## Math 215

Please box your answers for each of the exercises below. Also, be mindful of your presentation, I will deduct 10 points for disorganized or unintelligible answers.

## Exercises

- 1) Let  $y_1 = 6$ , and  $\forall n \in \mathbb{N}, \ y_{n+1} := \frac{2y_n 6}{3}$ .
  - Use induction to prove that  $\forall n \in \mathbb{N}, y_n > -6$ .
  - Use another induction argument to show that  $\forall n \in \mathbb{N}, y_{n+1} \leq y_n$ .
- 2) Give an example of each or state that the request is impossible:
  - $f: \mathbb{N} \to \mathbb{N}$  that is 1-1 but not onto.
  - $f: \mathbb{N} \to \mathbb{N}$  that is onto but not 1-1.
  - $f: \mathbb{N} \to \mathbb{Z}$  that is 1-1 and onto.
- 3) Section 2.1: Problem 8.
- 4) Section 2.1: Problem 9.
- 5) Section 2.1: Problem 20.
- 6) Section 2.1: Problem 22.
- 7) Section 2.2: Problem 3.
- 8) Section 2.2: Problem 4.
- 9) Section 2.2: Problem 5.
- 10) Section 2.2: Problem 11.