' = -u' \sin u$$

២៥.
$$(\tan x)' = \frac{1}{\cos^2 x} = 1 + \tan^2 x$$

២៦.
$$(\tan u)' = \frac{u'}{\cos^2 u} = u'(1 + \tan^2 u)$$

២៧.
$$(\cot x)' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$$

$$\text{UG. } (\cot u)' = -\frac{u'}{\sin^2 u} = -(1 + \cot^2 u)$$

UE.
$$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$

$$\text{M0. } (\arcsin u)' = \frac{u'}{\sqrt{1 - u^2}}$$

M9.
$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$$

MU.
$$(\arccos u)' = -\frac{u'}{\sqrt{1-u^2}}$$

$$MM. (\arctan x)' = \frac{1}{1+x^2}$$

$$\text{Md. } (\arctan u)' = \frac{u'}{1 + u^2}$$

M៥.
$$(\operatorname{arccot} x)' = -\frac{1}{1+x^2}$$

Mb. $(\operatorname{arccot} u)' = -\frac{u'}{1+u^2}$

Mb.
$$(\operatorname{arccot} u)' = -\frac{u'}{1 + u^2}$$

$$\mathbf{MN}. \ (\mathbf{u}^{\mathbf{v}})' = \left(\mathbf{v}'.\ln\mathbf{u} + \frac{\mathbf{v}.\mathbf{u}'}{\mathbf{u}}\right).\mathbf{u}^{\mathbf{v}}$$

លំមាន់ និទ ជំណោះស្រាយ

សំទាាត់ ២. គណនា f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1$$

U.
$$f(x) = 2x^2 - \sqrt{x} + \frac{2}{x}$$

M. $f(x) = (x^4 - 7x^2 + \sin a)^7$
G. $f(x) = (x^2 - \sqrt{x})^{2019}$

$$f(x) = (x^4 - 7x^2 + \sin a)^7$$

G.
$$f(x) = (x^2 - \sqrt{x})^{2019}$$

ರೆ.
$$f(x) = \sqrt{x^3 - x^2 + 3}$$

່ວ.
$$\sqrt[4]{x^3 - 2x}$$

$$\mathfrak{N}. \ f(x) = (x+1)(2x-1)^2$$

G.
$$f(x) = (x^2 + 2x + 3)(x^3 - 3x - 1)$$

$$\epsilon$$
. $f(x) = \frac{1}{x-1}$

8.
$$f(x) = \frac{1}{x-1}$$

90. $f(x) = \frac{x}{x+1}$

ស្សមាយមញ្ញាអ

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1 \implies f'(x) = 5x^4 - 4x^3 + 3x^2 - 2x + 1$$

$$\text{U. } f(x) = 2x^2 - \sqrt{x} - \frac{2}{x} \Longrightarrow f'(x) = 4x^2 + \frac{1}{2\sqrt{x}} - \frac{2}{x^2}$$

$$f'(x) = 7(x^4 - 7x^2 + \sin a)'(x^4 - 7x^2 + \sin a)^{7-1} = 7(4x^3 - 14x)(x^4 - 7x^2 + \sin a)^6$$

$$\mathbf{m.} \ \mathbf{f}(\mathbf{x}) = (\mathbf{x}^4 - 7\mathbf{x}^2 + \sin \mathbf{a})^7$$

G.
$$f(x) = (x^2 - \sqrt{x})^{2019} \implies f'(x) = 2019(x^2 - \sqrt{x})'(x^2 - \sqrt{x})^{2019-1}$$

$$=2019\left(2x-\frac{1}{2\sqrt{x}}\right)(x^2-\sqrt{x})^{2018}$$

$$\text{d. } f(x) = \sqrt{x^3 - x^2 + 3} \Longrightarrow f'(x) = \frac{(x^3 - x^2 + 3)'}{2\sqrt{x^3 - x^2 + 3}} = \frac{3x - 2}{2\sqrt{x^3 - x^2 + 3}}$$

$$\text{b. } \sqrt[4]{x^3 - 2x} \Longleftrightarrow f(x) = (x^3 - 2x)^{\frac{1}{4}}$$

