នេះខែខែអស់អន់ខុ

និយនន័យ

និយទន័យ ១. ដេរីវេនៃអនុគមន៍ y=f(x) ត្រង់ x_0 កំណត់ដោយ

$$\frac{dy}{dx} = y' = f'(x_0) = \lim_{\Delta x \to 0} \frac{\Delta y}{\Delta x} = \lim_{x \to x_0} \frac{f(x) - f(x_0)}{x - x_0} = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

សំនាល់ ១. គេអាចសរសេរដេរីវេដោយ y' , f'(x) ឬ $\frac{dy}{dx}$ ។

- $\ \square$ អនុគមន៍ f មានដេរីវេត្រង់ x_0 នោះ f ជាប់ត្រង់ x_0 ។
- $\ \square$ អនុគមន៍ f ជាប់ត្រង់ x_0 នោះ f អាចមានដេរីវេត្រង់ x_0 ឬ គ្មានដេរីវេត្រង់ x_0 ។

នាពមានដើម្រែ

និយទន័យ ២. អនុគមន៍ f មានដេរីវេត្រង់ x_0 លុះត្រាតែ

- \square អនុគមន៍ f ជាប់ត្រង់ x=0 ។
- $\ \square$ ដេរីវេឆ្វេងស្មើដេរីវេស្តាំត្រង់ចំណុច x_0 គឺ $f'_-(x_0)=f'_+(x_0)$ ដែល

$$f_-'(x_0) = \lim_{h o 0^-} rac{f(x_0+h) - f(x_0)}{h}$$
 និង $f_+'(x_0) = \lim_{h o 0^+} rac{f(x_0+h) - f(x_0)}{h}$ ។

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និយមន័យ ៣. អនុគមន៍ f ជាប់លើចន្លោះបើក (a,b) កាលណា f មានដេរីវេលើគ្រប់ចំណុច $x_0 \in (a,b)$ ។

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និយទន័យ ៤. អនុគមន៍ f មានដេរីវេលើចន្លោះបិទ [a,b] កាលណា f មានដេរីវេលើចន្លោះ (a,b) ហើយ f មាន ដេរីវេខាងឆ្វេងត្រង់ x=a និងខាងស្តាំត្រង់ x=b ។

លដ្ឋសាះនៃខេត្តខេ

ចំពោះ u,v ជាអនុគមន៍នៃ x និង k ជាចំនួនថេ នោះគេបាន៖

9.
$$(ku)' = ku'$$

$$\mathbf{M}. \ (u-v)' = u' - v'$$

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$$\left(\frac{u}{v}\right)' = \frac{u'v - v'u}{v^2}$$

$$\mathbf{G}. \ (uv)' = u'v + v'v$$

ថ.
$$\left(\frac{u}{v}\right)' = \frac{u'v - v'u}{v^2}$$

$$\text{b. } \left(\frac{1}{v}\right)' = -\frac{v'}{v^2}$$

ស្ខេសខេស្សាង

9. តាង f(x)=k.u(x) ដែល u=u(x) និង k ជាចំនួនថេ តាមនិយមន័យ

$$f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{ku(x_0 + h) - k.u(x_0)}{h}$$

$$= k. \lim_{h \to 0} \frac{u(x_0 + h) - u(x_0)}{h}$$

$$= k.u'(x_0)$$

$$\therefore (k.u)' = k.u'$$

២. តាង f(x)=u(x)+v(x) ដែល u=u(x) និង v=v(x) តាមនិយមន័យ

$$f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{u(x_0 + h) + v(x_0 + h) - (u(x_0) + v(x_0))}{h}$$

$$= \lim_{h \to 0} \frac{u(x_0 + h) - u(x_0)}{h} + \lim_{h \to 0} \frac{v(x_0 + h) - v(x_0)}{h}$$

$$= u'(x_0) + v'(x_0)$$

 $\therefore (u+v)' = u' + v'$

៣. ស្រាយដូចទី២

៤. តាង f(x)=uv ដែល u=u(x) និង v=v(x) តាមនិយមន័យគេបាន

$$f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{u(x_0 + h) \cdot v(x_0 + h) - u(x_0) \cdot v(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{u(x_0 + h) \cdot v(x_0 + h) - u(x_0) \cdot v(x_0 + h) + u(x_0) \cdot v(x_0 + h) + u(x_0) \cdot v(x_0)}{h}$$

$$= \lim_{h \to 0} \left[\frac{u(x_0 + h) \cdot v(x_0 + h) - u(x_0) \cdot v(x_0 + h)}{h} + \frac{u(x_0) \cdot v(x_0 + h) + u(x_0) \cdot v(x_0)}{h} \right]$$

$$= \lim_{h \to 0} \left[v(x_0 + h) \cdot \frac{u(x_0 + h) - u(x_0)}{h} + u(x_0) \cdot \frac{v(x_0 + h) + v(x_0)}{h} \right]$$

$$= v(x_0) \cdot \frac{d}{dx}(u(x_0)) + u(x_0) \cdot \frac{d}{dx}(v(x_0))$$

$$\therefore (uv)' = u'v + v'u \tag{9}$$

៥. យក u=u(x) និង v=v(x) តាង $f(x)=\frac{u}{v}\Leftrightarrow f(x).v=u$ ធ្វើដេរីវេអង្គទាំងពីរធៀបនឹង x នោះគេបាន [f(x).v]'=u' ប្រើតាមសមីការ (១) គេបាន

$$f'(x).v + v'f(x) = u', \ f(x) = \frac{u}{v}$$

$$f'(x).v + v'.\frac{u}{v} = u'$$

$$\frac{f'(x).v^2}{v} + \frac{v'u}{v} = u'$$

$$f'(x).v^2 + v'u = u'v$$

$$f'(x) = \frac{u'v - v'u}{v^2}$$

$$\therefore \quad \left(\frac{u}{v}\right)' = \frac{u'v - v'u}{v^2}$$
(b)

៦. យក v=v(x) តាង $f(x)=rac{1}{v}$ ប្រើសមីការ (២) គេបាន

$$f'(x) = \frac{(1)' \cdot v - v' \cdot (1)}{v^2}$$
$$= \frac{0 - v'}{v^2}$$
$$= -\frac{v'}{v^2}$$
$$\therefore \left(\frac{1}{v}\right)' = -\frac{v'}{v^2}$$

៤ នើទែលៃអនុគមន៍បណ្ណាអ់

សរិសិតខេយាង

តាង $F(x)=f\circ g=f(g(x))$ តាមនិយមន័យភាពមានដេរីវេត្រង់ $x=x_0$ នោះគេបាន

$$F'(x_0) = \lim_{x \to x_0} \frac{F(x) - F(x_0)}{x - x_0}$$

$$= \lim_{x \to x_0} \frac{f(g(x)) - f(g(x_0))}{x - x_0}$$

$$= \lim_{x \to x_0} \left(\frac{f(g(x)) - f(g(x_0))}{g(x) - g(x_0)} \times \frac{g(x) - g(x_0)}{x - x_0}\right)$$

$$= f'(g(x_0)) \times g'(x_0) \quad , u = g(x_0), y = f(x_0)$$

$$\therefore \quad \frac{d}{dx}(f \circ g) = \frac{dy}{du} \times \frac{dy}{dx}$$

ខាន្នៅ ៤.១. បើ y=c ដែល c ជាចំនួនថេរ នោះ y'=0 ។

សុទិរិតិនេះ

គេមាន $y=f(x_0)=c$ នោះ $f(x_0+h)=c$ $,c\in\mathbb{R}$ តាមនិយមន័យគេបាន

$$f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{c - c}{h}$$

$$= \lim_{h \to 0} \frac{0}{h}$$

$$\therefore \frac{d}{dx}(c) = 0$$

ខ្វិតាហរណ៍ ១. គណនា y' ដែល $y = \left(\ln x. \log_a(\sqrt{3})\right)$ ។

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គេមាន
$$y = \left(\ln x. \log_a(\sqrt{3})\right) \Rightarrow y' = \left(\ln x. \log_a(\sqrt{3})\right)' = 0$$

ន្ធទាហរណ៍ ២. ស្រាយបញ្ជាក់ថា បើ $y=x^n$ នោះ $y'=nx^{n-1}$ ។

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គេមាន $f(x_0)=x_0^n$ នាំឲ្យ $f(x_0+h)=(x_0+h)^n$ តាមនិយមន័យ

$$\begin{split} y' &= f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h} \\ &= \lim_{h \to 0} \frac{(x_0 + h)^n - x_0^n}{h} \\ &= \lim_{h \to 0} \frac{(x_0 + h - x_0)(x_0^{n-1} + x^{n-2}.x_0 + \dots + x_0.x^{n-2}x_0 + x_0^{n-1})}{h} \\ &= \lim_{h \to 0} (x_0^{n-1} + x_0^{n-1} + \dots + x_0^{n-1} + x_0^{n+1}) \\ &= x_0^{n-1} (\underbrace{1 + 1 + \dots + 1 + 1}_{n \text{ finus } 1}) \\ &= n.x_0^{n-1} \\ \therefore \quad \frac{d}{dx}(x^n) = n.x^{n-1} \end{split}$$

ខ្នុទាបារណ៍ ៣. គណនា f'(x)

9.
$$f(x) = x^3$$

$$f(x) = \sqrt{x}$$

$$f(x) = \sqrt[3]{x^2}$$

ដំណោះស្រាយ

9.
$$f(x) = x^3 \Rightarrow f'(x) = (x^3)' = 3x^{3-1} = 3x^2$$

$$\textbf{U}. \ f(x) = \sqrt{x} \Rightarrow f'(x) = (\sqrt{x})' = (x^{\frac{1}{2}})' = \frac{1}{2}x^{\frac{1}{2}-1} = \frac{1}{2}x^{-\frac{1}{2}} = \frac{1}{2\sqrt{x}}$$

$$\mathbf{M}. \ f(x) = \sqrt[3]{x^2} \Rightarrow f'(x) = (\sqrt[3]{x^2})' = (x^{\frac{2}{3}})' = \frac{2}{3}x^{\frac{2}{3}-1} = \frac{2}{3}x^{-\frac{1}{3}} = \frac{2}{3\sqrt[3]{x}}$$

ខានុនៅ ៤.២. បើ $y=u^n$ ដែល u ជាអនុគមន៍នៃ x នោះ $y'=nu'u^{n-1}$ ។

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គេមាន
$$y=u^n$$
 គេបាន $y'=rac{dy}{dx}=rac{dy}{du} imesrac{du}{dx}=rac{d}{du}(u^n) imes u'=nu'u^{n-1}$

ខ្វិតាហរណ៍ ៤. គណនា y'

9.
$$y = (2x + \ln 2)^4$$

២.
$$y=\sqrt{u}$$
 ដែល u ជាអនុគមន៍នៃ x ។

ជុំឈោះស្រាតា

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9.
$$y = (2x + \ln 2)^4 \Rightarrow y' = 4(2x + \ln 2)'(2x + \ln 2)^{4-1} = 4(2+0)(2x + \ln 2)^3 = 8(2x + \ln 2)^3$$

២.
$$y=\sqrt{u}=u^{\frac{1}{x}}$$
 នាំឲ្យ $y'=(u^{\frac{1}{2}})'=\frac{1}{2}u'u^{\frac{1}{2}-1}=\frac{1}{2}u'u^{-\frac{1}{2}}=\frac{u'}{2\sqrt{u}}$ ។

🟅 នើទៃនៃអនុអមស៍គ្រីអោលទេវុគ

9. បើ
$$y = \sin x$$
 នោះ $y' = \cos x$

២. បើ
$$y = \cos x$$
 នោះ $y' = -\sin x$

៤. បើ
$$y = \cot x$$
 នោះ $y' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$

សសៃតេតយ៉ាង

9. គេមាន $y = f(x_0) = \sin x_0$ នោះ $f(x_0 + h) = \sin(x_0 + h)$ តាមនិយមន័យ

$$y' = f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{\sin(x_0 + h) - \sin x_0}{h}$$

$$= \lim_{h \to 0} \frac{\sin x_0 \cos h + \sin h \cdot \cos x_0 - \sin x_0}{h}$$

$$= \lim_{h \to 0} \left(\cos x_0 \cdot \frac{\sin h}{h} - \sin x_0 \cdot \frac{1 - \cos h}{h}\right)$$

$$= \cos x_0 \quad \lim_{h \to 0} \frac{\sin h}{h} = 1 \lim_{h \to 0} \frac{1 - \cos h}{h} = 0$$

$$\therefore \quad \frac{d}{dx}(\sin x) = \cos x$$

២. គេមាន $y = f(x_0) = \cos x_0$ នោះ $f(x_0 + h) = \cos(x_0 + h)$ តាមនិយមន័យ

$$y' = f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{\cos(x_0 + h) - \cos x_0}{h}$$

$$= \lim_{h \to 0} \frac{\cos x_0 \cdot \cos h - \sin x_0 \cdot \sin h - \cos x_0}{h}$$

$$= \lim_{h \to 0} \left(-\frac{\sin h}{h} \cdot \sin x_0 - \cos x_0 \cdot \frac{1 - \cos h}{h} \right)$$

$$= -\sin x_0 \quad , \lim_{h \to 0} \frac{1 - \cos h}{h} = 0, \lim_{h \to 0} \frac{\sin h}{h} = 1$$

$$\therefore \quad \frac{d}{dx}(\cos x) = -\sin x$$

៣. តាង
$$y = \tan x = \frac{\sin x}{\cos x}$$
 តាមសមីការ (២) គេបាន

$$y' = \left(\frac{\sin x}{\cos x}\right)' = \frac{(\sin x)' \cos x - (\cos x)' \cdot \sin x}{(\cos x)^2}$$

$$= \frac{\cos x \cdot \cos x - (-\sin x) \cdot \sin x}{\cos^2 x}$$

$$= \frac{\cos^2 x + \sin^2 x}{\cos^2 x}$$

$$= 1 + \tan^2 x$$

$$= \frac{1}{\cos^2 x}, \sin^2 x + \cos^2 x = 1$$

$$\therefore (\tan x)' = \frac{1}{\cos^2} = 1 + \tan^2 x$$

៤. តាង $y = \cot x = \frac{\cos x}{\sin x}$ តាមសមីការ (២) គេបាន

$$y' = \left(\frac{\cos x}{\sin x}\right)' = \frac{(\cos x)' \cdot \sin x - (\sin x)' \cdot \cos x}{(\sin^2 x)^2}$$

$$= \frac{-\sin x \cdot \sin x - \cos x \cdot \cos x}{\sin^2 x}$$

$$= \frac{-\sin^2 x - \cos^2 x}{\sin^2 x}$$

$$= -\frac{\sin^2 x + \cos^2 x}{\sin^2 x}, \sin^2 x + \cos^2 x = 1$$

$$\therefore (\cot x)' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$$

ខាន្តនៅ ៥.១. បើ u ជាអនុគមន៍នៃ x គេបាន

២. បើ
$$y = \cos u$$
 នោះ $y' = -u' \sin u$

9. ប្រើ
$$y=\sin u$$
 នោះ $y'=u'\cos u$

២. ប្រើ $y=\cos u$ នោះ $y'=-u'\sin u$

៣. ប្រើ $y=\tan u$ នោះ $y'=\frac{u'}{\cos^2 u}=u(1+\tan^2 u)$

៤. បើ
$$y = \cot u$$
 នោះ $y' = -\frac{u'}{\sin^2 u} = -u'(1 + \cot^2 u)$

សម្រាយមញ្ជាអ

១. បើ u ជាអនុគមន៍នៃ x នោះ $y=\sin u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\sin u) \times \frac{du}{dx} = \cos u \times u' = u'\cos u$$

$$\therefore \frac{d}{dx}(\sin u) = u'\cos u$$

២. បើ u ជាអនុគមន៍នៃ x នោះ $y=\cos u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\cos u) \times \frac{du}{dx} = -\sin u \times u' = -u'\sin u$$

$$\therefore \frac{d}{dx}(\cos u) = -u'\sin u$$

៣. បើ u ជាអនុគមន៍នៃ x នោះ $y = \tan u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\tan u) \times \frac{du}{dx} = \frac{1}{\cos^2 u} \times u' = (1 + \tan^2 u) \times u'$$

$$\therefore \quad (\tan u)' = \frac{u'}{\cos^2 u} = u'(1 + \tan^2 u)$$

៤. បើ u ជាអនុគមន៍នៃ x នោះ $y=\cot u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\cot u) \times \frac{du}{dx} = -\frac{1}{\sin^2 u} \times u' = -(1 + \cot^2 u) \times u'$$

$$\therefore \quad (\cot u)' = -\frac{u'}{\sin^2 u} = -u'(1 + \cot^2 u)$$

ន្ធទាហរណ៍ ៥. គណនាដេវីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$y = \sin(2x + 1)$$

$$M. \ y = \tan(2x+1)$$

$$y = \cos(2x + 1)$$

G.
$$y = \cot(2x + 1)$$
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ជំណោះស្រាយ

9.
$$y = \sin(2x+1) \Rightarrow y' = (2x+1)'\cos(2x+1) = 2\cos(2x+1)$$

$$\textbf{0.} \ \ y = \cos(2x+1) \Rightarrow y' = -(2x+1)'\sin(2x+1) = -2\sin(2x+1)$$

$$\mathbf{M}. \ \ y = \tan(2x+1) \Rightarrow y' = \frac{(2x+1)'}{\cos^2(2x+1)} = \frac{2}{\cos^2(2x+1)} = 2[1 + \tan^2(2x+1)]$$

$$\text{M. } y = \tan(2x+1) \Rightarrow y' = \frac{(2x+1)'}{\cos^2(2x+1)} = \frac{2}{\cos^2(2x+1)} = 2[1+\tan^2(2x+1)]$$

$$\text{G. } y = \cot(2x+1) \Rightarrow y' = -\frac{(2x+1)'}{\sin^2(2x+1)} = -\frac{2}{\sin^2(2x+1)} = -2[1+\cot^2(2x+1)]$$

