DSC424Problem2HomeWork4RSyntaxfile

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#load the necessary packages

```
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
library(corrplot) # correlation visualization
## Warning: package 'corrplot' was built under R version 4.0.3
## corrplot 0.84 loaded
library(MASS) #for CV
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
library(caTools) # for splitting the data set into training and testing
## Warning: package 'caTools' was built under R version 4.0.3
#set the working directory
setwd("C:/Users/rejalu1/OneDrive - Henry Ford Health
System/DSC424/HomeWork4")
#Load the data set
heartds <- read.csv(file=".../HomeWork4/datasets/heart.csv", header=TRUE,
sep=",")
```

#the top 6 rows of this data set

```
head(heartds)
     age sex cp trestbps chol fbs restecg thalach exang oldpeak slope ca thal
##
## 1
      52
           1
              0
                      125
                           212
                                  0
                                          1
                                                168
                                                         0
                                                               1.0
                                                                        2
                                                                           2
                                                                                3
## 2
      53
           1
              0
                      140
                           203
                                  1
                                          0
                                                155
                                                         1
                                                               3.1
                                                                        0
                                                                           0
                                                                                3
                                                                        0 0
## 3
     70
           1
              0
                      145
                           174
                                  0
                                          1
                                                125
                                                         1
                                                               2.6
                                                                                3
                                                                        2 1
## 4
     61
           1
              0
                      148
                           203
                                  0
                                          1
                                                161
                                                         0
                                                               0.0
                                                                                3
                                                                        1 3
                                                                                2
## 5 62
           0 0
                      138
                           294
                                 1
                                          1
                                                         0
                                                               1.9
                                                106
## 6 58
                      100
                           248
                                          0
                                                                        1 0
                                                                                2
           0 0
                                  0
                                                122
                                                         0
                                                               1.0
##
     heartdisease
## 1
                 0
## 2
                 0
                 0
## 3
## 4
                 0
## 5
                 0
## 6
```

#structure of the ds

```
str(heartds)
## 'data.frame':
                 1025 obs. of 14 variables:
                      52 53 70 61 62 58 58 55 46 54 ...
   $ age
                : int
##
  $ sex
                : int
                      1111001111...
  $ cp
##
                : int
                      0000000000...
## $ trestbps
               : int 125 140 145 148 138 100 114 160 120 122 ...
               : int 212 203 174 203 294 248 318 289 249 286 ...
## $ chol
## $ fbs
                : int 0100100000...
## $ restecg
               : int 1011102000...
## $ thalach
               : int 168 155 125 161 106 122 140 145 144 116 ...
## $ exang
               : int
                      0 1 1 0 0 0 0 1 0 1 ...
## $ oldpeak
               : num 1 3.1 2.6 0 1.9 1 4.4 0.8 0.8 3.2 ...
                      2002110121...
## $ slope
                : int
## $ ca
                      2001303102...
                : int
## $ thal
                : int 3 3 3 3 2 2 1 3 3 2 ...
## $ heartdisease: int 0000010000...
```

#check if there are any missing values

```
sum(is.na(heartds))
## [1] 0
```

#Convert all the variables to numeric

```
heartdscleansed <- heartds %>%
  transmute(age = as.numeric(age)
   , sex = as.numeric(sex)
   , cp = as.numeric(cp)
   , trestbps = as.numeric(trestbps)
   , chol = as.numeric(chol)
   , fbs = as.numeric(fbs)
```

```
, restecg = as.numeric(restecg)
, thalach = as.numeric(thalach)
, exang = as.numeric(exang)
, oldpeak = oldpeak
, slope = as.numeric(slope)
, ca = as.numeric(ca)
, thal = as.numeric(thal)
, heartdisease = as.factor(heartdisease)
)
```