b.
$$\sqrt[4]{x^3 - 2x} \iff f(x) = (x^3 - 2x)^{\frac{1}{2}}$$

$$f'(x) = \frac{1}{4}(x^3 - 2x)'(x^3 - 2x)^{\frac{1}{4} - 1}$$
$$= \frac{1}{4}(3x^2 - 2)(x^3 - 2x)^{-\frac{3}{4}}$$

$$f'(x) = \frac{3x^2 - 2}{4\sqrt[4]{(x^3 - 2x)^3}}$$

 \mathfrak{N} . $f(x) = (x+1)(2x-1)^2$

$$f'(x) = (x+1)'(2x-1)^2 + [(2x-1)^2]'(x+1)$$

$$= (2x-1)^2 + 2(2x-1)'(2x-1)(x+1)$$

$$= (2x-1)(2x-1+4x+4)$$

$$\therefore f'(x) = (2x-1)(6x+3)$$

G. $f(x) = (x^2 + 2x + 3)(x^3 - 3x - 1)$

$$f'(x) = (x^2 + 2x + 3)'(x^2 - 3x - 1) + (x^2 - 3x - 1)'(x^2 + 2x + 3)$$

$$= (2x + 2)(x^2 - 3x - 1) + (2x - 3)(x^2 + 2x + 3)$$

$$= 2x^3 - 6x^2 - 2x + 2x^2 - 6x - 2 + 2x^3 + 4x^2 + 6x - 3x^2 - 6x - 9$$

$$\therefore f'(x) = 4x^3 - 3x^2 - 8x - 11$$

$$\mathcal{E}. \ f(x) = \frac{1}{x-1} \Longrightarrow f'(x) = -\frac{(x-1)'}{(x-1)^2} = -\frac{1}{(x-1)^2}$$

$$90. \ f(x) = \frac{x\sqrt{x}}{x+1}$$

$$\begin{split} f'(x) &= \frac{(x\sqrt{x})'(x+1) - (x+1)'x\sqrt{x}}{(x+1)^2} \\ &= \frac{[x'\sqrt{x} + (\sqrt{x})'x](x+1) - x\sqrt{x}}{(x+1)^2} \\ &= \frac{\left(x + \frac{x}{2\sqrt{x}}\right)(x+1) - x\sqrt{x}}{(x+1)^2} \\ &= \frac{x\sqrt{x} + \sqrt{x} + \frac{x}{2\sqrt{x}}(x+1) - x\sqrt{x}}{(x+1)^2} \\ & \therefore \quad f'(x) &= \frac{x^2 + 3x}{2\sqrt{x}(x+1)^2} \end{split}$$

សំសារត់ ៣. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x \cdot \sin x + \cos x$$

G.
$$f(x) = \sin^2 \sqrt{x} + \cos^2(3x)$$

$$0. f(x) = \sin^3 x - x \cdot \cos x$$

៥.
$$f(x) = \cos(3x + 4) + 3\cos x \cdot \sin x$$

$$\text{M. } f(x) = \cos(x^2 + 1) + 2\sin(x^2 - 1)$$

$$\delta$$
. $f(x) = \sin(\sin \sqrt{x}) + \cos^3 x$

ಜೀಚಾ:ಕ್ರಾಟ

9.
$$f(x) = x \cdot \sin x + \cos x$$

$$f'(x) = x' \sin x + (\sin x)'.x - \sin x$$
$$= \sin x + x.\cos x - \sin x$$

$$f'(x) = x \cdot \cos x$$

$$0. f(x) = \sin^3 x - x \cdot \cos x$$

$$f'(x) = 3(\sin x)' \sin^{3-1} x - [x'.\cos x + (\cos x)'.x]$$
$$= 3\cos x. \sin^2 x - (\cos x - x.\sin x)$$

$$f'(x) = 3\cos x \cdot \sin^2 x - \cos x + x\sin x$$

$$\text{ M. } f(x) = \cos(x^2 + 1) + 2\sin(x^2 - 1)$$

$$f'(x) = -(x^2 + 1)'\sin(x^2 + 1) + 2(x^2 - 1)'\cos(x^2 - 1)$$

$$\therefore \ f'(x) = -2x\sin(x^2 + 1) + 4x\cos(x^2 - 1)$$

$$\text{G. } f(x) = \sin^2 \sqrt{x} + \cos^2(3x)$$

$$\begin{split} f'(x) &= 2(\sin\sqrt{x})'\cos^{2-1}\sqrt{x} + 2(\cos(3x))'\sin(3x) \\ &= 2(\sqrt{x})'.\cos\sqrt{x}.\cos\sqrt{x} - 2(3x)'\sin(3x).\sin(3x) \\ &\therefore \quad f'(x) = \frac{1}{\sqrt{x}}.\cos^2\sqrt{x} - 6\sin^2(3x) \end{split}$$

