Multidimensional data fitting tool in Python

Python package for linear and non-linear fitting of multidimensional data.

PySurfaceFit was initially planned as a narrow-scope tool for fitting the molecular potential energy surface (PES) models to the ab initio data computed via quantum chemistry methods. Currently, PySurfaceFit is a flexible general-purpose least squares fitting tool supporting a number of global and local optimization methods.

PySurfaceFit supports fit constraints and Tikhonov regularization for the data points and models parameters. For the Sympy models, based on the Sympy symbolic math library, is is possible to use analytic Jacobians and Hessians if required by the particular optimization method.

Currently, PySurfaceFit heavily relies on the Scipy optimization and root finding library (scipy.optimize).

The basic supported local optimization methods:

- 1. Levenberg-Marquardt
- 2. Trust Region Reflective
- 3. Nelder-Mead
- 4. Powell
- 5. CG (Conjugate Gradient)
- 6. Newton-CG
- 7. Broyden-Fletcher-Goldfarb-Shanno (BFGS)
- 8. L-BFGS-B

The basic supported global optimization methods:

- 1. Simulated Annealing
- 2. Basin Hopping Optimization

Other custom optimization method backends are fairly easy to implement (see the Notebook tutorials on the optimization methods integration).

Installation

Pulling from Github

- git clone https://github.com/RomanKochanov/pysurfacefit.git
- 2. cd pysurfacefit
- 3. pip install.

From Python Package index

pip install pysurfacefit

PySurfaceFit CLI tool

PySurfaceFit provides two options of usage: as a CLI tool, and as a Python library. The CLI tool provides almost all basic functionality for managing the fit data points, creating fit models, and displaying the results of a fit. For beginners, it is

recommended using the CLI tool to avoid most of the programming fuss.

Once installed, PySurfaceFit can be run from the console:

```
pysurfacefit
```

To obtain initial help, use the --help flag:

```
pysurfacefit --help
```

OUTPUT:

```
usage: pysurfacefit [-h] [--config CONFIG] [--startproject STARTPROJECT]
                    [--template TEMPLATE [TEMPLATE ...]] [--merge MERGE]
                    [--set SET] [--init] [--split] [--fit] [--stat]
                    [--codegen] [--plot [PLOT [PLOT ...]]] [--calc]
Python package for linear and non-linear fitting of multidimensional data.
optional arguments:
  -h, --help
                        show this help message and exit
  --config CONFIG
                        Configuration file (mandatory for all steps except
                        --startproject)
  --startproject STARTPROJECT
                        Stage 1: start empty project, create dummy config
  --template TEMPLATE [TEMPLATE ...]
                                la: us a template for new project
                                 1b: take defaults from a config file
  --merge MERGE
  --set SET
                                 1c: explicitly set project parameters
  --init
                        Stage 2: create model package
                        Stage 3: split initial datafile with weighting scheme
  --split
                        Stage 4: start fitting model to data
  --fit
                        Stage 5: calculate statistics
  --stat
  --codegen
                        Stage 6: generate Fortran code for fitted model
  --plot [PLOT [PLOT ...]]
                        Stage 7: plot sections of the model and compare to
                        data
  --calc
                        Stage 8: calculate model values on grid
```

