Homework 8 Question 4

Let S = R, A = $\{x: x \in S \text{ and } 0 < x < 4\}$, B = $\{x: x \in S \text{ and } 1 < x \leq 3\}$, and C = $\{x: x \in S \text{ and } 2 < x \leq 5\}$ What are the sets:

$1 \quad A \cup B \cup C$

$$A \cup B \cup C = \{x: \ x \ \epsilon \ S \ and \ 0 < x < 4\} \cup \{x: \ x \ \epsilon \ S \ and \ 1 < x \le 3\} \cup \{x: \ x \ \epsilon \ S \ and \ 2 < x \le 5\} \\ = \{x: \ x \ \epsilon \ S \ and \ 0 < x \le 5\}$$

$2 A \cap B \cap C$

$$A \cap B \cap C = \{x: \ x \ \epsilon \ S \ and \ 0 < x < 4\} \cap \{x: \ x \ \epsilon \ S \ and \ 1 < x \le 3\} \cap \{x: \ x \ \epsilon \ S \ and \ 2 < x \le 5\} = \{x: \ x \ \epsilon \ S \ and \ 2 < x \le 3\}$$