

1 Math 215 Homework 5 Question 3

Evaluate as an infinite series

$$\int \frac{e^x}{x} dx \quad (1)$$

using a Taylor Expansion on e^x :

$$\int \frac{1}{x} \left(1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} \dots \right) dx \quad (2)$$

$$= \int \left(\frac{1}{x} + 1 + \frac{x}{2!} + \frac{x^2}{3!} + \frac{x^3}{4!} \dots \right) dx \quad (3)$$

$$= \int \frac{1}{x} dx + \int dx + \int \frac{x}{2!} dx + \int \frac{x^2}{3!} dx + \int \frac{x^3}{4!} dx \dots \quad (4)$$

$$= C + \ln|x| + \frac{x^2}{2 \cdot 2!} + \frac{x^3}{3 \cdot 3!} + \frac{x^4}{4 \cdot 4!} \dots \quad (5)$$

$$= C + \ln|x| + \sum \frac{x^n}{n!} \quad (6)$$

Q.E.D