This will generate an emply project with the sample config file, which will look something like this:

```
# Define rules to split the datafile to dataspec.
# Should be ignored if dataspec is empty.
split column:
split values:
split weights:
# Resulting data specification split-file.
# N.B.: if empty, then the raw datafile is used.
# Data specification *.txt file has the following format:
# alias path wht_mul type include
# ----- -----
# test1 test1.csv 1 0 1
# test2 test2.csv 1 0 1
# test3 test3.csv 1 0 1
dataspec: dataspec.txt
# Names and units of the input data columns.
# Input names must be separated by semicolon
# and should not contain dots.
# E.g.: X;Y;Z for names, X:X UNIT;Y:Y UNIT for units
input columns:
input units:
# Name of the output data column. See explanation above.
output column:
output units:
# Weight function.
wht fun: lambda v: 1
# Global data cutoff
global cutoff max:
global cutoff min:
#####################################
# FITTING MODEL SPECIFICATIONS #
######################################
[MODEL]
# Model package name.
model: fitmodel
# Model arguments. Argument names must be in the same order
# as the data column names from the DATA section.
# E.g.: X;Y;Z
arguments:
####################
# FITTER OPTIONS #
###################
[FIT]
# Weighted / unweighted fit mode.
weighted fit: True
# Use "rubber" regularization.
rubber on: True
```

```
# Fitting method (trf, lm, basinhopping).
# Available "local" methods:
     "trf" -> Trust Region Reflective (least squares, bounded).
     "lm" -> Levenberg Marquardt (least squares, unbounded).
     'Nelder-Mead' -> Gradient-free descent Nelder-Mead method.
#
     'Powell' -> modified Powell algorithm.
#
#
     'CG' -> conjugate gradient algorithm.
#
     'BFGS' -> BFGS algorithm.
#
     'Newton-CG' -> Newton-CG algorithm.
     'L-BFGS-B' -> L-BFGS-B algorithm.
#
#
     'TNC' -> truncated Newton (TNC) algorithm.
#
     'COBYLA' -> Constrained Optimization BY Linear Approximation.
     'SLSQP' -> Sequential Least Squares Programming.
#
     'trust-constr' -> minimize a scalar function subject to constraints.
#
    'dogleg' -> dog-leg trust-region algorithm.
#
     'trust-ncg' -> Newton conjugate gradient trust-region algorithm.
#
#
     'trust-exact' -> "nearly exact trust-region algorithm"
     'trust-krylov' -> "early exact trust-region algorithm"
# Available "global" methods:
     "basinhopping" -> local descents from a random starting point (bounded)
     "anneal" -> Simulated Annealing method
fitting method: trf
# Calculate analytic jacobian (only if ModelSympy is used).
analytic jacobian: True
# Fit options. Must be given as a list separated by semicolon.
# The valid options for most of the supported fitting methods
# can be found in the corresponding scipy.optimize documentation.
fit_options: max nfev=200;
# STATISTICS CALCULATION OPTIONS #
[STAT]
# Fit statistics file.
stat file: stat.out
# Calculate outlier statistics.
outlier stats flag: True
# Type of statistics: cook, dffits, leverage ,student.
outlier stats type: cook
# Output generated symbolic function, for debug purposes only.
output symbolic func:
###############################
# CODE GENERATOR OPTIONS #
####################################
[CODEGEN]
# Create Fortran code.
create fortran: False
# Compare original Python code with the generated Fortran.
```

```
compare fortran: False
# Fortran compiler executable
compiler fortran: ifort
# Grid specifications to calculate on.
# Format of the specification must be as follows:
# X=XMIN:XSTEP:XMAX; Y=YMIN:YSTEP:YMAX; ...
gridspec:
########################
# PLOTTING OPTIONS #
########################
[PLOTTING]
# ATTENTION: names of the plot coordinates correspond to the
# model argumen names given in the MODEL section.
# Type of the plot.
# Available plot modes:
# => "residuals":
            plot unweighted fit residuals.
# => "sections":
            plot sections/cuts of the fitted model vs datapoints.
plot mode: residuals
# Plot coordinate grid specifications.
# Format of the specification must be as follows:
# X=XVAL; Y=YMIN:YSTEP:YMAX; ...
# In case of the fixed coordinate, variable would only have a value, e.g. X=XVAL.
# In case of unfixed coordinate, there should be a full grid, e.g. Y=YMIN:YSTEP:YMAX
# N.B.: 1) order of the unfixed coords affects the order of the plot axes.
        2) order of the binding MUST correspond to the argument of the model's
           func method.
gridspec:
# Model components to plot.
model components:
# Calculate model's components.
calculate components: False
# Plot outlier statistics in color. If False, each datagroup has its own color.
plot outlier stats: False
# Plot weighted residuals.
resids weighted: False
# X axes to plot the resuduals versus.
# If empty, defaults to [DATA][output column].
resids x axes:
# Scatter settings (2D, 3D case)
scatter opacity: 1
marker size: 20
resize by weights: False
# Surface settings (3D case)
```

Now, let's perform a test fitting case step by step. First, let's generate a three-dimensional data we will fit our model to.