#structure of the heartdscleansed data set

```
str(heartdscleansed)
## 'data.frame':
                 1025 obs. of 14 variables:
                     52 53 70 61 62 58 58 55 46 54 ...
## $ age
               : num
               : num 1111001111...
## $ sex
## $ cp
               : num 0000000000...
## $ trestbps : num 125 140 145 148 138 100 114 160 120 122 ...
## $ chol
              : num 212 203 174 203 294 248 318 289 249 286 ...
               : num 0100100000...
## $ fbs
## $ restecg : num 1 0 1 1 1 0 2 0 0 0 ...
## $ thalach
               : num 168 155 125 161 106 122 140 145 144 116 ...
## $ exang
              : num 0110000101...
## $ oldpeak
               : num 1 3.1 2.6 0 1.9 1 4.4 0.8 0.8 3.2 ...
## $ slope
               : num 2002110121...
## $ ca
               : num
                     2001303102...
               : num 3 3 3 3 2 2 1 3 3 2 ...
## $ thal
## $ heartdisease: Factor w/ 2 levels "0","1": 1 1 1 1 1 2 1 1 1 1 ...
```

#determine how heartdisease is split

```
tabulate(heartds$heartdisease)
## [1] 526
```

#Run the correlation matrix and check for VIF

```
#m <- cor(heartdscleansedss)
#round(m, 2)
#m <- cor(heartdscleansedss, use='pairwise.complete.obs')
#round(m,2)
# M <- cor(heartdscleansedss)
# m <- corrplot(M, method="ellipse")
# m
# m <- corrplot(M, method="number")
# m
# model <- lm(heartdisease ~., data = heartds)
# VIF(model)</pre>
```

```
#Running LDA with cross-validation
```

#The depedent variable must be categorical

```
heartLDA <- lda(heartdisease ~., data = heartdscleansed)
#heartLDA</pre>
```

#plotting the model #we have to create a new without cross validation

```
#heartdiseaseLDA <- lda(heartdisease ~., data=heartdscleansed)
#heartdiseaseLDA
#plot(heartdiseaseLDA, xlab = "LDA1", ylab = "LDA2")</pre>
```

Try to predict the class from the original data

Note ... this is JUST a test to see how this works

In practice you will want to use cross-validation!

```
p <- predict(heartLDA, newdata=heartdscleansed[,1:13])$class</pre>
р
                        \begin{smallmatrix} 1 \end{smallmatrix} ] \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1cm} 1 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1c
1 1 1
                   0 0 0
                  [75] 0 1 1 0 1 1 1 0 1 1 1 1 1 1 1 0 0 1 1 0 0 1 1 1 0 1 1 1 1 1 1 1 0 0 0
101
0 1 1
0 1 0
1 1 1
## [260] 0 1 1 1 1 0 0 0 0 0 1 1 1 1 0 0 0 0 1 0 1 1 1 1 1 0 1 1 1 1 1 1 0 1
100
## [297] 0 0 1 1 1 1 1 0 1 0 1 1 1 1 1 0 0 0 1 1 1 1 1 0 0 1 1 1 0 0 0 1 1 0 0 0 1
1 0 1
## [334] 1 0 0 1 1 1 0 1 1 1 1 1 0 0 1 0 1 0 0 0 0 1 1 0 0 1 1 1 0 1 1 1 1 0
## [371] 0 0 1 1 1 0 1 0 0 1 0 0 0 0 0 1 1 0 0 1 1 1 1 0 0 1 0 0 0 1 0 1 1 1
0 1 1
```

```
## [408] 0 1 1 1 0 0 0 1 1 1 1 1 1 1 1 1 1 0 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1
0 0 1
100
## [482] 0 0 1 1 0 1 0 1 1 1 1 0 0 1 0 0 1 1 1 1 1 1 1 1 0 1 0 0 1 0 1 0 1
0 0 1
0 1 0
## [556] 0 0 1 1 0 1 1 1 1 0 1 1 1 1 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 0 0 1 0 0 0
0 1 0
## [593] 0 0 0 0 1 1 1 1 1 1 0 1 1 1 1 1 0 0 0 0 0 0 0 0 1 1 1 1 1 1 0 0 0 1 0 0
0 1 1
1 1 1
## [667] 1 1 1 0 1 0 1 1 0 0 0 0 1 0 1 0 0 0 1 0 1 0 1 1 1 0 1 0 0 1 1 1 0 0
0 0 0
## [741] 1 1 0 0 1 1 1 0 1 0 1 1 1 1 1 1 1 0 0 1 1 0 1 1 1 0 0 0 0 1 1 1 1 1 1 0
1 1 0
## [778] 0 1 1 0 0 0 1 1 0 0 0 0 0 0 0 0 1 1 1 1 0 1 1 1 1 1 0 0 1 1 1 0
100
1 0 1
000
## [889] 0 0 0 1 0 1 0 1 0 1 1 0 1 1 0 1 1 0 1 1 0 0 1 1 0 0 0 0 0 0 1 1 1 0 0
1 1 1
## [926] 0 0 1 0 0 0 1 1 1 1 1 1 1 0 1 0 1 1 1 0 1 1 1 0 0 0 1 1 1 1 0 1 1 1
1 1 1
## [963] 0 0 1 1 0 1 0 1 1 1 1 1 1 0 0 1 1 0 1 0 1 0 0 0 0 1 0 1 1 0 1 0 0 0
000
## Levels: 0 1
```