សង្រេរទំណើ្តមានម្យុននេះ ខេត្ត

ស្រាយថាបើ $y=a^x$ នោះ $y'=a^x$. $\ln a$

សសៃតាតយ៉ាង

គេមាន $y=a^x$ តាមនិយមន័យ គេបាន

$$y' = f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{a^{x_0 + h} - a^{x_0}}{h}$$

$$= \lim_{h \to 0} \frac{a^{x_0}(a^h - 1)}{h}$$

$$= a^{x_0} \lim_{h \to 0} \frac{a^h - 1}{h}$$
 ដោយ $\lim_{x \to 0} \frac{a^x - 1}{x} = \ln a$

$$= a^{x_0} \cdot \ln a$$

$$\therefore (a^x)' = a^x \cdot \ln a$$

ខាន្ទនៅ ៦.១. បើ u ជាអនុគមន៍នៃ x នោះ $(a^u)'=u'a^u$. $\ln a$ ។

ស្ខេសខណ្ឌង

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(a^u) \times \frac{du}{dx} = a^u \cdot \ln a \times u'$$

$$\therefore \quad (a^u)' = u' \cdot a^u \cdot \ln a$$

ខ្វុនាហរណ៍ ៦. គណនា y' ចំពោះ u ជាអនុគមន៍នៃ x នៃអនុគមន៍ខាងក្រោម៖

9.
$$y = e^x$$

U.
$$y = a^{x^2 - 1}$$

$$\mathbf{m}. \ y = e^u$$

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9.
$$y=e^x$$
 is: $y'=(e^x)'=e^x$. $\ln e=e^x$, $\ln e=1$

២.
$$y = a^{x^2-1}$$
 នោះ $y' = (x^{x^2-1})'a^{x^2-1} \ln a = 2x.a^{x^2-1} \ln a$

M.
$$y = e^u$$
 is: $y' = (e^u)' = u'e^u$. $\ln e = u'e^u$, $\ln e = 1$

👌 ខេះីទេខែអនុគមន៍អោភាគៃ

ស្រាយបញ្ជាក់ថា បើ $y=\log_a x\;, a>0, a\neq 1$ នោះ $y'=rac{1}{x\ln a}$ ។

សសៃតឧសិរាង

គេមាន $y = \log_a x$ តាមនិយមន័យ គេបាន

$$y' = f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{\log_a(x_0 + h) - \log_a(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{1}{h} \log_a \left(\frac{x_0 + h}{x_0}\right)$$

$$= \lim_{h \to 0} \log_a \left(1 + \frac{h}{x_0}\right)^{\frac{1}{h}}$$

$$= \log_a \left(\lim_{h \to 0} \ln\left(1 + \frac{h}{x_0}\right)^{\frac{1}{h}}\right)^{\frac{1}{x_0}}$$

$$= \log_a e^{\frac{1}{x_0}} = \frac{1}{x_0} \frac{\ln e}{\ln a}$$

$$\therefore (\log_a x)' = \frac{1}{x \ln a}, a > 0, a \neq 1$$

ខាន្ននៅ ៧.១. បើ u ជាអនុគមន៍នៃ x នោះ $(\log_a u)' = \frac{u'}{u \ln a} \;, a>0, a \neq 1$ ។

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បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\begin{split} \frac{dy}{dx} &= \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du} (\log_a u) \times \frac{du}{dx} = \frac{1}{u \ln a} \times u' \\ & \therefore \quad (\log_a u)' = \frac{u'}{u \ln a} \;, a > 0, a \neq 1 \end{split}$$

៨ ដើមែសៃអនុគមន៍លេអាអែនេពែ

ស្រាយបញ្ជាក់ថា បើ $y=\ln x$ នោះ $y'=rac{1}{x}$ ។

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គេមាន $y=\ln x$ តាមនិយមន័យ គេបាន

$$y' = f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{\ln(x_0 + h) - \ln(x_0)}{h}$$

$$= \lim_{h \to 0} \frac{\ln\left(\frac{x_0 + h}{x_0}\right)}{h}$$

$$= \lim_{h \to 0} \frac{1}{h} \ln\left(1 + \frac{h}{x_0}\right)$$

$$= \lim_{h \to 0} \ln\left(1 + \frac{1}{x_0}\right)^{\frac{1}{h}}$$

$$= \ln\left[\lim_{h \to 0} \left(1 + \frac{1}{\frac{x_0}{h}}\right)^{\frac{x_0}{h} \times \frac{1}{x_0}}\right], \lim_{h \to 0} \left(1 + \frac{1}{\frac{x_0}{h}}\right)^{\frac{x_0}{h}} = e$$

$$= \ln e^{\frac{1}{x_0}}, \ln e = 1$$

$$\therefore (\ln x)' = \frac{1}{x}$$

ខ្វុតាហរណ៍ ៧. រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x^2 \cdot \log_a x, a > 0, a \neq 1$$

G.
$$f(x) = \log(x^2 \sqrt{x^3 - 1})$$

$$0. \ f(x) = \sin(2x) + \log_2(x^2 + 1)$$

៥.
$$f(x) = (\sin x)^{\log x}$$

$$\text{m. } f(x) = \frac{e^{2x} + \log_3 x}{x^2}$$

$$\mathfrak{d}. \ f(x) = (\log_a x)^{\ln(2x)}, a > 0, a \neq 1$$

សង្ខាយមញ្ជាត់

9.
$$f(x) = x^2 \cdot \log_a x, a > 0, a \neq 1 \Longrightarrow f'(x) = (x^2)' \log_a x + (\log_a x)' x^2$$

$$= 2x \log_a x + \frac{1}{x \ln a} x^2$$

$$\therefore f'(x) = 2x \log_a x + \frac{x}{\ln a}, a > 0, a \neq 1$$

$$\text{U.} \quad f(x) = \sin(2x) + \log_2(x^2 + 1) \Longrightarrow f'(x) = -(2x)' \cos(2x) + \frac{(x^2 + 1)'}{(x^2 + 1) \ln 2}$$

$$\therefore \quad f'(x) = -2\cos(2x) + \frac{2x}{(x^2 + 1) \ln 2}$$

$$\begin{split} \text{M. } f(x) &= \frac{e^{2x} + \log_3 x}{x^2} \Longrightarrow f'(x) = \frac{(e^{2x} + \log_3 x)'x^2 - (x^2)'(e^{2x} + \log_3 x)}{x^4} \\ &= \frac{(2e^{2x} + \frac{1}{x \ln 3})x^2 - 2x(e^{2x} + \log_3 x)}{x^4} \\ &= \frac{2xe^{2x} + \frac{1}{\ln 3} - 2e^{2x} - 2\log_3 x}{x^3} \\ & \therefore \quad f'(x) = \frac{2e^{2x}(x - 1) + \frac{1}{\ln 3} - \log_3 x^2}{x^3} \end{split}$$

$$\begin{aligned} \text{G.} \quad f(x) &= \log(x^2 \sqrt{x^3 - 1}) = \log x^2 + \log(x^3 - 1)^{\frac{1}{2}} = 2\log x + \frac{1}{2}\log(x^3 - 1) \\ & \therefore \quad f'(x) = \frac{2}{x\ln 10} + \frac{(x^3 - 1)'}{2(x^3 - 1)\ln 10} = \frac{2}{x\ln 10} + \frac{3x^2}{2(x^3 - 1)\ln 10} \\ \text{G.} \quad f(x) &= (\sin x)^{\log x} \Longleftrightarrow \ln f(x) = \ln(\sin x)^{\log x} \end{aligned}$$

$$(\ln f(x))' = (\log x. \ln(\sin x))'$$

$$\frac{f'(x)}{f(x)} = (\log x)' \ln(\sin x) + (\ln(\sin x))' \log x$$

$$f'(x) = f(x) \left(\frac{1}{x \ln 10} \ln(\sin x) + \frac{(\sin x)'}{\sin x} \cdot \log x\right)$$

$$\therefore f'(x) = (\sin x)^{\log x} \left(\frac{\ln(\sin x)}{x \ln 10} + \cot x \cdot \log x\right)$$

$$\theta. \ f(x) = (\log_a x)^{\ln(2x)}, a > 0, a \neq 1 \iff \ln f(x) = \ln(\log_a x)^{\ln(2x)}$$

$$\begin{split} &(\ln f(x))' = (\ln(2x). \ln(\log_a x))' \\ &\frac{f'(x)}{f(x)} = (\ln(2x))' \ln(\log_a x) + (\ln(\log_a x))' \ln(2x) \\ &f'(x) = f(x) \left(\frac{(2x)'}{2x} \ln(\log_a x) + \frac{(\log_a x)'}{\log_a x} \ln(2x) \right) \\ &\therefore \quad f'(x) = (\log_a x)^{\ln(2x)} \left(\frac{\ln(\log_a x)}{x} + \frac{\ln(2x)}{x \ln a \log_a x} \right), a > 0, a \neq 1 \end{split}$$