After the test data file is generated, we can create an empty project named "test" from it.

```
pysurfacefit --startproject test
```

To generate a ready-to-go configuration file, one must provide additional data such as names for the argument columns (or "inputs"), and the name of the function column (or "output"). The entered names must correspond to the column names in the data file:

```
Enter the name of the data points CSV file: sampledata.csv Enter semicolon-separated names for model inputs: x; y; z Enter name for model output: v
```

If everything went fine, we should have the new fitting project created in a nested subfolder.

```
Created new project: test
New config file has been added: test/config.ini
Sample data specification file has been added: dataspec.txt
```

Now the project folder "test" inlcudes only three files:

```
cd test; ls
config.ini dataspec.txt sampledata.csv
```

The file "config.ini" is the main configuration file containing the project settings (see the example of the file above). This file is separated into the following sections:

1. GENERAL

Basic settings: contains only the name of the project so far.

2. DATA

Settings for the data to fit: defines the source file for the fitted data, names and units of the input and output columns, weight function and cutoff. Also contains settings for data splitting to apply more advanced weighting schemes which are defined in the dataspec.txt file.

3. MODEL

Containes the model name and names for model arguments. Usually, the argument names are the same as the names of the data inputs defined in the DATA section.

4. **FIT**

Settings for the fitter. Containes the switches for turning on/off weights and regularization, name of the optimization method, switch for analytic Jacobian, and number of iterations setting.

5. **STAT**

Additional settings to display the fit statistics.

6. CODEGEN

Settings for the code generation from the fitted model. Allows choosing the compiler. Currently only the Fortan code generation is supported.

7. PLOTTING

Settings for plotting the fit residuals and 1D/2D sections of the fitted model. 3D volume visualization is planned to be included.

8. CALC

Defines the output file and grid to calculate the fited model on.

To fit the data in the sampledata.csv file, let's generate a model file.

```
pysurfacefit --config config.ini --init
```

Note, that for all tasks except --startproject, we must supply the configuration file using the --config key.

The model is created and stored in a separate Python module file. The name of this file is defined in the MODEL section using the "model" parameter.

```
ls
config.ini dataspec.txt fitmodel.py sampledata.csv
```

The default model has just one fitting parameter which is a constant. Here is what a default model file looks like:

```
import os

from pysurfacefit.models.sympy import ModelSympy
from pysurfacefit.fitpars import Par, Parameters

class fitmodel(ModelSympy):
```

```
Test model for fitting data with just one parameter.
    def init (self,calc switch='numbified'):
        self.__check_symbolic__ = False
        self.__calc_switch__ = calc_switch # symbolic, lambdified, numbified
        self. components = \{\}
        # Initialize empty parameters.
        self. params = Parameters()
        # Add constant parameter.
        self.__params__.append(group='constant', pars=[
            Par(name='constant', value=0.0, flag=True),
        ])
    def units (self):
        return {"input": {}, "output": "None"}
        def func (self,params,x,y,z):
        # constant
        constant = params['constant'].get value()
        # final result
        res = constant
        # components
        self. components ['constant'] = constant
        return res
model = fitmodel()
if os.path.exists('fitmodel.csv'):
    model.load params('fitmodel.csv')
else:
    model.save params('fitmodel.csv')
```

So far, we will use this default constant model to fit the three-dimensional data we have generated earlier. To do that, use the "fit" command:

```
pysurfacefit --config config.ini --fit
```

This will start the fitting process and will print the intermediate fit statistics to the STDOUT:

- creating sympy objects for parameters
- get the Sympy expression by calling function with the Sympy objects
- create lambdified Python function from sympy expression
- create compiled (numbified) code from the lambdified function

CALC FUN 1>>> DIST:0.000000000e+00 SSE_RUB:0.000000000e+00 SSE_TOT:5.324527156e+14 ==> WEIGHTED_FIT =====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.325e+14 UNWHT_SSE: 5.325e+14 WHT SD: 2.580e+05 UNWHT SD: 2.580e+05

<<< calling __sympy_initialize_jac__ >>>>

Progress:

- get the Sympy expression by calling function with the Sympy objects
- create lambdified Python function from sympy expression
- create compiled (numbified) code from the lambdified function

CALC JAC 1>>> DIST:0.000000000e+00

CALC FUN 2>>> DIST:1.0000000000e+00 SSE_RUB:0.000000000e+00 SSE_TOT:5.324502669e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.325e+14 UNWHT_SSE:

5.325e+14 WHT_SD: 2.580e+05 UNWHT_SD: 2.580e+05

CALC JAC 2>>> DIST:1.000000000e+00

CALC FUN 3>>> DIST:3.000000000e+00 SSE_RUB:0.000000000e+00 SSE_TOT:5.324453696e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.324e+14 UNWHT_SSE:

5.324e+14 WHT_SD: 2.580e+05 UNWHT_SD: 2.580e+05

CALC JAC 3>>> DIST:3.000000000e+00

CALC FUN 4>>> DIST:7.000000000e+00 SSE_RUB:0.000000000e+00 SSE_TOT:5.324355753e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.324e+14 UNWHT_SSE:

5.324e+14 WHT_SD: 2.580e+05 UNWHT_SD: 2.580e+05

CALC JAC 4>>> DIST:7.000000000e+00

CALC FUN 5>>> DIST:1.500000000e+01 SSE_RUB:0.000000000e+00 SSE_TOT:5.324159873e+14 ==> WEIGHTED_FIT

=====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.324e+14 UNWHT_SSE:

5.324e+14 WHT_SD: 2.580e+05 UNWHT_SD: 2.580e+05

CALC JAC 5>>> DIST:1.500000000e+01

CALC FUN 6>>> DIST:3.100000000e+01 SSE_RUB:0.000000000e+00 SSE_TOT:5.323768145e+14 ==> WEIGHTED_FIT

=====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.324e+14 UNWHT_SSE:

5.324e+14 WHT_SD: 2.580e+05 UNWHT_SD: 2.580e+05

CALC JAC 6>>> DIST:3.100000000e+01

CALC FUN 7>>> DIST:6.300000000e+01 SSE_RUB:0.000000000e+00 SSE_TOT:5.322984811e+14 ==> WEIGHTED_FIT

=====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.323e+14 UNWHT_SSE:

5.323e+14 WHT_SD: 2.579e+05 UNWHT_SD: 2.579e+05

CALC JAC 7>>> DIST:6.300000000e+01

```
CALC FUN
           8>>> DIST:1.270000000e+02 SSE_RUB:0.000000000e+00 SSE_TOT:5.321418635e+14 ==> WEIGHTED_FIT
====data group statistics=====
                sampledata: N: 8000 MIN WHT: 1.0e+00 MAX WHT: 1.0e+00 WHT SSE: 5.321e+14 UNWHT SSE:
5.321e+14 WHT_SD: 2.579e+05 UNWHT_SD: 2.579e+05
_____
CALC JAC 8>>> DIST:1.270000000e+02
CALC FUN 9>>> DIST:2.550000000e+02 SSE_RUB:0.000000000e+00 SSE_TOT:5.318288249e+14 ==> WEIGHTED_FIT
====data group statistics====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.318e+14 UNWHT_SSE:
5.318e+14 WHT SD: 2.578e+05 UNWHT SD: 2.578e+05
_____
CALC JAC 9>>> DIST:2.550000000e+02
CALC FUN 10>>> DIST:5.110000000e+02 SSE_RUB:0.000000000e+00 SSE_TOT:5.312035342e+14 ==> WEIGHTED_FIT
====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.312e+14 UNWHT_SSE:
5.312e+14 WHT SD: 2.577e+05 UNWHT SD: 2.577e+05
_____
CALC JAC 10>>> DIST:5.110000000e+02
CALC FUN 11>>> DIST:1.023000000e+03 SSE RUB:0.000000000e+00 SSE TOT:5.299560985e+14 ==> WEIGHTED FIT
====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.300e+14 UNWHT SSE:
5.300e+14 WHT_SD: 2.574e+05 UNWHT_SD: 2.574e+05
_____
CALC JAC 11>>> DIST:1.023000000e+03
CALC FUN 12>>> DIST:2.047000000e+03 SSE_RUB:0.000000000e+00 SSE_TOT:5.274738099e+14 ==> WEIGHTED_FIT
====data group statistics=====
                 sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.275e+14 UNWHT_SSE:
5.275e+14 WHT SD: 2.568e+05 UNWHT SD: 2.568e+05
_____
CALC JAC 12>>> DIST:2.047000000e+03
CALC FUN 13>>> DIST:4.095000000e+03 SSE_RUB:0.000000000e+00 SSE_TOT:5.225595644e+14 ==> WEIGHTED_FIT
=====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.226e+14 UNWHT_SSE:
5.226e+14 WHT SD: 2.556e+05 UNWHT SD: 2.556e+05
CALC JAC 13>>> DIST:4.095000000e+03
CALC FUN 14>>> DIST:8.191000000e+03 SSE RUB:0.000000000e+00 SSE TOT:5.129324001e+14 ==> WEIGHTED FIT
====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.129e+14 UNWHT_SSE:
5.129e+14 WHT_SD: 2.532e+05 UNWHT_SD: 2.532e+05
_____
CALC JAC 14>>> DIST:8.191000000e+03
CALC FUN 15>>> DIST:1.638300000e+04 SSE_RUB:0.0000000000e+00 SSE_TOT:4.944833778e+14 ==> WEIGHTED_FIT
====data group statistics=====
                sampledata: N: 8000 MIN WHT: 1.0e+00 MAX WHT: 1.0e+00 WHT SSE: 4.945e+14 UNWHT SSE:
4.945e+14 WHT SD: 2.486e+05 UNWHT SD: 2.486e+05
_____
CALC JAC 15>>> DIST:1.638300000e+04
CALC FUN 16>>> DIST:3.276700000e+04 SSE_RUB:0.000000000e+00 SSE_TOT:4.608065586e+14 ==> WEIGHTED_FIT
=====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 4.608e+14 UNWHT_SSE:
4.608e+14 WHT_SD: 2.400e+05 UNWHT_SD: 2.400e+05
_____
CALC JAC 16>>> DIST:3.276700000e+04
CALC FUN 17>>> DIST:6.553500000e+04 SSE_RUB:0.000000000e+00 SSE_TOT:4.063378221e+14 ==> WEIGHTED_FIT
====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 4.063e+14 UNWHT_SSE:
4.063e+14 WHT_SD: 2.254e+05 UNWHT_SD: 2.254e+05
```

```
_____
CALC JAC
         17>>> DIST:6.553500000e+04
CALC FUN 18>>> DIST:1.310710000e+05 SSE RUB:0.000000000e+00 SSE TOT:3.489399568e+14 ==> WEIGHTED FIT
====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 3.489e+14 UNWHT_SSE:
3.489e+14 WHT_SD: 2.088e+05 UNWHT_SD: 2.088e+05
_____
CALC JAC 18>>> DIST:1.310710000e+05
CALC FUN 19>>> DIST:1.530418700e+05 SSE_RUB:0.0000000000e+00 SSE_TOT:3.450782038e+14 ==> WEIGHTED_FIT
====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 3.451e+14 UNWHT_SSE:
3.451e+14 WHT_SD: 2.077e+05 UNWHT_SD: 2.077e+05
_____
CALC JAC 19>>> DIST:1.530418700e+05
CALC FUN 20>>> DIST:1.530418700e+05 SSE_RUB:0.000000000e+00 SSE_TOT:3.450782038e+14 ==> WEIGHTED_FIT
====data group statistics=====
                sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 3.451e+14 UNWHT_SSE:
3.451e+14 WHT_SD: 2.077e+05 UNWHT_SD: 2.077e+05
_____
FND FTT
9.095534 seconds elapsed, 20 func evals, 19 jac evals
```

