

# X-Method for CPMC

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## 1 X-Method for CPMC

The problem will be solved in four steps:

- 1) Pre-analysis
- 2) Matlab Program Modification
- 3) Input/Output
- 4) Discussion

Notice:

Calculation used these parameters below if no special mention:

```
Lx=4;  
Ly=4;  
Lz=1;  
N_up=7;  
N_dn=7;  
kx=0;  
ky=0;  
kz=0;  
U=8;  
tx=1;  
ty=1;  
tz=1;  
deltau=0.01;  
N_wlk=[100:1:107];  
N_blksteps=100;  
N_eqblk=5;  
N_blk=10;  
itv_modsvd=5;  
itv_pc=10;  
itv_Em=20;  
N_y=1;
```

## 1.1 Pre-analysis

Using X-Method to simulate all the Green Functions of CPMC\_Groundstate with one ( $N_y=1$ ) or more walkers and doing CPMC again with these new Phi\_T (walkers).

Model:

$$|\varphi\rangle = \sum_{\vec{y}} W * \vec{y} * (e^{\sum_{i,j,k} y_i * a_{i,j,k} * C_j^\dagger C_k} |\phi_{up}\rangle) \otimes (e^{\sum_{i,j,k} -y_i * a_{i,j,k} * C_j^\dagger C_k} |\phi_{dn}\rangle)$$

where  $|\phi_*\rangle$  is Slater determinant,  $C^\dagger, C$  is particles creation and annihilation operators and  $a, w$  are variational parameters and the number of variational parameters is linear to  $N_{sites}^2 * N_y$ . (the size of lattice:  $N_{sites}$ , the number of walkers  $N_y$ .)

Many symmetry can be used in the calculation to accelerate this algorithm. In this report, "half-filled" is used.

$N_y$  is the number of walkers and here  $N_y=1$ , since it's easier to replace Phi\_T in CPMC.

## 1.2 Matlab Program Modification

```
batchsample_X.G.m;  
CPMC_Lab.G.m;  
CPMC_Lab_BP_X.m;  
halfK_X.m;  
initialization_X.m;  
initialization_BP_X.m;  
measure_BP.G.m;  
stepwtk_AP.G.m;  
X_Pickup.G.m;  
X_RBM_Energy_X_RBM.G.m;  
X_RBM.G.dif.m;  
X_RBM_Initialization_Pickup.m;  
X_RBM_update_Pickup.G.m;  
X_Return.G.m;
```

## 1.3 Input/Output

```
1.fig;
```

## 1.4 Discussion

1. This method is iterative and related to renormalization group transformation.
2. Effective variational methods can be applied to improve the efficiency.

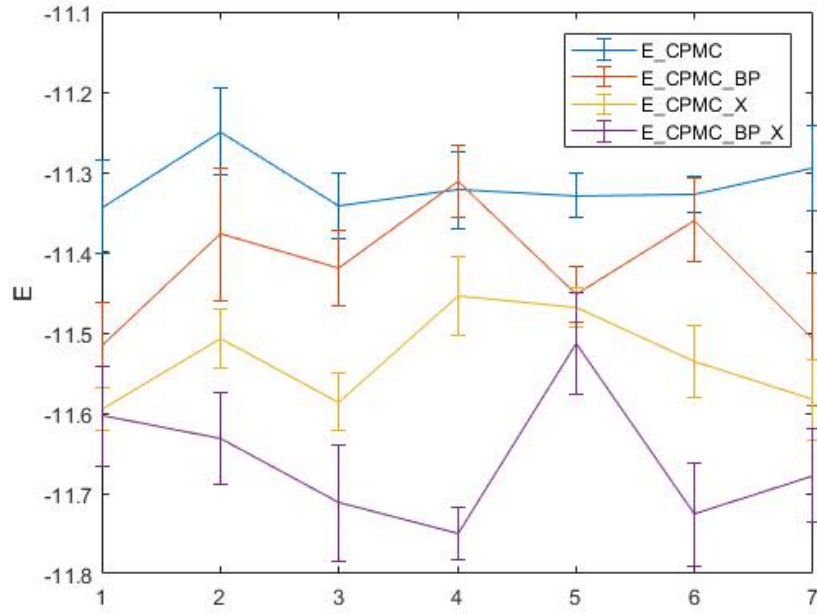


Figure 1: 1.fig; This is 7 times independent calculations of CPMC in 4 different methods;  $L_x = 4, L_y = 4, N_{up} = 7, N_{dn} = 7, U = 8$ ; E\_CPMC are the results of normal CPMC, E\_CPMC\_BP are the results of CPMC with back propagation, E\_CPMC\_X are the results of CPMC with one-iteration X-Method, E\_CPMC\_BP\_X are the results of CPMC with one-iteration X-Method and back propagation.