```
a)
In [155]: from sklearn.model_selection import StratifiedKFold
          from sklearn.preprocessing import OrdinalEncoder
          from sklearn.preprocessing import MinMaxScaler
          from sklearn.neighbors import KNeighborsClassifier
          from sklearn.tree import DecisionTreeClassifier
          from sklearn.naive_bayes import GaussianNB
          from sklearn import metrics
          import numpy as np
In [146]: def spec_score(y, y_pred):
              if(len(y) != len(y_pred)):
                  print( "Error in spec_score")
              fp = 0.
              tn = 0.
              for i in range(len(y_pred)):
                  if y_pred[i] == 0 and y[i] == 0:
                      tn += 1
                  elif y_pred[i] == 1 and y[i] == 0:
                      fp += 1
              return tn / (fp + tn)
In [187]: import csv
          spam = []
          with open('spam.csv') as csv_file:
              spam_file = csv.reader(csv_file, delimiter=',')
              linenum = 0;
              for row in spam_file:
                  if(linenum != 0):
                      spam.append(row)
                  linenum += 1
          #Transform Data to numeric type
          enc = OrdinalEncoder()
          enc.fit(spam)
          t_spam = enc.transform(spam)
          #Scale Data [0, 1]
          scaler = MinMaxScaler()
          scaler.fit(t_spam)
          s_spam = scaler.transform(t_spam)
          #Split data and target vector
          y = np.array(s_spam.T[len(s_spam[0]) - 1]) #target vector
          x = np.delete(s_spam, len(s_spam[0]) - 1, 1) #data
          skf = StratifiedKFold(n_splits=10)
          skf.get_n_splits(x, y)
          train_data = []
          test_data = []
          for train_i, test_i in skf.split(x, y):
              x_train, x_test = x[train_i], x[test_i]
              y_train, y_test = y[train_i], y[test_i]
              train_data.append((x_train, y_train))
              test_data.append((x_test, y_test))
          b)
In [188]:
          model_array = [ KNeighborsClassifier(n_neighbors = 3),
                          KNeighborsClassifier(n_neighbors = 7),
                          KNeighborsClassifier(n_neighbors = 11),
                          KNeighborsClassifier(n_neighbors = 15),
                          DecisionTreeClassifier(max_depth = 5),
                          DecisionTreeClassifier(criterion = "entropy", max_depth = 100, min_samples_split = 2
          5),
                         GaussianNB()]
          for model in model_array:
              print(model)
              split_accuracy = []
              split_auc = []
              split_recall = []
              split_spec = []
              for i in range(len(train_data)):
                  model.fit(train_data[i][0], train_data[i][1])
                  y_pred = model.predict(test_data[i][0])
                  split_accuracy.append(metrics.accuracy_score(test_data[i][1], y_pred))
                  split_auc.append(metrics.roc_auc_score(test_data[i][1], y_pred))
                  split_recall.append(metrics.recall_score(test_data[i][1], y_pred))
                  split_spec.append(spec_score(test_data[i][1], y_pred))
              for i in range(10):
                  print("Split: ", i, " Accuracy=", round(split_accuracy[i], 5),
                        "AUC=", round(split_auc[i], 5), " Recall=", round(split_recall[i], 5), " Specificity="
          , round(split_spec[i], 5))
              print("Average Accuracy over 10 splits:", np.mean(split_accuracy))
              print("Average AUC over 10 splits:", np.mean(split_auc))
              print("Average Recall over 10 splits:", np.mean(split_recall))
              print("Average Specificity over 10 splits:", np.mean(split_spec))
          KNeighborsClassifier(n_neighbors=3)
          Split: 0 Accuracy= 0.76606 AUC= 0.80833 Recall= 0.92958 Specificity= 0.68707
          Split: 1 Accuracy= 0.97235 AUC= 0.97222 Recall= 0.97183 Specificity= 0.9726
