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១.១ និយមន័យ

និយទន័យ ១.១.១ ដេរីវេនៃអនុគមន៍ y=f(x) ត្រង់ a កំណត់ដោយ

$$f'(a) = \lim_{x \to a} \frac{f(x) - f(a)}{x - a} \, \mathfrak{I} \tag{9.9}$$

- អនុគមន៍ f មានដេរីវេលើចន្លោះបើក (b,c) កាលណា f មានដេរីវេលើគ្រប់ចំណុច $a\in (b,c)$ ។
- អនុគមន៍ f មានដេរីវេលើចន្លោះបិទ [b,c] កាលណា f មានដេរីវេលើចន្លោះ (b,c) ហើយ f មានដេរីវេ ខាងឆ្វេងត្រង់ x=b និងខាងស្ដាំត្រង់ x=c ។
- ullet ឧនរមារស៍ ១.១ រកដើរីវេនៃអនុគមន៍ $y=f(x)=2x^2+3$ ត្រង់ 2 ។

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$$f'(2) = \lim_{x \to 2} \frac{f(x) - f(2)}{x - 2}$$
 ដែល $f(2) = 2(2)^2 + 3 = 11$
$$f'(2) = \lim_{x \to 2} \frac{2x^2 + 3x - 11}{x - 2}$$

$$= \lim_{x \to 2} \frac{2x^2 - 8}{x - 2}$$

$$= \lim_{x \to 2} \frac{2(x + 2)(x - 2)}{x - 2}, x \neq 2$$

$$= 2 \times 4 = 8$$

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តាង $h=x-a\Longrightarrow x=h+a$ បើ $h\longrightarrow 0$ នោះ $x\longrightarrow a$ នោះសមីការ (១.១) គេបាន

$$f'(a) = \lim_{h \to 0} \frac{f(h+a) - f(a)}{h} \tag{9.0}$$

- lacksquare ទំនន់ ១.១ គេអាចសរសេរដេរីវេដោយ y' , f'(x) ឬ $\dfrac{dy}{dx}$ ។
- ullet ឧនាទារសំ ១.២ ស្រាយថាបើ y=x នោះ y'=1 ។

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តាមនិយមន័យ

$$f'(x) = \lim_{h \to 0} \frac{f(h+x) - f(x)}{h}$$
 ដែល $y = f(x) = x, f(h+x) = h+x$
$$= \lim_{h \to 0} \frac{h+x-x}{h} = \lim_{h \to 0} 1 = 1$$
 $\therefore \quad \frac{dy}{dx} = 1$

 $oldsymbol{\mathfrak{g}}$ ទ្ធន្ន ១.១.១ បើអនុគមន៍ f មានដេរីវេត្រង់ x_0 នោះ f ជាប់ត្រង់ x_0 ។

សូរស្រសព្ធស្វាន់

ullet ទំណះ ១.២ បើអនុគមន៍ f ជាប់ត្រង់ x_0 នោះ f អាចមានដេរីវេត្រង់ x_0 ឬ គ្មានដេរីវេត្រង់ x_0 ។

១.២ នាពមានដើម

និយមន័យ ១.២.១ អនុគមន៍ f មានដេរីវេត្រង់ x លុះត្រាតែ

• អនុគមន៍
$$f$$
 ជាប់ត្រង់ x ។
• ដេរីវេឆ្វេងស្មើដេរីវេស្តាំត្រង់ចំណុច x គឺ $f_-'(x)=f_+'(x)$ ដែល
$$f_-'(x)=\lim_{h\to 0^-}\frac{f(x+h)-f(x)}{h}$$
 និង $f_+'(x)=\lim_{h\to 0^+}\frac{f(x+h)-f(x)}{h}$ ។

■ ឧទ្ធាមាន ១.៣ គេឲ្យអនុគមន៍ f កំណត់ដោយ $f(x)= egin{cases} \cos x & \ ext{tilde } x \leq \dfrac{\pi}{4} \\ a+bx & \ ext{tilde } x>\dfrac{\pi}{4} \end{cases}$ កំណត់តម្លៃ a និង b ដើម្បីឲ្យអនុគមន៍ f មានដេរីវេត្រង់ $x=rac{\pi}{4}$ ។

ស្សមានជាង

• បើអនុគមន៍ f ជាប់ត្រង់ $x=rac{\pi}{4}$ នោះ $\lim_{x
ightarrow \pi^-}f(x)=\lim_{x
ightarrow \pi^+}f(x)=f\left(rac{\pi}{4}
ight)$ $\lim_{x \to \frac{\pi}{4}^{-}} \cos x = \lim_{x \to \frac{\pi}{4}^{+}} (a + bx) = \cos \frac{\pi}{4} \Longleftrightarrow \frac{\sqrt{2}}{2} = a + b \cdot \frac{\pi}{4} = \frac{\sqrt{2}}{2} \Longrightarrow a = \frac{\sqrt{2}}{2} - \frac{\pi}{4} \cdot b$

$$\begin{split} f'_{-}\left(\frac{\pi}{4}\right) &= \lim_{h \to 0^{-}} \frac{f\left(\frac{\pi}{4} + h\right) - f\left(\frac{\pi}{4}\right)}{h}, f(x) = \cos x \\ &= \lim_{h \to 0^{-}} \frac{\cos\left(\frac{\pi}{4} + h\right) - \cos\frac{\pi}{4}}{h} \\ &= \lim_{h \to 0^{-}} \frac{\cos\frac{\pi}{4}\cos h - \sin\frac{\pi}{4}\sin h - \cos\frac{\pi}{4}}{h} \\ &= \lim_{h \to 0^{-}} \frac{-\cos\frac{\pi}{4}(1 - \cos h) - \sin\frac{\pi}{4}\sin h}{h} \\ &= \frac{\sqrt{2}}{2}\lim_{h \to 0^{-}} \left(-\frac{1 - \cos h}{h} - \frac{\sin h}{h}\right), \lim_{h \to 0^{-}} \frac{1 - \cos h}{h} = 0, \lim_{h \to 0^{-}} \frac{\sin h}{h} = 1 \\ &= \frac{\sqrt{2}}{2}(0 - 1) = -\frac{\sqrt{2}}{2} \end{split}$$

• ដើរីវេស្តាំ $f'_+(x)$

$$f'_{+}\left(\frac{\pi}{4}\right) = \lim_{h \to 0^{+}} \frac{f\left(\frac{\pi}{4} + h\right) - f\left(\frac{\pi}{4}\right)}{h}, f(x) = a + bx$$

$$= \lim_{h \to 0^{+}} \frac{a + b\left(\frac{\pi}{4} + h\right) - \left(a + b \cdot \frac{\pi}{4}\right)\right)}{h}$$

$$= \lim_{h \to 0^{+}} \frac{a + b \cdot \frac{\pi}{4} + bh - a - b \cdot \frac{\pi}{4}}{h}$$

$$= \lim_{h \to 0^{+}} \frac{bh}{h} = b$$

ដោយ f មានដេរីវេត្រង់ $x=\frac{\pi}{4}$ នោះ $f_-'(\frac{\pi}{4})=f_+'(\frac{\pi}{4})\Longleftrightarrow b=-\frac{\sqrt{2}}{2}\Longrightarrow a=\frac{\sqrt{2}}{2}\left(1+\frac{\pi}{4}\right)$

១.៣ លគ្គណៈនៃនៅទេ

 $oldsymbol{e}$ ចំពោះ u,v ជាអនុគមន៍នៃ x និង k ជាចំនួនថេ នោះគេបាន៖

9.
$$(ku)' = ku'$$

$$(u-v)' = u'-v'$$

ਫ.
$$\left(\frac{u}{v}\right)' = \frac{u'v - v'u}{v^2}$$

$$(u+v)' = u' + v$$

d.
$$\left(\frac{u}{v}\right)' = \frac{u'v - v'u}{v^2}$$
b. $\left(\frac{1}{v}\right)' = -\frac{v'}{v^2}$

សម្រាយមញ្ជាក់

9. តាង f(x) = k.u(x) ដែល u = u(x) និង k ជាចំនួនថេ តាមនិយមន័យ

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{ku(x+h) - k.u(x)}{h}$$

$$= k. \lim_{h \to 0} \frac{u(x+h) - u(x)}{h}$$

$$= k.u'(x)$$

$$\therefore (k.u)' = k.u'$$

២. តាង f(x) = u(x) + v(x) ដែល u = u(x) និង v = v(x) តាមនិយមន័យ

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{u(x+h) + v(x+h) - (u(x) + v(x))}{h}$$

$$= \lim_{h \to 0} \frac{u(x+h) - u(x)}{h} + \lim_{h \to 0} \frac{v(x+h) - v(x)}{h}$$

$$= u'(x) + v'(x)$$

$$\therefore (u+v)' = u'+v'$$

៣. ស្រាយដូចទី២

៤. តាង f(x) = uv ដែល u = u(x) និង v = v(x) តាមនិយមន័យគេបាន

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{u(x+h) \cdot v(x+h) - u(x) \cdot v(x)}{h}$$

$$= \lim_{h \to 0} \frac{u(x+h) \cdot v(x+h) - u(x) \cdot v(x+h) + u(x) \cdot v(x+h) + u(x) \cdot v(x)}{h}$$

$$= \lim_{h \to 0} \left[\frac{u(x+h) \cdot v(x+h) - u(x) \cdot v(x+h)}{h} + \frac{u(x) \cdot v(x+h) + u(x) \cdot v(x)}{h} \right]$$

$$= \lim_{h \to 0} \left[v(x+h) \cdot \frac{u(x+h) - u(x)}{h} + u(x) \cdot \frac{v(x+h) + v(x)}{h} \right]$$

$$= v(x) \cdot \frac{d}{dx}(u(x)) + u(x) \cdot \frac{d}{dx}(v(x))$$

$$\therefore (uv)' = u'v + v'u \tag{9.1}$$

៥. យក u=u(x) និង v=v(x) តាង $f(x)=\dfrac{u}{v}\Leftrightarrow f(x).v=u$ ធ្វើដេរីវេអង្គទាំងពីរធៀបនឹង x នោះគេបាន [f(x).v]'=u' ប្រើតាមសមីការ (១.៣) គេបាន

$$f'(x).v + v'f(x) = u', f(x) = \frac{u}{v}$$

$$f'(x).v + v'.\frac{u}{v} = u'$$

$$\frac{f'(x).v^2}{v} + \frac{v'u}{v} = u'$$

$$f'(x).v^2 + v'u = u'v$$

$$f'(x) = \frac{u'v - v'u}{v^2}$$

$$\therefore \quad \left(\frac{u}{v}\right)' = \frac{u'v - v'u}{v^2} \tag{9.6}$$

៦. យក v=v(x) តាង $f(x)=rac{1}{v}$ ប្រើសមីការ (១.៤) គេបាន

$$f'(x) = \frac{(1)' \cdot v - v' \cdot (1)}{v^2}$$
$$= \frac{0 - v'}{v^2}$$
$$= -\frac{v'}{v^2}$$
$$\therefore \left(\frac{1}{v}\right)' = -\frac{v'}{v^2}$$

១.៤ ដើទេខែអនុគមន៍មណ្ឌាអ់

ខាន្ទនៅ១ បើ
$$y=f(u)$$
 និង $u=g(x)$ នោះ $\frac{d}{dx}(f\circ g)=\frac{dy}{dx}=\frac{dy}{du} imes\frac{du}{dx}$ ។

ស្ខេសខណ្ឌង

តាង $F(x) = f \circ g = f(g(x))$ តាមនិយមន័យភាពមានដេរីវេត្រង់ x = a នោះគេបាន

$$F'(a) = \lim_{x \to a} \frac{F(x) - F(a)}{x - a}$$

$$= \lim_{x \to a} \frac{f(g(x)) - f(g(a))}{x - a}$$

$$= \lim_{x \to a} \left(\frac{f(g(x)) - f(g(a))}{g(x) - g(a)} \times \frac{g(x) - g(a)}{x - a}\right)$$

$$= f'(g(a)) \times g'(a) \quad , u = g(a), y = f(a)$$

$$\therefore \quad \frac{d}{dx}(f \circ g) = \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

ខានុនៅ ២ បើ y=c ដែល c ជាចំនួនថេរ នោះ $y^\prime=0$ ។

ស្រែតាតយ៉ាង

គេមាន $y=f(x_0)=c$ នោះ $f(x_0+h)=c\;,c\in\mathbb{R}$ តាមនិយមន័យគេបាន

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$
$$= \lim_{h \to 0} \frac{c - c}{h}$$
$$= \lim_{h \to 0} \frac{0}{h}$$
$$\therefore \quad \frac{d}{dr}(c) = 0$$

ullet ឧនាទារស័ ១.៤ គណនា y' ដែល $y = \left(\ln x. \log_a(\sqrt{3})\right)$ ។

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គេមាន
$$y = \left(\ln x. \log_a(\sqrt{3})\right) \Rightarrow y' = \left(\ln x. \log_a(\sqrt{3})\right)' = 0$$

lacksquare ឧនាទារណ៍ ១.៥ ស្រាយបញ្ជាក់ថា បើ $y=x^n$ នោះ $y'=nx^{n-1}$ ។

ស្និច នំខ្ចី

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គេមាន $f(x) = x^n$ នាំឲ្យ $f(x+h) = (x+h)^n$ តាមនិយមន័យ

$$y' = f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{(x+h)^n - x^n}{h}$$

$$= \lim_{h \to 0} \frac{(x+h-x)(x^{n-1} + x^{n-2}.x + \dots + x.x^{n-2}x + x^{n-1})}{h}$$

$$= \lim_{h \to 0} (x^{n-1} + x^{n-1} + \dots + x^{n-1} + x^{n+1})$$

$$= x^{n-1} \underbrace{(1+1+\dots+1+1)}_{n \text{ finds } 1}$$

$$= n.x^{n-1}$$

$$\therefore \frac{d}{dx}(x^n) = n.x^{n-1}$$

lacksquare ឧនាមារណ៍ ១.៦ គណនា f'(x)

9.
$$f(x) = x^3$$

$$f(x) = \sqrt{x}$$

$$f(x) = \sqrt[3]{x^2}$$

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9.
$$f(x) = x^3 \Rightarrow f'(x) = (x^3)' = 3x^{3-1} = 3x^2$$

$$\textbf{U}. \ \ f(x) = \sqrt{x} \Rightarrow f'(x) = (\sqrt{x})' = (x^{\frac{1}{2}})' = \frac{1}{2}x^{\frac{1}{2}-1} = \frac{1}{2}x^{-\frac{1}{2}} = \frac{1}{2\sqrt{x}}$$

$$\mathbf{m}. \ f(x) = \sqrt[3]{x^2} \Rightarrow f'(x) = (\sqrt[3]{x^2})' = (x^{\frac{2}{3}})' = \frac{2}{3}x^{\frac{2}{3}-1} = \frac{2}{3}x^{-\frac{1}{3}} = \frac{2}{3\sqrt[3]{x}}$$

 $m{\mathfrak{O}}$ ទុះទៅ ៣ បើ $y=u^n$ ដែល u ជាអនុគមន៍នៃ x នោះ $y'=nu'u^{n-1}$ ។

សង្ខាយមញ្ជាត់

គេមាន
$$y = u^n$$
 គេបាន $y' = \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(u^n) \times u' = nu'u^{n-1}$

lacksquare ឧនាមារស៍ ១.៧ គណនា y'

9.
$$y = (2x + \ln 2)^4$$

២.
$$y = \sqrt{u}$$
 ដែល u ជាអនុគមន៍នៃ x ។

ដំណោះស្រួយ

9.
$$y = (2x + \ln 2)^4 \Longrightarrow y' = 4(2x + \ln 2)'(2x + \ln 2)^{4-1} = 4(2+0)(2x + \ln 2)^3$$

$$y' = 8(2x + \ln 2)^3$$

$$\text{ U. } y = \sqrt{u} = u^{\frac{1}{x}} \Longrightarrow y' = (u^{\frac{1}{2}})' = \frac{1}{2}u'u^{\frac{1}{2}-1} = \frac{1}{2}u'u^{-\frac{1}{2}} = \frac{u'}{2\sqrt{u}} \text{ I}$$

១.៥ ខេរីទេខែអនុអនភ៌គ្រីអោលាទាគ្រ

9. ប៊ើ
$$y = \sin x$$
 នោះ $y' = \cos x$

២. បើ
$$y = \cos x$$
 នោះ $y' = -\sin x$

M. បើ
$$y = \tan x$$
 នោះ $y' = \frac{1}{\cos^2 x} = 1 + \tan^2 x$

ខេត្តលនះ ២ ដើរីវេអនុគមន៍ត្រីកោណមាត្រ

9. បើ
$$y = \sin x$$
 នោះ $y' = \cos x$

២. បើ $y = \cos x$ នោះ $y' = -\sin x$

៣. បើ $y = \tan x$ នោះ $y' = \frac{1}{\cos^2 x} = 1 + \tan^2 x$

៤. បើ $y = \cot x$ នោះ $y' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$

ស្សមានសាង

9. គេមាន $y = f(x) = \sin x$ នោះ $f(x+h) = \sin(x+h)$ តាមនិយមន័យ

$$y' = f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{\sin(x+h) - \sin x}{h}$$

$$= \lim_{h \to 0} \frac{\sin x \cos h + \sin h \cdot \cos x - \sin x}{h}$$

$$= \lim_{h \to 0} \left(\cos x \cdot \frac{\sin h}{h} - \sin x \cdot \frac{1 - \cos h}{h}\right)$$

$$= \cos x \quad , \lim_{h \to 0} \frac{\sin h}{h} = 1, \lim_{h \to 0} \frac{1 - \cos h}{h} = 0$$

$$\therefore \quad \frac{d}{dx}(\sin x) = \cos x$$

២. គេមាន $y = f(x) = \cos x$ នោះ $f(x+h) = \cos(x+h)$ តាមនិយមន័យ

$$y' = f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{\cos(x+h) - \cos x}{h}$$

$$= \lim_{h \to 0} \frac{\cos x \cdot \cos h - \sin x \cdot \sin h - \cos x}{h}$$

$$= \lim_{h \to 0} \left(-\frac{\sin h}{h} \cdot \sin x - \cos x \cdot \frac{1 - \cos h}{h} \right)$$

$$= -\sin x \quad , \lim_{h \to 0} \frac{1 - \cos h}{h} = 0, \lim_{h \to 0} \frac{\sin h}{h} = 1$$

$$\therefore \quad \frac{d}{dx}(\cos x) = -\sin x$$

 \mathbb{M} . តាង $y = \tan x = \frac{\sin x}{\cos x}$ តាមសមីការ (១.៤) គេបាន

$$y' = \left(\frac{\sin x}{\cos x}\right)' = \frac{(\sin x)' \cos x - (\cos x)' \cdot \sin x}{(\cos x)^2}$$

$$= \frac{\cos x \cdot \cos x - (-\sin x) \cdot \sin x}{\cos^2 x}$$

$$= \frac{\cos^2 x + \sin^2 x}{\cos^2 x}$$

$$= 1 + \tan^2 x$$

$$= \frac{1}{\cos^2 x}, \sin^2 x + \cos^2 x = 1$$

$$\therefore (\tan x)' = \frac{1}{\cos^2} = 1 + \tan^2 x$$

៤. តាង $y = \cot x = \frac{\cos x}{\sin x}$ តាមសមីការ (១.៤) គេបាន

$$y' = \left(\frac{\cos x}{\sin x}\right)' = \frac{(\cos x)' \cdot \sin x - (\sin x)' \cdot \cos x}{(\sin^2 x)^2}$$

$$= \frac{-\sin x \cdot \sin x - \cos x \cdot \cos x}{\sin^2 x}$$

$$= \frac{-\sin^2 x - \cos^2 x}{\sin^2 x}$$

$$= -\frac{\sin^2 x + \cos^2 x}{\sin^2 x}, \sin^2 x + \cos^2 x = 1$$

$$\therefore (\cot x)' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$$

ាន្ទៅ ៤បើ <math>u ជាអនុគមន៍នៃ x គេបាន

9. បើ
$$y = \sin u$$
 នោះ $y' = u' \cos u$

២. បើ
$$y = \cos u$$
 នោះ $y' = -u' \sin u$

M. បើ
$$y = \tan u$$
 នោះ $y' = \frac{u'}{\cos^2 u} = u(1 + \tan^2 u)$

ស្សមានសាង

9. បើ u ជាអនុគមន៍នៃ x នោះ $y = \sin u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\sin u) \times \frac{du}{dx} = \cos u \times u' = u'\cos u$$

$$\therefore \frac{d}{dx}(\sin u) = u'\cos u$$

២. បើ u ជាអនុគមន៍នៃ x នោះ $y = \cos u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\cos u) \times \frac{du}{dx} = -\sin u \times u' = -u'\sin u$$

$$\therefore \frac{d}{dx}(\cos u) = -u'\sin u$$

៣. បើ u ជាអនុគមន៍នៃ x នោះ $y = \tan u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\tan u) \times \frac{du}{dx} = \frac{1}{\cos^2 u} \times u' = (1 + \tan^2 u) \times u'$$

$$\therefore \quad (\tan u)' = \frac{u'}{\cos^2 u} = u'(1 + \tan^2 u)$$

៤. បើ u ជាអនុគមន៍នៃ x នោះ $y = \cot u$ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\cot u) \times \frac{du}{dx} = -\frac{1}{\sin^2 u} \times u' = -(1 + \cot^2 u) \times u'$$

$$\therefore (\cot u)' = -\frac{u'}{\sin^2 u} = -u'(1 + \cot^2 u)$$

■ **ឧនាទារស៍ ១.៤** គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$y = \sin(2x + 1)$$

$$\mathbf{m.} \ \ y = \tan(2x+1)$$

$$v = cos(2x+1)$$

$$G. \ y = \cot(2x+1) \ \Im$$

ជំនោះស្រួយ

9.
$$y = \sin(2x+1) \Rightarrow y' = (2x+1)'\cos(2x+1) = 2\cos(2x+1)$$

$$0. \ y = \cos(2x+1) \Rightarrow y' = -(2x+1)'\sin(2x+1) = -2\sin(2x+1)$$

$$\mathbf{m}. \ \ y = \tan(2x+1) \Rightarrow y' = \frac{(2x+1)'}{\cos^2(2x+1)} = \frac{2}{\cos^2(2x+1)} = 2[1 + \tan^2(2x+1)]$$

$$\text{M. } y = \tan(2x+1) \Rightarrow y' = \frac{(2x+1)'}{\cos^2(2x+1)} = \frac{2}{\cos^2(2x+1)} = 2[1 + \tan^2(2x+1)]$$

$$\text{G. } y = \cot(2x+1) \Rightarrow y' = -\frac{(2x+1)'}{\sin^2(2x+1)} = -\frac{2}{\sin^2(2x+1)} = -2[1 + \cot^2(2x+1)] \text{ 1}$$

១.៦ ខេរីខេអនុឝមន៍អិចស្ប៉ូណច់ស្យែល

ស្រាយថាថើ $y = a^x$ នោះ $y' = a^x . \ln a$

ស្សមានព្យាន់

គេមាន $y = a^x$ តាមនិយមន័យ គេបាន

$$y' = f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{a^{x+h} - a^x}{h}$$

$$= \lim_{h \to 0} \frac{a^x (a^h - 1)}{h}$$

$$= a^x \lim_{h \to 0} \frac{a^h - 1}{h} \text{ thu } \lim_{x \to 0} \frac{a^x - 1}{x} = \ln a$$

 $(a^x)' = a^x \cdot \ln a$

ខានុនៅ ៥ បើ u ជាអនុគមន៍នៃ x នោះ $(a^u)' = u'a^u \cdot \ln a$ ។

ស្សមានពេលដ

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(a^u) \times \frac{du}{dx} = a^u \cdot \ln a \times u'$$

$$\therefore (a^u)' = u' \cdot a^u \cdot \ln a)$$

ullet ឧនាទារស៍ ១.៩ គណនា y' ចំពោះ u ជាអនុគមន៍នៃ x នៃអនុគមន៍ខាងក្រោម៖

9.
$$y = e^x$$

$$v = a^{x^2 - 1}$$

$$\mathbb{M}. \ y=e^u$$

ಜೀನಾ:ಕ್ರಾಟ

9.
$$y = e^x$$
 is: $y' = (e^x)' = e^x$. $\ln e = e^x$, $\ln e = 1$

$$v = a^{x^2 - 1}$$
 is: $y' = (x^{x^2 - 1})' a^{x^2 - 1} \ln a = 2x \cdot a^{x^2 - 1} \ln a$

M.
$$y = e^u$$
 in: $y' = (e^u)' = u'e^u$. $\ln e = u'e^u$, $\ln e = 1$

ស្រាយបញ្ជាក់ថា បើ $y = \log_a x$ $, a > 0, a \ne 1$ នោះ $y' = \frac{1}{x \ln a}$ ។

ស្រាតាតយ៉ាង

គេមាន $y = \log_a x$ តាមនិយមន័យ គេបាន

$$y' = f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{\log_a(x+h) - \log_a(x)}{h}$$

$$= \lim_{h \to 0} \frac{1}{h} \log_a \left(\frac{x+h}{x}\right)$$

$$= \lim_{h \to 0} \log_a \left(1 + \frac{h}{x}\right)^{\frac{1}{h}}$$

$$= \log_a \left(\lim_{h \to 0} \left(1 + \frac{1}{\frac{x}{h}}\right)^{\frac{x}{h}}\right)^{\frac{1}{x}} \text{ thus } \lim_{x \to 0} (1 + \frac{1}{x})^x = e$$

$$= \log_a e^{\frac{1}{x}} = \frac{1}{x \ln a}$$

$$\therefore (\log_a x)' = \frac{1}{x \ln a}, a > 0, a \neq 1$$

ខាន្នៅ៦ បើ u ជាអនុគមន៍នៃ x នោះ $(\log_a u)' = \frac{u'}{u \ln a} \; , a>0, a \neq 1 \;$ ។

ស្រាតាតយាង

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\log_a u) \times \frac{du}{dx} = \frac{1}{u \ln a} \times u'$$

$$\therefore \quad (\log_a u)' = \frac{u'}{u \ln a}, a > 0, a \neq 1$$

១.៨ នើទៃខែអនុគមន៍លេអាវិតនេះព

ស្រាយបញ្ហាក់ថា បើ $y=\ln x$ នោះ $y'=rac{1}{x}$ ។

ស្សមានពេលដ

គេមាន $y = \ln x$ តាមនិយមន័យ គេបាន

$$y' = f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{\ln(x+h) - \ln(x)}{h}$$

$$= \lim_{h \to 0} \frac{1}{h} \ln\left(1 + \frac{h}{x}\right)$$

$$= \lim_{h \to 0} \ln\left(1 + \frac{h}{x}\right)$$

$$= \lim_{h \to 0} \ln\left(1 + \frac{1}{x}\right)^{\frac{1}{h}}$$

$$= \ln\left[\lim_{h \to 0} \left(1 + \frac{1}{\frac{1}{h}}\right)^{\frac{x}{h} \times \frac{1}{x}}\right], \lim_{h \to 0} \left(1 + \frac{1}{\frac{x}{h}}\right)^{\frac{x}{h}} = e$$

$$= \ln e^{\frac{1}{x}}, \ln e = 1$$

$$\therefore (\ln x)' = \frac{1}{x}$$

lacksquare ឧនាទារស៍ ១.១០ រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x^2 \cdot \log_a x, a > 0, a \neq 1$$