 $g(x) = \cos(3x + 4) + 3\cos x \cdot \sin x$

$$f'(x) = -(3x + 4)' \cdot \sin(3x + 4) + 3[(\cos x)' \cdot \sin x + (\sin x)' \cdot \cos x]$$

$$= -3\sin(3x + 4) + 3[-\sin x \cdot \sin x + \cos x \cdot \cos x]$$

$$\therefore f'(x) = -3[\sin(3x + 4) + \sin^2 x - \cos^2 x]$$

 δ . $f(x) = \sin(\sin \sqrt{x}) + \cos^3 x$

$$\begin{split} f'(x) &= (\sin\sqrt{x})' \cdot \cos(\sin\sqrt{x}) + 3(\cos x)\cos^{3-1}x \\ &= (\sqrt{x})' \cdot \cos\sqrt{x} \cdot \cos(\sin\sqrt{x}) - 3\sin x\cos^2 x \\ &\therefore \quad f'(x) &= \frac{1}{2\sqrt{x}}\cos\sqrt{x} \cdot \cos(\sin\sqrt{x}) - 3\sin x \cdot \cos^2 x \end{split}$$

សំខាន់ ៤. គណនាដើរវៃនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = (1 + \tan x)^4$$

$$\text{ \it m. } f(x) = x. \tan(x^2 - 1) + x \cot(2x^2 - 3)$$

9.
$$f(x) = (1 + \tan x)^4$$

9. $f(x) = x^2 \tan x + (1 + \cot x)^2$

G.
$$f(x) = \frac{\tan(2x)}{1 - \cos x}$$

នុះឃោះទេខ

9. $f(x) = (1 + \tan x)^4$

$$f'(x) = 4(1 + \tan x)'(1 + \tan^2 x)^{4-1}$$

:
$$f'(x) = 4(1 + \tan^2 x)(1 + \tan x)^3$$

 $0. f(x) = x^2 \tan x + (1 + \cot x)^2$

$$f'(x) = (x^2)' \tan x + (\tan x)' x^2 + 2(1 + \cot x)' (1 + \cot x)^{2-1}$$

$$\therefore f'(x) = 2x \tan x + x^2 (1 + \tan^2 x) - 2(1 + \cot^2 x)(1 + \cot x)$$

$$f(x) = x \cdot \tan(x^2 - 1) + x \cot(2x^2 - 3)$$

$$\begin{split} f'(x) &= x' \tan(x^2 - 1) + [\tan(x^2 - 1)]'x + x' \cot(2x^2 - 3) + [\cot(2x^2 - 3)]'x \\ &= \tan(x^2 - 1) + (x^2 - 1)'[1 + \tan^2(x^2 - 1)]x - (2x^2 - 3)'[1 + \cot^2(2x^2 - 3)]x \\ &\therefore \quad f'(x) = \tan(x^2 - 1) + 2x^2[1 + \tan^2(x^2 - 1)] - 4x^2[1 + \cot^2(2x^2 - 3)] \end{split}$$

សំទាាត់ ៥. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \frac{1 - x - 2x^2}{x^3 - \ln 3}$$

10. $f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x - x^2}}$
11. $f(x) = \sin x^2 \cdot \tan(2x + 3)$
12. $f(x) = \sin(x^2 + 5) + \cos(\sin x)$
13. $f(x) = \sin(x^2 + 5) + \cos(\sin x)$
14. $f(x) = \sin(x^2 + 5) + \cos(\sin x)$
15. $f(x) = \sin(x^2 + 5) + \cos(\sin x)$

ដំណោះស្រាយ

9.
$$f(x) = \frac{1 - x - 2x^{2}}{x^{3} - \ln 3}$$

$$f'(x) = \frac{(1 - x - 2x^{2})'(x^{3} - \ln 3) - (x^{3} - \ln 3)'(1 - x - 2x^{2})}{(x^{3} - \ln 3)^{2}}$$

$$= \frac{(-1 - 4x)(x^{3} - \ln 3) - 3x^{2}(1 - x - 2x^{2})}{(x^{3} - \ln 3)^{2}}$$

$$= \frac{-x^{3} + \ln 3 - 4x^{4} + 4x \ln 3 - 3x^{2} + 3x^{3} + 6x^{4}}{(x^{3} - \ln 3)^{2}}$$

$$\therefore f'(x) = \frac{2x^{4} + 2x^{3} - 3x^{2} + 4x \cdot \ln 3 + \ln 3}{(x^{3} - \ln 3)^{2}}$$

២.
$$f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x - x^2}} \iff f(x).\sqrt{1 + 2x - x^2} = 2x^2 + 3x + 4$$
 ធ្វើដេរីជអង្គសងខាង គេបាន

$$\begin{split} [f(x)\sqrt{1+2x-x^2}]' &= (2x^2+3x+4)' \\ f'(x)\sqrt{1+2x-x^2} + (\sqrt{1+2x-x^2})'f(x) &= 4x+3 \\ f'(x)\sqrt{1+2x-x^2} + \frac{(1+2x-x^2)'}{2\sqrt{1+2x-x^2}}f(x) &= 4x+3 \\ f'(x)\sqrt{1+2x-x^2} &= 4x+3 - \frac{1-x}{\sqrt{1+2x-x^2}}.f(x) \\ & \therefore \quad f'(x) &= \frac{4x+3}{\sqrt{1+2x-x^2}} + \frac{(x-1)(2x^2+3x+4)}{(1+2x-x^2)\sqrt{1+2x-x^2}} \end{split}$$

$$f(x) = \sin x^2 \cdot \tan(2x + 3)$$

$$\begin{split} f'(x) &= (\sin x^2)' \tan(2x+3) + (\tan(2x+3))' \sin x^2 \\ &= (x^2)' \cdot \sin x^2 \cdot \tan(2x+3) + (2x+3)' [1 + \tan^2(2x+3)] \sin x^2 \\ &= 2x \sin x^2 \cdot \tan(2x+3) + 2 \sin x^2 [1 + \tan^2(2x+3)] \\ & \therefore \quad f'(x) = 2 \sin x^2 [\tan^2(2x+3) + x \tan(2x+3) + 1] \end{split}$$

G.
$$f(x) = \sin(x^2 + 5) + \cos(\sin x)$$

$$f'(x) = (x^2 + 5)' \cos(x^2 + 5) - (\sin x)' \sin(\sin x)$$

$$\therefore f'(x) = 2x \cos(x^2 + 5) - \cos x \sin(\sin x)$$

ಡೆ.
$$f(x) = \frac{\sin(\tan\sqrt{x})}{\sin(\sqrt{x})} \iff f(x).\sin\sqrt{x} = \sin(\tan\sqrt{x})$$

$$f'(x).\sin\sqrt{x} + (\sin\sqrt{x})'f(x) = (\tan\sqrt{x})'\cos(\tan\sqrt{x})$$

$$f'(x).\sin\sqrt{x} + (\sqrt{x})'\cos\sqrt{x}.f(x) = (\sqrt{x})'(1 + \tan^2\sqrt{x})\cos(\tan\sqrt{x})$$

 $(f(x). \sin \sqrt{x})' = (\sin(\tan \sqrt{x}))'$

$$f'(x)\sin\sqrt{x} + \frac{1}{2\sqrt{x}}\cos\sqrt{x}.f(x) = \frac{1}{2\sqrt{x}}(1 + \tan^2\sqrt{x})\cos(\tan\sqrt{x})$$

$$f'(x)\sin\sqrt{x} = \frac{1}{2\sqrt{x}}\left[(1 + \tan^2\sqrt{x})\cos(\tan\sqrt{x}) - \cos\sqrt{x}f(x)\right]$$

$$\therefore f'(x) = \frac{1}{2\sqrt{x}.\sin\sqrt{x}}\left[(1 + \tan^2\sqrt{x})\cos(\tan\sqrt{x}) - \cos\sqrt{x}f(x)\right]$$

$$,f(x) = \frac{\sin(\tan\sqrt{x})}{\sin(\sqrt{x})}$$

សំខាន់ ៦. គណនាដើរវៃនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = xe^x + \frac{1}{2}x^2$$

10. $f(x) = e^{x^2 + 2x + 1} + (x^2 - 3)e^x$
11. $f(x) = \frac{\sqrt{x}}{e^x}$

៤.
$$f(x) = x^3 e^{-3x}$$

$$f(x) = e^{x^2+2x+1} + (x^2-3)e^x$$

ರೆ.
$$f(x) = e^{2x}3^{x^2+1}$$

$$\mathbf{m.} \ \mathbf{f(x)} = \frac{\sqrt{\mathbf{x}}}{\mathbf{e}^{\mathbf{x}}}$$

$$\delta$$
. $f(x) = e^{\sin x \cos x}$

ជំនាះស្រួយ

9.
$$f(x) = xe^x + \frac{1}{2}x^2$$

$$f'(x) = x'e^x + (e^x)'x + \frac{1}{2}.2x = e^x + e^x x + x = e^x(1+x) + x$$

$$varpsite 0. f(x) = e^{x^2 + 2x + 1} + (x^2 - 3)e^x$$

$$f'(x) = (x^2 + 2x + 1)'e^{x^2 + 2x + 1} + (x^2 - 3)'e^x + (e^x)'(x^2 - 3)$$
$$= (2x + 2)e^{x^2 + 2x + 1} + 2xe^x + e^x(x^2 - 3)$$
$$\therefore f'(x) = 2(x + 1)e^{x^2 + 2x + 1} + e^x(2x + x^2 - 3)$$

$$\text{M. } f(x) = \frac{\sqrt{x}}{e^x}$$

$$f'(x) = \frac{(\sqrt{x})'e^x + (e^x)'\sqrt{x}}{(e^x)^2} = \frac{\frac{1}{2\sqrt{x}}e^x + e^x\sqrt{x}}{e^{2x}} = \frac{1 + 2x}{2\sqrt{x}e^x}$$

$$f(x) = x^3 e^{-3x}$$

$$f'(x) = (x^3)'e^{-3x} + (e^{-3x})'x^3$$

$$= 3x^2e^{-3x} + (-3x)'e^{-3x}x^3$$

$$= 3x^2e^{-3x} - 3e^3e^{-3x}$$

$$\therefore f'(x) = 3x^2e^{-3x}(1-x)$$

៥.
$$f(x) = e^{2x}3^{x^2+1}$$

$$\begin{split} f'(x) &= (e^{2x})'3^{x^2+1} + (3^{x^2+1})'.e^{2x} \\ &= (2x)'e^{2x}.3^{x^2+1} + (x^2+1)'3^{x^2+1}\ln 3.e^{2x} \\ &= 2.e^{2x}3^{x^2+1} + 2x3^{x^2+1}\ln 3.e^{2x} \\ & \therefore \quad f'(x) = 2e^{2x}3^{x^2+1}(1+x\ln 3) \end{split}$$

 $b. f(x) = e^{\sin x \cos x}$

$$f'(x) = (\sin x \cos x)' e^{\sin x \cos x}$$

$$= [(\sin x)' \cos x + (\cos x)' \cos x] e^{\sin x \cos x}$$

$$\therefore f'(x) = (\cos^2 x - \sin^2 x) e^{\sin x \cos x}$$

សំសាន់ ៧. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = (x^2 - 1) \ln(x^2 - 1)$$

$$\mathsf{M.}\ \mathrm{f}(\mathrm{x}) = \ln(\sin \mathrm{x}.\cos(2\mathrm{x}))$$

9.
$$f(x) = (x^2 - 1) \ln(x^2 - 1)$$

10. $f(x) = \ln\left(\frac{x^2 - 2}{\sqrt[3]{x^2 - 2}}\right)$

G.
$$f(x) = \ln\left(\sqrt{\frac{1+\sin x}{1-\sin x}}\right)$$

ជំណោះស្រួយ

9.
$$f(x) = (x^2 - 1) \ln(x^2 - 1) \Longrightarrow f'(x) = (x^2 - 1)' \ln(x^2 - 1) + \ln(x^2 - 1)'(x^2 - 1)$$

$$= 2x \ln(x^2 - 1) + \frac{(x^2 - 1)'}{x^2 - 1}.(x^2 - 1)$$
$$= 2x \ln(x^2 - 1) + 2x$$