As it can be seen from the fit, the result is not good since the generated data is not described by a constaint value. To improve the accuracy of the fit, let's change the code contained in the fitmodel.py by adding the three-dimensional polynomial:

```
import os
from functools import reduce
from pysurfacefit.models.sympy import ModelSympy
from pysurfacefit.fitpars import Par, Parameters
from pysurfacefit.models.library import generate powers layer 3d, poly3d
class fitmodel(ModelSympy):
   Test model for fitting data with just one parameter.
   def init (self, calc switch='numbified'):
       self. check symbolic = False
        self.__calc_switch__ = calc_switch # symbolic, lambdified, numbified
        self.__components__ = {}
       # Initialize empty parameters.
        self.__params__ = Parameters()
       # Add polynomial parameters
        self. powers = reduce(lambda a,b:a+b,
            [generate powers layer 3d(n) for n in range(1,4)]
        )
        for i,j,k in self.__powers__:
            self. params .append(group='poly', pars=[
                Par(name='poly %d %d %d'%(i,j,k), value=0.0, flag=True),
            ])
       # Add constant parameter.
```

```
self. params .append(group='constant', pars=[
               Par(name='constant', value=0.0, flag=True),
           ])
           def units (self):
           return {"input": {}, "output": "None"}
       def func (self,params,x,y,z):
           # polynomial
           p = params.get values(group='poly')
           poly = poly3d(p,x,y,z,self. powers)
           # constant
           constant = params['constant'].get value()
           # final result
           res = poly + constant
           # components
           self. components ['constant'] = constant
           return res
   model = fitmodel()
   if os.path.exists('fitmodel.csv'):
       model.load params('fitmodel.csv')
   else:
       model.save params('fitmodel.csv')
Let's run the fit again with more advanced model:
   pysurfacefit --config config.ini --fit
```

This will start the fitting process and will print the intermediate fit statistics to the STDOUT:

```
Treating sampledata fitgroup as FitPoints
BEGIN FIT
USING SCIPY.OPTIMIZE.LEAST_SQUARES: METHOD= trf
\label{eq:method_options: problem} \textbf{METHOD_OPTIONS: } \{ \text{'max\_nfev': 200, 'bounds': [(-inf, -inf, 
inf, inf, inf, inf, inf, inf, inf)], 'jac': <function Fitter.fit_least_squares.<locals>.<lambda> at 0x7f5def410560>}
<c<< calling __sympy_initialize_func__ >>>>
_____
Progress:
               - creating sympy objects for inputs
               - creating sympy objects for parameters
               - get the Sympy expression by calling function with the Sympy objects
               - create lambdified Python function from sympy expression
               - create compiled (numbified) code from the lambdified function
                                                                                                                                                                                                                                                                                  ==> WEIGHTED FIT
CALC FUN
                                      1>>> DIST:0.000000000e+00 SSE RUB:0.000000000e+00 SSE TOT:5.324527156e+14
```

Progress:

- get the Sympy expression by calling function with the Sympy objects
- create lambdified Python function from sympy expression
- create compiled (numbified) code from the lambdified function

CALC JAC 1>>> DIST:0.000000000e+00

CALC FUN 2>>> DIST:1.0000000000e+00 SSE_RUB:0.0000000000e+00 SSE_TOT:5.223291702e+14 ==> WEIGHTED_FIT =====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.223e+14 UNWHT_SSE:

5.223e+14 WHT_SD: 2.555e+05 UNWHT_SD: 2.555e+05

CALC JAC 2>>> DIST:1.000000000e+00

CALC FUN 3>>> DIST:2.999995352e+00 SSE_RUB:0.0000000000e+00 SSE_TOT:5.024183860e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.024e+14 UNWHT_SSE:

5.024e+14 WHT_SD: 2.506e+05 UNWHT_SD: 2.506e+05

CALC JAC 3>>> DIST:2.999995352e+00

CALC FUN 4>>> DIST:6.999923483e+00 SSE_RUB:0.000000000e+00 SSE_TOT:4.639397348e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 4.639e+14 UNWHT_SSE:

4.639e+14 WHT_SD: 2.408e+05 UNWHT_SD: 2.408e+05

CALC JAC 4>>> DIST:6.999923483e+00

CALC FUN 5>>> DIST:1.499903800e+01 SSE_RUB:0.000000000e+00 SSE_TOT:3.923332008e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 3.923e+14 UNWHT_SSE:

3.923e+14 WHT_SD: 2.215e+05 UNWHT_SD: 2.215e+05

CALC JAC 5>>> DIST:1.499903800e+01

CALC FUN 6>>> DIST:3.098657439e+01 SSE_RUB:0.000000000e+00 SSE_TOT:2.703038473e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 2.703e+14 UNWHT_SSE:

2.703e+14 WHT_SD: 1.838e+05 UNWHT_SD: 1.838e+05

CALC JAC 6>>> DIST:3.098657439e+01

CALC FUN 7>>> DIST:6.266232927e+01 SSE_RUB:0.000000000e+00 SSE_TOT:1.075696361e+14 ==> WEIGHTED_FIT

====data group statistics=====

sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 1.076e+14 UNWHT_SSE:

1.076e+14 WHT_SD: 1.160e+05 UNWHT_SD: 1.160e+05

CALC JAC 7>>> DIST:6.266232927e+01

CALC FUN 8>>> DIST:1.160883053e+02 SSE_RUB:0.000000000e+00 SSE_TOT:1.093359850e+13 ==> WEIGHTED_FIT

=====data group statistics=====

sampledata: N: 8000 MIN WHT: 1.0e+00 MAX WHT: 1.0e+00 WHT SSE: 1.093e+13 UNWHT SSE:

1.093e+13 WHT_SD: 3.697e+04 UNWHT_SD: 3.697e+04

CALC JAC 8>>> DIST:1.160883053e+02

CALC FUN 9>>> DIST:1.900605403e+02 SSE_RUB:0.000000000e+00 SSE_TOT:2.602526806e+12 ==> WEIGHTED_FIT

====data group statistics===== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 2.603e+12 UNWHT_SSE: 2.603e+12 WHT SD: 1.804e+04 UNWHT SD: 1.804e+04 _____ 9>>> DIST:1.900605403e+02 CALC JAC CALC FUN 10>>> DIST:3.975523481e+02 SSE_RUB:0.000000000e+00 SSE_TOT:1.507914353e+12 ==> WEIGHTED_FIT ====data group statistics===== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 1.508e+12 UNWHT_SSE: 1.508e+12 WHT_SD: 1.373e+04 UNWHT_SD: 1.373e+04 _____ 10>>> DIST:3.975523481e+02 CALC JAC CALC FUN 11>>> DIST:8.545961426e+02 SSE RUB:0.000000000e+00 SSE TOT:5.250210120e+11 ==> WEIGHTED FIT =====data group statistics===== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 5.250e+11 UNWHT_SSE: 5.250e+11 WHT_SD: 8.101e+03 UNWHT_SD: 8.101e+03 _____ CALC JAC 11>>> DIST:8.545961426e+02 CALC FUN 12>>> DIST:1.639588009e+03 SSE_RUB:0.000000000e+00 SSE_TOT:1.170270161e+11 ==> WEIGHTED_FIT ====data group statistics===== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 1.170e+11 UNWHT_SSE: 1.170e+11 WHT_SD: 3.825e+03 UNWHT_SD: 3.825e+03 _____ CALC JAC 12>>> DIST:1.639588009e+03 CALC FUN 13>>> DIST:3.039288277e+03 SSE_RUB:0.000000000e+00 SSE_TOT:3.211110377e+10 ==> WEIGHTED_FIT ====data group statistics===== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 3.211e+10 UNWHT_SSE: 3.211e+10 WHT_SD: 2.003e+03 UNWHT_SD: 2.003e+03 _____ CALC JAC 13>>> DIST:3.039288277e+03 CALC FUN 14>>> DIST:6.369248010e+03 SSE_RUB:0.000000000e+00 SSE_TOT:2.288170913e+09 ==> WEIGHTED_FIT =====data group statistics===== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 2.288e+09 UNWHT_SSE: 2.288e+09 WHT_SD: 5.348e+02 UNWHT_SD: 5.348e+02 _____ CALC JAC 14>>> DIST:6.369248010e+03 CALC FUN 15>>> DIST:7.993910245e+03 SSE RUB:0.000000000e+00 SSE TOT:9.174559605e-16 ==> WEIGHTED FIT =====data group statistics===== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 9.175e-16 UNWHT_SSE: 9.175e-16 WHT_SD: 3.386e-10 UNWHT_SD: 3.386e-10 _____ CALC JAC 15>>> DIST:7.993910245e+03 CALC FUN 16>>> DIST:7.993910245e+03 SSE_RUB:0.000000000e+00 SSE_TOT:1.549934571e-17 ==> WEIGHTED_FIT ====data group statistics==== sampledata: N: 8000 MIN_WHT: 1.0e+00 MAX_WHT: 1.0e+00 WHT_SSE: 1.550e-17 UNWHT_SSE:

