Frames

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Frame operator

Frame operator defined as

$$F * v = \sum_{k} \langle v \mid b_k \rangle * b_k$$

- The set of b_k may be finite
- Continue list...

Follows from the definition

$$< F * u \mid v > = < u \mid F * v >, u, v \in V$$

Dual frame

Bases and frames

If b_k does not span V, there exists a $v \in V$ that is orthogonal to all b_k

$$\sum_{k} |\langle v \mid b_k \rangle|^2 = 0$$

Tight frames

Matrix formulation

Frame operator

$$F = BB^*G_0$$

Reconstructing coefficients

v = Bc, B is frame, c reconstructing coefficients