G.
$$f(x) = \log(x^2 \sqrt{x^3 - 1})$$

$$f(x) = \sin(2x) + \log_2(x^2 + 1)$$

៥.
$$f(x) = (\sin x)^{\log x}$$

$$\text{ \it U. } f(x) = \sin(2x) + \log_2(x^2 + 1)$$

$$\text{ \it M. } f(x) = \frac{e^{2x} + \log_3 x}{x^2}$$

$$b. \ f(x) = (\log_a x)^{\ln(2x)}, a > 0, a \neq 1$$

សម្រាយបញ្ជាក់

9.
$$f(x) = x^{2} \cdot \log_{a} x, a > 0, a \neq 1 \Longrightarrow f'(x) = (x^{2})' \log_{a} x + (\log_{a} x)' x^{2}$$
$$= 2x \log_{a} x + \frac{1}{x \ln a} x^{2}$$
$$\therefore f'(x) = 2x \log_{a} x + \frac{x}{\ln a}, a > 0, a \neq 1$$

$$0. \ f(x) = \sin(2x) + \log_2(x^2 + 1) \Longrightarrow f'(x) = -(2x)'\cos(2x) + \frac{(x^2 + 1)'}{(x^2 + 1)\ln 2}$$

$$f'(x) = -2\cos(2x) + \frac{2x}{(x^2+1)\ln 2}$$

$$\mathfrak{M}. \ f(x) = \frac{e^{2x} + \log_3 x}{x^2} \Longrightarrow f'(x) = \frac{(e^{2x} + \log_3 x)'x^2 - (x^2)'(e^{2x} + \log_3 x)}{x^4}$$

$$= \frac{(2e^{2x} + \frac{1}{x \ln 3})x^2 - 2x(e^{2x} + \log_3 x)}{x^4}$$

$$= \frac{2xe^{2x} + \frac{1}{\ln 3} - 2e^{2x} - 2\log_3 x}{x^3}$$

$$\therefore \ f'(x) = \frac{2e^{2x}(x-1) + \frac{1}{\ln 3} - \log_3 x^2}{3}$$

G.
$$f(x) = \log(x^2 \sqrt{x^3 - 1}) = \log x^2 + \log(x^3 - 1)^{\frac{1}{2}} = 2\log x + \frac{1}{2}\log(x^3 - 1)$$

$$f'(x) = \frac{2}{x \ln 10} + \frac{(x^3 - 1)'}{2(x^3 - 1)\ln 10} = \frac{2}{x \ln 10} + \frac{3x^2}{2(x^3 - 1)\ln 10}$$

$$\mathsf{G.} \ \ f(x) = (\sin x)^{\log x} \Longleftrightarrow \ln f(x) = \ln(\sin x)^{\log x}$$

$$(\ln f(x))' = (\log x. \ln(\sin x))'$$

$$\frac{f'(x)}{f(x)} = (\log x)' \ln(\sin x) + (\ln(\sin x))' \log x$$

$$f'(x) = f(x) \left(\frac{1}{x \ln 10} \ln(\sin x) + \frac{(\sin x)'}{\sin x}. \log x\right)$$

$$\therefore f'(x) = (\sin x)^{\log x} \left(\frac{\ln(\sin x)}{x \ln 10} + \cot x. \log x\right)$$

$$\text{b. } f(x) = (\log_a x)^{\ln(2x)}, a > 0, a \neq 1 \Longleftrightarrow \ln f(x) = \ln(\log_a x)^{\ln(2x)}$$

$$(\ln f(x))' = (\ln(2x) \cdot \ln(\log_a x))'$$

$$\frac{f'(x)}{f(x)} = (\ln(2x))' \ln(\log_a x) + (\ln(\log_a x))' \ln(2x)$$

$$f'(x) = f(x) \left(\frac{(2x)'}{2x} \ln(\log_a x) + \frac{(\log_a x)'}{\log_a x} \ln(2x) \right)$$

$$\therefore f'(x) = (\log_a x)^{\ln(2x)} \left(\frac{\ln(\log_a x)}{x} + \frac{\ln(2x)}{x \ln a \log_a x} \right), a > 0, a \neq 1$$

១.៨ ដេរីវេនៃអនុគមន៍លោការឹតនេពែ

 \mathfrak{S} ន្ទនេះ ៧ បើ u ជាអនុគមន៍នៃ x នោះ $(\ln u)' = \frac{u'}{u'}$ ។

ស្សមានព្យាន់

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\ln u) \times \frac{du}{dx} = \frac{1}{u} \times u'$$

$$\therefore \quad (\ln u)' = \frac{u'}{u}$$

lacksquare ឧធាមារណ៍ ១.១១ រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x \cdot \ln x$$

$$f(x) = \ln(x^2 \sqrt{x^3 - 1})$$

$$f(x) = x^2 + \ln(x^2 + 1)$$

ਫ.
$$f(x) = x^x$$

$$f(x) = \frac{e^x + \ln x}{x^2}$$

$$\delta \cdot f(x) = (\sin x)^{\cos x}$$

សម្រាយមញ្ជាក់

9.
$$f(x) = x \cdot \ln x \implies f'(x) = x' \ln x + (\ln x)' x = \ln x + \frac{1}{x} \cdot x = \ln x + 1$$

$$f(x) = x^2 + \ln(x^2 + 1) \Longrightarrow f'(x) = (x^2)' + \frac{(x^2 + 1)''}{x^2 + 1} = 2x + \frac{2x}{x^2 + 1}$$

$$f(x) = \frac{e^x + \ln x}{x^2} \Longrightarrow f'(x) = \frac{(e^x + \ln x)'x^2 - (x^2)'(e^x + \ln x)}{(x^2)^2}$$

$$\mathbf{m.} \ f(x) = \frac{e^x + \ln x}{x^2} \Longrightarrow f'(x) = \frac{(e^x + \ln x)'x^2 - (x^2)'(e^x + \ln x)}{(x^2)^2}$$

$$= \frac{\left(e^x + \frac{1}{x}\right)x^2 - 2x(e^x + \ln x)}{x^4}$$

$$\therefore f'(x) = \frac{xe^x + 1 - 2e^x - 2\ln x}{x^3}$$

$$f'(x) = \frac{xe^x + 1 - 2e^x - 2\ln x}{x^3}$$

G.
$$f(x) = \ln(x^2 \sqrt{x^3 - 1}) = \ln x^2 + \ln \sqrt{x^3 - 1} = 2\ln x + \ln(x^3 - 1)^{\frac{1}{2}}$$

$$f'(x) = 2(\ln x)' + \frac{1}{2}[\ln(x^3 - 1)]'$$
$$= 2 \cdot \frac{1}{x} + \frac{1}{2} \cdot \frac{(x^3 - 1)'}{x^3 - 1}$$

$$f'(x) = \frac{2}{x} + \frac{3}{2} \cdot \frac{x^2}{x^3 - 1}$$

$$\mathcal{E}. \ f(x) = x^x \Longleftrightarrow \ln f(x) = \ln x^x = x \ln x$$

$$(\ln f(x))' = (x \ln x)'$$

$$\frac{f'(x)}{f(x)} = x' \ln x + (\ln x)'x$$

$$f'(x) = f(x)(\ln x + \frac{1}{x}.x)$$

$$\therefore f'(x) = x^{x}(\ln x + 1)$$

$$\delta \cdot f(x) = (\sin x)^{\cos x} \Longleftrightarrow \ln f(x) = \ln(\sin x)^{\cos x}$$

$$(\ln f(x))' = (\cos x \ln \sin x)'$$

$$\frac{f'(x)}{f(x)} = (\cos x)' \ln \sin x + (\ln \sin x)' \cos x$$

$$f'(x) = f(x) \left(-\sin x \ln \sin x + \frac{(\sin x)'}{\sin x} \cdot \cos x \right)$$

$$\therefore f'(x) = (\sin x)^{\cos x} (\cos x \cot x - \sin x \ln \sin x)$$

១.៩ នេះីទេខែអនុឝមន៍ Arc Sine និខ Arc Tangent

$$y = \arcsin x \iff x = \sin y$$
 និង $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$, $y = \arctan x \iff x = \tan y$ និង $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$,

$$lacksquare$$
 ឧន្ទាមរស្នាំ ១.១២ ស្រាយថា បើ $y=rcsin x$ នោះ $y'=rac{1}{\sqrt{1-x^2}}$ ។

សូស្រាលព្ធលំ

បើ $y = \arcsin x$ នោះ $x = \sin y$ ធ្វើដេរីវេអង្គសងខាងធៀបនឹង x គេបាន

$$(x)' = (\sin y)' \iff 1 = y' \cos y$$

$$y' = \frac{1}{\cos y} \text{ in w } \sin^2 y + \cos^2 y = 1$$

$$\implies \cos y = \pm \sqrt{1 - \sin^2 x}$$

$$\text{in w } -\frac{\pi}{2} \le y \le \frac{\pi}{2} \implies \cos y \ge 0 \implies \cos y = \sqrt{1 - x^2}$$

$$\therefore \quad (\arcsin x)' = \frac{1}{\sqrt{1 - x^2}}$$

lacksquare ឧន្ទាមរស័រ ១.១៣ ស្រាយថា បើ $y=\arctan x$ នោះ $y'=rac{1}{1+x^2}$ ។

ស្ខេតខេស្សាង

បើ $y = \arctan x$ នោះ $x = \tan y$ ធ្វើដេរីវេអង្គសងខាងធៀបនឹង x គេបាន

$$(x)' = (\sin y)' \iff 1 = y'(1 + \tan^2 y)$$
$$y' = \frac{1}{1 + \tan^2 y}$$
$$\therefore (\arctan x)' = \frac{1}{1 + x^2}$$

ខាន្នៅ ៤ បើ u ជាអនុគមន៍នៃ x នោះ $(\arcsin u)' = \frac{u'}{\sqrt{1-x^2}}$

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បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\arcsin u) \times \frac{du}{dx} = \frac{1}{\sqrt{1 - u^2}} \times u'$$

$$\therefore (\arcsin u)' = \frac{u'}{\sqrt{1 - u^2}}$$

ខានុនៅ ៩ បើ u ជាអនុគមន៍នៃ x នោះ $(\arctan u)' = \frac{u'}{1+u^2}$

ស្សេសសេស្តាន់

បើ u ជាអនុគមន៍នៃ x នោះ គេបាន

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = \frac{d}{du}(\arctan u) \times \frac{du}{dx} = \frac{1}{1 - u^2} \times u'$$

$$\therefore (\arctan u)' = \frac{u'}{1 + u^2}$$

■ ឧនាមារណ៍ ១.១៤ គណនាដើរវៃនៃអនុគមន៍ខាងក្រោម៖

9. $f(x) = \arcsin x \cdot \sin x$

 $\mathfrak{m}. \ f(x) = \sin(\arcsin x)$

 \mathfrak{v} . $f(x) = \arctan x \cos x$

 $f(x) = \arctan(\tan x)$

សូស្រាលព្ធលំ

9. $f(x) = \arcsin x \cdot \sin x \Longrightarrow f'(x) = (\arcsin x)' \sin x + (\sin x)' \arcsin x$

$$\therefore f'(x) = \frac{\sin x}{\sqrt{1 - x^2}} + \cos x. \arcsin x$$

 \mathfrak{V} . $f(x) = \arctan x \cos x \Longrightarrow f'(x) = (\arctan x)' \cos x + (\cos x)' \arctan$

$$f'(x) = \frac{\cos x}{1 + x^2} - \sin x. \arctan x$$

 $\mathsf{m.}\ \ f(x) = \sin(\arcsin x) \Longrightarrow f'(x) = (\arcsin x)' \cos(\arcsin x)$

$$f'(x) = \frac{\cos(\arcsin x)}{\sqrt{1 - x^2}}$$

G. $f(x) = \arctan(\tan x) \Longrightarrow f'(x) = \frac{(\tan x)'}{1 + (\tan x)^2} = \frac{1 + \tan^2 x}{1 + \tan^2 x}$

$$\therefore f'(x) = 1$$

9.90 រួមមន្តនៃសើរទេ

បើ C,a,b,c ជាចំនួនថេ និង u ជាអនុគមន៍នៃ x ដែល $n\in\mathbb{N}$ គេបាន៖

9.
$$(C)' = 0$$

$$v(x)' = 1$$

$$\mathsf{m.} \ (ax+b)'=a$$

G.
$$(ax^2 + bx + c)' = 2ax + b$$

៥.
$$(x^n)' = nx^{n-1}$$

$$\mathfrak{d}. \ (u^n)' = n.u'.u^{n-1}$$

$$\mathfrak{N}. \ (x)^{-n} = -\frac{n}{x^{n+1}}$$

$$G. \left(\frac{1}{x}\right)' = -\frac{1}{x^2}$$

$$\mathcal{E}. \left(\frac{1}{u}\right)' = -\frac{u}{u^2}$$

$$90. \ (\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$99. \ (\sqrt{u})' = \frac{u'}{2\sqrt{u}}$$

90.
$$(\sqrt[n]{x})' = \frac{1}{n\sqrt[n]{x^{n-1}}}$$

$$\mathfrak{Im}. \ (\ln x)' = \frac{1}{x}$$

୭G.
$$(\ln u)' = \frac{u'}{u}$$

១៥.
$$(\log_a x)' = \frac{1}{x \ln a}, a > 0, a \neq 1$$

95.
$$(\log_a u)' = \frac{u'}{u \ln a}, a > 0, a \neq 1$$

$$\mathfrak{I}. \ (a^x)' = a^x \ln a, a > 0, a \neq 1$$

$$\mathfrak{GG}. \ (a^u)' = u'a^u \ln a, a > 0, a \neq 1$$

១៩.
$$(e^x)' = e^x$$

២០.
$$(e^u)' = u'e^u$$

២១.
$$(\sin x)' = \cos x$$

២២.
$$(\sin u)' = u' \cos u$$

$$\mathbf{UM.} (\cos x)' = -\sin x$$

២៤.
$$(\cos u)' = -u' \sin u$$

២៥.
$$(\tan x)' = \frac{1}{\cos^2 x} = 1 + \tan^2 x$$

$$\text{vb. } (\tan u)' = \frac{\cos^2 x}{u'} = u'(1 + \tan^2 u)$$

$$\mathbf{vn.} \ (\cot x)' = -\frac{1}{\sin^2 x} = -(1 + \cot^2 x)$$

$$\text{OG. } (\cot u)' = -\frac{u'}{\sin^2 u} = -(1 + \cot^2 u)$$

$$\mathfrak{DE}. \ (\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$

$$\text{MO. } (\arcsin u)' = \frac{u'}{\sqrt{1 - u^2}}$$

M9.
$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$$

$$\text{MU. } (\arccos u)' = -\frac{u'}{\sqrt{1-u^2}}$$

$$\mathbf{MM.} \ (\arctan x)' = \frac{1}{1+x^2}$$

$$\mathbf{MG.} \ (\arctan u)' = \frac{u'}{1+u^2}$$

M៥.
$$(\operatorname{arccot} x)' = -\frac{1}{1+x^2}$$

$$\mathbb{M}\mathfrak{d}. \ (\operatorname{arccot} u)' = -\frac{u'}{1+u^2}$$

$$\mathbf{mN}. \ (u^{v})' = \left(v'.\ln u + \frac{v.u'}{u}\right).u^{v}$$

លំខាង និខ ជំណោះស្រាយ

 ${f \mathring{c}}$ ទោត់ ១ គណនា f'(x) នៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1$$

$$b. \sqrt[4]{x^3 - 2x}$$

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1$$

10. $f(x) = 2x^2 - \sqrt{x} + \frac{2}{x}$
11. $f(x) = (x^4 - 7x^2 + \sin a)^7$
12. $f(x) = (x^4 - 7x^2 + \sin a)^7$
13. $f(x) = (x^4 - 7x^2 + \sin a)^7$
14. $f(x) = (x^4 - 7x^2 + \sin a)^7$
15. $f(x) = (x^4 - 7x^2 + \sin a)^7$
16. $f(x) = (x^4 - 7x^2 + \sin a)^7$
17. $f(x) = (x^4 - 7x^2 + \sin a)^7$
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21. $f(x) = (x^4 - 7x^2 + \sin a)^7$
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26. $f(x) = (x^4 - 7x^2 + \sin a)^7$
27. $f(x) = (x^4 - 7x^2 + \sin a)^7$
28. $f(x) = (x^4 - 7x^2 + \sin a)^7$
29. $f(x) = (x^4 - 7x^2 + \sin a)^7$
20. $f(x) = (x^4 - 7x^2 + \sin a)^7$
20. $f(x) = (x^4 - 7x^2 + \sin a)^7$
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23. $f(x) = (x^4 - 7x^2 + \sin a)^7$
24. $f(x) = (x^4 - 7x^2 + \sin a)^7$
25. $f(x) = (x^4 - 7x^2 + \sin a)^7$
26. $f(x) = (x^4 - 7x^2 + \sin a)^7$

$$\mathfrak{N}. \ f(x) = (x+1)(2x-1)^2$$

$$\text{M. } f(x) = (x^4 - 7x^2 + \sin a)^7$$

G.
$$f(x) = (x^2 + 2x + 3)(x^3 - 3x - 1)$$

G.
$$f(x) = (x^2 - \sqrt{x})^{2019}$$

$$\mathfrak{E}. \ f(x) = \frac{1}{x-1}$$

$$\xi f(x) = \sqrt{x^3 - x^2 + 3}$$

$$90. \ f(x) = \frac{x\sqrt{x}}{x+1}$$

ស្សមានជាង

9.
$$f(x) = x^5 - x^4 + x^3 - x^2 + x - 1 \implies f'(x) = 5x^4 - 4x^3 + 3x^2 - 2x + 1$$

$$f(x) = 2x^2 - \sqrt{x} - \frac{2}{x} \Longrightarrow f'(x) = 4x^2 + \frac{1}{2\sqrt{x}} - \frac{2}{x^2}$$

$$f'(x) = 7(x^4 - 7x^2 + \sin a)'(x^4 - 7x^2 + \sin a)^{7-1} = 7(4x^3 - 14x)(x^4 - 7x^2 + \sin a)^6$$

$$\mathbf{m.} \ f(x) = (x^4 - 7x^2 + \sin a)^7$$

G.
$$f(x) = (x^2 - \sqrt{x})^{2019} \Longrightarrow f'(x) = 2019(x^2 - \sqrt{x})'(x^2 - \sqrt{x})^{2019 - 1}$$

$$=2019\left(2x-\frac{1}{2\sqrt{x}}\right)(x^2-\sqrt{x})^{2018}$$

$$f(x) = \sqrt{x^3 - x^2 + 3} \Longrightarrow f'(x) = \frac{(x^3 - x^2 + 3)'}{2\sqrt{x^3 - x^2 + 3}} = \frac{3x - 2}{2\sqrt{x^3 - x^2 + 3}}$$

$$b. \ \sqrt[4]{x^3 - 2x} \Longleftrightarrow f(x) = (x^3 - 2x)^{\frac{1}{4}}$$

$$f'(x) = \frac{1}{4}(x^3 - 2x)'(x^3 - 2x)^{\frac{1}{4} - 1}$$
$$= \frac{1}{4}(3x^2 - 2)(x^3 - 2x)^{-\frac{3}{4}}$$