1.550e-17 WHT SD: 4.402e-11 UNWHT SD: 4.402e-11

CALC JAC 16>>> DIST:7.993910245e+03

END FIT

11.802427 seconds elapsed, 16 func evals, 16 jac evals

/home/roman/work/python/PyDev/PySurfaceFit/git-repo/pysurfacefit-master/showcase/test jeanny, Ver.3.0

| # | group | names | values | bounds | weights | flags |
|---|-------|------------|--------------|-------------|---------|-------|
| | | | | | | |
| 0 | poly | poly_0_0_1 | 7500 | (-inf, inf) | 0 | 1 |
| 1 | poly | poly_0_1_0 | -2.92517e-11 | (-inf, inf) | 0 | 1 |
| 2 | poly | poly_1_0_0 | 1.48667e-12 | (-inf, inf) | 0 | 1 |
| 3 | poly | poly 0 0 2 | -2750 | (-inf, inf) | 0 | 1 |

| 4 | poly | poly_0_1_1 | -3.5252e-13 | (-inf, | inf) | 0 | 1 |
|----|----------|------------|--------------|--------|------|---|---|
| 5 | poly | poly_0_2_0 | -3.17951e-12 | (-inf, | inf) | 0 | 1 |
| 6 | poly | poly_1_0_1 | -1.55127e-13 | (-inf, | inf) | 0 | 1 |
| 7 | poly | poly_1_1_0 | 2.3229e-13 | (-inf, | inf) | 0 | 1 |
| 8 | poly | poly_2_0_0 | 1 | (-inf, | inf) | 0 | 1 |
| 9 | poly | poly_0_0_3 | 300 | (-inf, | inf) | 0 | 1 |
| 10 | poly | poly_0_1_2 | 7.33912e-15 | (-inf, | inf) | 0 | 1 |
| 11 | poly | poly_0_2_1 | -1.30851e-14 | (-inf, | inf) | 0 | 1 |
| 12 | poly | poly_0_3_0 | 0.1 | (-inf, | inf) | 0 | 1 |
| 13 | poly | poly_1_0_2 | 3.78018e-14 | (-inf, | inf) | 0 | 1 |
| 14 | poly | poly_1_1_1 | 1.25425e-14 | (-inf, | inf) | 0 | 1 |
| 15 | poly | poly_1_2_0 | 1.44824e-14 | (-inf, | inf) | 0 | 1 |
| 16 | poly | poly_2_0_1 | 4.30556e-14 | (-inf, | inf) | 0 | 1 |
| 17 | poly | poly_2_1_0 | -1.16635e-14 | (-inf, | inf) | 0 | 1 |
| 18 | poly | poly_3_0_0 | -1.22386e-14 | (-inf, | inf) | 0 | 1 |
| 19 | constant | constant | 10 | (-inf, | inf) | 0 | 1 |

The code above lists the fitted parameters for the updated model.