          Split: 2 Accuracy= 0.97696 AUC= 0.97926 Recall= 0.98592 Specificity= 0.9726
          Split: 3 Accuracy= 0.96313 AUC= 0.95813 Recall= 0.94366 Specificity= 0.9726
          Split: 4 Accuracy= 0.94009 AUC= 0.93377 Recall= 0.91549 Specificity= 0.95205
          Split: 5 Accuracy= 0.92627 AUC= 0.91626 Recall= 0.88732 Specificity= 0.94521
          Split: 6 Accuracy= 0.92627 AUC= 0.91626 Recall= 0.88732 Specificity= 0.94521
          Split: 7 Accuracy= 0.95853 AUC= 0.95833 Recall= 0.95775 Specificity= 0.9589
          Split: 8 Accuracy= 0.97235 AUC= 0.96498 Recall= 0.94366 Specificity= 0.9863
          Split: 9 Accuracy= 0.85714 AUC= 0.79254 Recall= 0.60563 Specificity= 0.97945
          Average Accuracy over 10 splits: 0.9259142603475248
          Average AUC over 10 splits: 0.9200087675432898
          Average Recall over 10 splits: 0.9028169014084508
          Average Specificity over 10 splits: 0.9372006336781288
          KNeighborsClassifier(n_neighbors=7)
          Split: 0 Accuracy= 0.74771 AUC= 0.79472 Recall= 0.92958 Specificity= 0.65986
          Split: 1 Accuracy= 0.97696 AUC= 0.98288 Recall= 1.0 Specificity= 0.96575
          Split: 2 Accuracy= 0.97235 AUC= 0.97583 Recall= 0.98592 Specificity= 0.96575
          Split: 3 Accuracy= 0.95853 AUC= 0.95471 Recall= 0.94366 Specificity= 0.96575
          Split: 4 Accuracy= 0.96774 AUC= 0.96517 Recall= 0.95775 Specificity= 0.9726
          Split: 5 Accuracy= 0.92166 AUC= 0.9056 Recall= 0.85915 Specificity= 0.95205
          Split: 6 Accuracy= 0.92166 AUC= 0.91284 Recall= 0.88732 Specificity= 0.93836
          Split: 7 Accuracy= 0.97235 AUC= 0.97222 Recall= 0.97183 Specificity= 0.9726
          Split: 8 Accuracy= 0.96774 AUC= 0.95794 Recall= 0.92958 Specificity= 0.9863
          Split: 9 Accuracy= 0.87097 AUC= 0.81729 Recall= 0.66197 Specificity= 0.9726
          Average Accuracy over 10 splits: 0.927766033906904
          Average AUC over 10 splits: 0.9239202665438162
          Average Recall over 10 splits: 0.9126760563380282
          Average Specificity over 10 splits: 0.935164476749604
          KNeighborsClassifier(n_neighbors=11)
          Split: 0 Accuracy= 0.73394 AUC= 0.78452 Recall= 0.92958 Specificity= 0.63946
          Split: 1 Accuracy= 0.97235 AUC= 0.97945 Recall= 1.0 Specificity= 0.9589
                 2 Accuracy= 0.97235 AUC= 0.97583 Recall= 0.98592 Specificity= 0.96575
          Split: 3 Accuracy= 0.95853 AUC= 0.95471 Recall= 0.94366 Specificity= 0.96575
          Split: 4 Accuracy= 0.97235 AUC= 0.97222 Recall= 0.97183 Specificity= 0.9726
          Split: 5 Accuracy= 0.91705 AUC= 0.9058 Recall= 0.87324 Specificity= 0.93836
          Split: 6 Accuracy= 0.91705 AUC= 0.90942 Recall= 0.88732 Specificity= 0.93151
          Split: 7 Accuracy= 0.97235 AUC= 0.97222 Recall= 0.97183 Specificity= 0.9726
          Split: 8 Accuracy= 0.95392 AUC= 0.94043 Recall= 0.90141 Specificity= 0.97945
          Split: 9 Accuracy= 0.87097 AUC= 0.81729 Recall= 0.66197 Specificity= 0.9726
          Average Accuracy over 10 splits: 0.9240857396524754
          Average AUC over 10 splits: 0.9211875296134275
          Average Recall over 10 splits: 0.9126760563380282
          Average Specificity over 10 splits: 0.9296990028888269
          KNeighborsClassifier(n_neighbors=15)
          Split: 0 Accuracy= 0.7156 AUC= 0.77091 Recall= 0.92958 Specificity= 0.61224
          Split: 1 Accuracy= 0.96313 AUC= 0.9726 Recall= 1.0 Specificity= 0.94521
          Split: 2 Accuracy= 0.97235 AUC= 0.97583 Recall= 0.98592 Specificity= 0.96575
          Split: 3 Accuracy= 0.96774 AUC= 0.96156 Recall= 0.94366 Specificity= 0.97945
          Split: 4 Accuracy= 0.97235 AUC= 0.97583 Recall= 0.98592 Specificity= 0.96575
          Split: 5 Accuracy= 0.91705 AUC= 0.90942 Recall= 0.88732 Specificity= 0.93151
          Split: 6 Accuracy= 0.91244 AUC= 0.90237 Recall= 0.87324 Specificity= 0.93151