$$f'(x) = \frac{3x^2 - 2}{4\sqrt[4]{(x^3 - 2x)^3}}$$

$$\mathfrak{n}$$
. $f(x) = (x+1)(2x-1)^2$

$$f'(x) = (x+1)'(2x-1)^2 + [(2x-1)^2]'(x+1)$$
$$= (2x-1)^2 + 2(2x-1)'(2x-1)(x+1)$$
$$= (2x-1)(2x-1+4x+4)$$

$$f'(x) = (2x-1)(6x+3)$$

G.
$$f(x) = (x^2 + 2x + 3)(x^3 - 3x - 1)$$

$$f'(x) = (x^2 + 2x + 3)'(x^2 - 3x - 1) + (x^2 - 3x - 1)'(x^2 + 2x + 3)$$

$$= (2x + 2)(x^2 - 3x - 1) + (2x - 3)(x^2 + 2x + 3)$$

$$= 2x^3 - 6x^2 - 2x + 2x^2 - 6x - 2 + 2x^3 + 4x^2 + 6x - 3x^2 - 6x - 9$$

$$f'(x) = 4x^3 - 3x^2 - 8x - 11$$

$$\mathcal{E}. \ f(x) = \frac{1}{x-1} \Longrightarrow f'(x) = -\frac{(x-1)'}{(x-1)^2} = -\frac{1}{(x-1)^2}$$

$$90. \ f(x) = \frac{x\sqrt{x}}{x+1}$$

$$f'(x) = \frac{(x\sqrt{x})'(x+1) - (x+1)'x\sqrt{x}}{(x+1)^2}$$

$$= \frac{[x'\sqrt{x} + (\sqrt{x})'x](x+1) - x\sqrt{x}}{(x+1)^2}$$

$$= \frac{\left(x + \frac{x}{2\sqrt{x}}\right)(x+1) - x\sqrt{x}}{(x+1)^2}$$

$$= \frac{x\sqrt{x} + \sqrt{x} + \frac{x}{2\sqrt{x}}(x+1) - x\sqrt{x}}{(x+1)^2}$$

$$\therefore f'(x) = \frac{x^2 + 3x}{2\sqrt{x}(x+1)^2}$$

<mark>ចំទាាត់ ២</mark> គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = x \cdot \sin x + \cos x$$

$$G. f(x) = \sin^2 \sqrt{x} + \cos^2(3x)$$

$$\mathfrak{V}. \ f(x) = \sin^3 x - x.\cos x$$

$$f(x) = \cos(3x+4) + 3\cos x \cdot \sin x$$

$$\mathbf{m}. \ f(x) = \cos(x^2 + 1) + 2\sin(x^2 - 1) \qquad \mathbf{b}. \ f(x) = \sin(\sin\sqrt{x}) + \cos^3 x$$

$$b. \ f(x) = \sin(\sin\sqrt{x}) + \cos^3 x$$

នំណោះស្រួយ

$$9. \ f(x) = x.\sin x + \cos x$$

$$f'(x) = x' \sin x + (\sin x)' \cdot x - \sin x$$
$$= \sin x + x \cdot \cos x - \sin x$$

$$\therefore f'(x) = x \cdot \cos x$$

$$0. f(x) = \sin^3 x - x.\cos x$$

$$f'(x) = 3(\sin x)' \sin^{3-1} x - [x' \cdot \cos x + (\cos x)' \cdot x]$$
$$= 3\cos x \cdot \sin^2 x - (\cos x - x \cdot \sin x)$$

$$f'(x) = 3\cos x \cdot \sin^2 x - \cos x + x\sin x$$

$$f(x) = \cos(x^2 + 1) + 2\sin(x^2 - 1)$$

$$f'(x) = -(x^2 + 1)'\sin(x^2 + 1) + 2(x^2 - 1)'\cos(x^2 - 1)$$

$$f'(x) = -2x\sin(x^2+1) + 4x\cos(x^2-1)$$

G.
$$f(x) = \sin^2 \sqrt{x} + \cos^2(3x)$$

$$f'(x) = 2(\sin\sqrt{x})'\cos^{2-1}\sqrt{x} + 2(\cos(3x))'\sin(3x)$$
$$= 2(\sqrt{x})' \cdot \cos\sqrt{x} \cdot \cos\sqrt{x} - 2(3x)'\sin(3x) \cdot \sin(3x)$$
$$f'(x) = \frac{1}{2}\cos^2\sqrt{x} - 6\sin^2(3x)$$

$$f'(x) = \frac{1}{\sqrt{x}} \cdot \cos^2 \sqrt{x} - 6\sin^2(3x)$$

៥.
$$f(x) = \cos(3x+4) + 3\cos x \cdot \sin x$$

$$f'(x) = -(3x+4)' \cdot \sin(3x+4) + 3[(\cos x)' \cdot \sin x + (\sin x)' \cdot \cos x]$$
$$= -3\sin(3x+4) + 3[-\sin x \cdot \sin x + \cos x \cdot \cos x]$$

$$f'(x) = -3[\sin(3x+4) + \sin^2 x - \cos^2 x]$$

$$b. \ f(x) = \sin(\sin\sqrt{x}) + \cos^3 x$$

$$f'(x) = (\sin \sqrt{x})' \cdot \cos(\sin \sqrt{x}) + 3(\cos x)\cos^{3-1}x$$
$$= (\sqrt{x})' \cdot \cos \sqrt{x} \cdot \cos(\sin \sqrt{x}) - 3\sin x \cos^2 x$$

$$f'(x) = \frac{1}{2\sqrt{x}}\cos\sqrt{x}.\cos(\sin\sqrt{x}) - 3\sin x.\cos^2 x$$

<mark>សំទាាត់ ៣</mark> គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = (1 + \tan x)^4$$

$$f(x) = x \cdot \tan(x^2 - 1) + x \cot(2x^2)$$

9.
$$f(x) = (1 + \tan x)^4$$

9. $f(x) = x^2 \tan x + (1 + \cot x)^2$

$$G. f(x) = \frac{\tan(2x)}{1 - \cos x}$$

ជំនោះស្រួយ

9.
$$f(x) = (1 + \tan x)^4$$

$$f'(x) = 4(1 + \tan x)'(1 + \tan^2 x)^{4-1}$$

$$f'(x) = 4(1 + \tan^2 x)(1 + \tan x)^3$$

$$f(x) = x^2 \tan x + (1 + \cot x)^2$$

$$f'(x) = (x^2)' \tan x + (\tan x)' x^2 + 2(1 + \cot x)' (1 + \cot x)^{2-1}$$

$$f'(x) = 2x \tan x + x^2 (1 + \tan^2 x) - 2(1 + \cot^2 x)(1 + \cot x)$$

$$f(x) = x \cdot \tan(x^2 - 1) + x \cot(2x^2)$$

$$f'(x) = x' \tan(x^2 - 1) + [\tan(x^2 - 1)]'x + x' \cot(2x^2) + [\cot(2x^2)]'x$$
$$= \tan(x^2 - 1) + (x^2 - 1)'[1 + \tan^2(x^2 - 1)]x - (2x^2)'[1 + \cot^2(2x^2)]x$$

$$f'(x) = \tan(x^2 - 1) + 2x^2[1 + \tan^2(x^2 - 1)] - 4x^2[1 + \cot^2(2x^2)]$$

<mark>សំទាាត់ ៤</mark> គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \frac{1 - x - 2x^2}{x^3 - \ln 3}$$

10. $f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x - x^2}}$

$$f(x) = \sin x^2 \cdot \tan(2x+3)$$

$$f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x^2}}$$

$$G. f(x) = \sin(x^2 + 5) + \cos(\sin x)$$

$$G. f(x) = \frac{\sin(\tan\sqrt{x})}{\sin(\sqrt{x})}$$

ខំឈោះស្រាយ

9.
$$f(x) = \frac{1 - x - 2x^2}{x^3 - \ln 3}$$

$$f'(x) = \frac{(1 - x - 2x^2)'(x^3 - \ln 3) - (x^3 - \ln 3)'(1 - x - 2x^2)}{(x^3 - \ln 3)^2}$$

$$= \frac{(-1 - 4x)(x^3 - \ln 3) - 3x^2(1 - x - 2x^2)}{(x^3 - \ln 3)^2}$$

$$= \frac{-x^3 + \ln 3 - 4x^4 + 4x \ln 3 - 3x^2 + 3x^3 + 6x^4}{(x^3 - \ln 3)^2}$$

$$f'(x) = \frac{2x^4 + 2x^3 - 3x^2 + 4x \cdot \ln 3 + \ln 3}{(x^3 - \ln 3)^2}$$

២.
$$f(x) = \frac{2x^2 + 3x + 4}{\sqrt{1 + 2x - x^2}} \Longleftrightarrow f(x).\sqrt{1 + 2x - x^2} = 2x^2 + 3x + 4$$
 ធ្វើដេរីវេអង្គសងខាង គេបាន

$$[f(x)\sqrt{1+2x-x^2}]' = (2x^2+3x+4)'$$

$$f'(x)\sqrt{1+2x-x^2} + (\sqrt{1+2x-x^2})'f(x) = 4x+3$$

$$f'(x)\sqrt{1+2x-x^2} + \frac{(1+2x-x^2)'}{2\sqrt{1+2x-x^2}}f(x) = 4x+3$$

$$f'(x)\sqrt{1+2x-x^2} = 4x+3 - \frac{1-x}{\sqrt{1+2x-x^2}} \cdot f(x)$$

$$\therefore f'(x) = \frac{4x+3}{\sqrt{1+2x-x^2}} + \frac{(x-1)(2x^2+3x+4)}{(1+2x-x^2)\sqrt{1+2x-x^2}}$$

$$f(x) = \sin x^2 \cdot \tan(2x+3)$$

$$f'(x) = (\sin x^2)' \tan(2x+3) + (\tan(2x+3))' \sin x^2$$

$$= (x^2)' \cdot \sin x^2 \cdot \tan(2x+3) + (2x+3)'[1 + \tan^2(2x+3)] \sin x^2$$

$$= 2x \sin x^2 \cdot \tan(2x+3) + 2\sin x^2[1 + \tan^2(2x+3)]$$

$$\therefore f'(x) = 2\sin x^2[\tan^2(2x+3) + x\tan(2x+3) + 1]$$

$$f(x) = \sin(x^2 + 5) + \cos(\sin x)$$

$$f'(x) = (x^2 + 5)'\cos(x^2 + 5) - (\sin x)'\sin(\sin x)$$

$$f'(x) = 2x\cos(x^2 + 5) - \cos x \sin(\sin x)$$

$$\text{c. } f(x) = \frac{\sin(\tan\sqrt{x})}{\sin(\sqrt{x})} \Longleftrightarrow f(x) \cdot \sin\sqrt{x} = \sin(\tan\sqrt{x})$$

$$f'(x).\sin\sqrt{x} + (\sin\sqrt{x})'f(x) = (\tan\sqrt{x})'\cos(\tan\sqrt{x})$$
$$f'(x).\sin\sqrt{x} + (\sqrt{x})'\cos\sqrt{x}.f(x) = (\sqrt{x})'(1 + \tan^2\sqrt{x})\cos(\tan\sqrt{x})$$

 $(f(x).\sin\sqrt{x})' = (\sin(\tan\sqrt{x}))'$

$$f'(x)\sin\sqrt{x} + \frac{1}{2\sqrt{x}}\cos\sqrt{x}.f(x) = \frac{1}{2\sqrt{x}}(1 + \tan^2\sqrt{x})\cos(\tan\sqrt{x})$$

$$f'(x)\sin\sqrt{x} = \frac{1}{2\sqrt{x}}\left[\left(1 + \tan^2\sqrt{x}\right)\cos(\tan\sqrt{x}) - \cos\sqrt{x}.f(x)\right]$$

$$\therefore f'(x) = \frac{(1 + \tan^2 \sqrt{x}) \cos(\tan \sqrt{x}) - \cos \sqrt{x} \cdot f(x)}{2\sqrt{x} \cdot \sin \sqrt{x}} \text{ in } f(x) = \frac{\sin(\tan \sqrt{x})}{\sin(\sqrt{x})}$$

១.១១ លំហាត់ នឹង ដំណោះស្រាយ

<mark>សំទាាត់ ៥</mark> គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = xe^x + \frac{1}{2}x^2$$

G.
$$f(x) = x^3 e^{-3x}$$

9.
$$f(x) = xe^x + \frac{1}{2}x^2$$

10. $f(x) = e^{x^2 + 2x + 1} + (x^2 - 3)e^x$
11. $f(x) = \frac{\sqrt{x}}{e^x}$

៥.
$$f(x) = e^{2x}3^{x^2+1}$$

$$\mathbf{m.} \ f(x) = \frac{\sqrt{x}}{e^x}$$

$$\mathfrak{d.} \ f(x) = e^{\sin x \cos x}$$

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9.
$$f(x) = xe^x + \frac{1}{2}x^2$$

$$f'(x) = x'e^x + (e^x)'x + \frac{1}{2} \cdot 2x = e^x + e^x x + x = e^x (1+x) + x$$

U.
$$f(x) = e^{x^2 + 2x + 1} + (x^2 - 3)e^x$$

$$f'(x) = (x^2 + 2x + 1)'e^{x^2 + 2x + 1} + (x^2 - 3)'e^x + (e^x)'(x^2 - 3)$$
$$= (2x + 2)e^{x^2 + 2x + 1} + 2xe^x + e^x(x^2 - 3)$$

$$f'(x) = 2(x+1)e^{x^2+2x+1} + e^x(2x+x^2-3)$$

$$\mathbf{m.} \ f(x) = \frac{\sqrt{x}}{e^x}$$

$$f'(x) = \frac{(\sqrt{x})'e^x + (e^x)'\sqrt{x}}{(e^x)^2} = \frac{\frac{1}{2\sqrt{x}}e^x + e^x\sqrt{x}}{e^{2x}} = \frac{1+2x}{2\sqrt{x}e^x}$$

G.
$$f(x) = x^3 e^{-3x}$$

$$f'(x) = (x^3)'e^{-3x} + (e^{-3x})'x^3$$
$$= 3x^2e^{-3x} + (-3x)'e^{-3x}x^3$$
$$= 3x^2e^{-3x} - 3e^3e^{-3x}$$

$$f'(x) = 3x^2e^{-3x}(1-x)$$

$$\text{c. } f(x) = e^{2x} 3^{x^2 + 1}$$

$$f'(x) = (e^{2x})'3^{x^2+1} + (3^{x^2+1})' \cdot e^{2x}$$

$$= (2x)'e^{2x} \cdot 3^{x^2+1} + (x^2+1)'3^{x^2+1} \ln 3 \cdot e^{2x}$$

$$= 2 \cdot e^{2x}3^{x^2+1} + 2x3^{x^2+1} \ln 3 \cdot e^{2x}$$

$$f'(x) = 2e^{2x}3^{x^2+1}(1+x\ln 3)$$

$$\mathfrak{d.} \ f(x) = e^{\sin x \cos x}$$

$$f'(x) = (\sin x \cos x)' e^{\sin x \cos x}$$
$$= [(\sin x)' \cos x + (\cos x)' \cos x] e^{\sin x \cos x}$$
$$\therefore f'(x) = (\cos^2 x - \sin^2 x) e^{\sin x \cos x}$$

លំសាត់ ៦ គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

ដំណោះស្រួយ

9.
$$f(x) = (x^{2} - 1) \ln(x^{2} - 1) \Longrightarrow f'(x) = (x^{2} - 1)' \ln(x^{2} - 1) + \ln(x^{2} - 1)'(x^{2} - 1)$$

$$= 2x \ln(x^{2} - 1) + \frac{(x^{2} - 1)'}{x^{2} - 1}.(x^{2} - 1)$$

$$= 2x \ln(x^{2} - 1) + 2x$$

$$\therefore f'(x) = 2x [\ln(x^{2} - 1) + 1]$$

$$\text{19. } f(x) = \ln\left(\frac{x^{2} - 2}{\sqrt[3]{x^{2} - 2}}\right) = \ln(x^{2} - 2) - \ln(x^{2} - 2)^{\frac{1}{3}}$$

$$f'(x) = \frac{(x^{2} - 2)'}{x^{2} - 2} - \frac{1}{3} \cdot \frac{(x^{2} - 2)'}{x^{2} - 2}$$

$$= \frac{3(2x) - 2x}{3(x^{2} - 2)}$$

$$\therefore f'(x) = \frac{4x}{3(x^{2} - 2)}$$

$$\mathsf{M.}\ \ f(x) = \ln(\sin x.\cos(2x)) = \ln(\sin x) + \ln(\cos(2x))$$

$$f'(x) = \frac{(\sin x)'}{\sin x} + \frac{(\cos(2x))'}{\cos(2x)}$$
$$= \frac{\cos x}{\sin x} - \frac{2\sin(2x)}{\cos(2x)}$$

$$\therefore f'(x) = \cot x - 2\tan(2x)$$

១.១១ លំហាត់ និង ដំណោះស្រាយ

G.
$$f(x) = \ln\left(\sqrt{\frac{1+\sin x}{1-\sin x}}\right) = \ln\left(\frac{1+\sin x}{1-\sin x}\right)^{\frac{1}{2}} = \frac{1}{2}\left(\ln(1+\sin x) - \ln(1-\sin x)\right)$$

$$f'(x) = \frac{1}{2}\left(\frac{(1+\sin x)'}{1+\sin x} - \frac{(1-\sin x)'}{1-\sin x}\right)$$

$$= \frac{1}{2}\left(\frac{\cos x}{1+\sin x} + \frac{\cos x}{1-\sin x}\right)$$

$$= \frac{1}{2} \cdot \frac{(\cos x(1-\sin x + 1 + \sin x))}{1-\sin^2 x}$$

$$\therefore f'(x) = \frac{2\cos x}{2\cos^2 x} = \frac{1}{\cos x}$$

លំសាត់ ៧ គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

9.
$$f(x) = \cos(\arcsin x)$$

៥.
$$f(x) = \arcsin \sqrt{x}$$

$$\mathfrak{V}. \ f(x) = \cot(\arctan x)$$

$$\mathfrak{d}. \ f(x) = \arctan(\sin x)$$

9.
$$f(x) = \cos(\arcsin x)$$

10. $f(x) = \cot(\arctan x)$
11. $f(x) = \tan(\arctan x)$

$$\mathfrak{A}. \ f(x) = \frac{\arctan x}{\arcsin x}$$

$$G$$
. $f(x) = \arcsin(2x)$

ជំណោះស្រួយ

9. $f(x) = \cos(\arcsin x) \Longrightarrow f'(x) = -(\arcsin x)' \sin(\arcsin x)$

$$\therefore f'(x) = -\frac{\sin(\arcsin x)}{\sqrt{1-x^2}}$$

 $\texttt{U}. \ \ f(x) = \cot(\arctan x) \Longrightarrow f'(x) = -(\arctan x)'[1 + \cot^2(\arctan x)]$

$$f'(x) = -\frac{1 + \cot^2(\arctan x)}{1 + x^2}$$

 $\mathbf{m.} \ f(x) = \tan(\arctan x) \Longrightarrow f'(x) = (\arctan x)'[1 + \tan^2(\arctan x)]$

$$f'(x) = \frac{1 + \tan^2(\arctan x)}{1 + x^2}$$

$$\text{G. } f(x) = \arcsin(2x) \Longrightarrow f'(x) = \frac{(2x)'}{\sqrt{1 - (2x)^2}}$$

$$\therefore f'(x) = \frac{2}{\sqrt{1 - 4x^2}}$$

$$\text{G. } f(x) = \arcsin \sqrt{x} \Longrightarrow f'(x) = \frac{(\sqrt{x})'}{\sqrt{1 - (\sqrt{x})^2}} = \frac{\frac{1}{2\sqrt{x}}}{\sqrt{1 - x^2}} = \frac{1}{2\sqrt{x}\sqrt{1 - x^2}}$$

$$\therefore f'(x) = \frac{1}{2\sqrt{x - x^2}}$$

$$\mathfrak{d}. \ f(x) = \arctan(\sin x) \Longrightarrow f'(x) = \frac{(\sin x)'}{1 + (\sin x)^2}, \sin^2 x + \cos^2 x = 1$$

$$f'(x) = \frac{\cos x}{2 - \cos^2 x}$$

$$\mathfrak{N}. \ f(x) = \frac{\arctan x}{\arcsin x} \Longrightarrow f'(x) = \frac{(\arctan x)' \arcsin x - (\arcsin x)' \arctan x}{(\arcsin x)^2}$$

$$f'(x) = \frac{\frac{\arcsin x}{1+x^2} - \frac{\arctan x}{\sqrt{1-x^2}}}{(\arcsin x)^2}$$

<mark>၁.၅</mark>င္က လိုအေၾဖေး၌ဆ

១. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

(ii)
$$y = x^3 + 2x^2$$

(2)
$$y = x^3 - 4x^2$$

(គ)
$$y = x^4 - 27x$$

(11)
$$y = x^4 - 5x^2 + 4$$

(a)
$$y = x^5 - 16x$$

$$(\mathfrak{V}) \ \ y = \frac{x}{x+1}$$

$$(\mathfrak{S}) \ \ y = \frac{x^2}{1 + x^2}$$

$$(\mathfrak{I}) \ \ y = x - \frac{1}{x}$$

(AU)
$$y = x^3 + 2x^2 - x$$

$$(\mathfrak{M}) \ \ y = x^4 - 2x^3 + 2x$$

(ជ)
$$y = \sqrt{1 + x^2}$$

(t)
$$y = \sqrt[4]{1 + x^2}$$

២. រក f'(x) នៃអនុគមន៍ខាងក្រោម៖

(fi)
$$f(x) = \sin x + \cos x$$

(2)
$$f(x) = 2\sin x - 3\cos x$$

(គ)
$$f(x) = 3\sin x + 2\cos x$$

$$(\mathfrak{W}) \ f(x) = x \sin x + \cos x$$

(ង)
$$f(x) = x \cos x - \sin x$$

(
$$\mathfrak{V}$$
) $f(x) = \cos(2x)$

(3)
$$f(x) = \frac{1 - \sin(2x)}{1 - \sin x}$$

(ជ)
$$f(x) = 1 + \sin x^2$$

(All)
$$f(x) = \cot x - \cos x$$

$$(\mathfrak{g}) \quad f(x) = \sin(2x) - \cos(3x)$$

(ជ)
$$f(x) = \sin(\cos(3x))$$

(1)
$$f(x) = \frac{\sin x^2}{x^2}$$

(2)
$$f(x) = \tan(1+x^2)$$

(A3)
$$f(x) = \cos 2x - \cos x^2$$

(M)
$$f(x) = (1 + \sqrt{1+x})^3$$

៣. រក y' នៃអនុគមន៍ខាងក្រោម៖

១.១២ លំហាត់មេជ្យុន

(ii)
$$xy = \frac{\pi}{6}$$

$$(2) \sin(xy) = 1$$

$$(\mathfrak{F}) \ xy = \frac{1}{x+y}$$

$$(\mathfrak{W}) \ x + y = xy$$

(ង)
$$(y-1)^2 + x = 0$$

(
$$\mathfrak{v}$$
) $(y+1)^2 + y - x = 0$

(3)
$$(y-x)^2 + x = 0$$

(ជ)
$$(y+x) + 2y - x = 0$$

$$(NU) (y^2 - 1)^2 + x = 0$$

$$(\mathfrak{Q}) (y^2 + 1)^2 - x = 0$$

(ii)
$$x^3 + xy + y^3 = 3$$

(t)
$$\sin x + \sin y = 1$$

$$(2) \sin x + xy + y^5 = \pi$$

(
$$\mathfrak{A}\mathfrak{J}$$
) $\tan x + \tan y = 1$

$$(\Omega \Omega) x \ln y = e^{\ln \sin x}$$

$$(\mathfrak{h}) (\sin x)^{\ln y} = (\tan y)^{e^{3x}}$$

៤. គណនាដេរីវេនៃអនុគមន៍ខាងក្រោម៖

$$f(x) = \sqrt{1-x}$$

(8)
$$f(x) = \sqrt[4]{x + x^2}$$

(គ)
$$y = \sqrt{1 - \sqrt{x}}$$

$$(\mathbf{W}) \ \ y = \sqrt{x - \sqrt{x}}$$

(a)
$$y = \sqrt[3]{\sqrt{2x+1} - x^2}$$

(i)
$$y = \sqrt[4]{x + x^2}x + x^2$$

(3)
$$y = \sqrt[3]{x - \sqrt{2x + 1}}$$

(ii)
$$y = \sqrt[4]{\sqrt[3]{x}} + \sqrt[3]{\sqrt{x}} + \sqrt{x}$$

៥. គណនាដេរីវេនៃអនៃអនុគមន៍ខាងក្រោម៖

(fi)
$$f(x) = e^x + e^{-x}$$

(2)
$$f(x) = e^{3x} + 4e^x$$

$$(\mathfrak{F}) \ f(x) = \frac{e^x}{1 + e^x}$$

(11)
$$f(x) = \frac{2e^{2x}}{1 + e^{2x}}$$

(ង)
$$f(x) = xe^{-x} + x \ln x$$

(ii)
$$f(x) = \sqrt{x}e^{-\frac{x}{4}} + x^2e^{x+2}$$

(3)
$$f(x) = x^{-\frac{1}{2}x} + \ln \sqrt{x}$$

(ii)
$$f(x) = (\ln x)^2 + \ln x + 1$$

$$(\mathfrak{N}) \ f(x) = \frac{\ln x}{x} + \ln \frac{1}{x}$$

$$(\mathfrak{Q}) \ f(x) = \ln\left(\sqrt{\frac{\sqrt{x}+1}{\sqrt{x}-1}}\right)$$

៦. គណនាដេរីវេនៃអនៃអនុគមន៍ខាងក្រោម៖

(ñ)
$$f(x) = \tan(\arctan x)$$

(2)
$$f(x) = \arcsin(\sin x)$$

(គ)
$$f(x) = \sin(\arctan x)$$

$$(\mathfrak{W}) \ f(x) = (\arcsin x)^2$$

(ង)
$$f(x) = \frac{1}{1 + (\arctan x)^2}$$

(i)
$$f(x) = \sqrt{1 - (\arcsin x)^2}$$

៧. គណនាជេរីវេនៃអនុគមន៍ខាងក្រោម៖

(fi)
$$y = (x+1)(x-1)$$

(2)
$$y = (x^2 + 1)(x^2 - 1)$$

(a)
$$y = \frac{1}{x+1} + \frac{1}{1+\sin x}$$

(b) $y = \frac{1}{1+x^2} + \frac{1}{1-\sin x}$

(w)
$$y = \frac{1}{1+x^2} + \frac{1}{1-\sin x}$$

(a)
$$y = (x-1)(x-2)(x-3)$$

$$(\mathfrak{F}) \ \ y = x^2 \cos x + 2x \sin x$$

(3)
$$y = x^{\frac{1}{2}}(x + \sin x)$$

(a)
$$y = x^{\frac{1}{2}} \sin^2 x + (\sin x)^{\frac{1}{2}}$$

$$(\mathfrak{M}) \ \ y = x^4 \cos x + x \cos x$$

$$(\mathfrak{Q}) \ \ y = \frac{1}{2}x^2\sin x - x\cos x + \sin x$$

(i)
$$y = \sqrt{x}(\sqrt{x} + 1)(\sqrt{x} + 2)$$

(t)
$$y = (x-6)^{10} + \sin^{10} x$$

$$(2) y = (\sin x \cos x)^3 + \sin(2x)$$

(AS)
$$y = x^{\frac{1}{2}} \sin(2x) + (\sin x)^{\frac{1}{2}}$$

(M)
$$y = \frac{\sin x - \cos x}{\sin x + \cos x}$$

(an)
$$y = \frac{\sin x - \cos x}{\sin x + \cos x}$$
(b)
$$y = \frac{1}{\tan x} - \frac{1}{\cot x}$$