#Compare the results of the prediction

```
t <- table(p, heartdscleansed$heartdisease)
t

##
## p 0 1
## 0 376 41
## 1 123 485</pre>
```

#determine the accuracy

```
acc <- mean(p==heartdscleansed$heartdisease)
acc
## [1] 0.84</pre>
```

#you're going to do a set seed, because every set seed will give you a different randomization #So if you want to have the same exact. #If you want to know exactly where you got that randomization from, you want to set the seed to the same number

```
set.seed(123)
```

#put in sample split the original data set in this case we're going to do a 7030 split #so 70% is going into training #and 30% is going into testing.

```
sample <- sample.split(heartdscleansed, SplitRatio = 0.70)#Splits the data in
the ratio mentioned in the SplitRatio
train <- subset(heartdscleansed, sample==TRUE)
test <- subset(heartdscleansed, sample==FALSE)</pre>
```

#The depedent variable must be categorial (Assuming No Cross-Validation)

```
heartLDA <- lda(heartdisease ~., data = train)
heartLDA
## Call:
## lda(heartdisease ~ ., data = train)
## Prior probabilities of groups:
         0
## 0.508346 0.491654
##
## Group means:
##
                               cp trestbps
                                               chol
                                                          fhs
         age
                                                                restecg
                    sex
thalach
## 0 56.45373 0.8179104 0.5104478 133.3373 252.4657 0.1701493 0.4537313
138.7045
## 1 52.27778 0.5370370 1.4444444 129.6265 241.7068 0.1450617 0.5956790
158.5679
                oldpeak
                            slope
        exang
                                         ca
                                                thal
## 0 0.5611940 1.6435821 1.146269 1.1671642 2.543284
## 1 0.1450617 0.5496914 1.629630 0.3364198 2.104938
##
## Coefficients of linear discriminants:
                     LD1
## age
            -0.006501605
## sex
            -0.855971953
            0.373364594
## cp
## trestbps -0.001604870
## chol -0.002299697
```

```
## fbs 0.076949989
## restecg
            0.154638530
## thalach
            0.010245005
## exang
           -0.606056064
## oldpeak -0.196089733
## slope
            0.510724746
           -0.428958496
## ca
## thal
           -0.456359144
#plot(heartLDA)
#Ls(heartLDA)
```

#we can predict on the training

```
p <- predict(heartLDA, newdata = heartdscleansed[,1:13])$class</pre>
р
                  \begin{smallmatrix} 1 \end{smallmatrix} ] \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1cm} 1 \hspace{.1cm} 1 \hspace{.1cm} 1 \hspace{.1cm} 0 \hspace{.1cm} 1 \hspace{.1c
##
1 1 1
##
              [38] 1 0 0 1 1 1 0 1 1 1 0 1 0 1 0 1 0 0 0 1 1 1 1 1 1 0 1 1 1 1 0 1 0 0
0 0 0
             [75] 0 1 1 0 1 1 1 0 1 1 1 1 1 1 0 0 1 1 0 0 1 1 1 0 1 1 1 1 1 1 1 0 0 0
##
1 0 1
0 1 1
0 1 1
0 1 0
## [223] 1 1 1 1 0 1 1 0 0 1 0 1 1 1 0 1 0 1 1 1 1 1 1 1 1 1 0 1 1 0 1 0 0 0 1
1 1 0
## [260] 0 1 1 1 1 0 0 0 0 0 1 1 1 1 0 1 0 0 1 0 1 1 1 1 1 0 1 1 1 1 1 0 0 0
100
## [297] 0 0 1 1 1 1 1 0 1 0 1 1 1 1 1 0 0 0 1 1 1 1 1 0 1 1 1 1 0 0 1 1 1 0 0 1
1 0 1
## [334] 1 0 0 1 0 0 0 1 1 1 1 1 1 0 0 1 0 0 0 0 0 1 1 1 0 0 1 1 1 1 1 1 0
0 0 1
## [371] 0 0 1 0 1 1 1 0 0 1 0 0 0 0 0 1 1 0 0 1 1 1 1 0 0 1 0 0 1 1 0 1 1 1
## [408] 0 1 1 1 0 0 0 1 1 0 0 0 1 1 1 1 1 1 0 0 1 1 0 1 1 0 1 1 1 1 1 1 0 1 0 1
0 0 1
100
## [482] 0 0 1 1 0 1 0 1 0 1 1 0 0 1 0 0 1 1 1 1 1 1 1 1 1 0 1 0 0 1 0 1 0 1
0 0 1
0 1 0
## [556] 0 0 1 1 0 1 1 1 1 0 1 1 1 1 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 0 0 1 0 0 0
0 1 0
0 0 1
```

```
1 1 1
## [667] 1 1 1 0 1 0 1 1 0 0 0 0 1 0 1 0 0 0 1 0 1 0 0 1 0 1 0 1 0 1 0 0 1 0 0 1
1 0 1
0 0 0
## [741] 1 1 0 0 1 1 1 0 1 0 1 1 1 1 1 1 1 1 0 1 1 1 1 0 0 0 0 0 1 1 1 1 1 0
1 1 0
100
## [815] 1 0 1 1 1 0 0 0 0 1 0 1 1 0 1 0 1 0 0 0 1 1 1 1 0 1 0 1 0 1 0
100
0 0 0
## [889] 0 0 0 1 0 1 0 0 0 1 1 0 0 1 0 1 1 0 1 1 0 0 1 1 0 0 0 0 0 1 1 0 0 0
## [926] 0 0 1 0 0 0 1 1 0 1 1 1 1 0 1 0 1 1 1 0 1 1 1 0 0 0 0 1 1 1 0 1 1 1
1 1 1
## [963] 0 0 1 1 0 1 0 1 1 1 1 1 1 0 0 1 1 0 1 0 1 0 0 0 0 1 0 1 1 0 1 0 0 0
000
## Levels: 0 1
```

#we can use the table to get the same confusion matrix

```
t1 <- table(p, heartdscleansed$heartdisease)
t1

##
## p 0 1
## 0 401 49
## 1 98 477</pre>
```

#calculate the accuracy by using the mean

```
acc1 <- mean(p==heartdscleansed$heartdisease)
acc1
## [1] 0.8565854</pre>
```

#We can also do as we said before the Cross validation come up with the table, #and if we use coefficients remember if we do Ls. # Setting "CV = T" will have the lda function perform # "Leave-one-out" cross-validation

```
## [75] 0 1 1 0 1 1 1 0 1 1 1 1 1 1 0 0 1 1 0 0 1 1 1 1 1 1 1 1 0 0 0
1 0 1
0 1 1
0 1 1
0 1 0
## [223] 1 1 1 1 0 1 1 0 0 1 0 1 1 1 0 1 0 1 1 1 1 1 1 1 1 1 0 1 1 0 1 0 0 0 1
1 1 1
## [260] 0 1 1 1 1 0 0 0 0 0 1 1 1 1 0 0 0 0 1 0 1 1 1 1 1 0 1 1 1 1 1 1 0 0
100
1 0 1
## [334] 1 0 0 1 1 1 0 1 1 1 1 1 0 0 1 0 1 0 0 0 0 1 1 0 0 1 1 1 0 1 1 1 1 0
## [371] 0 0 1 1 1 0 1 0 0 1 0 0 0 0 0 1 1 0 0 1 1 1 1 0 0 1 0 0 0 1 0 1 1 1
0 1 1
## [408] 0 1 1 1 0 0 0 1 1 1 1 1 1 1 1 1 1 1 0 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1
0 0 1
100
## [482] 0 0 1 1 0 1 0 1 0 1 1 0 0 1 0 0 1 1 1 1 1 1 1 1 1 0 1 0 0 1 0 1 0 1
0 1 0
## [556] 0 0 1 1 0 1 1 1 1 0 1 1 1 1 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 0 0 1 0 0 0
0 1 0
0 1 1
## [667] 1 1 1 0 1 0 1 1 1 0 0 0 0 1 0 1 0 0 0 1 0 1 0 1 0 1 0 1 0 1 0 0 1 1 0 0
101
0 0 0
## [741] 1 1 0 0 1 1 1 0 1 0 1 1 1 0 1 1 0 0 1 1 0 1 1 0 0 0 0 1 1 1 1 1 1 0
1 1 0
## [778] 0 1 1 0 0 0 1 1 0 0 0 0 0 0 0 0 1 1 1 1 0 1 1 1 1 1 0 0 1 1 1 0
100
1 0 1
000
## [889] 0 0 0 1 0 1 0 1 0 1 1 0 1 1 0 1 1 0 1 1 0 0 1 1 0 0 0 0 0 0 1 1 1 0 0
1 1 1
## [926] 0 0 1 0 0 0 1 1 1 1 1 1 1 0 1 0 1 1 1 0 0 0 1 1 1 1 0 0 0 1 1 1 1
## [963] 0 0 1 1 0 1 0 1 1 1 1 1 1 0 0 1 1 0 1 0 1 0 0 0 0 1 0 1 1 0 1 0 0 0
000
```

```
## Levels: 0 1
##
## $posterior
##
                  0
                               1
## 1
        0.767608548 0.2323914521
## 2
        0.981677756 0.0183222441
## 3
        0.986367250 0.0136327504
## 4
        0.616250115 0.3837498846
## 5
        0.918466648 0.0815333518
## 6
        0.251656048 0.7483439524
## 7
        0.974792687 0.0252073126
## 8
        0.980252913 0.0197470874
## 9
        0.607370801 0.3926291988
## 10
        0.993671030 0.0063289698
## 11
        0.222754578 0.7772454220
## 12
        0.905451979 0.0945480210
## 13
        0.006597333 0.9934026675
## 14
        0.999185014 0.0008149864
## 15
        0.217150645 0.7828493546
## 16
        0.006597333 0.9934026675
## 17
        0.093848688 0.9061513118
## 18
        0.992083114 0.0079168859
## 19
        0.023115111 0.9768848890
## 20
        0.050017267 0.9499827326
## 21
        0.336276742 0.6637232580
## 22
        0.225861676 0.7741383241
## 23
        0.884010942 0.1159890579
## 24
        0.009117245 0.9908827549
## 25
        0.006133200 0.9938667997
## 26
        0.793932563 0.2060674366
## 27
        0.080120249 0.9198797509
## 28
        0.164587517 0.8354124827
## 29
        0.368723635 0.6312763652
## 30
        0.886773991 0.1132260088
## 31
        0.782648686 0.2173513137
        0.023115111 0.9768848890
## 32
## 33
        0.968479141 0.0315208589
## 34
        0.974220731 0.0257792685
## 35
        0.027867276 0.9721327245
## 36
        0.400501761 0.5994982389
## 37
        0.390364797 0.6096352031
## 38
        0.223109894 0.7768901056
        0.978840223 0.0211597767
## 39
## 40
        0.460641091 0.5393589085
## 41
        0.049034060 0.9509659399
## 42
        0.296769131 0.7032308691
## 43
        0.065517555 0.9344824452
## 44
        0.607370801 0.3926291988
## 45
        0.040134255 0.9598657454
```

```
## 46
        0.133843716 0.8661562836
## 47
        0.101218565 0.8987814355
## 48
        0.909796444 0.0902035563
## 49
        0.077114795 0.9228852049
## 50
        0.941783465 0.0582165351
## 51
        0.009708566 0.9902914341
## 52
        0.677749448 0.3222505521
## 53
        0.344096257 0.6559037435
## 54
        0.851796776 0.1482032238
## 55
        0.997693244 0.0023067557
## 56
        0.997693244 0.0023067557
## 57
        0.167630558 0.8323694423
## 58
        0.147893241 0.8521067586
## 59
        0.413600088 0.5863999120
## 60
        0.278650711 0.7213492885
## 61
        0.032737956 0.9672620442
## 62
        0.077114795 0.9228852049
## 63
        0.971867702 0.0281322984
        0.105723767 0.8942762334
## 64
## 65
        0.032737956 0.9672620442
        0.202917203 0.7970827974
## 66
## 67
        0.268659678 0.7313403222
        0.797080181 0.2029198190
## 68
## 69
        0.003381987 0.9966180130
## 70
        0.996184027 0.0038159730
## 71
        0.996055392 0.0039446075
## 72
        0.969334291 0.0306657090
        0.921913239 0.0780867612
## 73
## 74
        0.802740885 0.1972591149
## 75
        0.944659298 0.0553407024
  76
        0.063803953 0.9361960465
##
## 77
        0.104182533 0.8958174668
## 78
        0.994118557 0.0058814432
## 79
        0.231805303 0.7681946974
## 80
        0.231805303 0.7681946974
## 81
        0.349310811 0.6506891893
## 82
        0.505213604 0.4947863962
## 83
        0.400501761 0.5994982389
## 84
        0.344096257 0.6559037435
        0.003381987 0.9966180130
## 85
## 86
        0.051656160 0.9483438397
## 87
        0.050017267 0.9499827326
## 88
        0.436694899 0.5633051013
        0.897398392 0.1026016083
## 89
## 90
        0.982955930 0.0170440702
## 91
        0.006516781 0.9934832195
## 92
        0.034714706 0.9652852936
## 93
        0.994118557 0.0058814432
## 94
        0.782648686 0.2173513137
## 95
        0.174443466 0.8255565337
```

```
## 96
        0.345734319 0.6542656814
## 97
        0.152677469 0.8473225308
## 98
        0.996048452 0.0039515481
## 99
        0.428650137 0.5713498631
## 100
        0.054219308 0.9457806923
## 101
        0.008690240 0.9913097601
## 102
        0.139888333 0.8601116674
## 103
        0.208002709 0.7919972908
## 104
        0.063803953 0.9361960465
## 105
        0.005115040 0.9948849602
## 106
        0.942196452 0.0578035482
## 107
        0.821896702 0.1781032984
## 108
        0.926136363 0.0738636371
## 109
        0.283356555 0.7166434454
## 110
        0.912147251 0.0878527488
## 111
        0.214761953 0.7852380469
## 112
        0.921849227 0.0781507727
## 113
        0.944659298 0.0553407024
## 114
        0.984378360 0.0156216396
## 115
        0.217532269 0.7824677307
## 116
        0.793932563 0.2060674366
## 117
        0.922202522 0.0777974777
## 118
        0.967561344 0.0324386558
## 119
        0.032737956 0.9672620442
## 120
        0.079090984 0.9209090163
## 121
        0.208002709 0.7919972908
## 122
        0.782648686 0.2173513137
## 123
        0.996273866 0.0037261341
## 124
        0.081683915 0.9183160848
## 125
        0.988257112 0.0117428875
## 126
        0.004665957 0.9953340429
## 127
        0.567041118 0.4329588816
## 128
        0.268659678 0.7313403222
## 129
        0.446167396 0.5538326040
## 130
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## 962
        0.251656048 0.7483439524
## 963
        0.877021434 0.1229785661
## 964
        0.677749448 0.3222505521
## 965
        0.005208393 0.9947916067
## 966
       0.054219308 0.9457806923
## 967
        0.996347869 0.0036521305
## 968
        0.021601735 0.9783982650
## 969
        0.981677756 0.0183222441
## 970
       0.086442558 0.9135574419
## 971
        0.344096257 0.6559037435
## 972
       0.162065330 0.8379346700
## 973
        0.005115040 0.9948849602
## 974
        0.216054370 0.7839456297
## 975
       0.268191461 0.7318085387
## 976
       0.683585493 0.3164145071
## 977
        0.681513786 0.3184862142
## 978
        0.042633465 0.9573665347
## 979
        0.214761953 0.7852380469
## 980
       0.991267664 0.0087323365
## 981
        0.229973106 0.7700268938
        0.683585493 0.3164145071
## 982
## 983
        0.225861676 0.7741383241
## 984
       0.978840223 0.0211597767
## 985
        0.633395305 0.3666046948
## 986
        0.886487839 0.1135121613
## 987
        0.886773991 0.1132260088
## 988
        0.278650711 0.7213492885
## 989
        0.946564124 0.0534358758
## 990
        0.193692580 0.8063074196
## 991
        0.076488428 0.9235115724
## 992
        0.941783465 0.0582165351
## 993
        0.045420369 0.9545796310
## 994
        0.994732495 0.0052675054
## 995
      0.963836109 0.0361638911
```

```
## 996 0.134440101 0.8655598987
## 997 0.969453585 0.0305464149
## 998 0.917133740 0.0828662604
## 999 0.797080181 0.2029198190
## 1000 0.860231859 0.1397681408
## 1001 0.888916630 0.1110833704
## 1002 0.133843716 0.8661562836
## 1003 0.798418405 0.2015815953
## 1004 0.877021434 0.1229785661
## 1005 0.093848688 0.9061513118
## 1006 0.827248769 0.1727512309
## 1007 0.050017267 0.9499827326
## 1008 0.167630558 0.8323694423
## 1009 0.079090984 0.9209090163
## 1010 0.283356555 0.7166434454
## 1011 0.821896702 0.1781032984
## 1012 0.111769660 0.8882303397
## 1013 0.425161802 0.5748381983
## 1014 0.974792687 0.0252073126
## 1015 0.005208393 0.9947916067
## 1016 0.997024705 0.0029752955
## 1017 0.148792530 0.8512074701
## 1018 0.996048452 0.0039515481
## 1019 0.305358038 0.6946419620
## 1020 0.192878819 0.8071211808
## 1021 0.255066274 0.7449337256
## 1022 0.988182586 0.0118174135
## 1023 0.942196452 0.0578035482
## 1024 0.045420369 0.9545796310
## 1025 0.917133740 0.0828662604
##
## $terms
## heartdisease ~ age + sex + cp + trestbps + chol + fbs + restecg +
       thalach + exang + oldpeak + slope + ca + thal
## attr(,"variables")
## list(heartdisease, age, sex, cp, trestbps, chol, fbs, restecg,
##
       thalach, exang, oldpeak, slope, ca, thal)
## attr(,"factors")
                age sex cp trestbps chol fbs restecg thalach exang oldpeak
##
slope
## heartdisease
                         0
                                        0
                                                                   0
                                                                           0
## age
                  1
                      0
                         0
                                        0
                                                                           0
0
## sex
                      1
                  0
                         0
                                   0
                                        0
                                            0
                                                    0
                                                             0
                                                                   0
                                                                           0
0
## cp
                  0
                      0
                         1
                                   0
                                        0
                                            0
                                                    0
                                                             0
                                                                   0
                                                                           0
## trestbps
                  0
                      0
                                   1
                                        0
                                            0
                                                    0
                                                             0
                                                                   0
                                                                           0
```

```
## chol
                       0
                          0
                                        1
                                            0
                                                     0
                                                                    0
                                                                            0
0
## fbs
                   0
                       0
                          0
                                                     0
                                                             0
                                                                            0
                                   0
                                        0
                                             1
                                                                    0
0
                       0
                          0
                                   0
                                        0
                                             0
                                                             0
                                                                    0
                                                                            0
## restecg
                  0
                                                     1
0
## thalach
                  0
                       0
                          0
                                   0
                                        0
                                             0
                                                     0
                                                             1
                                                                    0
                                                                            0
## exang
                   0
                       0
                          0
                                   0
                                        0
                                                     0
                                                             0
                                                                    1
                                                                            0
0
                  0
                       0
                          0
                                   0
                                        0
                                                     0
                                                             0
                                                                            1
## oldpeak
                                             0
                                                                    0
                       0
## slope
                  0
                          0
                                   0
                                        0
                                             0
                                                     0
                                                             0
                                                                    0
                                                                            0
1
## ca
                   0
                       0
                                   0
                                        0
                                             0
                                                     0
                                                             0
                                                                    0
                                                                            0
## thal
                  0
                       0
                          0
                                   0
                                        0
                                            0
                                                     0
                                                             0
                                                                    0
                                                                            0
0
##
                ca thal
## heartdisease
                 0
                 0
                       0
## age
                 0
                       0
## sex
                 0
                       0
## cp
## trestbps
                 0
                       0
                 0
## chol
## fbs
                 0
                       0
                 0
                       0
## restecg
                 0
## thalach
                       0
                 0
                       0
## exang
                 0
                       0
## oldpeak
## slope
                 0
                       0
                 1
## ca
                       0
## thal
## attr(,"term.labels")
## [1] "age"
                   "sex"
                               "cp"
                                           "trestbps" "chol"
                                                                  "fbs"
                                          "oldpeak" "slope"
## [7] "restecg" "thalach" "exang"
                                                                  "ca"
## [13] "thal"
## attr(,"order")
## [1] 1 1 1 1 1 1 1 1 1 1 1 1 1
## attr(,"intercept")
## [1] 1
## attr(,"response")
## [1] 1
## attr(,".Environment")
## <environment: R_GlobalEnv>
## attr(,"predvars")
## list(heartdisease, age, sex, cp, trestbps, chol, fbs, restecg,
       thalach, exang, oldpeak, slope, ca, thal)
## attr(,"dataClasses")
## heartdisease age sex
                                                      cp trestbps
```

```
chol
##
       "factor"
                     "numeric"
                                   "numeric"
                                                  "numeric"
                                                                "numeric"
"numeric"
             fbs
                                     thalach
                                                                  oldpeak
##
                       restecg
                                                      exang
slope
##
      "numeric"
                     "numeric"
                                   "numeric"
                                                  "numeric"
                                                                "numeric"
"numeric"
##
              ca
                          thal
      "numeric"
                     "numeric"
##
##
## $call
## lda(formula = heartdisease \sim ., data = heartdscleansed, CV = T)
##
## $xlevels
## named list()
#use the table() to get a confusion matrix by using the class
```

```
t2 <- table(heartLDA2$class, heartdscleansed$heartdisease)
t2

##
## 0 1
## 0 373 50
## 1 126 476
```

#calculate the accuracy by hand

```
accuracy <- (373 + 476)/(373 + 476 + 126 + 50)
accuracy
## [1] 0.8282927
```

#Coming up with the different performance metrics #build a model with a train()

```
library(caret)
## Warning: package 'caret' was built under R version 4.0.3
## Loading required package: lattice
## Loading required package: ggplot2
## Warning: package 'ggplot2' was built under R version 4.0.3
heartModelFit <- train(heartdisease ~., method = "lda",
preProcess=c("scale", "center"), data=train)</pre>
```

#And then predict this data on the training data and come up with a confusion matrix.

```
p <- predict(heartModelFit, train)
cm <- confusionMatrix(train$heartdisease, p, dnn=c("Actual Group", "Predicted")</pre>
```

```
Group"))
\mathsf{cm}
## Confusion Matrix and Statistics
##
               Predicted Group
## Actual Group 0 1
##
              0 272 63
##
              1 26 298
##
##
                  Accuracy : 0.8649
##
                    95% CI: (0.8365, 0.8901)
##
       No Information Rate : 0.5478
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa : 0.7303
##
##
   Mcnemar's Test P-Value: 0.0001356
##
               Sensitivity: 0.9128
##
##
               Specificity: 0.8255
##
            Pos Pred Value: 0.8119
            Neg Pred Value : 0.9198
##
##
                Prevalence: 0.4522
##
            Detection Rate: 0.4127
##
      Detection Prevalence: 0.5083
##
         Balanced Accuracy: 0.8691
##
##
          'Positive' Class : 0
##
```