          Split: 7 Accuracy= 0.96774 AUC= 0.96517 Recall= 0.95775 Specificity= 0.9726
          Split: 8 Accuracy= 0.94931 AUC= 0.93339 Recall= 0.88732 Specificity= 0.97945
          Split: 9 Accuracy= 0.86175 AUC= 0.8032 Recall= 0.6338 Specificity= 0.9726
          Average Accuracy over 10 splits: 0.9199467298017165
          Average AUC over 10 splits: 0.9170293778325531
          Average Recall over 10 splits: 0.908450704225352
          Average Specificity over 10 splits: 0.925608051439754
          DecisionTreeClassifier(max_depth=5)
          Split: 0 Accuracy= 0.98624 AUC= 0.98251 Recall= 0.97183 Specificity= 0.9932
          Split: 1 Accuracy= 0.94931 AUC= 0.92254 Recall= 0.84507 Specificity= 1.0
          Split: 2 Accuracy= 0.94931 AUC= 0.93701 Recall= 0.90141 Specificity= 0.9726
          Split: 3 Accuracy= 0.97235 AUC= 0.96136 Recall= 0.92958 Specificity= 0.99315
          Split: 4 Accuracy= 0.91244 AUC= 0.87705 Recall= 0.77465 Specificity= 0.97945
          Split: 5 Accuracy= 0.91705 AUC= 0.88047 Recall= 0.77465 Specificity= 0.9863
          Split: 6 Accuracy= 0.97235 AUC= 0.97222 Recall= 0.97183 Specificity= 0.9726
          Split: 7 Accuracy= 0.98157 AUC= 0.98268 Recall= 0.98592 Specificity= 0.97945
          Split: 8 Accuracy= 0.98157 AUC= 0.98268 Recall= 0.98592 Specificity= 0.97945
          Split: 9 Accuracy= 0.8894 AUC= 0.8346 Recall= 0.67606 Specificity= 0.99315
          Average Accuracy over 10 splits: 0.9511584154229908
          Average AUC over 10 splits: 0.9333131535461956
          Average Recall over 10 splits: 0.8816901408450704
          Average Specificity over 10 splits: 0.9849361662473208
          DecisionTreeClassifier(criterion='entropy', max_depth=100, min_samples_split=25)
          Split: 0 Accuracy= 0.92661 AUC= 0.92373 Recall= 0.91549 Specificity= 0.93197
          Split: 1 Accuracy= 0.94009 AUC= 0.93016 Recall= 0.90141 Specificity= 0.9589
          Split: 2 Accuracy= 0.94931 AUC= 0.93701 Recall= 0.90141 Specificity= 0.9726
          Split: 3 Accuracy= 0.91705 AUC= 0.92027 Recall= 0.92958 Specificity= 0.91096
          Split: 4 Accuracy= 0.92166 AUC= 0.89837 Recall= 0.83099 Specificity= 0.96575
          Split: 5 Accuracy= 0.8894 AUC= 0.85993 Recall= 0.77465 Specificity= 0.94521
          Split: 6 Accuracy= 0.88018 AUC= 0.87478 Recall= 0.85915 Specificity= 0.89041
          Split: 7 Accuracy= 0.96313 AUC= 0.96175 Recall= 0.95775 Specificity= 0.96575
          Split: 8 Accuracy= 0.97235 AUC= 0.97222 Recall= 0.97183 Specificity= 0.9726
          Split: 9 Accuracy= 0.88018 AUC= 0.83137 Recall= 0.69014 Specificity= 0.9726
          Average Accuracy over 10 splits: 0.9239969559886696
          Average AUC over 10 splits: 0.9109580837930388
          Average Recall over 10 splits: 0.8732394366197183
          Average Specificity over 10 splits: 0.9486767309663593
          GaussianNB()
          Split: 0 Accuracy= 0.72477 AUC= 0.69397 Recall= 0.60563 Specificity= 0.78231
          Split: 1 Accuracy= 0.91244 AUC= 0.87343 Recall= 0.76056 Specificity= 0.9863
          Split: 2 Accuracy= 0.99078 AUC= 0.99315 Recall= 1.0 Specificity= 0.9863
          Split: 3 Accuracy= 0.90323 AUC= 0.89552 Recall= 0.87324 Specificity= 0.91781
          Split: 4 Accuracy= 0.95853 AUC= 0.96194 Recall= 0.97183 Specificity= 0.95205
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Split: 5 Accuracy= 0.85714 AUC= 0.82148 Recall= 0.71831 Specificity= 0.92466
Split: 6 Accuracy= 0.88018 AUC= 0.84946 Recall= 0.76056 Specificity= 0.93836
Split: 7 Accuracy= 0.91705 AUC= 0.89495 Recall= 0.83099 Specificity= 0.9589
Split: 8 Accuracy= 0.89401 AUC= 0.86335 Recall= 0.77465 Specificity= 0.95205
Split: 9 Accuracy= 0.80645 AUC= 0.72231 Recall= 0.47887 Specificity= 0.96575

Average Accuracy over 10 splits: 0.88445863104046 Average AUC over 10 splits: 0.8569576296657964 Average Recall over 10 splits: 0.7774647887323944

Average Specificity over 10 splits: 0.9364504705991985

In []: