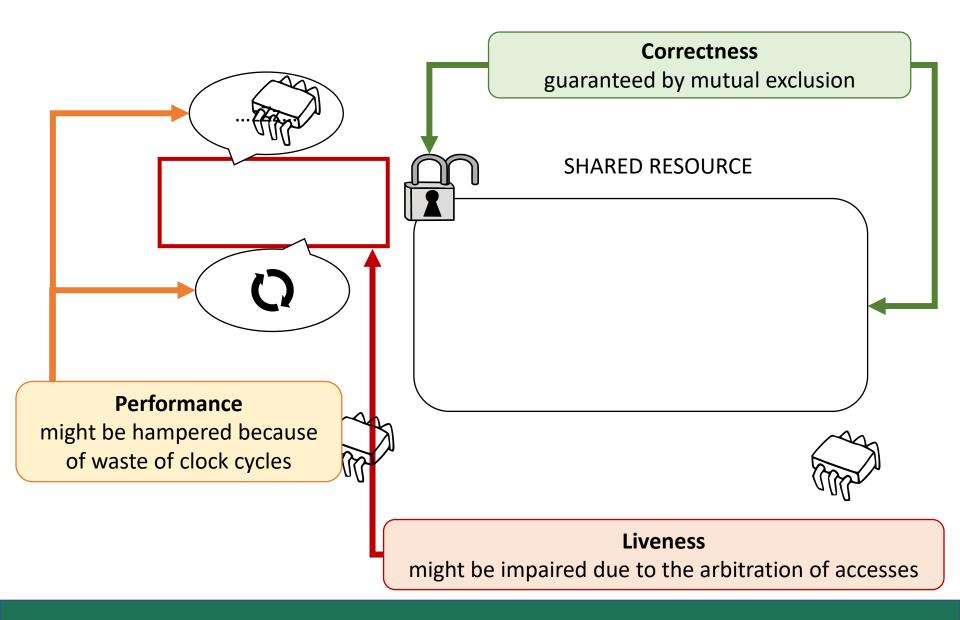
#### Programmazione concorrente

Laurea Magistrale in Ingegneria Informatica Università Tor Vergata Docente: Romolo Marotta

# **Properties of Concurrent Programs**

- 1. Speed up
- 2. Correctness
- 3. Progress

## On concurrent programming



Properties

#### What do we want from parallel programs?

- Safety: nothing wrong happens (Correctness)
  - parallel versions of our programs should be correct as their sequential implementations
- Liveliness: something good happens eventually (Progress)
  - if a sequential program terminates with a given input, we want that its parallel alternative also completes with the same input

#### Performance

we want to exploit our parallel hardware

Properties

# A bit of terminology

- Hardware
  - Processor
  - CPU
  - CPU-Core
  - Logical Core
  - Hardware thread
- Software
  - Process
  - Thread
  - Fiber
  - Task

- Programs
  - Sequential
  - Concurrent
  - Parallel
  - Distrubuted
- Memory
  - Shared
  - Distributed

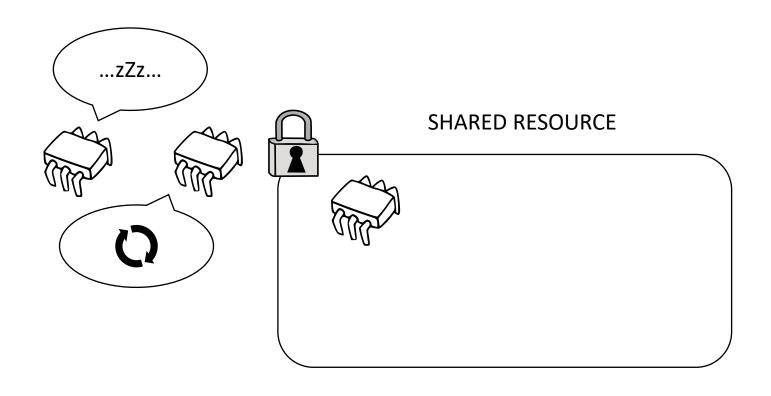
# The system model

- Threads (aka processes)
- Cores (aka cpus)
- Shared memory
- Arbitrary long asynchronous delays
- Scheduler
  - A system component that decides which/when a thread runs on a given core

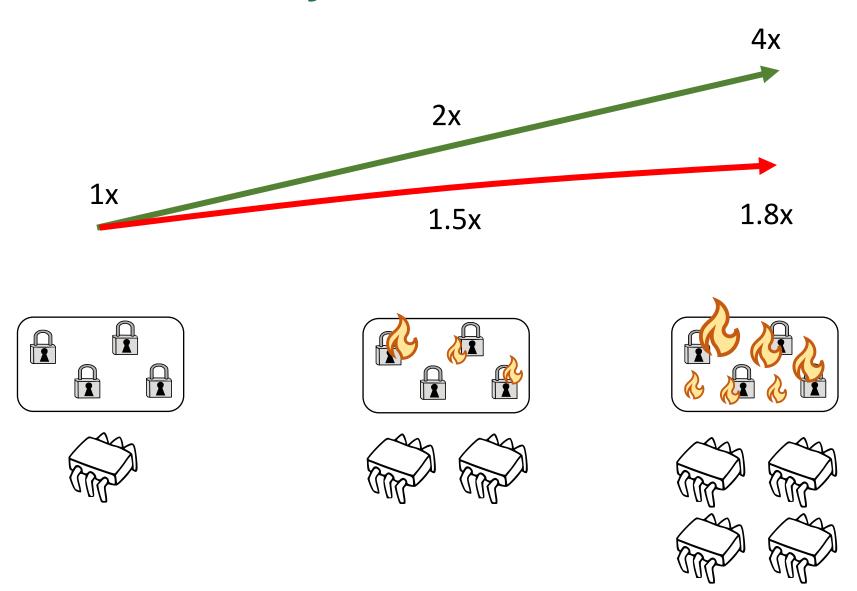
Properties

# Speed up Correctness conditions Progress conditions

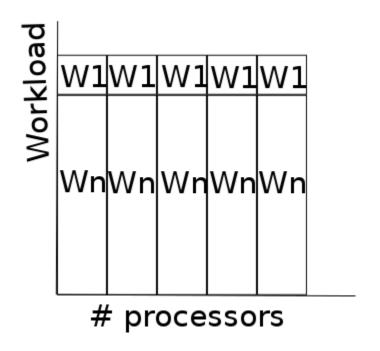
#### The cost of synchronization

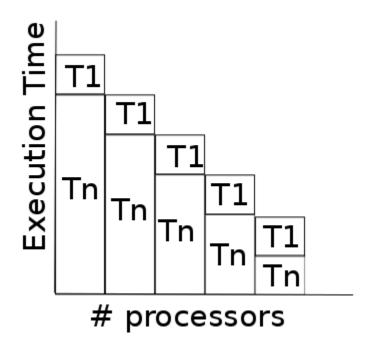


#### The cost of synchronization



# Amdahl Law - Fixed-size Model (1967)





#### Amdahl Law - Fixed-size Model (1967)

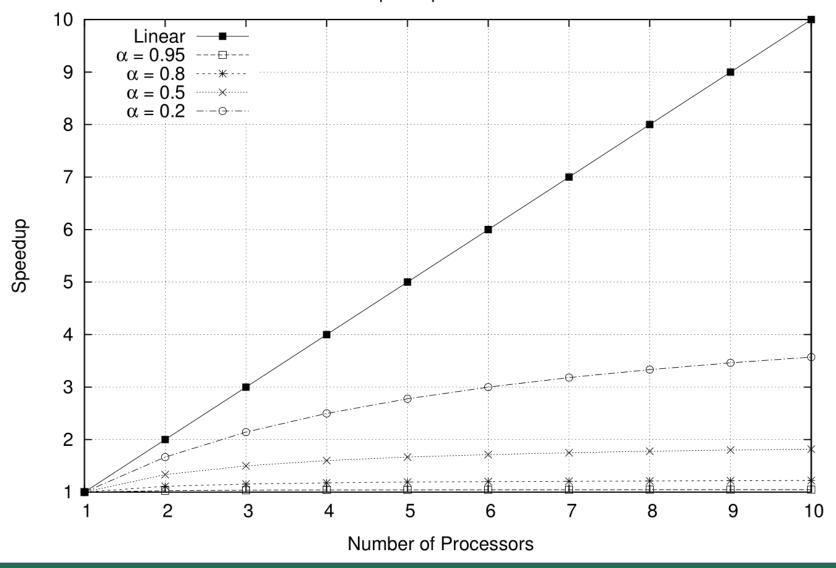
 The workload is fixed: it studies how the behavior of the same program varies when adding more computing power

$$S_{Amdahl} = \frac{T_S}{T_p} = \frac{T_S}{\alpha T_S + (1 - \alpha)\frac{T_S}{p}} = \frac{1}{\alpha + \frac{(1 - \alpha)}{p}}$$

- where:
  - $\alpha \in [0,1]$ : Serial fraction of the program
  - $p \in N$ : Number of processors
  - T<sub>s</sub>: Serial execution time
  - $T_p$ : Parallel execution time
- It can be expressed as well vs. the parallel fraction  $P = 1 \alpha$

#### Amdahl Law - Fixed-size Model (1967)

Parallel Speedup vs. Serial Fraction



#### How real is this?

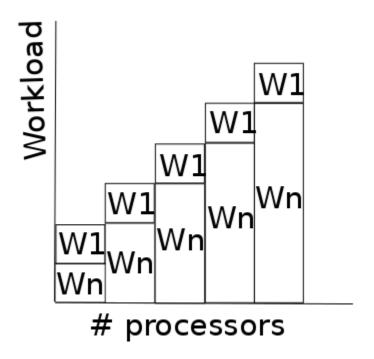
$$\lim_{p \to \infty} S_{Amdahl} = \lim_{p \to \infty} \frac{1}{\alpha + \frac{(1 - \alpha)}{p}} = \frac{1}{\alpha}$$

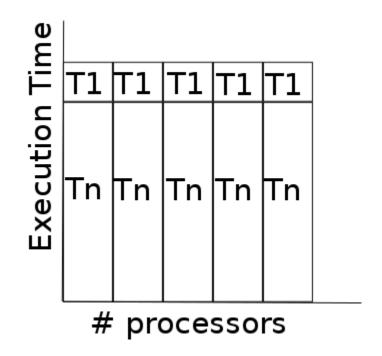
• If the sequential fraction is 20%, we have:

$$\lim_{p\to\infty} S_{Amdahl} = \frac{1}{0.2} = 5$$

Speedup 5 using infinite processors!

#### **Fixed-time model**





#### Gustafson Law—Fixed-time Model (1989)

 The execution time is fixed: it studies how the behavior of the <u>scaled</u> program varies when adding more computing power

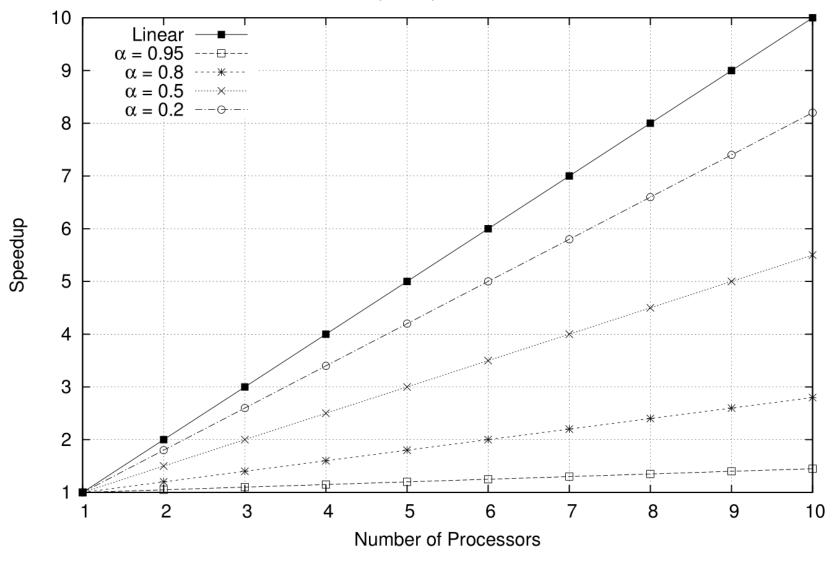
$$W' = \alpha W + (1 - \alpha)pW$$

$$S_{Gustafson} = \frac{W'}{W} = \alpha + (1 - \alpha)p$$

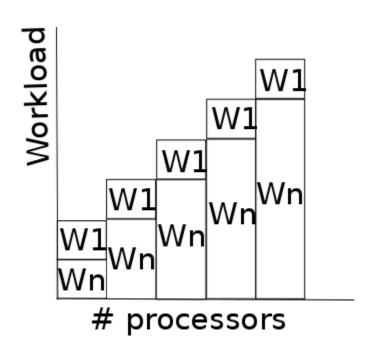
- where:
  - $\alpha \in [0,1]$ : Serial fraction of the program
  - $p \in N$ : Number of processors
  - W : Original workload
  - W': Scaled workload

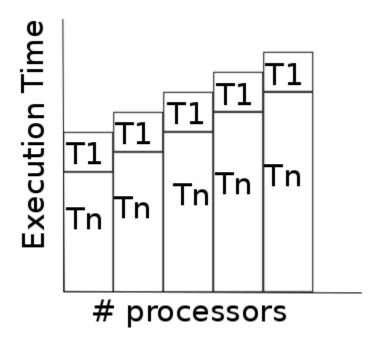
# Speed-up according to Gustafson

Parallel Speedup vs. Serial Fraction



#### Memory-bounded model





#### Sun Ni Law—Memory-bounded Model (1993)

The workload is scaled, bounded by memory

$$S_{Sun-Ni} = \frac{sequential\ time\ for\ W^*}{parallel\ time\ for\ W^*}$$

$$S_{Sun-Ni} = \frac{\alpha W + (1-\alpha)G(p)W}{\alpha W + (1-\alpha)G(p)\frac{W}{p}} = \frac{\alpha + (1-\alpha)G(p)}{\alpha + (1-\alpha)\frac{G(p)}{p}}$$

- where:
  - G(p) describes the workload increase as the memory capacity increases
  - $W^* = \alpha W + (1 \alpha)G(p)W$

# Speed-up according to Sun Ni

$$S_{Sun-Ni} = \frac{\alpha + (1-\alpha)G(p)}{\alpha + (1-\alpha)\frac{G(p)}{p}}$$

• If G(p) = 1

$$S_{Amdahl} = \frac{1}{\alpha + \frac{(1 - \alpha)}{p}}$$

• If G(p) = p

$$S_{Gustafson} = \alpha + (1 - \alpha)p$$

• In general, G(p) > p gives a higher scale-up

#### Superlinear speedup

- Can we have a Speed-up γ₁β₂!?
  - Workload increases more than computing power (G(p) > p)
  - Cache effect: larger accumulated cache size. More or even all of the working set can fit into caches and the memory access time reduces dramatically
  - RAM effect: enables the dataset to move from disk into RAM drastically reducing the time required, e.g., to search it.

# **Scalability**

Efficiency

$$E = \frac{speedup}{\#processors}$$

 Strong Scalability: If the efficiency is kept fixed while increasing the number of processes and maintain fixed the problem size

 Weak Scalability: If the efficiency is kept fixed while increasing at the same rate the problem size and the number of processes