

# Back Propagation and Exact Diagonalization

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## 1 Back Propagation and Exact Diagonalization

The problem will be solved in five steps:

- 1) Pre-analysis
- 2) Matlab Program Modification
- 3) Input
- 4) Output
- 5) Discussion

Notice:

Calculation used these parameters below if no special mention:

```
Lx=2;  
Ly=2;  
Lz=1;  
N_up=1;  
N_dn=1;  
kx=0;  
ky=0;  
kz=0;  
U=4;  
tx=1;  
ty=1;  
tz=1;  
deltat=0.01;  
N_wlk=100;  
N_blksteps=[100:100:1000];  
N_eqblk=5;  
N_blk=10;  
itv_modsvd=5;  
itv_pc=5;  
itv_Em=[10:10:100].
```

## 1.1 Pre-analysis

$N_{up}=1$  and  $N_{dn}=1$  is used because in this situation commutation relation of Fermions can be ignored and it is easier to programming.

## 1.2 Matlab Program Modification

batchsample\_itv\_Em\_BP\_ED.m;  
CPMC\_Lab\_ED.m;  
initialization\_ED.m.

## 1.3 Input/Output

3.1.mat; 3.1.jpg; 3.2.jpg; 3.3.jpg; 3.2.mat; 3.4.jpg; 3.5.jpg; 3.6.jpg;

## 1.4 Discussion

The error of back propagation method is from the difference between  $e^{itv\_Em*deltau*H}$  and  $\sum W_i * B_i$  which is the QMC estimation of  $e^{itv\_Em*deltau*H}$  and is hard to corrected by increasing itv\_Em\*deltau.

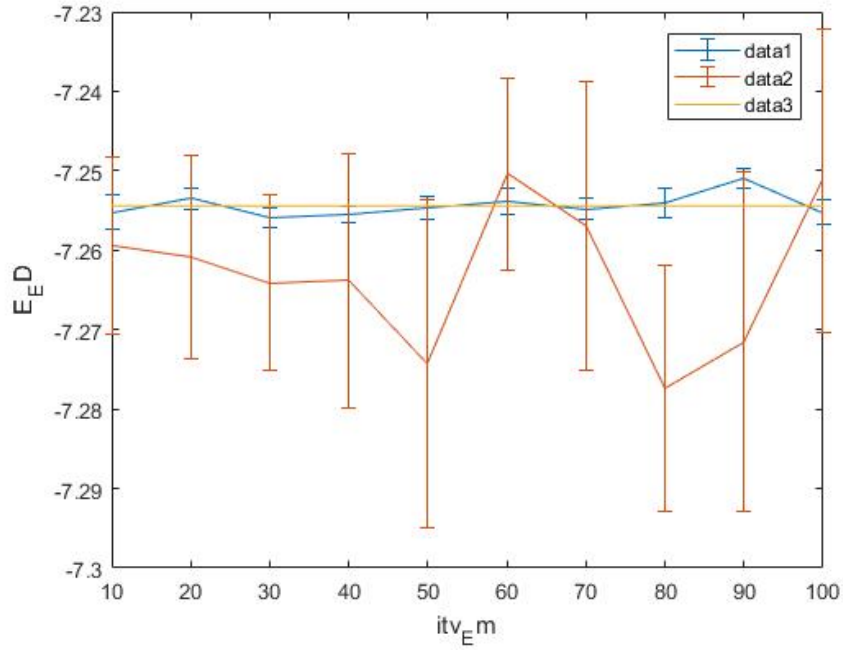


Figure 1: Data 1 is mixed Groundstate Energy, Data 2 is Back Propagation Ground State Energy, Data 3 is Exact Diagonalization Back Propagation Energy.  $itv_{Em} \cdot \delta\tau$  is the length of back propagation and the length of detect distance.

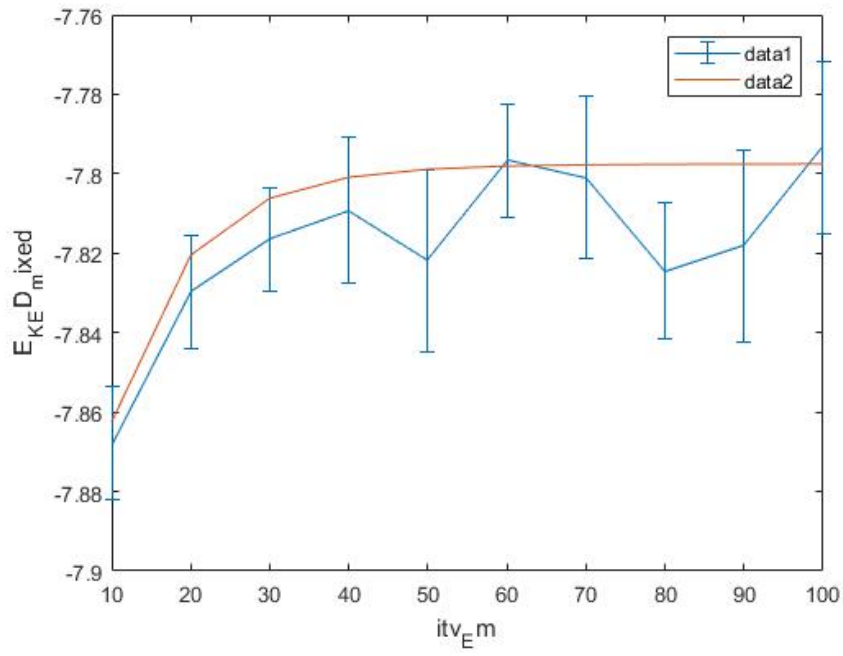


Figure 2: Data 1 is Back Propagation Kinetic Energy, Data 2 is Exact Diagonalization Back Propagation Kinetic Energy.  $itv_{Em} \cdot \delta\tau$  is the length of back propagation and the length of detect distance.

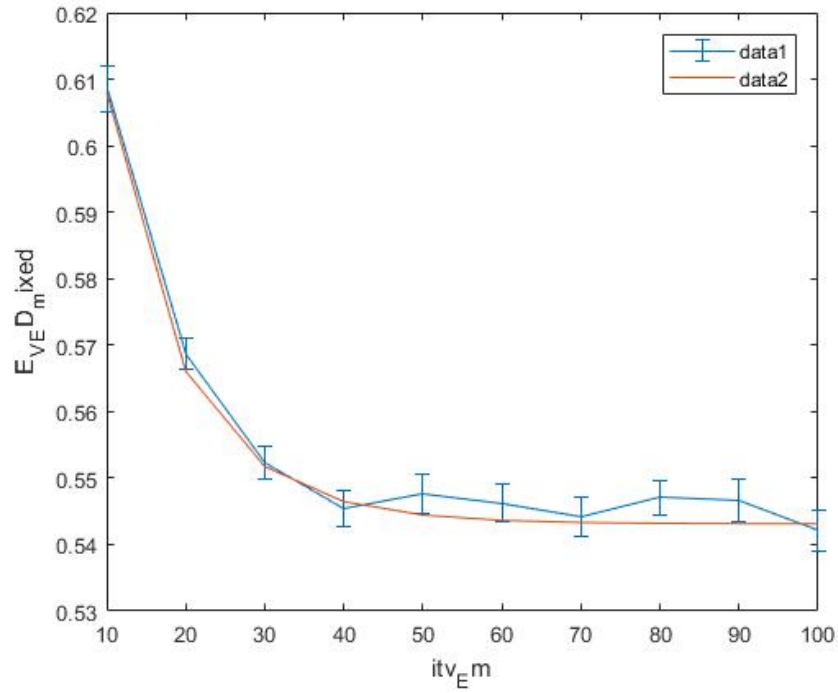
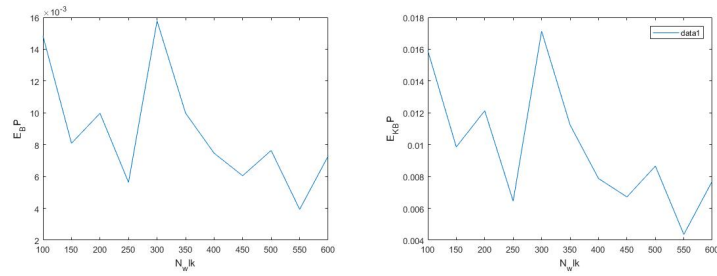
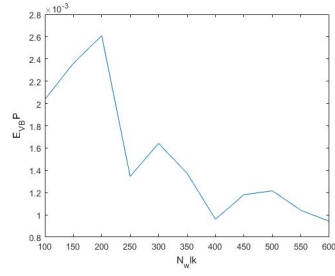


Figure 3: Data 1 is Back Propagation Potential Energy, Data 2 is Exact Diagonalization Back Propagation Potential Energy.  $itv_{Em} \cdot \delta\tau$  is the length of back propagation and the length of detect distance.

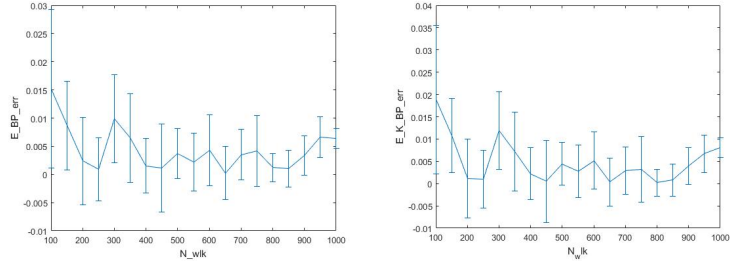


(a) The Y axis is the error bar of Back Propagation Groundstate Energy and the X axis is the number of walker. (b) The Y axis is the error bar of Back Propagation Kinetic Energy and the X axis is the number of walker.

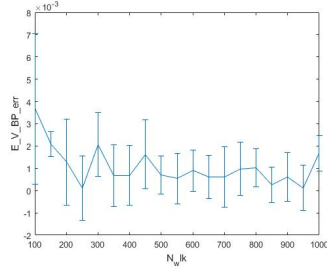


(c) The Y axis is the error bar of Back Propagation Potential Energy and the X axis is the number of walker.

Figure 4:



(a) The Y axis is the error of Back Propagation Groundstate Energy ("E\_BP-E\_ED") and the X axis is the number of walker. (b) The Y axis is the error of Back Propagation Kinetic Energy ("E\_K\_BP-E\_K\_ED") and the X axis is the number of walker.



(c) The Y axis is the error of Back Propagation Potential Energy ("E\_V\_BP-E\_V\_ED") and the X axis is the number of walker.

Figure 5: