

Introduction to Program Synthesis (WS 2024/25)

Chapter 1 - Introduction

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Why program synthesis? Some major software bug issues...

- 1962 • Mariner 1 Spacecraft → incorrect guidance signals → \$320 million
- 1994 • Pentium FDIV Bug → → lookup table bug → \$475 million
- 1996 • ESA Ariane 5 Flight V88 → conversion error → \$370 million
- 2019 • Boeing 737 Max → MCAS software bug → fatalities
- 2024 • Intel Raptor Lake → stability issues
- 2024 • CrowdStrike Falcon software update → world-wide outage

General Idea

- ▶ Software development process → can be automated (to some extend)
- ▶ Synthesis of **correct** and **efficient** computer programs with respect to predefined specifications
- ▶ Universal approach → not limited to a specific programming language, paradigm or level

Definition and Problem Statement

Definition (Program Synthesis)

Automated discovery of executable programs that match predefined forms of constraints such as input-output relations.

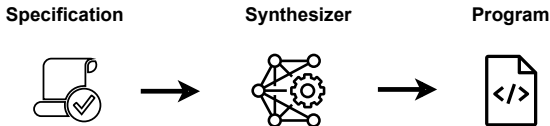
Fundamental Notations

Table: Notation

Symbol	Definition
\mathcal{P}	Program
\mathcal{X}	Set of inputs
\mathcal{Y}	Set of outputs
Φ	Constraints
ψ	Specification

Program Synthesis

- ▶ Generation of computer programs from a collection of **artifacts**
 - ▶ **Automated search** in a space of possible programs
 - ▶ Matching **semantic** and **syntactic requirements**
- ▶ Interaction between **synthesis** and **machine learning**

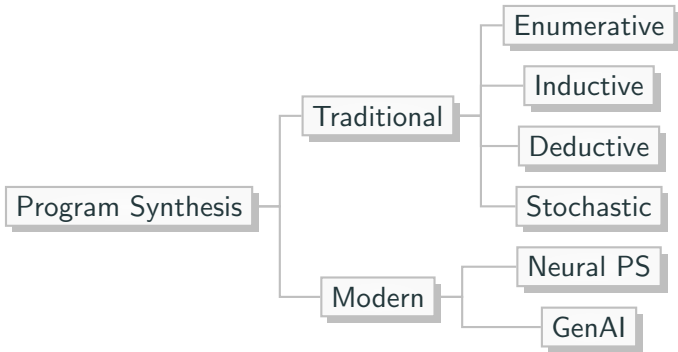


General Definition and Problem Statement

Definition (Program Statement)

Seek a program P that satisfies a specification ψ on a input set \mathcal{X} and is subject to constraints Φ .

Taxonomy (excerpt)



Further Classification

- ▶ PS search methods are often performed directly on **high-level symbolic representations** of problems
 - ▶ Discovery of human-readable solutions
- ▶ Modern PS methodology → based on ML paradigms
- ▶ PS can be therefore nowadays considered as **symbolic AI/ML** methodology.

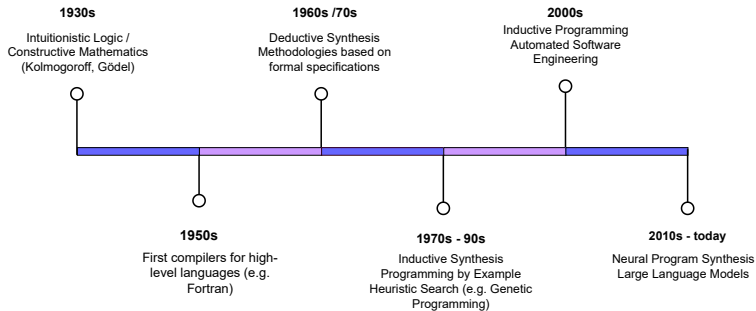
Scope and Distinction

- ▶ Synthesis of programs from a collection of given artifacts
 - ▶ **Artifacts** → represent semantic and syntactic requirements (for the programs)
- ▶ Program synthesis by its definition is not (merely):
 - ▶ **Compilation** → Thus, compilation and synthesis are very closely related as they share the similar goals
 - ▶ **Machine learning** → Incremental and transformative synthesis process that is nowadays *backed and guided* by ML concepts and techniques
 - ▶ **Optimization** → Definition of optimization objectives for the synthesis process

Historical Background

- 1932 • Discovery of algorithms with proofs (Kolmogorov, 1932) [Kol32]
- 1954 • FORTRAN Automatic Coding System (Backus et al., 1954) [Bac+57]
- 1957 • Applications of recursive arithmetic to the problem of circuit synthesis (Alonzo Church) [Fri63]
- 1969 • Solving Sequential Conditions by Finite State Strategies (Buchi and Landweber) [BL90]
- 1971 • Toward automatic program synthesis (Mannar et al., 1971) [MW71]
- 1975 • Transformational synthesis (Manna & Waldinger, 1975) [Kol32]
- 1977 • *Synthesis-by-transformations* paradigm (Burstall & Darlington, 1977) [BD77]
- 1979-80 • Automated Deduction (Manna & Waldinger, 1979; Manna & Waldinger, 1980; Bibel, 1980) [MW79; MW80; Bib80]
- 1980s • Efficient strategies for synthesis (generate & test, divide & conquer, problem reduction) (Smith, 1985b; Smith, 1987b) [Smi83; Smi86]
- 1985 • Adaptive Generation of Simple Sequential Programs (Michael L. Cramer) [Cra85]
- 1989 • Hierarchical Genetic Algorithms Operating on Populations of Computer Programs (John R. Koza) [Koz89]
- 1992 • Genetic Programming (John R. Koza) [Koz93]

Timeline



Paradigms

- ▶ **Proofs-as-programs:**
 - ▶ Synthesis of an algorithm \rightarrow constructive proof of the statement
- ▶ **Synthesis by transformations:**
 - ▶ Derivation of programs from given specifications by forward propagation
 - ▶ Originally based on rewrite rules that encode logical laws

Paradigms

- ▶ **Deductive**

- ▶ Clean and simple version being transformed to a specified version that matches the specification

- ▶ **Inductive**

- ▶ Incremental synthesis based on given examples (i.e. input-output mappings)

- ▶ **Stochastic** → Applying principles of randomized search heuristics

- ▶ **Neural** → Use of deep learning based methodologies

Search spaces

- ▶ **Symbolic:** Compositions from a finite set of functions \mathcal{F} and set of finite terminals (e.g. variables or constants) \mathcal{T}
 - ▶ $\mathcal{P} \in \mathcal{F} \times \mathcal{T}$
 - ▶ Often represented as non-linear data structures such as trees and graphs
- ▶ **Syntactical:** Compositions from nonterminal symbols \mathcal{N} and terminal symbols \mathcal{T} in accordance to production rules \mathcal{P}
 - ▶ Syntax space is language specific
 - ▶ Terminal symbols \rightarrow
 - ▶ Nonterminal symbols \rightarrow
- ▶ **Semantic:** Discrete or continuous output space of candidate programs
 - ▶ $\mathcal{P}(\mathcal{X}) \in \mathbb{R}^n$ or \mathbb{N}^n

Objectives

- ▶ **Feasibility:** Discovery whether a feasible program can be obtained that matches the predefined specification
 - ▶ Usually no constraints specified
 - ▶ No prior knowledge given → *Synthesis from scratch*
- ▶ **Efficiency:** Consideration of optimization objectives to obtain a more efficient solution
 - ▶ Minimization of runtime and/or complexity
- ▶ **Reliability:** Construction of robust programs that guarantee the predefined specification

Challenges

- ▶ Search in symbolic and syntax space is often **ill-conditioned**:
 - ▶ Large search spaces
 - ▶ Roughness of the cost function landscape
 - ▶ No gradient descent → gradient-free methods needed
 - ▶ Poor local search features
- ▶ **Fragility** of syntactical compositions
- ▶ Programming requires **formal reasoning**

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