ខានុនៅ ៤.១. បើ
$$u$$
 ជាអនុគមន៍នៃ x នោះ $(\ln u)' = \frac{u'}{u}$ ។

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បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\ln u) \times \frac{du}{dx} = \frac{1}{u} \times u'$$

$$\therefore \quad (\ln u)' = \frac{u'}{u}$$

ខ្វុទាហរណ៍ \mathbf{d} . រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x \cdot \ln x$$

G.
$$f(x) = \ln(x^2 \sqrt{x^3 - 1})$$

$$f(x) = x^2 + \ln(x^2 + 1)$$

៥.
$$f(x) = x^x$$

$$\mathbf{m.} \ f(x) = \frac{e^x + \ln x}{x^2}$$

$$b. \ f(x) = (\sin x)^{\cos x}$$

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9.
$$f(x) = x \cdot \ln x \implies f'(x) = x' \ln x + (\ln x)' x = \ln x + \frac{1}{x} \cdot x = \ln x + 1$$

$$f(x) = x^2 + \ln(x^2 + 1) \Longrightarrow f'(x) = (x^2)' + \frac{(x^2 + 1)'}{x^2 + 1} = 2x + \frac{2x}{x^2 + 1}$$

$$f(x) = \frac{e^x + \ln x}{x^2} \Longrightarrow f'(x) = \frac{(e^x + \ln x)'x^2 - (x^2)'(e^x + \ln x)}{(x^2)^2}$$

$$\mathbf{m}. \ f(x) = \frac{e^x + \ln x}{x^2} \Longrightarrow f'(x) = \frac{(e^x + \ln x)'x^2 - (x^2)'(e^x + \ln x)}{(x^2)^2}$$

$$= \frac{\left(e^x + \frac{1}{x}\right)x^2 - 2x(e^x + \ln x)}{x^4}$$

$$\therefore f'(x) = \frac{xe^x + 1 - 2e^x - 2\ln x}{x^3}$$

d.
$$f(x) = \ln(x^2 \sqrt{x^3 - 1}) = \ln x^2 + \ln \sqrt{x^3 - 1} = 2 \ln x + \ln(x^3 - 1)^{\frac{1}{2}}$$

$$f'(x) = 2(\ln x)' + \frac{1}{2}[\ln(x^3 - 1)]'$$
$$= 2 \cdot \frac{1}{x} + \frac{1}{2} \cdot \frac{(x^3 - 1)'}{x^3 - 1}$$
$$\therefore f'(x) = \frac{2}{x} + \frac{3}{2} \cdot \frac{x^2}{x^3 - 1}$$

$$\mathsf{d}. \ f(x) = x^x \Longleftrightarrow \ln f(x) = \ln x^x = x \ln x$$

$$(\ln f(x))' = (x \ln x)'$$

$$\frac{f'(x)}{f(x)} = x' \ln x + (\ln x)'x$$

$$f'(x) = f(x)(\ln x + \frac{1}{x}.x)$$

$$\therefore f'(x) = x^x(\ln x + 1)$$

$$\mathfrak{d}. \ f(x) = (\sin x)^{\cos x} \Longleftrightarrow \ln f(x) = \ln(\sin x)^{\cos x}$$

$$(\ln f(x))' = (\cos x \ln \sin x)'$$

$$\frac{f'(x)}{f(x)} = (\cos x)' \ln \sin x + (\ln \sin x)' \cos x$$

$$f'(x) = f(x) \left(-\sin x \ln \sin x + \frac{(\sin x)'}{\sin x} \cdot \cos x \right)$$

$$\therefore f'(x) = (\sin x)^{\cos x} (\cos x \cot x - \sin x \ln \sin x)$$

៩ ខេរីទេខែអនុគមន៍ Arc Sine និទ Arc Tangent

$$\begin{split} y &= \arcsin x \Longleftrightarrow x = \sin y \; \$ \ \ \, 1 - \frac{\pi}{2} \leqslant y \leqslant \frac{\pi}{2}, \\ y &= \arctan x \Longleftrightarrow x = \tan y \; \$ \ \ \, 1 - \frac{\pi}{2} \leqslant y \leqslant \frac{\pi}{2}, \end{split}$$

បើ
$$y = \arcsin x$$
 នោះ $y' = \frac{1}{\sqrt{1-x^2}}$ ។

សរិសិតខេយ់ង

បើ $y= \arcsin x$ នោះ $x=\sin y$ ធ្វើដេរីវេអង្គសងខាងធៀបនឹង x គេបាន

$$(x)' = (\sin y)' \iff 1 = y' \cos y$$

$$y' = \frac{1}{\cos y}, \sin^2 y + \cos^2 y = 1 \implies \cos y = \pm \sqrt{1 - \sin^2 x}$$

$$\lim -\frac{\pi}{2} \leqslant y\frac{\pi}{2} \Longrightarrow \cos y \geqslant 0 \Longrightarrow \cos y = \sqrt{1-x^2}$$

$$\therefore \quad (\arcsin x)' = \frac{1}{\sqrt{1 - x^2}}$$

បើ $y=\arctan x$ នោះ $y'=rac{1}{1+x^2}$ ។

សសៃតេតយ៉ាង

បើ $y=\arctan x$ នោះ $x=\tan y$ ធ្វើដេរីវេអង្គសងខាងធៀបនឹង x គេបាន

$$(x)' = (\sin y)' \Longleftrightarrow 1 = y'(1 + \tan^2 y)$$

$$y' = \frac{1}{1 + \tan^2 y}$$

$$\therefore \quad (\arctan x)' = \frac{1}{1 + x^2}$$

ខានុនៅ ៩.១. បើ u ជាអនុគមន៍នៃ x នោះ $(\arcsin u)' = \frac{u'}{\sqrt{1-x^2}}$

សម្រាយបញ្ជាអ

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\arcsin u) \times \frac{du}{dx} = \frac{1}{\sqrt{1 - u^2}} \times u'$$

$$\therefore \quad (\arcsin u)' = \frac{u'}{\sqrt{1 - u^2}}$$

ខាន្នៅ ៩.២. បើ u ជាអនុគមន៍នៃ x នោះ $(\arctan u)' = \frac{u'}{1+u^2}$

អគិរាតាតយ៉ាង

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\begin{split} \frac{dy}{dx} &= \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\arctan u) \times \frac{du}{dx} = \frac{1}{1 - u^2} \times u' \\ &\therefore \quad (\arctan u)' = \frac{u'}{1 + u^2} \end{split}$$

សំសាន់ ១. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \arcsin x \cdot \sin x$$

$$f(x) = \sin(\arcsin x)$$

$$\mathbf{U}. \ f(x) = \arctan x \cos x$$

G.
$$f(x) = \arctan(\tan x)$$

ស្រាតាតយាង

9.
$$f(x) = \arcsin x \cdot \sin x \Longrightarrow f'(x) = (\arcsin x)' \sin x + (\sin x)' \arcsin x$$

$$f'(x) = \frac{\sin x}{\sqrt{1 - x^2}} + \cos x. \arcsin x$$

$$\mathfrak{b}. \ f(x) = \arctan x \cos x \Longrightarrow f'(x) = (\arctan x)' \cos x + (\cos x)' \arctan x$$

$$\therefore f'(x) = \frac{\cos x}{1+x^2} - \sin x. \arctan x$$

$$\mathsf{M.} \ \ f(x) = \sin(\arcsin x) \Longrightarrow f'(x) = (\arcsin x)' \cos(\arcsin x)$$

$$\therefore f'(x) = \frac{\cos(\arcsin x)}{\sqrt{1 - x^2}}$$

$$\text{G. } f(x)=\arctan(\tan x)\Longrightarrow f'(x)=\frac{(\tan x)'}{1+(\tan x)^2}=\frac{1+\tan^2 x}{1+\tan^2 x}$$

$$\therefore f'(x) = 1$$

លអ្នសាះនៃខេរិទេ

បើ f,g,y,u,v ជាអនុគមន៍នៃ x និង k ជាចំនួនថេនោះគេបាន៖

9.
$$(u \pm v)' = u' \pm v'$$

$$\mathbf{M.} \ (uv)' = u'v + v'u$$

$$\mathbf{d.} \ \frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$$

២.
$$(ku)' = ku'$$

$$\mathfrak{d}. \left(\frac{1}{v}\right)' = -\frac{v'}{v^2}$$

រួមមន្ត្តនៃនេះទេ

បើ C,a,b,c ជាចំនួនថេ និង u ជាអនុគមន៍នៃ x ដែល $n\in\mathbb{N}$ គេបាន៖

9.
$$(C)' = 0$$

២.
$$(x)' = 1$$

$$\mathbf{m}. \ (ax+b)'=a$$

G.
$$(ax^2 + bx + c)' = 2ax + b$$

៥.
$$(x^n)' = nx^{n-1}$$

៦.
$$(u^n)' = n.u'.u^{n-1}$$

$$\mathbf{N}. \ (x)^{-n} = -\frac{n}{x^{n+1}}$$

$$\mathbf{G.} \ \left(\frac{1}{x}\right)' = -\frac{1}{x^2}$$

$$\mathcal{E}. \left(\frac{1}{u}\right)' = -\frac{u}{u^2}$$

90.
$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

99.
$$(\sqrt{u})' = \frac{u'}{2\sqrt{u}}$$

9 ປີ.
$$(\sqrt[n]{x})' = \frac{1}{n\sqrt[n]{x^{n-1}}}$$
 ງ ເພື່ອ. $(\ln x)' = \frac{1}{x}$ ງ ເພື່ອ. $(\ln u)' = \frac{u'}{u}$

$$\mathfrak{Im}. \ (\ln x)' = \frac{1}{x}$$

១៤.
$$(\ln u)' = \frac{u'}{u}$$

១៥.
$$(\log_a x)' = \frac{1}{x \ln a}, a > 0, a \neq 1$$

95.
$$(\log_a u)' = \frac{u'}{u \cdot \ln a}, a > 0, a \neq 1$$

$$\mathfrak{In}. \ (a^x)' = a^x \ln a, a > 0, a \neq 1$$

$$\mathfrak{IG.} \ (a^u)' = u'a^u \ln a, a > 0, a \neq 1$$

98.
$$(e^x)' = e^x$$

២០.
$$(e^u)' = u'e^u$$

២១.
$$(\sin x)' = \cos x$$

២២.
$$(\sin u)' = u' \cos u$$

$$\mathbf{UM.} (\cos x)' = -\sin x$$

២៤.
$$(\cos u)' = -u' \sin u$$

២៥.
$$(\tan x)' = \frac{1}{\cos^2 x} = 1 + \tan^2 x$$

២៦.
$$(\tan u)' = \frac{u'}{\cos^2 u} = u'(1 + \tan^2 u)$$
២៧. $(\cot x)' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$

$$\mathbf{vn.} \ (\cot x)' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$$

$$\text{OG. } (\cot u)' = -\frac{u'}{\sin^2 u} = -(1 + \cot^2 u)$$

$$\text{UE. } (\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$

$$\mathbf{M0.} \ (\arcsin u)' = \frac{u'}{\sqrt{1 - u^2}}$$

M9.
$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$$

MU.
$$(\arccos u)' = -\frac{u'}{\sqrt{1-u^2}}$$
 MM. $(\arctan x)' = \frac{1}{1+x^2}$

MM.
$$(\arctan x)' = \frac{1}{1 + x^2}$$

MG.
$$(\arctan u)' = \frac{u'}{1 + u^2}$$

៣៥.
$$(\operatorname{arccot} x)' = -\frac{1}{1+x^2}$$

Mb.
$$(\operatorname{arccot} u)' = -\frac{u'}{1+u^2}$$

$$\mathbf{MN}. \ (u^v)' = \left(v'.\ln u + \frac{v.u'}{u}\right).u^v$$

លំខាង និខ ជំណោះស្រាយ 90

សំសាន់ ២. គណនា f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1$$

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1$$

10. $f(x) = 2x^2 - \sqrt{x} + \frac{2}{x}$
11. $f(x) = (x^4 - 7x^2 + \sin a)^7$
12. $f(x) = (x^4 - 7x^2 + \sin a)^7$
13. $f(x) = (x^4 - 6x^2 + \sin a)^7$
14. $f(x) = (x^4 - 6x^2 + \sin a)^7$
15. $f(x) = (x^4 - 6x^2 + \sin a)^7$
16. $f(x) = (x^4 - 6x^2 + \sin a)^7$
17. $f(x) = (x^4 - 6x^2 + \sin a)^7$
18. $f(x) = (x^4 - 6x^2 + \sin a)^7$
19. $f(x) = (x^4 - 6x^2 + \sin a)^7$
20. $f(x) = (x^4 - 6x^2 + \sin a)^7$
21. $f(x) = (x^4 - 6x^2 + \sin a)^7$
22. $f(x) = (x^4 - 6x^2 + \sin a)^7$
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29. $f(x) = (x^4 - 6x^2 + \sin a)^2$
29. $f(x) = (x^4 - 6$

$$\mathbf{n}. \ f(x) = (x+1)(2x-1)^2$$

$$\mathbf{m}. \ f(x) = (x^4 - 7x^2 + \sin a)^7$$

G.
$$f(x) = (x^2 + 2x + 3)(x^3 - 3x - 1)$$

G.
$$f(x) = (x^2 - \sqrt{x})^{2019}$$

$$\mathcal{E}. \ f(x) = \frac{1}{x-1}$$

$$f(x) = \sqrt{x^3 - x^2 + 3}$$

90.
$$f(x) = \frac{x\sqrt{x}}{x+1}$$

ស្សសាលមណ្ឌង

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1 \Longrightarrow f'(x) = 5x^4 - 4x^3 + 3x^2 - 2x + 1$$

$$\textbf{U}. \ f(x) = 2x^2 - \sqrt{x} - \frac{2}{x} \Longrightarrow f'(x) = 4x^2 + \frac{1}{2\sqrt{x}} - \frac{2}{x^2}$$

$$f'(x) = 7(x^4 - 7x^2 + \sin a)'(x^4 - 7x^2 + \sin a)^{7-1} = 7(4x^3 - 14x)(x^4 - 7x^2 + \sin a)^6$$

$$\mathbf{m.} \ f(x) = (x^4 - 7x^2 + \sin a)^7$$

G.
$$f(x) = (x^2 - \sqrt{x})^{2019} \Longrightarrow f'(x) = 2019(x^2 - \sqrt{x})'(x^2 - \sqrt{x})^{2019-1}$$

$$=2019\left(2x-\frac{1}{2\sqrt{x}}\right)(x^2-\sqrt{x})^{2018}$$

ය.
$$f(x) = \sqrt{x^3 - x^2 + 3} \Longrightarrow f'(x) = \frac{(x^3 - x^2 + 3)'}{2\sqrt{x^3 - x^2 + 3}} = \frac{3x - 2}{2\sqrt{x^3 - x^2 + 3}}$$

$$b. \ \sqrt[4]{x^3 - 2x} \Longleftrightarrow f(x) = (x^3 - 2x)^{\frac{1}{4}}$$

$$f'(x) = \frac{1}{4}(x^3 - 2x)'(x^3 - 2x)^{\frac{1}{4} - 1}$$
$$= \frac{1}{4}(3x^2 - 2)(x^3 - 2x)^{-\frac{3}{4}}$$

$$\therefore f'(x) = \frac{3x^2 - 2}{4\sqrt[4]{(x^3 - 2x)^3}}$$

11.
$$f(x) = (x+1)(2x-1)^2$$

$$f'(x) = (x+1)'(2x-1)^2 + [(2x-1)^2]'(x+1)$$

$$= (2x-1)^2 + 2(2x-1)'(2x-1)(x+1)$$

$$= (2x-1)(2x-1+4x+4)$$

$$\therefore f'(x) = (2x-1)(6x+3)$$

G.
$$f(x) = (x^2 + 2x + 3)(x^3 - 3x - 1)$$

$$f'(x) = (x^2 + 2x + 3)'(x^2 - 3x - 1) + (x^2 - 3x - 1)'(x^2 + 2x + 3)$$

$$= (2x + 2)(x^2 - 3x - 1) + (2x - 3)(x^2 + 2x + 3)$$

$$= 2x^3 - 6x^2 - 2x + 2x^2 - 6x - 2 + 2x^3 + 4x^2 + 6x - 3x^2 - 6x - 9$$

$$\therefore f'(x) = 4x^3 - 3x^2 - 8x - 11$$

8.
$$f(x) = \frac{1}{x-1} \Longrightarrow f'(x) = -\frac{(x-1)'}{(x-1)^2} = -\frac{1}{(x-1)^2}$$
90. $f(x) = \frac{x\sqrt{x}}{x+1}$

$$f'(x) = \frac{(x\sqrt{x})'(x+1) - (x+1)'x\sqrt{x}}{(x+1)^2}$$

$$= \frac{[x'\sqrt{x} + (\sqrt{x})'x](x+1) - x\sqrt{x}}{(x+1)^2}$$

$$= \frac{\left(x + \frac{x}{2\sqrt{x}}\right)(x+1) - x\sqrt{x}}{(x+1)^2}$$

$$= \frac{x\sqrt{x} + \sqrt{x} + \frac{x}{2\sqrt{x}}(x+1) - x\sqrt{x}}{(x+1)^2}$$

