

FUNCTIONAL AND CONCURRENT PROGRAMMING

SI4

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MORE ABOUT FUNCTIONS

Closure, Currying, Tail Recursion

CLOSURE

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- **Functions have a context**
- Example
 - ```
Lst<Integer> greaterThan(Lst<Integer> l, int v) {
 return filter(x -> x > v, l);
}
```
  - `v` is defined in the context of the lambda `x -> x > v`
- **Closure = function + context**
- **What we use to call “function” is a closure!**
  - Function may use or not this context

# CLOSURE AND METHOD REFERENCES

- **Every functional interface has a context**

- Example

- ```
class Counter {  
    int v = 0;  
    public int next() {  
        return v++;  
    }  
}
```

- counterInstance::next has v in its context
- Counter::next does not

CLOSURE AND VARIABLES

- Functions cannot modify local variables

- ```
static void print(Lst<T> l) {
 int i = 0;
 iter(x -> { System.out.println((i++) + ": " + x); }, l);
}
```

- Accessed variables must be (implicitly) final

- ```
static void print(Lst<T> l) {  
    int i = 0; i += 1;  
    iter(x -> { System.out.println(i + ": " + x); }, l);  
}
```

CLOSURE AND SIDE-EFFECT

- But closures can access mutable objects

- ```
static void print(Lst<T> l) {
 final AtomicInteger i = new AtomicInteger(0);
 iter(x -> { System.out.println(i.getAndIncrement() + ": " + x); }, l);
}
```

- Or even modify (instance or class) attributes

- ```
static int i;  
static void print(Lst<T> l) {  
    i = 0;  
    iter(x -> { System.out.println((i++) + ": " + x); }, l);  
}
```

NON-SAFE CLOSURE

- A closure that uses a mutable context is “NON-SAFE” (aka non-functional)
- No longer a pure function (something else may modify the context)
 - Non repeatable
 - Difficult to test
 - Difficult to parallelise
 - ...

SAFETY AND PARALLELISM

- A non-safe closure is still **parallelisable** if the context is thread-safe
 - AtomicInteger, AtomicBoolean, AtomicLong, AtomicLongArray, ...
 - **synchronized** instructions
 - Synchronized data structures: Collections.synchronizedList(), ...
- But easily **not distributable**
 - Ref shared nothing infrastructures

NON-FUNCTIONALITY

- This print is not functional

- ```
static int i;
static void print(Lst<T> l) {
 i = 0;
 iter(x -> { System.out.println((i++) + ": " + x); }, l);
}
```

- This one is not (but still thread-safe)

- ```
static void print(Lst<T> l) {
    final AtomicInteger i = new AtomicInteger(0);
    iter(x -> { System.out.println(i.getAndIncrement() + ": " + x); }, l);
}
```

CURRYING

CURRYING

- Translating the evaluation of a function that takes multiple arguments into evaluating a sequence of functions, each with a single argument
- Example
 - $f.\text{apply}(a, b) \quad \Rightarrow \quad f.\text{apply}(a).\text{apply}(b)$
 - $T \times R \rightarrow U \quad \Rightarrow \quad T \rightarrow (R \rightarrow U)$
 - `int add(int x, int y) { return x + y; }`
 - `Function<Integer,Integer> addc(int x) { return y -> x + y; }`

CURRYING ADVANTAGE

- Make a closure functional
- ```
class Foo {
 Integer b;
 Lst<Integer> calc(Lst<Integer> l) {
 return map(x -> x * b, l);
 }

 Lst<Integer> calcf(Lst<Integer> l) {
 Function<Integer, Function<Integer, Integer>> cf =
 y -> x -> x * y;
 return map(cf.apply(b), l);
 }
}
```
- The map in calcf is thread-safe while not in calc

# CURRYING USAGE EXAMPLE

- Have more than 2 parameters (beside BiFunction)
  - $T_1 \times T_2 \times \dots \times T_N \rightarrow R \Rightarrow T_1 \rightarrow T_2 \rightarrow \dots \rightarrow T_N \rightarrow R$

- Builder Pattern

```
• class Letter {
 static AddReturnAddress builder(){
 return returnAddress
 -> closing
 -> dateOfLetter
 -> insideAddress
 -> salutation
 -> body
 -> new Letter(returnAddress, insideAddress, dateOfLetter,
salutation, body, closing);
 }

 interface AddReturnAddress { Letter.AddClosing withReturnAddress(String
returnAddress); }
```

# **TAIL RECURSION**

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- **A function is tail recursive** if the recursive call is the **last statement** that is executed by the function

- ```
static void print(int n) {  
    if (n < 0) return;  
    System.out.print(" " + n);  
    print(n - 1);  
}
```

- But not

- ```
static int fact(int n) {
 if (n == 0) return 1;
 return n * fact(n - 1);
}
```



## WHY TAIL RECURSION?

- A tail recursion fonction can be executed as a loop
  - So without call stack comsuption
  - Many languages compile/interpret tail recursion as loop (Tail Call Optimization)
  - But not (yet) Java ☹
    - Only with specific libraries (e.g. [https://github.com/judekeyser/tail\\_rec](https://github.com/judekeyser/tail_rec))
- Better control on time complexity
  - Double recursion :  $O(2^n)$  versus tail recursion :  $O(n \cdot c_{body}(n))$  - Usually
  - But still programming easiness of recursion

# TAIL ACCUMULATOR

- Tail recursive function often use helper functions with supplementary parameters for
  - Loop variables
  - Or accumulator (the result being calculated)
- Example
  - ```
static long power(int base, int exponent) {  
    return power(base, exponent, 1);  
}
```



```
static long power(int base, int exponent, int res) {  
    if (exponent == 0) return res;  
    return power(base, exponent - 1, res * base);  
}
```
 - Helps memoization (dynamic programming approach)

COMPLEXITY COMPARED

Function	Non-tail rec	Tail rec
reverse list	$O(n^2)$	$O(n)$
fibonnaci	$O(2^n)$	$O(n)$
palindrome	$O(n^2)$	$O(n)$
edit distance	$O(2^n)$	$O(n^2)$
...		

- Not always easy (e.g. tree traversals) or possible without stack simulation (e.g. quicksort)