:
$$f'(x) = 2x[\ln(x^2-1) + 1]$$

$$\text{ \it v. } f(x) = \ln \left(\frac{x^2 - 2}{\sqrt[3]{x^2 - 2}} \right) = \ln(x^2 - 2) - \ln(x^2 - 2)^{\frac{1}{3}}$$

$$\begin{split} f'(x) &= \frac{(x^2-2)'}{x^2-2} - \frac{1}{3} \cdot \frac{(x^2-2)'}{x^2-2} \\ &= \frac{3(2x)-2x}{3(x^2-2)} \end{split}$$

$$\therefore f'(x) = \frac{4x}{3(x^2 - 2)}$$

 $\mathsf{M}.\ \mathrm{f}(\mathrm{x}) = \ln(\sin \mathrm{x}.\cos(2\mathrm{x})) = \ln(\sin \mathrm{x}) + \ln(\cos(2\mathrm{x}))$

$$f'(x) = \frac{(\sin x)'}{\sin x} + \frac{(\cos(2x))'}{\cos(2x)}$$
$$= \frac{\cos x}{\sin x} - \frac{2\sin(2x)}{\cos(2x)}$$

$$\therefore f'(x) = \cot x - 2\tan(2x)$$

$$\text{G. } f(x) = \ln\left(\sqrt{\frac{1+\sin x}{1-\sin x}}\right) = \ln\left(\frac{1+\sin x}{1-\sin x}\right)^{\frac{1}{2}} = \frac{1}{2}\left(\ln(1+\sin x) - \ln(1-\sin x)\right)$$

$$\begin{split} f'(x) &= \frac{1}{2} \left(\frac{(1 + \sin x)'}{1 + \sin x} - \frac{(1 - \sin x)'}{1 - \sin x} \right) \\ &= \frac{1}{2} \left(\frac{\cos x}{1 + \sin x} + \frac{\cos x}{1 - \sin x} \right) \\ &= \frac{1}{2} \cdot \frac{(\cos x (1 - \sin x + 1 + \sin x))}{1 - \sin^2 x} \\ \therefore \quad f'(x) &= \frac{2 \cos x}{2 \cos^2 x} = \frac{1}{\cos x} \end{split}$$

សំសាត់ ៤. គណនាដេរីជេនអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \cos(\arcsin x)$$

៥.
$$f(x) = \arcsin \sqrt{x}$$

$$\mathfrak{V}$$
. $f(x) = \cot(\arctan x)$

$$\vartheta$$
. $f(x) = \arctan(\sin x)$

$$M$$
. $f(x) = \tan(\arctan x)$

$$\mathfrak{A}. f(x) = \frac{\arctan x}{\arcsin x}$$

$$G. f(x) = \arcsin(2x)$$

ಕ್ಷೀಚಾ:ಕಿಲಡಾ

9. $f(x) = \cos(\arcsin x) \Longrightarrow f'(x) = -(\arcsin x)' \sin(\arcsin x)$

$$\therefore f'(x) = -\frac{\sin(\arcsin x)}{\sqrt{1-x^2}}$$

 $0. \ f(x) = \cot(\arctan x) \Longrightarrow f'(x) = -(\arctan x)'[1 + \cot^2(\arctan x)]$

$$\therefore f'(x) = -\frac{1 + \cot^2(\arctan x)}{1 + x^2}$$

 $\label{eq:force_function} \mathfrak{M}.\ f(x) = \tan(\arctan x) \Longrightarrow f'(x) = (\arctan x)'[1 + \tan^2(\arctan x)]$

$$\therefore f'(x) = \frac{1 + \tan^2(\arctan x)}{1 + x^2}$$

$$\text{G. } f(x) = \arcsin(2x) \Longrightarrow f'(x) = \frac{(2x)'}{\sqrt{1 - (2x)^2}}$$

$$\therefore \ f'(x) = \frac{2}{\sqrt{1-4x^2}}$$

$$\text{c. } f(x) = \arcsin \sqrt{x} \Longrightarrow f'(x) = \frac{(\sqrt{x})'}{\sqrt{1 - (\sqrt{x})^2}} = \frac{\frac{1}{2\sqrt{x}}}{\sqrt{1 - x^2}} = \frac{1}{2\sqrt{x}\sqrt{1 - x^2}}$$