$$\therefore f'(x) = \frac{x^2 + 3x}{2\sqrt{x}(x+1)^2}$$

សំសាន់ ៣. គណនាដើរីវេនៃអនុគមន៍ខាងក្រោម៖

$$9. \ f(x) = x.\sin x + \cos x$$

$$G. f(x) = \sin^2 \sqrt{x} + \cos^2(3x)$$

9.
$$f(x) = x \cdot \sin x + \cos x$$
10.
$$f(x) = \sin^3 x - x \cdot \cos x$$

៥.
$$f(x) = \cos(3x+4) + 3\cos x \cdot \sin x$$

M.
$$f(x) = \cos(x^2 + 1) + 2\sin(x^2 - 1)$$
 b. $f(x) = \sin(\sin(\sqrt{x})) + \cos^3(x)$

$$f(x) = \sin(\sin\sqrt{x}) + \cos^3 x$$

ជំណោះស្រាយ

9.
$$f(x) = x \cdot \sin x + \cos x$$

$$f'(x) = x' \sin x + (\sin x)' \cdot x - \sin x$$
$$= \sin x + x \cdot \cos x - \sin x$$

$$f'(x) = x \cdot \cos x$$

$$\mathbf{U}. \ f(x) = \sin^3 x - x.\cos x$$

$$f'(x) = 3(\sin x)' \sin^{3-1} x - [x' \cdot \cos x + (\cos x)' \cdot x]$$
$$= 3\cos x \cdot \sin^2 x - (\cos x - x \cdot \sin x)$$

$$\therefore f'(x) = 3\cos x \cdot \sin^2 x - \cos x + x\sin x$$

$$\mathbf{m.} \ f(x) = \cos(x^2 + 1) + 2\sin(x^2 - 1)$$

$$f'(x) = -(x^2 + 1)'\sin(x^2 + 1) + 2(x^2 - 1)'\cos(x^2 - 1)$$

$$f'(x) = -2x\sin(x^2 + 1) + 4x\cos(x^2 - 1)$$

d.
$$f(x) = \sin^2 \sqrt{x} + \cos^2(3x)$$

$$f'(x) = 2(\sin \sqrt{x})' \cos^{2-1} \sqrt{x} + 2(\cos(3x))' \sin(3x)$$

$$= 2(\sqrt{x})' \cdot \cos \sqrt{x} \cdot \cos \sqrt{x} - 2(3x)' \sin(3x) \cdot \sin(3x)$$

$$\therefore f'(x) = \frac{1}{\sqrt{x}} \cdot \cos^2 \sqrt{x} - 6\sin^2(3x)$$

 $f(x) = \cos(3x+4) + 3\cos x \cdot \sin x$

$$f'(x) = -(3x+4)' \cdot \sin(3x+4) + 3[(\cos x)' \cdot \sin x + (\sin x)' \cdot \cos x]$$
$$= -3\sin(3x+4) + 3[-\sin x \cdot \sin x + \cos x \cdot \cos x]$$
$$\therefore f'(x) = -3[\sin(3x+4) + \sin^2 x - \cos^2 x]$$

 $b. \ f(x) = \sin(\sin\sqrt{x}) + \cos^3 x$

$$f'(x) = (\sin \sqrt{x})' \cdot \cos(\sin \sqrt{x}) + 3(\cos x) \cos^{3-1} x$$
$$= (\sqrt{x})' \cdot \cos \sqrt{x} \cdot \cos(\sin \sqrt{x}) - 3\sin x \cos^2 x$$
$$\therefore \quad f'(x) = \frac{1}{2\sqrt{x}} \cos \sqrt{x} \cdot \cos(\sin \sqrt{x}) - 3\sin x \cdot \cos^2 x$$

សំសាត់ ៤. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = (1 + \tan x)^4$$

$$\text{ f.} \quad f(x) = x \cdot \tan(x^2 - 1) + x \cot(2x^2 - 3)$$

$$\text{ f.} \quad f(x) = \frac{\tan(2x)}{1 - \cos x}$$

9.
$$f(x) = (1 + \tan x)^4$$

9. $f(x) = x^2 \tan x + (1 + \cot x)^2$

$$\mathbf{G.} \ f(x) = \frac{\tan(2x)}{1 - \cos x}$$

ជំណោះស្រួយ

9.
$$f(x) = (1 + \tan x)^4$$

$$f'(x) = 4(1+\tan x)'(1+\tan^2 x)^{4-1}$$

$$f'(x) = 4(1 + \tan^2 x)(1 + \tan x)^3$$

$$f(x) = x^2 \tan x + (1 + \cot x)^2$$

$$f'(x) = (x^2)' \tan x + (\tan x)' x^2 + 2(1 + \cot x)' (1 + \cot x)^{2-1}$$

$$f'(x) = 2x \tan x + x^2(1 + \tan^2 x) - 2(1 + \cot^2 x)(1 + \cot x)$$

$$f(x) = x \cdot \tan(x^2 - 1) + x \cot(2x^2 - 3)$$

$$f'(x) = x' \tan(x^2 - 1) + [\tan(x^2 - 1)]'x + x' \cot(2x^2 - 3) + [\cot(2x^2 - 3)]'x$$

$$= \tan(x^2 - 1) + (x^2 - 1)'[1 + \tan^2(x^2 - 1)]x - (2x^2 - 3)'[1 + \cot^2(2x^2 - 3)]x$$

$$f'(x) = \tan(x^2 - 1) + 2x^2[1 + \tan^2(x^2 - 1)] - 4x^2[1 + \cot^2(2x^2 - 3)]$$

សំទាាត់ ៥. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \frac{1 - x - 2x^2}{x^3 - \ln 3}$$

1. $f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x - x^2}}$

$$f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x - x^2}}$$

$$\mathbf{m.} \ f(x) = \sin x^2 \cdot \tan(2x+3)$$

G.
$$f(x) = \sin(x^2 + 5) + \cos(\sin x)$$

ජ.
$$f(x) = \frac{\sin(\tan\sqrt{x})}{\sin(\sqrt{x})}$$

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9.
$$f(x) = \frac{1 - x - 2x^2}{x^3 - \ln 3}$$

$$f'(x) = \frac{(1 - x - 2x^2)'(x^3 - \ln 3) - (x^3 - \ln 3)'(1 - x - 2x^2)}{(x^3 - \ln 3)^2}$$

$$= \frac{(-1 - 4x)(x^3 - \ln 3) - 3x^2(1 - x - 2x^2)}{(x^3 - \ln 3)^2}$$

$$= \frac{-x^3 + \ln 3 - 4x^4 + 4x \ln 3 - 3x^2 + 3x^3 + 6x^4}{(x^3 - \ln 3)^2}$$

$$\therefore f'(x) = \frac{2x^4 + 2x^3 - 3x^2 + 4x \cdot \ln 3 + \ln 3}{(x^3 - \ln 3)^2}$$

២.
$$f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x - x^2}} \Longleftrightarrow f(x).\sqrt{1 + 2x - x^2} = 2x^2 + 3x + 4$$
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$$[f(x)\sqrt{1+2x-x^2}]' = (2x^2+3x+4)'$$

$$f'(x)\sqrt{1+2x-x^2} + (\sqrt{1+2x-x^2})'f(x) = 4x+3$$

$$f'(x)\sqrt{1+2x-x^2} + \frac{(1+2x-x^2)'}{2\sqrt{1+2x-x^2}}f(x) = 4x+3$$

$$f'(x)\sqrt{1+2x-x^2} = 4x+3 - \frac{1-x}{\sqrt{1+2x-x^2}}.f(x)$$

$$\therefore f'(x) = \frac{4x+3}{\sqrt{1+2x-x^2}} + \frac{(x-1)(2x^2+3x+4)}{(1+2x-x^2)\sqrt{1+2x-x^2}}$$

$$f(x) = \sin x^2 \cdot \tan(2x + 3)$$

$$f'(x) = (\sin x^2)' \tan(2x+3) + (\tan(2x+3))' \sin x^2$$

$$= (x^2)' \cdot \sin x^2 \cdot \tan(2x+3) + (2x+3)'[1 + \tan^2(2x+3)] \sin x^2$$

$$= 2x \sin x^2 \cdot \tan(2x+3) + 2 \sin x^2[1 + \tan^2(2x+3)]$$

$$\therefore f'(x) = 2 \sin x^2[\tan^2(2x+3) + x \tan(2x+3) + 1]$$

$$f(x) = \sin(x^2 + 5) + \cos(\sin x)$$

$$f'(x) = (x^2 + 5)' \cos(x^2 + 5) - (\sin x)' \sin(\sin x)$$

$$\therefore f'(x) = 2x \cos(x^2 + 5) - \cos x \sin(\sin x)$$

ය.
$$f(x) = \frac{\sin(\tan\sqrt{x})}{\sin(\sqrt{x})} \Longleftrightarrow f(x).\sin\sqrt{x} = \sin(\tan\sqrt{x})$$

$$(f(x).\sin\sqrt{x})' = (\sin(\tan\sqrt{x}))'$$

$$f'(x)$$
. $\sin \sqrt{x} + (\sin \sqrt{x})' f(x) = (\tan \sqrt{x})' \cos(\tan \sqrt{x})$

$$f'(x)$$
. $\sin \sqrt{x} + (\sqrt{x})' \cos \sqrt{x}$. $f(x) = (\sqrt{x})'(1 + \tan^2 \sqrt{x}) \cos(\tan \sqrt{x})$

$$f'(x)\sin\sqrt{x} + \frac{1}{2\sqrt{x}}\cos\sqrt{x}.f(x) = \frac{1}{2\sqrt{x}}(1+\tan^2\sqrt{x})\cos(\tan\sqrt{x})$$

$$f'(x)\sin\sqrt{x} = \frac{1}{2\sqrt{x}}\left[(1+\tan^2\sqrt{x})\cos(\tan\sqrt{x}) - \cos\sqrt{x}f(x)\right]$$

$$f'(x) = \frac{1}{2\sqrt{x} \cdot \sin \sqrt{x}} \left[(1 + \tan^2 \sqrt{x}) \cos(\tan \sqrt{x}) - \cos \sqrt{x} f(x) \right]$$

$$f(x) = \frac{\sin(\tan \sqrt{x})}{\sin(\sqrt{x})}$$

សំទាាត់ ៦. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = xe^x + \frac{1}{2}x^2$$

 9.
$$f(x) = e^{x^2 + 2x + 1} + (x^2 - 3)e^x$$

 9.
$$f(x) = \frac{\sqrt{x}}{e^x}$$

G.
$$f(x) = x^3 e^{-3x}$$

$$\int_{0}^{\infty} f(x) = e^{x^2 + 2x + 1} + (x^2 - 3)e^x$$

ය.
$$f(x) = e^{2x} 3^{x^2+1}$$

$$\mathbf{m.} \ f(x) = \frac{\sqrt{x}}{e^x}$$

$$b. \ f(x) = e^{\sin x \cos x}$$

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9.
$$f(x) = xe^x + \frac{1}{2}x^2$$

$$f'(x) = x'e^x + (e^x)'x + \frac{1}{2} \cdot 2x = e^x + e^x + x = e^x(1+x) + x$$

$$\mathbf{0.} \ f(x) = e^{x^2 + 2x + 1} + (x^2 - 3)e^x$$

$$f'(x) = (x^2 + 2x + 1)'e^{x^2 + 2x + 1} + (x^2 - 3)'e^x + (e^x)'(x^2 - 3)$$
$$= (2x + 2)e^{x^2 + 2x + 1} + 2xe^x + e^x(x^2 - 3)$$

$$f'(x) = 2(x+1)e^{x^2+2x+1} + e^x(2x+x^2-3)$$

$$\mathbf{m.} \ f(x) = \frac{\sqrt{x}}{e^x}$$

$$f'(x) = \frac{(\sqrt{x})'e^x + (e^x)'\sqrt{x}}{(e^x)^2} = \frac{\frac{1}{2\sqrt{x}}e^x + e^x\sqrt{x}}{e^{2x}} = \frac{1+2x}{2\sqrt{x}e^x}$$

G.
$$f(x) = x^3 e^{-3x}$$

$$f'(x) = (x^3)'e^{-3x} + (e^{-3x})'x^3$$
$$= 3x^2e^{-3x} + (-3x)'e^{-3x}x^3$$
$$= 3x^2e^{-3x} - 3e^3e^{-3x}$$
$$\therefore f'(x) = 3x^2e^{-3x}(1-x)$$

៥.
$$f(x) = e^{2x}3^{x^2+1}$$

$$f'(x) = (e^{2x})'3^{x^2+1} + (3^{x^2+1})'.e^{2x}$$

$$= (2x)'e^{2x}.3^{x^2+1} + (x^2+1)'3^{x^2+1}\ln 3.e^{2x}$$

$$= 2.e^{2x}3^{x^2+1} + 2x3^{x^2+1}\ln 3.e^{2x}$$

$$\therefore f'(x) = 2e^{2x}3^{x^2+1}(1+x\ln 3)$$

$$b. \ f(x) = e^{\sin x \cos x}$$

$$f'(x) = (\sin x \cos x)' e^{\sin x \cos x}$$
$$= [(\sin x)' \cos x + (\cos x)' \cos x] e^{\sin x \cos x}$$
$$\therefore f'(x) = (\cos^2 x - \sin^2 x) e^{\sin x \cos x}$$

សំសាត់ ៧. គណនាដើរវៃនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = (x^2 - 1)\ln(x^2 - 1)$$

$$\mathbf{m}. \ f(x) = \ln(\sin x. \cos(2x))$$

9.
$$f(x) = (x^2 - 1) \ln(x^2 - 1)$$

10. $f(x) = \ln\left(\frac{x^2 - 2}{\sqrt[3]{x^2 - 2}}\right)$

$$\text{ f.} \quad f(x) = \ln(\sin x \cdot \cos(2x))$$

$$\text{ f.} \quad f(x) = \ln\left(\sqrt{\frac{1 + \sin x}{1 - \sin x}}\right)$$

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9.
$$f(x) = (x^2 - 1) \ln(x^2 - 1) \Longrightarrow f'(x) = (x^2 - 1)' \ln(x^2 - 1) + \ln(x^2 - 1)'(x^2 - 1)$$

$$= 2x \ln(x^2 - 1) + \frac{(x^2 - 1)'}{x^2 - 1} \cdot (x^2 - 1)$$

$$= 2x \ln(x^2 - 1) + 2x$$

$$\therefore f'(x) = 2x [\ln(x^2 - 1) + 1]$$

$$\text{U. } f(x) = \ln\left(\frac{x^2 - 2}{\sqrt[3]{x^2 - 2}}\right) = \ln(x^2 - 2) - \ln(x^2 - 2)^{\frac{1}{3}}$$

$$f'(x) = \frac{(x^2 - 2)'}{x^2 - 2} - \frac{1}{3} \cdot \frac{(x^2 - 2)'}{x^2 - 2}$$
$$= \frac{3(2x) - 2x}{3(x^2 - 2)}$$
$$\therefore f'(x) = \frac{4x}{3(x^2 - 2)}$$

 $\mathbf{M}. \ f(x) = \ln(\sin x. \cos(2x)) = \ln(\sin x) + \ln(\cos(2x))$

$$f'(x) = \frac{(\sin x)'}{\sin x} + \frac{(\cos(2x))'}{\cos(2x)}$$
$$= \frac{\cos x}{\sin x} - \frac{2\sin(2x)}{\cos(2x)}$$

$$\therefore f'(x) = \cot x - 2\tan(2x)$$

G.
$$f(x) = \ln\left(\sqrt{\frac{1+\sin x}{1-\sin x}}\right) = \ln\left(\frac{1+\sin x}{1-\sin x}\right)^{\frac{1}{2}} = \frac{1}{2}\left(\ln(1+\sin x) - \ln(1-\sin x)\right)$$

$$f'(x) = \frac{1}{2} \left(\frac{(1 + \sin x)'}{1 + \sin x} - \frac{(1 - \sin x)'}{1 - \sin x} \right)$$

$$= \frac{1}{2} \left(\frac{\cos x}{1 + \sin x} + \frac{\cos x}{1 - \sin x} \right)$$

$$= \frac{1}{2} \cdot \frac{(\cos x (1 - \sin x + 1 + \sin x))}{1 - \sin^2 x}$$

$$\therefore f'(x) = \frac{2 \cos x}{2 \cos^2 x} = \frac{1}{\cos x}$$

លំសាន់ ៤. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \cos(\arcsin x)$$

៥.
$$f(x) = \arcsin \sqrt{x}$$

9.
$$f(x) = \cos(\arcsin x)$$

10. $f(x) = \cot(\arctan x)$
11. $f(x) = \tan(\arctan x)$

$$\mathfrak{d}. \ f(x) = \arctan(\sin x)$$

$$\mathbf{m}. \ f(x) = \tan(\arctan x)$$

$$\mathfrak{N}. \ f(x) = \frac{\arctan x}{\arcsin x}$$

G.
$$f(x) = \arcsin(2x)$$

ជំណោះស្រួយ

9.
$$f(x) = \cos(\arcsin x) \Longrightarrow f'(x) = -(\arcsin x)' \sin(\arcsin x)$$

$$\therefore f'(x) = -\frac{\sin(\arcsin x)}{\sqrt{1-x^2}}$$

$$\textbf{0}. \ \ f(x) = \cot(\arctan x) \Longrightarrow f'(x) = -(\arctan x)'[1 + \cot^2(\arctan x)]$$

$$f'(x) = -\frac{1 + \cot^2(\arctan x)}{1 + x^2}$$

$$\text{M. } f(x) = \tan(\arctan x) \Longrightarrow f'(x) = (\arctan x)'[1 + \tan^2(\arctan x)]$$

$$f'(x) = \frac{1 + \tan^2(\arctan x)}{1 + x^2}$$

G.
$$f(x) = \arcsin(2x) \Longrightarrow f'(x) = \frac{(2x)'}{\sqrt{1 - (2x)^2}}$$

$$\therefore f'(x) = \frac{2}{\sqrt{1 - 4x^2}}$$

ය.
$$f(x) = \arcsin \sqrt{x} \Longrightarrow f'(x) = \frac{(\sqrt{x})'}{\sqrt{1 - (\sqrt{x})^2}} = \frac{\frac{1}{2\sqrt{x}}}{\sqrt{1 - x^2}} = \frac{1}{2\sqrt{x}\sqrt{1 - x^2}}$$

$$\therefore f'(x) = \frac{1}{2\sqrt{x - x^2}}$$

$$f(x)=\arctan(\sin x) \Longrightarrow f'(x)=rac{(\sin x)'}{1+(\sin x)^2}, \sin^2 x+\cos^2 x=1$$

$$\therefore f'(x) = \frac{\cos x}{2 - \cos^2 x}$$

$$\mathfrak{N}. \ f(x) = \frac{\arctan x}{\arcsin x} \Longrightarrow f'(x) = \frac{(\arctan x)' \arcsin x - (\arcsin x)' \arctan x}{(\arcsin x)^2}$$

$$f'(x) = \frac{\arcsin x}{1+x^2} - \frac{\arctan x}{\sqrt{1-x^2}}$$

$$(\arcsin x)^2$$

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១. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

(fi)
$$y = x^3 + 2x^2$$

(2)
$$y = x^3 - 4x^2$$

(គ)
$$y = x^4 - 27x$$

(W)
$$y = x^4 - 5x^2 + 4$$

(ង)
$$y = x^5 - 16x$$

(0)
$$y = \frac{x}{x+1}$$

(
$$\mathfrak{s}$$
) $y = \frac{x^2}{1 + x^2}$
(\mathfrak{s}) $y = x - \frac{1}{x}$

(ជ)
$$y = x - \frac{1}{x}$$

(NV)
$$y = x^3 + 2x^2 - x$$

$$(\mathfrak{Q}) \ y = x^4 - 2x^3 + 2x$$

(ដ)
$$y = \sqrt{1 + x^2}$$

(1)
$$y = \sqrt[4]{1+x^2}$$

២. រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

(fi)
$$f(x) = \sin x + \cos x$$

(2)
$$f(x) = 2\sin x - 3\cos x$$

(គ)
$$f(x) = 3\sin x + 2\cos x$$

(W)
$$f(x) = x \sin x + \cos x$$

(
$$\mathfrak{h}$$
) $f(x) = x \cos x - \sin x$

(
$$\mathfrak{V}$$
) $f(x) = \cos(2x)$

$$(\mathfrak{F}) \ f(x) = \frac{1 - \sin(2x)}{1 - \sin x}$$

(11)
$$f(x) = 1 + \sin x^2$$

(
$$\mathfrak{M}$$
) $f(x) = \cot x - \cos x$

$$(\mathfrak{J}) \quad f(x) = \sin(2x) - \cos(3x)$$

(ដ)
$$f(x) = \sin(\cos(3x))$$

$$(t) f(x) = \frac{\sin x^2}{r^2}$$

(2)
$$f(x) = \tan(1+x^2)$$

$$(\mathfrak{M}) \ f(x) = \cos 2x - \cos x^2$$

(M)
$$f(x) = (1 + \sqrt{1+x})^3$$

៣. រក y' នៃអនុគមន៍ខាងក្រោម៖

(fi)
$$xy = \frac{\pi}{6}$$

$$(2) \sin(xy) = 1$$

(គ)
$$xy = \frac{1}{x+y}$$

(
$$\mathbf{W}$$
) $x + y = xy$

(법)
$$(y-1)^2 + x = 0$$

(
$$\mathfrak{v}$$
) $(y+1)^2 + y - x = 0$

(3)
$$(y-x)^2 + x = 0$$

(ជ)
$$(y+x) + 2y - x = 0$$

$$(\mathfrak{W}) (y^2 - 1)^2 + x = 0$$

$$(\mathfrak{m}) (y^2 + 1)^2 - x = 0$$

$$(\vec{u}) \ x^3 + xy + y^3 = 3$$

(
$$\mathfrak{V}$$
) $\sin x + \sin y = 1$

$$(2) \sin x + xy + y^5 = \pi$$

(
$$\mathfrak{A}\mathfrak{J}$$
) $\tan x + \tan y = 1$

៤. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

(n)
$$f(x) = \sqrt{1-x}$$

(2)
$$f(x) = \sqrt[4]{x + x^2}$$

(គ)
$$y = \sqrt{1 - \sqrt{x}}$$

(W)
$$y = \sqrt{x - \sqrt{x}}$$

(1)
$$y = \sqrt[3]{\sqrt{2x+1}} - x^2$$

(
$$\mathfrak{v}$$
) $y = \sqrt[4]{x + x^2}x + x^2$

$$(5) \ y = \sqrt[3]{x - \sqrt{2x + 1}}$$

(ជ)
$$y = \sqrt[4]{\sqrt[3]{x}} + \sqrt[3]{\sqrt{x}} + \sqrt{x}$$

៥. គណនាដេរីវេនៃអនៃអនុគមន៍ខាងក្រោម៖

(n)
$$f(x) = e^x + e^{-x}$$

(2)
$$f(x) = e^{3x} + 4e^x$$

(1)
$$f(x) = \frac{e^x}{1 + e^x}$$

(1) $f(x) = \frac{2e^{2x}}{1 + e^{2x}}$

$$f(\mathbf{w}) \ f(x) = \frac{2e^{2x}}{1 + e^{2x}}$$

(ង)
$$f(x) = xe^{-x} + x \ln x$$

(
$$\mathfrak{G}$$
) $f(x) = \sqrt{x}e^{-\frac{x}{4}} + x^2e^{x+2}$

$$f(x) = x^{-\frac{1}{2}x} + \ln \sqrt{x}$$

$$(\mathfrak{U}) \ f(x) = (\ln x)^2 + \ln x + 1$$

(
$$\mathfrak{W}$$
) $f(x) = \frac{\ln x}{x} + \ln \frac{1}{x}$

$$(\mathfrak{Q}) \ f(x) = \ln\left(\sqrt{\frac{\sqrt{x}+1}{\sqrt{x}-1}}\right)$$

៦. គណនាដេរីវេនៃអនៃអនុគមន៍ខាងក្រោម៖

(f)
$$f(x) = \tan(\arctan x)$$

(2)
$$f(x) = \arcsin(\sin x)$$

(គ)
$$f(x) = \cot(\arcsin x)$$

$$(\mathbf{W}) \ f(x) = \sin(\arctan x)$$

(ង)
$$f(x) = (\arcsin x)^2$$

(v)
$$f(x) = \frac{1}{1 + (\arctan x)^2}$$

$$(5) f(x) = \sqrt{1 - (\arcsin x)^2}$$

៧. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

(f)
$$y = (x+1)(x-1)$$

(8)
$$y = (x^2 + 1)(x^2 - 1)$$

(f)
$$y = \frac{1}{x+1} + \frac{1}{1+\sin x}$$
(W) $y = \frac{1}{1+x^2} + \frac{1}{1-\sin x}$

$$(\mathbf{w}) \ \ y = \frac{1}{1+x^2} + \frac{1}{1-\sin x}$$

(
$$y = (x-1)(x-2)(x-3)$$

$$(\mathfrak{V}) \ \ y = x^2 \cos x + 2x \sin x$$

(3)
$$y = x^{\frac{1}{2}}(x + \sin x)$$

(1)
$$y = x^{\frac{1}{2}} \sin^2 x + (\sin x)^{\frac{1}{2}}$$

$$(\mathbf{W}) \ \ y = x^4 \cos x + x \cos x$$

$$(\mathfrak{Q}) \ y = \frac{1}{2}x^2\sin x - x\cos x + \sin x$$

(ដ)
$$y=\sqrt{x}(\sqrt{x}+1)(\sqrt{x}+2)$$

(f)
$$y = (x-6)^{10} + \sin^{10} x$$

$$(3) \quad y = (\sin x \cos x)^3 + \sin(2x)$$

$$(\mathfrak{A}) \ y = x^{\frac{1}{2}} \sin(2x) + (\sin x)^{\frac{1}{2}}$$

$$(\mathfrak{M}) \ y = \frac{\sin x - \cos x}{\sin x + \cos x}$$

$$(\mathfrak{H}) \ y = \frac{1}{\tan x} - \frac{1}{\cot x}$$

$$(\mathfrak{h}) \ \ y = \frac{1}{\tan x} - \frac{1}{\cot x}$$