$$\therefore f'(x) = \frac{1}{2\sqrt{x-x^2}}$$

$$\mathfrak{d}.\ f(x)=\arctan(\sin x)\Longrightarrow f'(x)=\frac{(\sin x)'}{1+(\sin x)^2},\sin^2 x+\cos^2 x=1$$

$$\therefore f'(x) = \frac{\cos x}{2 - \cos^2 x}$$

$$\mathfrak{N}.\ f(x) = \frac{\arctan x}{\arcsin x} \Longrightarrow f'(x) = \frac{(\arctan x)'\arcsin x - (\arcsin x)'\arctan x}{(\arcsin x)^2}$$

$$\therefore f'(x) = \frac{\frac{\arcsin x}{1 + x^2} - \frac{\arctan x}{\sqrt{1 - x^2}}}{(\arcsin x)^2}$$

១. គណនាដេរីជនៃអនុគមន៍ខាងក្រោម៖

(fi)
$$y = x^3 + 2x^2$$

(2)
$$y = x^3 - 4x^2$$

(គ)
$$y = x^4 - 27x$$

(W)
$$v = x^4 - 5x^2 + 4$$

(ង)
$$y = x^5 - 16x$$

$$(\mathfrak{V}) \ y = \frac{x}{x+1}$$

២. រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

(ñ)
$$f(x) = \sin x + \cos x$$

(2)
$$f(x) = 2 \sin x - 3 \cos x$$

$$(\mathfrak{P}) f(x) = 3\sin x + 2\cos x$$

(W)
$$f(x) = x \sin x + \cos x$$

(ង)
$$f(x) = x \cos x - \sin x$$

(
$$\mathfrak{v}$$
) $f(x) = \cos(2x)$

$$(\mathfrak{F}) f(x) = \frac{1 - \sin(2x)}{1 - \sin x}$$

$$(\vec{u}) f(x) = 1 + \sin x^2$$

៣. រក y' នៃអនុគមន៍ខាងក្រោម៖

(fi)
$$xy = \frac{\pi}{6}$$

(2)
$$\sin(xy) = 1$$

(ল)
$$xy = \frac{1}{x + y}$$

(
$$\mathfrak{W}$$
) $x + y = xy$

(ង)
$$(y-1)^2 + x = 0$$

(
$$\Im$$
) $(y+1)^2 + y - x = 0$

(5)
$$(y-x)^2 + x = 0$$

(5)
$$y = \frac{x^2}{1 + x^2}$$

(ជ)
$$y = x - \frac{1}{x}$$

$$(w) y = x^3 + 2x^2 - x$$

$$(\mathfrak{Q}) y = x^4 - 2x^3 + 2x$$

(ដ)
$$y = \sqrt{1 + x^2}$$

(t)
$$y = \sqrt[4]{1 + x^2}$$

$$(\mathfrak{W}) \ f(x) = \cot x - \cos x$$

$$(\mathfrak{N}) f(x) = \sin(2x) - \cos(3x)$$

(ដ)
$$f(x) = \sin(\cos(3x))$$

(1)
$$f(x) = \frac{\sin x^2}{x^2}$$

$$(2) f(x) = \tan(1 + x^2)$$

(A)
$$f(x) = \cos 2x - \cos x^2$$

(M)
$$f(x) = (1 + \sqrt{1+x})^3$$

(
$$\ddot{u}$$
) $(y + x) + 2y - x = 0$

$$(\mathfrak{W}) \ (y^2 - 1)^2 + x = 0$$

$$(\mathfrak{O}) \ (y^2 + 1)^2 - x = 0$$

(
$$\ddot{a}$$
) $x^3 + xy + y^3 = 3$

(ប)
$$\sin x + \sin y = 1$$

$$(2) \sin x + xy + y^5 = \pi$$

(AS)
$$\tan x + \tan y = 1$$

(n)
$$f(x) = \sqrt{1-x}$$

(2)
$$f(x) = \sqrt[4]{x + x^2}$$

(គ)
$$y = \sqrt{1 - \sqrt{x}}$$

(W)
$$y = \sqrt{x - \sqrt{x}}$$

(ង)
$$y = \sqrt[3]{\sqrt{2x+1}} - x^2$$

(ii)
$$y = \sqrt[4]{x + x^2}x + x^2$$

(5)
$$y = \sqrt[3]{x - \sqrt{2x + 1}}$$

(
$$\vec{a}$$
) $y = \sqrt[4]{3}\sqrt{x} + \sqrt[3]{\sqrt{x}} + \sqrt{x}$

៥. គណនាដេរីវេនៃអនៃអនុគមន៍ខាងក្រោម៖

(fi)
$$f(x) = e^x + e^{-x}$$

(2)
$$f(x) = e^{3x} + 4e^x$$

$$(\mathbf{\tilde{n}}) \ \mathbf{f}(\mathbf{x}) = \frac{\mathbf{e}^{\mathbf{x}}}{1 + \mathbf{e}^{\mathbf{x}}}$$

$$\begin{array}{l} \text{(fi)} \ \ f(x) = \frac{e^x}{1 + e^x} \\ \text{(W)} \ \ f(x) = \frac{2e^{2x}}{1 + e^{2x}} \end{array}$$

(ង)
$$f(x) = xe^{-x} + x \ln x$$

(ii)
$$f(x) = \sqrt{x}e^{-\frac{x}{4}} + x^2e^{x+2}$$

(3)
$$f(x) = x^{-\frac{1}{2}x} + \ln \sqrt{x}$$

$$(\vec{u}) \ f(x) = (\ln x)^2 + \ln x + 1$$

(W)
$$f(x) = \frac{\ln x}{x} + \ln \frac{1}{x}$$

$$(\mathfrak{O}) \ f(x) = \ln\left(\sqrt{\frac{\sqrt{x}+1}{\sqrt{x}-1}}\right)$$

៦. គណនាដេរីវេនៃអនៃអនុគមន៍ខាងក្រោម៖

(
$$\tilde{n}$$
) $f(x) = \tan(\arctan x)$

(2)
$$f(x) = \arcsin(\sin x)$$

(គ)
$$f(x) = \cot(\arcsin x)$$

(
$$\mathfrak{W}$$
) $f(x) = \sin(\arctan x)$

(ង)
$$f(x) = (\arcsin x)^2$$

$$(\mathfrak{F}) \ \mathrm{f}(\mathrm{x}) = \frac{1}{1 + (\arctan \mathrm{x})^2}$$

$$(\mathfrak{F}) \ f(x) = \sqrt{1 - (\arcsin x)^2}$$

៧. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

(ñ)
$$y = (x+1)(x-1)$$

(2)
$$y = (x^2 + 1)(x^2 - 1)$$

(f)
$$y = \frac{1}{x+1} + \frac{1}{1+\sin x}$$

(w) $y = \frac{1}{1+x^2} + \frac{1}{1-\sin x}$

(w)
$$y = \frac{1}{1+x^2} + \frac{1}{1-\sin x}$$

(ង)
$$y = (x-1)(x-2)(x-3)$$

(ii)
$$y = x^2 \cos x + 2x \sin x$$

(5)
$$y = x^{\frac{1}{2}}(x + \sin x)$$

(
$$\beta$$
) $y = x^{\frac{1}{2}} \sin^2 x + (\sin x)^{\frac{1}{2}}$

$$(\mathbf{W}) \ \mathbf{y} = \mathbf{x}^4 \cos \mathbf{x} + \mathbf{x} \cos \mathbf{x}$$

(iii)
$$y = \frac{1}{2}x^2 \sin x - x \cos x + \sin x$$

(ii)
$$y = \sqrt{x}(\sqrt{x} + 1)(\sqrt{x} + 2)$$

(
$$t$$
) $y = (x-6)^{10} + \sin^{10} x$

$$(2) y = (\sin x \cos x)^3 + \sin(2x)$$

(N)
$$y = x^{\frac{1}{2}} \sin(2x) + (\sin x)^{\frac{1}{2}}$$

(An)
$$y = \frac{\sin x - \cos x}{\sin x + \cos x}$$

(fi) $y = \frac{1}{\tan x} - \frac{1}{\cot x}$

$$(\mathfrak{h}) \ y = \frac{1}{\tan x} - \frac{1}{\cot x}$$